



**Large Volume Plasma Device** 

### **Experimental Study on ETG Turbulence Induced Plasma Transport in Large Volume Plasma Device**

### **Prabhakar Srivastav**

\*e-mail: prabhakar.srivastav@ipr.res.in

$$egin{aligned} \Omega_{ci} < \omega \ll \Omega_{ce} \ k_\perp 
ho_e \leq 1 \end{aligned}$$

Talk at PPPL (August 28, 2019)



## Outline

- Introduction
- **Experimental setup**
- □ Identification of ETG instability in LVPD
- □ Investigation of particle and energy transport,
  - **Electrostatic particle flux** ( $\Gamma_{es} = \langle \delta n_e \delta v_r \rangle$ )
  - **Electromagnetic particle flux**( $\Gamma_{em} = \frac{\langle \delta J_{\parallel,q} \delta B_r \rangle}{qB}$ )
  - **Total heat flux**  $(Q_{total} = \frac{3}{2} < \delta p_e \delta v_r >)$
- **Summary & conclusion**







- \* Transport involves study of physical processes responsible for particles, momentum and energy displacement.
- **\*** Transport determines the profile of the system self-consistently.
- Transport in plasma can be understood under the following three categories namely,
  - 1. Classical transport  $\propto v (\lambda_f^2)$
  - 2. Neo-classical transport  $\propto \nu (\lambda_f^2)(1+2q^2)$  [in tokamaks]
  - 3. Turbulent transport  $\propto \left|\widetilde{\boldsymbol{\phi}}\right|^2$



- \* Turbulent Transport is a universal phenomenon present in laboratory, space and astrophysical systems.
- Turbulence leads to generation of particle as well as heat transport of the order of magnitudes higher than the classical and neoclassical flux predictions in fusion devices.
- \* This anomalous flux is attributed to turbulent fluctuations due to various instabilities inherent in the system.
- \* Confined systems are naturally inhomogeneous which act as source of free energy to drive the system, any perturbations can evolve over a wide range of scale, from electron to ion and up to system scale.
- ★ Large scale perturbations are easy to probe in tokamaks and tremendous progress has already been made on ion temperature gradient driven micro-turbulent mode ( $k_{\perp}\rho_i \leq 1$ ) and MHD modes.



Small scale fluctuations, of the order of electron scale excited due to electron temperature gradient in high magnetic field (~Tesla) of tokamak are difficult to  $probes(k_{\perp}\rho_{e} \leq 1)$ .



 $0.55 \text{ T}, 1 \text{ MA}, R_0 \sim 0.85 \text{ m}, A \ge 1.32$ 

Tore Supra, (Horton *et al.* Phys. Plasmas, Vol. 11, No. 5, (2004))
NSTX, (Mazzucato *et al.* Phys. Rev. Lett. 101, 075001 (2008))



To understand such small scales fluctuation some linear devices like Columbia Linear Machine (CLM), Large Volume Plasma Device (LVPD) have taken initiatives.



- ★ X. Wei *et. al.* Phys. Plasmas **17**, 042108 (2010)
- ★ V. Sokolov and A. K. Sen, Phys. Rev. Lett. **107**, 155001 (2011)
- ✤ Fu et al. Phys. Plasmas 19, 032303 (2012)



★ In LVPD with finite plasma beta,  $\beta \sim (0.06 - 0.4)$ , electron temperature gradient driven turbulence is observed in energetic electrons free plasma by making use of



What is the role of ETG scale fluctuation on plasma transport in LVPD?



### **Turbulent Transport Mechanism**









### $\Box$ Coil arrangement for axial magnetic field ( $B_z$ )





### Radial confinement















Photo Graph of EE<sup>#4</sup>















### **Experimental plasma parameters**

	Source	EEF	Target
Plasma density, $n_e$ (cm <sup>-3</sup> )	$6.0 \times 10^{11}$	$2.3 \times 10^{11}$	$1 \times 10^{11}$
Electron temperature, $T_e(eV) \& T_i = T_e/10$	8.0	2.5	2.2
Plasma beta, $oldsymbol{eta}$	1.6	10 <sup>-3</sup>	0.2
$f_{pe}$	$7 \times 10^{9}$	$4.9 \times 10^{9}$	$3.5  imes 10^{9}$
f <sub>pi</sub>	$3 \times 10^{7}$	$1.8 \times 10^{7}$	$1.3 \times 10^{7}$
f <sub>ce</sub>	$1.0 \times 10^{7}$	$2.8 \times 10^{8}$	$1.0 \times 10^{7}$
f <sub>ci</sub>	236	$6 \times 10^{3}$	236
Debye length, $\lambda_{De}$ ( <i>cm</i> )	$2.1 \times 10^{-3}$	$2.3 \times 10^{-3}$	$2.7 \times 10^{-3}$
Electron gyro-radius, $ ho_{e}\left( cm ight)$	0.8	0.02	0.5
Ion gyro-radius, $ ho_i$ (cm)	73	2.2	46



□Pulse characteristic of plasma shot



19



☐ Mean plasma profile





### Temporal Evolution of Fluctuation



### Radial Profile of fluctuation and Power Spectra of fluctuation



Fluctuation enhances when EEF is ON in the core

Density and Potential fluctuation share common frequency band of spectrum



### $\square$ Correlation between $\tilde{n}$ and $\tilde{\phi}$



### Diamagnetic Drift Direction and Poloidal Rotation of the mode



✓ Mode propagation is in positive y-direction, similar to  $V_{di}$ ✓ Measured poloidal propagation velocity,  $V_{\theta} = 2.5 \times 10^3 m/sec$ 



### □ Characterization of ETG turbulence

$$\eta_e = rac{L_n}{L_{T_e}} > rac{2}{3}, rac{k_z}{k_\perp} \ll 1$$

1. Frequency ordering  $(v_{in}(3 \times 10^3 s^{-1}) < \omega)$ 

$$\label{eq:sec} \begin{split} \Omega_{ci}(1.5\ krad/sec) &< \omega(6-100\ krad/sec) \ll \Omega_{ce}(10^3krad/sec) \\ sec) \end{split}$$

- 2. Wavelength ordering  $(\rho_e \approx 0.5 \text{ cm and } \rho_i \approx 40 \text{ cm})$  $k_\perp \rho_e \leq 1, \quad k_\perp \rho_i > 1$
- 3. Density and potential fluctuations  $\widetilde{n} = -\tau_e^* \widetilde{\phi}$



## **Theoretical Understanding of slab ETG**

### Electron Dynamics **Continuity Equation** $\frac{\partial n_e}{\partial t} + \nabla . \left( n_e v_{e\perp} \right) + \nabla_{\perp} (n_e v_{ez}) = 0$ Momentum Equation $m_e n_e \left( \frac{\partial v_e}{\partial t} + v_e . \nabla v_e \right)$ $= en_e \nabla_\perp \phi - \nabla p_e - en_e \frac{v_e \times B_z}{c}$ $-m_e n_e v_{en} v_e$ **Energy Equation** $\frac{3}{2}n_e\frac{dT_e}{dt} + p_e\nabla . v_e = -\nabla . q_e^*$ Electron drift can be following terms $v_{e\perp} = \left(v_E + v_{*pe}\right) \left(1 - \frac{\delta B_z}{B_-}\right) + v_{pe} + v_{\pi}$ Ampere's Law $\nabla \times B = \frac{4\pi}{a} j \approx \frac{4\pi e n_e}{a} v_e$

lon dynamics **Continuity Equation**  $\frac{\partial n_i}{\partial t} + \nabla . \left( n_i v_{i\perp} \right) = 0$ **Momentum Equation**  $m_i n_i \left( \frac{\partial v_i}{\partial t} + v_i \cdot \nabla v_i \right) = -e n_i \nabla_{\perp} \phi - T_i \nabla_{\perp} n_i$ **ETG model equations;**  $\widetilde{n}_i = -\tau_o^* \phi$  $\widetilde{T}_{e} = \left| \left( \frac{1}{L_{T}} - \frac{2}{3} \frac{1}{L_{T}} \right) \frac{k_{y} \rho_{e} c_{e}}{\omega} - \frac{2}{3} \tau_{e}^{*} \right| \widetilde{\phi}$  $\widetilde{B} = \widehat{\beta} \left[ \left( 1 + \frac{5}{3} \tau_e^* \right) - \left( \frac{1}{L_T} - \frac{2}{3} \frac{1}{L_T} \right) \frac{k_y \rho_e c_e}{\omega} \right] \widetilde{\phi}$ 

Zb

## **Theoretical Understanding of slab ETG**

### Numerical Solution of W-ETG dispersion relation and comparison with experimental data

$$\omega \left[ \omega \tau^* + \omega_{*e} + k_{\perp}^2 \rho_e^2 \left( \omega - \omega_{*pe} \right) + \frac{\beta_e}{2} \left( 1 + \tau_e^* \right) \left( \omega - \omega_{*pe} \right) \right] - \frac{\beta_e}{2} \left( \omega - \omega_{*pe} \right) \left[ \left( \eta_e - \frac{2}{3} \right) \omega_{*e} - \frac{2}{3} \tau_e^* \omega \right]$$

$$= k_z^2 c_e^2 k_{\perp}^2 \rho_e^2 \left[ \frac{\left( 1 + \tau_e \right) \omega - \left( \eta_e - \frac{2}{3} \right) \omega_{*e} + \frac{2}{3} \tau_e^* \omega}{\left\{ \omega \left( \frac{\beta_e}{2} + k_{\perp}^2 \rho_e^2 \right) + i \nu_e \, k_{\perp}^2 \rho_e^2 \right\} - \frac{\beta_e}{2} \, \omega_{*pe}} \right]$$



### □ Flux Probe Assembly and Fluctuation Measurement



## I. Study of electrostatic particle lux

### $\Box$ Particle flux, $\Gamma_{es}$ measurement



Particle flux for (a) EEF OFF and (b) EEF ON case is shown. The flux is enhanced in EEF ON case and is prominently negative. In EEF OFF plasma insignificantly low level of flux is observed.

### Probability Distribution Function (PDF)



Probability distribution function (PDF) for particle flux ( $\Gamma_{es}$ ), in the units of standard deviation (  $\sigma_{\Gamma_{es}} \approx 4 \times 10^{18} m^{-2} \text{ sec}^{-1}$ ) for different averaging time. The distribution of particle flux is asymmetric. **N** 

### □ Recalculation of ion response on ETG mode

- By considering un-magnetized and collision-less ion in ETG dynamics, where  $k_{\perp} V_{thi} \sim |\omega|$ , ETG mode resonates with background ions, which results in deviation of ions from Boltzmann condition.
- This response of ions can be determined by drift kinetic equation as follows;

Assuming Maxwellian equilibrium distribution function for ions in one dimension,

$$f_{oi} = n_{io} \sqrt{\frac{m_i}{2\pi T_i}} \exp\left(-\frac{V_y^2}{V_{thi}^2}\right) \dots \dots \dots \dots (2)$$

Where  $V_{thi}^2 = \frac{2T_i}{m_i}$ , using above distribution for ion in equation (1), we get fluctuating ion distribution as  $\tilde{f}_i = -\tau_e \,\tilde{\phi} \, \frac{V_y}{V_y - \frac{\omega}{k_y}} f_{oi} \, \dots \dots \dots (3)$ 

Then the ion density fluctuation

uctuation 
$$\tilde{n}_{i} = \frac{1}{n_{io}} \int \tilde{f}_{i} dV_{\perp}$$
$$\tilde{n}_{io} = -\frac{\tau_{e} \tilde{\phi}}{\pi^{\frac{1}{2}} V_{thi}} \int dV_{y} \frac{V_{y}}{V_{y} - \frac{\omega}{k_{y}}} \exp\left(-\frac{V_{y}^{2}}{V_{thi}^{2}}\right) \dots \dots \dots \dots (4)$$

# **X**

### I. Study of electrostatic particle flux

Re-writing equation (4)

Where  $\xi = V_y / V_{thi}$  and  $\hat{\omega} = \frac{\omega}{k_y V_{thi}}$ 

Simplifying equation (5), we have  $\tilde{n}_i = -\tau_e \tilde{\phi} [1 + \hat{\omega} Z(\hat{\omega})] \dots \dots \dots \dots \dots (6)$ 

*Where*  $Z(\widehat{\omega})$  is know as Dispersion function and defined as  $Z(\widehat{\omega}) = \frac{1}{\pi^{1/2}} \int_{-\infty}^{\infty} \frac{e^{-\xi^2}}{(\xi - \widehat{\omega})} d\xi$ For small ' $\widehat{\omega}$ ',

$$Z(\widehat{\omega}) = i\pi^{1/2}e^{-\widehat{\omega}^2} - 2\widehat{\omega}\left[1 - \frac{2\widehat{\omega}^2}{3} + \cdots \dots + 1\right] = i\pi^{1/2}e^{-\widehat{\omega}^2} - 2\widehat{\omega} + \cdots \dots$$

**Particle Flux;**  $\Gamma_{es} = \sum_{k_{\theta}} \frac{ik_{\theta}}{B} \tilde{n} \tilde{\phi}^*$ , for slab geometry  $k_{\theta} \sim k_y$ . Using equation(6) and above expansion in flux expression, the part of particle flux becomes

For  $\Gamma_{es} < 0$ ,  $k_y \omega < 0$ , ETG mode should propagate in Ion diamagnetic drift direction.



We considered the ion non-adiabatic response by using kinetic approximation of ion dynamics perpendicular to static magnetic field, i.e.

$$\tilde{n} = -\frac{T_e}{T_i} \left[ 1 + \frac{i\pi^{1/2}\omega}{k_y v_{thi}} \exp\left(-\frac{\omega^2}{k_y^2 v_{thi}^2}\right) \right] \tilde{\phi} \dots \dots (A)$$

Using this relation the estimated particle flux is given by,

$$\Gamma_r = <\delta n \delta v_r > = \sum_k \pi^{\frac{1}{2}} \frac{T_e}{T_i} n c_e k_y \rho_e \left(\frac{\omega_r}{k_\perp V_{thi}}\right) \left[\exp\left(-\frac{\omega_r^2}{k_\perp^2 V_{thi}^2}\right)\right] \left|\tilde{\phi}_k\right|^2 \dots \dots (B)$$

For  $\Gamma_{es} < 0$ ,  $k_y \omega < 0$ , ETG mode should propagate in Ion diamagnetic drift direction.



 $\Box$  Plasma beta,  $\beta$  effect on electrostatic and electromagnetic flux



### Temporal and Spectral Characteristics of Fluctuations



A comparison of particle flux due to electrostatic and electromagnetic fluctuations



✓ The obtained ratio of EM to Electrostatic flux is ,  $\left|\frac{\Gamma_{em}}{\Gamma_{es}}\right| \approx 10^{-5}$  ??

### **Understanding of electromagnetic particle flux**

Electromagnetic electron particle flux is given by,

$$\Gamma_{em} \approx <\delta J_{\parallel e} \delta B_r > = <\delta J_{\parallel} \delta B_r > = <\nabla_{\perp}^2 A_{\parallel} \frac{\partial}{\partial y} A_{\parallel} > = Real(\sum_{\vec{k}} ik_{\perp}^2 k_y \mid A_{\parallel} \mid^2) = 0$$

If the total parallel current is  $\delta J_{\parallel} = \delta J_{\parallel e} + \delta J_{\parallel i}$ . Then the electron flux will

$$\Gamma_{em}^{e} = \frac{1}{eB} < \delta J_{\parallel i} \delta B_{x} > -\frac{1}{eB} \frac{c}{4\pi} \frac{\partial}{\partial x} < \delta B_{x} \delta B_{y} > -\frac{1}{eB} \frac{c}{4\pi} < \delta B_{y} \frac{\partial}{\partial z} \delta B_{z} > -\frac{1}{eB} \frac{c}{4\pi} < \delta B_{y} \frac{\partial}{\partial z} \delta B_{z} > -\frac{1}{eB} \frac{c}{4\pi} < \delta B_{y} \frac{\partial}{\partial z} \delta B_{z} > -\frac{1}{eB} \frac{c}{4\pi} + \frac{1}{eB} \frac{c}{4\pi} + \frac{1$$

$$\Gamma_{em}^{e} = \frac{1}{\mathrm{eB}} < \delta J_{\parallel i} \delta B_{x} > = -\frac{\beta_{e} m_{e}}{m_{i}} n_{o} c_{e} \sum_{\vec{k}} \frac{k_{\parallel} c_{e} k_{y} \rho_{e}}{|\omega|^{2}} \delta_{k} [\gamma Im(R_{A}) + \omega_{r} Real(R_{A})] \left| \frac{e \delta \phi_{k}}{T_{eo}} \right|^{2}$$

Hence, the ratio of electromagnetic to electrostatic particle flux is obtained as

$$\frac{\Gamma_{em}^e}{\Gamma_{es}^e} \approx \frac{\beta_e m_e}{2m_i \tau_e} \times (10 \sim 100) \approx \mathbf{10^{-5}}$$

#### (Srivastav et al., Plasma Phys. Control. Fusion 61, 055010 (2019))





- Study of total flux due to fluctuations in the background of ETG turbulence leads to the study of turbulent particle flux and heat flux simultaneously.
- Since particle flux is already characterised for ETG turbulence, hence we will be measuring the heat flux.
   Conductive
   Convective
- Energy/heat flux is basically defined as

$$Q_e = \frac{3}{2} < \tilde{v}_r (n_o \tilde{T}_e + \tilde{n} T_e) = \frac{3}{2} n_o < \tilde{T}_e \tilde{v}_r > + \frac{3}{2} T_e < \tilde{n} \tilde{v}_r >$$

Heat flux (q)

- Investigation Activity for Study of heat flux can be subdivided in following category:
  - Diagnostic Development for accurate measurement of real time temperature fluctuations and Heat flux
  - ✓ Validation for  $T_e$  and  $\delta T_e$
  - ✓ Investigation of Heat flux in ETG background
  - Theoretical Estimation and its Comparison with experimental observations

Heat flux (q)





## Schematic of Probe assembly for simultaneous measurement of particle flux, $\Gamma_{es}$ and heat flux, q



**Construction** Selection of Bias voltage for  $T_e$  measurement with TLP



✓ For proper selection of fixed bias voltage  $V_{d3}$  we perform the  $T_e$  measurement for different  $V_{d3}$  and compared it with Single and Double probes measurement

✓ It is fond that the  $T_e$  measured with TLP is very close SLP and DLP measurement for 6.0V to 15.0 V i.e.  $5V_{d2} < V_{d3} > 10V_{d2}$  where  $V_{d2} \approx T_e/1.44$ T



### **Comparison of mean** $T_e$ and fluctuations with other diagnostics



Radial Comparison of Mean  $T_e$  with SLP and TLP diagnostic

Temperature fluctuation comparison of TLP and Two probe diagnostic



### Fluctuation Measurement





**Radial profile of fluctuation observed** 



### Fluctuation Characterization



**Correlation Temperature and density fluctuations with potential fluctuations** 



Power spectra, phase angle and coherency plot of Temperature fluctuations and potential fluctuations



□ Phase angle comparison with ETG turbulence

 Further justification for temperature fluctuation is done with phase angle measurement with respect to potential fluctuations



By considering ion non-adiabatic response.

Phase Angle comparison between temperature fluctuation and potential fluctuations



### Conductive heat flux and its comparison



48



(a) Radial variation of total heat fluxes and(b) Comparison of convective heat fluxes.

Electron thermal conductivity due to temperature fluctuations present in the system.



**\*** Observation shows that thermal conductivity exhibits a quadratic dependency for the normalized fluctuations for levels between 5% and 20%.



- **1. Inward particle transport due to electrostatic fluctuations is observed** (*Srivastav et al.*, *Physics of Plasmas 24, 112115 (2017)*)
  - Net particle flux results from the phase difference between the density and potential fluctuations, other than 180 degrees for ETG driven modes.
  - ii. The experimental cross phase angle and flux have been compared with the cross phase and flux resulting due to the non-adiabatic ion response due to the resonant interaction of the ions with the ETG mode  $k_{\perp}V_{thi} \sim \omega$ .
  - iii. The experiment and theoretical results quantitatively follow the same trend across the radius and match within 20% with each other.



- 2. Particle transport due to electromagnetic fluctuations is experimentally estimated observed and theoretical model is proposed (*Srivastav et al.*, *Plasma Phys. Control. Fusion 61, 055010 (2019)*)
- i. Theory for particle flux due to electromagnetic fluctuation is developed and we found the ratio of electromagnetic flux to electrostatic flux is in agreement with our experimental findings in ETG background .
- ii. Experimentally obtained ion flux values agrees well with numerically obtained values using theoretical model of electromagnetic flux.
- iii. Non-ambipolar EM flux is observed at R=40 cm which may be one cause of change in potential profile at R=40cm that leads us to create a shear flow in poloidal direction.



## **Summary & Conclusion**

3. Heat transport due to electrostatic fluctuations is measured and compared with theoretical model

#### (Srivastav et al., Physics of Plasmas 26, 052303 (2019))

- Mean temperature measurements using TLP are validated with SLP and temperature fluctuation is validated by two probe technique before applying for real time temperature fluctuations.
- ii. Radial measurement of phase angle is supported by theoretical model of ETG turbulence for  $R \le 50$  cm.
- iii. Radial measurement of heat flux is obtained by simultaneous measurement of fluctuations in  $T_e$  and  $\phi_f$  which is in good agreement with theoretical estimations.



### **Summary & conclusion**





### Acknowledgement



#### Collaborators



**Dr. Lalit Mohan Awasthi** Scientific Officer – G, Head of LVPD



**Dr. Amulya Kumar Sanyasi** Scientific Officer - D



**Prof. Raghvendra Singh** Senior Professor (Retired) Senior Researcher, NFRI, Republic of Korea



**Mr. Pankaj Kumar Srivastava** Scientific Officer - D





**Dr. Ritesh** Sugandhi Scientific Officer - F

**Dr. Rameshwar Singh** Postdoctoral Researcher — University of California San Diego

# Thank you for your kind attention



### **Diffusion of electrons across magnetic field of EEF**

**Cold Electrons :** 

$$T_e \sim 1.0 \ eV, \quad n_e \sim 3 \times 10^{11} cm^{-3}, B = 160 \ Gauss$$

$$v_{ei} = n_i \sigma v_e = 1.3 \times 10^7 \ s^{-1}, \quad \lambda_f^c \sim 3 cm$$
Avg. dis. ~ 600 cm, suffers 200 collisions
$$\rho_{ec} \sim 0.015 \ cm, \quad Perp. \ dis. \ by \ cold \ electron \sim 3 cm$$

#### **Hot Electrons**

 $T_{e} \sim 23 eV \qquad v_{en} = n_{n} \sigma v_{e} = 1.0 \times 10^{6} s^{-1}, \ \lambda_{f}^{h} = 200 cm$   $Avg. \ dis. \sim 600 cm, \ suffers \ 3 collisions$   $\rho_{eh} \sim 0.08 \ cm \ Perp. \ dis. \ by \ hot \ electron \sim 0.24 cm/s$ 

• Since majority of the experimental studies shows that the floating potential fluctuation measurement with conventional Langmuir probe can be approximated with plasma potential fluctuation measurement as

$$\varphi_{pl} = \varphi_{fl} + \mu \frac{T_e}{e}$$

For fluctuation

$$\tilde{\varphi}_{pl} = \tilde{\varphi}_{fl} + \mu \frac{\tilde{T}_e}{e}$$

In absence of temperature fluctuations

$$\tilde{\varphi}_{pl} = \tilde{\varphi}_{fl}$$

So, poloidal electric field fluctuation can be calculated with floating potential fluctuations.

Hence, in presence of temperature fluctuation, above relation can't be considered as accurate

# $\hfill \hfill \hfill$



Emissive Probe assembly to measure particle flux with plasma potential fluctuation along with ion-saturation fluctuation with conventional Langmuir probe[ Diameter =0.2 mm, Length=10mm]

Triple Probe assembly to measure particle flux with floating potential fluctuation measurement[ Diameter =0.5mm, Length=10mm]

### □ Validation of Plasma Potential measurement: Varying Heating current

- □ The floating potential measurement with  $\geq 2.0$  Amp heating current shows no significant change.
- Implies heated filament works as emissive probe as it floats now at plasma potential.

✓	At	I <sub>emissive</sub>	$\approx$	2.1	A	mp,	we	
	measured		plasma		a	potential		
	fluctuation		fo	r	particle		flux	
	estir	nation.						



### Comparison Plot for Electrostatic particle flux estimated with floating potential fluctuation ( $\delta \phi_f$ ) and plasma potential fluctuation ( $\delta \phi_p$ )



\* No significant deviation is observed in particle flux measurement with  $\phi_p$  and  $\phi_f$ fluctuation measurement.

This is only possible when Temperature fluctuations are completely cancels out in poloidal electric field fluctuation calculations.

Particle flux measured with floating potential fluctuation and plasma potential fluctuation for comparison.