



## A Synthetic Diagnostic for Studying Electron Scale Turbulence at NSTX and NSTX-U

J. Ruiz Ruiz<sup>1</sup>

Y. Ren<sup>2</sup>, W. Guttenfelder<sup>2</sup>, A. E. White<sup>1</sup>, N. F. Loureiro<sup>1</sup>, S.M. Kaye<sup>2</sup>, B. P. LeBlanc<sup>2</sup>, E. Mazzucato<sup>2</sup>, K.C. Lee<sup>3</sup>, C.W. Domier<sup>4</sup>, D. R. Smith<sup>5</sup>, H. Yuh<sup>6</sup> 1. MIT 2. PPPL 3. NFRI 4. UC Davis 5. U Wisconsin 6. Nova Photonics, Inc.

> NSTX-U Science Meeting Dec 5, 2016







# Outline

- Motivation
- Old high-k scattering system at NSTX
- The GYRO code
- Previous Work on synthetic high-k
- New Synthetic Diagnostic for the high-k scattering system
  - 1. Coordinate mapping (this talk)
  - 2. Filtering (ongoing work)
- Results from Coordinate Mapping
  - 1. Old high-k system
  - 2. New high-k system

### Understanding Electron Thermal Transport is a Main Thrust in the NSTX and NSTX-U Research Program

- NSTX H-mode plasmas that are driven by neutral beams exhibit ion thermal transport close to neoclassical (collisional) levels, due to *suppression of ion scale turbulence by ExB shear* [*cf. Kaye NF 2007*].
- Electron thermal transport is always anomalous ( >> neoclassical).
- <u>Goal</u>: Study electron thermal transport caused by electron-scale turbulence in NSTX and NSTX-U.



# Outline

- Motivation
- Old high-k scattering system at NSTX
- The GYRO code
- Previous Work on synthetic high-k
- New Synthetic Diagnostic for the high-k scattering system
  - 1. Coordinate mapping (this talk)
  - 2. Filtering (ongoing work)
- Results from Coordinate Mapping
  - 1. Old high-k system
  - 2. New high-k system

# Old High-k Microwave Scattering Diagnostic System at NSTX



Measurement of density fluctuations

Scattered power density

$$\overline{P_s} \propto \left(\frac{\delta n}{n}\right)^2$$

Three wave-coupling

$$\vec{k}_s = \vec{k} + \vec{k}_i \qquad \omega_s = \omega + \omega$$

#### **Details of diagnostic**

- Gaussian Probe beam: 15 mW, 280 GHz,  $\lambda_i \sim 1.07$  mm, a = 3 cm (1/e<sup>2</sup> radius).
- Propagation close to midplane  $=> k_r$  spectrum.
- 5 detection channels => range  $k_R \sim 5-30 \text{ cm}^{-1}$  (high-k).
- Wavenumber resolution  $\Delta k = \pm 0.7 \text{ cm}^{-1}$ .
- Radial coverage: R = 106-144 cm.
- Radial resolution:  $\Delta R = \pm 2 \text{ cm}$  (unique feature).



# High-k Scattering Allows the Study of Frequency and Wavenumber Spectrum of Electron Scale Turbulence



- Frequency analysis of scattered power  $\rightarrow$  frequency spectrum.
- Different channels  $\rightarrow$  different k  $\rightarrow$  wavenumber spectrum of turbulence

# Outline

- Motivation
- Old high-k scattering system at NSTX
- The GYRO code
- Previous Work on synthetic high-k
- New Synthetic Diagnostic for the high-k scattering system
  - 1. Coordinate mapping (this talk)
  - 2. Filtering (ongoing work)
- Results from Coordinate Mapping
  - 1. Old high-k system
  - 2. New high-k system

#### The GYRO code Numerically solves the Gyrokinetic-Maxwell System

- Turbulence and transport in tokamaks is studied with gyrokinetics.
- The gyrokinetic-Maxwwell system cannot be solved analytically except in simple limits
   → needs to be solved numerically (GYRO)
- Inputs: experimental plasma parameters plasma shape, equilibrium geometry, profiles, ...
- Outputs: moments and fields
  - Moments of the distribution function *h<sub>s</sub>*
  - Perturbed electromagnetic field components
- Turbulent fluxes (particle  $\Gamma_s$ , heat  $Q_s$ , ... ) can be reconstructed from outputs, and compared with experimental values.



#### Examples of GYRO output from an NSTX H-mode plasma



# A Quantitative Comparison between Experiment and GYRO is not Possible due to Different k-definitions



 $k_{\perp} = (k_{R}, k_{Z})$  (cylindrical coordinates)

 $k = (k_r, k_{\theta})$  (internal GYRO definitions – field aligned coordinate system)

• 
$$k_{\theta} = nq/r$$

### Principles of the Synthetic Diagnostic

- Goal: A quantitative comparison between experiment and simulation of electron scale turbulence (e.g. frequency and k-spectrum below).
- Need to map experiment and simulation into a common coordinate system
- I have done: Written a series of Matlab routines that perform the geometric mapping between the experimental frame and simulation frame.



# Outline

- Motivation
- Old high-k scattering system at NSTX
- The GYRO code
- Previous Work on synthetic high-k
- New Synthetic Diagnostic for the high-k scattering system
  - 1. Coordinate mapping (this talk)
  - 2. Filtering (ongoing work)
- Results from Coordinate Mapping
  - 1. Old high-k system
  - 2. New high-k system

- Previous synthetic high-k scattering was implemented with GTS (*cf.* Poli PoP 2010).
- Synthetic spectra was affected by 'systematic errors' (simulation run time, low k<sub>θ</sub> detected, scattering localization)
- No quantitative agreement was obtained between experimental and simulated frequency spectra.



# Outline

- Motivation
- Old high-k scattering system at NSTX
- The GYRO code
- Previous Work on synthetic high-k
- New Synthetic Diagnostic for the high-k scattering system
  - 1. Coordinate mapping (this talk)
  - 2. Filtering (ongoing work)
- Results from Coordinate Mapping
  - 1. Old high-k system
  - 2. New high-k system

#### Preliminary Steps Prior to the Implementation a Synthetic High-k Scattering Diagnostic using GYRO

#### Preliminary Steps:

- 1. High-k scattering diagnostic  $\rightarrow$  experimental density fluctuation spectra  $|\delta n_e|^2_{kR,kZ}(\omega)$
- 2. Ray tracing code:
  - Scattering location + resolution
  - Turbulence wavenumber + resolution

 $(\mathsf{R}_{\mathsf{loc}}, \mathsf{Z}_{\mathsf{loc}}) + (\Delta \mathsf{R}_{\mathsf{loc}}, \Delta \mathsf{Z}_{\mathsf{loc}}) \\ (\mathsf{k}_{\mathsf{R}}^{\mathsf{exp}}, \mathsf{k}_{\mathsf{Z}}^{\mathsf{exp}}) + (\Delta \mathsf{k}_{\mathsf{R}}^{\mathsf{exp}}, \Delta \mathsf{k}_{\mathsf{Z}}^{\mathsf{exp}})$ 

3. Run a nonlinear gyrokinetic simulation (used GYRO here) capturing scattering location + resolving the experimentally measured wavenumber.

#### Summary Steps of the Synthetic High-k Scattering Diagnostic using GYRO

#### Steps in synthetic diagnostic implementation

 Coordinate Mapping (done): Coordinate mapping GYRO (r, θ, φ) Wavenumber mapping (k<sub>r</sub>ρ<sub>s</sub>,k<sub>θ</sub>ρ<sub>s</sub>)<sub>GYRO</sub>



- **2. Filtering:** Apply instrumental selectivity function to simulated density fluctuations from GYRO. Preliminary only (ongoing work)
- **3. Quantitative comparison** between experiment and simulation (future work).



# Outline

- Motivation
- Old high-k scattering system at NSTX
- The GYRO code
- Previous Work on synthetic high-k
- New Synthetic Diagnostic for the high-k scattering system
  - 1. Coordinate mapping (this talk)
  - 2. Filtering (ongoing work)

#### Results from Coordinate Mapping

- 1. Old high-k system
- 2. New high-k system

# **Results of mapping**

#### Experiment (shot 141767, ch1)

#### <u>GYRO</u>

 $k_R = -18.57 \text{ cm}^{-1}$  →  $k_r \rho_s = -2.68$  $k_Z = 4.93 \text{ cm}^{-1}$  →  $k_\theta \rho_s = 4.99$ 

 $\rho_s^{GYRO}$  = 0.2 cm

Next step is to run a GYRO simulation that resolves the experimental wavenumbers and the high-k ETG spectrum.



# Mapped ( $k_R$ , $k_Z$ )<sup>exp</sup> to GYRO ( $k_r \rho_s$ , $k_\theta \rho_s$ )<sub>GYRO</sub> in Standard electron Scale Simulation



- Blue dots: (k<sub>r</sub>ρ<sub>s</sub>, k<sub>θ</sub>ρ<sub>s</sub>)<sup>exp</sup> of channels
   1, 2, 3 of high-k system.
- Ellipses are e<sup>-1</sup> and e<sup>-2</sup> amplitude of (k<sub>r</sub>, k<sub>θ</sub>) gaussian filter (simplified selectivity function)

$$F(k_r, k_{\theta}) = F_r(k_r) F_{\theta}(k_r)$$
  

$$F_r(k_r) = \exp\left(-(k_r - k_r^{\exp})^2 / \Delta k_r^2\right)$$
  

$$F_{\theta}(k_{\theta}) = \exp\left(-(k_{\theta} - k_{\theta}^{\exp})^2 / \Delta k_{\theta}^2\right)$$

Numerical grid of standard e- scale simulation does NOT accurately resolve the experimental wavenumber.

## Numerical Resolution Details of the Scale Simulations Presented

#### Experimental profiles used as input

Local, flux-tube simulations performed at scattering location (r/a~0.7, R~136 cm).

- Only electron scale turbulence included.
- 3 kinetic species, D, C, e (Z<sub>eff</sub>~1.85-1.95)
- Electromagnetic:  $A_{\parallel}+B_{\parallel}$ ,  $\beta_e \sim 0.3$  %.
- Collisions ( $v_{ei} \sim 1 c_s/a$ ).
- ExB shear ( $\gamma_E \sim 0.13 c_s/a$ ) + parallel flow shear ( $\gamma_p \sim 1 c_s/a$ )
- Fixed boundary conditions with  $\Delta^{b} \sim 1.5 \rho_{s}$  buffer widths.

#### Standard e- scale resolution parameters

- $L_r \times L_y = 6 \times 4 \rho_s$ .
- n<sub>r</sub> x n = 192 x 48.
- $k_{\theta}\rho_{s}$  [min, max] = [1.5, 74]
- $k_r \rho_s$  [min, max] = [1, 50]
- $[n_{\parallel}, n_{\lambda}, n_{e}] = [14, 12, 12]$

#### **<u>Big-box e- scale</u>** resolution parameters

- $L_r \times L_y = 21 \times 21 \rho_s$ .
- $n_r x n = 512 x 142$ .
- $k_{\theta}\rho_{s}[min, max] = [0.3, 43]$
- k<sub>r</sub>ρ<sub>s</sub> [min, max] = [0.3, 38]
- $[n_{\parallel}, n_{\lambda}, n_{e}] = [14, 12, 12]$
- Big-box e- scale runs presented here are NOT multiscale:
- lons are not resolved correctly  $\Delta k_{\theta} \rho_s \sim 0.3$ ,  $L_r \propto L_y = 21 \times 21 \rho_s$ .
- Simulation ran only for electron time scales ( $\sim 20a/c_s$ ), ions are not fully developed.



Big-box simulation spectra show well resolved (k<sub>R</sub>,k<sub>Z</sub>)<sup>exp</sup> and electron scale spectrum.

### A Big-Simulation-Domain Electron Scale Simulation Was Performed to Apply New Synthetic Diagnostic

- Outboard mid-plane δn<sub>e</sub>(R, Z) in a bigsimulation domain e- scale GYRO simulation of real NSTX plasma discharge.
- Shot 141767, time t = 398 ms (*cf.* Ruiz Ruiz PoP 2015).
- Dots are scattering location for channels
   1, 2, and 3 of high-k diagnostic.
- Dashed circles are e<sup>-1</sup> and e<sup>-2</sup> amplitude of microwave beam.
- Scattering location and scattering volume extent are within GYRO simulation domain.





### Mapped Experimental Wavenumbers in GYRO Density Spectra



- (k<sub>r</sub>, k<sub>θ</sub>)<sup>exp</sup> are closer to the spectral peak of fluctuations than previously thought
   → more transport relevant!
- Black dots: scattering  $(k_r, k_{\theta})^{exp}$  for channels 1,2,3

# Outline

- Motivation
- Old high-k scattering system at NSTX
- The GYRO code
- Previous Work on synthetic high-k
- New Synthetic Diagnostic for the high-k scattering system
  - 1. Coordinate mapping (this talk)
  - 2. Filtering (ongoing work)

#### Results from Coordinate Mapping

- 1. Old high-k system
- 2. New high-k system

## Operating Space of New High-k Scattering Diagnostic

 A new high-k scattering system is being designed to detect streamers based on previous predictions: Old high-k system: high-k<sub>p</sub>, intermediate k<sub>θ</sub>

New high-k system: high- $k_{\theta}$ , intermediate  $k_r \rightarrow$  streamers

- My goal: project the operating space of the new high-k scattering diagnostic using the mapping I implemented.
- **Disclaimer**: k-mapping of new high-k scattering system is based on:
  - Experimental turbulence wavenumbers from previous studies (Barchfeld APS 2015, UC-Davis/NSTX-U Review of Fluct. Diagnostics May 2016).
     k<sub>Z</sub> = 7-40 cm<sup>-1</sup>
     k<sub>R</sub> = 0 cm<sup>-1</sup>
     → High-k<sub>θ</sub> scattering diagnostic.
  - 2. Current plasma conditions (B ~ 0.5 T,  $T_e$  ~ 0.4 keV).

#### Mapped Wavenumbers of New High-k to GYRO 2D Fluctuation Spectrum



- Black dots: old hk
- <u>White dots</u>: new hk Picked k's in predicted measurement range  $k_Z = 7, 18, 29, 40 \text{ cm}^{-1}$  $k_R = 0 \text{ cm}^{-1}$ 
  - Blue star: streamers

26

#### Mapped Wavenumbers of New High-k to GYRO 2D Fluctuation Spectrum



#### **NSTX-U**

#### NSTX-U Science Meeting, Dec 5 2016

# Mapped Wavenumbers of New High-k Diagnostic to GYRO $k_{\theta}$ Fluctuation Spectrum



- Spectrum is integrated in k<sub>r</sub>.
- Lowest-k channel will be closest to peak of fluctuation spectrum (streamers) k<sub>R</sub>=0, k<sub>7</sub>=7 cm<sup>-1</sup>
- Need to resolve very high-k ( $k_{\theta}\rho_{s}$  ~ 50) to capture highest-k channel.
- Red band: measurement range of old system.
- Gray bands: measurement range of new system.

# Future Work and Conclusions on Synthetic Diagnostic Implementation

#### Future work

- Implementation of selectivity function and filtering.
- Use syn. diagnostic for quantitative comparisons with experiment.
- Can apply mapping to project operating space of additional scattering diagnostics (e.g. DBS).

#### **Conclusions**

- Computationally expensive simulations are needed to simultaneously resolve full ETG spectrum and experimental k in old high-k system (not in the new system).
- Old high-k system is sensitive to k that are closer to the spectral peak of fluctuations than previously thought → more transport relevant!
- New high-k system could detect streamers in lowest-k channel.
- For the first time, we're getting *close* to a quantitative comparison experiment-simulation of electron scale turbulence in NSTX and NSTX-U.
   → Important step to understand electron thermal transport in NSTX-U!

This work is supported by US. D.O.E. Contract No. DE-AC02-09CH11466. Computer simulations were carried out at the National Energy Research Scientific Computing Center, US. D.O.E. Contract No. DE-AC02-05CH11231.

# **Back-up slides**



#### Spherical Tokamaks such as NSTX Exhibit High Levels of Toroidal Rotation



Standard tokamak

Spherical tokamak (ST)

- Spherical tokamaks are more compact than standard tokamaks: easier to drive toroidal rotation.
- Toroidal rotation gives rise to perpendicular flows ( $\omega_{ExB}$  shearing rate)  $\rightarrow$  important key parameter in turbulence and transport.

#### Use a High-k Scattering Diagnostic to Probe Electron Scale Turbulence in NSTX and NSTX-U



#### Gyrokinetics is the Leading Theory that Describes Turbulence and Transport in Fusion Plasmas

- Start with Fokker-Planck equation + Assume:  $k_{\perp}\rho_i \sim 1$   $\omega/\omega_{ci} << 1$
- Gyroaverage  $\rightarrow$  remove gyrophase coordinate!



- Arrive to the gyrokinetic-Maxwell system: 5D, nonlinear system of coupled equations: unknowns
  - perturbed distribution function of species s
  - perturbed electromagnetic field components

h<sub>s</sub>  $\delta \phi$ ,  $\delta A_{\parallel}$ ,  $\delta B_{\parallel}$ 

Real Space Mapping:  $(R, Z, \phi) \rightarrow (r, \theta, \phi)$ 

• Start from expression of  $R(r,\theta)$ ,  $Z(r,\theta)$ . Ex: Miller-like equilibrium

 $\begin{cases} R(r,\theta) = R_0(r) + r * \cos(\theta + \arcsin(\delta(r))\sin(\theta)) \\ Z(r,\theta) = Z_0(r) + r * \kappa(r) * \sin(\theta + \zeta(r)\sin(2\theta)) \end{cases}$ 

κ elongation
δ triangularity
ζ squareness

• Given ( $R_{loc}$ ,  $Z_{loc}$ ): Determine ( $r_{loc}$ ,  $\theta_{loc}$ ) by nonlinear solve of

 $\begin{cases} R(r_{loc}, \theta_{loc}) = R_{loc} \\ Z(r_{loc}, \theta_{loc}) = Z_{loc} \end{cases}$ 

• Next: determine k-mapping



# Wavenumber Mapping: $(k_R, k_Z) \rightarrow (k_r, k_\theta)$

Mapping (k<sub>R</sub>, k<sub>Z</sub>) → (k<sub>r</sub>, k<sub>θ</sub>) is done using the GYRO definitions of k + transformation of coordinate systems.
 Result is:

$$\begin{cases} k_{\rm r} - \frac{r}{q} \frac{\partial v}{\partial r} k_{\theta} = \frac{\partial R}{\partial r} k_{R} + \frac{\partial Z}{\partial r} k_{Z} \\ - \frac{r}{q} \frac{\partial v}{\partial \theta} k_{\theta} = \frac{\partial R}{\partial \theta} k_{R} + \frac{\partial Z}{\partial \theta} k_{Z} \end{cases}$$

- Need to compute  $\partial R/\partial r$ ,  $\partial R/\partial \theta$ ,  $\partial Z/\partial r$ ,  $\partial Z/\partial \theta @ (r_{loc}, \theta_{loc})$
- Given  $(k_R, k_Z)^{exp}$  (ray-tracing), will obtain  $(k_r, k_{\theta})^{exp}$  in GYRO coordinates!

## **Summary of Coordinate Mapping**

The mapping in real-space: obtain  $(r_{loc}, \theta_{loc})$  from  $(R_{loc}, Z_{loc})$ 

$$\begin{cases} R(r_{loc}, \theta_{loc}) = R_{loc} \\ Z(r_{loc}, \theta_{loc}) = Z_{loc} \end{cases}$$

The mapping in k-space: obtain  $(k_r, k_{\theta})$  from  $(k_R, k_Z)^{exp}$ 

$$\begin{cases} k_{\rm r} - \frac{r}{q} \frac{\partial v}{\partial r} k_{\theta} = \frac{\partial R}{\partial r} k_{R} + \frac{\partial Z}{\partial r} k_{Z} \\ - \frac{r}{q} \frac{\partial v}{\partial \theta} k_{\theta} = \frac{\partial R}{\partial \theta} k_{R} + \frac{\partial Z}{\partial \theta} k_{Z} \end{cases}$$



#### New High-k Scattering System was Designed to Detect Streamers based on Previous Predictions

- Old high-k system: high- $k_r$ , intermediate  $k_{\theta}$
- New high-k system: high-k<sub> $\theta$ </sub>, intermediate k<sub>r</sub>  $\rightarrow$  streamers
- y-axis scales are different, x-axis scales are similar





#### New High-k Scattering System was Designed to Detect Peak in Fluctuation Amplitude: streamers

- Old high-k system: high- $k_r$ , intermediate  $k_{\theta}$
- New high-k system: high-k<sub> $\theta$ </sub>, intermediate k<sub>r</sub>  $\rightarrow$  streamers





### Standard Electron Scale Simulation Captures Correctly Wavenumbers Detected by New High-k System



- $k_{\theta}$  values are restricted to [-5,5]
- k<sub>r</sub> shown are full simulated spectrum.
- A big-box e- scale simulation is not needed to resolve spectrum of new high-k system.

Given from experiment (ray tracing)

 $k_R = -1857 \text{ m}^{-1}$ ,  $k_Z = 493 \text{ m}^{-1}$  (channel 1 of high-k diagnostic, shot 141767, t = 398 ms)

#### Get from GYRO (internally calculated)

- $(\rho_s)_{GYRO} \sim 0.002 \text{ m} (B_unit \sim 1.44)$
- |∇r| ~ 1.43, κ ~ 2

Apply k-mapping : close to the midplane, use simplified approx.

$$\begin{cases} (k_r \rho_s)_{GYRO} = k_R * (\rho_s)_{GYRO} / |\nabla r| \\ (k_{\theta} \rho_s)^{loc} = k_Z * \kappa * (\rho_s)_{GYRO} \end{cases}$$
  
Obtain experimental wavenumbers mapped to GYRC

$$(\kappa_n \rho_s)_{\text{GYRO}} \sim -2.0$$
  
 $(k_\theta \rho_s)^{loc} \sim 2.0 \Rightarrow (k_\theta \rho_s)_{\text{GYRO}} \sim 5$ 

#### Past Work on NSTX H-mode Plasma Showed Stabilization of e- scale Turbulence by Density Gradient

- NSTX NBI heated H-mode featured a controlled current ramp-down. Shot 141767.
- An increase in the equilibrium density gradient was correlated to a decrease in high-k density fluctuation amplitude (measured by a high-k scattering system). *cf.* Ruiz Ruiz PoP 2015.





#### Experiment, Linear and Nonlinear Gyrokinetic Simulation Showed Density Gradient Stabilization of e- scale Turbulence

- Experimental k-spectrum is measured with a high-k scattering diagnostic (*cf.* Smith RSI 2008).
- Peak amplitude in experimental k-spectra, linear growth rate and nonlinear electron heat flux using gyrokinetic simulation is reduced, and shifted to higher wavenumber with increasing density gradient.



#### Probe Origins of Anomalous Electron Heat Flux Using Two Different Approaches:

1. Revisit the assumption:

#### 'Ion scale turbulence is suppressed by ExB shear in NSTX NBI heated Hmode plasmas'.

Approach: Identify ion scale instability and ion scale turbulence contributions to  $Q_e$  using linear and nonlinear gyrokinetic simulation (GYRO).

#### 2. To what level of confidence do we trust transport predictions from previous escale simulations?

Approach: **Develop a synthetic high-k scattering diagnostic** for quantitative comparisons between electron scale turbulence measurements and nonlinear GYRO simulations.





## **Prerequisites to Coordinate Mapping**

#### We want to perform:

- coordinate mapping GYRO ( $r, \theta, \varphi$ )
- wavenumber mapping  $(k_n \rho_s, k_{\theta} \rho_s)_{GYRO}$

#### **Prerequisites**

- Units: r[m], R[m], Z[m],  $\theta, \phi \in [0, 2\pi]$
- GYRO definition of  $k_{\theta}^{loc}$  and  $k_{\theta}^{FS}$

$$k_{\theta}^{loc}(r,\theta) = -\frac{n}{r}\frac{\partial v}{\partial \theta}, \quad k_{\theta}^{FS} = \frac{nq}{r}$$

Consistent with GYRO definition of flux-surface averaged  $k_{\theta}^{FS}$ =nq/r (*cf.* backup)

• Wavenumber mapping under simplifying assumptions

$$k_{R} = (k_{r}\rho_{s})_{GYRO} \left|\nabla r\right| / (\rho_{s})_{GYRO}$$

$$k_{Z} = (k_{\theta} \rho_{s})_{GYRO}^{loc} / (\kappa . \rho_{s})_{GYRO}$$

- Miller-like parametrization
- $\zeta=0$ ,  $d\zeta/dr=0$  (squareness)
- $Z_0=0$ ,  $dZ_0/dr=0$  (elevation)
- UD symmetric (up-down symmetry)  $\rightarrow$ ( $\theta$ =0)

←→ physical (R, Z, 
$$φ$$
)  
←→ (k<sub>R</sub>, k<sub>z</sub>)

## Numerical Resolution Comparison with Traditional Ion Scale, Electron Scale and Multiscale Simulation

Poloidal wavenumber resolution ( $k_{\theta}\rho_{s}$  here means  $k_{\theta}\rho_{s}^{FS}$ )

	$\Delta k_{\theta} \rho_s$	$k_{\theta} \rho_s^{max}$	n #tor. modes
lon scale	~0.05	~1	~20-30
e- scale	~1-1.5	~50	~50
Multi-scale	~0.1	~40	~500
Big-box e- scale	0.3	43	142

Radial resolution  $\Delta r$ – radial box size L<sub>r</sub>

	Δr	L <sub>r</sub>	n <sub>r</sub> radial grid
lon scale	$\sim 0.5 \ \rho_s$	~80-100 ρ <sub>s</sub>	~ 200
e- scale	~ 2 p <sub>e</sub>	~ 6-8 ρ <sub>s</sub>	~ 200
Multi-scale	~ 2 ρ <sub>e</sub>	~ 40-60 ρ <sub>s</sub>	~ 1500
Big-box e- scale	2.5 ρ <sub>e</sub>	20 ρ <sub>s</sub>	512

## Input Parameters into Nonlinear Gyrokinetic Simulations Presented

	t=398 t	= 565			
r/a	0.71	0.68	R <sub>o</sub> /a	1.52	1.59
a [m]	0.6012	0.596	SHIFT =dR <sub>0</sub> /dr	-0.3	-0.355
n <sub>e</sub> [10^19 m-3]	4.27	3.43	KAPPA = κ	2.11	1.979
T <sub>e</sub> [keV]	0.39	0.401	s <sub>k</sub> =rdln(κ)/dr	0.15	0.19
a/L <sub>ne</sub>	1.005	4.06	DELTA = $\delta$	0.25	168
a/L <sub>Te</sub>	3.36	4.51	s <sub>δ</sub> =rd(δ)/dr	0.32	0.32
$\beta_e^{unit}$	0.0027	0.003	Μ	0.2965	0.407
a/L <sub>nD</sub>	1.497	4.08	Υ <sub>E</sub>	0.126	0.1646
a/L <sub>Ti</sub>	2.96	3.09	γ <sub>p</sub>	1.036	1.1558
T <sub>i</sub> /T <sub>e</sub>	1.13	1.39	ρ*	0.003	0.0035
n <sub>D</sub> /n <sub>e</sub>	0.785030	0.80371	λ <sub>D</sub> /a	0.000037	0.0000426
n <sub>c</sub> /n <sub>e</sub>	0.035828	0.032715	c <sub>s</sub> /a (10 <sup>5</sup> s-1)	4.4	2.35
a/L <sub>nC</sub>	-0.87	4.08	Qe (gB)	3.82	0.0436
a/L <sub>TC</sub>	2.96	3.09	Qi (gB)	0.018	0.0003
Z <sub>eff</sub>	1.95	1.84			
nu <sub>ei</sub> (a/c <sub>s</sub> )	1.38	1.03			
q	3.79	3.07			
S	1.8	2.346			

# Mapping $(k_r \rho_s, k_\theta \rho_s)_{GYRO} \rightarrow (k_R, k_Z)^{exp}$

We want to perform:

- coordinate mapping GYRO ( $r, \theta, \varphi$ )
- wavenumber mapping  $(k_n \rho_s, k_{\theta} \rho_s)_{GYRO}$

#### Preamble 1

- Units: r[m], R[m], Z[m]  $\theta, \phi \in [0, 2\pi]$
- GYRO definition of  $k_{\theta}^{loc}$  and  $k_{\theta}^{FS}$

$$ik_{\theta}^{loc}(r,\theta) = \frac{1}{r}\frac{\partial}{\partial\theta} \Longrightarrow k_{\theta}^{loc}(r,\theta) = -\frac{n}{r}\frac{\partial\nu}{\partial\theta} \qquad \text{(To be shown in slide 17)}$$

 $\leftarrow \rightarrow$  physical (R, Z,  $\varphi$ )

 $\leftarrow \rightarrow (k_R, k_7)$ 

Consistent with GYRO definition of flux-surface averaged  $k_{\theta}^{FS}=nq/r$  (*cf.* out.gyro.run)

$$k_{\theta}^{FS} = \frac{1}{2\pi} \int_{0}^{2\pi} k_{\theta}^{loc} d\theta = \frac{1}{2\pi} \int_{0}^{2\pi} -\frac{n}{r} \frac{\partial v}{\partial \theta} d\theta = \left(-\frac{n}{r}\right) \frac{v(r, 2\pi) - v(r, 0)}{2\pi} = \frac{nq(r)}{r}$$

# Mapping $(k_r \rho_s, k_\theta \rho_s)_{GYRO} \rightarrow (k_R, k_Z)^{exp}$

Preamble 2 why is 
$$k_{\theta}^{loc}(r,\theta) = -\frac{n}{r} \frac{\partial v}{\partial \theta}$$
 ??  
GYRO decomposition of fields

$$\delta\phi(r,\theta,\alpha) = \sum_{j=-Nn+1}^{Nn-1} \delta\hat{\phi}_n(r,\theta) e^{-in\alpha} e^{in\overline{\omega}_0 t} = \sum_{j=-Nn+1}^{Nn-1} \delta\phi_n(r,\theta), \quad \alpha = \varphi + \nu(r,\theta)$$

Set  $\phi$ =0 and  $\omega_0$  = 0. Focus on transformation of one toroidal mode n. By definition of  $k_{\theta}^{loc}$ 

$$ik_{\theta}^{loc}\delta\phi_{n}(r,\theta) = \frac{1}{r}\frac{\partial}{\partial\theta}(\delta\phi_{n}(r,\theta)) = \frac{1}{r}\frac{\partial}{\partial\theta}(\delta\hat{\phi}_{n}(r,\theta)e^{-in\nu(r,\theta)}) = \frac{1}{r}\frac{\partial}{\partial\theta}(\delta\hat{\phi}_{n}(r,\theta)e^{-in\nu(r,\theta)}) = \frac{1}{r}\frac{\partial}{\partial\theta}e^{-in\nu} + \delta\hat{\phi}_{n}\left(-in\frac{\partial\nu}{\partial\theta}e^{-in\nu}\right) \Longrightarrow \delta\phi_{n}(r,\theta)\left(\frac{-in}{r}\frac{\partial\nu}{\partial\theta}\right)$$

**Conclusion**: we assume definition of  $k_{\theta}^{loc}$  is **correct**. There is a one-to-one relation between n and  $k_{\theta}^{loc}$ .

$$k_{\theta}^{loc}(r,\theta) = -\frac{n}{r} \frac{\partial v}{\partial \theta}$$

#### **NSTX-U**

#### NSTX-U Science Meeting, Dec 5 2016

Mapping  $(k_r \rho_s, k_\theta \rho_s)_{GYRO} \rightarrow (k_R, k_7)^{exp}$ 

**Preamble 3** Wavenumber mapping under simplifying assumptions

$$k_{R} = (k_{r}\rho_{s})_{GYRO} \left|\nabla r\right| / (\rho_{s})_{GYRO}$$

$$k_{Z} = (k_{\theta} \rho_{s})_{GYRO}^{loc} / (\kappa . \rho_{s})_{GYRO}$$

- Assumptions
  - $-\zeta=0$ , d $\zeta$ /dr=0 (squareness + radial derivative)
  - $Z_0 = 0$ ,  $dZ_0/dr = 0$  (elevation + radial derivative)
  - UD symmetric (up-down asymmetry of flux surface)
- In the following slides, develop mapping when assumptions are not satisfied, invert
   (R(r A) Z(r A))=(R Z ) (r A)

 $(\mathsf{R}(\mathsf{r},\theta),\mathsf{Z}(\mathsf{r},\theta))=(\mathsf{R}_{\exp},\mathsf{Z}_{\exp}) \rightarrow (\mathsf{r}_{\exp},\theta_{\exp})$ .

## Principle of Geometric Mapping is Independent of Flux Surface Parametrization

Computation of metric coefficients

- Whether you use a Model Grad-Shafranov equilibrium (GS, Miller-type) or a general equilibrium (Fourier), procedure is the same.
- In cases shown here, I use GS equilibrium.
  - In GYRO simulation, I use input parameters THETA\_PLOT=8, THETA\_MULT=128 (fine poloidal grid).
  - Get r[m] from out.gyro.profiles (use a<sub>ref</sub> !!)
  - − Create a θ array  $\in$  [0,2π], size THETA\_PLOT\*THETA\_MULT+1=1025.
  - Define  $R(r,\theta)$  and  $Z(r,\theta)$  (GS or general eq.). Used GS equilibrium here:

$$R(r,\theta) = R_0(r) + r * \cos(\theta + \arcsin(\delta(r))\sin(\theta)) \quad [m]$$
  
$$Z(r,\theta) = Z_0(r) + r * \kappa(r) * \sin(\theta + \zeta(r)\sin(2\theta)) \quad [m]$$

How am I sure that these derivatives are computed correctly?
 Comparisons with output from out.gyro.geometry\_arrays!

# Wavenumber Mapping: $(k_R, k_Z) \rightarrow (k_r, k_\theta)$

- Definitions of  $k_R$ ,  $k_Z$ ,  $k_p$ ,  $k_{\theta}^{loc}$
- + Jacobian transformation

$$ik_{R} = \frac{\partial}{\partial R}, \quad ik_{Z} = \frac{\partial}{\partial Z} + \begin{pmatrix} \frac{\partial}{\partial r} \\ \frac{\partial}{\partial r} \\ \frac{\partial}{\partial \theta} \end{pmatrix} = \begin{pmatrix} \frac{\partial R}{\partial r} & \frac{\partial Z}{\partial r} \\ \frac{\partial R}{\partial \theta} & \frac{\partial Z}{\partial \theta} \end{pmatrix} \begin{pmatrix} \frac{\partial}{\partial R} \\ \frac{\partial}{\partial R} \\ \frac{\partial}{\partial R} & \frac{\partial}{\partial z} \end{pmatrix}$$

$$ik_{r} = \frac{\partial}{\partial r}, \quad ik_{\theta}^{loc} = \frac{1}{r} \frac{\partial}{\partial \theta} + k_{Z} \frac{\partial R}{\partial r}$$

$$k_{\theta}^{loc} = k_{R} \frac{1}{r} \frac{\partial R}{\partial \theta} + k_{Z} \frac{1}{r} \frac{\partial Z}{\partial \theta}$$

- Need to compute  $\partial R/\partial r$ ,  $\partial R/\partial \theta$ ,  $\partial Z/\partial r$ ,  $\partial Z/\partial \theta$  @ ( $r_{loc}$ ,  $\theta_{loc}$ )
- Given  $k_R^{exp}$ ,  $k_Z^{exp}$ , will obtain  $(k_r, k_\theta)_{exp}$  in GYRO coordinates!



- Standard e- scale simulation does not accurately resolve experimental k.
- Big-box simulation spectra show well resolved (k<sub>R</sub>,k<sub>Z</sub>)<sup>exp</sup> and ETG spectrum.
- Experimental wavenumbers produce non-negligible  $\delta n_e$  and  $Q_e$  consistent with previous e- scale simulation results ( $Q_e \sim 0.4$  MW).



- Standard e- scale simulation does not accurately resolve experimental k.
- Big-box simulation spectra show well resolved  $(k_R, k_Z)^{exp}$  and ETG spectrum.
- Experimental wavenumbers produce non-negligible  $\delta n_e$  and  $Q_e$  consistent with previous e- scale simulation results ( $Q_e \sim 0.4$  MW).



- Spectra show well resolved  $(k_R, k_Z)^{exp}$  and ETG spectrum.
- Experimental wavenumbers produce non-negligible  $\delta n_e$  and  $Q_e$  consistent with previous e- scale simulation results ( $Q_e \sim 0.4$  MW).

## Computed GYRO Geometric Coefficients agree with GYRO output



**Conclusion**: Agreement between output from out.gyro.geometry\_arrays and computed coefficients gives us confidence the mapping is being performed correctly.



## Poloidal Cross Section of High-Resolution Electron Scale Simulation



#### **NSTX-U**

#### NSTX-U Science Meeting, Dec 5 2016

### Linear Growth Rates for Low-k and High-k Turbulence

- Note ion propagating high-k mode + electron propagating, non-balloning mode at krho~12.
- Microtearing turbulence?



# $k_{\theta}$ resolution in synhk GYRO sim.

Huge e- scale run for syn hk (tested it in debug!  $\rightarrow$  1h30m for 1 a/cs)

16,488 cores, ~ 24h, 4 open MP threads( 4x4,032cores), Edison (x1.2) → 500,000 h (400,000h)

Run for 20 a/cs

Distribution points 495,452,160



# Appendix: Compute ( $\Delta k_R, \Delta k_Z$ ) $\rightarrow (\Delta k_r \rho_s, \Delta k_\theta \rho_s)^{GYRO}$

Assume  $\Delta k_R = \Delta k_Z = \Delta k = 66.7 \text{ m}^{-1}$ 

$$\begin{bmatrix} k_r = k_R \frac{\partial R}{\partial r} + k_Z \frac{\partial Z}{\partial r} \\ rk_\theta = k_R \frac{\partial R}{\partial \theta} + k_Z \frac{\partial Z}{\partial \theta} \end{bmatrix} \Rightarrow \begin{bmatrix} (\Delta k_r)^2 = (\Delta k_R)^2 \left(\frac{\partial R}{\partial r}\right)^2 + (\Delta k_Z)^2 \left(\frac{\partial Z}{\partial r}\right)^2 \\ (\Delta k_\theta)^2 = (\Delta k_R)^2 \left(\frac{1}{r} \frac{\partial R}{\partial \theta}\right)^2 + (\Delta k_Z)^2 \left(\frac{1}{r} \frac{\partial Z}{\partial \theta}\right)^2 \end{bmatrix}$$

This assumes beam radius a = 3cm, such that  $\Delta k = 2/a = 66.7$ m<sup>-1</sup>

As a first approximation, assume simplest selectivity function: gaussian is  $k_r$  and  $k_\theta$ 

$$F(k_r, k_{\theta}) = F_r(k_r) F_{\theta}(k_r)$$
  

$$F_r(k_r) = \exp\left(-(k_r - k_r^{\exp})^2 / \Delta k_r^2\right)$$
  

$$F_{\theta}(k_{\theta}) = \exp\left(-(k_{\theta} - k_{\theta}^{\exp})^2 / \Delta k_{\theta}^2\right)$$









NSTX-U Science Meeting, Dec 5 2016



## Appendix: Compute Inverse Derivatives

### Start from the coordinate transformation

$$\begin{pmatrix} \delta R \\ \delta Z \end{pmatrix} = \begin{pmatrix} \frac{\partial R}{\partial r} & \frac{\partial R}{\partial \theta} \\ \frac{\partial Z}{\partial r} & \frac{\partial Z}{\partial \theta} \end{pmatrix} \begin{pmatrix} \delta r \\ \delta \theta \end{pmatrix} = J \begin{pmatrix} \delta r \\ \delta \theta \end{pmatrix} \implies \begin{pmatrix} \delta r \\ \delta \theta \end{pmatrix} = J^{-1} \begin{pmatrix} \delta R \\ \delta Z \end{pmatrix}$$

Additionally, we can write the inverse transformation

$$\begin{pmatrix} \delta r \\ \delta \theta \end{pmatrix} = \begin{pmatrix} \frac{\partial r}{\partial R} & \frac{\partial r}{\partial Z} \\ \frac{\partial \theta}{\partial R} & \frac{\partial \theta}{\partial Z} \end{pmatrix} \begin{pmatrix} \delta R \\ \delta Z \end{pmatrix}$$

Compute inverse matrix J<sup>-1</sup>

$$J^{-1} = \frac{1}{\det J} \begin{pmatrix} \frac{\partial Z}{\partial \theta} & -\frac{\partial R}{\partial \theta} \\ -\frac{\partial Z}{\partial r} & \frac{\partial R}{\partial r} \end{pmatrix}, \quad \det J = \frac{\partial R}{\partial r} \frac{\partial Z}{\partial \theta} - \frac{\partial R}{\partial \theta} \frac{\partial Z}{\partial r}$$

\* Recall dRdθ =0\* Recall dZ/dr =0

## **Appendix: Compute Inverse Derivatives**

## We find

$\int \frac{\partial r}{\partial r}$	$1 \frac{\partial Z}{\partial Z}$
$\partial R$	$\det J \ \overline{\partial \theta}$
$\partial r$	$1 \partial R$
$\int \frac{\partial Z}{\partial Z}$	$\frac{1}{\det J} \frac{\partial \theta}{\partial \theta}$
$\partial \theta$	$1  \partial Z$
$\partial R$	$\frac{1}{\det J} \frac{\partial r}{\partial r}$
$\partial \theta$	1 $\partial R$
$\left\lfloor \frac{\partial Z}{\partial Z} \right\rfloor$	$\frac{1}{\det J} \frac{1}{\partial r}$

$$\det J = \frac{\partial R}{\partial r} \frac{\partial Z}{\partial \theta} - \frac{\partial R}{\partial \theta} \frac{\partial Z}{\partial r}$$

## Steps:

Compute forward derivatives

Compute inverse derivatives

Complete (k<sub>R</sub>,k<sub>Z</sub>) mapping



- Spectra show well resolved  $(k_R, k_Z)^{exp}$  and ETG spectrum.
- Experimental wavenumbers produce non-negligible  $\delta n_e$  and  $Q_e$  consistent with previous e- scale simulation results ( $Q_e \sim 0.4$  MW).

## Conclusions and Future Work on Synthetic Diagnostic

- Implement instrumental selectivity function and wavenumber filtering.
- **Goal**: a direct, quantitative comparison between experiment-GYRO simulation of e- scale turbulence.
  - Compare fluctuation spectrum high-k diagnostic/synthetic high-k.
  - Study energy transfer between different k's (different channels).
- Project operating space of new high-k diagnostic.
  - Are streamers predicted to be detected with the new high-k system?
- Study turbulence characteristics in high-resolution e- scale run → towards multiscale simulation in NSTX-U.
  - High-resolution electron scale runs presented here are NOT multiscale
    - lons are not resolved correctly  $\Delta k_{\theta} \rho_s \sim 0.3$ ,  $L_r \propto L_y = 21 \propto 21 \rho_s$ .
    - Simulation ran only for electron time scales ( $\sim 20a/c_s$ ), ions are not fully developped.
  - In future, can apply synthetic high-k to multiscale simulation in NSTX-U.

This work is supported by US. D.O.E. Contract No. DE-AC02-09CH11466. Computer simulations were carried out at the National Energy Research Scientific Computing Center, US. D.O.E. Contract No. DE-AC02-05CH11231.



# Title here

Column 1

Column 2



# Intro

- First level
  - Second level
    - Third level
      - You really shouldn't use this level the font is probably too small

# Here are the official NSTX-U icons / logos

**NSTX Upgrade NSTX Upgrade NSTX-U NSTX-U** National Spherical Torus eXperiment Upgrade **National Spherical Torus experiment Upgrade** 

## Instructions for editing bottom text banner

Go to View, Slide Master, then select top-most slide - Edit the text box (meeting, title, author, date) at the bottom of the page Then close Master View plate new v1.pptx - Microsoft PowerPe Colors \* Delete Aa Title Rename A Fonts -Themes Page Slide Close Setup Orientation \* Master View Effects \* Click to edit Master title style ick to edit Master text style hird level Click to edit Master title style C ENERGY Click to edit Master text styles - Second level Third level Click to edit Master title styl Fourth level - Tripleral - Tripleral - Facebook » Fifth level - Tractice - Tractice - Tractice - Tractice - Tractice - Tractice -Secret land -Secr Click to edit Master title style - Second Incel - Triglevel - Triglevel - Triglevel - Triglevel **NSTX-U** Meeting name, presentation title, author name, date

#### **NSTX-U**

#### NSTX-U Science Meeting, Dec 5 2016