

# Stress Multipliers for the NSTX Upgrade Digital Coil Protection System

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**Abstract**—Conceptual design of the upgrade to NSTX, explored designs sized to accept the worst loads that power supplies could produce. This produced excessive structures that would have been difficult to install and were much more costly than needed to meet the scenarios required for the upgrade mission. Instead, the project decided to rely on a digital coil protection system (DCPS). Initial sizing was then based on the 96 scenarios in the project design point with some headroom to accommodate operational flexibility and uncertainty. This has allowed coil support concepts that minimize alterations to the existing hardware. The digital coil protection system theory, hardware and software are described in another paper at this conference. The intention of this paper is to describe the generation of stress multipliers, and algorithms that are used to characterize the stresses at key areas in the tokamak, as a function of either loads calculated by the influence coefficients computed in the DCPS software, or directly from the coil currents.

**Keywords**—component; NSTX; Influence Coefficients; Poloidal Field Coils (*key words*)

## I. INTRODUCTION

Two approaches are used to provide the needed multipliers/algorithms. The first is to use the loads on PF coils computed by the DCPS software and apply these to local models of components. This works well for coil supports and for uniformly supported coils. It is usual practice to utilize influence coefficient calculations to determine hoop and axial (vertical for tokamak's) loads from coil currents. However the centroid of the Lorentz loads may not be at the geometric center of the coils. Where there is significant offset between the Lorentz centroid and the geometric center, there will be a moment about the coil geometric center in addition to the net loads. This may be a significant contributor to the support reaction loads and to the stresses in the coils. In design and analysis of coil systems, distributions of fields and forces are typically calculated for a useful structural/magnetic mesh which is typically fine enough to properly distribute the Lorentz forces and resolve any moments about the coil current centers. When influence coefficients are used in control systems, for operating tokamaks, to check coil stresses and support loading, the effect of moments has been omitted. To the author's knowledge, this is true of Alcator C-Mod, TFTR and NSTX. Addition of the moment coefficients completes the three degrees of freedom available from the axisymmetric analysis of ring coils.

The second approach to calculating the stress multipliers/algorithms, is to utilize a global model that simulates the whole structure and includes an adequately refined modeling of the component in question. Unit terminal currents are applied to each coil separately, Lorentz Loads calculated, and the response of the whole tokamak and local component stress is computed. For superposition to work, stress multipliers must be computed for specific locations and individual stress components (not equivalent, von Mises, or Tresca) must be calculated. Results for two components are presented after the discussion of moment coefficients.

## II. COMPUTATION OF INFLUENCE COEFFICIENTS INCLUDING MOMENT COEFFICIENTS

### A. Utility of Moment Coefficients

Addition of Moment Influence Coefficients to DCPS

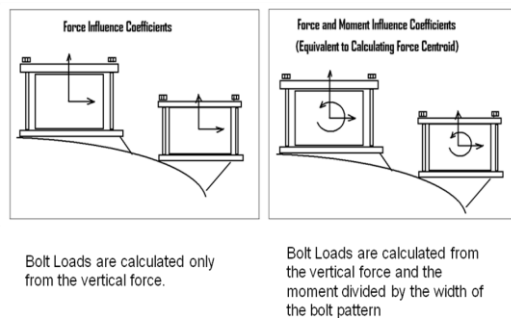


Figure 1. Representation of Applied Forces and Moments on Coils

In the example in figure 1, at left, the retainer bolts would simply be stressed by the vertical loading, and at right the bolts would see the vertical load plus a force equal to the moment divided by the clamp bolt spacing. Obviously more complex structural interactions are possible, and for the coil aspect ratios shown, there will not be a large difference between the current and geometric centers. Other coil shapes and magnetic configurations may see larger effects from calculated moments. For NSTX Upgrade the inner PF coils are effected significantly by moments.

B. The Analysis Code

Mesh generation , calculation of the Lorentz forces, and generation of the influence coefficients is done using a code written by the author of this report. The mesh generation feature of the code is checked visually and within ANSYS during the PREP7 geometry check. . The authors code uses elliptical integrals for 2D field calculations, and Biot Savart solution for 3D field calculations. These are based 2D formulations, and single stick field calculations from ref.R [1] with some help from R. Pillsbury's FIELD3D code to catch all the coincident current vectors, and other singularities.

The code in various forms has been used for 20 years and is suitable for structural calculations. It is also being used for calculation of load files in an NSTX global model[9]. Recent checks include NSTX out-of-plane load comparisons with ANSYS [10] and MAXWELL and calculations of trim coil fields for W7X compared with N. Pomphrey's calculations. Some information on the code, named FTM (Win98) and NTFTM2 (NT,XP), is available at: <http://198.125.178.188/ftm/manual.pdf> . or, within PPPL: at P:\public\Snap-srv\Titus\NTFTM

C. The Axisymmetric Model

The influence coefficient methodology allows choice of coil groups or partial coil groups with which to construct the influence coefficient matrices. This also allows odd shaped coil segments or shaped or shifted plasmas that are treated simply as another coil group by the program. Computation of influence coefficients is done by computing contributions of fields and forces in one element group with respect to other element groups. The element groups are identified by member element real constant numbers. For this paper, the element designations used by R. Hatcher's calculation [2] have been used to allow a comparison with other calculated force influence coefficients..

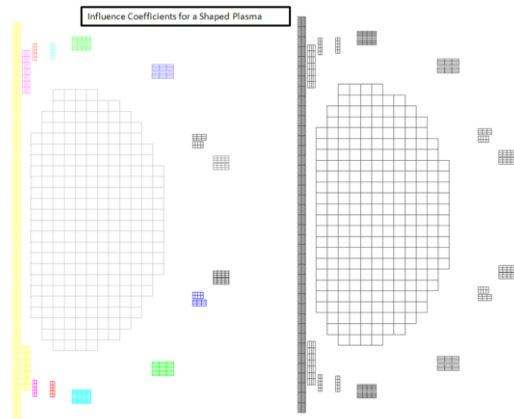


Figure 2. Axisymmetric Model Used to Compute Influence Coefficients. At Left, Colors Represent Real Constant Assignments

Moment coefficients require the computation of the force contributions with a running summation of forces multiplied by the element force times the appropriate radial or axial lever arm

with respect to the element group centroid. Computation of the moment influence coefficients also produces the force influence coefficients. Figure 2 shows a coil and plasma mesh used for computation of the influence coefficients tabulated in this paper. Two plasma shapes have been investigated a rectangular cross section and a shaped plasma. The shaped plasma is shown in figure 2. Tabulated influence coefficients are for the rectangular plasma.

	(cm)	(cm)	(cm)	(cm)						
OH (half-plane)	24.2083	6.934	106.04	212.08	4	110	442	0.701		
PF1a	32.4434	6.2454	159.06	46.3296	4	16	64	0.825		
PF1b	40.038	3.36	180.42	18.1167	2	16	32	0.794		
PF1c	55.052	3.7258	181.36	16.6379	2	10	20	0.856		
PF2a	79.9998	16.271	193.3473	6.797	7	2	14	0.741		
PF2b	79.9998	16.271	185.26	6.797	7	2	14	0.741		
PF3a	149.446	18.644	163.3474	6.797	7.5	2	15	0.693		
PF3b	149.446	18.644	155.26	6.797	7.5	2	15	0.693		
PF4b	179.4612	8.1542	80.7212	6.797	2	4	8	0.753		
PF4c	180.6473	11.527	88.8086	6.797	4.5	2	9	0.672		
PF5a	201.2796	13.533	65.2069	6.858	6	2	12	0.773		
PF5b	201.2796	13.533	57.8002	6.858	6	2	12	0.773		

Figure 3. Coil Builds for NSTX Upgrade

Coil builds for the NSTX Upgrade are shown in Figure 3. In the table at left. At right, the commands used to apply the unit currents are shown. In this case one kiloamp is the unit current, but 250 amps is input because subsequently the mesh density is increased by a factor of 4.

D. Results

A full set of force and moment influence coefficients are included near the end of this paper.

E. A Test Case

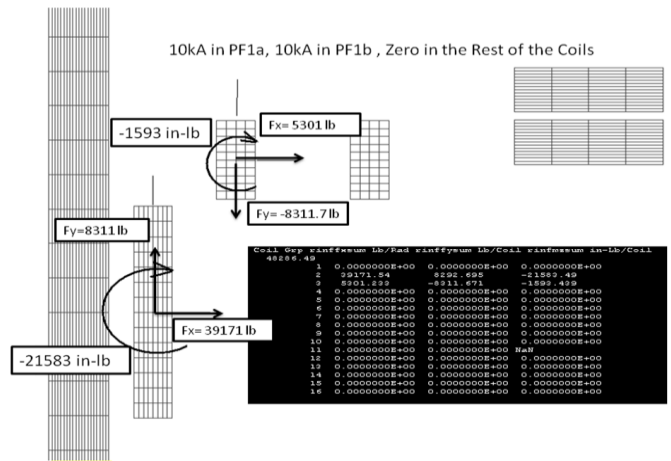


Figure 4. Upper Inner Corner of the NSTX Poloidal Field Coil Array

For NSTX the effect of the moment coefficients is small for the compact ring coils but is interesting for the thin solenoids - the OH and PF1a,b, and c. In Figure 4, The upper inner portion of the NSTX PF coil array is shown This includes an upper segment of the tall thin OH and PF1 a,b and c. The staggered coils will develop current centers that aren't coincident with their geometric centers. For the case with

10kA in PF1a and 10kA in Pf1b, the forces and moments are shown.

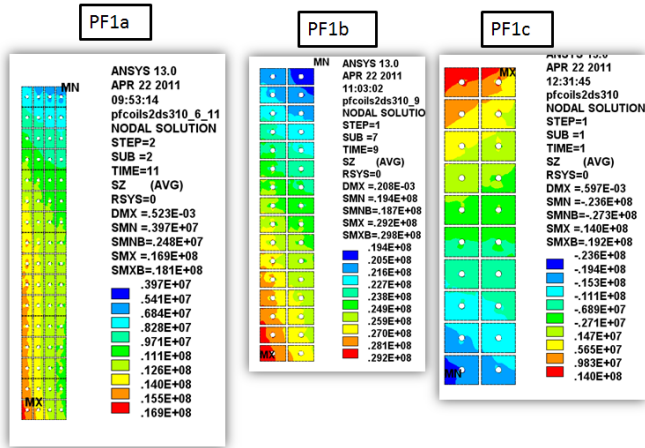


Figure 5. Inner PF Coil Results from [6]

Stress analysis of the inner PF coils performed for NSTX upgrade showed a strong variation in the vertical distribution of hoop stress in PF 1a and b similar to the behavior shown in the test case. Figure 5 shows some results from the qualification of the inner PF coils, in [6]

TABLE I. EXCERPT FROM THE SHAPED PLASMA MOMENT INFLUENCE COEFFICIENTS

	OH	PF1AU	PF1bU	PF1cU	PF2U	PF3U	PF4U		
OH	1	0.00E+00	-20165.7	-9837.4	-5246.08	-5607.03	-3893.17	-1291.17	
	PF5U	PF1AL	PF1bL	PF1cL	PF2L	PF3L	PF4L	PF5L	Ip
	-1209.61	20165.75	9837.401	5246.083	5607.024	3893.168	1291.17	1209.613	1.582384

The largest moment influence factors are for moments on the OH from PF1aU and L currents as might be expected from the coil geometries. The effect on the outer ring coils is minimal. The results of this calculation were compared with R. Hatchers results for the 2009 coil builds and with R. Woolley's calculations for the 2011 coil builds. The comparison with Wooley's moment coefficients show results typically within 2 to 5 % with two outliers at 8%, and large difference ratios when the two analyses are both calculating essentially zero factors.

### III. TF INNER LEG STRESS INFLUENCE COEFFICIENTS USING THE TOKAMAK GLOBAL MODEL RESULTS WITH UNIT CURRENTS APPLIED

#### A. Methodology

Out-of-Plane (OOP) loads on a toroidal field (TF) coil system result from the cross product of the poloidal field and toroidal field coil current. Support of OOP loads is statically indeterminate, or multiply redundant, requiring an understanding of the flexibility of the outboard structures and the inboard

stiffness of the central column. There are a number of ways in which the torsional shear stress in the inner leg of the TF can be calculated. The global model is the primary tool for this computation. A single TF cyclic symmetry model was investigated to see if the inner leg OOP forces alone dominate and if the outer structures could be ignored. This turned out not to be the case. This means that the global torsional stiffness's of all the tokamak structures, the umbrella structure, it's proposed upgrade reinforcements, the port region stiffness, the top and bottom spoked lid assembly stiffness, and the pedestal stiffness, all will have some effect on the inner leg torsional shear.

The global model was run with full TF current and 1000kA of current in each PF coil. The influence coefficients are based on 1 kA, but it was expected that TF loading might overwhelm the loads from individual smaller coils. The model is linear and the stress due to the PF loads should be fully scalable by current. The influence coefficients are corrected in the spreadsheet. The force calculations are computed and applied to the global model. The torsional shear in the upper, middle, and lower inner leg were then determined from each of the 16 load cases that resulted.

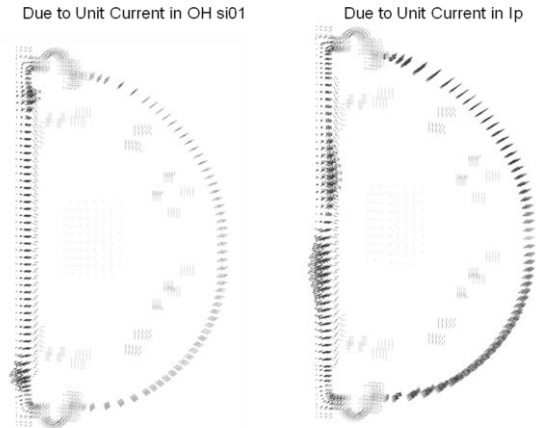


Figure 6. Detailed Model of PF4/5 with Equatorial Plane Symmetry

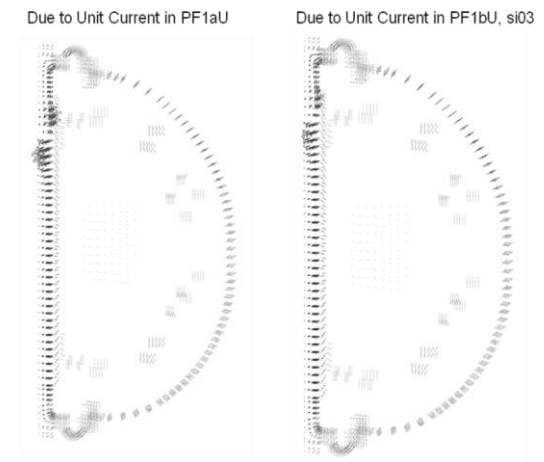


Figure 7. PF5 "Smeared" Coil Bending Stress.

**B. Results**

Based on the DCPS influence coefficient TF inner leg upper corner torsional shear, for all 96 June 3 2010 scenarios are all below 20 MPa with and without plasma. Rigorously these should have the 10% headroom applied (the coefficients do not include this) - Consequently, the torsional shear stress to compare with the allowable is 22 MPa. Acceptable results from testing the CTD-101K/Cyanate Ester primer system[7], Indicate that the torsional shear is acceptable. Influence coefficients for the DCPS algorithm have been generated based on the global model [2].

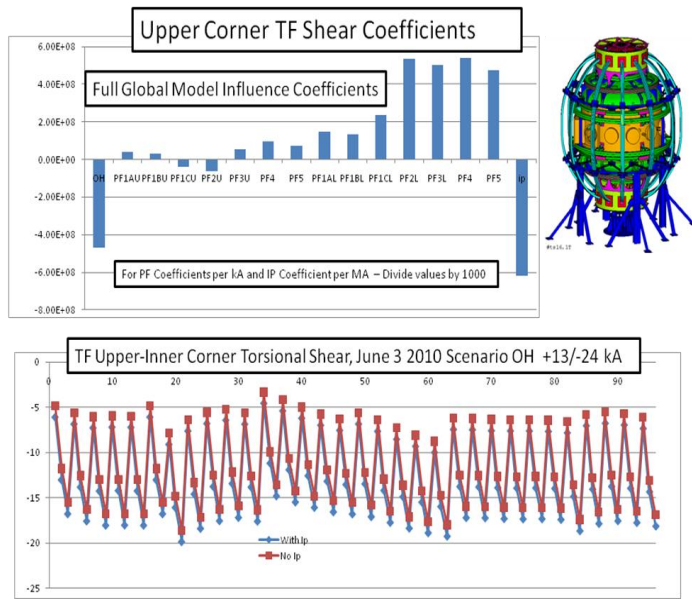


Figure 8. Upper TF Torsional Shear Stress Multipliers and Results for the Project's 96 Equilibria, with and without plasma

**IV. COMPUTATION OF PF CONDUCTOR HOOP STRESS STRESS MULTIPLIERS**

**A. Approach for Calculation PF Stress Multipliers**

The approach used for the PF4 and 5 coils for calculating the stress multipliers/algorithms is to utilize a global model (same as shown for the TF torsional shear coefficients) that simulates the whole structure and includes an adequately refined modeling of the component in question. As in the TF torsional shear stress multipliers, a limited number of sections must be identified from an understanding of the results for likely critical locations. This is done by evaluating results for the 96 design scenarios for NSTX.

**B. PF5 Hoop Stress Multiplier**

Unit terminal currents are applied to each coil separately, paired with PF5 Lorentz loads are calculated, and the response of the whole tokamak and local component stress is computed. Figure 10 shows a Biot Savart computation with unit loads in PF4 and 5.

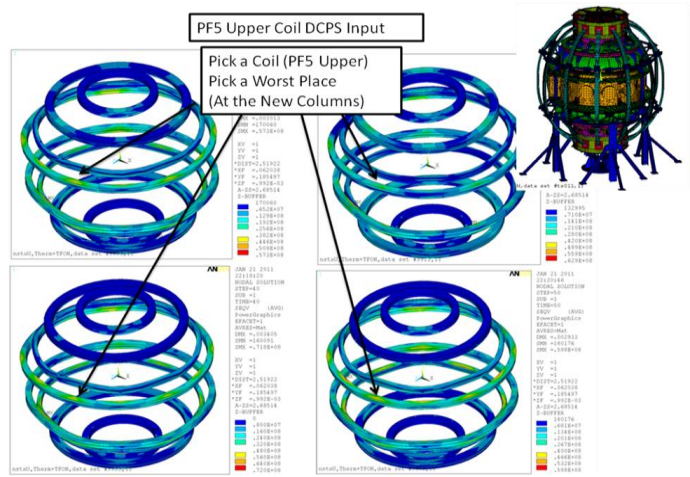


Figure 9. "Smearred" PF Coil Bending Stress From the Global Model.

This approach is correct for stresses that are a consequence of an individual coil load which is in turn a result of the superposition of contributions from all other coil currents. Local component stresses may then be computed in the DCPS or in a spreadsheet for the many scenarios required by the GRD. This approach has been applied to the PF4 and 5 coil stress. Where a component stress is a consequence of multiple coil loads, the approach must derive coefficients from unit loads which in turn are computed from the influence coefficients.

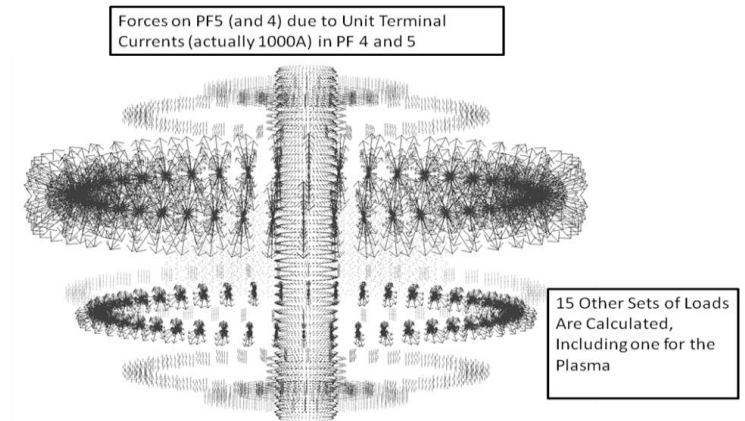


Figure 10. Lorentz Loads for a Unit Terminal Currents for PF4 and 5

Figure 8 shows the Lorentz forces for the interaction between PF4 and 5 with unit currents. Loading for interactions between PF 5 and the rest of the 16 coil set that defines the NSTX poloidal coil system are computed.

C. Identify the Headings

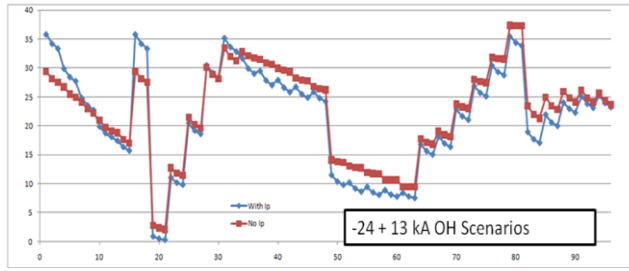


Figure 11. PF5 "Smeared" Coil Bending Stress.

"Smeared" results are determined from the influence coefficients. A more detailed model is used to calculate the local stress in the conductor and insulator. The load case in the detailed model is the full current in PF4 and 5 and is up-down symmetric. This must be used to estimate the local stresses for 96 designs scenarios, and operational currents in the DCPS.

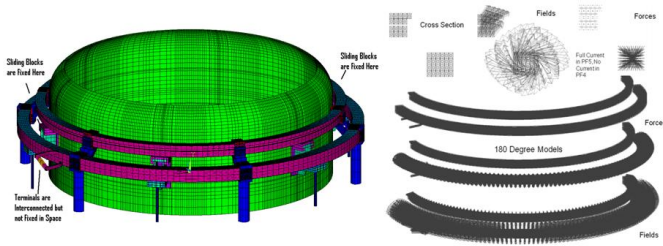


Figure 12. Detailed Model of PF4/5 with Equatorial Plane Symmetry

To form a basis of comparison between the influence coefficient calculations based on "smeared" results, and the detailed model, the influence coefficients were applied to the PF 4/5 up-down symmetric analysis used for the detailed model.

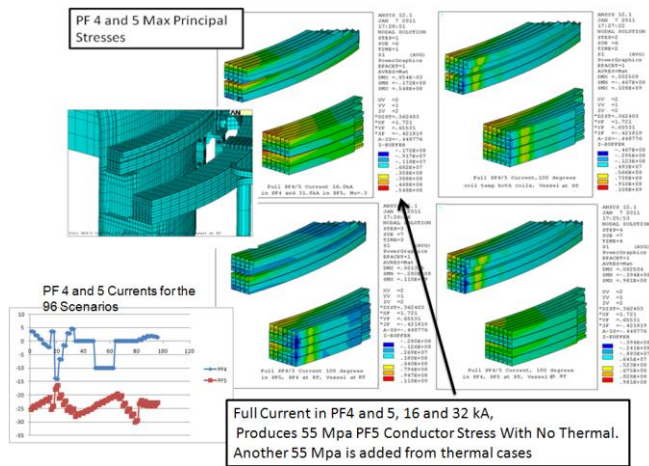


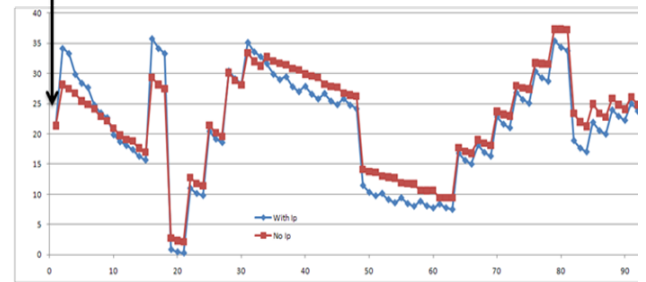
Figure 13. Local Conductor Stresses from the Detailed Model Shown in Figure 10.

In addition to the Lorentz force loads on the coils, there are thermal stresses that result from constraints of the thermal expansion of the coil needed to maintain concentricity of the

coil centers (control the n=1 error while allowing n=2 errors) This constitutes an additional 55 MPa in the conductor max principal stress that adds to the values from the Lorentz loading. Stress results for the detailed model are shown in fig. 13.

1	2	3	4	5	6	7	8	9	10	11	12	13
OH	PF1AU	PF1BU	PF1CU	PF2U	PF3U	PF4	PF5	PF1AL	PF1BL	PF1CL	PF2L	PF3L
0	0	0	0	0	0	16	32	0	0	0	0	0
13.0237626	-5.8489759	9.4451	13.3051	2.9049	-8.822	3.482	-24.5839	-6.07	9.4451	13.3051	2.9049	-8.822
-24	-1.4573	6.2247	6.7393	-2.2799	-10.2215	2.1806	-24.6842	-1.4573	6.2247	6.7393	-2.2799	-10.2215
0	-1.2113	7.8008	9.0773	2.1979	-8.4659	2.071	-23.82	-1.2113	7.8008	9.0773	2.1979	-8.4659
13.0237626	-1.0236493	8.5927533	10.2738039	4.66796512	-7.478427	2.0253083	-23.38663	-1.0236493	8.5927533	10.2738039	4.66796512	-7.478427

Full Current in PF4 and 5, 16 and 32 kA, Produces 21 Mpa Smeared Stress from the influence coefficients



Multiply Influence Coefficient Results by 37/21 to get conductor stress

Figure 14. Influence Coefficients Calculation Including One Data Point at the PF4/5 Full Coil Current Case Used in the Detailed Analysis .

The ratio of the detailed model results divided by the smeared influence coefficient results was found to be 37/21 or 1.76 . This is then used as a part of the DCPS algorithm by additionally applying this factor to teh influence coefficients to obtain the PF5 Lorentz hoop stress for the current operating condition.

V. CONCLUSION

NSTX Upgrade is planning to implement the Digital Coil Protection System or DCPS. It is an extensive system of computer and power supply controls intended protect the coils and support structures. During the NSTX Upgrade design phase a number of algorithms have been developed to predict stresses in critical components of the tokamak. Addition of moment influence coefficients to the usual set of radial and axial force influence coefficients has been described. Specific stress multipliers based on unit currents have been described in this paper. Initial operation of the DCPS and tokamak operation will test the utility and accuracy of these stress simulations. When the full complexity of all the component stress checks is implemented, and de-bugged, the DCPS should become a useful tool for shot planning, and machine protection.

TABLE II. INFLUENCE COEFFICIENTS IN SI UNITS

FX	OH	PF1AU	PF1bU	PF1cU	PF2U	PF3U	PF4U	PF5U	PF1AL	PF1bL	PF1cL	PF2L	PF3L	PF4L	PF5L	Ip	
		Influence Matrix		N/rad													
OH	1	25230.3	3806.061	1708.908	967.1191	1134.092	1209.182	776.9004	1080.26	3806.043	1708.914	967.123	1134.096	1209.203	776.8887	1080.252	58.04883
PF1AU	2	-140.673	856.7656	804.679	402.8212	385.0967	267.9286	97.79694	113.873	2.693542	1.662048	1.908569	5.065918	19.87793	25.48993	46.92737	1.891357
PF1bU	3	-111.435	-147.157	344.059	462.4921	333.3344	164.4536	52.2583	60.96289	1.346069	0.843353	0.970917	2.600311	10.30087	13.1109	24.38876	0.834534
PF1cU	4	-49.8817	-66.3434	-186.161	152.8504	363.0069	147.4613	44.34793	51.61908	1.111908	0.69957	0.805283	2.161407	8.583679	10.90804	20.36479	0.65506
PF2U	5	-31.1968	-44.1531	-82.4588	-136.834	292.1378	317.2212	81.96744	95.94821	1.96759	1.253113	1.443481	3.899963	15.58963	19.65652	37.01328	1.009399
PF3U	6	-21.5523	-26.2723	-19.4406	-24.8062	-74.7123	400.619	163.52	198.7234	3.382355	2.227905	2.566162	7.052979	28.73105	35.6076	68.99472	0.94574
PF4U	7	-14.8351	-3.98004	-1.31325	-1.43192	-0.89291	16.79922	150.6147	444.4194	2.456009	1.717377	1.986237	5.62558	23.96396	30.02812	62.74477	-0.35266
PF5U	8	-20.3084	-2.72794	-0.53848	-0.5621	1.093414	15.20554	-199.776	300.6638	2.999451	2.246582	2.606537	7.632538	33.50699	39.08331	86.71771	-1.09036
PF1AL	9	-140.673	2.693604	1.662109	1.908752	5.066101	19.87787	25.4903	46.92773	856.7654	804.6786	402.821	385.0972	267.929	97.79706	113.8729	1.891724
PF1bL	10	-111.435	1.3461	0.843353	0.970947	2.600433	10.30093	13.11102	24.38889	-147.157	344.0589	462.4922	333.3345	164.4537	52.25842	60.96298	0.834717
PF1cL	11	-49.8816	1.111908	0.699554	0.805328	2.161484	8.583694	10.90807	20.36481	-66.3433	-186.161	152.8504	363.007	147.4612	44.34799	51.61909	0.655121
PF2L	12	-31.1969	1.96756	1.253174	1.443481	3.900024	15.58957	19.65646	37.01309	-44.1531	-82.459	-136.834	292.1379	317.2212	81.9675	95.9483	1.00943
PF3L	13	-21.5522	3.382446	2.227753	2.566376	7.05304	28.73096	35.6077	68.99469	-26.2725	-19.4405	-24.8061	-74.7123	400.6189	163.5069	198.7233	0.945801
PF4L	14	-14.8352	2.456024	1.717377	1.986221	5.625595	23.96391	30.02812	62.74481	-3.97992	-1.31326	-1.43192	-0.89294	16.79919	150.6147	444.4194	-0.35263
PF5L	15	-20.3084	2.999481	2.246521	2.606598	7.632538	33.50702	39.08334	86.7178	-2.72781	-0.53839	-0.56195	1.093506	15.20557	-199.776	300.6637	-1.09033
Ip	16	-0.65479	0.39844	0.250672	0.287969	0.757769	2.9888	4.106287	6.647198	0.39844	0.250672	0.287969	0.757769	2.9888	4.106287	6.647198	0.205512
FY		Influence Matrix		N/rad													
OH	1	0.00E+00	101.6216	132.1296	87.8682	115.5602	56.18751	13.25849	12.59733	-101.621	-132.129	-87.8677	-115.56	-56.1874	-13.2583	-12.5974	1.15E-04
PF1AU	2	-101.118	0.00E+00	384.1478	118.9599	77.54909	0.139336	-8.96284	-10.4976	-0.15052	-9.56E-02	-0.14978	-0.4568	-2.08736	-2.97952	-5.23168	-0.41885
PF1bU	3	-131.409	-386.426	0.00E+00	13.84991	35.47831	-9.61017	-7.17572	-7.91616	-9.66E-02	-6.30E-02	-9.43E-02	-0.28422	-1.29785	-1.85637	-3.34522	-0.21371
PF1cU	4	-87.757	-119.389	-13.8709	0.00E+00	67.80286	-13.4356	-8.80649	-9.60769	-0.14898	-9.25E-02	-0.12476	-0.35941	-1.56134	-2.19689	-3.96695	-0.23739
PF2U	5	-115.714	-77.7934	-35.61	-68.2043	0.00E+00	-69.1412	-26.9411	-28.6129	-0.45662	-0.28304	-0.36006	-1.00674	-4.25728	-5.93188	-10.8552	-0.55093
PF3U	6	-56.2119	-0.1395	9.6224	13.45625	69.21666	0.00E+00	-157.733	-149.975	-2.08676	-1.29659	-1.56193	-4.25708	-17.5993	-24.5514	-46.0942	-1.64419
PF4U	7	-13.2569	8.966514	7.175429	8.808064	26.94148	157.7714	0.00E+00	-368.7	-0.83501	0.288889	-5.35E-02	-3.78803	-22.4096	-33.9093	-67.3666	0.65353
PF5U	8	-12.5961	10.50075	7.915802	9.609217	28.61358	149.9904	371.0913	0.00E+00	-5.23136	-3.34403	-3.96774	-10.8557	-46.0978	-69.5098	-140.886	-1.53568
PF1AL	9	101.1179	0.150541	9.56E-02	0.149777	0.456797	2.08738	2.979534	5.231685	0.00E+00	-384.148	-118.96	-77.5491	-0.13934	8.962835	10.49761	0.418849
PF1bL	10	131.4086	9.55E-02	6.19E-02	9.32E-02	0.283148	1.296791	1.855291	3.344139	386.4264	0.00E+00	-13.8499	-35.4783	9.61014	7.175722	7.916151	0.213699
PF1cL	11	87.75694	0.149756	9.33E-02	0.125511	0.360171	1.562139	2.197661	3.967718	119.3888	13.87093	0.00E+00	-67.8029	13.43558	8.80649	9.607681	0.23738
PF2L	12	115.7142	0.456672	0.283127	0.360149	1.00679	4.257355	5.931921	10.85529	77.79339	35.61006	68.20438	0.00E+00	69.14127	26.94106	28.61289	0.550955
PF3L	13	56.21167	2.086667	1.296516	1.561787	4.257044	17.59918	24.55125	46.09405	0.139395	-9.62249	-13.4564	-69.2168	0.00E+00	157.7327	149.9749	1.644278
PF4L	14	13.25691	2.97919	1.855294	2.19768	5.932143	24.55371	36.0535	69.51076	-8.96656	-7.17546	-8.80807	-26.9415	-157.772	0.00E+00	368.6999	0.65354
PF5L	15	12.59614	5.231288	3.343943	3.967732	10.85565	46.09769	69.50972	140.8862	-10.5008	-7.91585	-9.60928	-28.6136	-149.991	-371.092	0.00E+00	1.535666
Ip	16	-1.55E-08	0.419172	0.212848	0.238377	0.551498	1.645014	1.489633	1.53422	-0.41917	-0.21285	-0.23838	-0.5515	-1.64501	-1.48963	-1.53422	0.00E+00
MZ		Influence Matrix		N-m/rad													
OH	1	0.00E+00	-5784.29	-2838.07	-1513.56	-1616.71	-1121.45	-371.817	-348.327	5784.292	2838.077	1513.561	1616.714	1121.453	371.8189	348.3287	1.54E-03
PF1AU	2	7.152492	0.00E+00	-73.6636	-20.0842	-10.7058	-1.67E-02	1.050949	1.221679	4.40E-02	2.56E-02	2.81E-02	7.11E-02	0.266337	0.352855	0.613915	4.54E-02
PF1bU	3	0.450232	-6.49832	0.00E+00	-0.48198	-0.75231	0.146579	0.101039	0.110743	3.10E-03	1.88E-03	2.03E-03	5.06E-03	1.95E-02	2.64E-02	4.72E-02	2.47E-03
PF1cU	4	-4.01E-02	-1.14453	-0.29893	0.00E+00	-1.36518	0.137595	7.59E-02	8.12E-02	2.03E-03	1.17E-03	1.35E-03	3.36E-03	1.35E-02	1.80E-02	3.27E-02	1.64E-03
PF2U	5	3.73E-02	3.25E-02	8.51E-03	-3.28E-02	0.00E+00	-2.93E-02	-9.37E-03	-9.36E-03	1.93E-04	4.89E-04	-2.55E-04	-2.66E-05	-5.84E-04	-1.09E-03	-2.90E-03	-5.31E-05
PF3U	6	3.28E-02	-8.45E-05	-1.69E-02	-2.42E-02	-0.13652	0.00E+00	-0.19286	-0.17624	-1.35E-03	-6.15E-04	-1.23E-03	-2.31E-03	-1.18E-02	-1.78E-02	-3.60E-02	1.01E-05
PF4U	7	1.81E-03	1.45E-02	1.02E-02	1.26E-02	3.48E-02	0.208274	0.00E+00	1.686089	-8.70E-02	-8.69E-02	-8.68E-02	-8.67E-02	-8.36E-02	-7.60E-02	-5.52E-02	-8.88E-02
PF5U	8	6.00E-04	2.37E-03	1.34E-03	1.66E-03	4.70E-03	2.13E-02	0.34347	0.00E+00	3.96E-04	9.27E-05	2.31E-04	5.87E-04	4.05E-03	4.44E-03	1.63E-02	-6.30E-04
PF1AL	9	-7.15235	-4.34E-02	-2.57E-02	-2.80E-02	-7.17E-02	-0.2658	-0.35305	-0.61401	0.00E+00	73.66515	20.08523	10.70527	1.58E-02	-1.05117	-1.22179	-4.59E-02
PF1bL	10	-0.45037	-3.05E-03	-1.71E-03	-1.99E-03	-5.31E-03	-1.96E-02	-2.65E-02	-4.71E-02	6.498307	0.00E+00	0.482262	0.752478	-0.14651	-0.1009	-0.11069	-2.63E-03
PF1cL	11	3.99E-02	-1.98E-03	-1.10E-03	-1.35E-03	-3.52E-03	-1.34E-02	-1.81E-02	-3.26E-02	1.14442	0.298811	0.00E+00	1.365146	-0.13729	-7.59E-02	-8.14E-02	-1.71E-03
PF2L	12	-3.69E-02	-3.48E-04	-3.97E-04	4.51E-05	-2.21E-04	4.78E-04	1.18E-03	2.56E-03	-3.21E-02	-7.84E-03	3.30E-02	0.00E+00	2.88E-02	9.07E-03	8.70E-03	-2.28E-04
PF3L	13	-3.30E-02	1.25E-03	9.91E-04	1.05E-03	2.59E-03	1.25E-02	1.79E-02	3.62E-02	3.17E-04	1.61E-02	2.39E-02	0.136112	0.00E+00	0.193252	0.176294	5.08E-05
PF4L	14	-1.84E-03	-1.38E-04	-1.84E-04	-1.52E-04	-3.86E-04	-3.46E-03	-1.12E-02	-3.20E-02	-0.0248	-1.27E-02	-3.48E-02	-0.20831	0.00E+00	-1.68622	8.86E-02	0.00E+00
PF5L	15	-5.71E-04	-3.25E-04	-9.78E-05	-4.88E-04	-9.94E-04	-3.86E-03	-4.33E-03	-1.58E-02	-2.34E-03	-1.28E-03	-1.46E-03	-4.74E-03	-2.13E-02	-0.34239	0.00E+00	5.13E-04
Ip	16	-4.60E-10	-1.95E-02	-1.32E-02	-1.53E-02	-4.05E-02	-0.16181	-0.22447	-0.26779	1.95E-02	1.32E-02	1.53E-02	4.05E-02	0.161809	0.224468	0.267794	0.00E+00

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