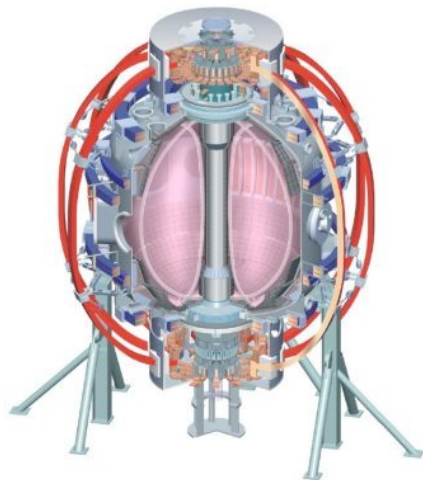


# Optimization and Utilization of Beta-Control

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**NSTX 2010 Research Forum  
MS TSG Breakout Session  
Dec. 1<sup>st</sup>, 2009**

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# Overview

- Background
  - Rudimentary PCS control of NB injection was shown in 2008.
  - $\beta_N$  control was demonstrated in 2009.
    - Not “tuned up”.
  - Improved rtEFIT basis vectors were implemented at the very end of the 2009 run.
- Goals of Proposed XP:
  - Achieve reasonable values of the parameters in the  $\beta_N$  control algorithm.
  - Test the ability of  $\beta_N$  control to enable non-disruptive operation near the  $\beta_N$  limit.
- Contributes to:
  - MS Milestone R(10-1): Assess sustainable beta and disruptivity near and above the ideal no-wall limit.

# Implementation of $\beta_N$ Control in NSTX

- Compare **filtered**  $\beta_N$  value from rtEFIT to a request, and compute an error.

$$e = \beta_{N,request} - LPF(\beta_{N,RTEFIT}; \tau_{LPF})$$

- Use **PID** on the error to compute a new requested power.

## 2009 PID Algorithm

$$\Delta P_{inj} = P_{\beta_N} \bar{C}_{\beta_N} e + I_{\beta_N} \bar{C}_{\beta_N} \int e dt + D_{\beta_N} \bar{C}_{\beta_N} \frac{de}{dt}$$

$$P_{inj,i} = P_{inj,i-1} + \Delta P_{inj}$$

$$\bar{C}_{\beta_N} = \tau \frac{I_P V B_T}{200 \mu_0 a} \cdot \frac{dt}{0.001}$$

## 2010 PID Algorithm (?)

$$P_{inj} = P_{\beta_N} \bar{C}_{\beta_N} e + I_{\beta_N} \bar{C}_{\beta_N} \int e dt + D_{\beta_N} \bar{C}_{\beta_N} \frac{de}{dt}$$

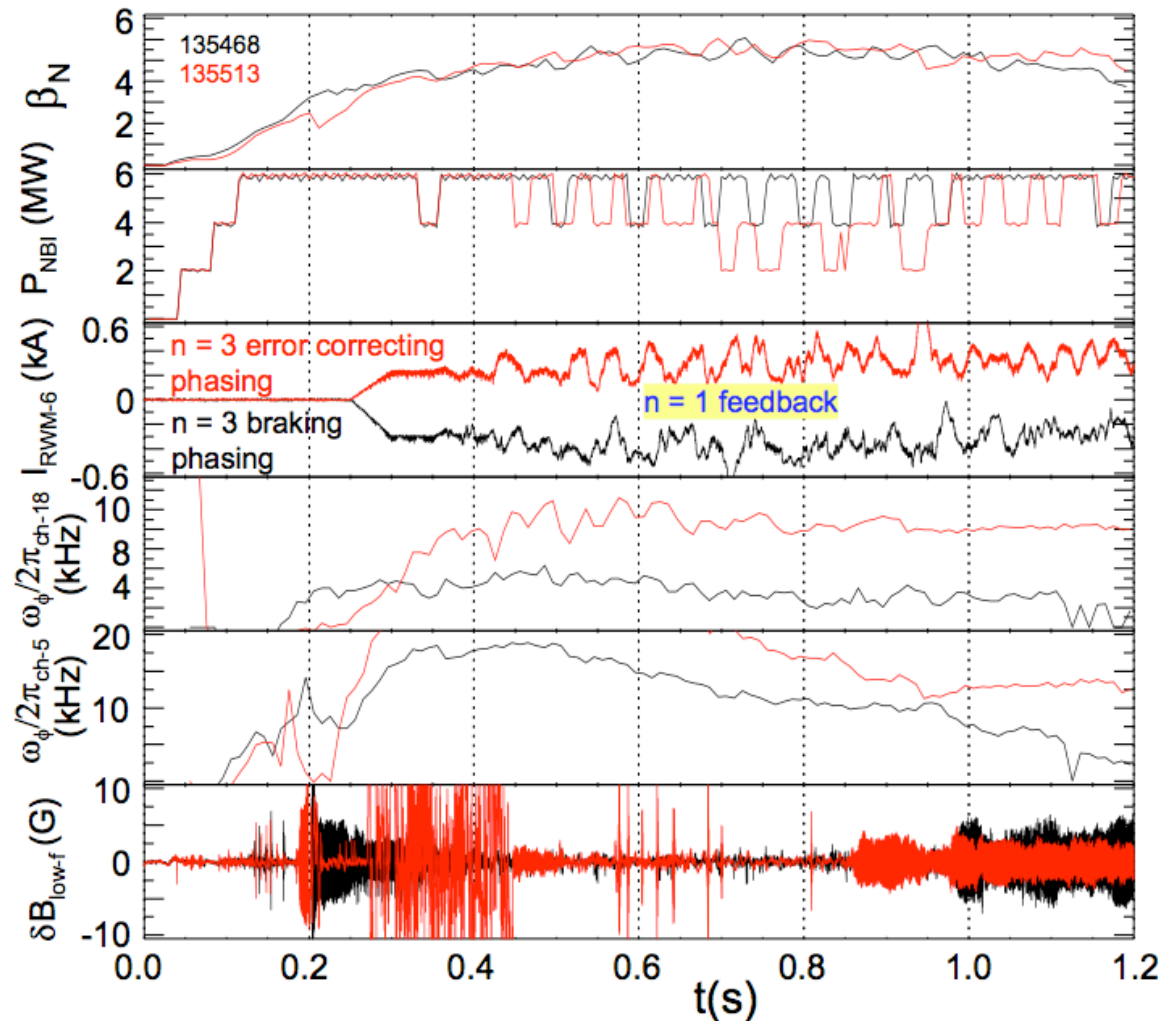
$$\bar{C}_{\beta_N} = \tau \frac{I_P V B_T}{200 \mu_0 a} \cdot \frac{dt}{0.001}$$

- Use power from the PID operation, **source powers**, and “**batting order**” to determine the duty cycles for each source.
- Use the duty cycles and **min. on/off times** to determine when to block.

## Many Available Adjustments

- Filter time constant on the  $\beta_N$  value sent from rtEFIT.
  - Useful for smoothing transients in the measured  $\beta_N$ .
- Proportional, integral, and derivative gains.
  - Determines the response of the system to transients.
- Batting order array.
  - Determines which sources modulate
  - Switch to a different source if a given source reaches the maximum number of blocks.
  - Also able to prevent A modulations, to keep MSE and CHERS.
- Source powers
  - Can be adjusted in order to prevent modulations.
- Minimum Source On/Off Times.
  - Smaller values will lead to better control, but possibly at the expense of source reliability.
  - 20 msec. has seemed OK so far.

# $\beta_N$ Control Has Been Demonstrated in 2009



- $\beta_N$  algorithm compensates for loss of confinement with  $n=3$  braking.
- Control works over a range of rotation levels.
- Goal of XP is to optimize the system.

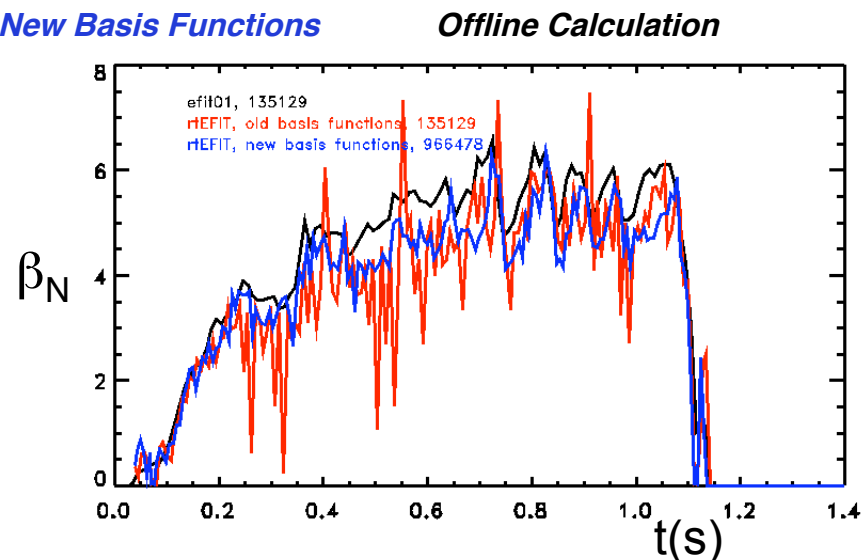
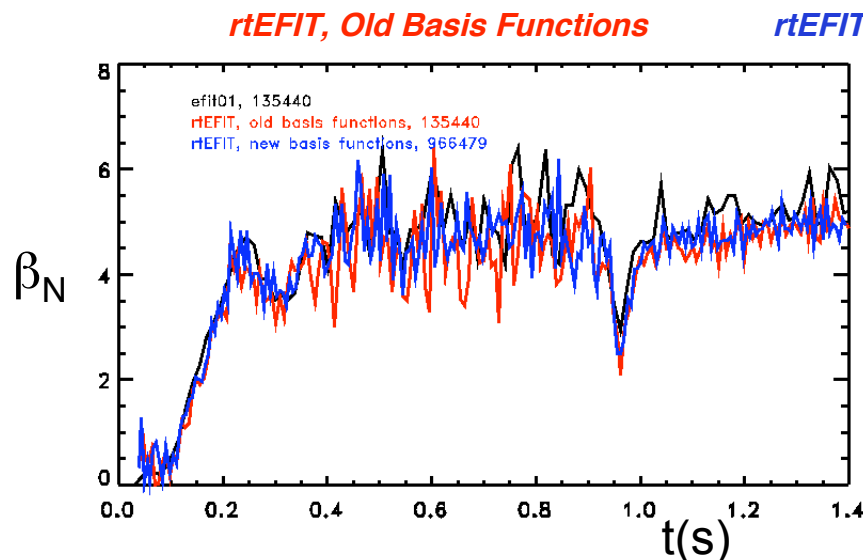
S.A. Sabbagh, 2009 NSTX Results Review

# Modifications to the rtEFIT Basis Functions Resulted in Improved Real-time Reconstructions

- Occasional poorly converged equilibria lead to incorrect outer gap,  $\beta_N$ 
  - Kick off an deleterious transient in the vertical field coil current.
  - Edge current not allowed
- New basis function model based on those developed for off-line magnetics-only reconstruction (Columbia University)
  - Tested on literally > 2 million equilibria
  - Finite edge current through  $ff'(\psi_n)$
- Considerable real-time reconstruction improvement
  - Reduction in  $\beta_N$  “noise” indicative of improved reconstructions

$$p'(\psi_n) = a_1 \psi_n (1 - \psi_n)$$

$$ff'(\psi_n) = b_0 + b_1 \psi_n \left(1 - \frac{1}{3} \psi_n^2\right) + b_2 \psi_n^2 \left(1 - \frac{2}{3} \psi_n\right)$$



*Improvement made on 2nd to last day of run...we should take advantage of it this year.*

## Simple Model For NB Heating

- Coupled equations for the stored energy in thermal particles and fast particles.

$$\frac{dW_{th}}{dt} = \frac{W_f}{\tau_f} - \frac{W_{th}}{\tau_{E,th}}$$

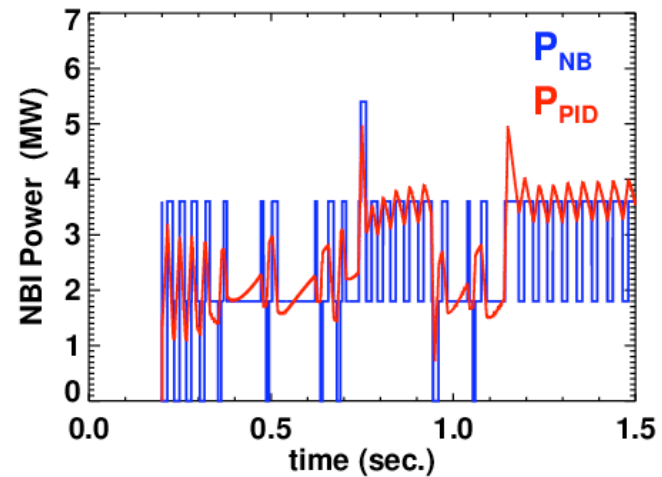
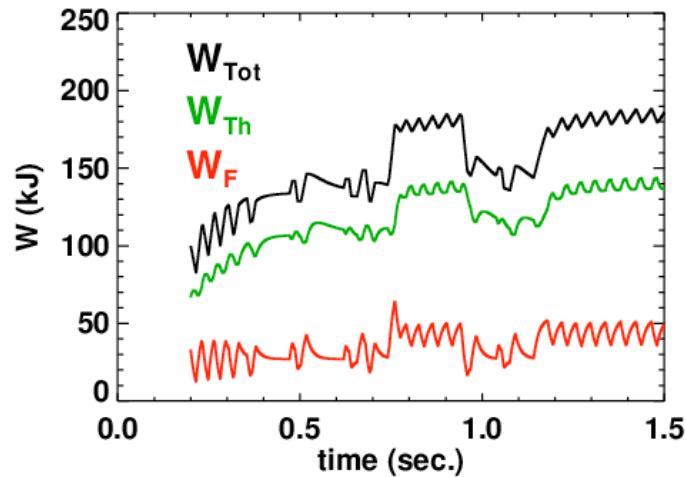
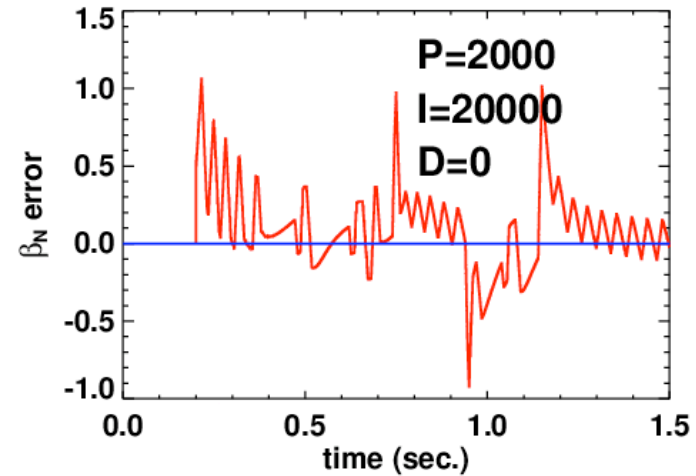
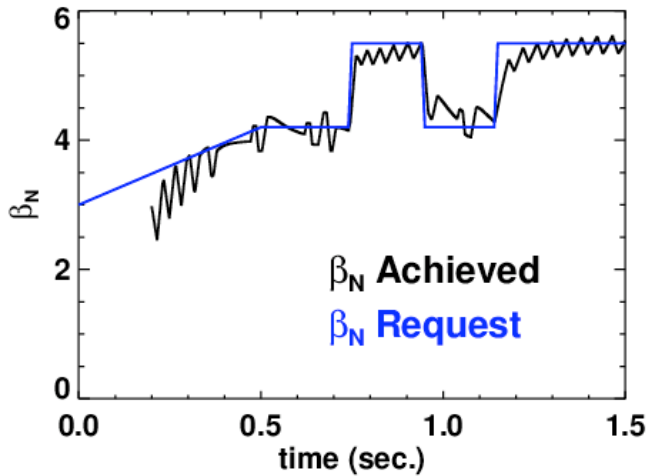
$$\frac{dW_f}{dt} = P_{inj} - \frac{W_f}{\tau_f}$$

$$\tau_{E,th} = \tau_{E,0} \left( \frac{4 \times 10^6}{P_{inj}} \right)^{p_{exp}}$$

$$W = W_{th} + W_f$$

- Two free parameters in model:
  - Time-scale for thermal energy loss:  $\tau_{E,th}$
  - Time-scale of energy transfer from fast to thermal particles:  $\tau_f$
- Compute these parameters using beam modulations and TRANSP
- Simple model designed for control.
  - No direct fast-ion loss.
  - Collapse thermal electron and ion energy loss rates into a single parameter.
- Tune the model parameters ( $\tau_f$ ,  $\tau_{E,th}$ ,  $p_{exp}$ ) with TRANSP.
- Use model in a feedback simulation to get gains correct.

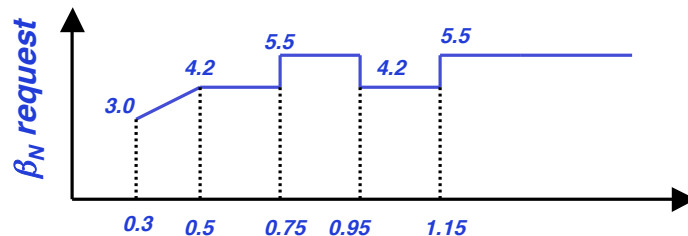
# Example: Proportional And Integral FB, Modulating All Sources



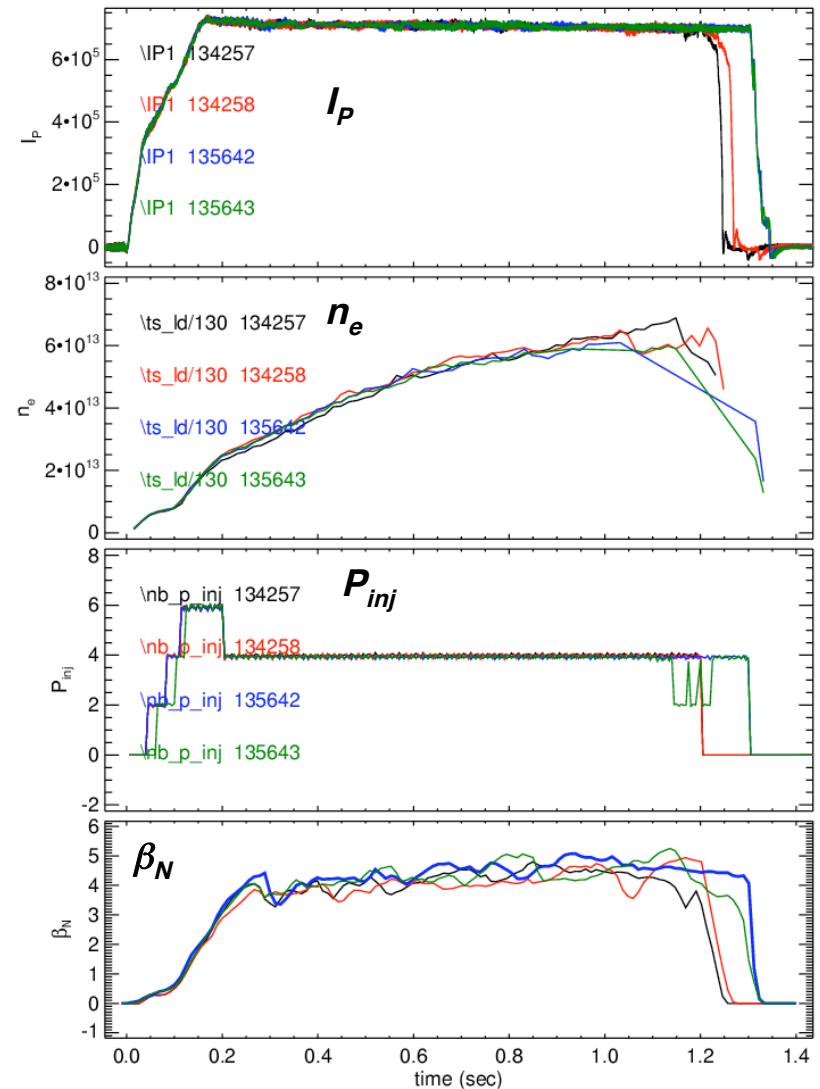


# XP Plan: Algorithm Optimization (1/2 day)

- Establish a high-performance reference.
  - Should be long pulse at 4 MW, to allow room for modulations.
  - Consider 700-800 kA fiducial.
- Add in  $\beta_N$  control with reasonable parameters, step in  $\beta_N$  request.
- Adjust gains to achieve best match to desired waveform.
- What min on/off times to use?
  - 20/20 was used last year.
- Use full RWM control.



Potential Target: Long Pulse 700 kA with Fiducial Shape.



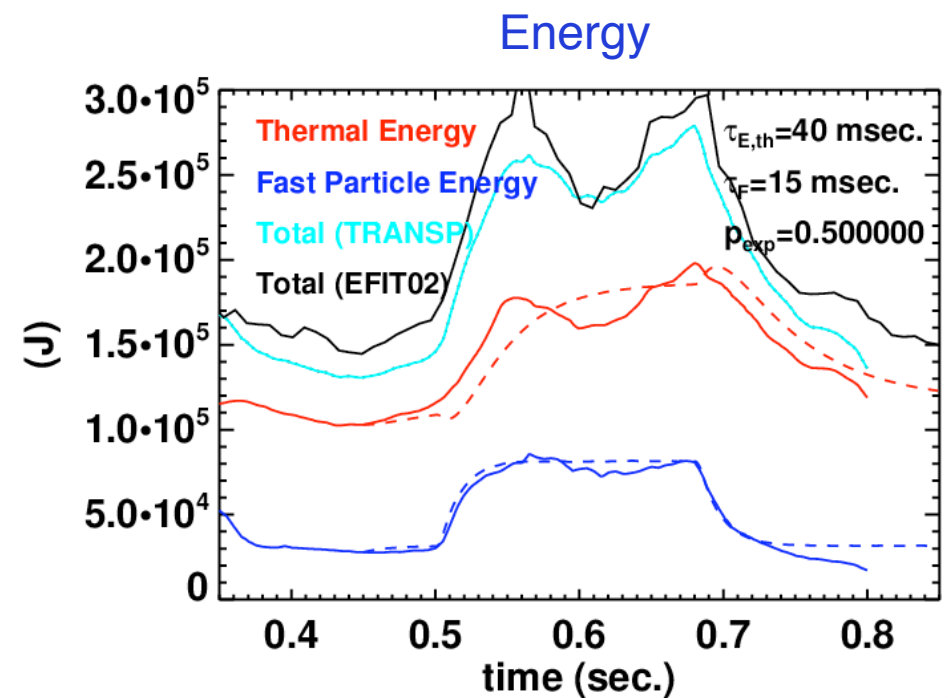
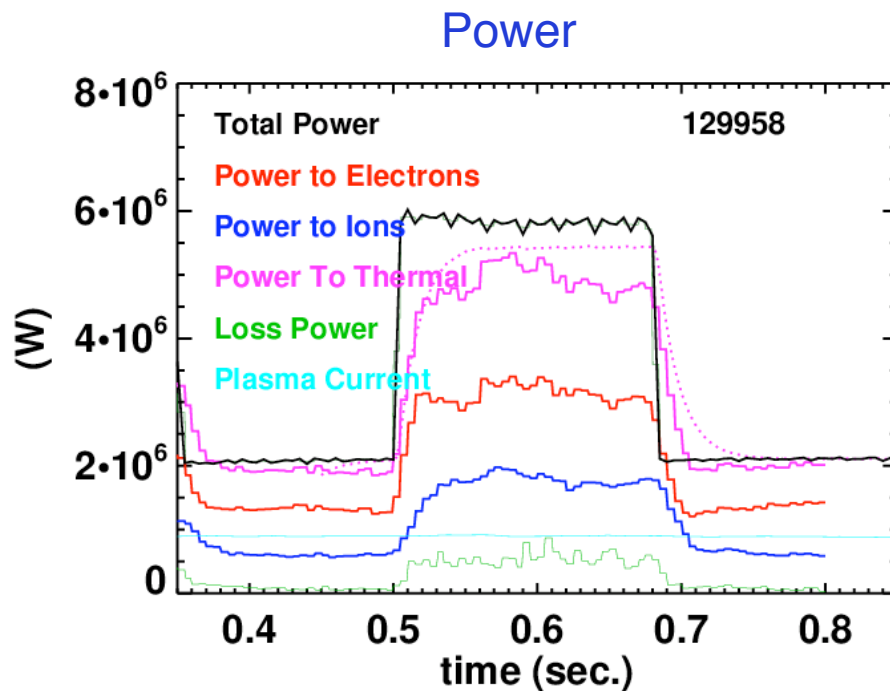
## XP Plan: Test For Disruptivity Reduction (1/2 day)

- Establish a discharge regime that disrupts with a 6 MW of input power.
  - Maybe just use the previous 700 kA target?
- Re-run with  $\beta_N$  request reasonably below the disruptive value.
  - Should not disrupt any more
- Increase the  $\beta_N$  request in small increments to where it disrupts.
  - Bracket the unstable heating power.
- Adjust the source voltage to achieve approximately the same waveforms.
  - These are pre-programmed
  - Re-run and see if the level of  $\beta_N$  fluctuations is increased, disruptions re-appear.
- Status of RWM Control?
  - Inclined to use slow control (DEFC), but not fast feedback.
  - Provides test of disruption control in the wall-stabilized regime.

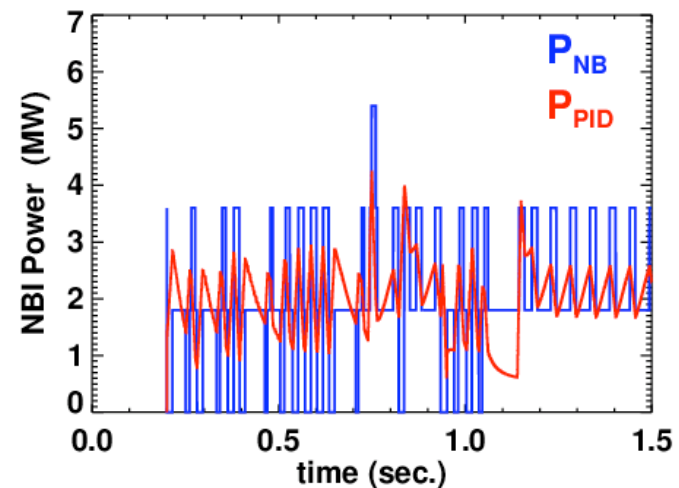
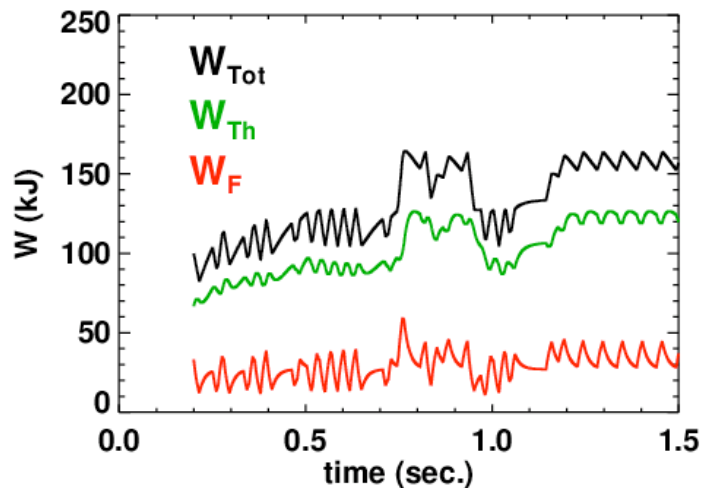
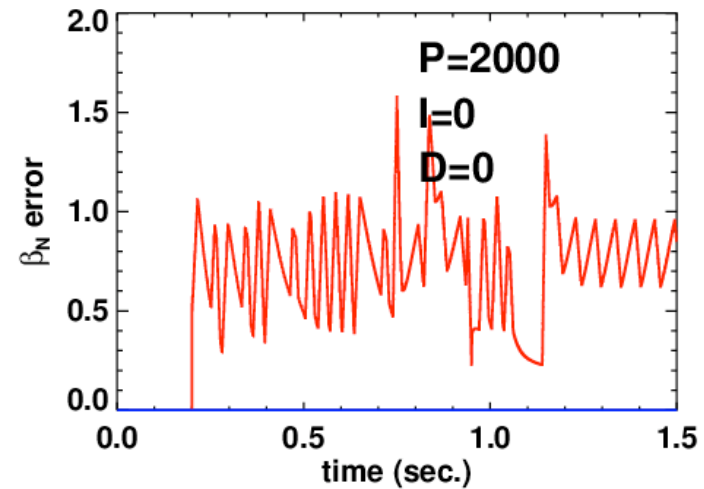
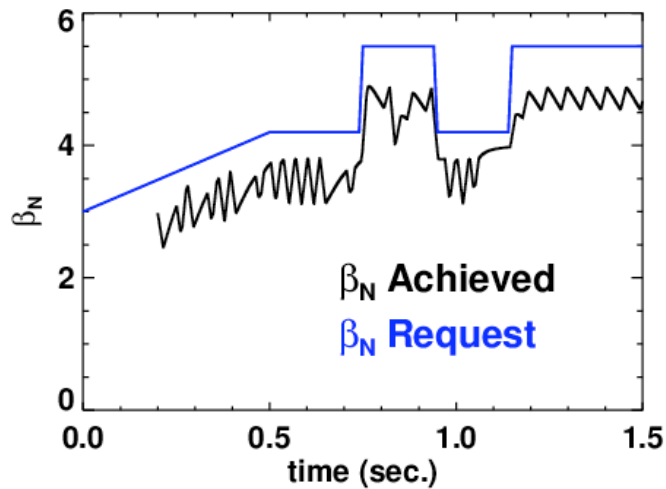
# Backup

## Example of Model

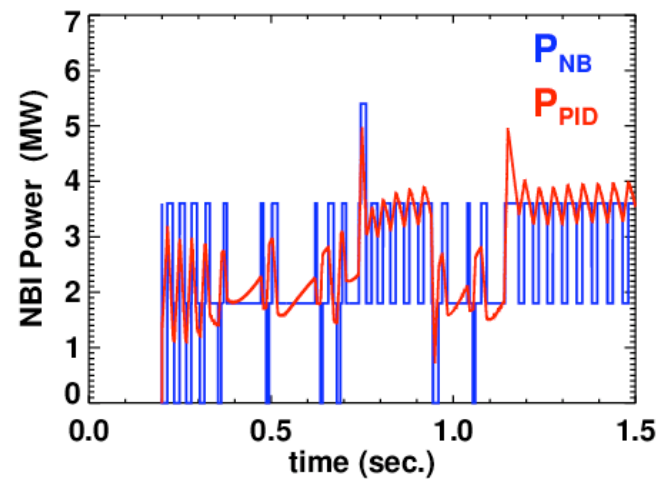
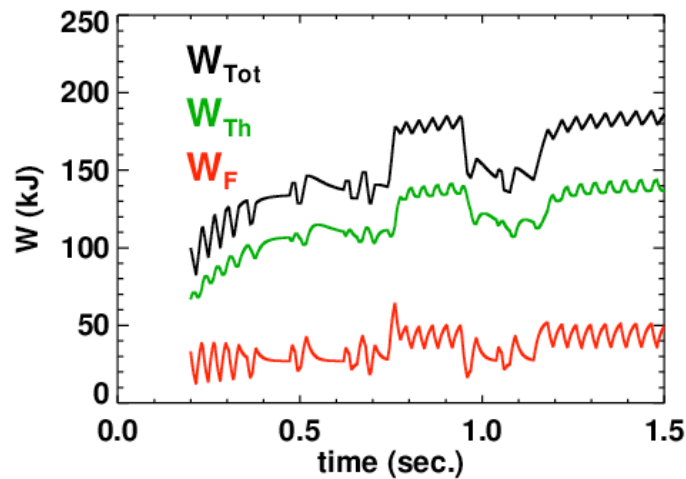
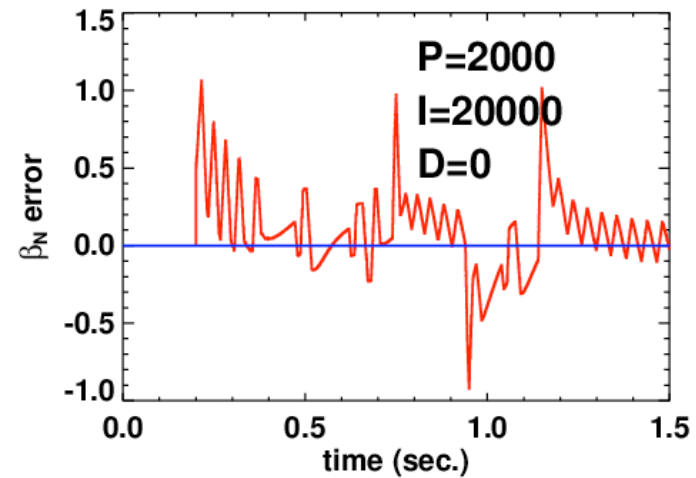
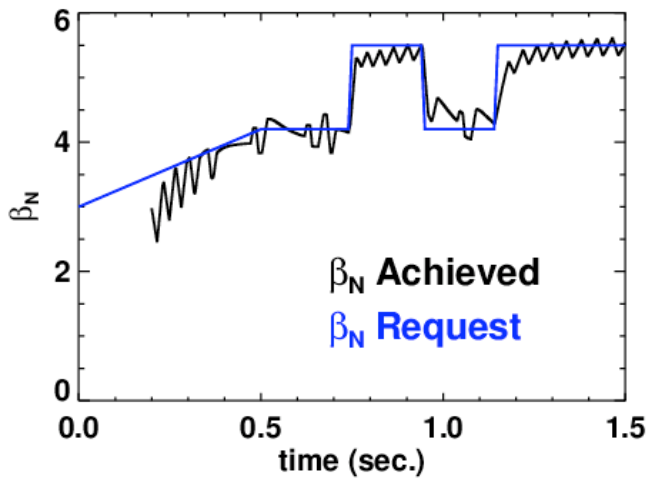
- Solid: TRANSP Quantities
- Dashed: Model
- 900 kA fiducial like discharge



# Simulation #1: Proportional FB Only, Modulating All Sources



# Simulation #2: Proportional And Integral FB, Modulating All Sources



# Simulation #3: Proportional And Integral FB, Modulating B & C Only

