

# Bispectral Analysis of the L-H transition as seen in the NSTX GPI data

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# ***Outline***

- Introduction
- Background and motivation
- Application of bispectral analysis to NSTX GPI data
- Summary/Conclusions
- Future Work

# ***Bispectral Analysis***

## **Bispectrum**

$$B(f_1, f_2) = \langle \Phi(f_1)\Phi(f_2)\Phi^*(f_3) \rangle$$

$$f_1 + f_2 = f_3$$

## **Squared Bicoherence**

$$b^2(f_1, f_2) = \frac{|B(f_1, f_2)|^2}{\langle |\Phi(f_1)\Phi(f_2)|^2 \rangle \langle |\Phi(f_3)|^2 \rangle}$$

$$0 \leq b^2(f_1, f_2) \leq 1$$

The bicoherence is a measure of phase coherence between three Fourier modes in the system

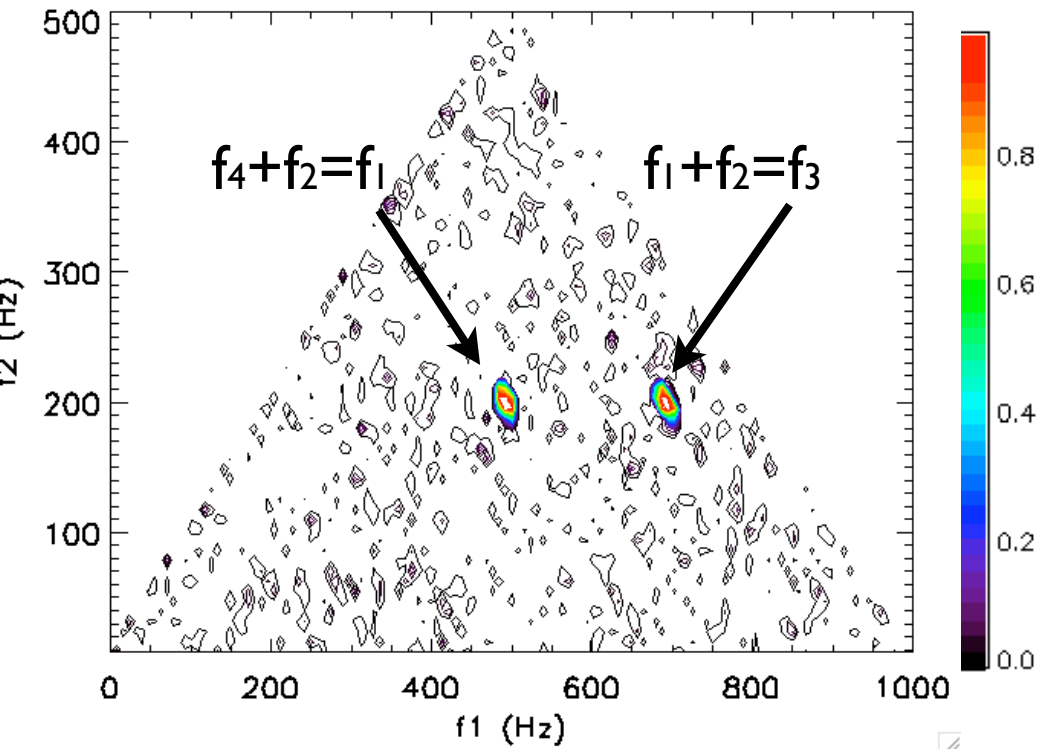
# Interpretation of bicoherence figures

$$g(t) = \sin(f_1 + \phi_1) + \sin(f_2 + \phi_2) + \sin(f_3 + \phi_3) + \sin(f_4 + \phi_4)$$

$$f_1 + f_2 = f_3 \quad f_1 - f_2 = f_4 \quad \phi_{1,2} = \text{random}[-\pi, \pi]$$

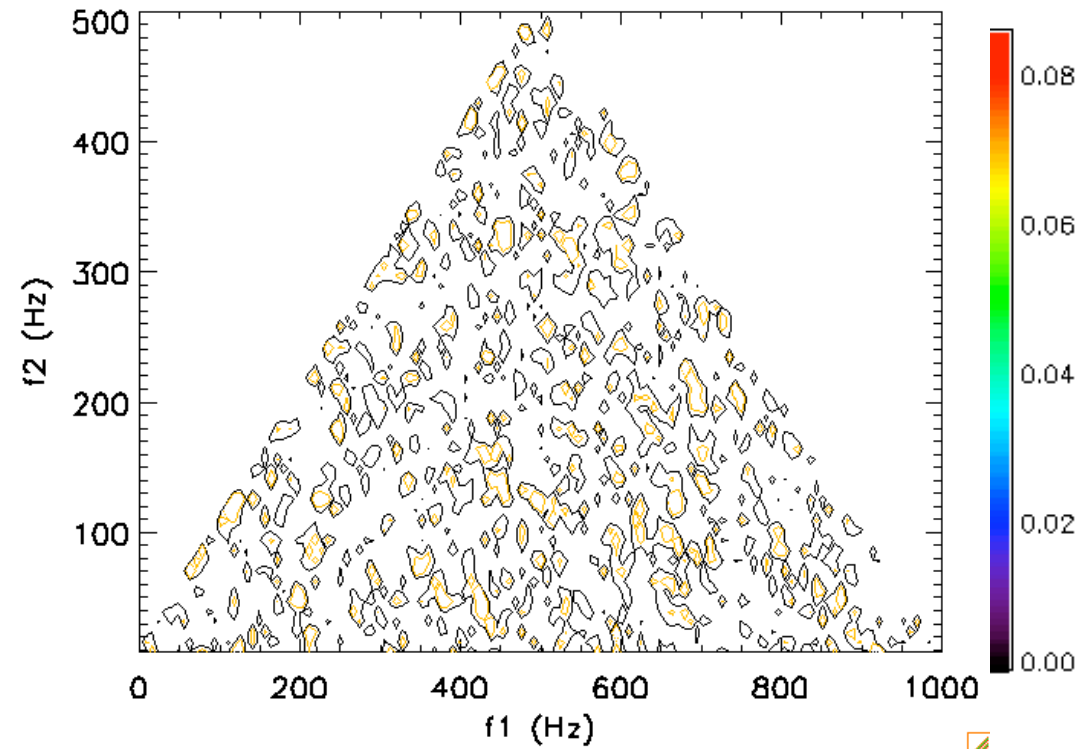
**Coupled**

$$\begin{aligned} \phi_1 + \phi_2 &= \phi_3 \\ \phi_1 - \phi_2 &= \phi_4 \end{aligned}$$



**Uncoupled**

$$\begin{aligned} \phi_3 &= \text{random}[-\pi, \pi] \\ \phi_4 &= \text{random}[-\pi, \pi] \end{aligned}$$



# Interpretation of bicoherence figures

**Summed bicoherence** gives a measure of the strength of the coupling at the sum frequency  $f_3$  with respect to all other frequencies

$$b^2(f_3) = \sum_{f_1 + f_2 = f_3} b_{f_3}^2(f_1, f_2)$$

**Total bicoherence** gives a measure of the relative strength of coupling summed over all frequencies

$$b^2 = \sum_{f_1} \sum_{f_2} b_{f_3}^2(f_1, f_2)$$

# Background and Motivation

It was reported in 2001 that the nonlinear coupling between small scale high-frequency turbulence and larger scale low-frequency fluctuations increases prior to an L-H transition in DIII-D .

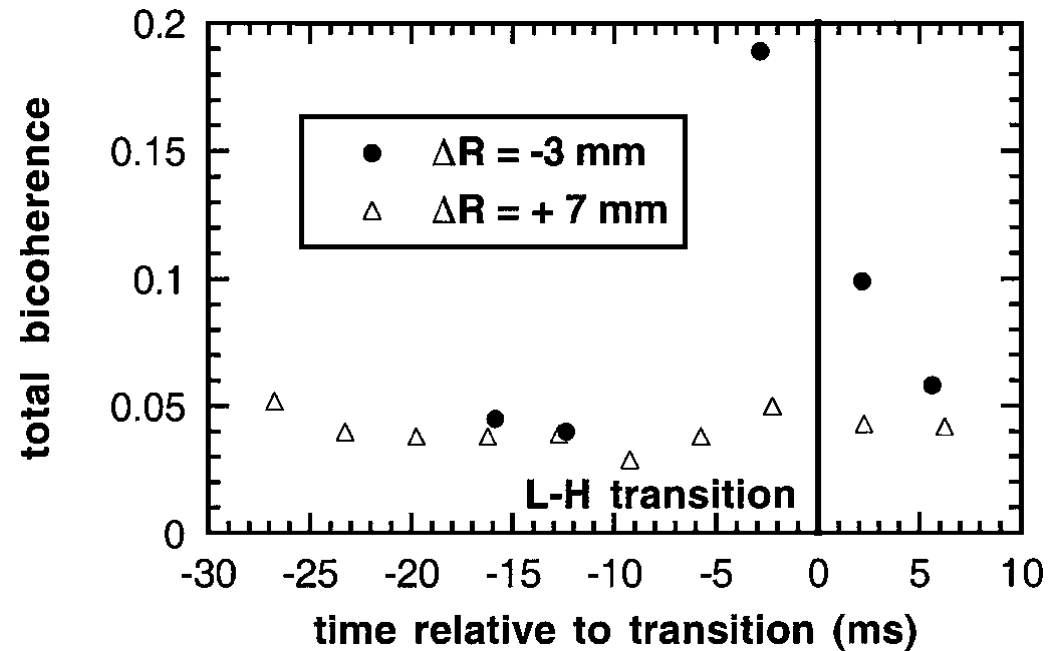
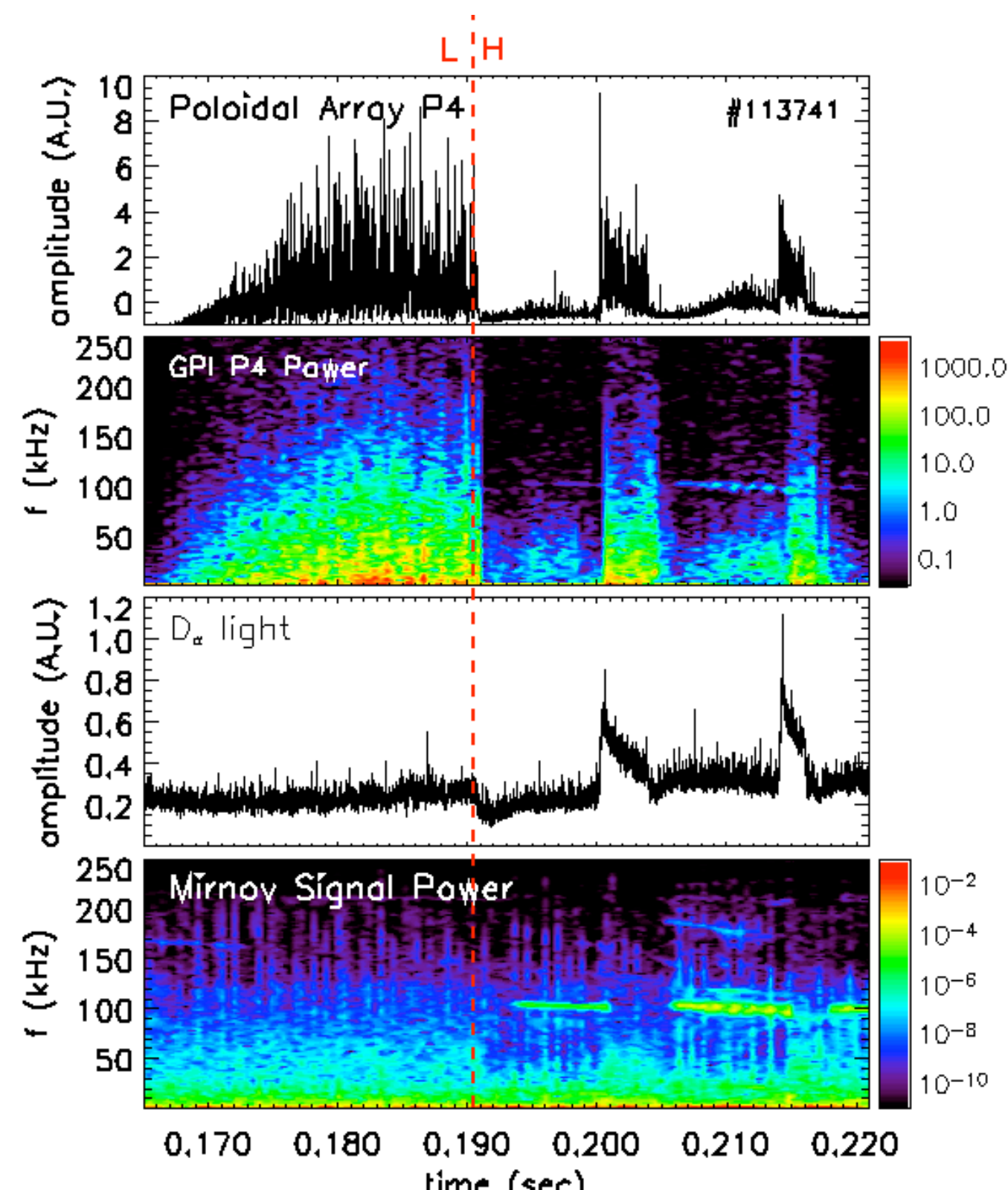


FIG. 4. Evolution of the total bicoherence of  $I_{\text{sat}}$  3 mm inside (●) and 7 mm outside ( $\Delta$ ) the separatrix.

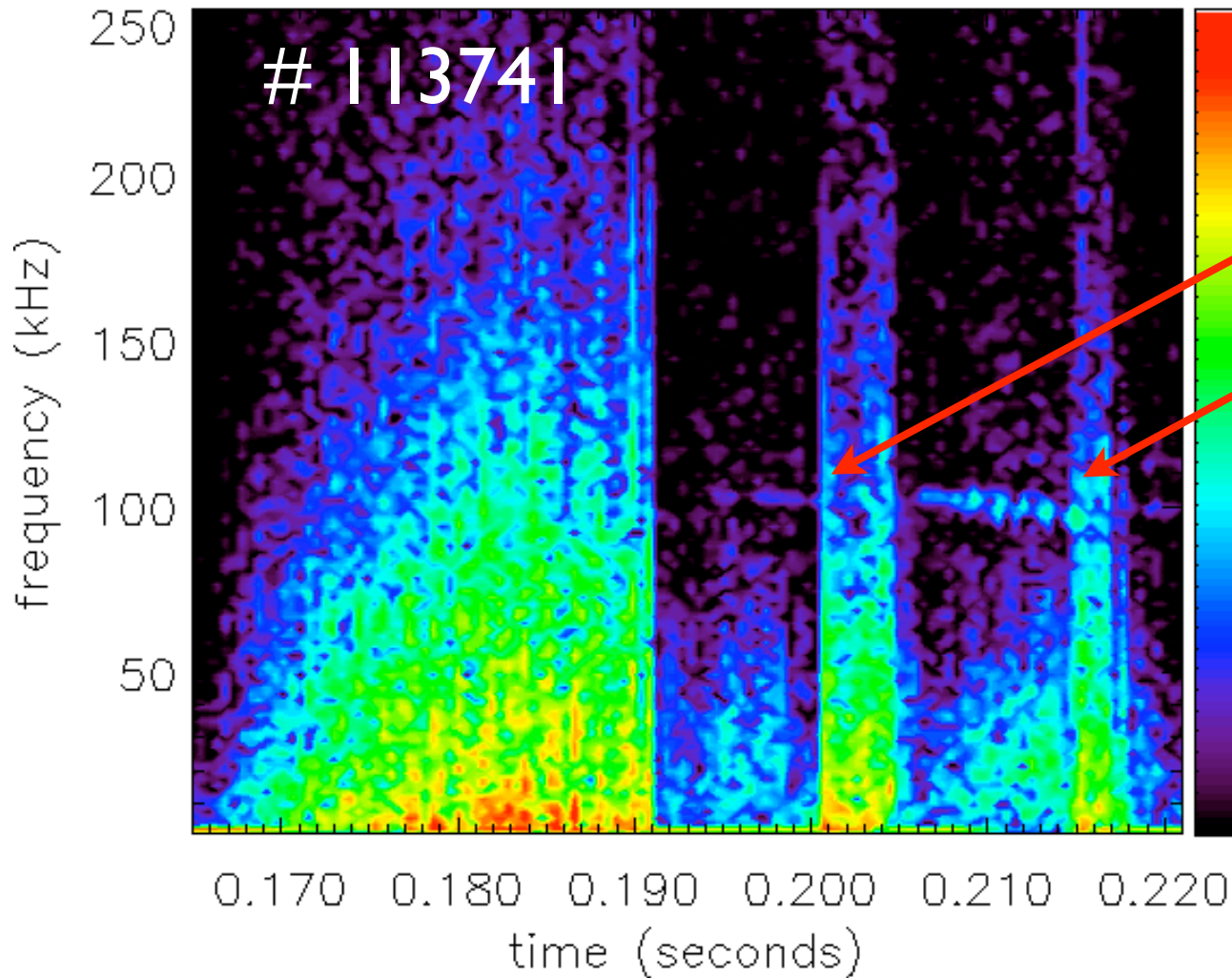
Figure and caption taken from:  
*Increased Nonlinear Coupling between Turbulence and Low-Frequency Fluctuations at the L-H Transition*  
R. A. Moyer, G. R. Tynan, C. Holland, and M. J. Burin  
Phys. Rev. Lett. 87, 135001 (2001)

## ***GPI Chord Data***

Light amplitude signals from the GPI  
1-D chords show decreased fluctuation amplitude after the L-H transition



# Power Spectrum from GPI chord signal

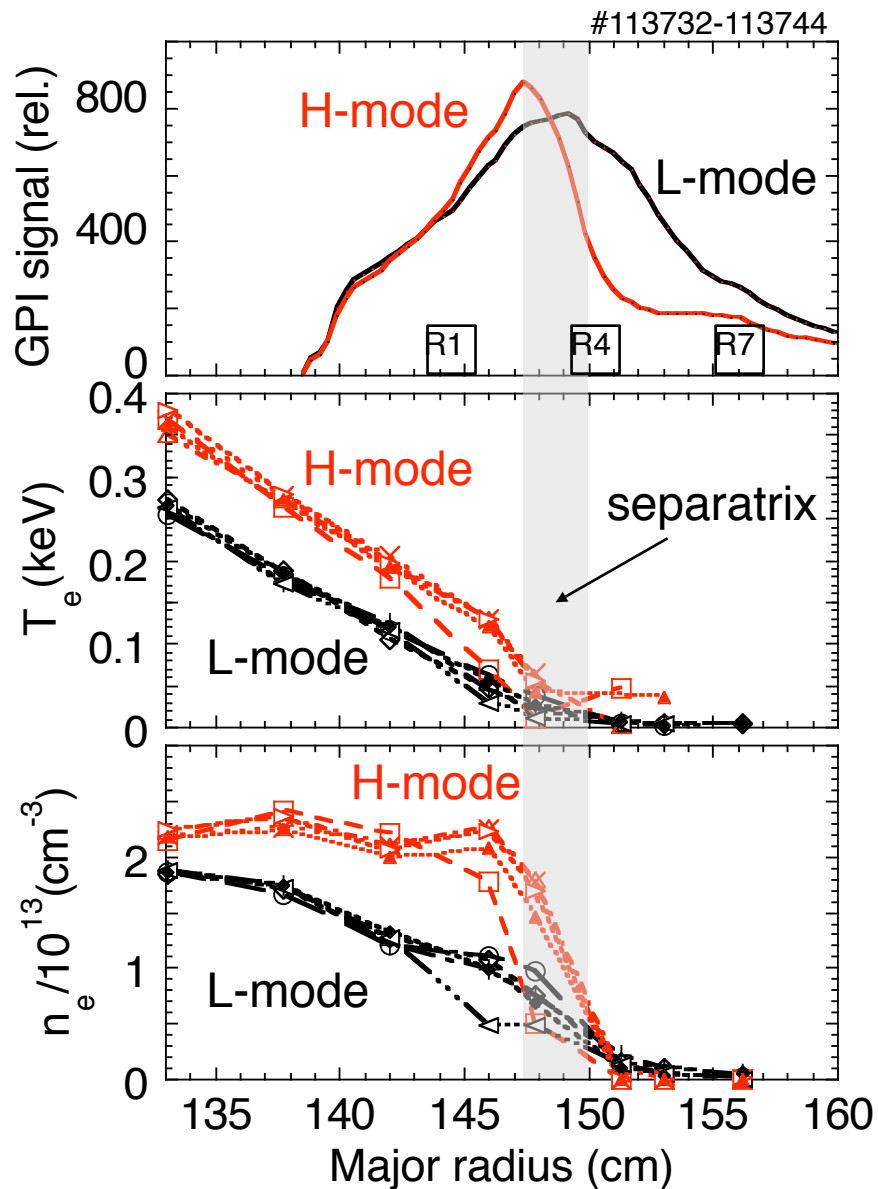


A mode at  
~100 kHz  
appears  
during the  
H-mode

There are  
no long-  
lived modes  
during the  
L-mode or  
during  
Ohmic  
shots



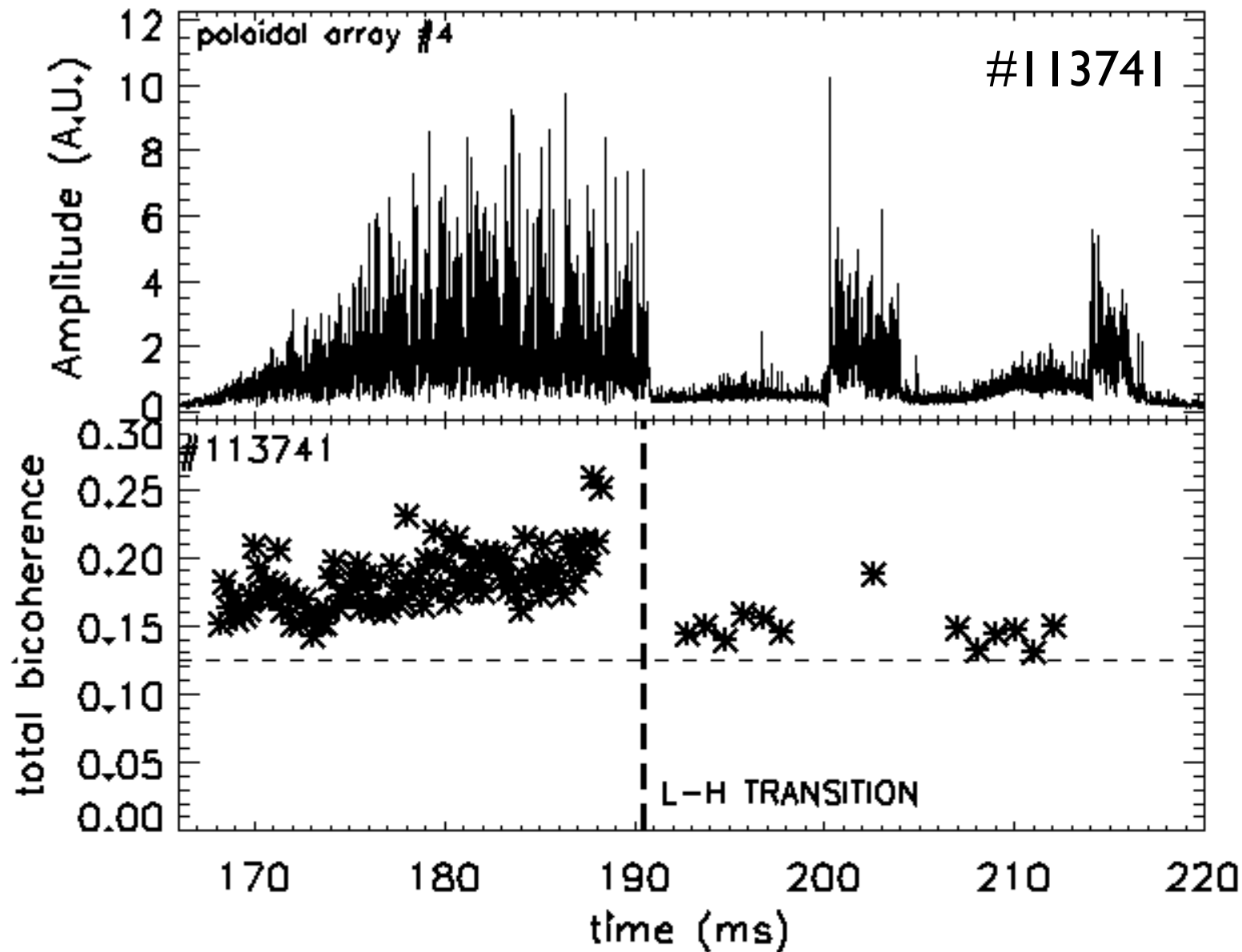
# Viewing region of GPI chord data with respect to the separatrix may affect bicoherence results



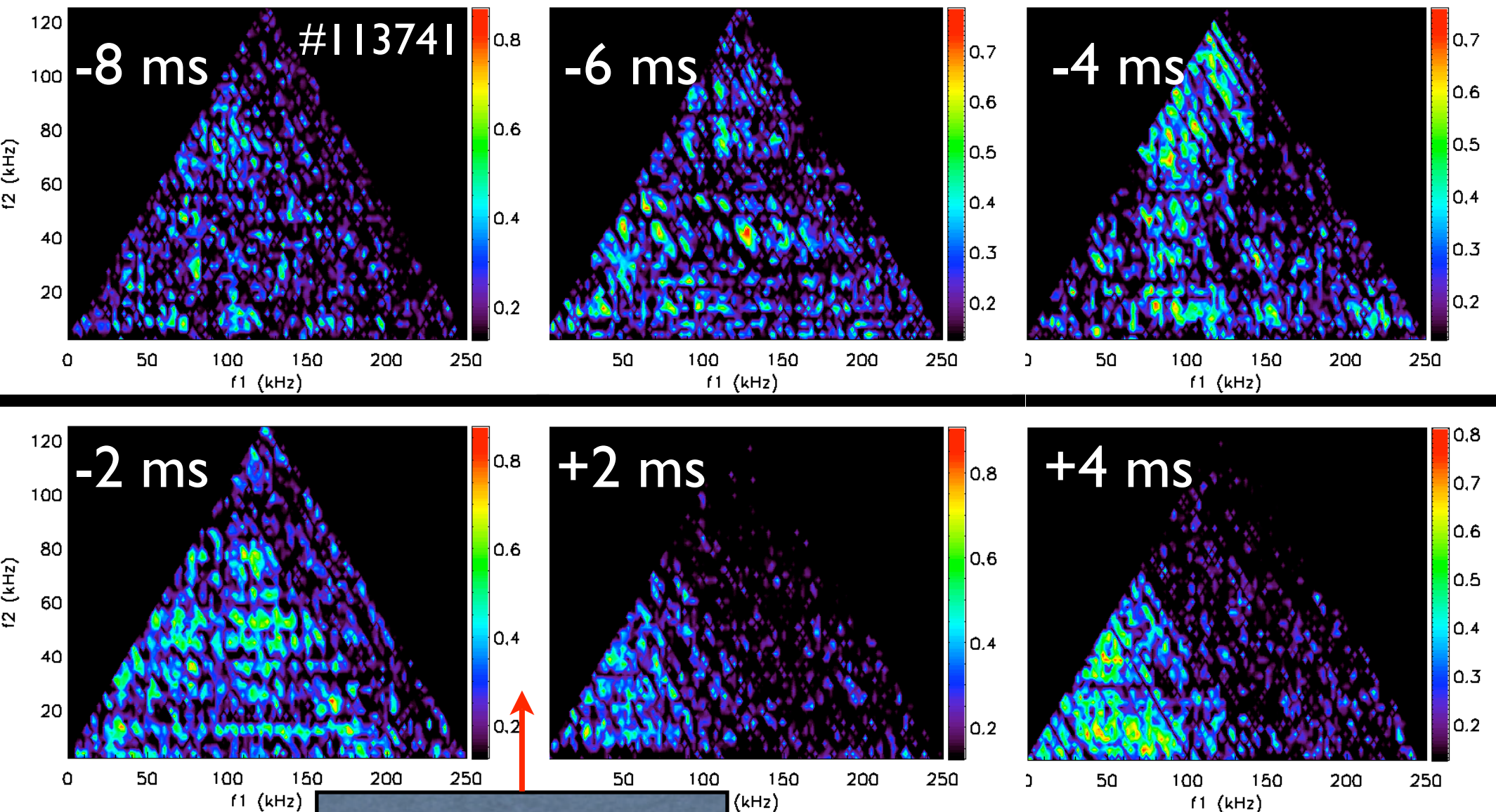
The GPI poloidal detector array on NSTX was located near the separatrix for the shots analysed

The DIID study saw an increase in bicoherence just inside the separatrix

Total bicoherence of the GPI signal tends to decrease following the L-H transition

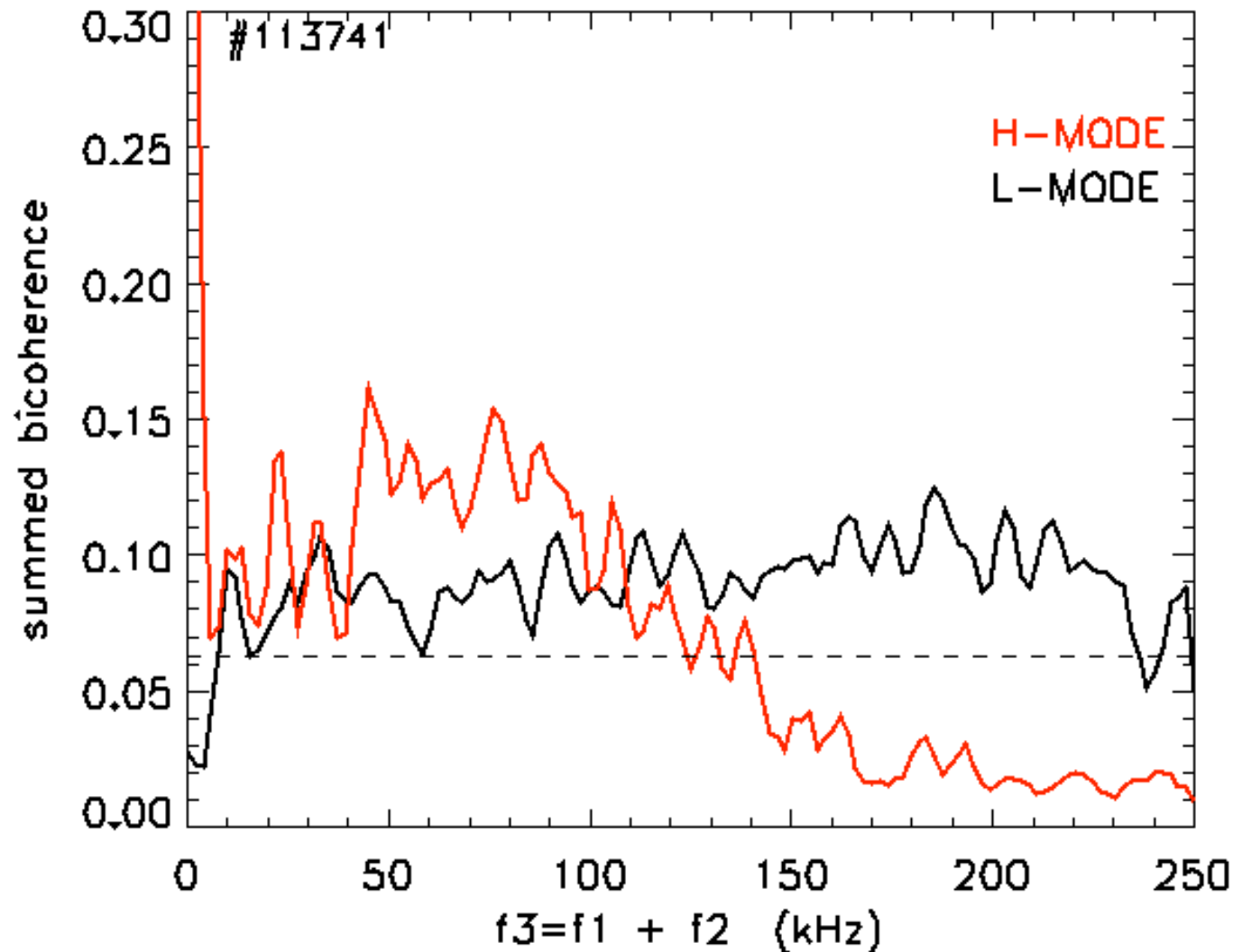


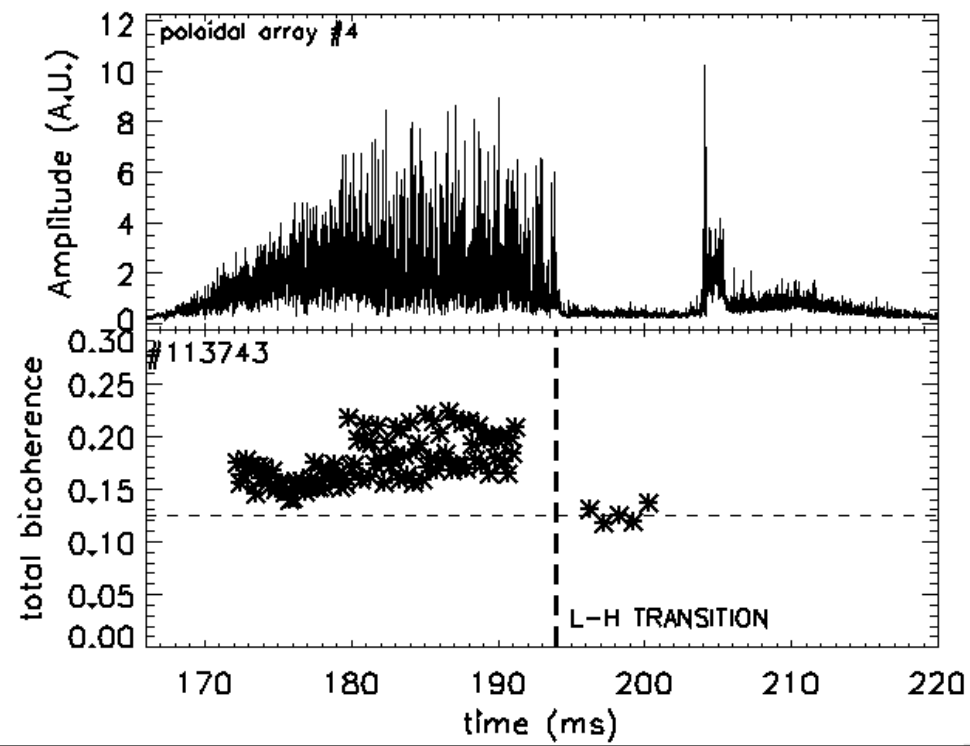
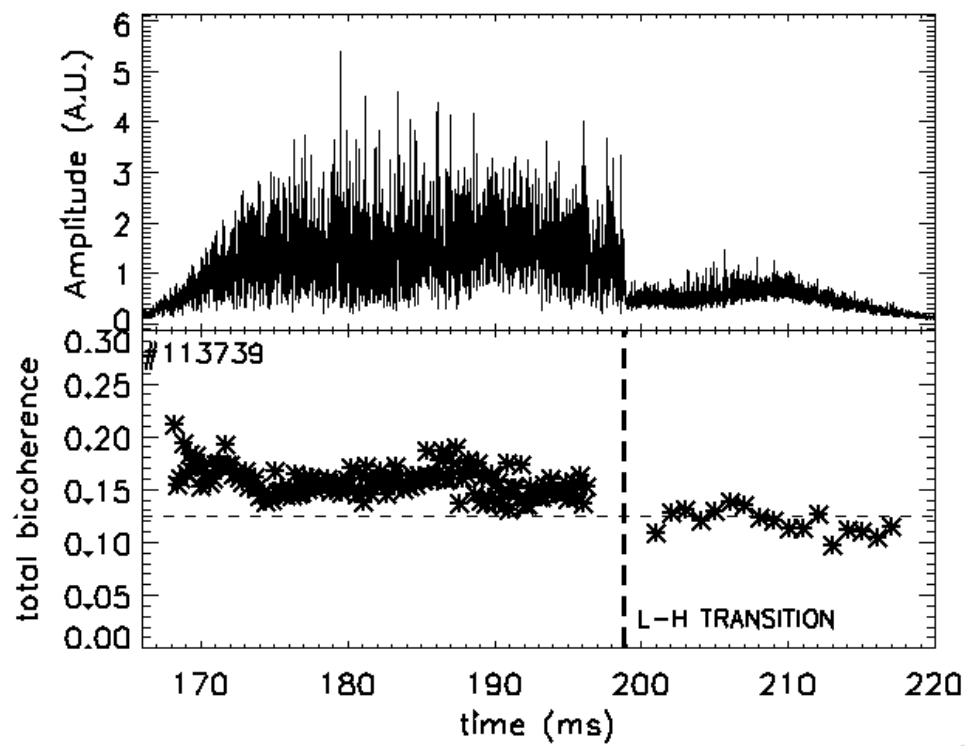
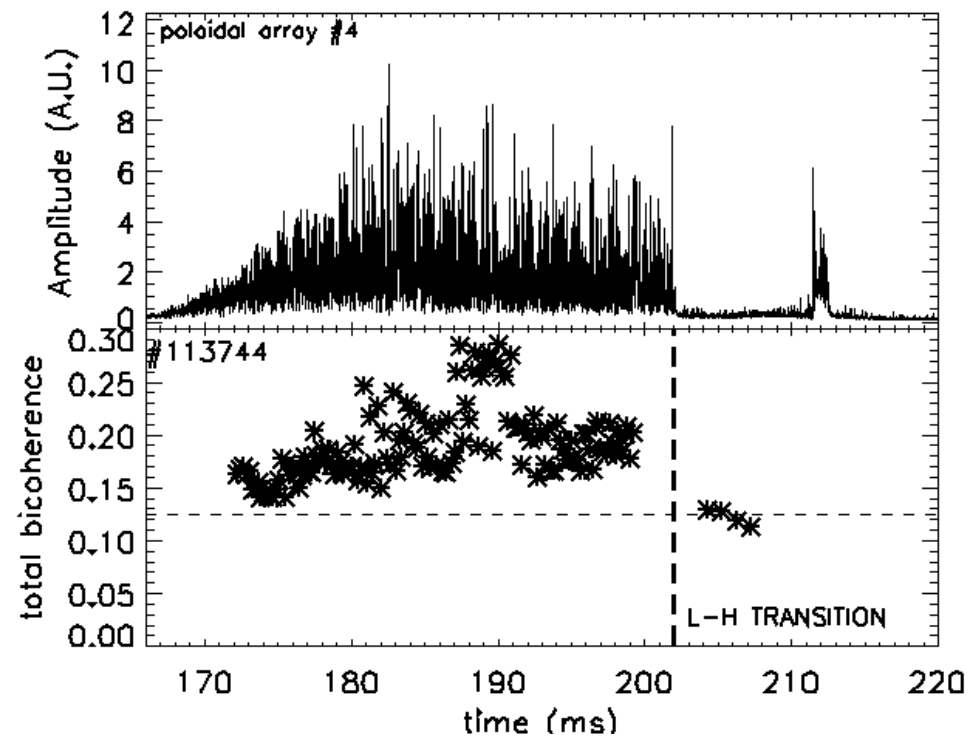
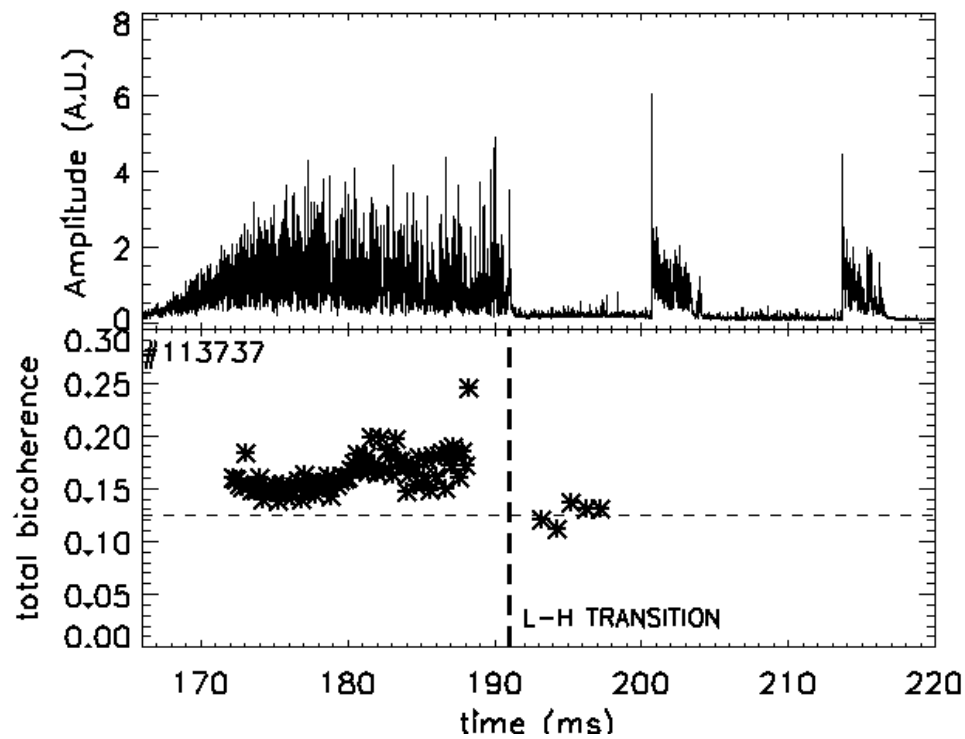
Total bicoherence decreases following the L-H transition and the coupling is localized to low sum frequencies



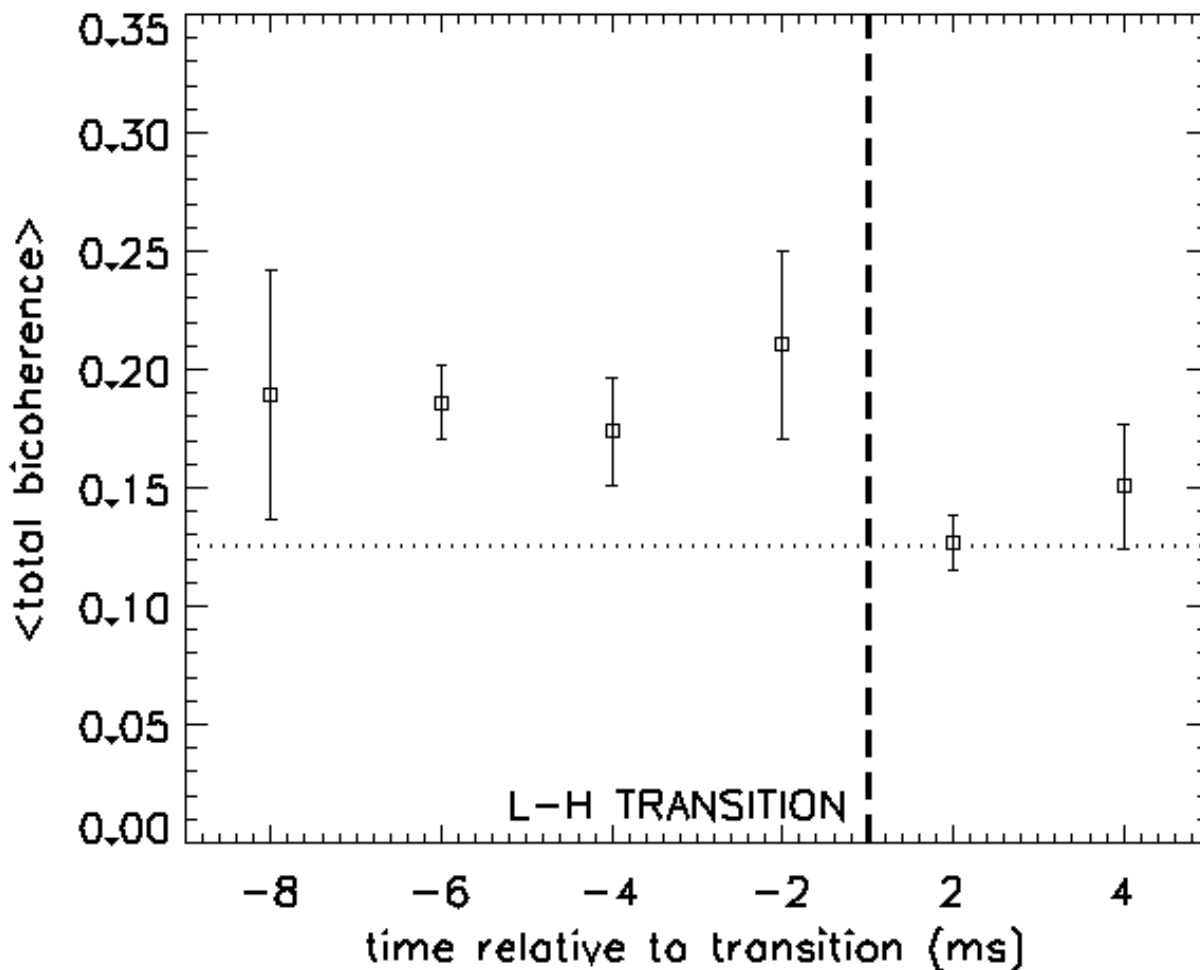
**L-H TRANSITION**

The summed auto-bicoherence indicates that coupling shifts to low sum frequencies following the L-H transition





The total bicoherence averaged over 5 shots with an L-H transition shows a typical trend found in NSTX data



113737  
113739  
113741  
113743  
113744

# ***Summary of NSTX results and Conclusions***

- The total bicoherence decreases going from L-mode to H-mode
- During H-mode, coupling occurs mostly at low sum frequencies ( $f_3 < 100$  kHz), implying either sum coupling of large scales with other larger scales or difference coupling between small and large scales
- All L-H transition NSTX shots indicate there is no significant increase in the amount of coupling prior to the L-H transition

# ***Future Work***

- Calculate radial profile of the bicoherence
- Increase the digitization rate of the GPI 1-D detector data
- Compare bicoherence evolution with 2-D camera images.
- Apply wavelet analysis to compute the bicoherence of GPI data and compare to FFT method