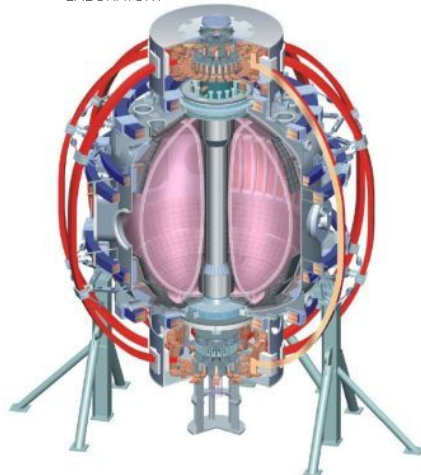


Recap of 0-D projections and 2-D SOLPS interpretive modeling of density control from lithium

R. Maingi, J.M. Canik 

Columbia U
CompX
General Atomics
FIU
INL
Johns Hopkins U
LANL
LLNL
Lodestar
MIT
Nova Photonics
New York U
ORNL
PPPL
Princeton U
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U Maryland
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U Wisconsin

Li Research TSG, PPPL
26 Jan 2012



Culham Sci Ctr
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NFRI
KAIST
POSTECH
ASIPP
ENEA, Frascati
CEA, Cadarache
IPP, Jülich
IPP, Garching
ASCR, Czech Rep

Summary of 0-D predictive modeling and 2-D interpretive modeling of lithium coatings in NSTX

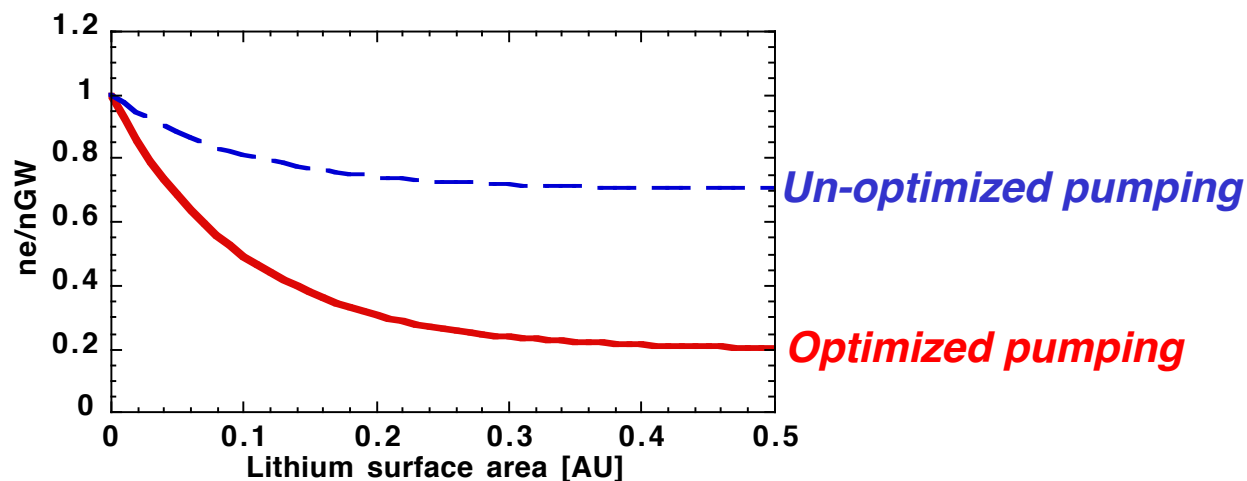
- 0-D predictive modeling was done for guidance of LLD location and width
 - Assumed ideal sticking of D to liquid lithium ($R_p=0.15$), and an application of lithium to LLD only
 - Predicted 20-50% density reduction with LLD
 - Actual experiment had lithium deposited mostly away from LLD on inboard side: lithium pumping on graphite would dominate the LLD effects for short pulse lengths
 - NSTX-U: need local lithium deposition on LLD to isolate effect
- 2-D SOLPS interpretive modeling of lithium on graphite was performed
 - For $\delta \sim 0.5$, R_p went from 0.98 to ~ 0.9 (Canik, PoP 11)
 - For $\delta \sim 0.8$, R_p dropped to ~ 0.85 (Pigarov, Smirnov)

Calculations needed for LLD Tray Design Specification

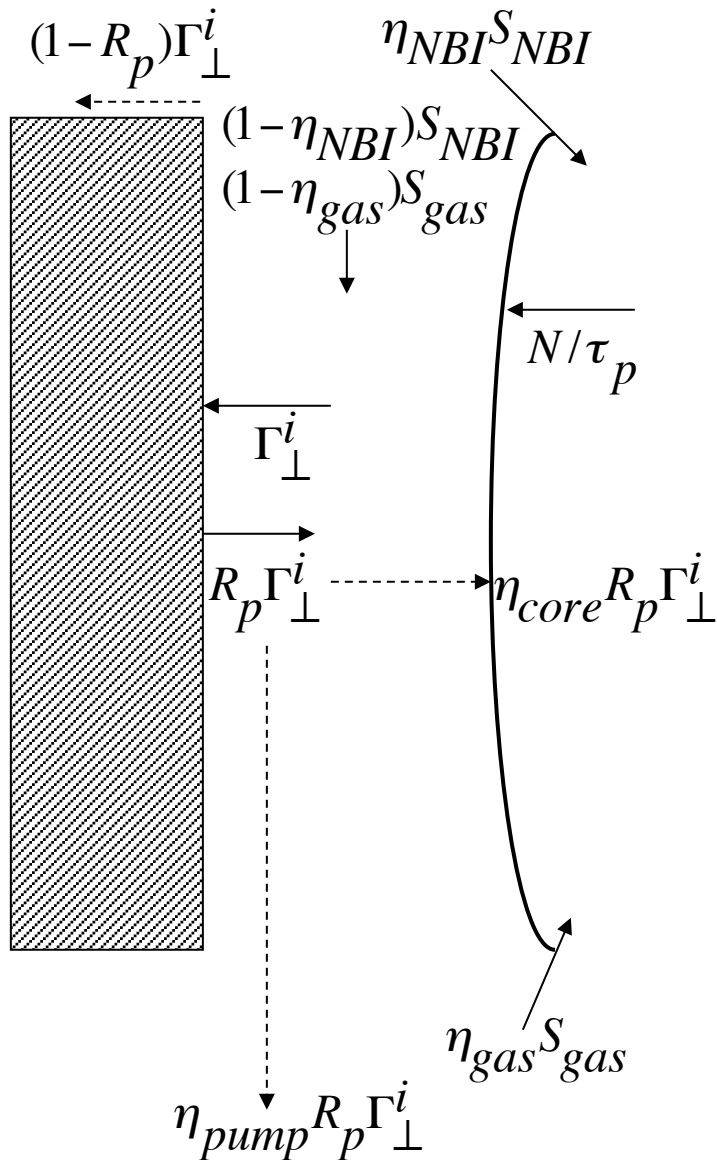


- The following LLD design parameters need to be specified (target: April 15, 2007):
 - 1) Tray Width
 - 2) Tray Major Radius R_{tray}
 - 3) Number of tray segments, gap size(s) between segments, and clocking of segments ($\phi_{\text{min}} - \phi_{\text{max}}$)
- Minimum density will depend on tray-OSP distance

*Large distance between
OSP and LLD radius*



Particle Balance and Recycling Model



- Consider core and SOL particle content equations

$$\frac{dN}{dt} = \eta_{NBI} S_{NBI} + \eta_{gas} S_{gas} - \frac{N}{\tau_p} + \eta_{core} R_p \Gamma_{\perp}^i$$

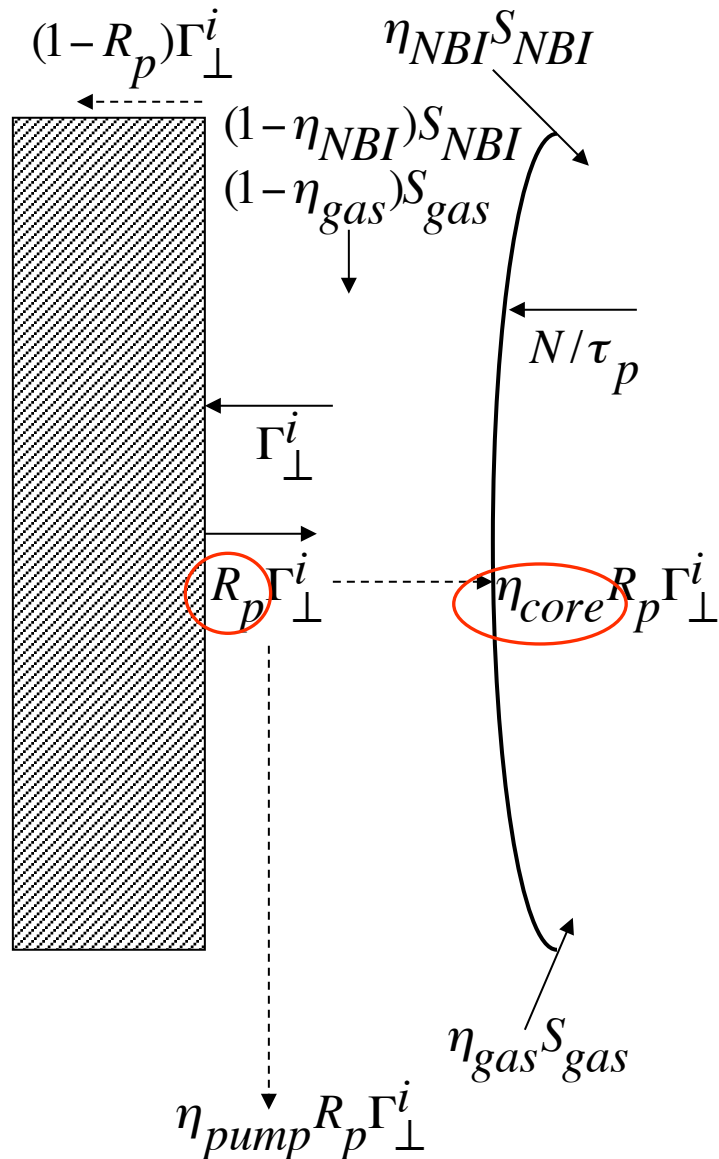
$$\frac{dN_i^{SOL}}{dt} + \frac{dN_0^{SOL}}{dt} = (1 - \eta_{NBI}) S_{NBI} + (1 - \eta_{gas}) S_{gas} + \frac{N}{\tau_p} - (1 - R_p) \Gamma_{\perp}^i - R_p \Gamma_{\perp}^i (\eta_{pump} + \eta_{core})$$

- Assume SOL neutral and ion density in steady state

$$\frac{dN}{dt} = (1 + \beta - \beta \eta_{NBI}) S_{NBI} + (1 + \beta - \beta \eta_{gas}) S_{gas} - \frac{N(1 - \beta)}{\tau_p}, \text{ where}$$

$$\beta \equiv R_p \eta_{core} \left[(1 - R_p) + R_p (\eta_{pump} + \eta_{core}) \right]$$

Particle Balance and Recycling Model



- Consider core and SOL particle content equations

$$\frac{dN}{dt} = \eta_{NBI}S_{NBI} + \eta_{gas}S_{gas} - \frac{N}{\tau_p} + \eta_{core}R_p\Gamma_{\perp}^i$$

$$\frac{dN_i^{SOL}}{dt} + \frac{dN_0^{SOL}}{dt} = (1-\eta_{NBI})S_{NBI} + (1-\eta_{gas})S_{gas} + \frac{N}{\tau_p} - (1-R_p)\Gamma_{\perp}^i - R_p\Gamma_{\perp}^i(\eta_{pump} + \eta_{core})$$

- Assume SOL neutral and ion density in steady state

$$\frac{dN}{dt} = (1+\beta-\beta\eta_{NBI})S_{NBI} + (1+\beta-\beta\eta_{gas})S_{gas} - \frac{N(1-\beta)}{\tau_p}, \text{ where}$$

$$\beta \equiv R_p \eta_{core} \left[(1-R_p) + R_p(\eta_{pump} + \eta_{core}) \right]$$

Method to Relate 0-D Pump Probability to Divertor Plasma and Lithium tray parameters



In/out particle flux ratio - 0.8

Li surface particle sticking probability - 0.85

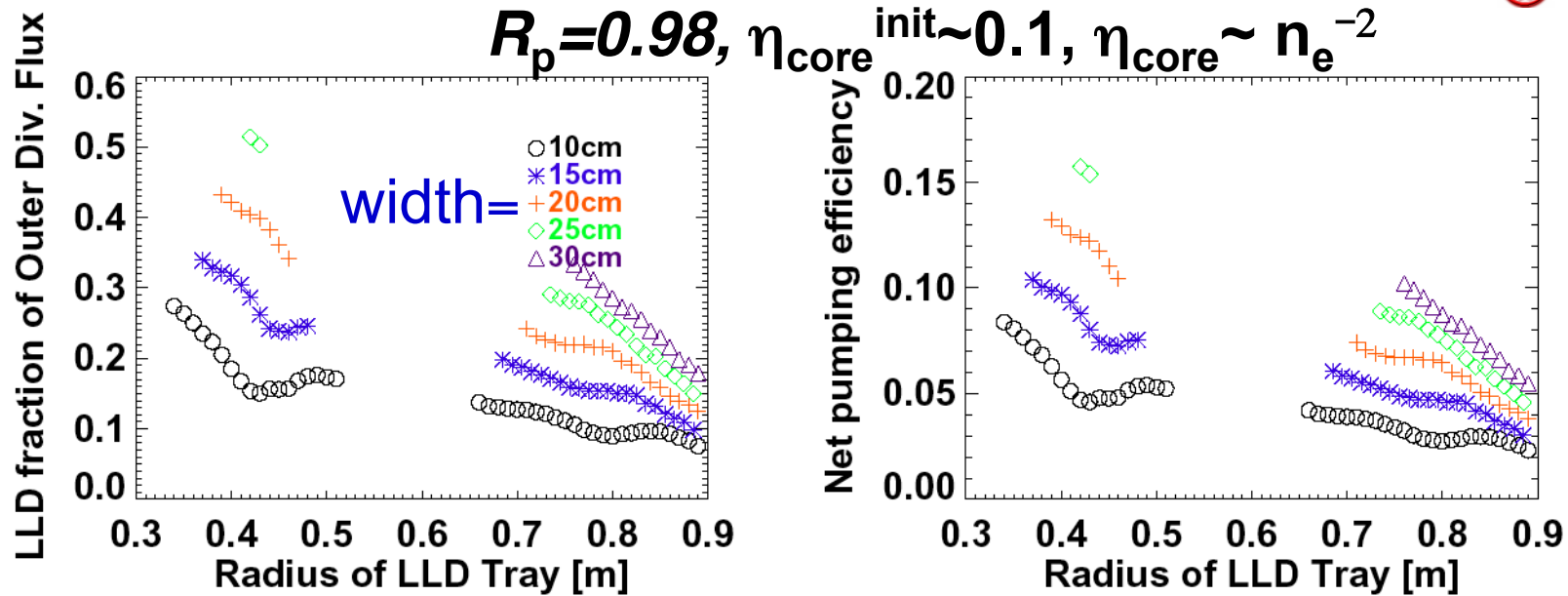
Tray toroidal coverage - 0.9

$$\eta_{pump} \cong \gamma_{Li}^{sticking} \frac{\int_{R_{min, tray}}^{R_{max, tray}} \Gamma_{\perp}(R) R dR}{\int_{R_{min}}^{R_{max}} \Gamma_{\perp}(R) R dR} \left(\frac{\Gamma_{out}}{\Gamma_{in} + \Gamma_{out}} \right) \left(\frac{\Gamma_{down}}{\Gamma_{up} + \Gamma_{down}} \right) f_{\phi}$$

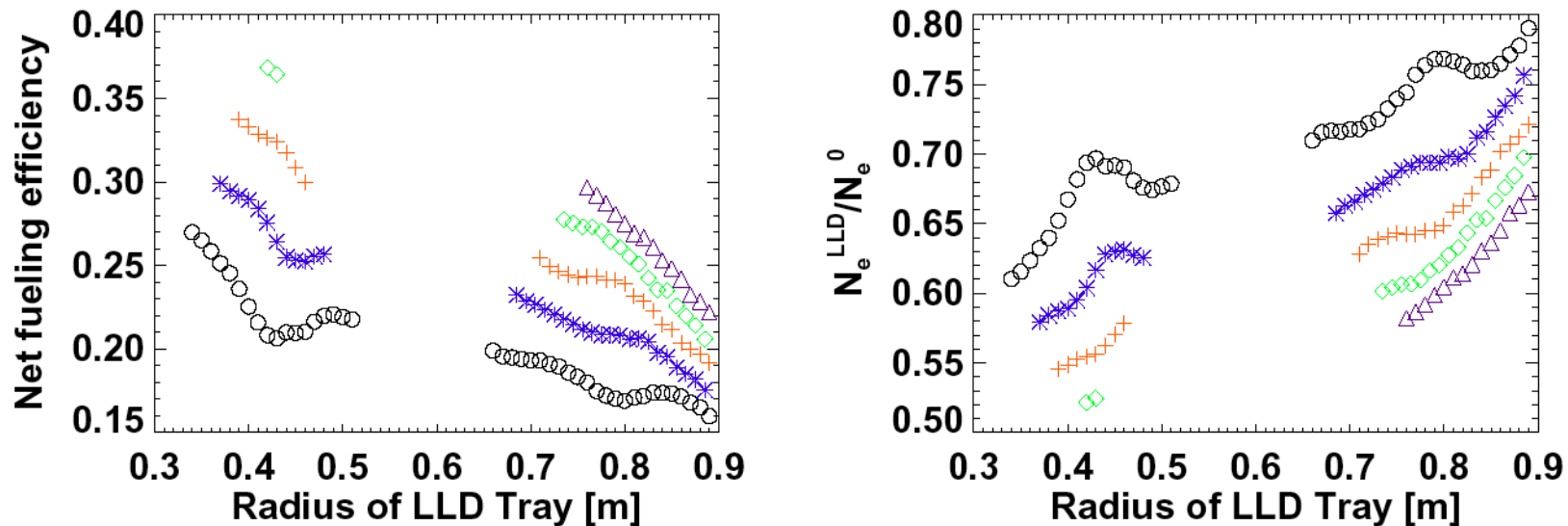
Impact of R_{tray} , Δ_{tray} , $(R_{OSP} - R_{tray})$
(Γ estimated from D_{α} profile)

Up/down particle flux ratio
 0.5 (δ_r^{sep} important)

Achievable edge density reduction depends on tray radius and width in high δ discharge



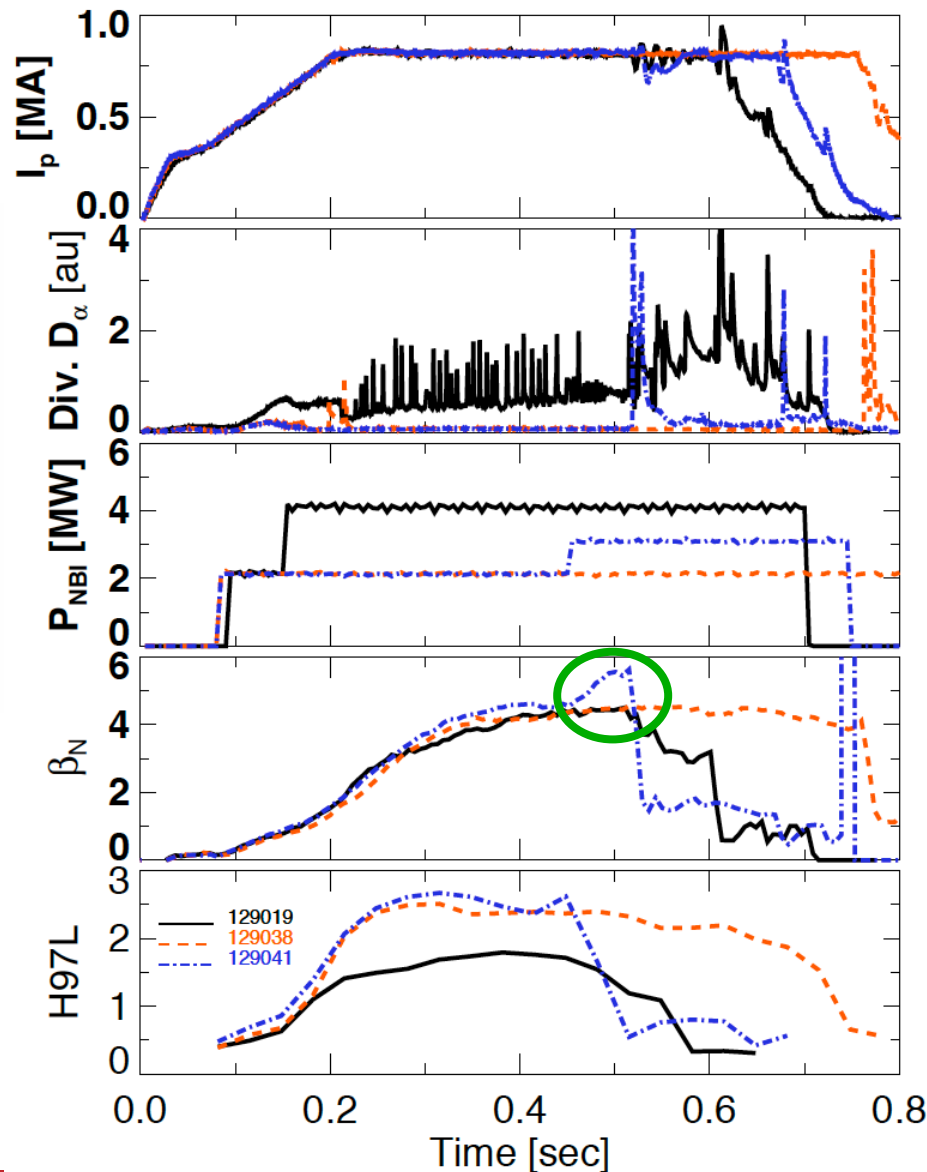
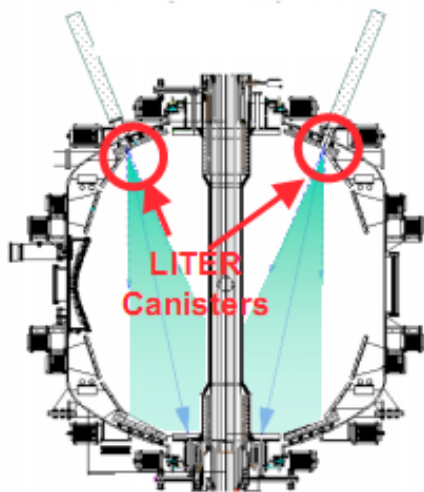
#121238 @ 0.3 sec



Summary of 0-D predictive modeling and 2-D interpretive modeling of lithium coatings in NSTX

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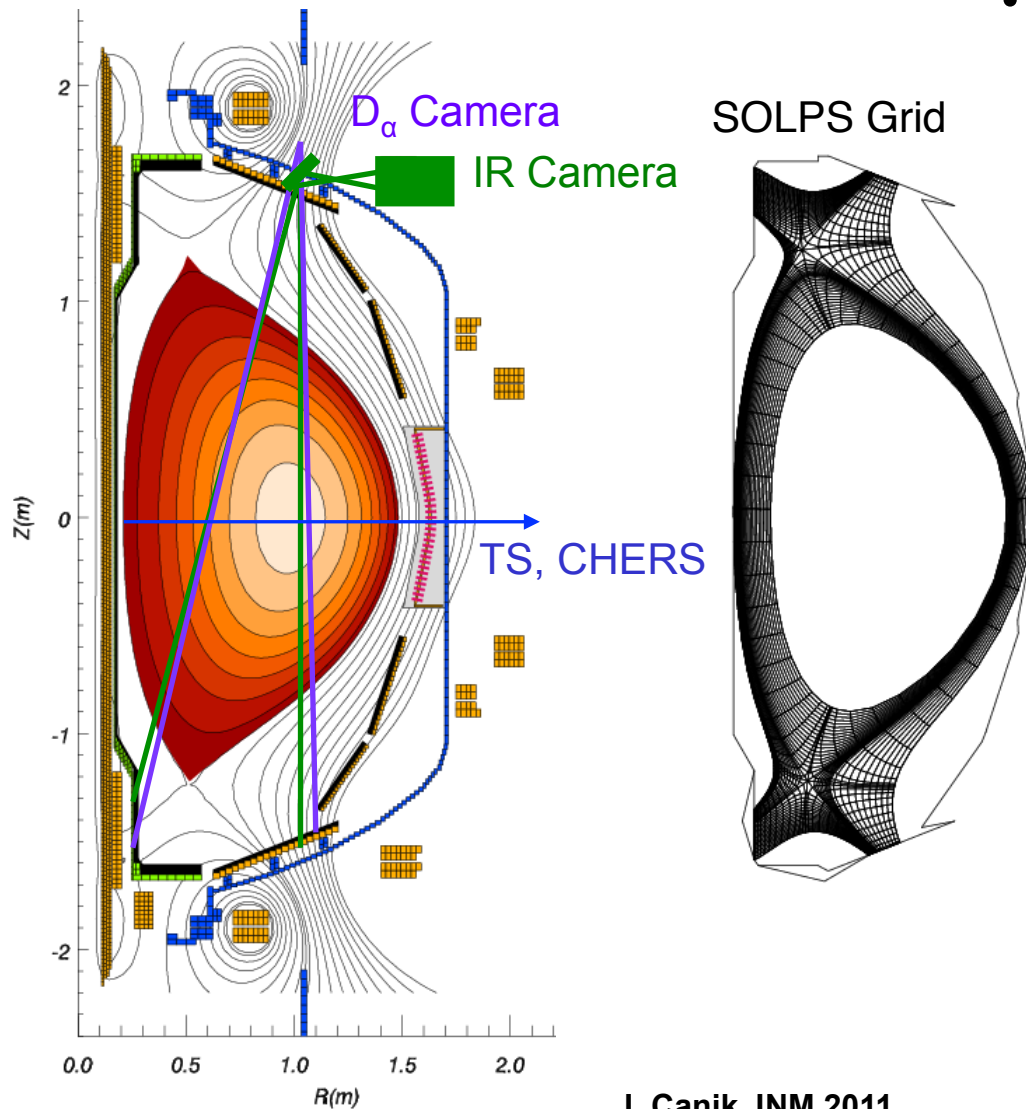
Edge stability limits pushed beyond global stability limits with lithium coatings in NSTX



- Without Li, **With Li**, **With Li**
- **ELM-free**, reduced divertor recycling
- Power scan to identify β limit
- Core β limit observed, but no ELMs

D. Mansfield, JNM 09
R. Maingi, PRL 09

Divertor recycling and cross-field transport coefficients quantified with data-constrained interpretive modeling



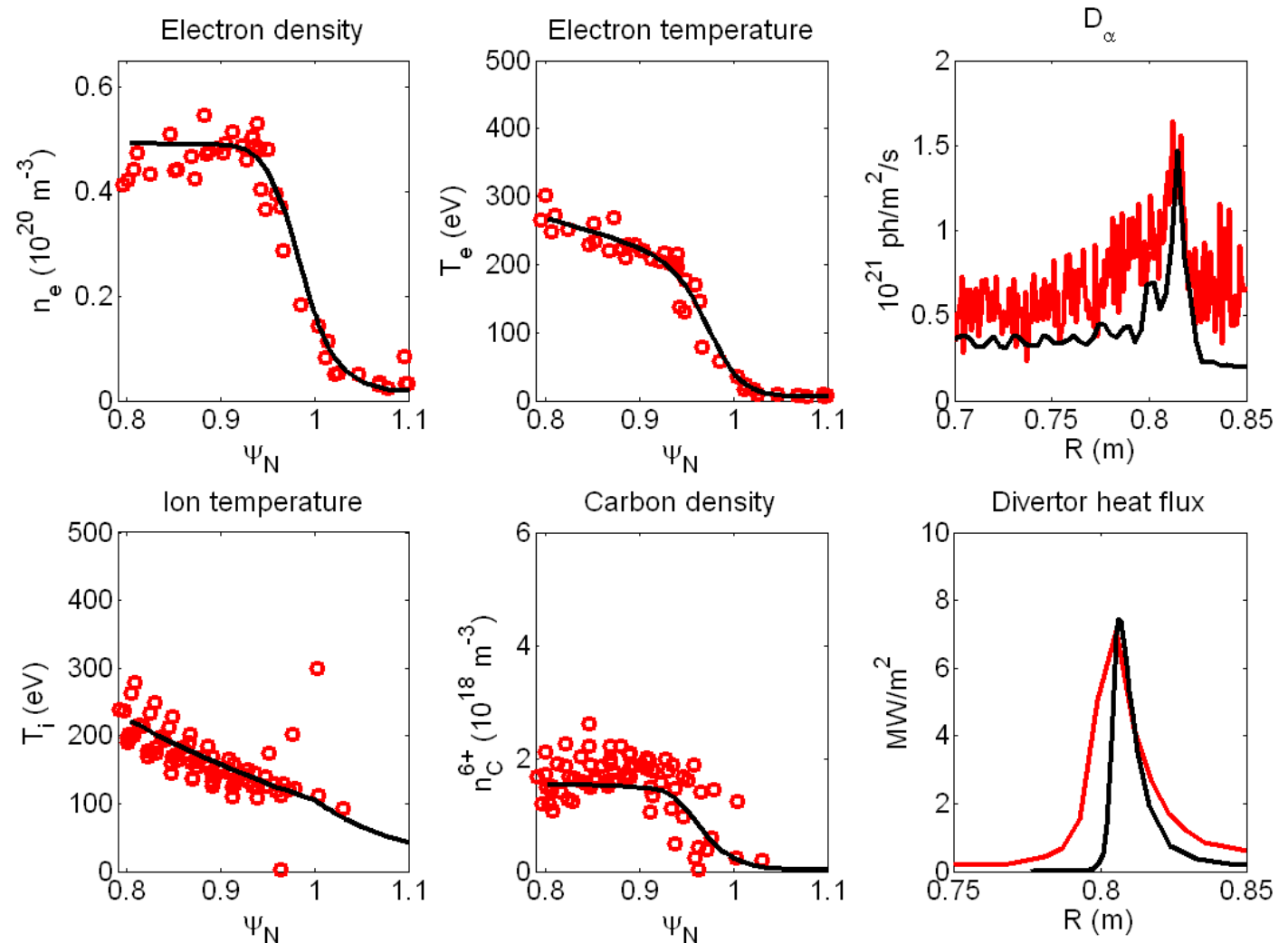
- SOLPS (B2-EIRENE: 2D fluid plasma + MC neutrals) used to model NSTX experimental data
 - Iterative Method
 - ✓ Neutrals, impurities contributions
 - ✓ Recycling changes due to lithium

Parameters adjusted to fit data	Measurements used to constrain code
Radial transport coefficients D_\perp, χ_e, χ_i	Midplane n_e, T_e, T_i profiles
Divertor recycling coefficient	Calibrated D_α camera
Separatrix position/ T_e^{sep}	Peak divertor heat flux

J. Canik JNM 2011

Midplane and divertor profiles from modeling compare well to experiment for the pre-lithium case

- $P=3.7$ MW
- $R=0.98$
- Good match to midplane profiles
- Carbon included: sputtering from PFCs, inward convection to match measured n_C^{6+}
- Heat flux and D_α , radial decay sharper than experiment



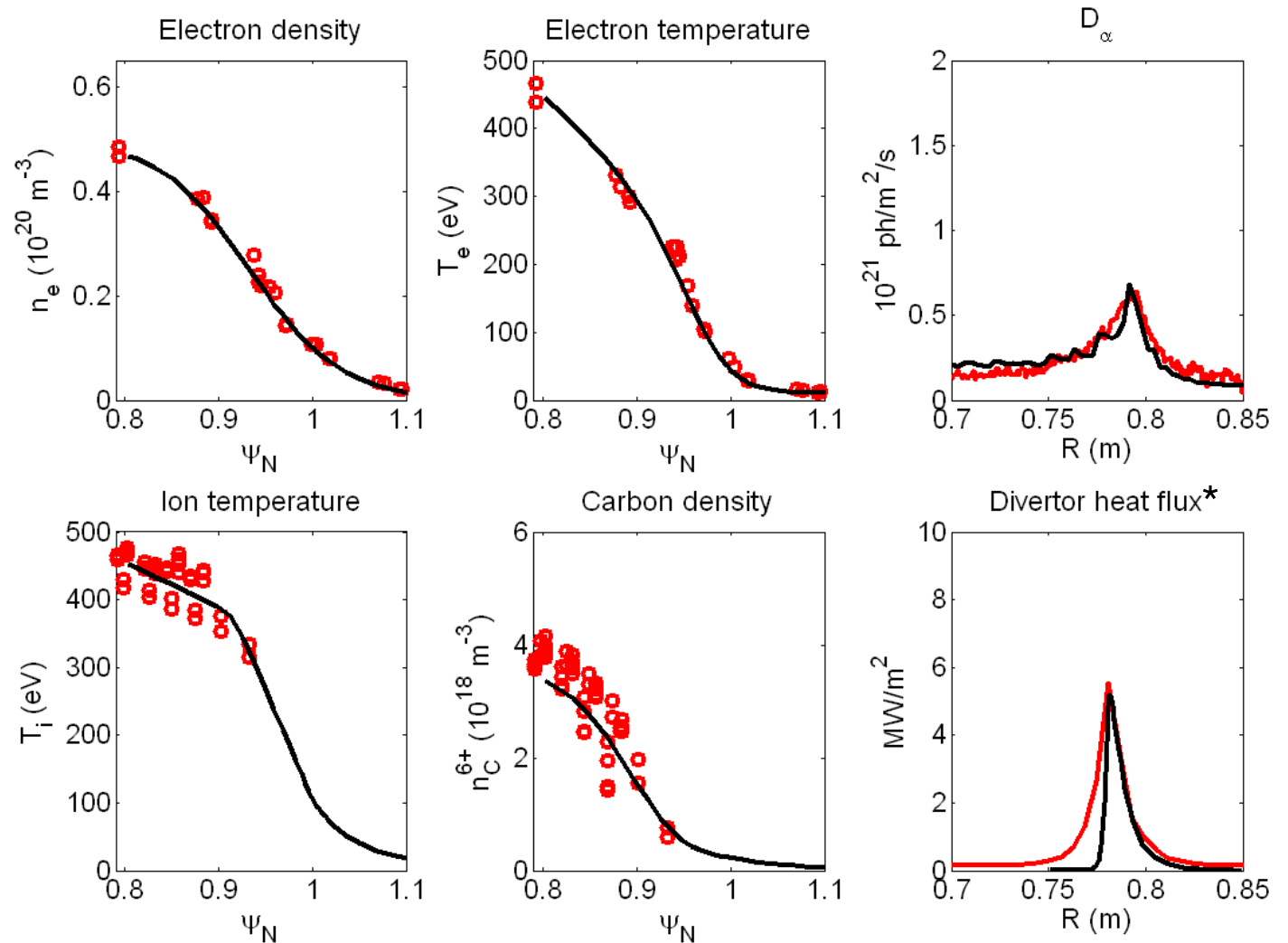
J. Canik PoP 2011

Combining reduced recycling and transport changes gives match to measurements with lithium

- $P=1.9$ MW
- $R=0.90$
- Transport coefficients adjusted to recover fit to upstream data

- Good match to both peak and profile for heat flux and D_α (except PFR)

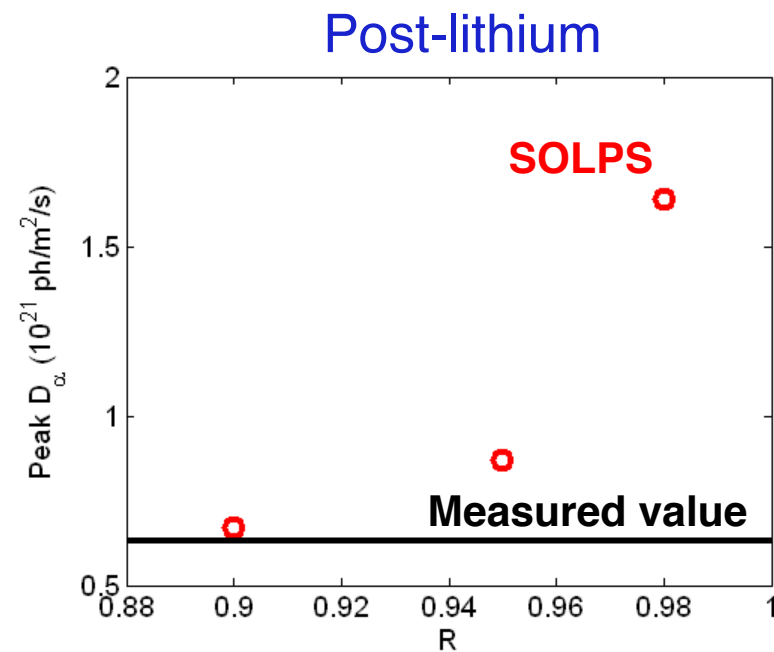
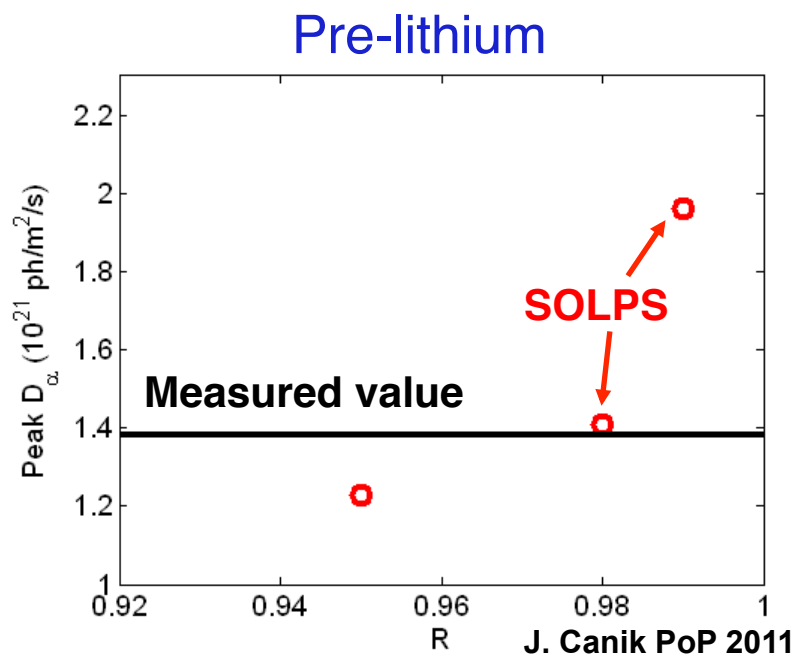
*Uncertainty exists in IR measurements, due to emissivity change with lithium films



J. Canik PoP 2011

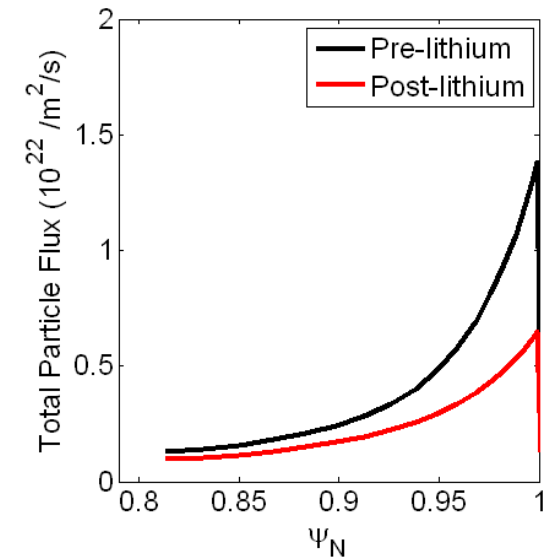
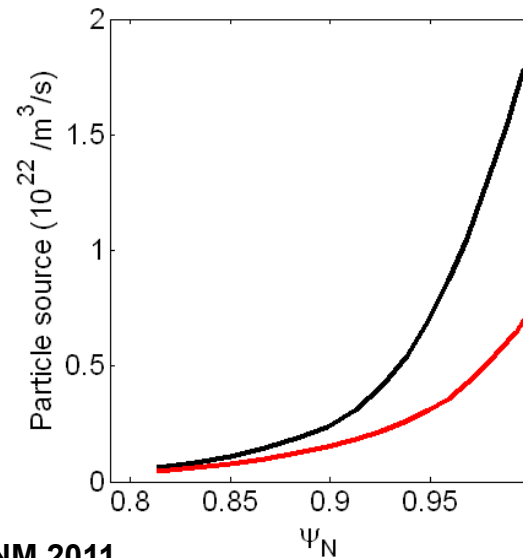
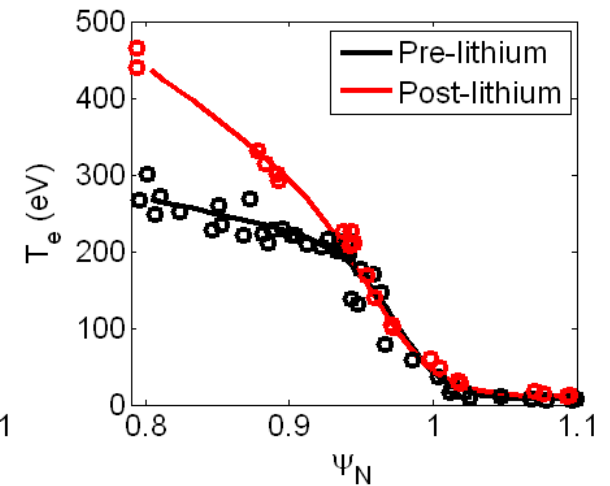
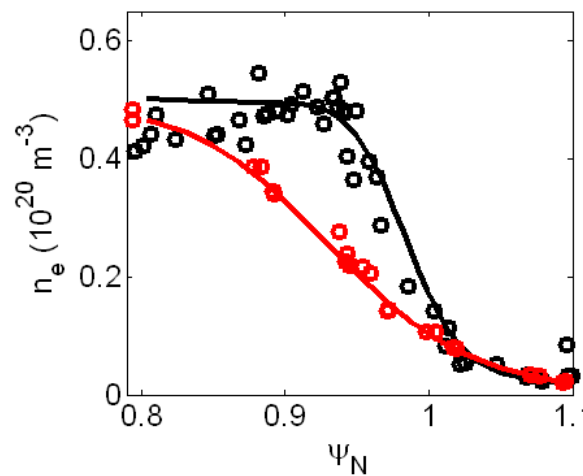
Peak D_α brightness is matched to experiment to constrain PFC recycling coefficient: lithium reduces R from ~ 0.98 to ~ 0.9

- For each discharge modeled, PFC recycling coefficient R is scanned
 - Fits to midplane data are redone at each R to maintain match to experiment
- D_α emissivity from code is integrated along lines of sight of camera, compared to measured values
 - Best fit indicates reduction of recycling from $R \sim 0.98$ to $R \sim 0.9$ when lithium coatings are applied



Particle and heat sources are reduced with lithium

- Pre-lithium case shows typical H-mode structure
 - Barrier region in D , χ_e just inside separatrix
- Pedestal is much wider with lithium
 - D_{\perp} , χ_e similar outside of $\psi_N \sim 0.95$
 - Low D_{\perp} , χ_e persist to inner boundary of simulation ($\psi_N \sim 0.8$)
- Changes to profiles with lithium are due to reduced fluxes combined with wide transport barrier



J. Canik JNM 2011

Possible next steps

- Extend 0-D predictive model to include variable lithium deposition as in NSTX, and compute effect of LLD
- Extend 0-D model to NSTX-U with improved lithium deposition control?
- Continue 2-D SOLPS interpretive modeling of $I_p=1.2$ MA discharges to obtain transport coefficients
 - Extrapolate to NSTX-U using known heat flux width scaling in absence of lithium and with lithium
- Extend SOLPS modeling to snowflake scenarios? (being done with UEDGE)

Backup

Motivation and Technique



- Desire predictive models for effect of pumping on NSTX edge plasma
 - Provide means for comparing density control schemes, e.g. different Lithium tray design parameters (or even in-vessel cryopumping)
 - Should be compared with other experiments and more detailed calculations
- Consider simple recycling model to evaluate examples of each scheme
 - DIII-D data from first cryopump in 1993
 - CDX-U data from liquid Lithium
- Goal: Predict range of reduction in edge density in H-mode

Pumping calculations will help specify the LLD design parameters

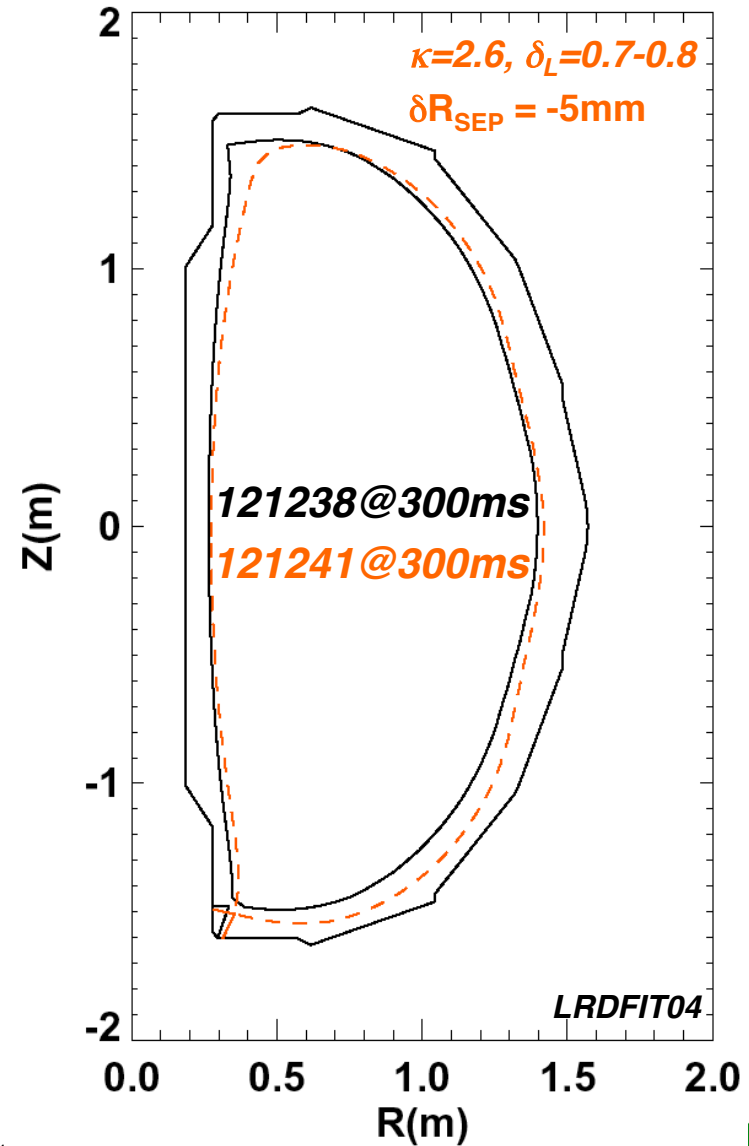
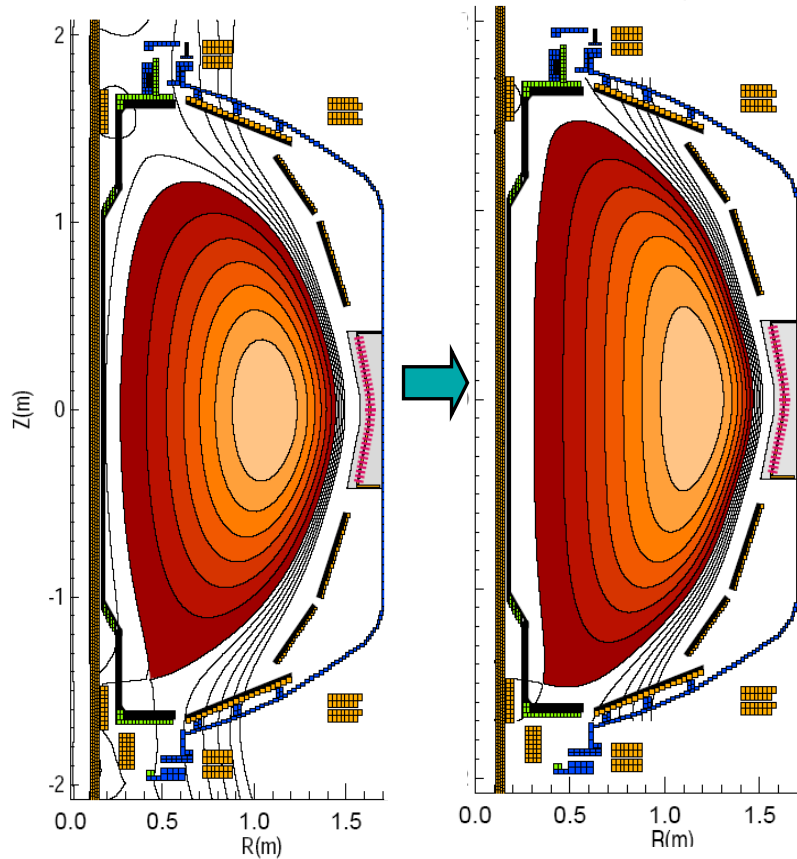


- **0-D calculations presented in this talk:**
 - **Parameterized as ratio of pump to core fueling probabilities**
 - **Requires an assumed relation between pump probability and lithium surface area**
- 1-D calculations
 - Onion-skin OEDGE type, *requires assessment for NSTX*
- 2-D fluid calculations (model)
 - T. Rognlien did NSTX calculations in the past for ALPS/APEX
- 2-D fluid + lithium transport calculations (model)
 - T. Rognlien/J. Brooks did NSTX calcs in the past for ALPS/APEX
- 2-D fluid plasma (data-constrained base case)
 - G. Porter, L. Owen, and R. Maingi have done these for DIII-D
- 2-D fluid plasma + kinetic neutrals (data-constrained base case)
 - L. Owen, M. Rensink, and R. Maingi have done these for DIII-D

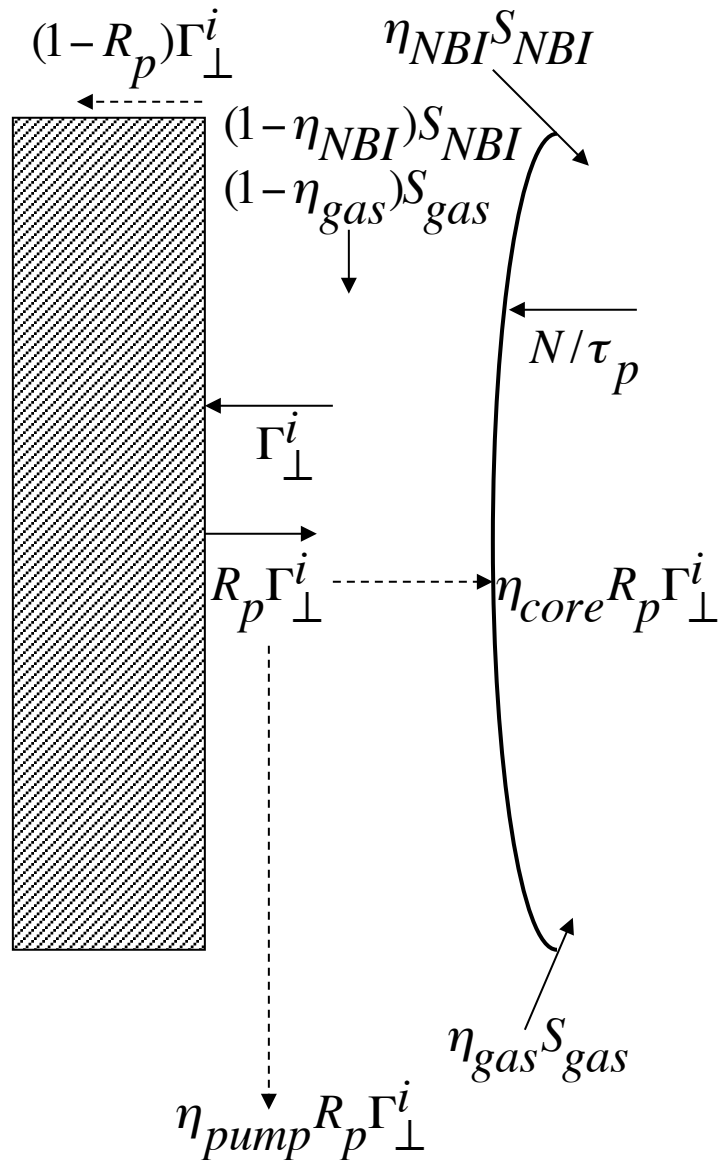
Discharges #116318 @ 0.6 sec and #121238 @ 0.3 sec used for design calculations

Existing #116313
 $\kappa = 2.3, \delta_{X-L} = 0.75$
 $\delta R_{SEP} = -1\text{cm}$

New target shape
 $\kappa = 2.6, \delta_{X-L} = 0.85$
 $\delta R_{SEP} = -2\text{mm}$



Simplified Particle Balance and Recycling Model



- Define $\tau_p^* = \tau_p / (1 - \beta)$
 - Steady state: $\tau_p^* = N / (S_{NBI} + S_{gas})$
- Normal assumptions:
 - $\eta_{NBI} \sim 1$
 - ~~$R_p(\eta_{pump} + \eta_{core}) \gg (1 - R_p)$~~
 - η_{pump}, η_{core} independent of time
- Particle balance equation becomes:

$$\frac{dN}{dt} = S_{NBI} + (1 + \beta(1 - \eta_{gas}))S_{gas} - \frac{N}{\tau_p^*}$$

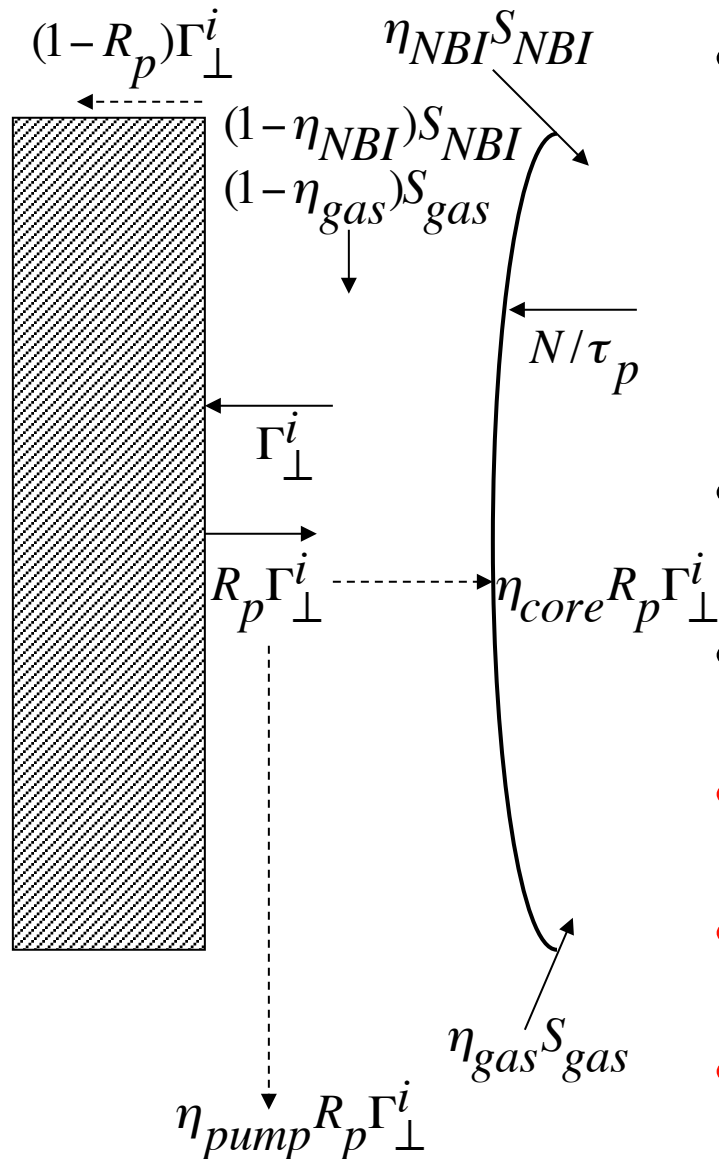
$$\text{Let } S = S_{NBI} + (1 + \beta(1 - \eta_{gas}))S_{gas}$$

Solution:

$$N(t) = S\tau_p^{*1} + S(\tau_p^{*2} - \tau_p^{*1})\exp(-t/\tau_p^{*2})$$

- Has been used to model step change in τ_p (L-H) and pumping ($\eta_{pump} > 0$)

Simplified Particle Balance and Recycling Model



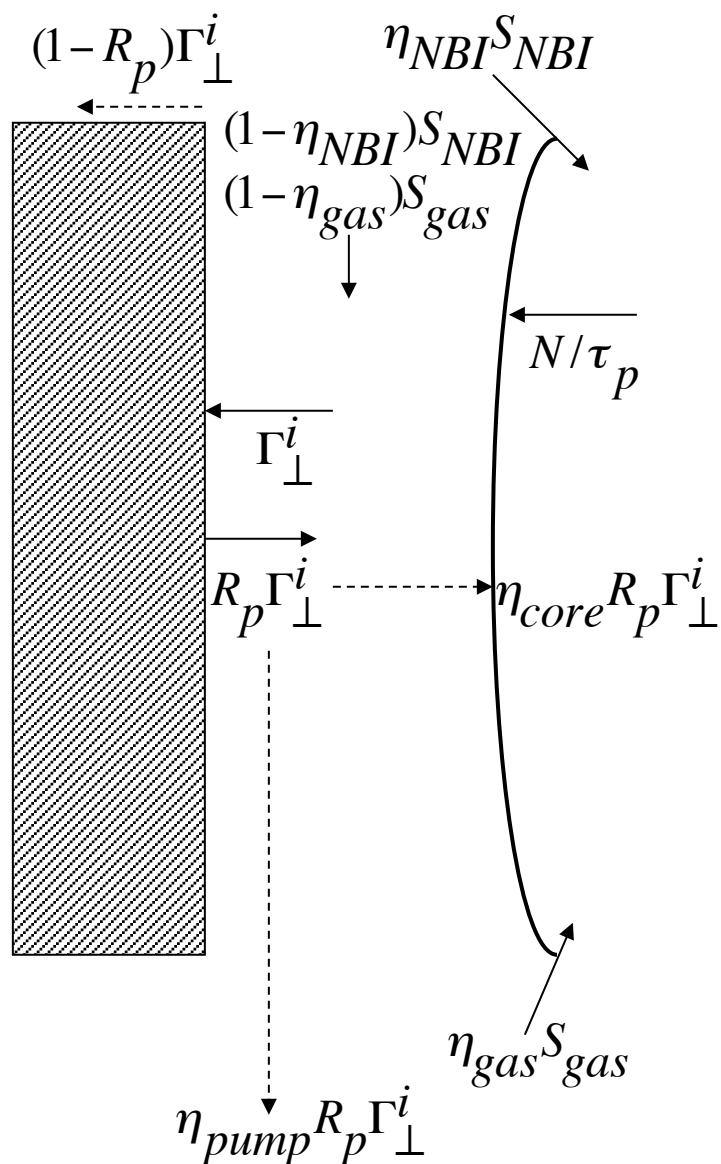
- Density reduction factor

$$n_e^{red} = \tau_{p,pump}^* / \tau_{p,nopump}^*$$

$$= (1-\beta)_{noLi} / (1-\beta)_{Li} \quad \underline{\text{constant } \tau_p}$$

- $\beta_{noLi} = \eta_{core}R_p / ((1-R_p) + R_p^*\eta_{core})$
- $\beta_{Li} = \eta_{core}R_p / ((1-R_p) + R_p^*(\eta_{core} + \eta_{pump}))$
- **Need prescription to estimate η_{Li}**
- **Is η_{core} really independent of n_e ?**
- **Is τ_p really independent of n_e ?**

Limits of Particle Balance and Recycling Model



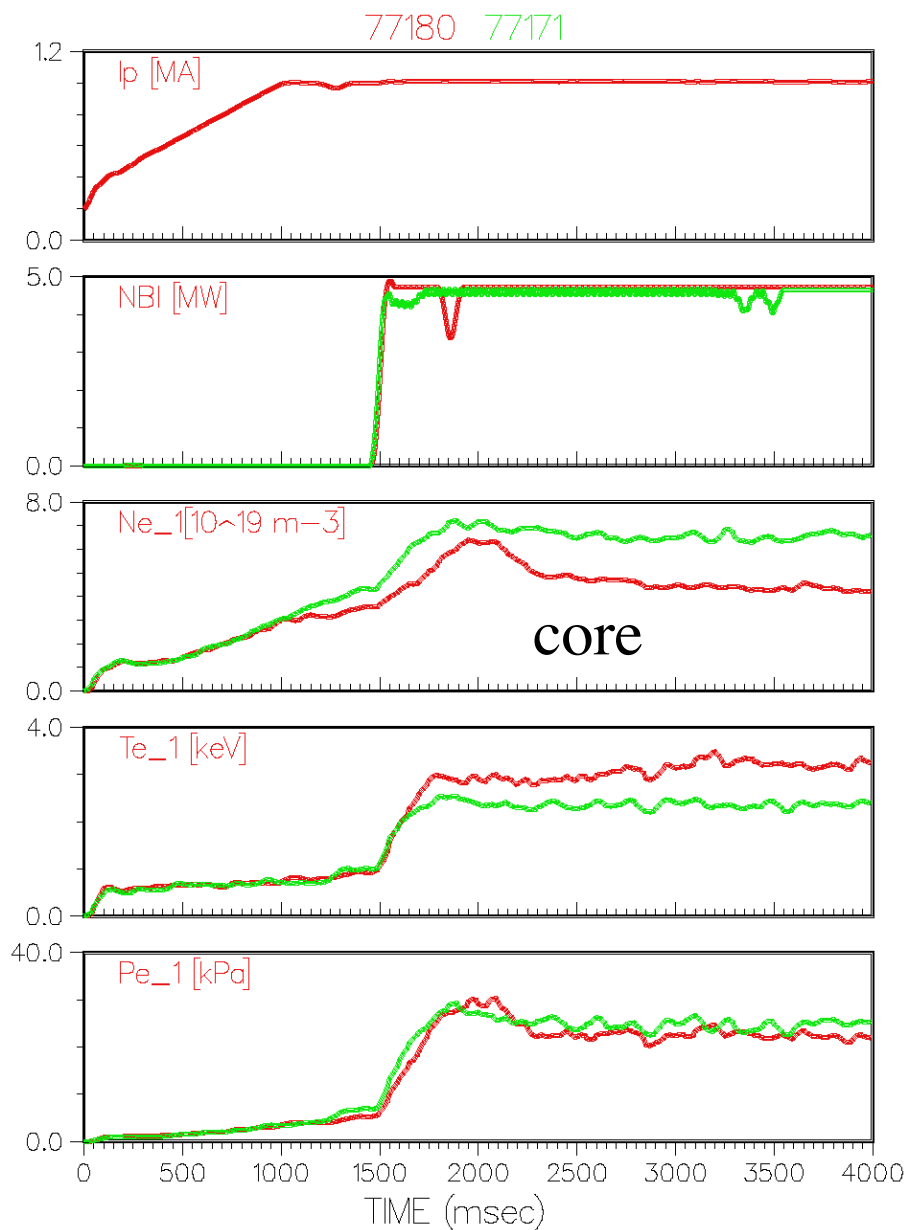
- Note $\tau_p^*/\tau_p = 1/(1-\beta)$
- Pump off: $\tau_p^*/\tau_p \sim 1 + \eta_{core}R_p/(1-R_p)$
 - $\tau_p^*/\tau_p \sim 6$
- Pump on: $\tau_p^*/\tau_p \sim (\eta_{core} + \eta_{pump})/\eta_{pump}$
 - $\tau_p^*/\tau_p \sim 2$
- n_e should go down by 2/3 w/pumping
 - ⇒ *Smaller n_e reduction observed, maybe due to increased core fueling probability at low n_e*
- Input data (from DIII-D studies):
 - $R_p \sim 0.98$ for carbon (reference?)
 - $\eta_{core} \sim 0.1$ (Rensink, PoF B 1993)
 - $\eta_{pump} \sim 0.1$ (Maingi, NF 1999)

Procedure

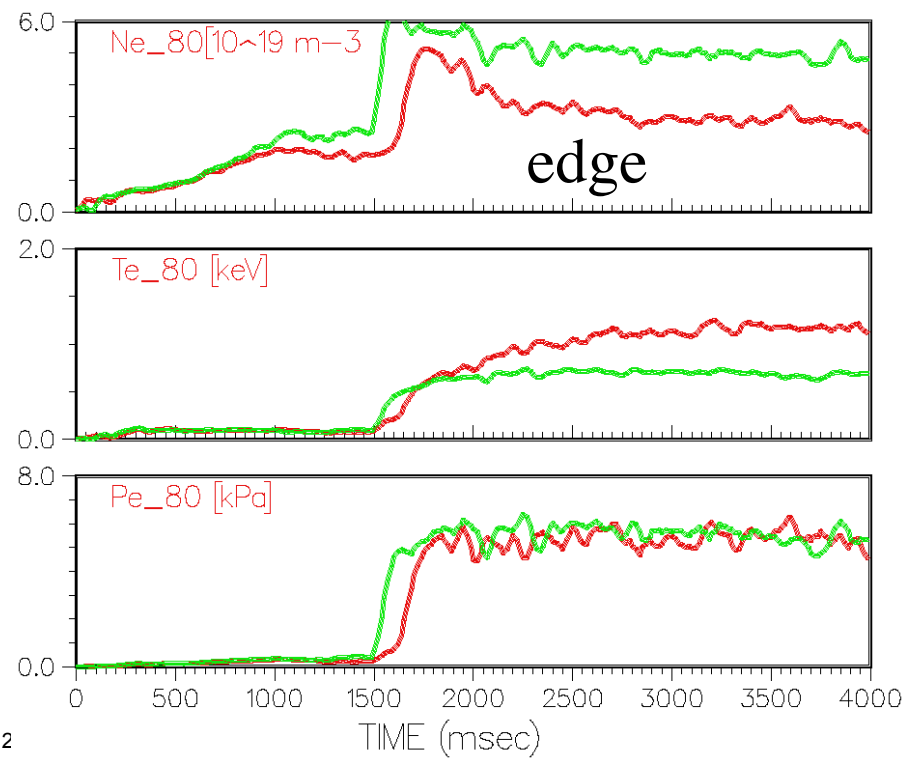


- Convert D_α to particle flux with magic number of 20 ionizations per photon
- Estimate LLD flux intercept fraction from data for a given R_{tray} , W_{tray} , etc. for a given time slice
 - Vary R_{tray} 1 cm at a time
 - R_{tray} starting point a few cm inside of the outer strike point; avoids interpretation of partially detached inner region
 - Avoid covering CHI gap with tray
 - Iterate on $\eta_{\text{core}} \sim 1/n_e^\alpha$ (default: $\alpha=2$)
- Repeat for different W_{tray} , R_p , and other input parameters
- Repeat calculations for different shots with different poloidal flux expansion

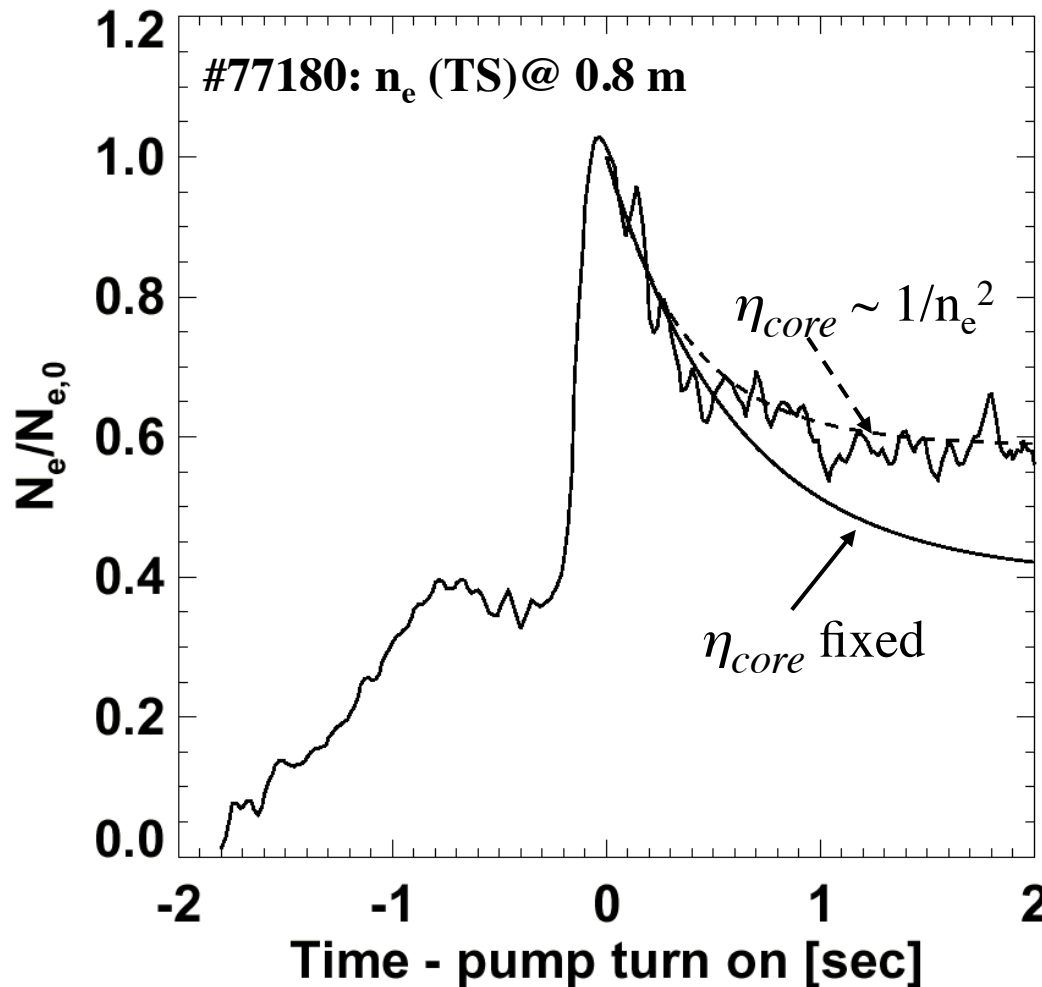
Comparison of Unpumped and Pumped DIII-D Discharges



- Edge electron pressure holds constant as n_e reduced
- Relative change in edge n_e larger than core

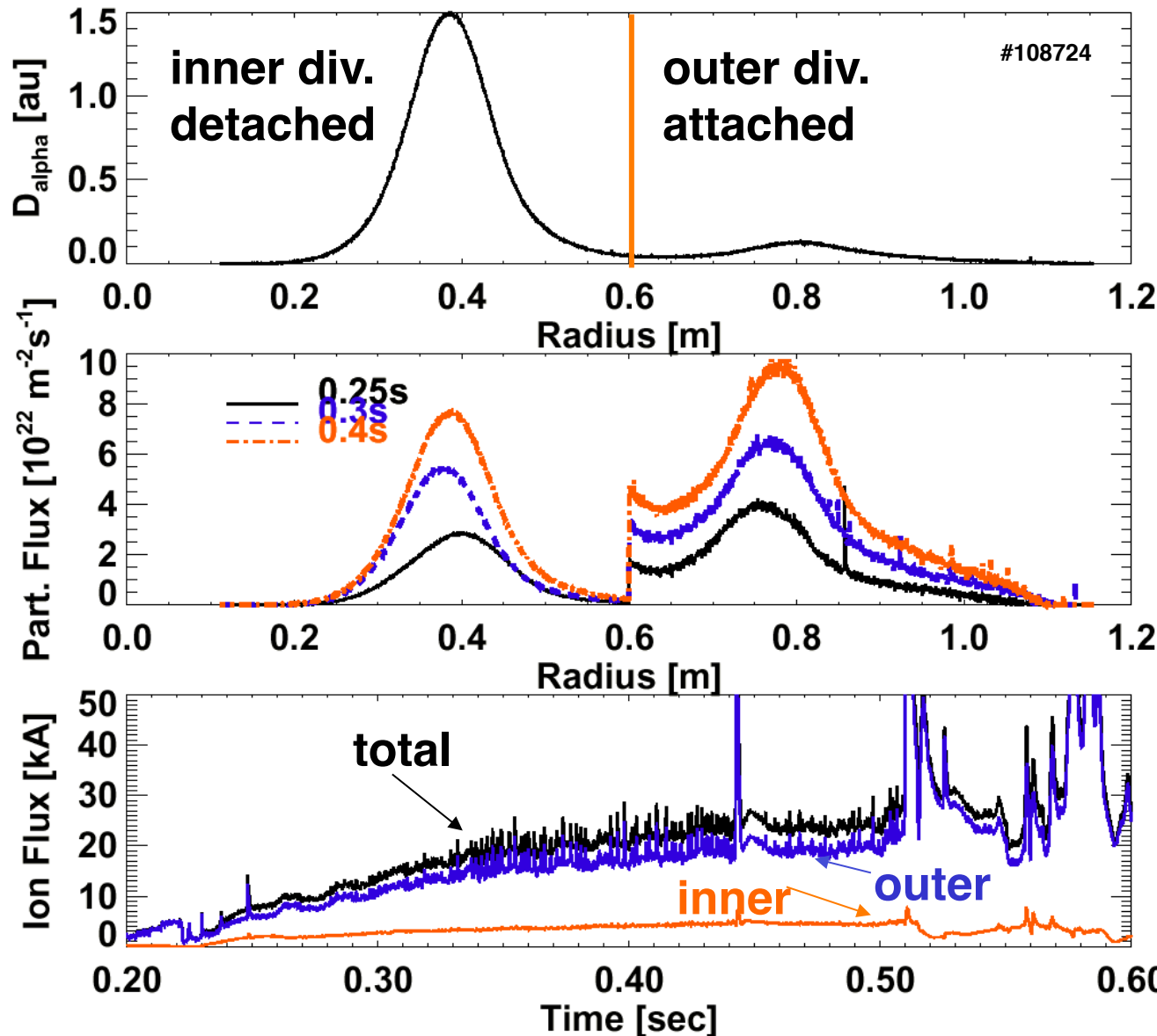


Particle Balance and Recycling Model - DIII-D cryopump



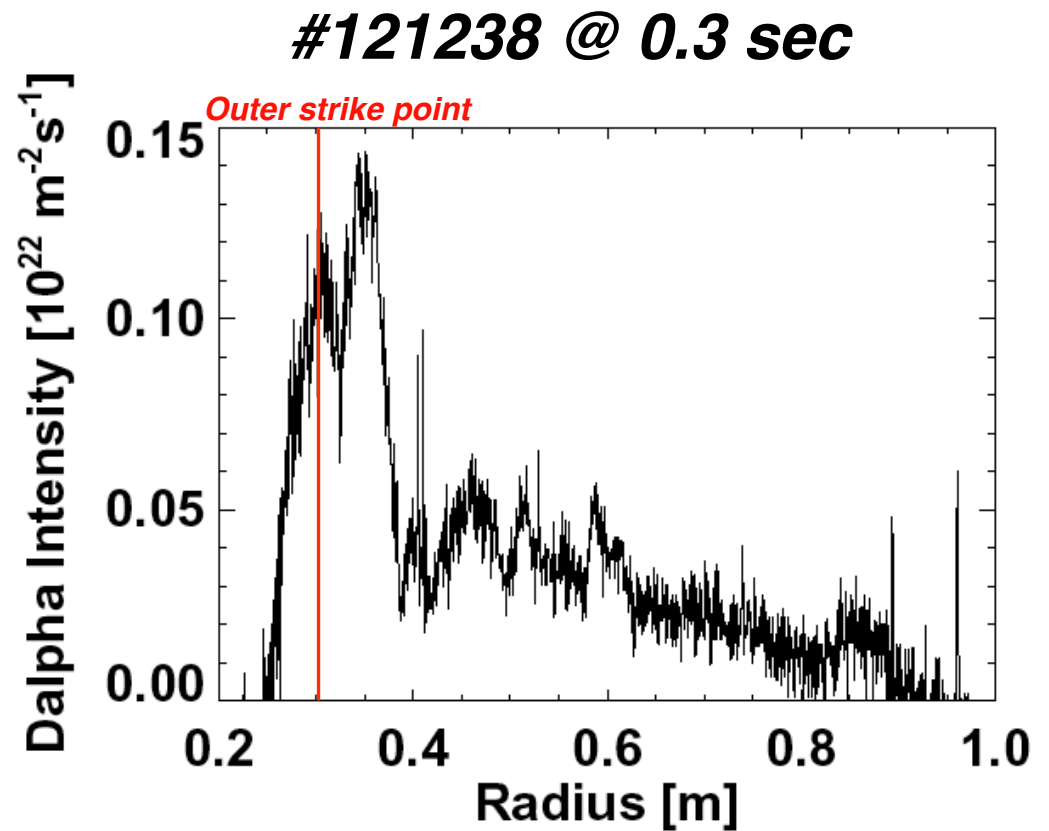
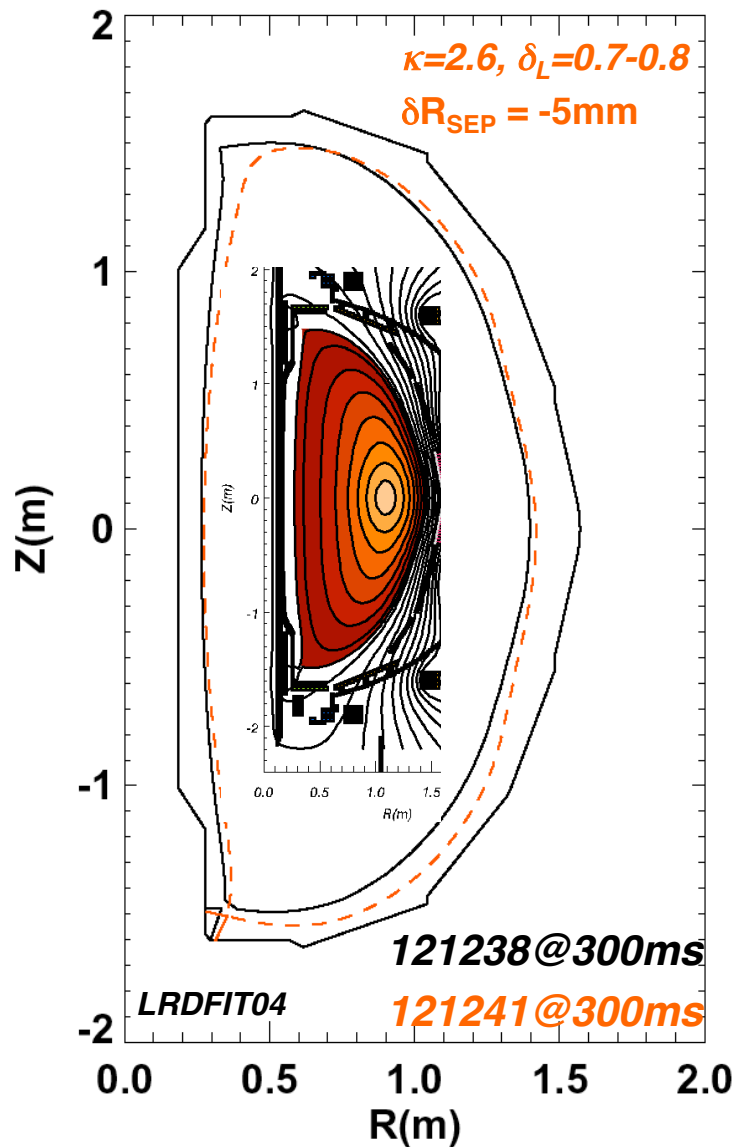
- DIII-D specific data:
 - $R_p \sim 0.98$ for carbon (reference?)
 - R_p changes slowly (Maingi, NF 1996)
 - $\eta_{core} \sim 0.05-0.15$ (Rensink, PoF B 1993)
 - $\eta_{pump} \sim 0.1$ (Maingi, NF 1999)
 - $\eta_{gas} \sim 0.1$ (Maingi, JNM 1997)
 - $\tau_p/\tau_E = 2.5$ (\sim Owen, JNM 1997)
- Solid η_{core} - fixed in time
 - N_e goes down on τ_p^* timescale
- Dashed $\eta_{core} \sim 1/n_e^2$
 - τ_p^* increases with time
 - N_e equilibrates faster than initial τ_p^*

NSTX D_α Peaked on Inboard Side, but Particle Flux Peaked on Outboard side because Inner Divertor is Usually Partially Detached



- Inner side detached
- Outer side attached
- Ions/ photon=1 (detach)
- Ions/ photon=20 (attach)
- Division at $R \sim 0.6$ m
- Out div. has ~ 4 x times current of inner div.

Broad SOL D_α profile in high δ (pf1a) #121238

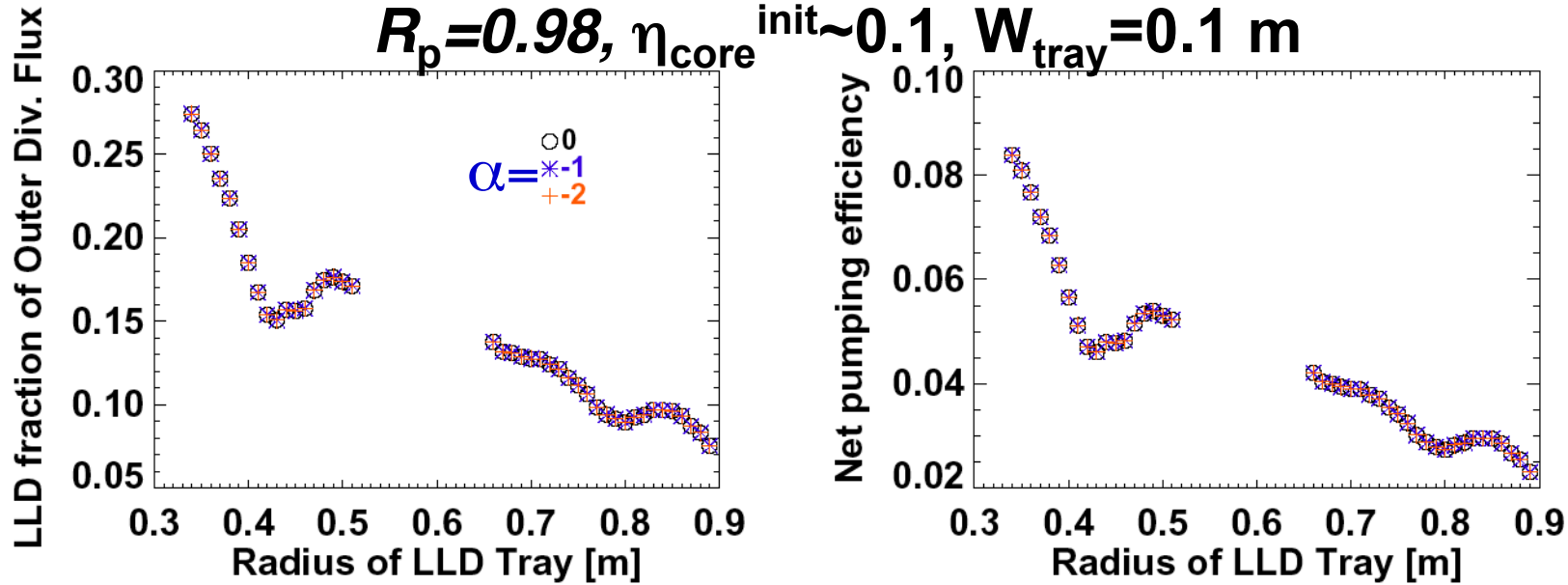


Soukhanovskii

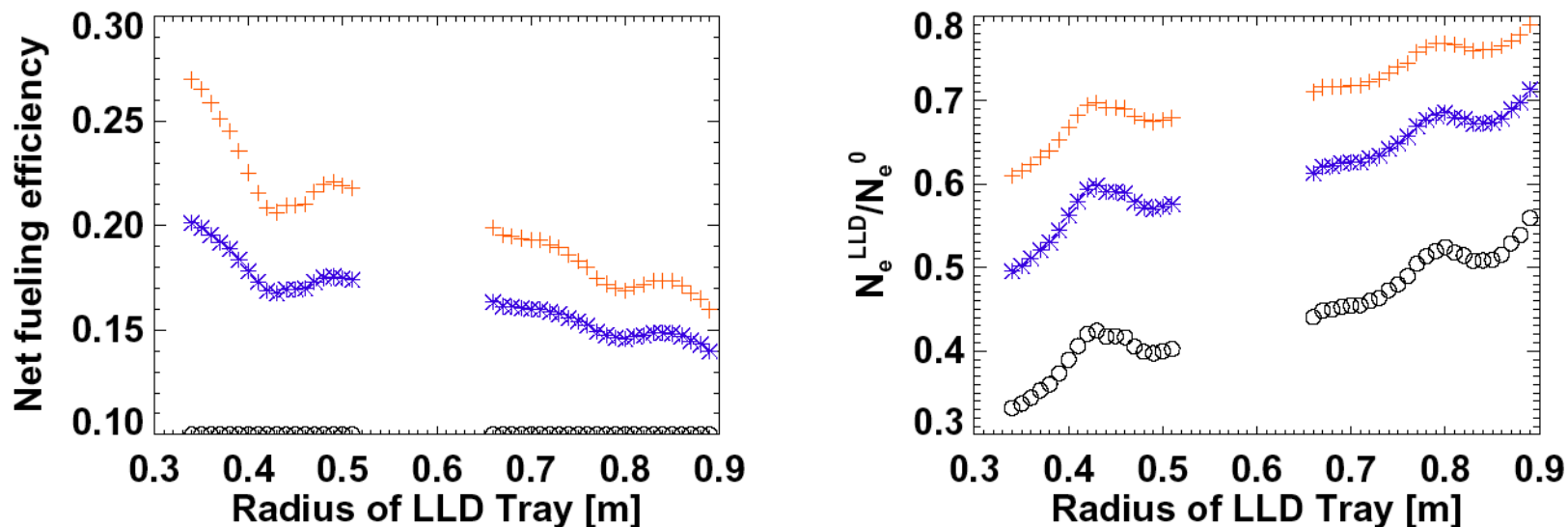
Achievable edge density reduction is reduced if core
 fueling efficiency $\eta_{\text{core}} \sim n_e^\alpha$



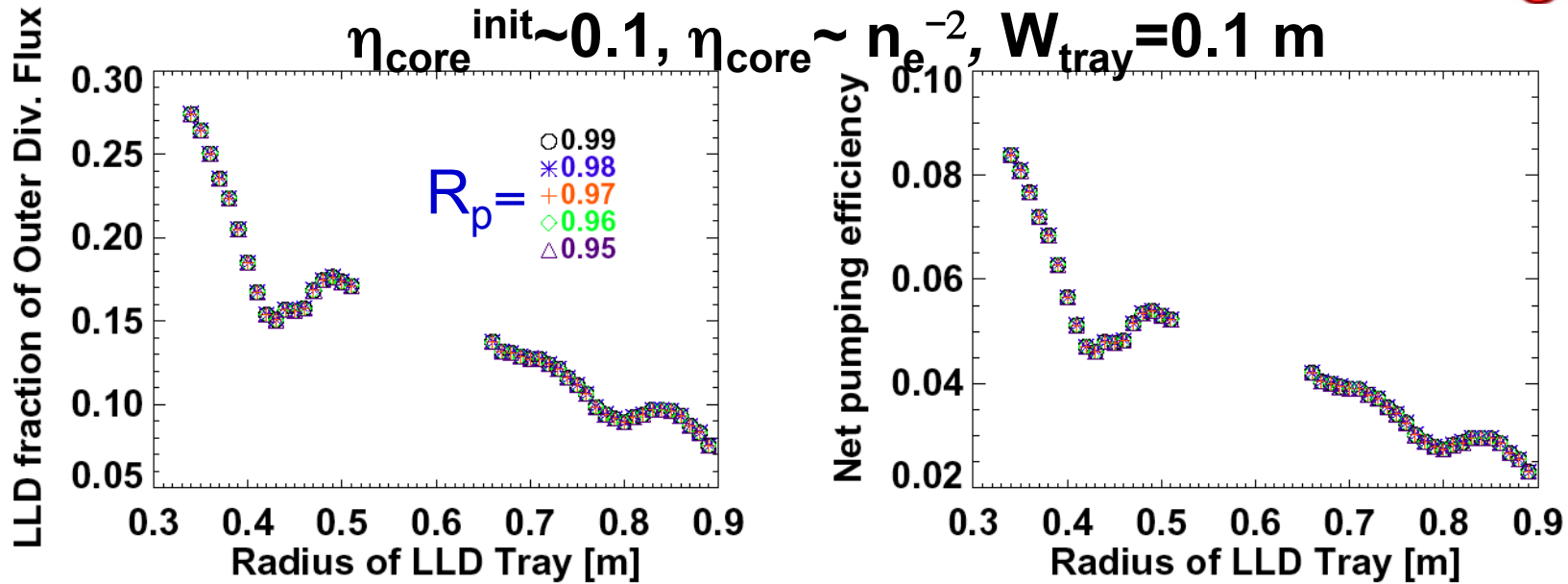
$R_p = 0.98, \eta_{\text{core}}^{\text{init}} \sim 0.1, W_{\text{tray}} = 0.1 \text{ m}$



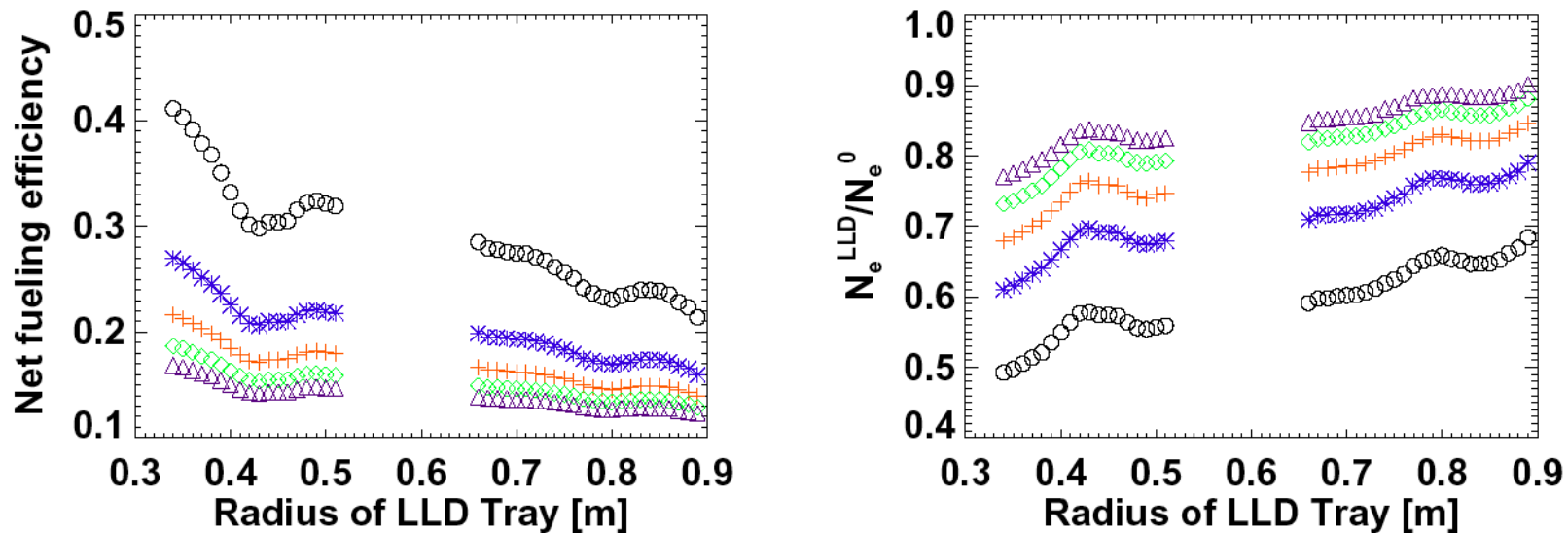
#121238 @ 0.3 sec



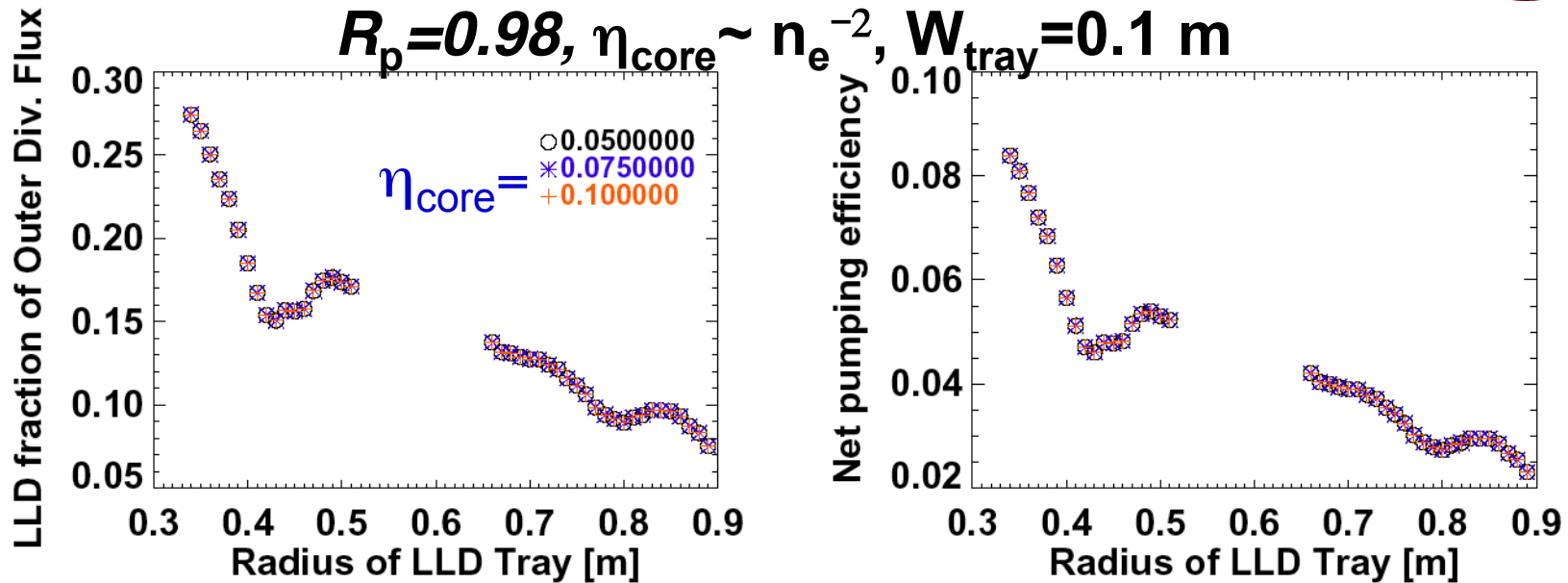
Achievable edge density reduction decreases with assumed initial wall recycling coefficient, R_p



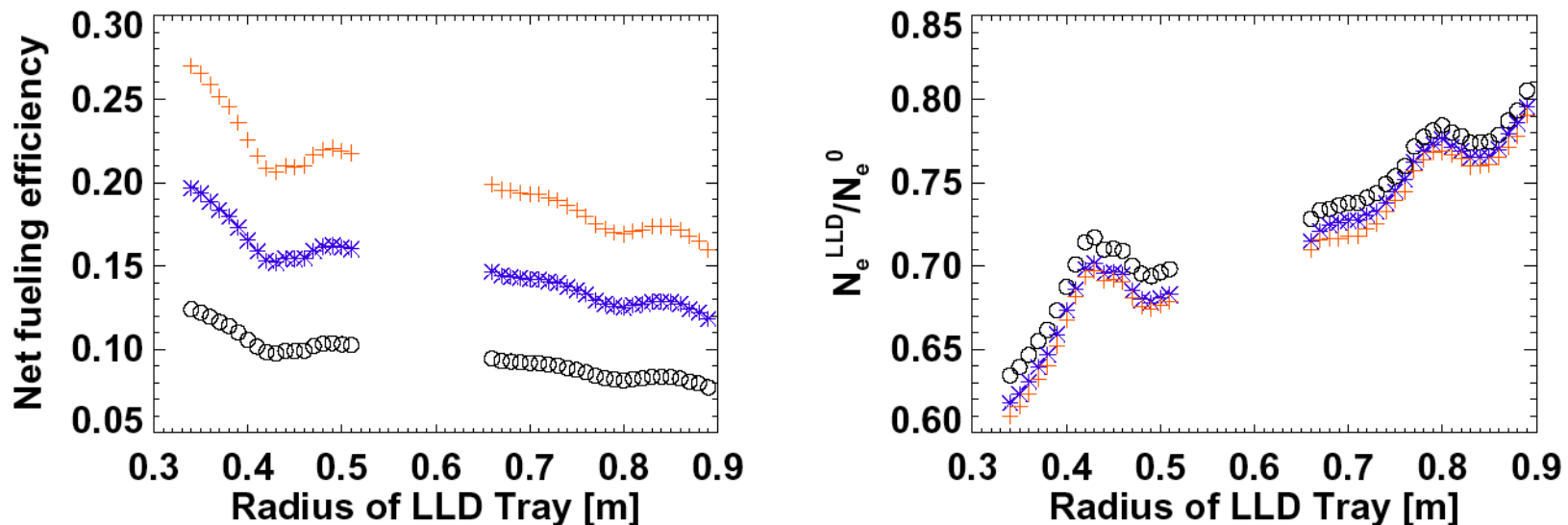
#121238 @ 0.3 sec



Achievable edge density reduction nearly independent of initial core fueling probability, η_{core}

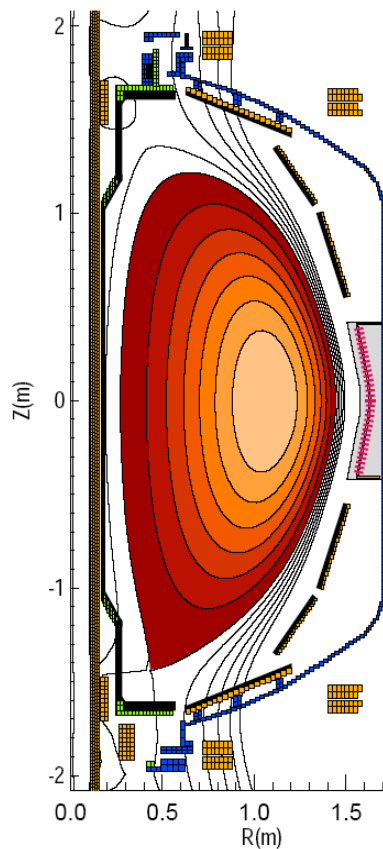


#121238 @ 0.3 sec



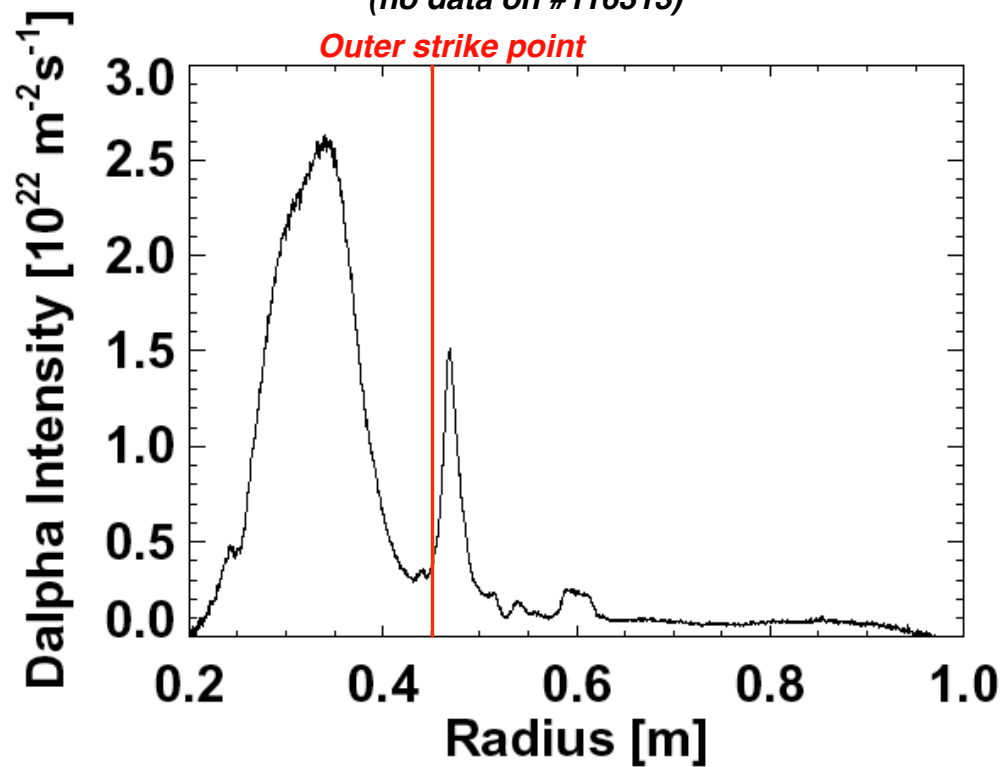
Narrow SOL D_α profile in medium δ (pf1b) #116318

Existing #116313
 $\kappa = 2.3$, $\delta_{X-L} = 0.75$
 $\delta R_{SEP} = -1\text{cm}$



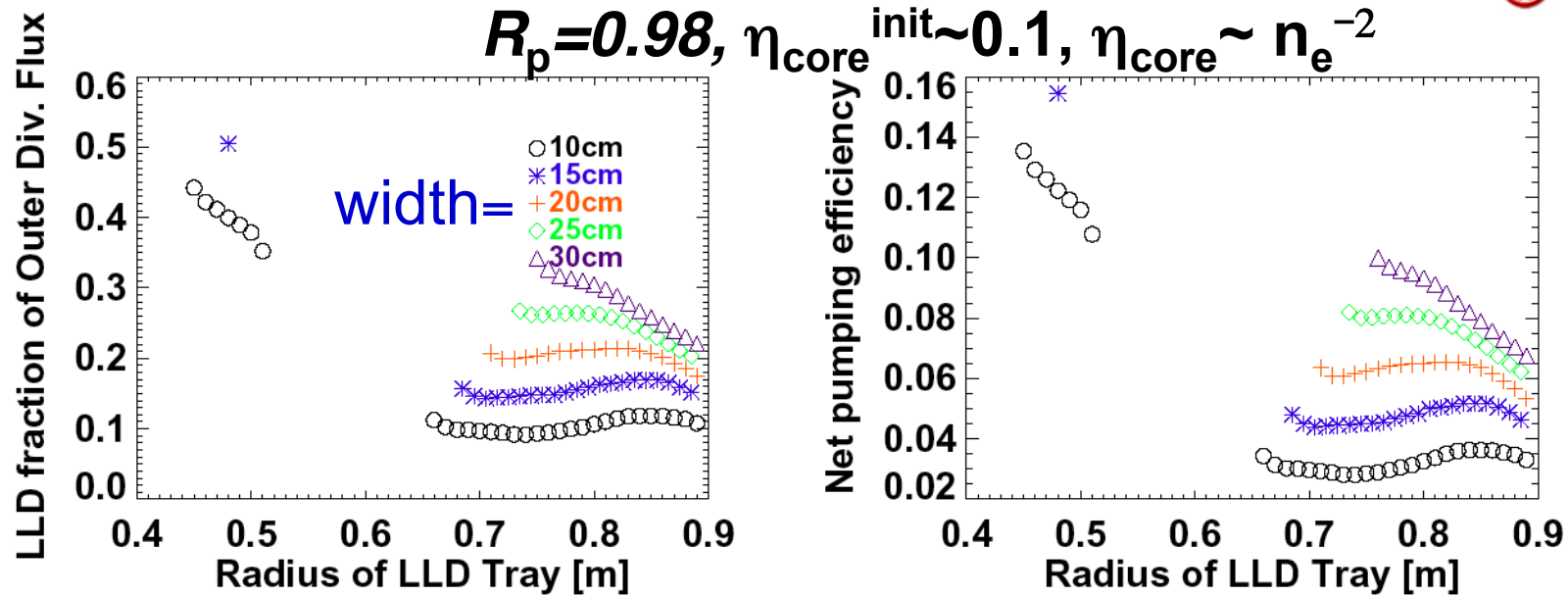
#116318 @ 0.6 sec

(no data on #116313)

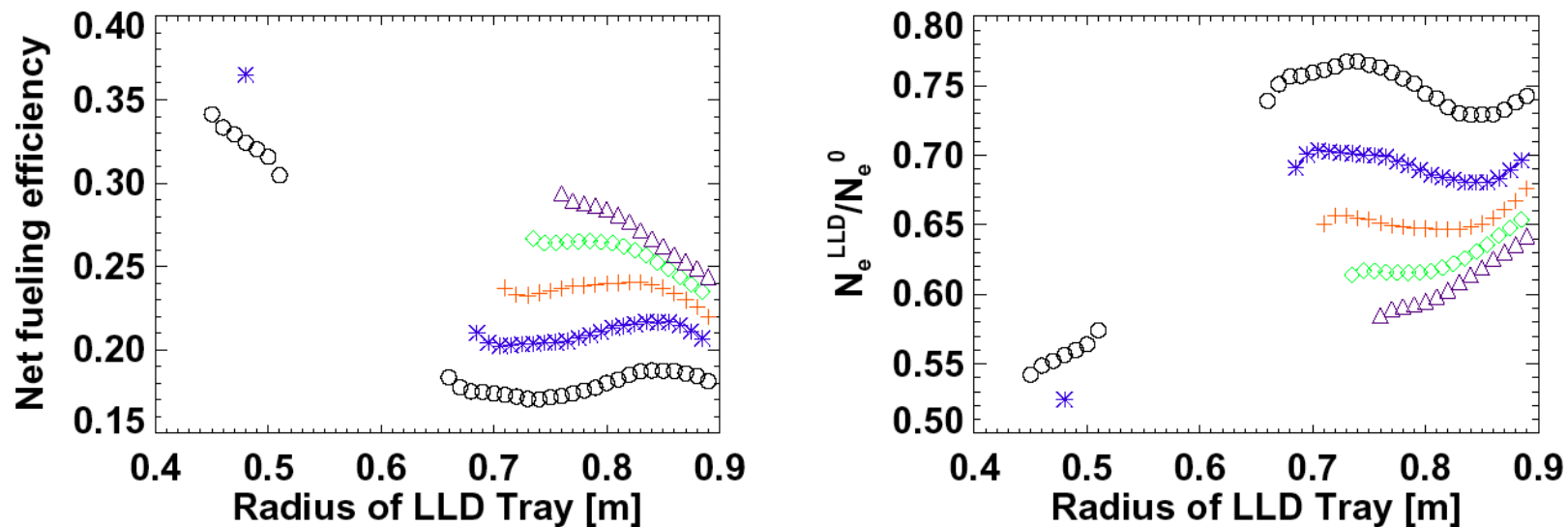


Soukhanovskii

Achievable edge density reduction depends on tray radius and width

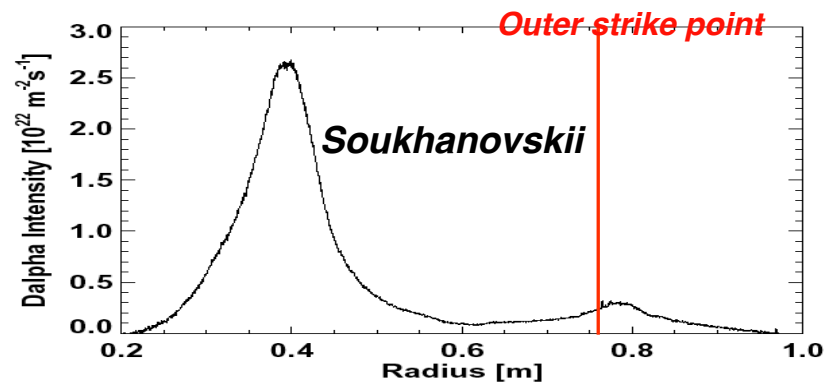
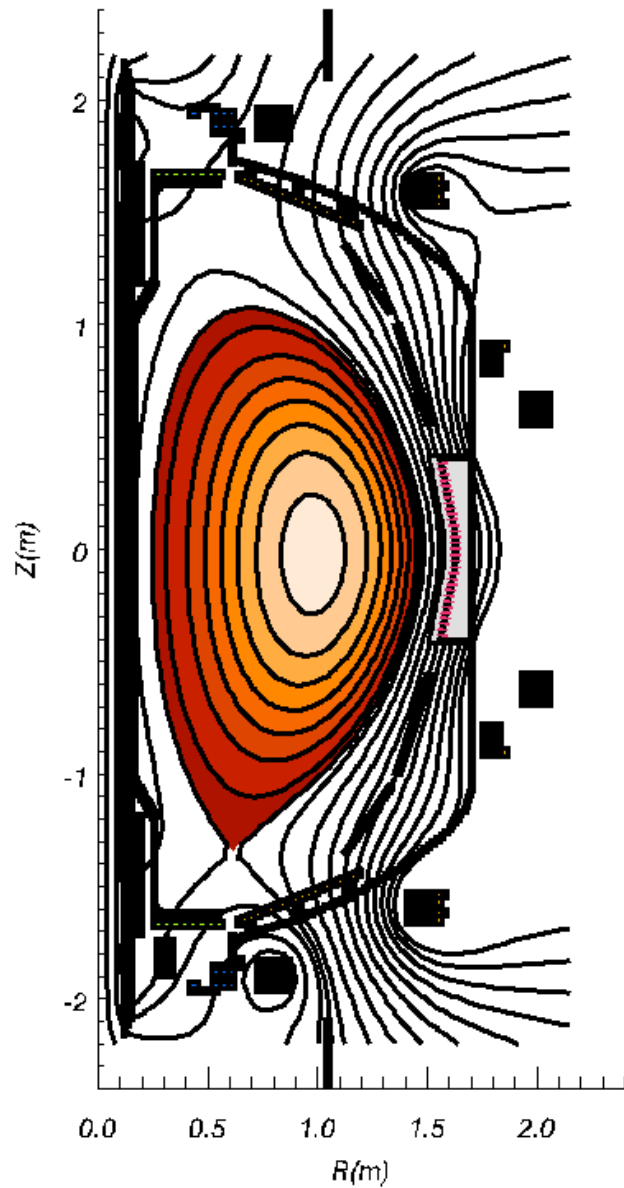


#116318 @ 0.6 sec

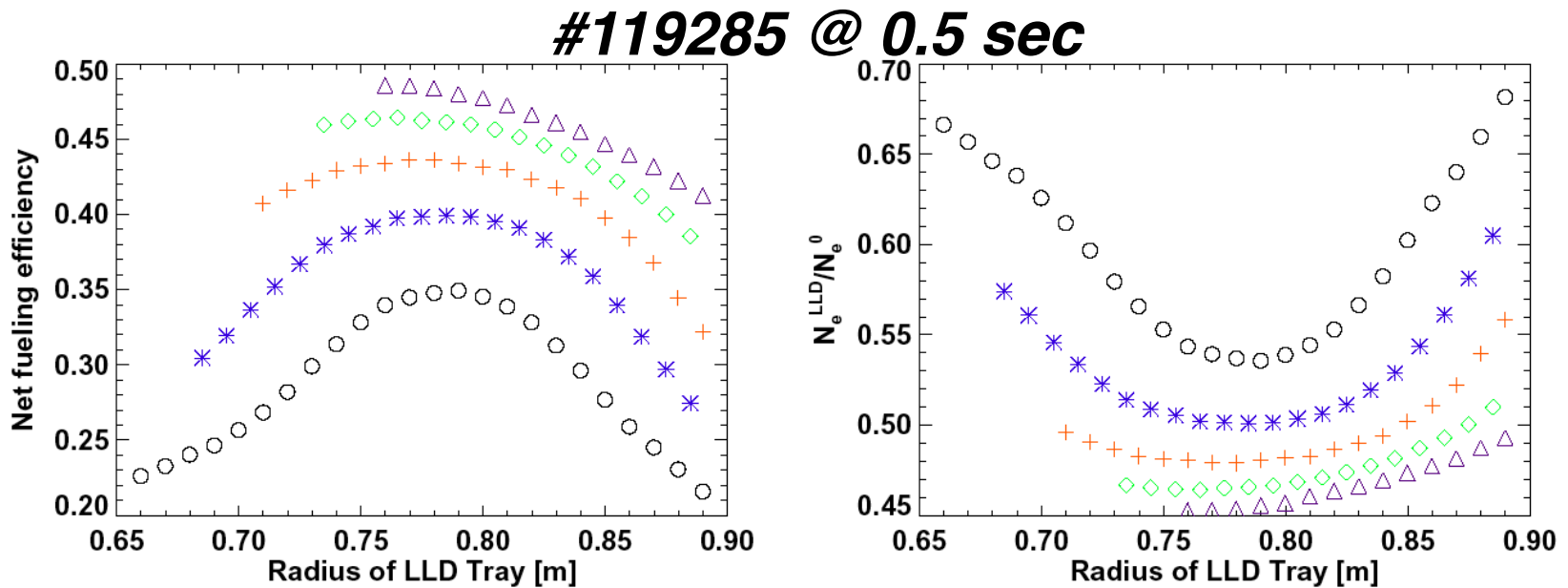
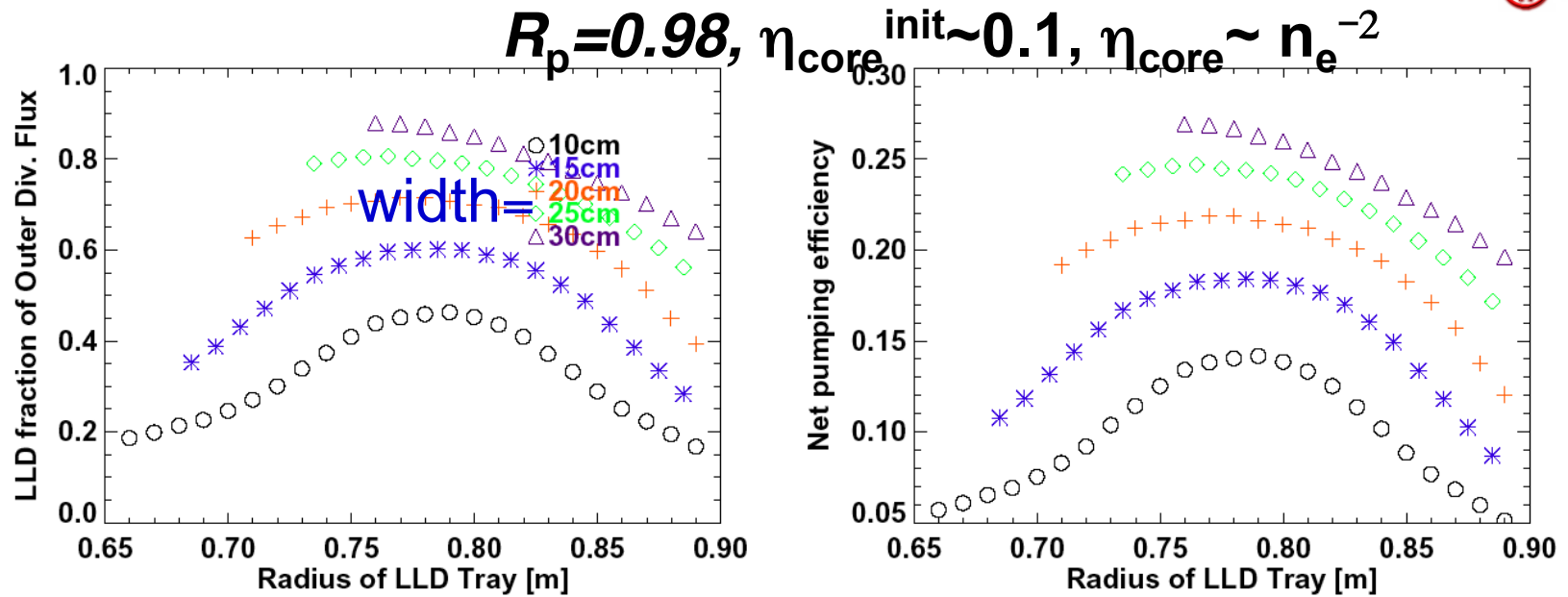


Narrow SOL D_α profile in low δ (pf2) #119285

Shot= 119285, time= 499ms



Achievable edge density reduction depends on tray radius and width



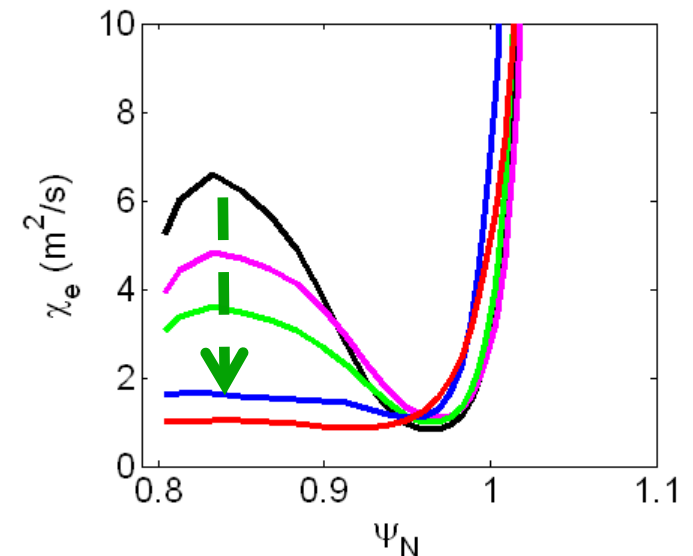
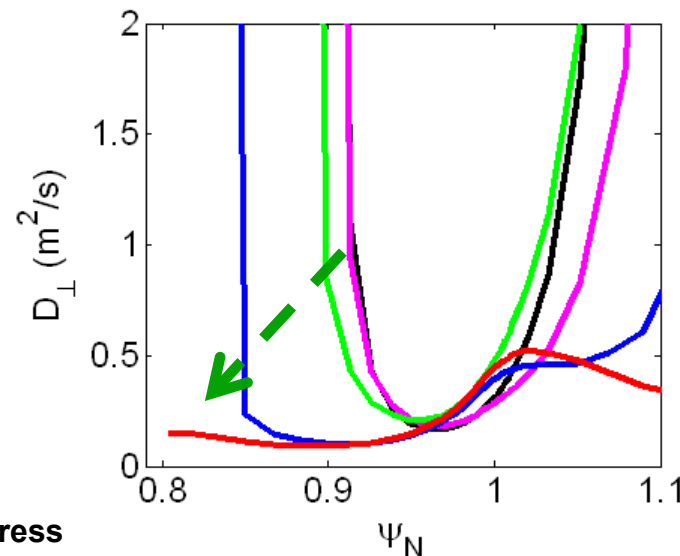
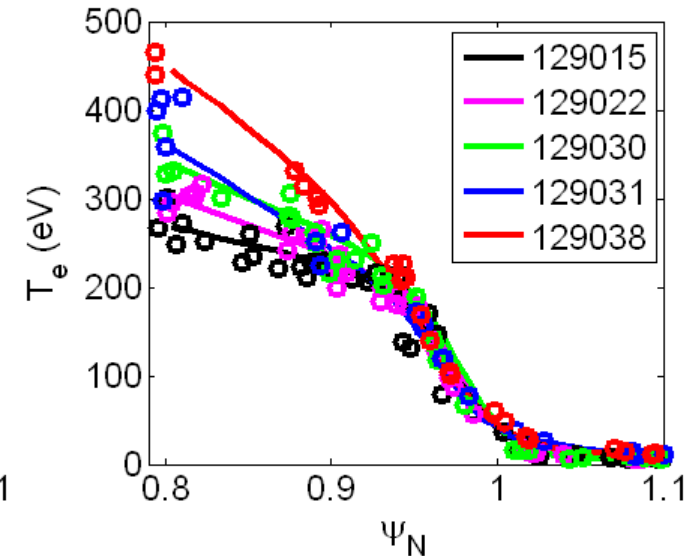
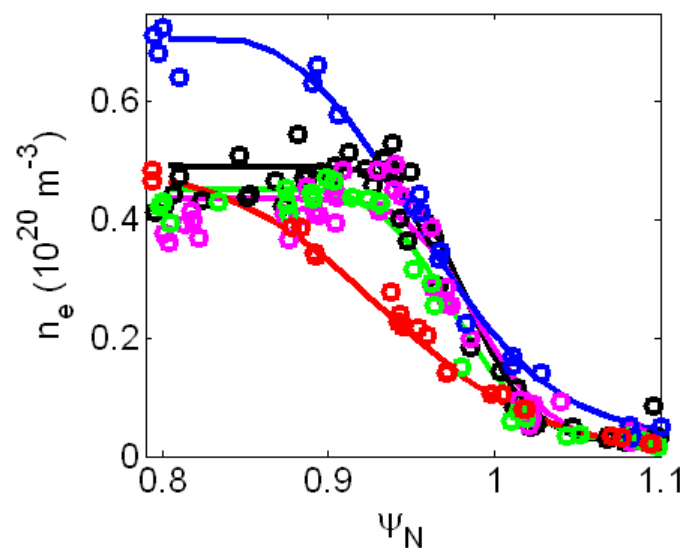
Discussion and Conclusions



- 20cm wide tray just outboard of the CHI gap likely to provide sufficient density reduction as required for long pulse high non-inductive fraction reported at the Dec. 2006 research forum
- To get a full 50% density reduction will probably require a tray near the outer strike point
 - Inboard of CHI gap for high δ discharges
 - Outboard of CHI gap for low δ discharges
- Actual density reduction factor depend strongly on how quickly core fueling efficiency increases with decreasing density, and the pre-Li global wall recycling coefficient
- Intend to compare with 2-D calculations, when available

Inner region: as lithium coatings thicken, transport barrier widens, pedestal-top χ_e reduced

- Several shots analyzed with increasing lithium thickness (direction of arrow) - ➔
- ELMy to reduced frequency to ELM-free



J. Canik PoP 2011 at press