

# Study of chirping Toroidicity-induced Alfvén Eigenmodes in the National Spherical Torus Experiment

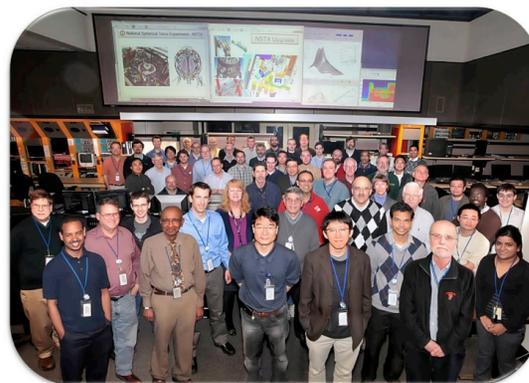
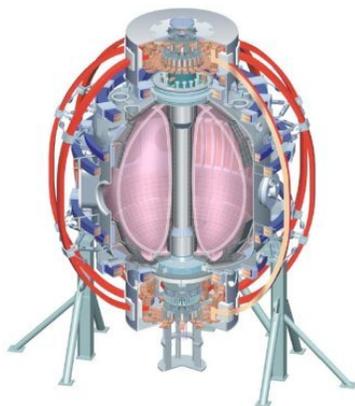
**Mario Podestà**

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*and the NSTX Research Team*

**12<sup>th</sup> IAEA technical meeting on Energetic Particles in  
magnetic confinement systems**

**Austin, TX  
Sep. 7-10, 2011**

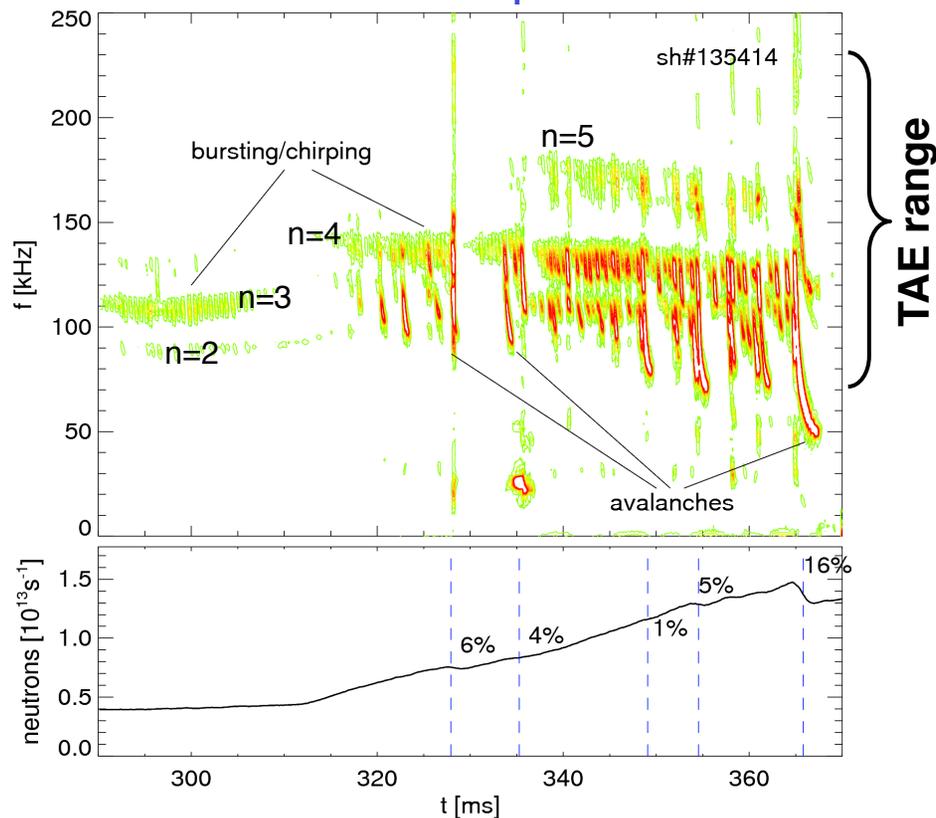


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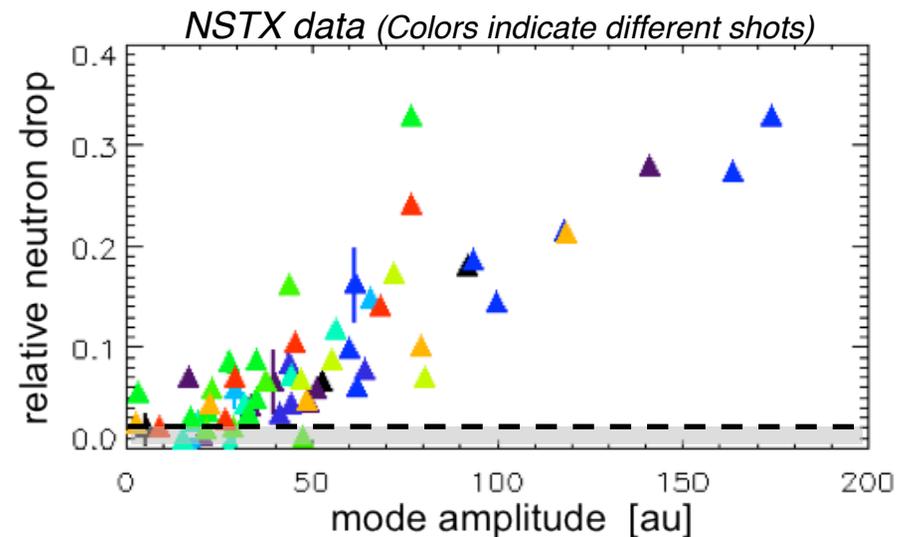
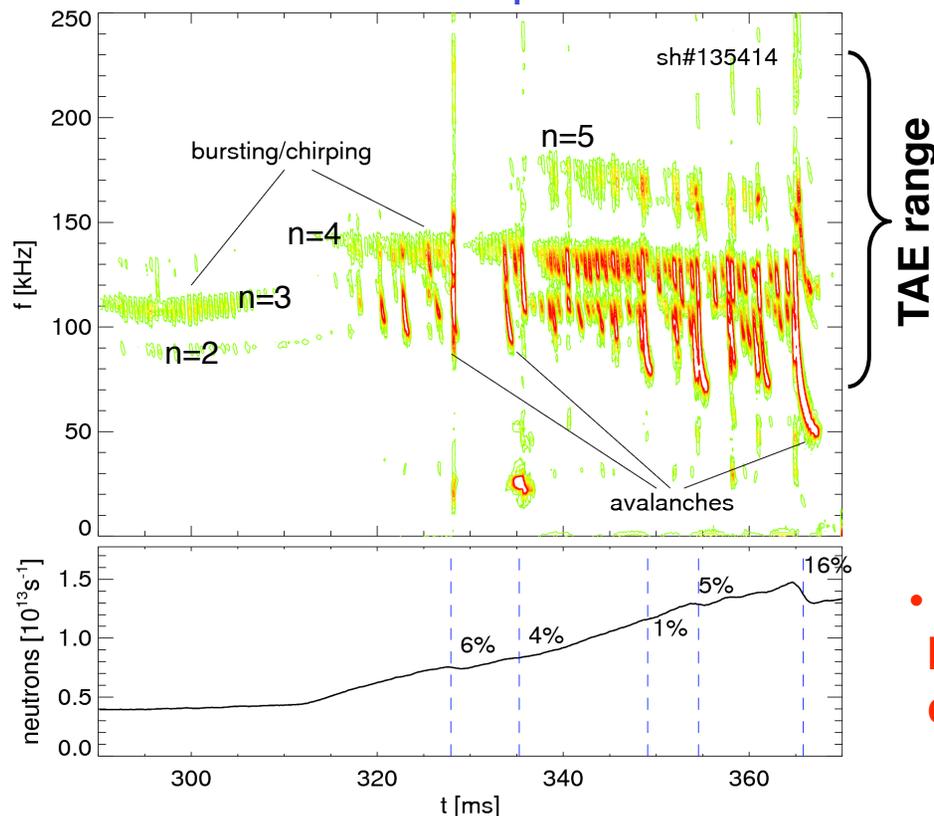
# Bursting toroidicity-induced Alfvén eigenmodes (TAEs) can lead to enhanced fast-ion transport

- Multiple TAEs can be simultaneously destabilized
  - Possible overlap of many resonances in phase space
  - Non-linear development into “TAE *avalanches*”



# Bursting toroidicity-induced Alfvén eigenmodes (TAEs) can lead to enhanced fast-ion transport

- Multiple TAEs can be simultaneously destabilized
  - Possible overlap of many resonances in phase space
  - Non-linear development into “TAE *avalanches*” -> fast ion losses



- Need to understand the physics of bursting TAEs, improve predictive capability for future devices (ITER)

**Spherical tokamaks such as NSTX provide excellent test-bed**

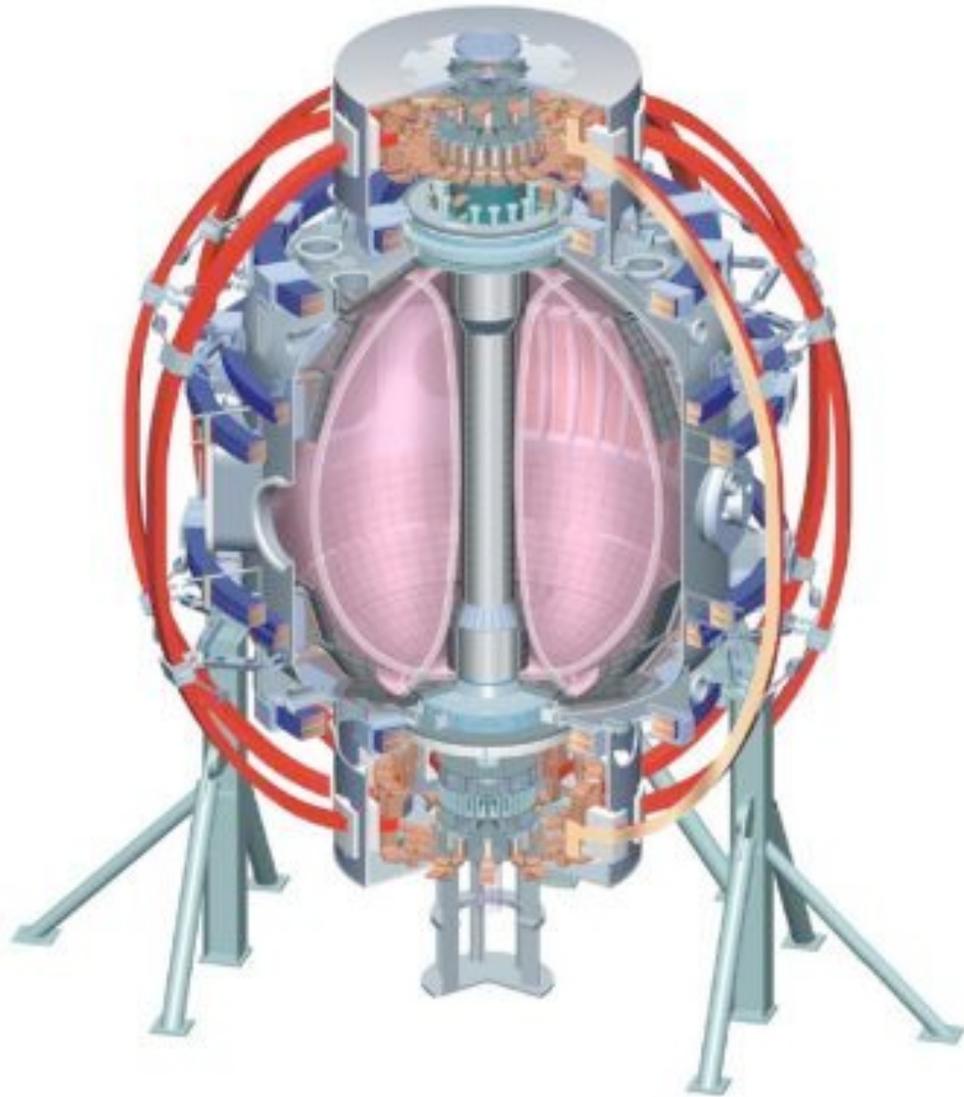
# Outline

- Experimental scenario, diagnostics
- General features of TAEs on NSTX
  - Frequency, amplitude dynamics
  - Mode structure
  - Role of fast ion drive
- Non-linear dynamics, mode-mode coupling
- Summary and open issues

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# NSTX parameters

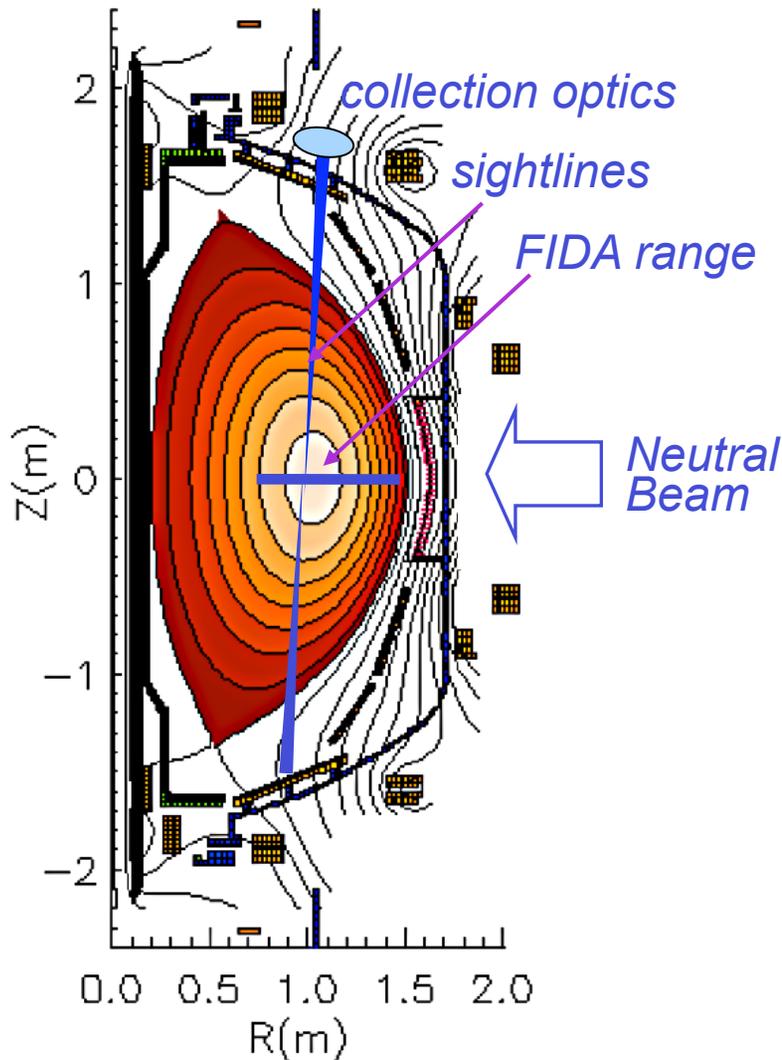


Major radius	0.85 m
<b>Aspect ratio</b>	1.3
Elongation	2.7
Triangularity	0.8
Plasma current $\sim 1$ MA	
<b>Toroidal field</b>	$< 0.55$ T
Pulse length	$< 2$ s
<b>3 Neutral Beam sources</b>	
$P_{\text{NBI}} \leq 6$ MW, $E_{\text{injection}} \leq 95$ keV	
$1 < v_{\text{fast}}/v_{\text{Alfvén}} < 5$	

***This work:***  
***Focus on TAEs in L-mode plasma***  
***Center-stack limited***  
***Deuterium plasma***  
 **$B_{\text{tor}} = 0.55$  T,  $I_p = 0.7-0.9$  MA**

# Mode activity and fast ion diagnostics on NSTX

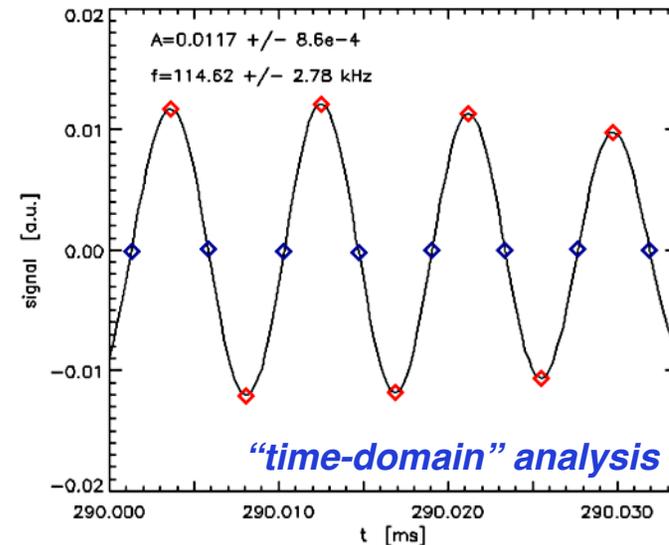
shot#135404, t=320 ms



- Mirnov coils
  - Magnetic fluctuations up to 2.5 MHz
- Multi-channel reflectometer
  - Mode structure (monotonic profiles)

UCLA

FFT analysis complemented by analysis in time domain to study mode dynamics over short time scale



UCIrvine  
University of California, Irvine

- Fast Ion diagnostics
  - Fast Ion D-Alpha systems (fast ion radial profile and spectrum)
  - Neutral Particle Analyzers, Fast Ion Loss probe, neutron rate

# Experimental scenario :

$P_{NB} < 3\text{MW}$ ,  $n_e \sim 3\text{-}4 \times 10^{19}\text{m}^{-3}$ ,  $T_i \sim T_e = 1\text{-}1.5\text{keV}$

- NB-heated, L-mode plasmas

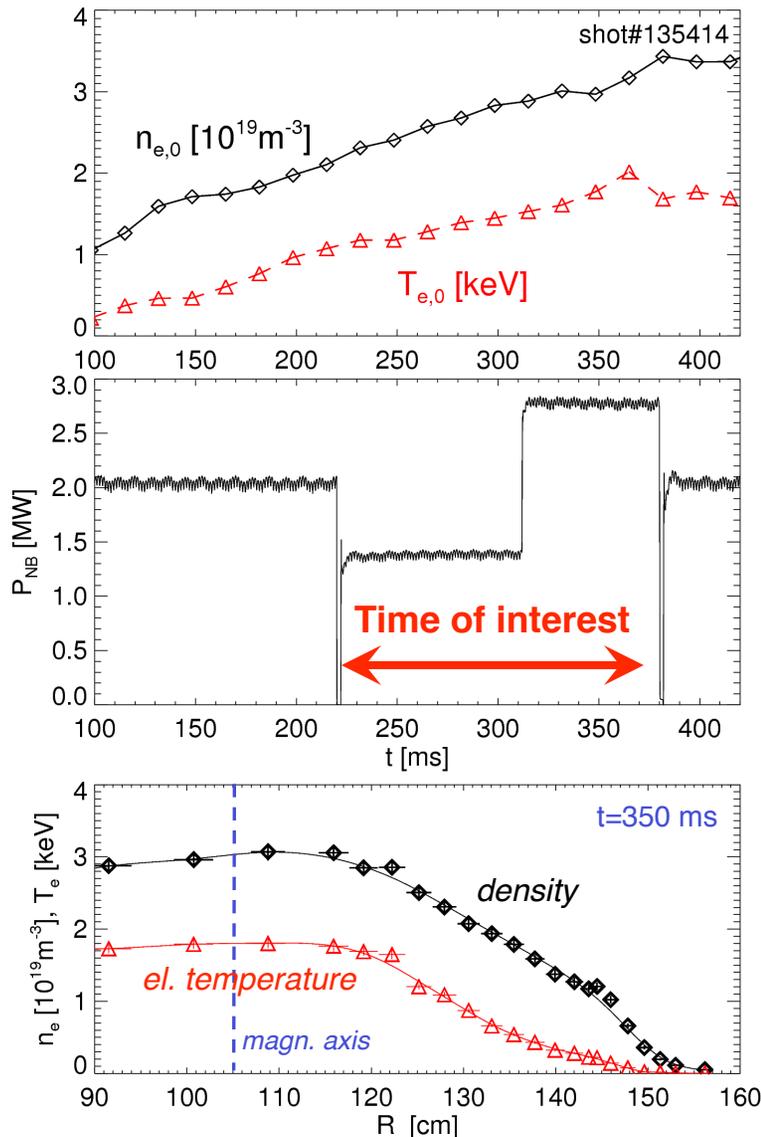
- Plasma limited on center-stack
- NB power and timing varied to affect mode stability

- Plasma profiles evolving in time

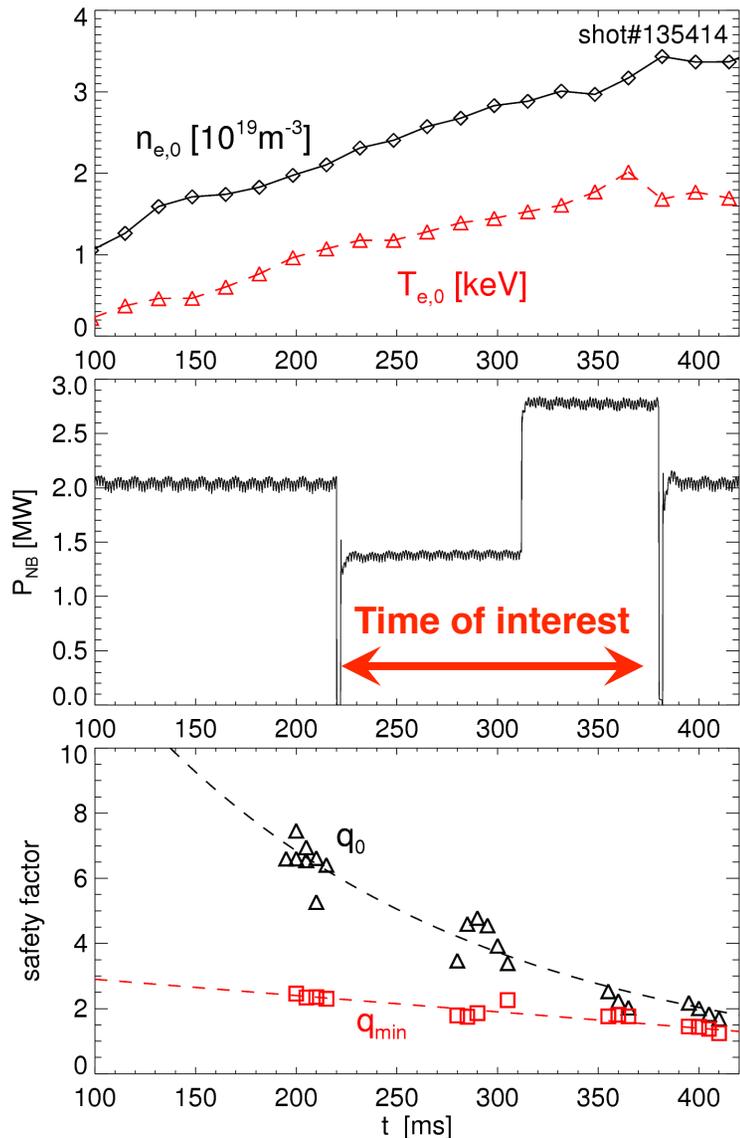
- > Monotonic, centrally peaked: OK for reflectometer measurements

- Central plasma rotation up to 40kHz

- > Large Doppler shift of mode frequency



# Safety factor profile evolves from strongly to slightly-reversed shear



- NB-heated, L-mode plasmas

- Plasma limited on center-stack
- NB power and timing varied to affect mode stability

- Plasma profiles evolving in time

- Reversed-shear  $q$  profile

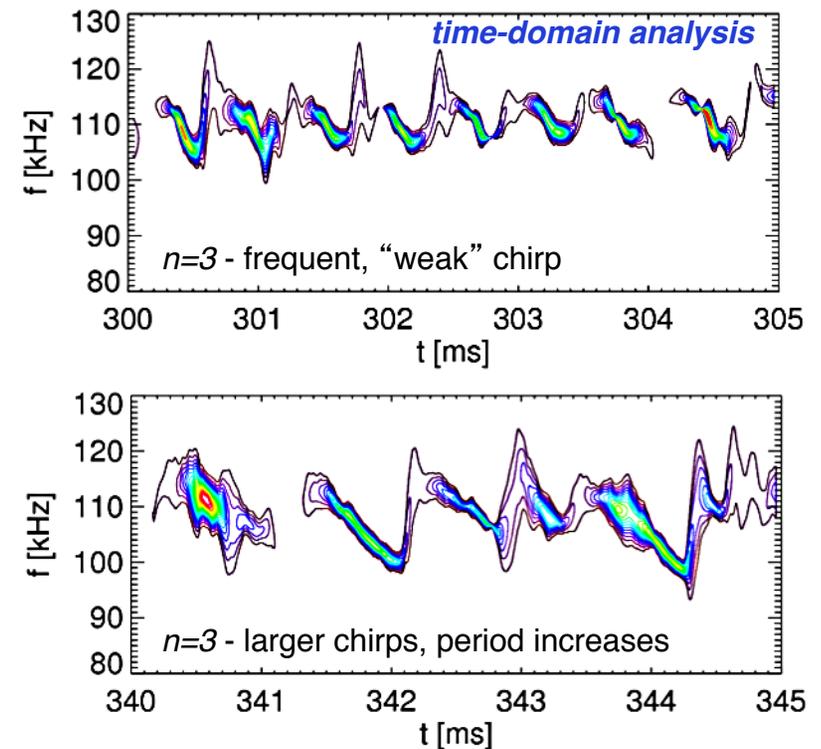
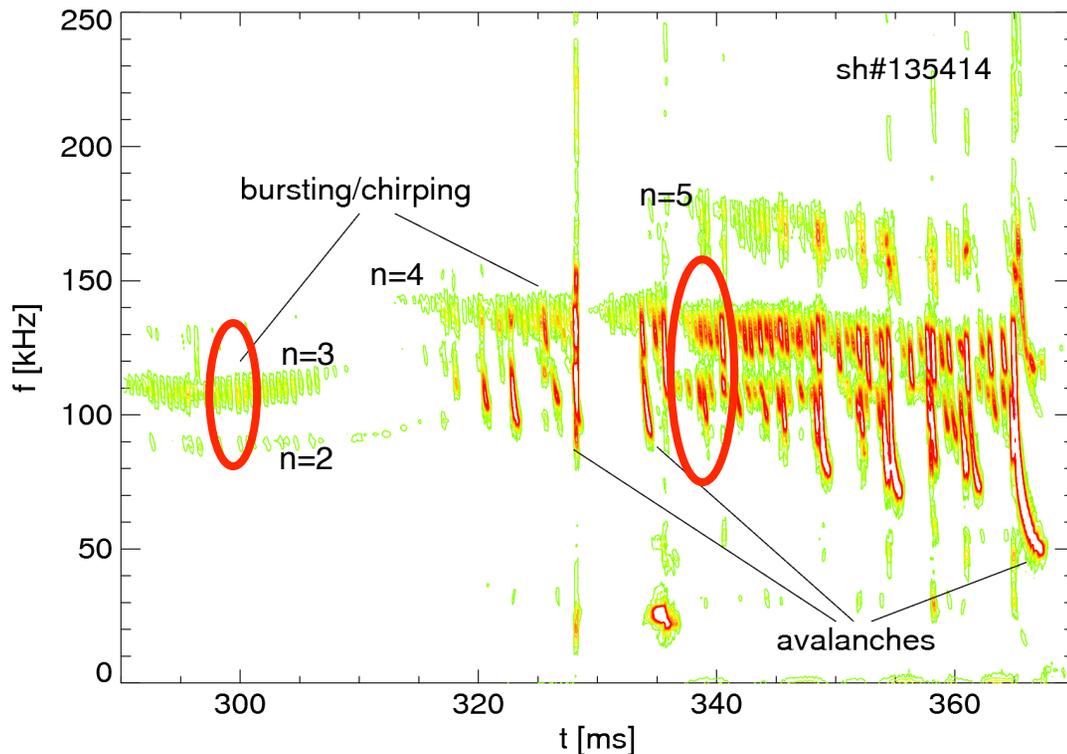
>  $q_{\text{min}} \sim 1$  toward end of discharge

- Safety factor evolution reconstructed through LRDFIT code constrained by MSE data

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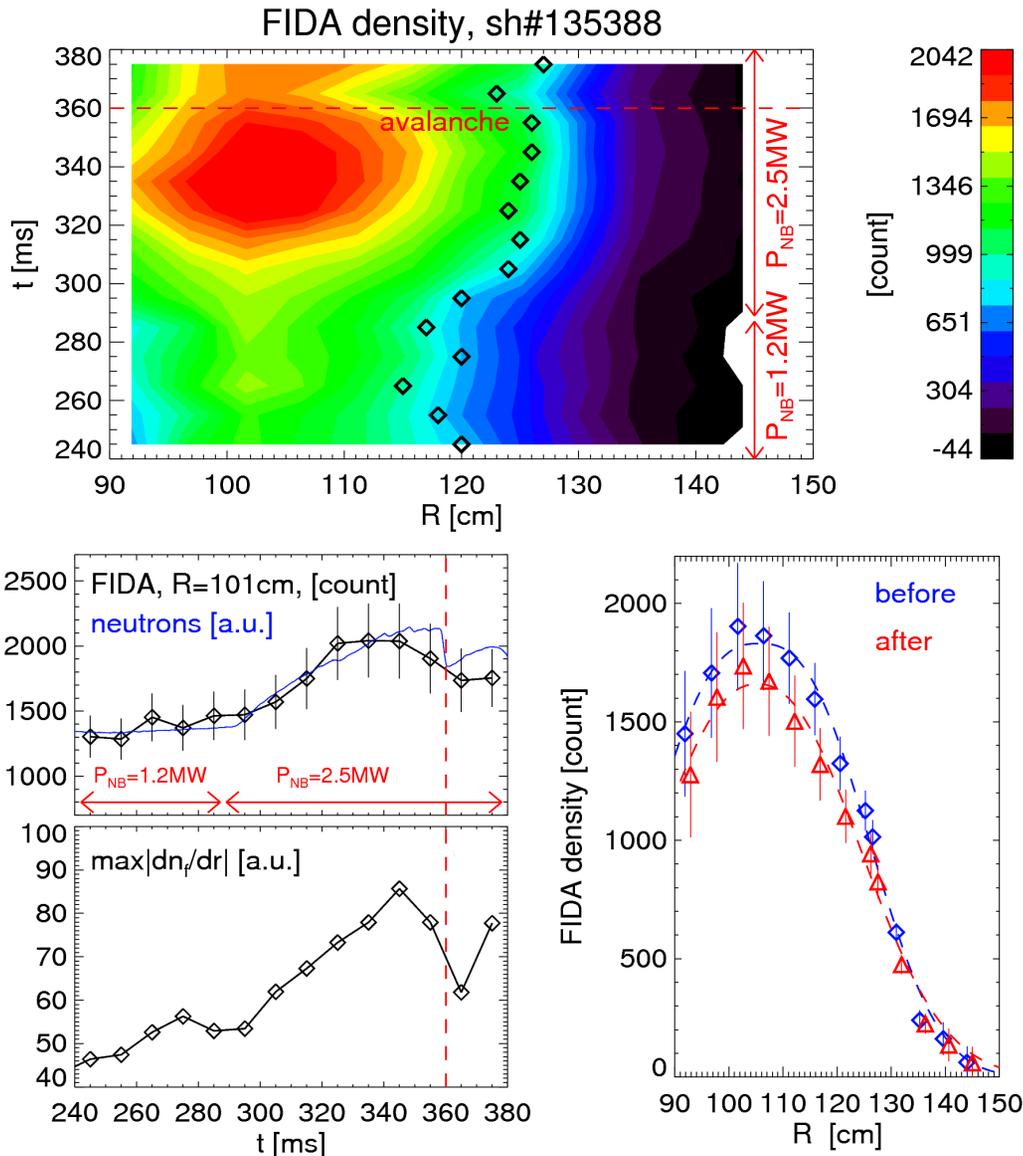
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# TAEs with low-intermediate toroidal mode number ( $n=2 \rightarrow 7$ ) are observed, with dominant $n=2-4$ modes



- Burst separation 0.5 – 2 ms
  - No systematic variation with  $n_e$ ,  $T_e$ ,  $P_{NB}$ , ...
  - Frequency evolution does not follow unique patten (e.g.  $t^{-1/2}$ , linear, exponential)
- Usually, each mode chirps independently of the others...
- ... but, eventually, *avalanches* occur:
  - Drop in neutron rate, FIDA

# Up to ~30% of fast ions can be lost during a single TAE avalanche



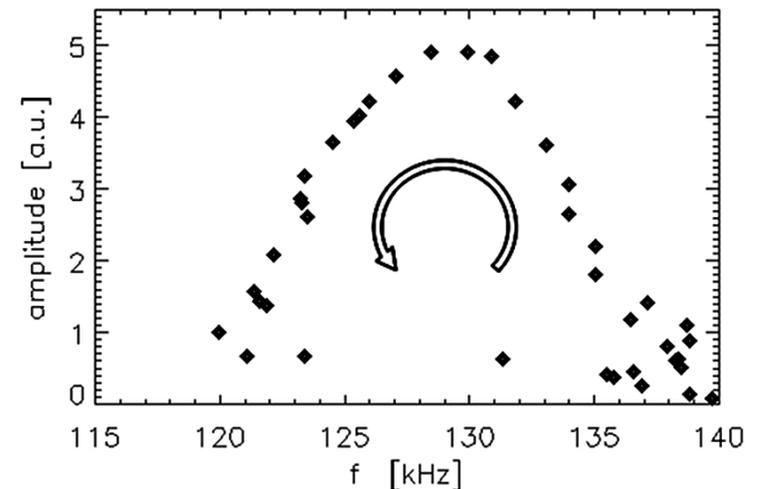
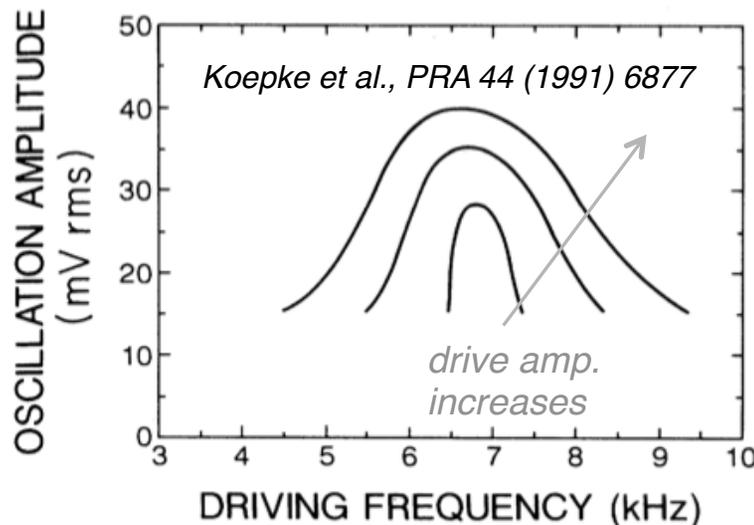
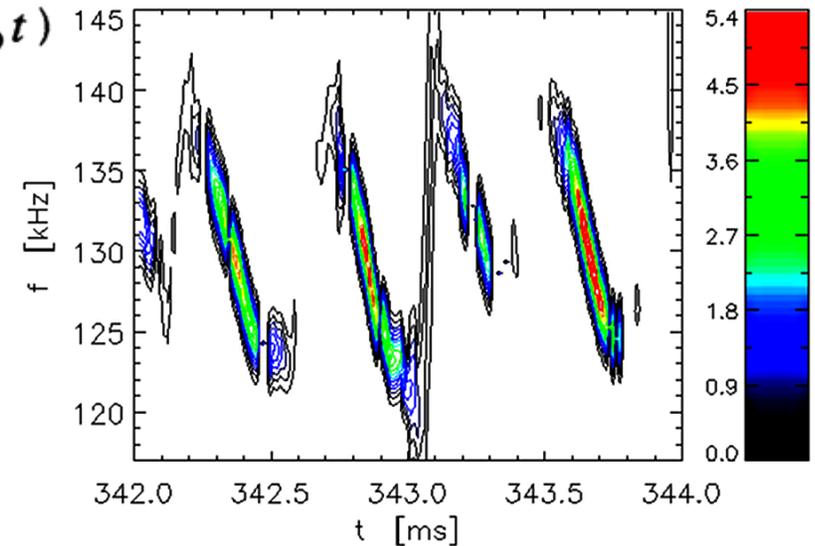
# Frequency vs. amplitude are correlated; reminiscent of driven, non-linear system

- E.g., non-linear Van der Pol oscillator:

$$\ddot{x} - \epsilon(1 - \beta x^2)\omega_0 \dot{x} + (\omega_0^2 + \eta x^2)x = M\omega_0^2 \sin(\omega_D t)$$

damping      'non-linearity' factor      'restoring' term      driving force

- Can get info on damping, drive (resonant) frequency and their temporal variations?
- Comparison with chirping TAE data under way



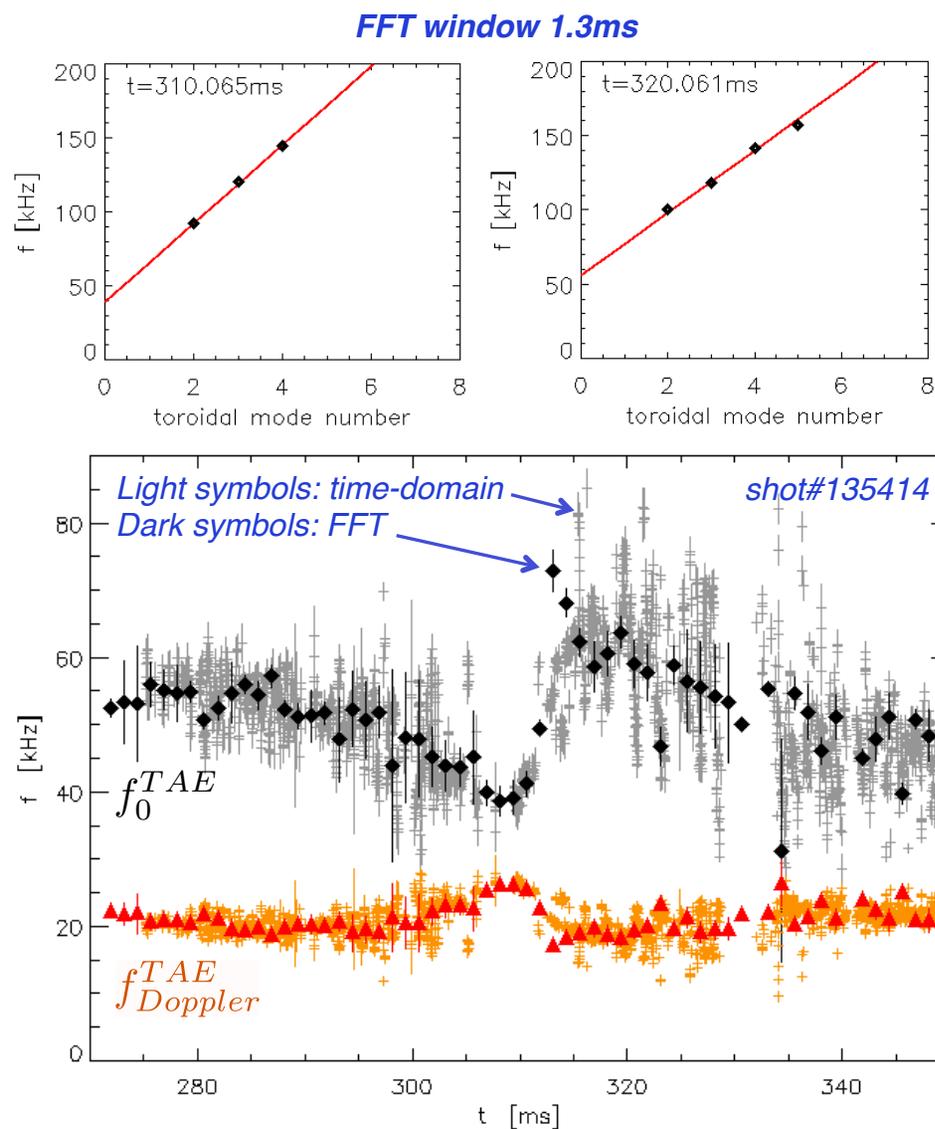
# On average, TAE frequencies are consistent with a common frequency *in the plasma frame*

Measured frequency consistent with:

$$f_{lab,n}^{TAE} = f_0^{TAE} + n f_{Doppler}^{TAE}$$

↓ lab frame    
 ↓ plasma frame    
 ↓ shift from plasma rotation

- Valid for time scales >1 ms
- In general, each mode shows a different sub-millisecond dynamic



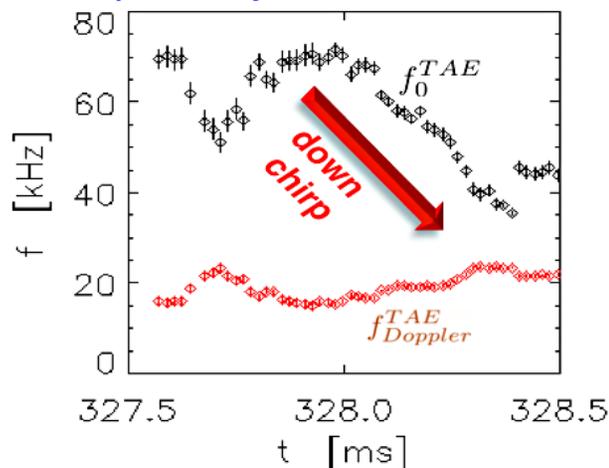
# On average, TAE frequencies are consistent with a common frequency *in the plasma frame*

Measured frequency consistent with:

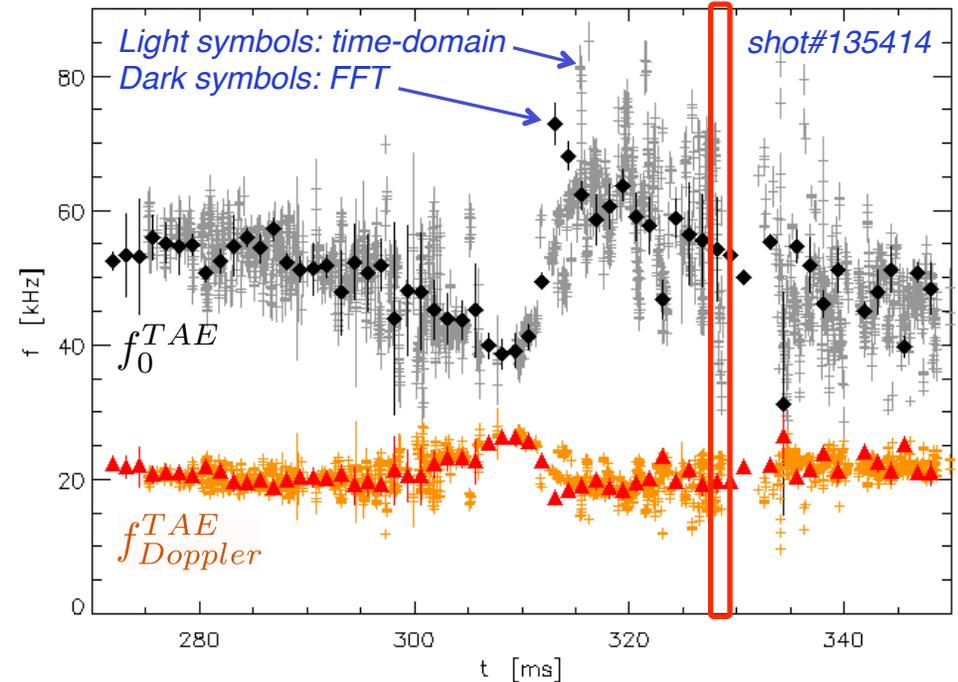
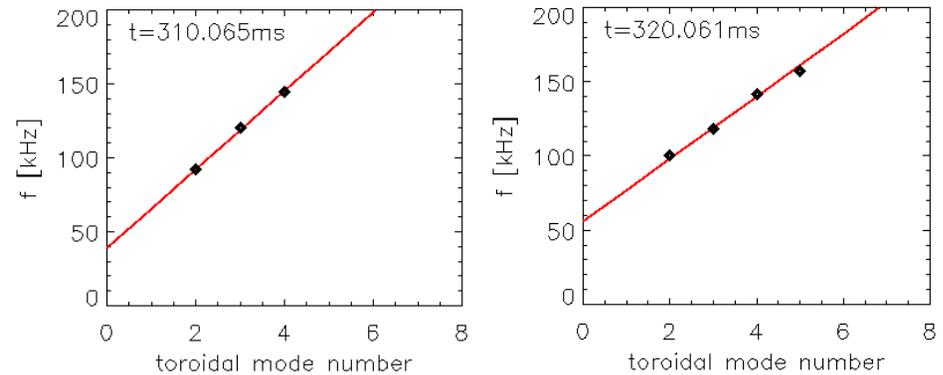
$$f_{lab,n}^{TAE} = f_0^{TAE} + n f_{Doppler}^{TAE}$$

↓ lab frame    
 ↓ plasma frame    
 ↓ shift from plasma rotation

- Valid for time scales >1 ms
- In general, each mode shows a different sub-millisecond dynamic...
- ...except during large bursts:
  - Doppler shift only slightly changed here
  - Chirp mainly due to decrease in  $f_0^{TAE}$



FFT window 1.3ms

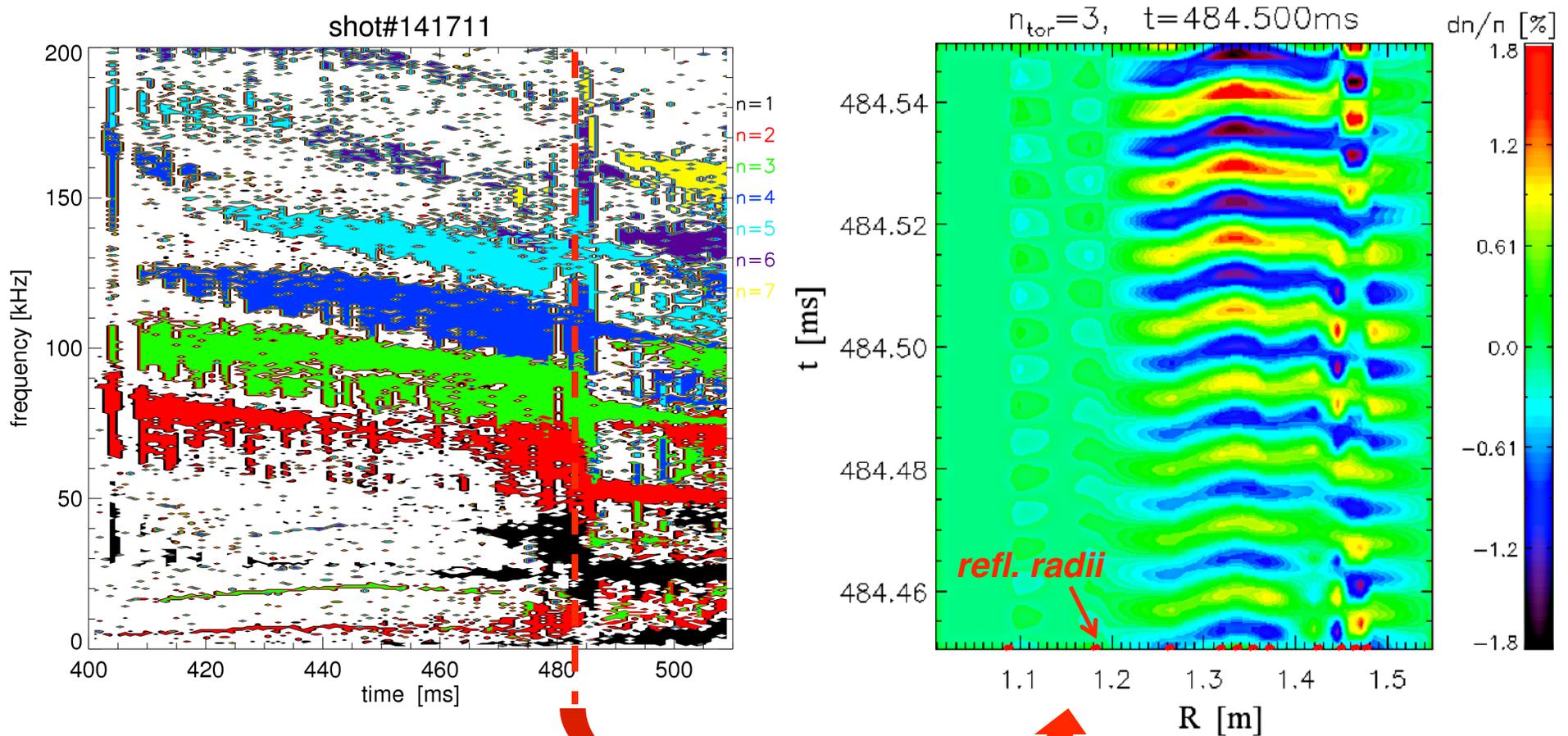


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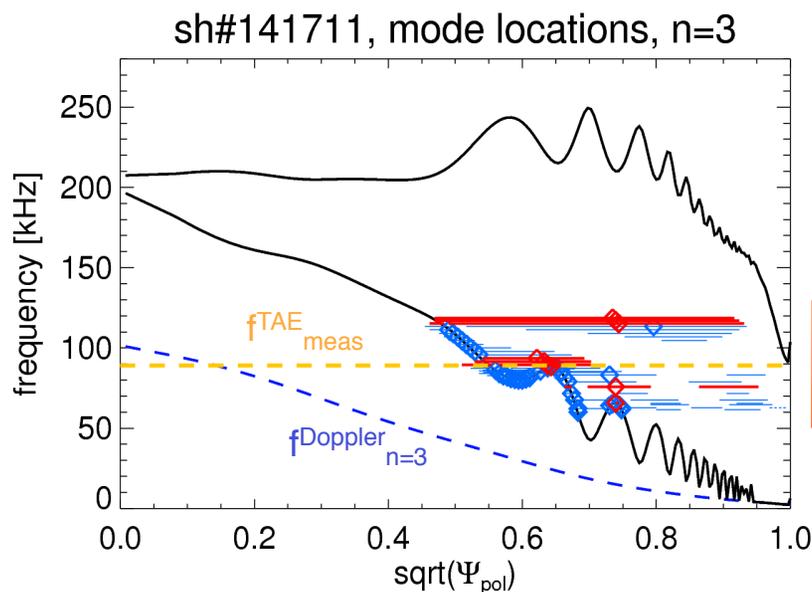
# Multi-channel reflectometer is main tool to unravel details of mode structure evolution

Crocker et al., PPCF 2011



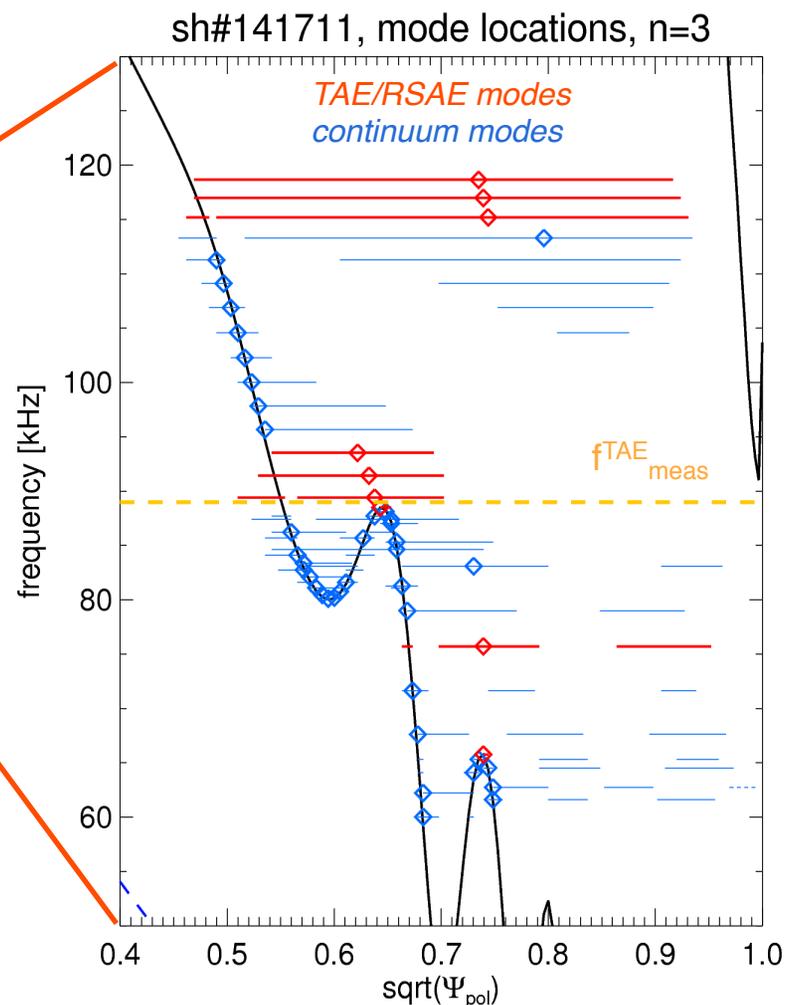
- Makes it possible comparison with codes – e.g. NOVA – in terms of  $dn/n$

# NOVA eigenmodes selected from matching with measured frequency, mode number, structure



search range

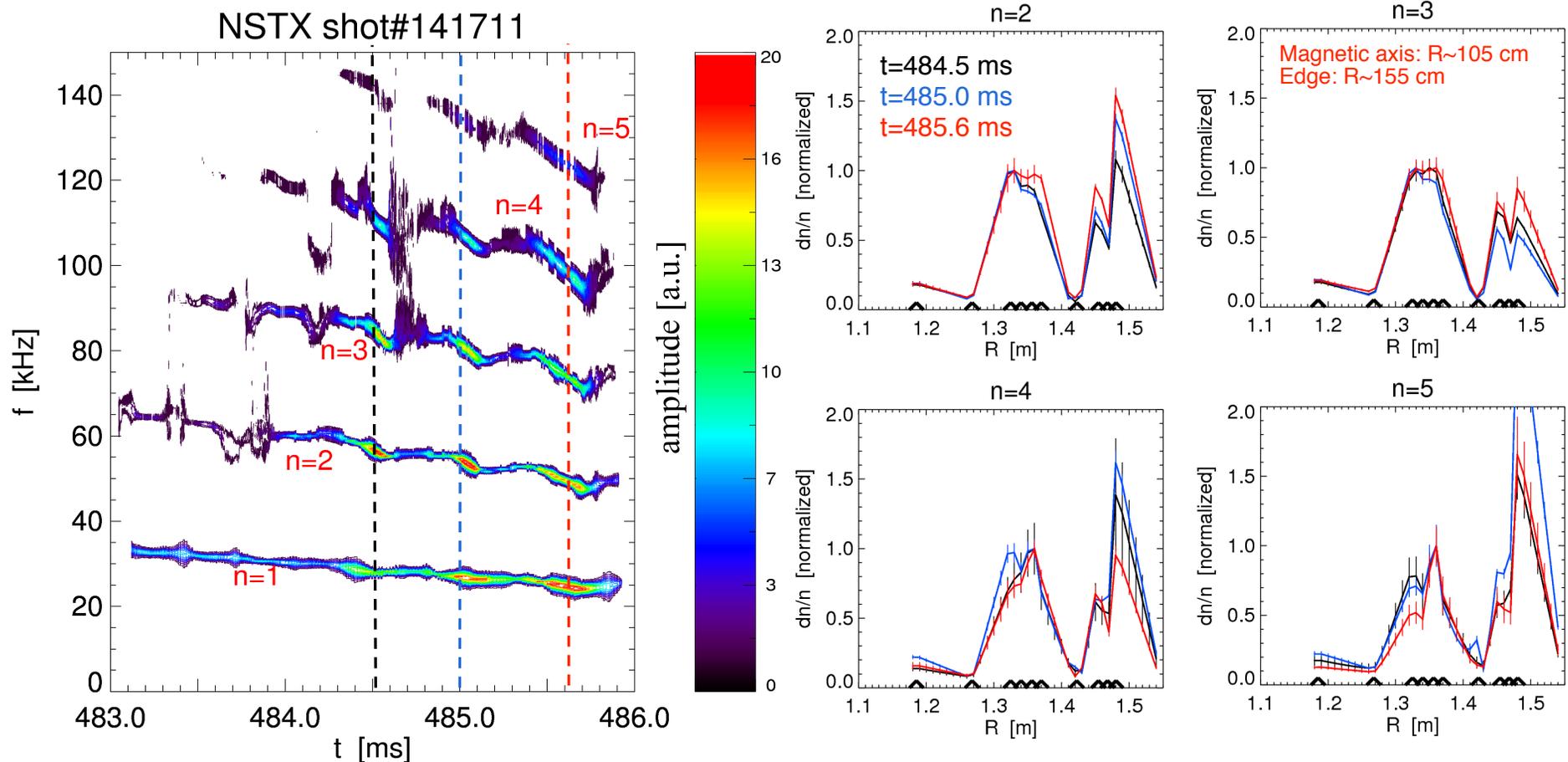
- NOVA provides *all, ideal* eigenmodes in a given frequency range
- Match mode structure ( $dn/n$ ) from reflectometer to NOVA solutions
- Select ‘observed’ mode; re-scale NOVA solution according to measured  $dn/n$



Fredrickson et al., PoP 2009

Fredrickson, P1.7

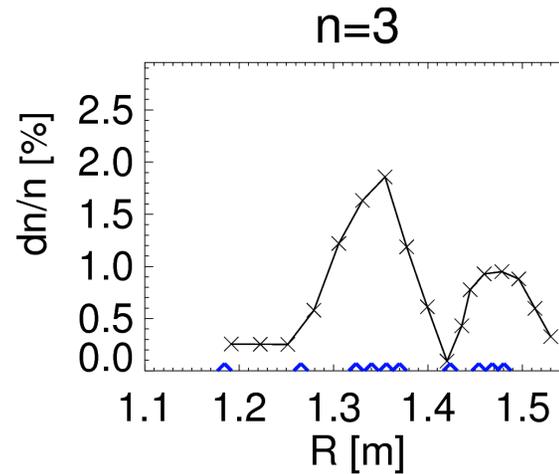
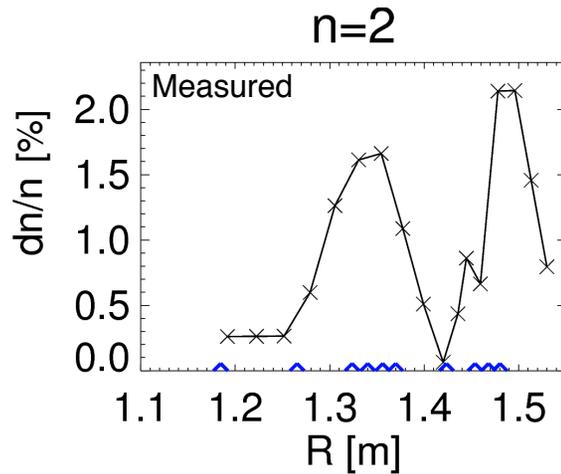
# Mode structure maintains its shape even during strong, *multi-step* avalanches



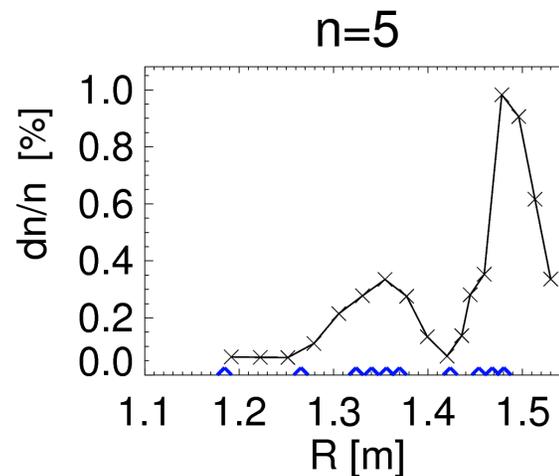
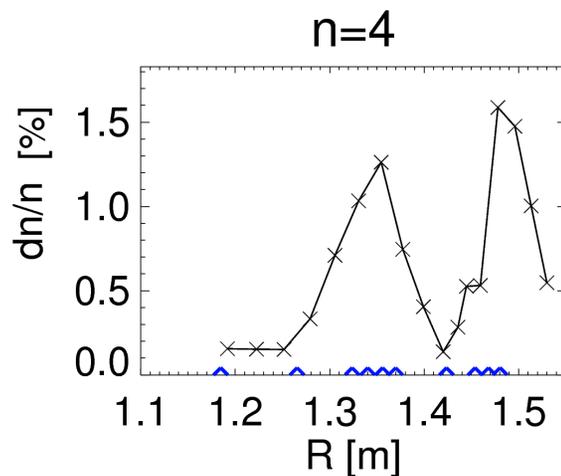
- Re-scaled  $dn/n$  shown (compare radial structure, not amplitude)
- Outward propagation of *unstable front* during burst not observed
  - Broad mode structure,  $\sim$  minor radius
  - Incomplete transition TAE  $\rightarrow$  EPM?

Zonca et al., NF 2005

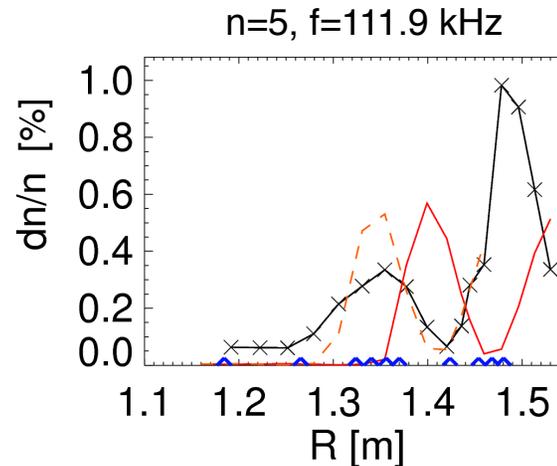
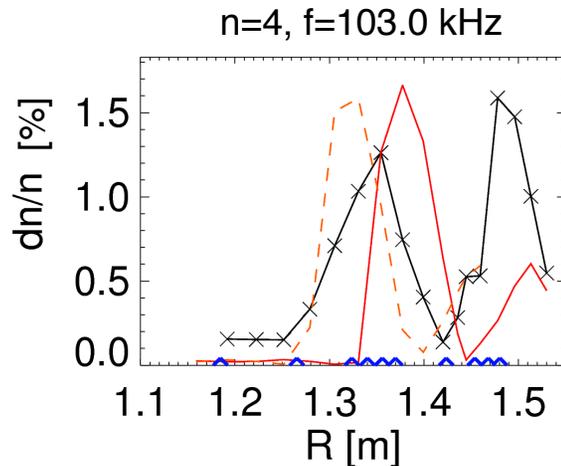
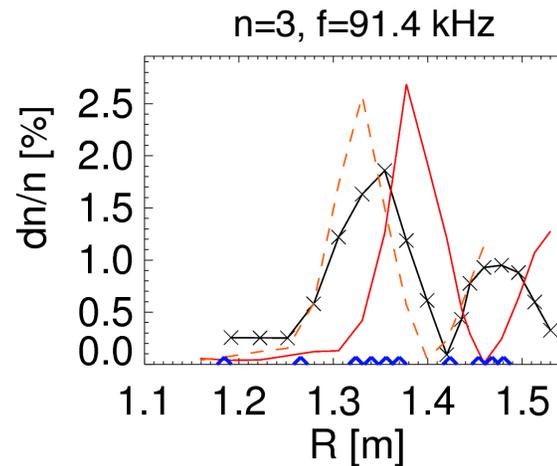
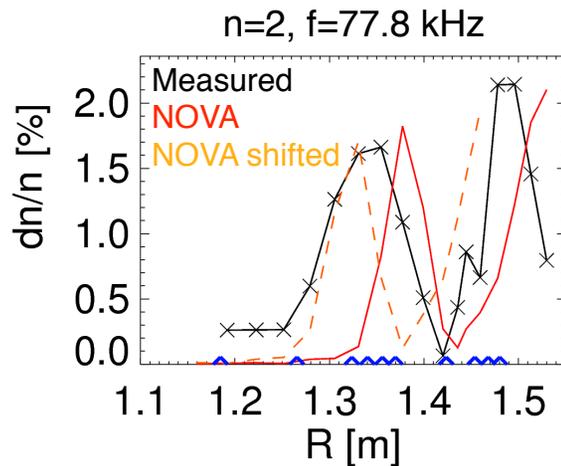
# Modes have broad mode structure, extending over good fraction of minor radius; peak at mid-radius



- sh#141711
- t=470ms
- Magnetic axis:  
R~105 cm
- Edge: R~155 cm



# Comparison with NOVA (ideal MHD!) is satisfactory; however, no good match for $n=1$ ... if 'TAE'

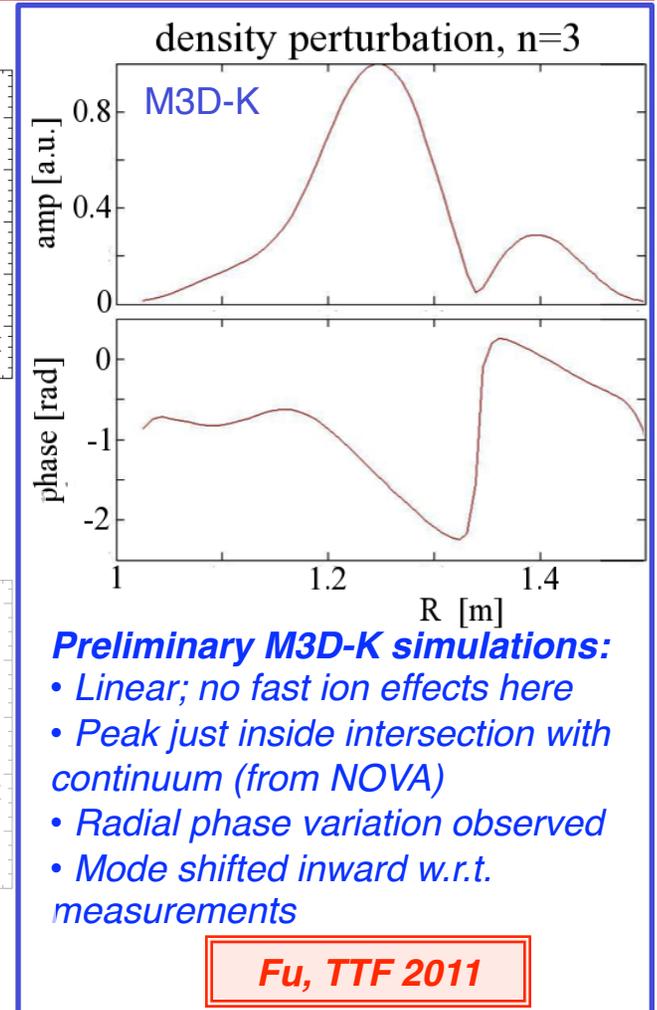
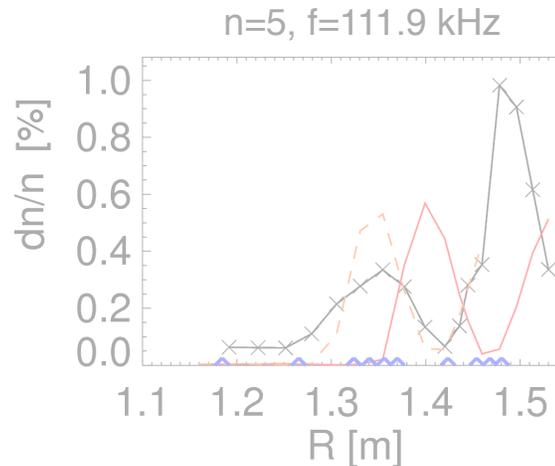
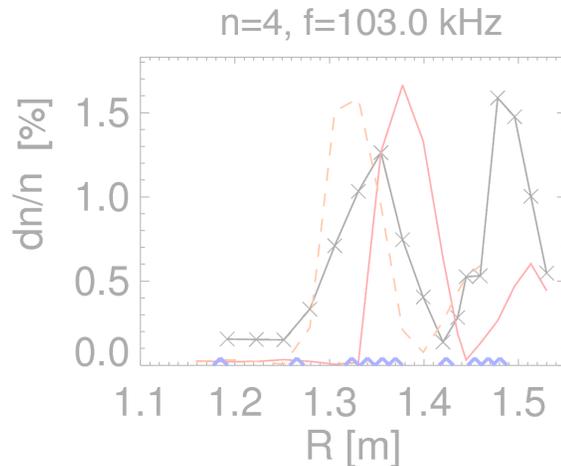
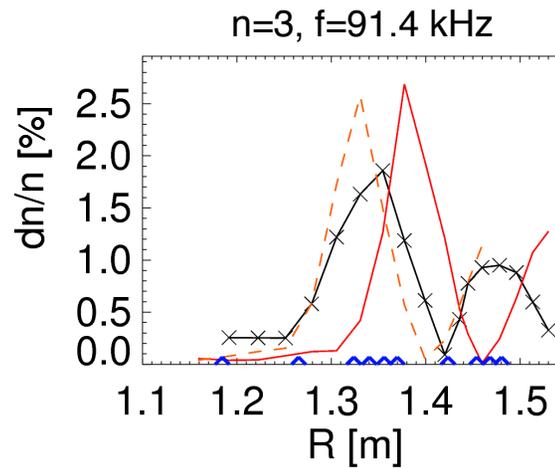
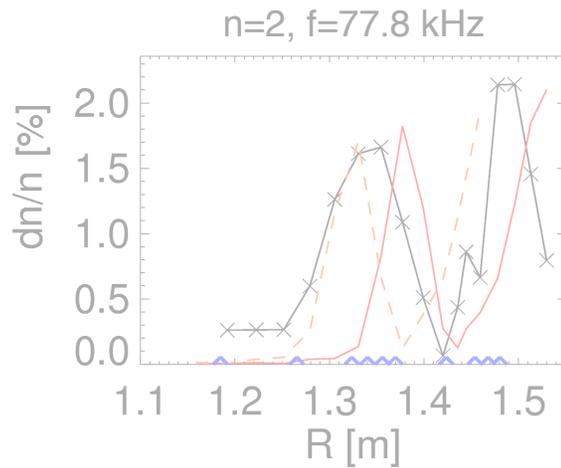


- Frequency from NOVA ~ consistent with experiment
- Doppler shift is included
- But: radial shift of 2-5 cm between measured and simulated dn/n

$n_{tor}$	$f_{meas}$ [kHz]	$f_{NOVA}$ [kHz]
2	60-80	77.8
3	80-100	91.4
4	110-125	103
5	130-140	111.9

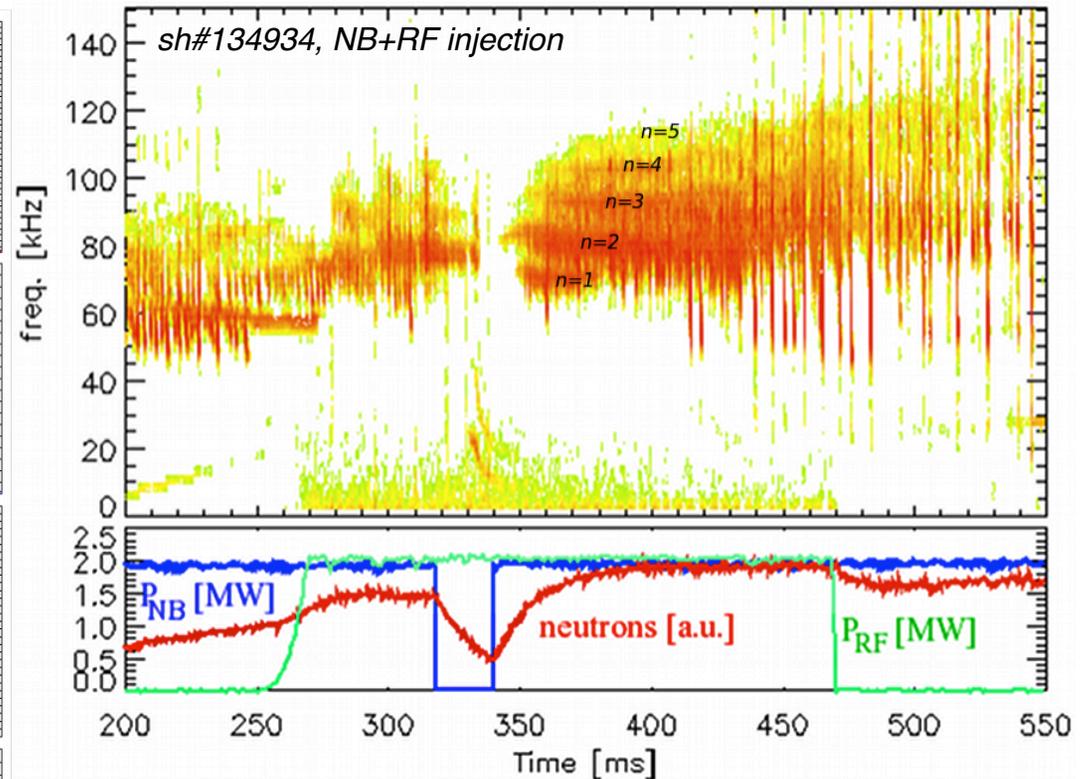
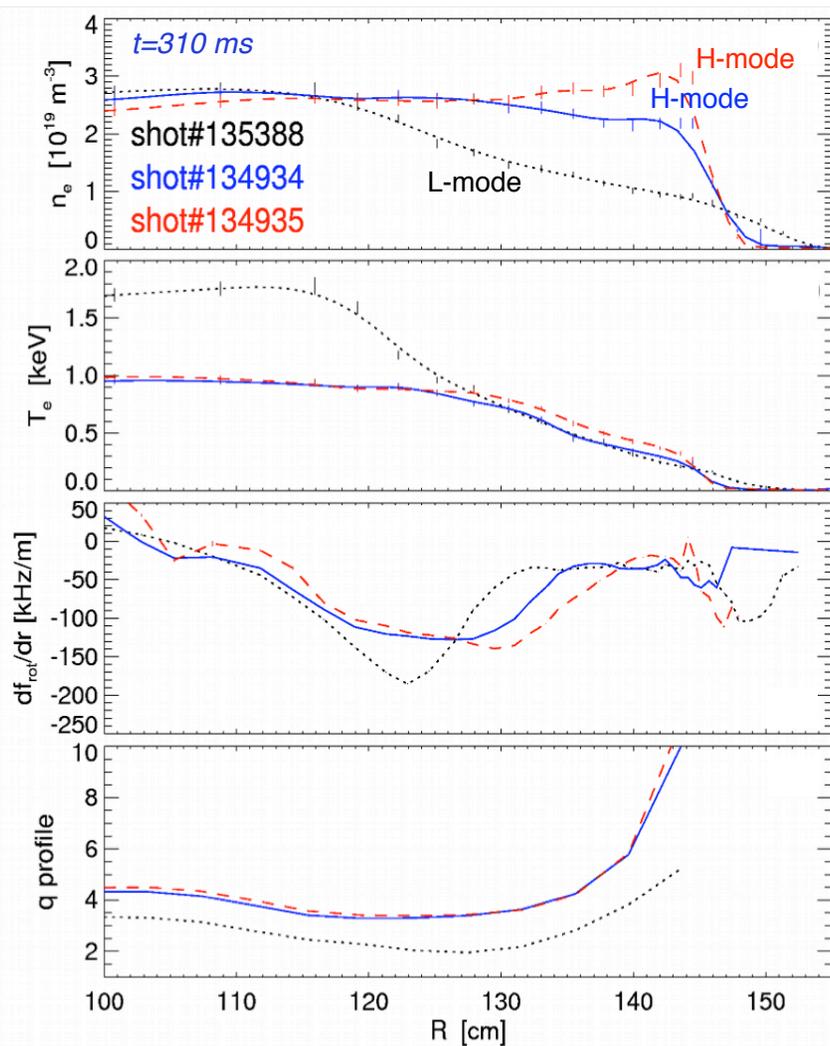
- NOVA results assume ideal MHD, no fast ion effects
- *Need to carefully check profile consistency between experimental data (MPTS, CHERS) and TRANSP output / NOVA input*

# Initial results from [non-linear, self-consistent] code M3D-K consistent with experiments, too



- NOVA results assume ideal MHD, no fast ion effects
- *Need to carefully check profile consistency between experimental data (MPTS, CHERS) and TRANSP output / NOVA input ... and M3D-K*

# Similar features observed in L- and H-mode plasmas and during combined NB+RF : *robust* dynamics



- Example: H-mode, NB / NB+RF
  - Profiles different from L-mode
  - Higher safety factor than for L-mode discharges
  - Reversed shear in both L- and H-mode

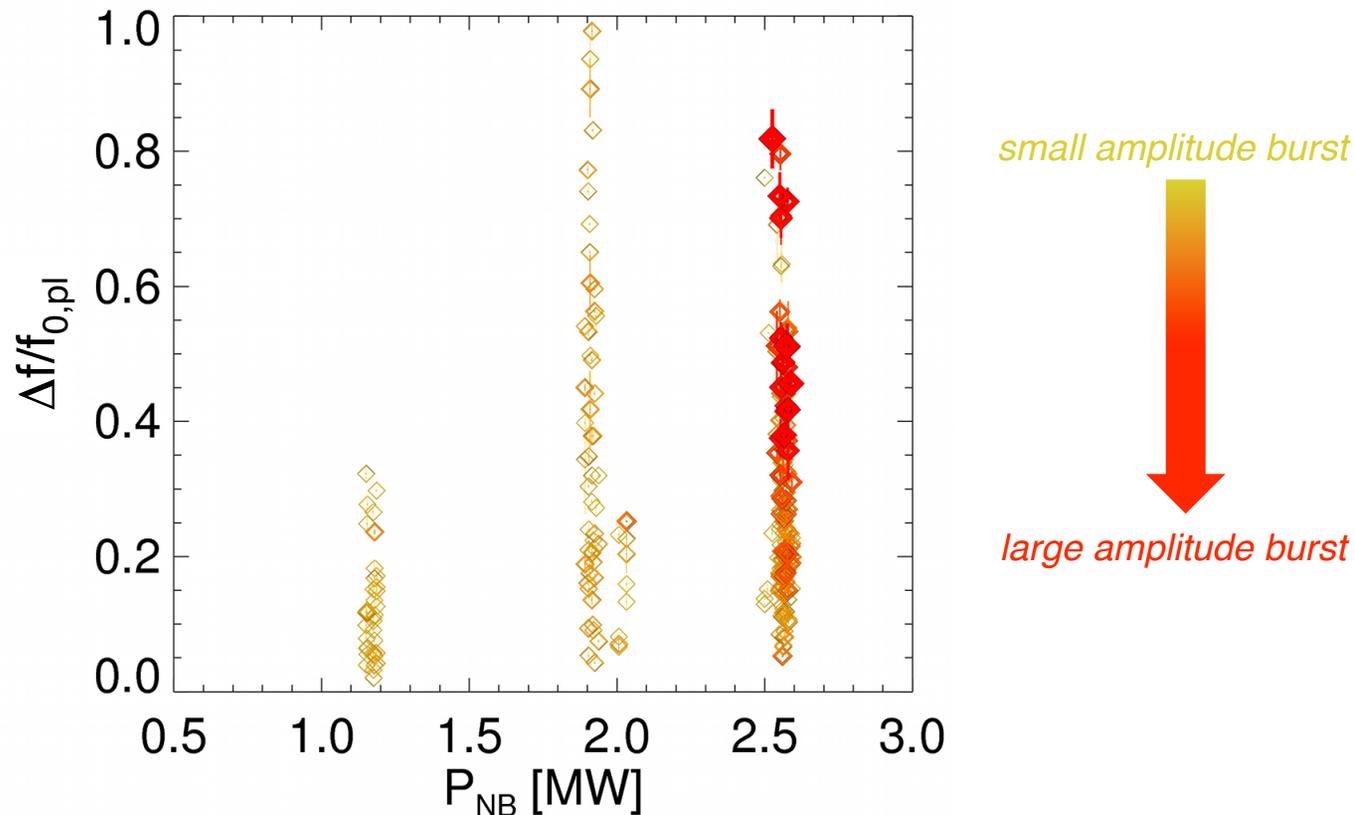
Fredrickson, P1.7

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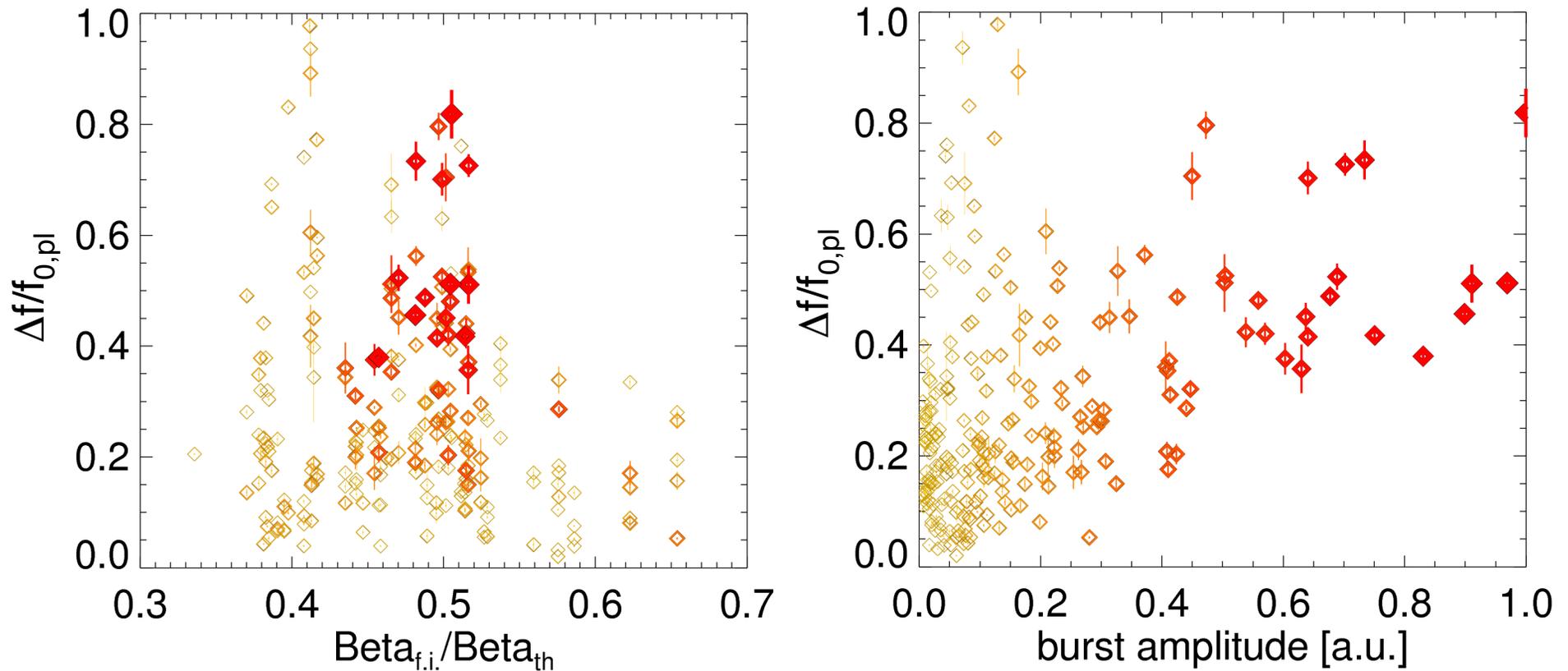
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# Onset of bursting/chirping regime strongly dependent on injected NB (and RF) power

- Take fractional frequency variation  $\Delta f/f_{0,pl}$  as metric for severity of bursts
  - $f_{0,pl}$ : mode frequency in the plasma frame
- Each symbol represents values for single  $n$  mode, 5 ms average

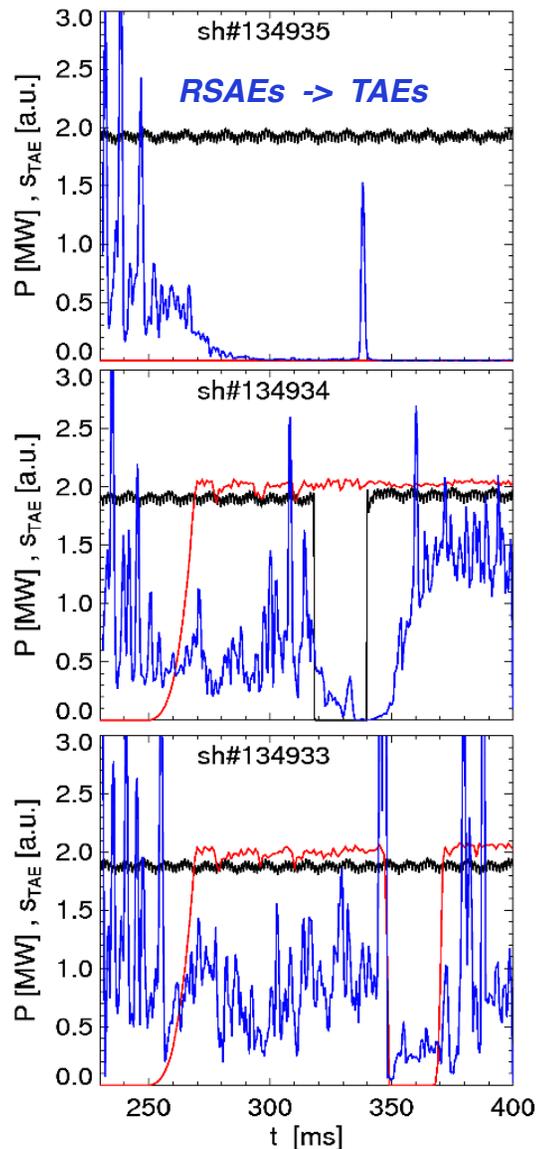


# High ratio of fast ion to thermal $\beta$ leads to bursts/chirps – but other factors determine mode dynamics

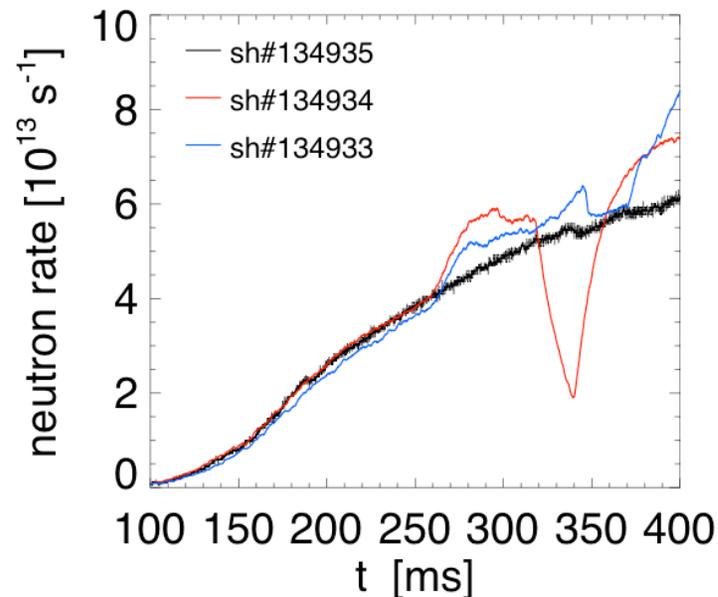


- Modes show more bursting character as discharge evolves
  - NB power increases, fast ion population and  $\beta_{f,i}$  builds up
  - Typical bursts have *edge*  $\delta B/B \sim 10^{-4}$  (from Mirnov coils)
    - > Can increase more than x10 during avalanches

# Destabilization of TAEs correlates with variations of heating scheme, e.g. NB vs. NB+RF



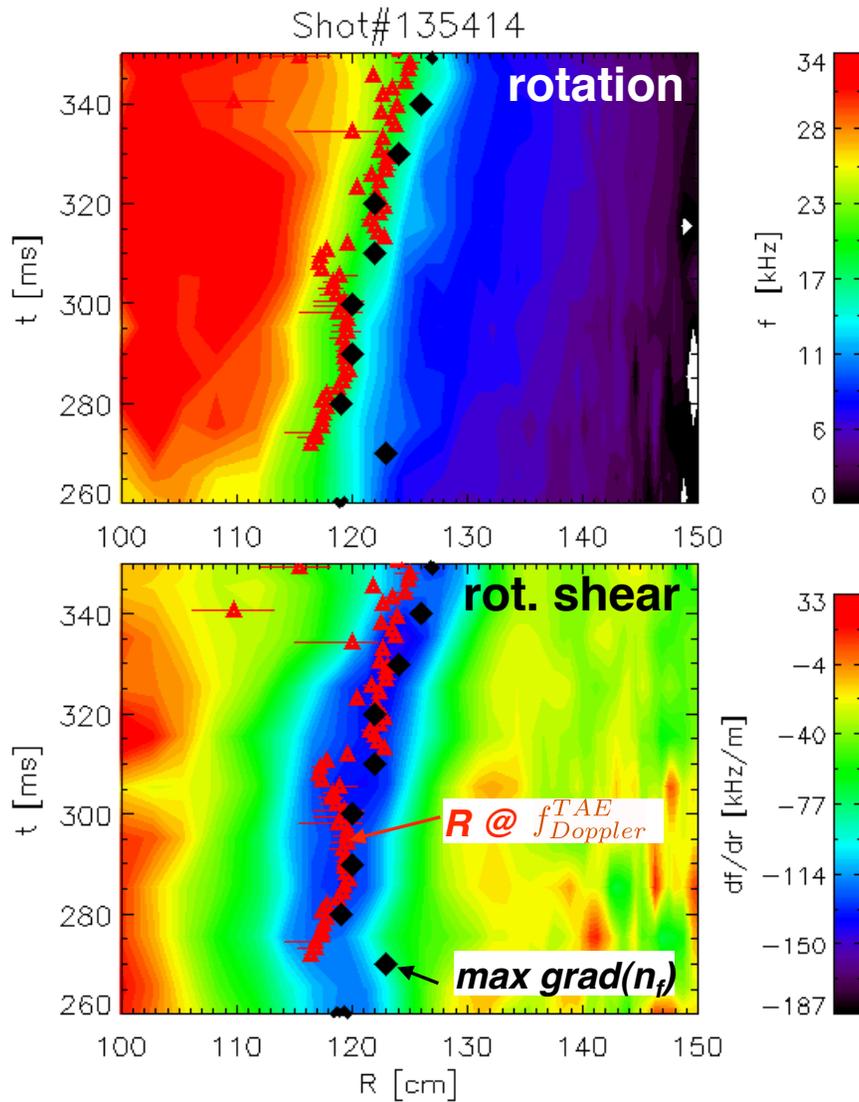
- Example: H-mode discharges with NB and NB+RF heating
  - Different profiles with respect to L-mode (e.g. higher safety factor)
  - Reversed shear in both L- and H-mode



**NB only**  
**NB+RF, NB notch**  
**NB+RF, RF notch**

- Here NB alone does not drive TAEs
- NB+RF does: increase in fast ions

# Strong dependence on NB drive leads to entangled evolution of TAEs, fast ions and thermal plasma



- Mode location,  $R^{TAE}$ , obtained by matching  $f_{Doppler}^{TAE}$  with measured rotation profile:

$$f_{rot}(R^{TAE}) = f_{Doppler}^{TAE}$$

- Correlation between

- Mode location  $R @ f_{Doppler}^{TAE}$
- Max fast ion gradient  $max grad(n_f)$
- Max rotation shear

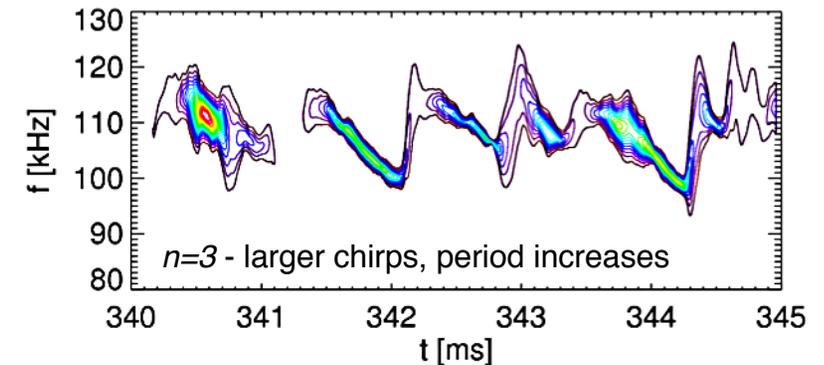
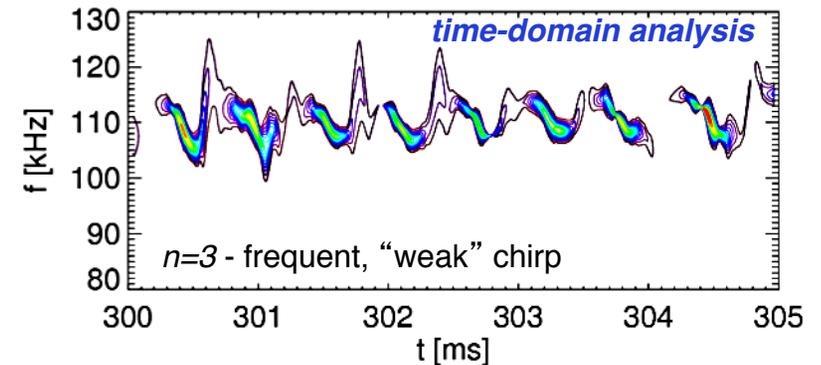
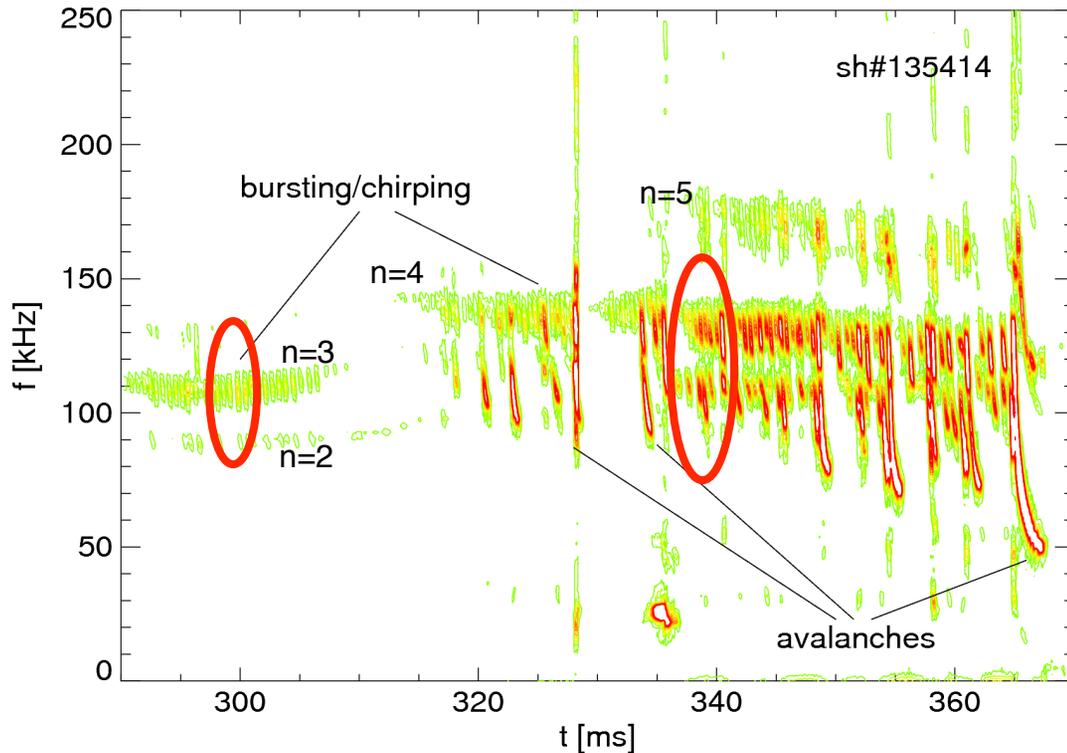
Coupling through common  
“source term”, i.e. NB injection



Modes cluster at similar radius:  
may enhance coupling

Podestà et al., PoP 2010

# Once set up, bursting/chirping TAE regime is rather insensitive to variations in plasma parameters

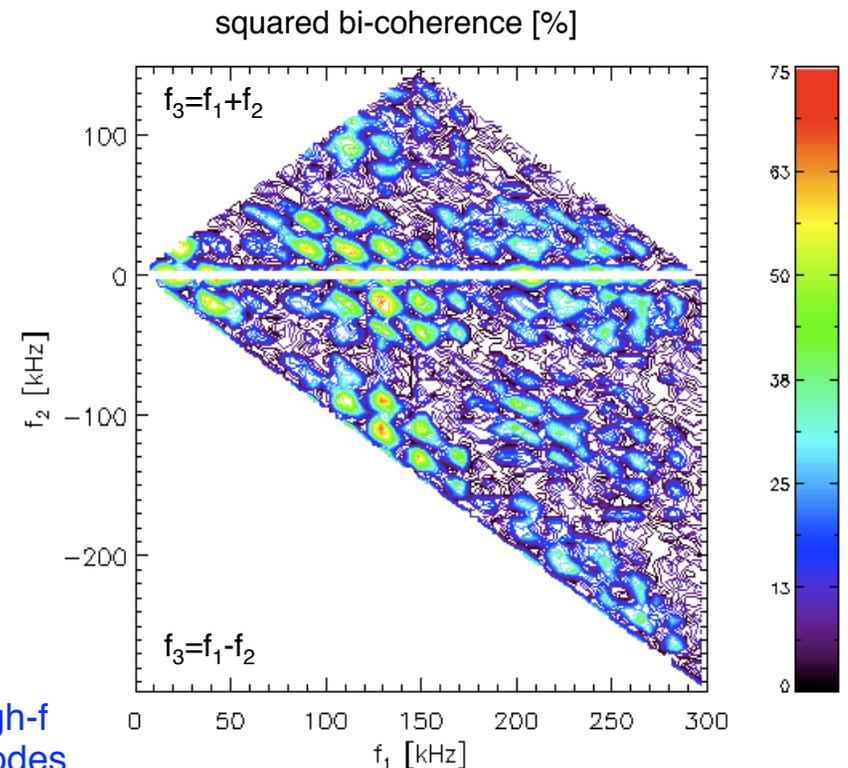
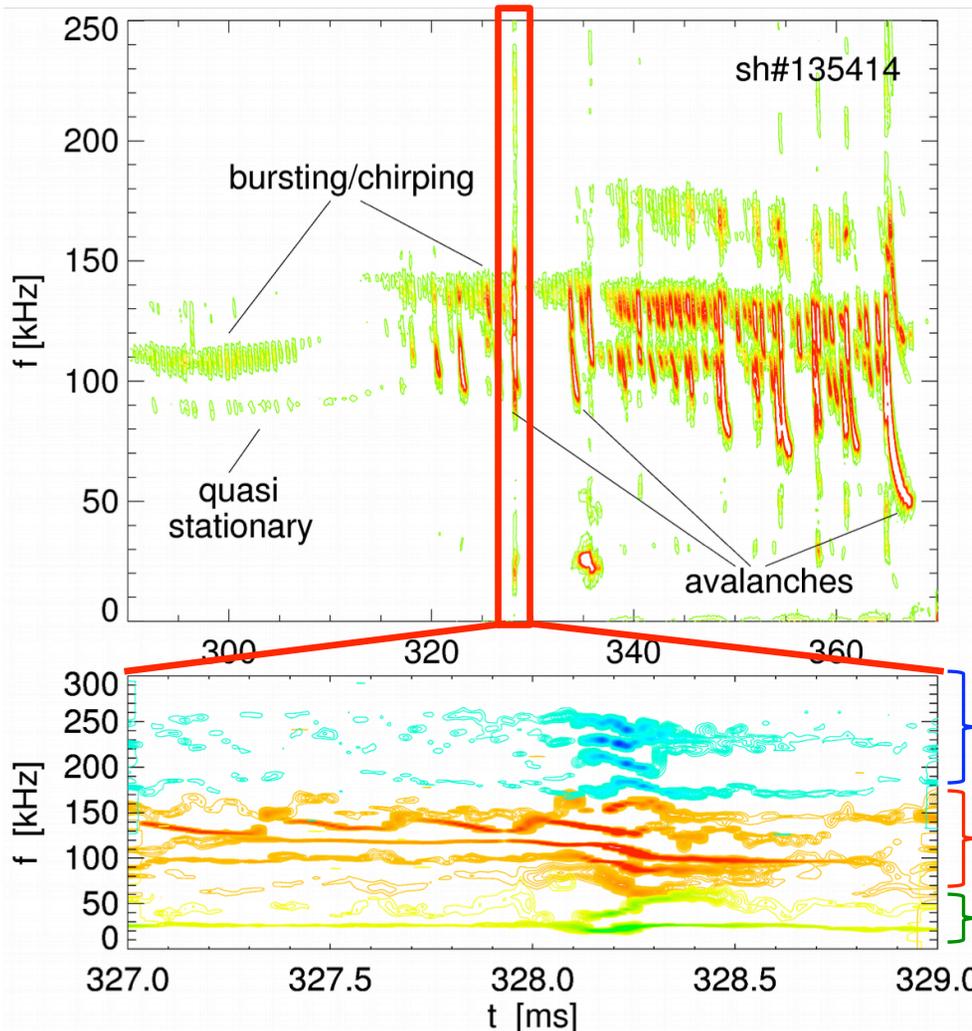


- Burst separation 0.5 – 2 ms
  - No systematic variation with  $n_e$ ,  $T_e$ ,  $P_{NB}$ , ...
  - Frequency evolution does not follow unique pattern (e.g.  $t^{-1/2}$ , linear, exponential)
- Usually, each mode chirps independently of the others...
- ... but, eventually, *avalanches* occur:
  - **Multiple modes lock on similar dynamic, mode-mode coupling**

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# Coupling between multiple TAEs with $\Delta n_{\text{tor}}=1$ , enhanced losses observed during explosive modes' growth



- Coupling generates higher/lower frequency modes

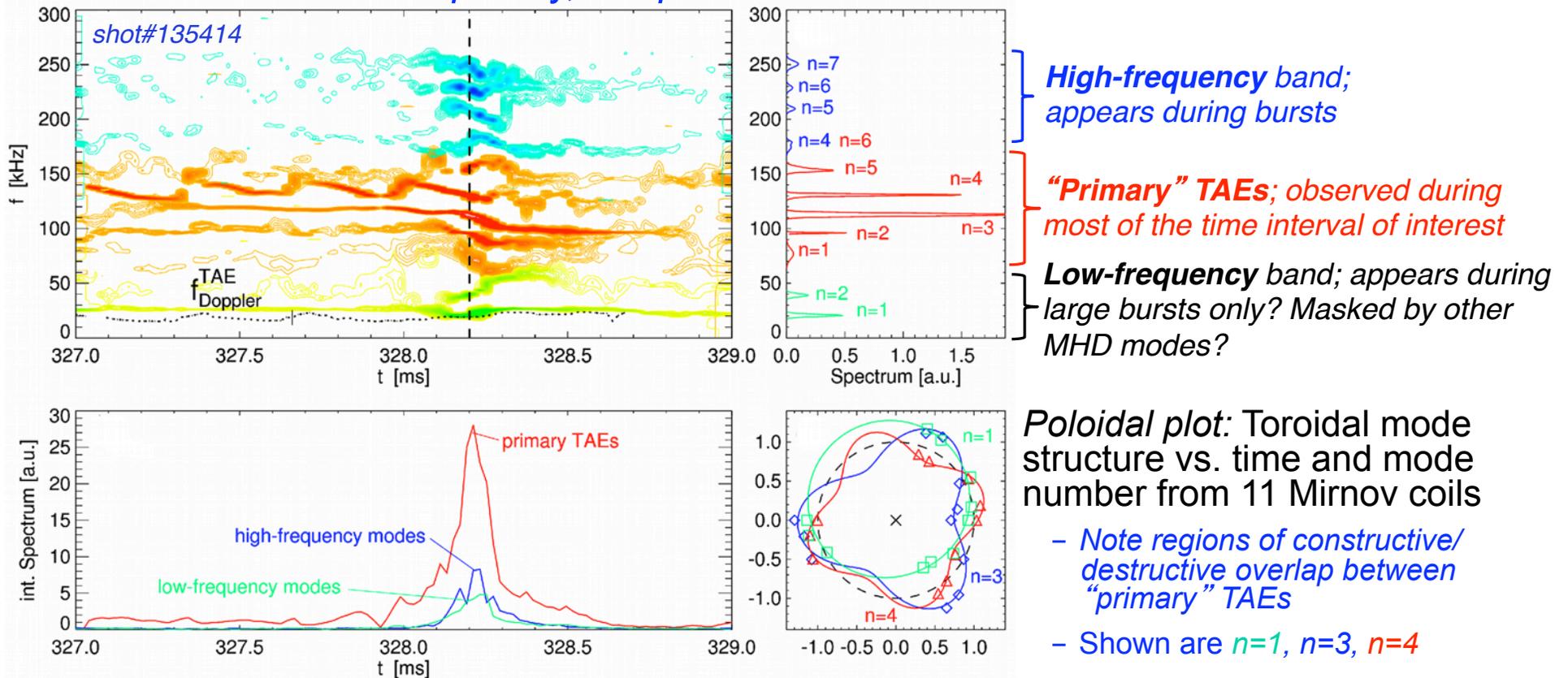
- Multiple modes follow similar dynamic during the burst
  - *Transition from single- to multi-mode regime*

Podestà et al., NF 2011

# 'New' modes appear in the spectrum above/below TAE range during large bursts

- Modes can be classified into three groups

– Discriminant: frequency, temporal evolution



- Picture consistent with primary TAEs

- coupling to each other
- generating/pumping secondary modes through sum/difference with  $\Delta n=1$

# Simple model based on quadratic interactions can be used to investigate coupling between TAEs

$$\dot{s}_{n_3} = \langle c_{(n_1, n_2)} s_{n_1} s_{n_2} \rangle_{f_{n_3}}$$

$s_{n_2} \rightarrow s_{n_2}^*$  (complex conjugate) for difference interaction

Right-hand side filtered around frequency  $f_{n_3}$

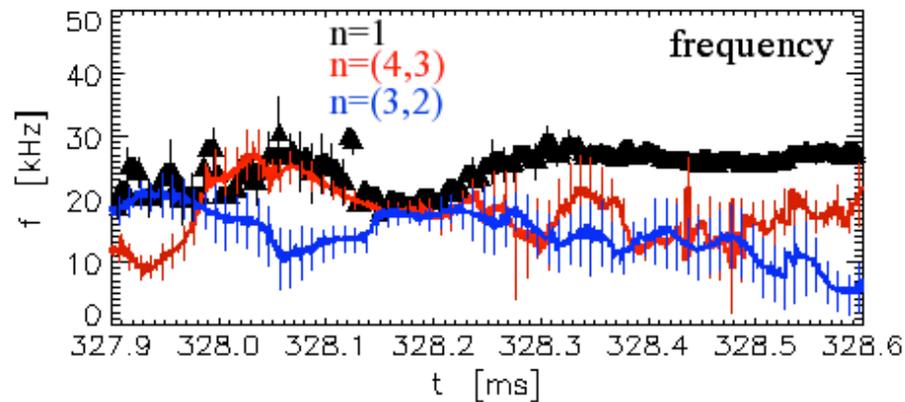
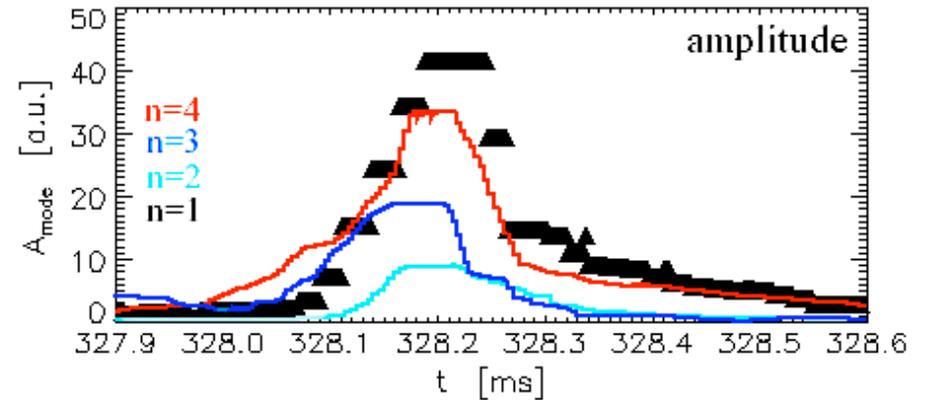
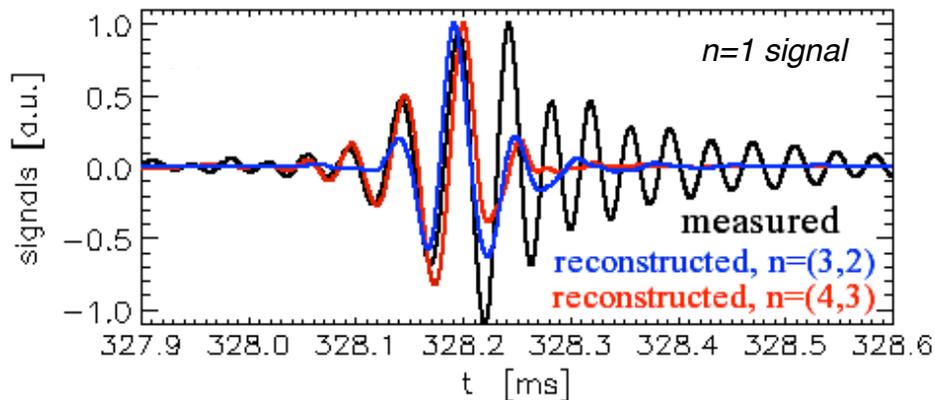
Modes must satisfy matching conditions  $\begin{cases} n_3 = n_1 \pm n_2 \\ f_{n_3} = f_{n_1} \pm f_{n_2} \end{cases}$

$c(n_1, n_2)$  is the coupling coefficient, here used as ‘free scaling parameter’

In practice:

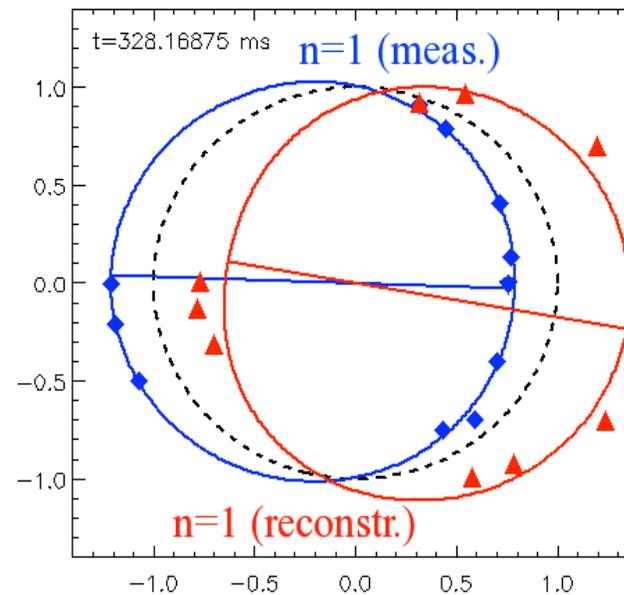
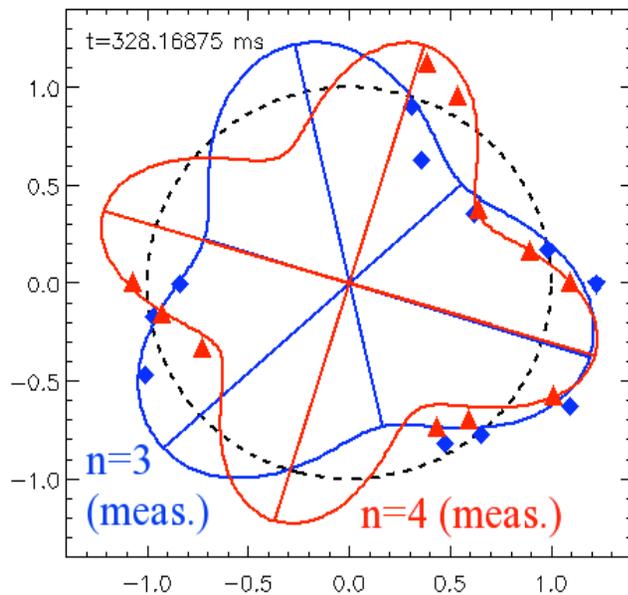
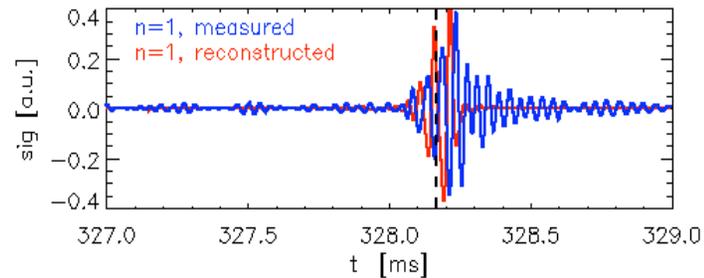
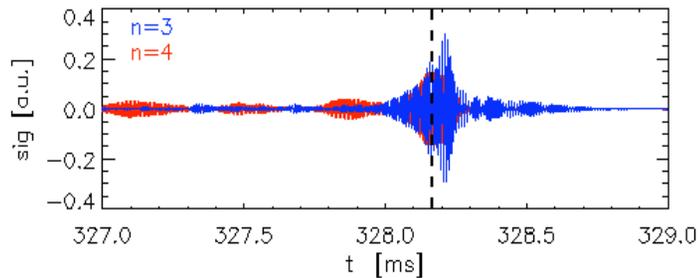
- Real signals  $s_{n_1}, s_{n_2}, s_{n_3}$  measured for each possible triplet, e.g. from Mirnov coils
- “Reconstruct”  $s_{n_3} \rightarrow s_{n_3, rec}$  from measured  $s_{n_1}, s_{n_2}$
- Compare measured and reconstructed  $\dot{s}_{n_3}$
- Frequency match must be verified in the plasma frame:
  - Rotation profile and location of each mode must be accurately known

# Good agreement with quadratic interactions' model: amplitude evolution and frequency matching



- $n=1$  mode fades away when either amplitude of pump modes or frequency matching vanishes

# Mode number matching condition verified

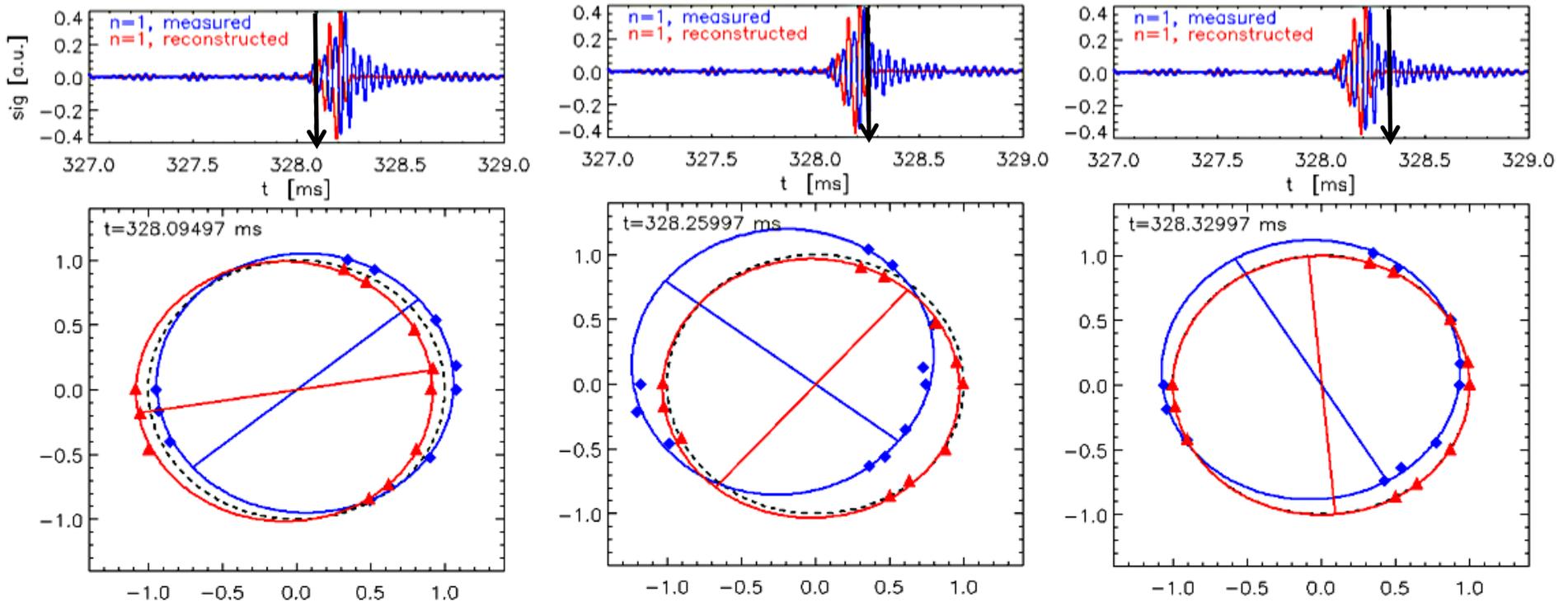


- Symbols: rms mode amplitude data from 11 Mirnov coils
- Solid lines: fit for a given  $n$  ( $n=1$  here)
- Dashed line: unit circle (zero-amplitude reference)

• “Reconstructed” toroidal structure of  $n=1$  mode also agrees with measured one

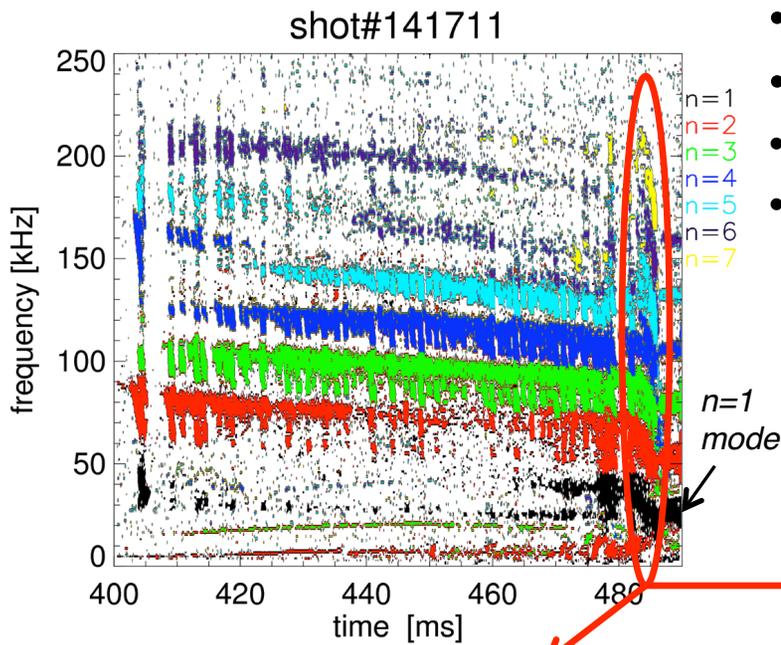
– Phase shift of  $\sim 180$  degrees during strongest mode activity

# Phase matching condition is *transiently* verified for tens of (primary) mode cycles during large bursts

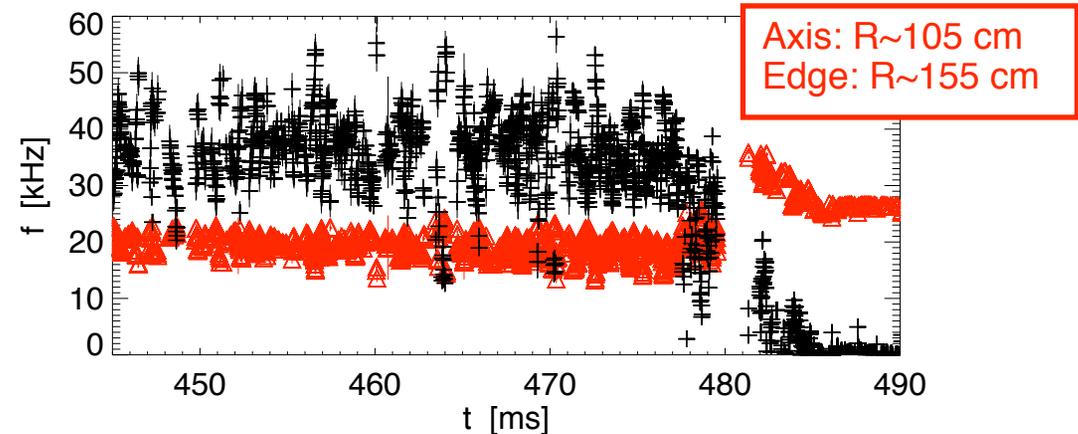
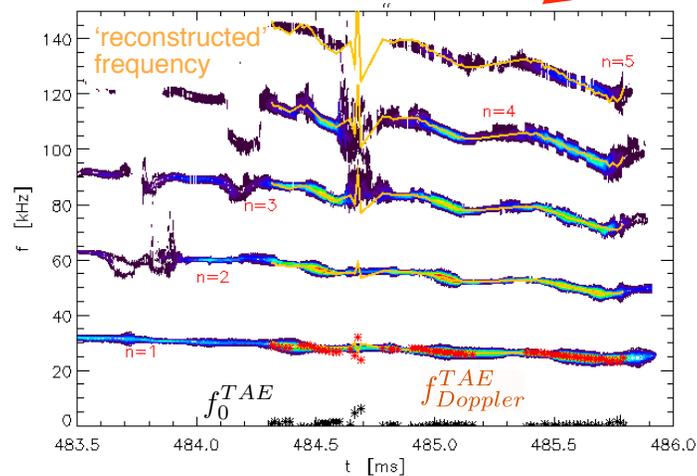
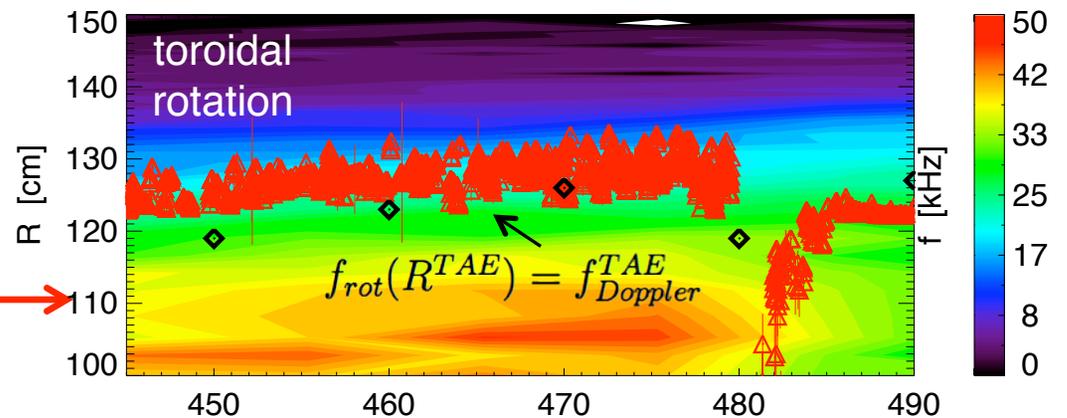


- Stationary phase during quadratic interaction is important!
  - $n=1$  mode fades away  $\Leftrightarrow$  phase changes rapidly in time
  - “Single mode” dynamic, with each mode following its own chirp/burst cycle, is effective in reducing efficiency of quadratic interactions
  - Result: small bursts (single mode), and occasional multi-mode avalanches
- $n=1$  mode mediates coupling: what is it?

# $f_{n=1}$ consistent with central plasma rotation: avalanches drive $f_0^{TAE} \rightarrow 0$ (plasma frame), cause coupling to 'kinks' ?

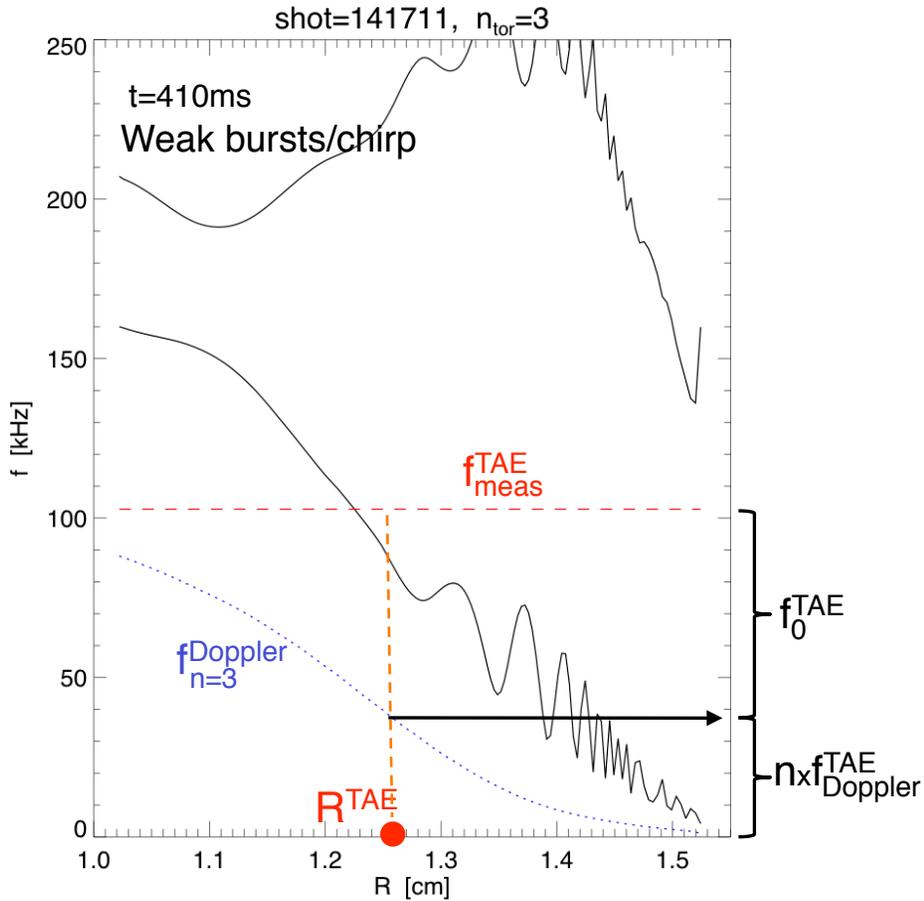


- Kink-like modes destabilized during avalanche
- Sustained fast ion losses Bortolon, O-12
- TAE mode structure  $\sim$  maintained
- Doppler shift radius  $R^{TAE}$  sweeps from plasma center out in  $\sim 2$  ms



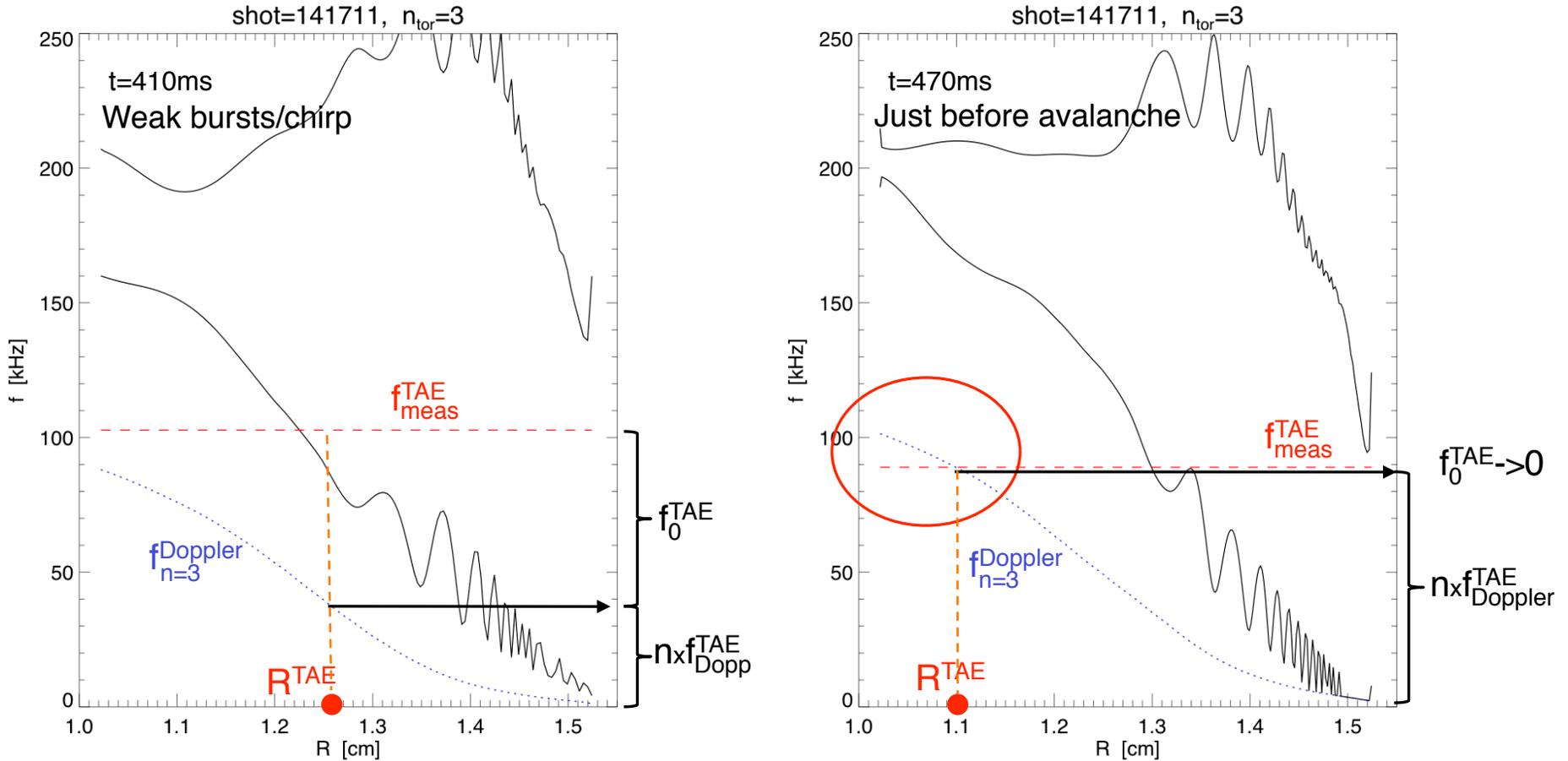
# Meaning of $f_0^{TAE}$ : mode frequency at the mode location $R^{TAE}$ , i.e. where drive is maximum

TAE continuum from NOVA-K



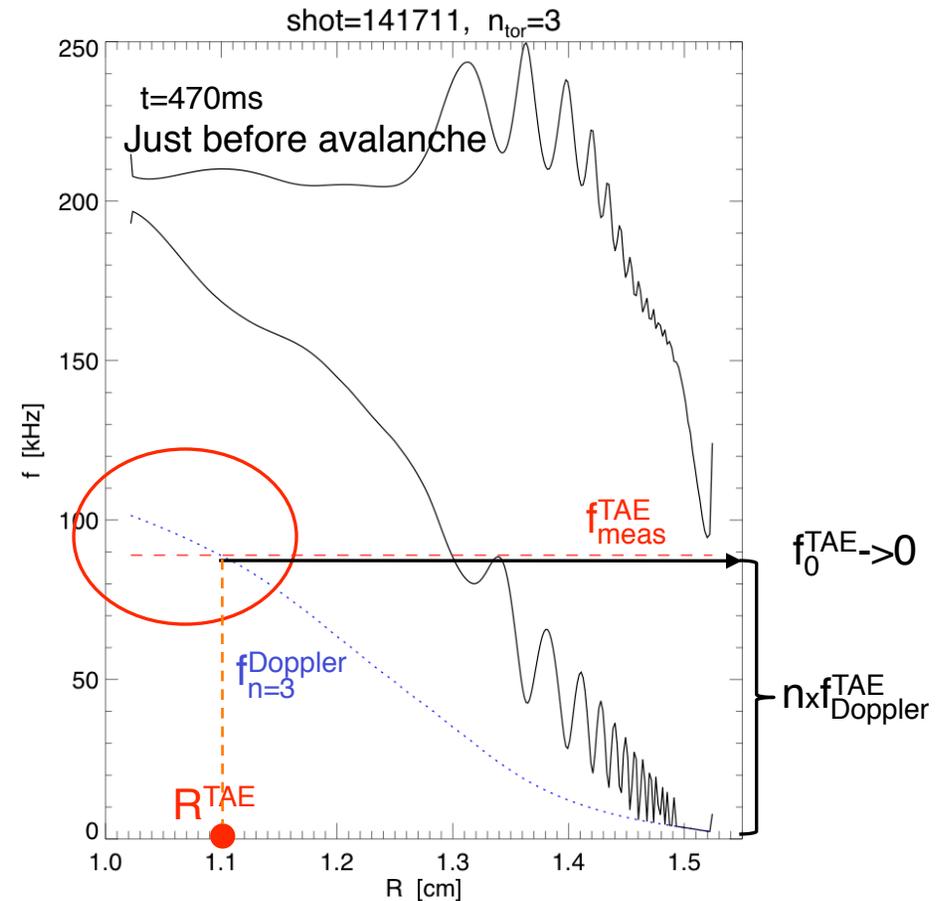
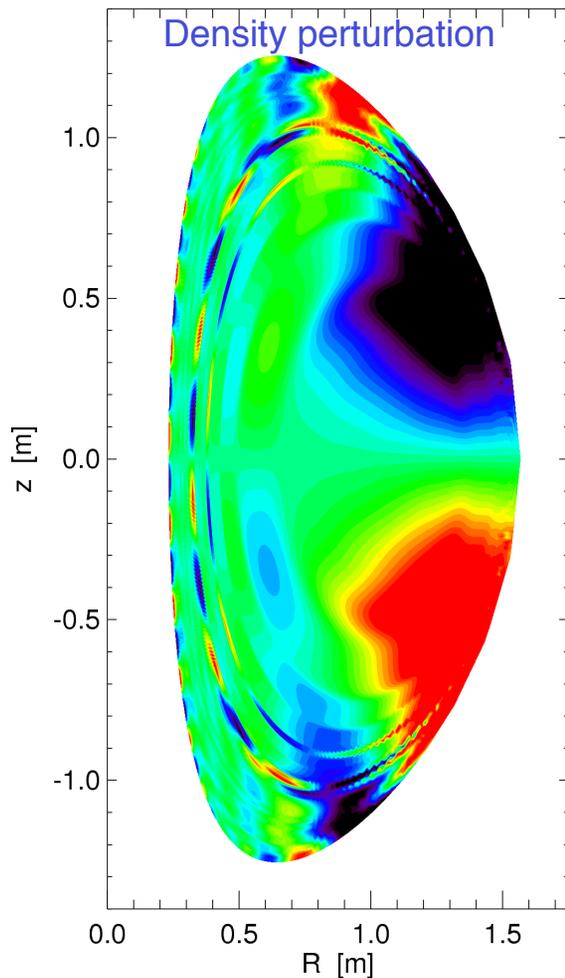
# Meaning of $f_0^{TAE} \rightarrow 0$ : $f^{TAE}$ beats with $n \times$ rotation frequency at the plasma center

TAE continuum from NOVA-K



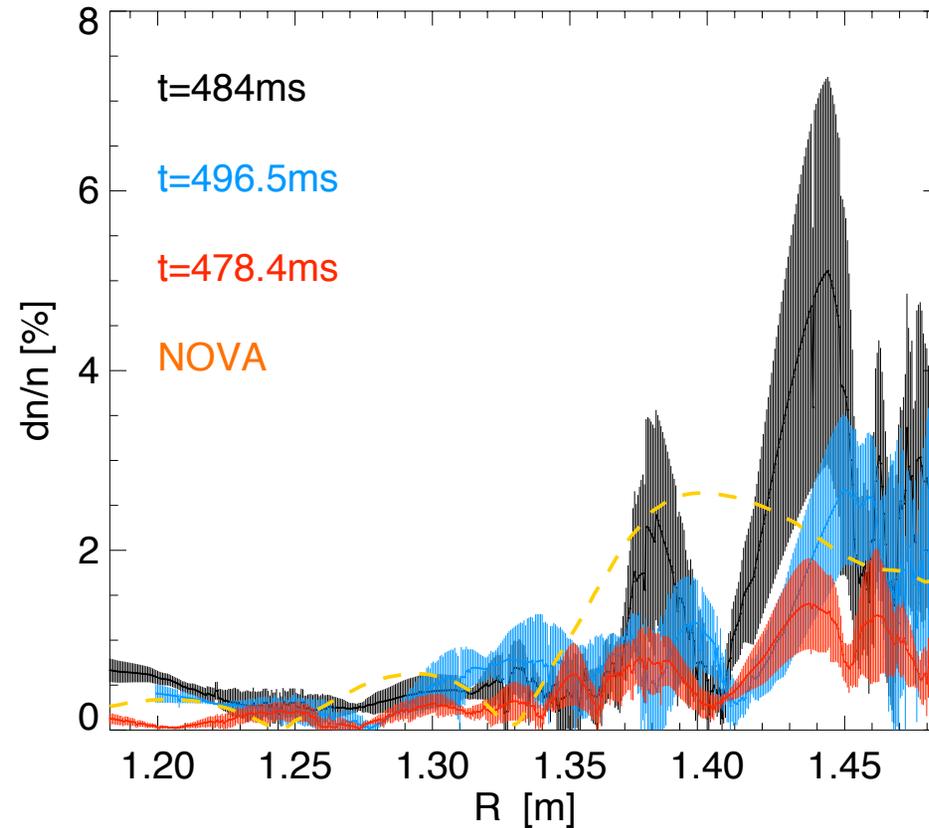
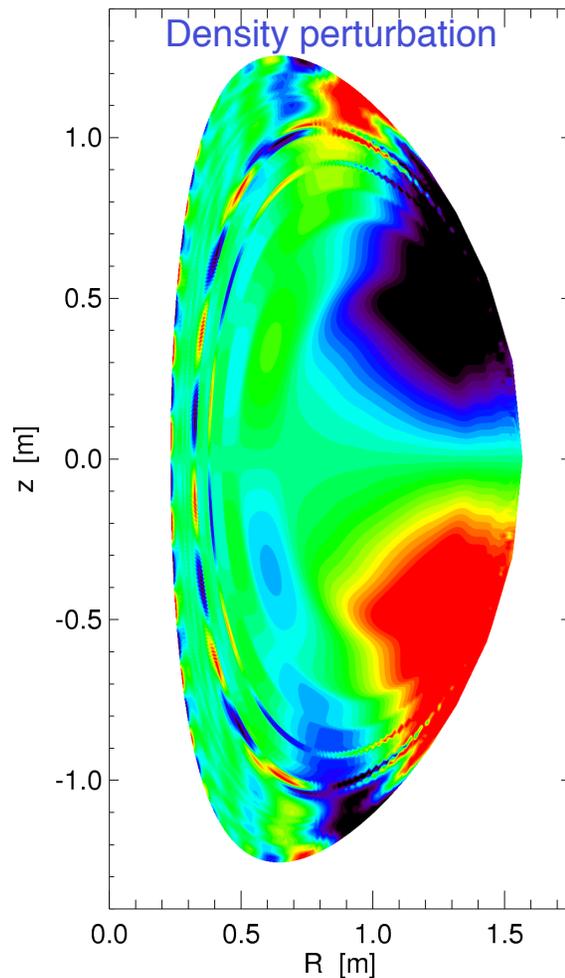
- Coupling with kink-like modes favored when  $n_{tor} \times f_{rot}$  on axis  $\sim f^{TAE}$
- Observed for  $q > 1$ : fishbone branch involved?

# $n=1, m=-2, \dots, +2$ kink found through ideal MHD code NOVA with no rotation, free boundaries



- Large edge perturbation, consistent with reflectometer's data

# Measured perturbation evolves during burst; large edge component, $dn/n > 5\%$



- Data from inversion of multi-channel reflectometer signals
- Assume 'linear' model for reflectometer, pure O-mode propagation, fixed  $n_{0,e}$
- Roughly consistent with (ideal) NOVA solution

# Outline

- Experimental scenario, diagnostics
- General features of TAEs on NSTX
  - Frequency, amplitude dynamics
  - Mode structure
  - Role of fast ion drive
- Non-linear dynamics, mode-mode coupling
- Summary and open issues

# Summary

- After onset, bursting/chirping TAE regime is “robust” against small variations of plasma parameters
  - L-mode vs. H-mode, NB only, NB+RF, ... : all show similar features
- Non-linearities at play in both single-mode and multi-mode (avalanching) TAE dynamics
  - But only avalanches seem to cause significant fast ion losses
  - Coupling manifests as intermittent, chaotic process
  - Coupling can encompass multiple ‘scales’: TAE, kink/fishbones (, GAE, ...)
  - Dynamics complicated by link between fast ions, TAEs, thermal plasma through NB injection
- Different physics for weak chirps vs. avalanches?
  - Single-mode; weak chirps regulated by phase-space, fast ion profile effects
  - Multi-mode; avalanches lock on underlying kink/fishbone (‘global’)
- Present experiments allow thorough benchmark of codes
  - Linear MHD satisfactory for first-order estimates of mode structure
  - Non-linear, self consistent codes required to capture full dynamics

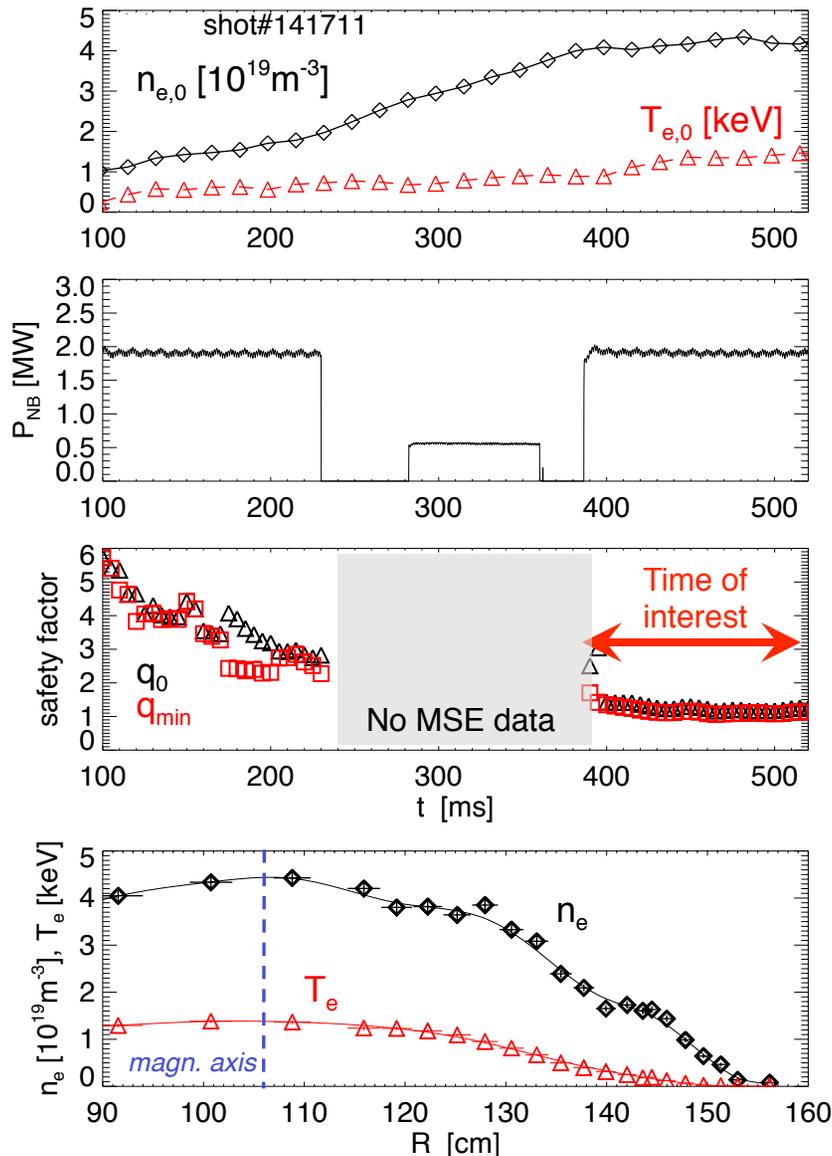
# Backup slides

# Experimental scenario :

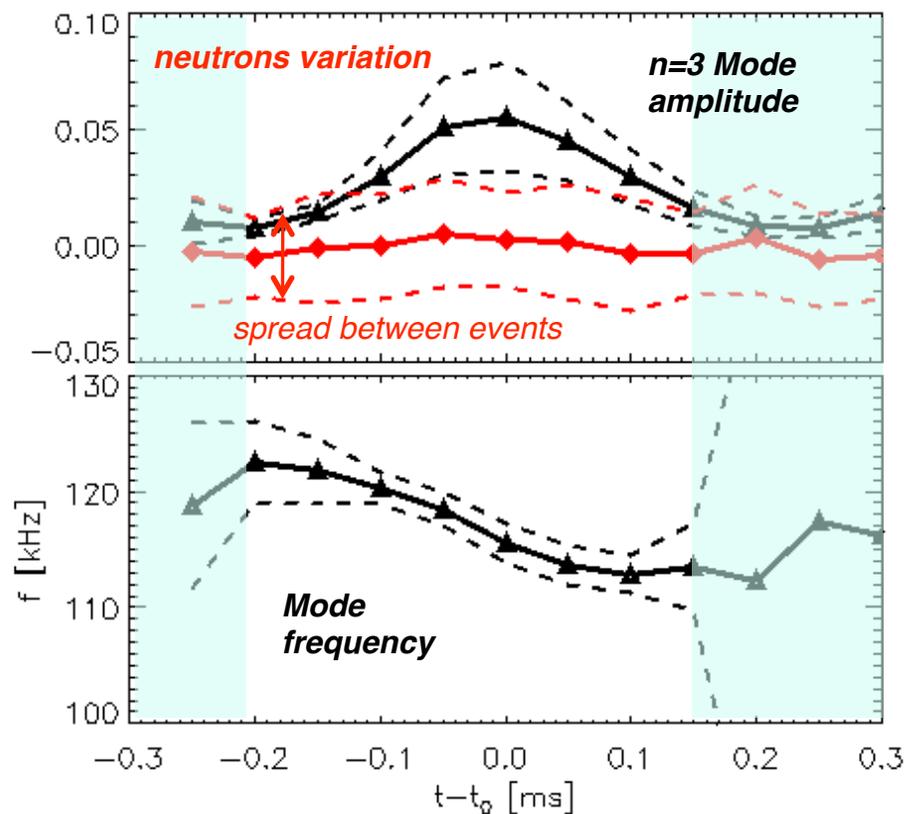
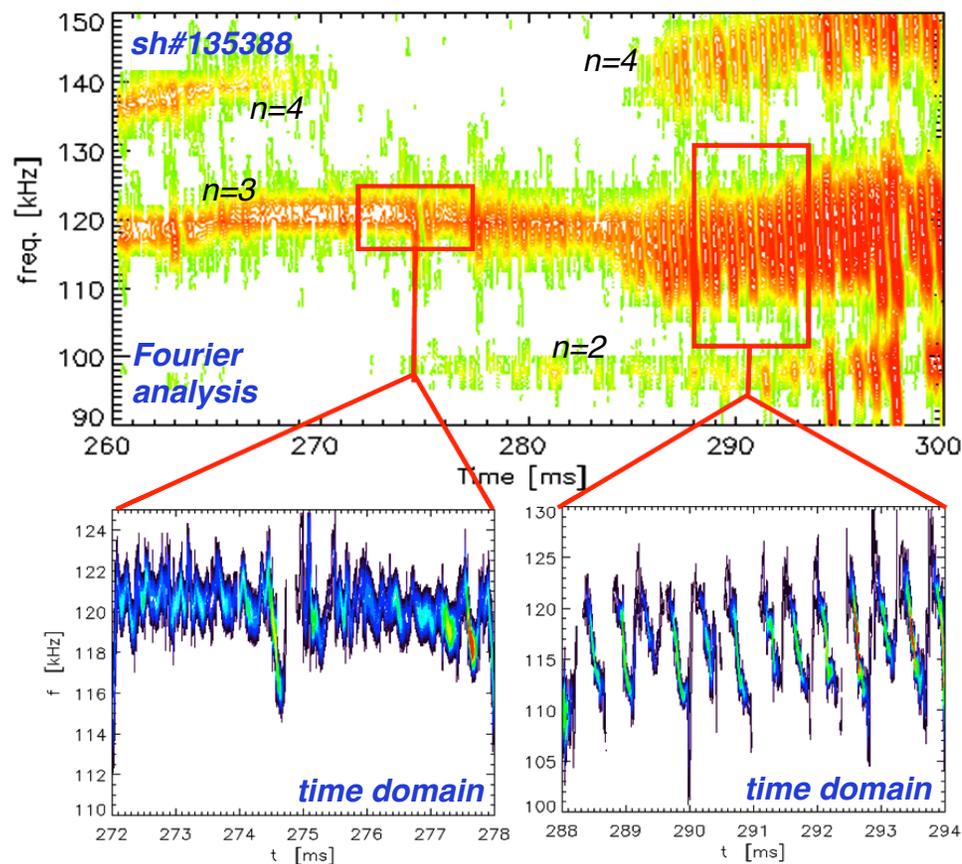
$P_{NB} < 3\text{MW}$ ,  $n_e \sim 3\text{-}4 \times 10^{19}\text{m}^{-3}$ ,  $T_i \sim T_e = 1\text{-}1.5\text{keV}$

## NB-heated, L-mode plasmas

- Plasma limited on center-stack
- NB power and timing varied to affect mode stability
- Plasma profiles evolving in time
  - > Monotonic, centrally peaked: OK for reflectometer measurements
- Central plasma rotation up to 40kHz
  - > Large Doppler shift of mode frequency
- Reversed-shear  $q$  profile
  - >  $q_{\min} \sim 1$  toward end of discharge
- Safety factor evolution reconstructed through LRDFIT code constrained by MSE data

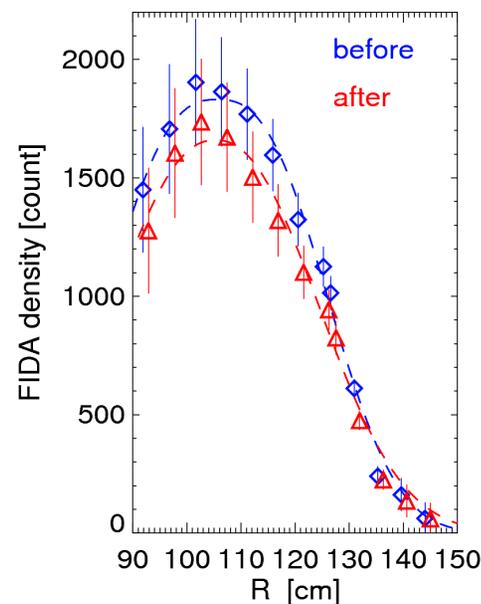
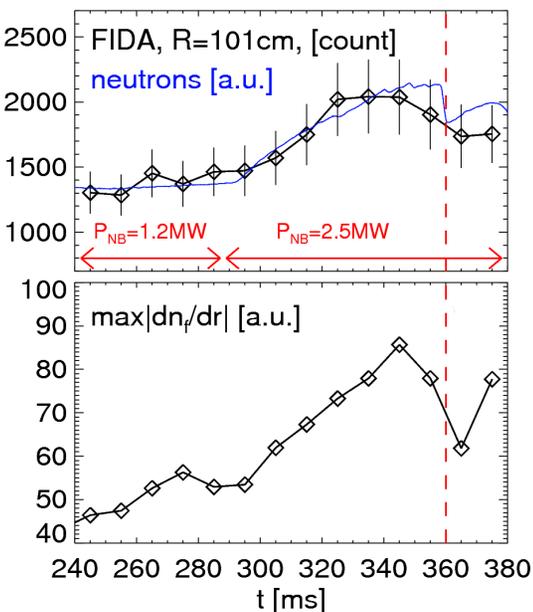
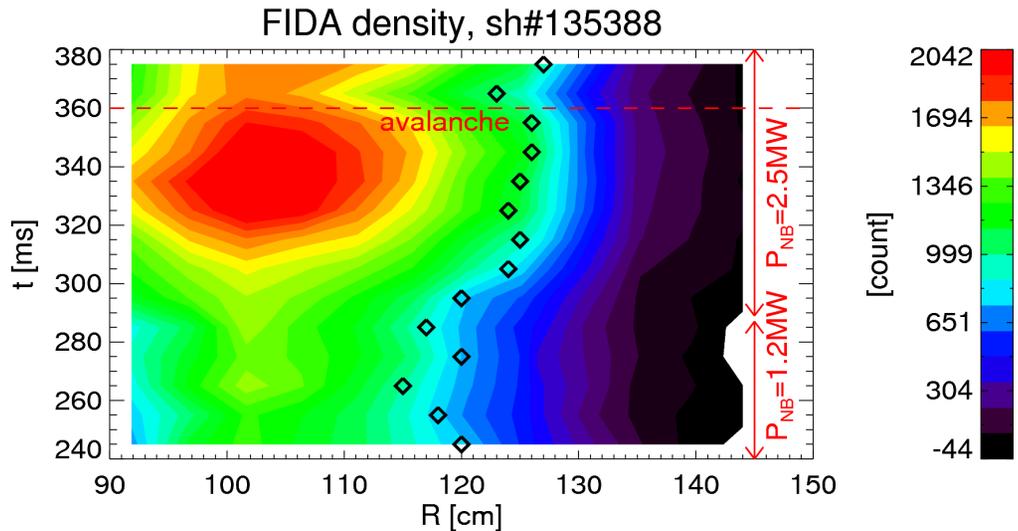


# No detectable fast ion losses are observed during weakly bursting/chirping phase



- Statistical average over  $\sim 20$  events ( $\sim 10$ ms)
- No clear evidence of losses from neutrons, FIDA
  - Does not exclude “continuous” (non-bursting) losses

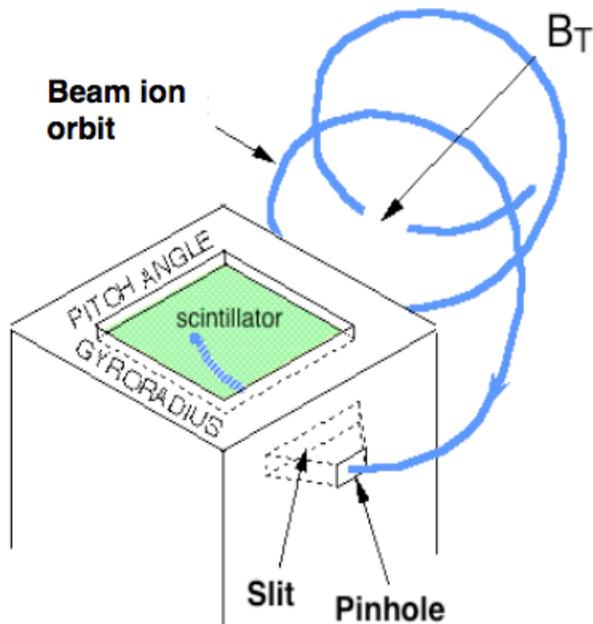
# Up to ~30% of fast ions can be lost during a single TAE avalanche



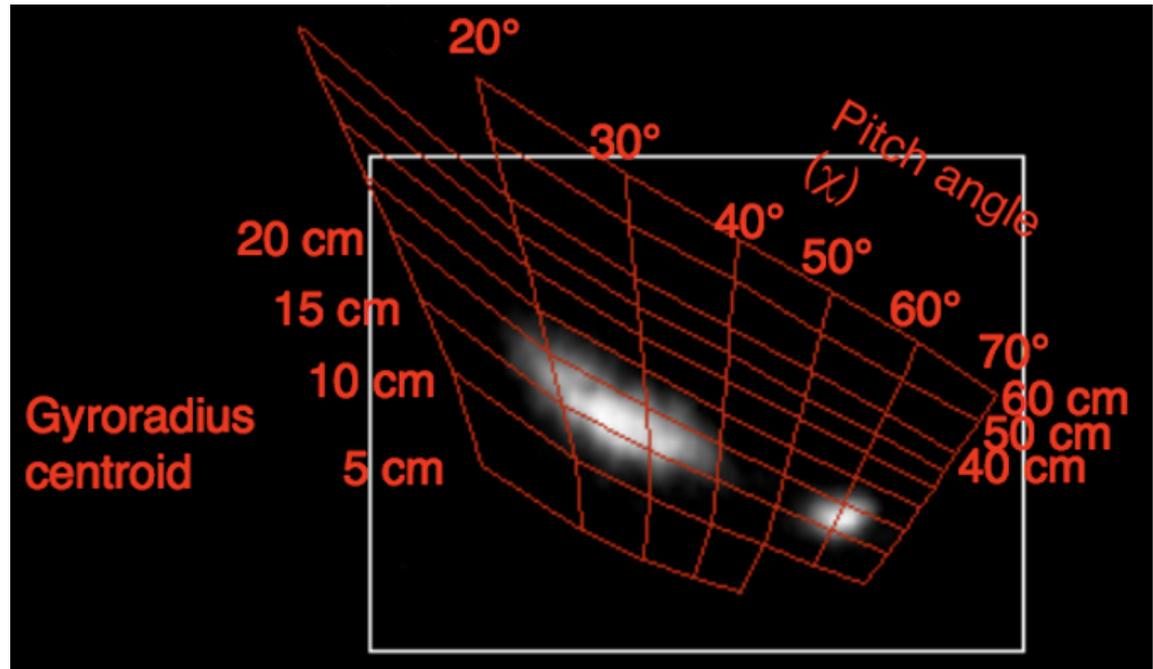
- Fast ion density (FIDA) drops over most of minor radius
- Loss results in a relaxation of the radial gradient  $\rightarrow$  drive for TAEs is reduced
- Comparable losses estimated from FIDA and neutron rate
  - Large portion of phase space affected
- Losses increase with (total) mode amplitude
  - Linear? Quadratic?

# Fast ion loss probe at vessel wall captures transient loss, provides details of affected phase space region

## Scintillator probe, sFLIP:

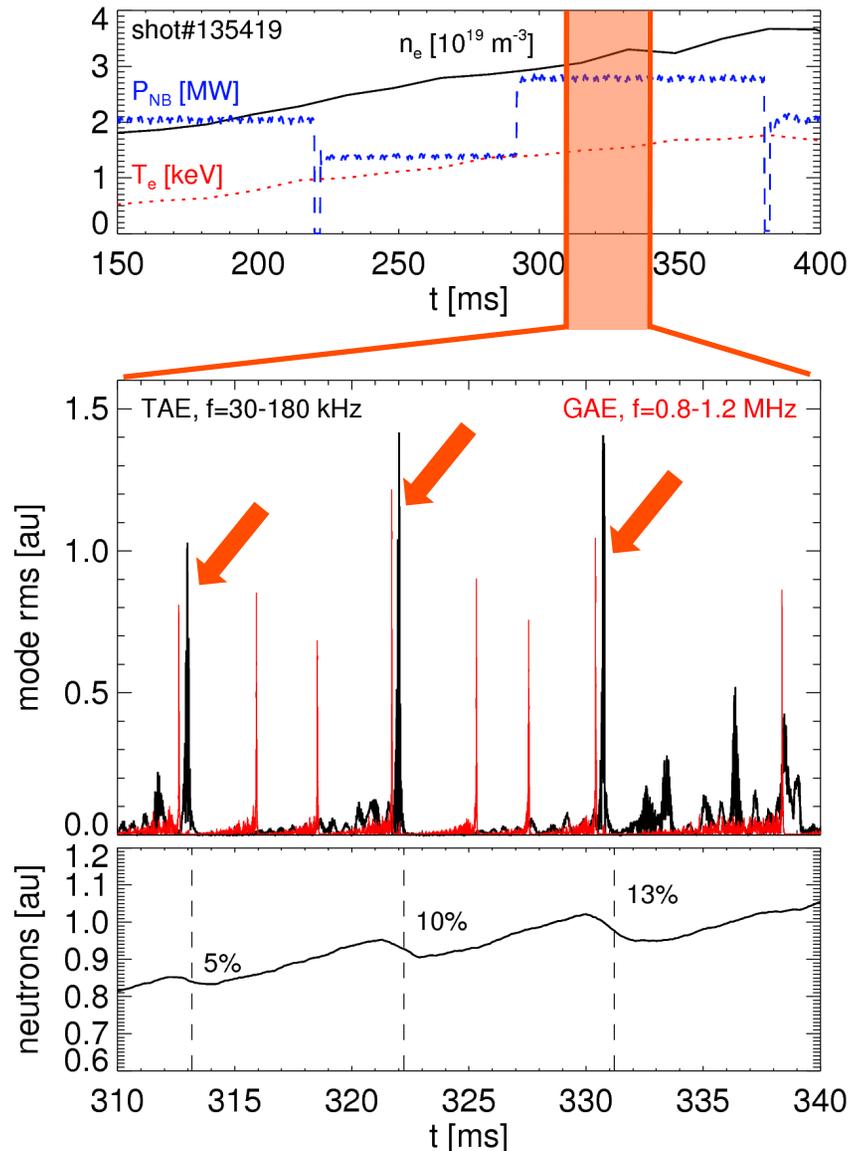


- ‘Magnetic spectrometer’
- Provides  $\Gamma_{\text{loss}}(\rho, \chi, t)$
- $5\text{cm} \leq r \leq 60\text{cm}$
- $15^\circ \leq \chi \leq 80^\circ$
- $f_{\text{sampl}} = 30\text{ kHz}$



- Observed losses at  $E \sim E_{\text{inj}}$ , wide pitch range
  - Possible signature of phase space stochastization
- Phase space model help understand loss process, measurements
- Simulations with ORBIT code Darrow, O-1 under way

# Evidence of redistribution at play – multiple frequency scales can be involved



- Bursting GAEs sometimes observed at  $f \sim 1 \text{ MHz}$  during TAE activity
- GAE bursts precede TAE avalanches
  - But not all TAE avalanches are preceded by GAE burst
- Indication of fast ion redistribution by GAEs?
  - Different mode localization with respect to TAEs
- Losses only observed after TAE avalanches

*Fredrickson, IAEA 2010*

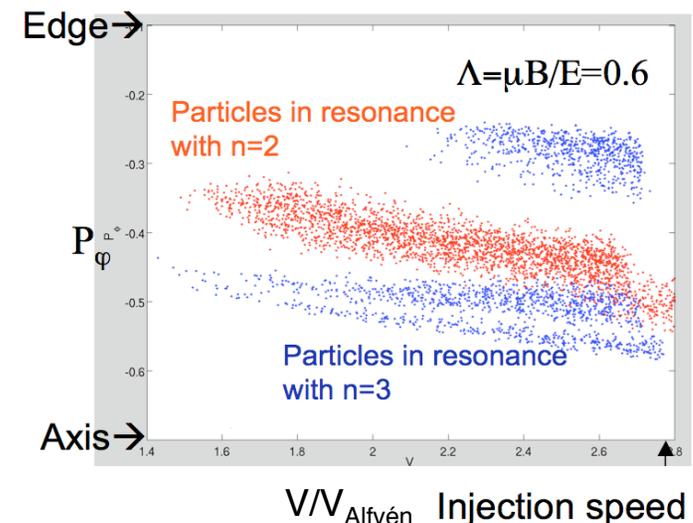
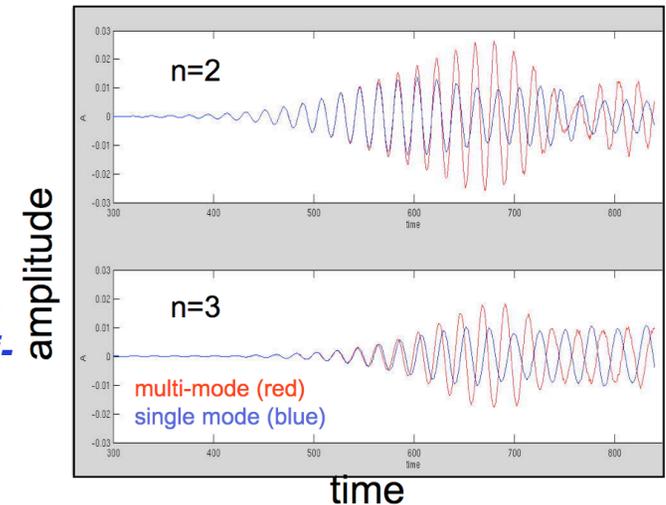
# M3D-K – non-linear, self-consistent Hybrid/MHD code

G.-Y. Fu et al., *Phys. Plasmas* 13, 052517 (2006)

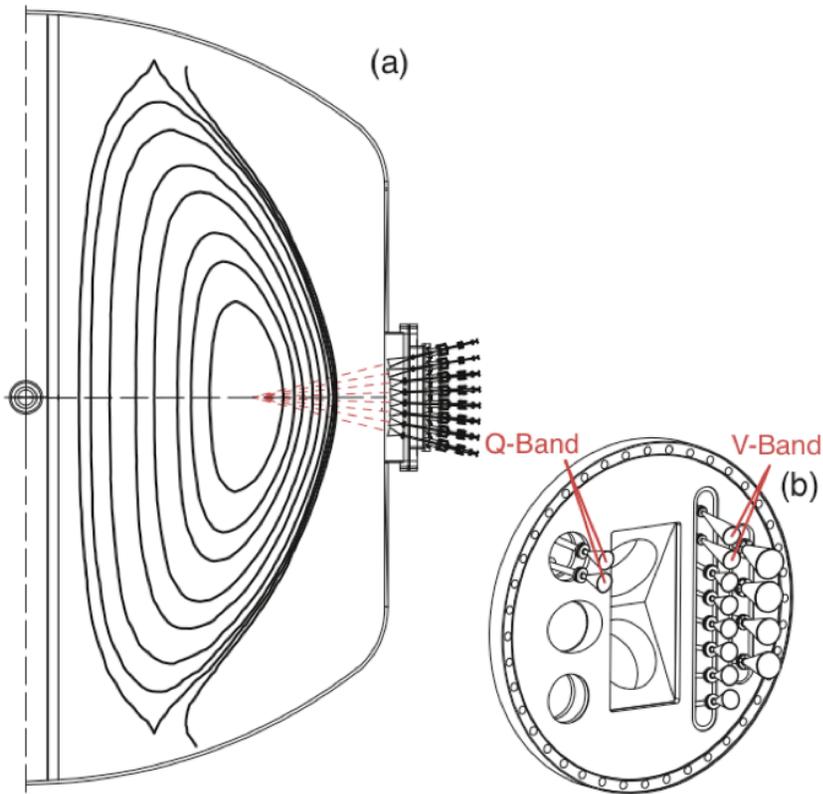
*M3D-K code developed at PPPL and used to investigate fast-ion driven Alfvénic modes and MHD*

- **3-D nonlinear.**
- **Several different physical models:**
  - Resistive MHD.
  - Hybrid (fluid electrons, particle ions).
  - MHD/particle (one-fluid thermal plasma, + energetic particle ions).
- **Full-orbit kinetic ions.**
- **Drift-kinetic electrons.**
- **For particles: Drift-kinetic or gyrokinetic.**

*M3D-K simulation of single vs. multi-mode TAE dynamics*

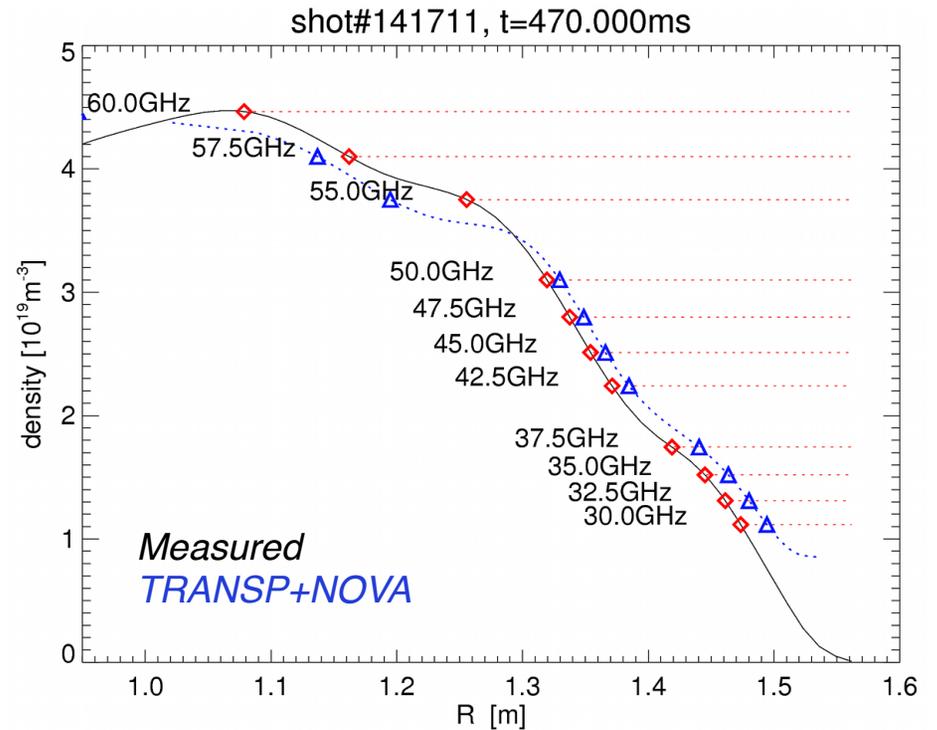


# NSTX reflectometers are used to measure density fluctuations



NSTX Multi-channel reflectometer system (UCLA)

- N. Crocker et al., PPCF 2011 (in press)

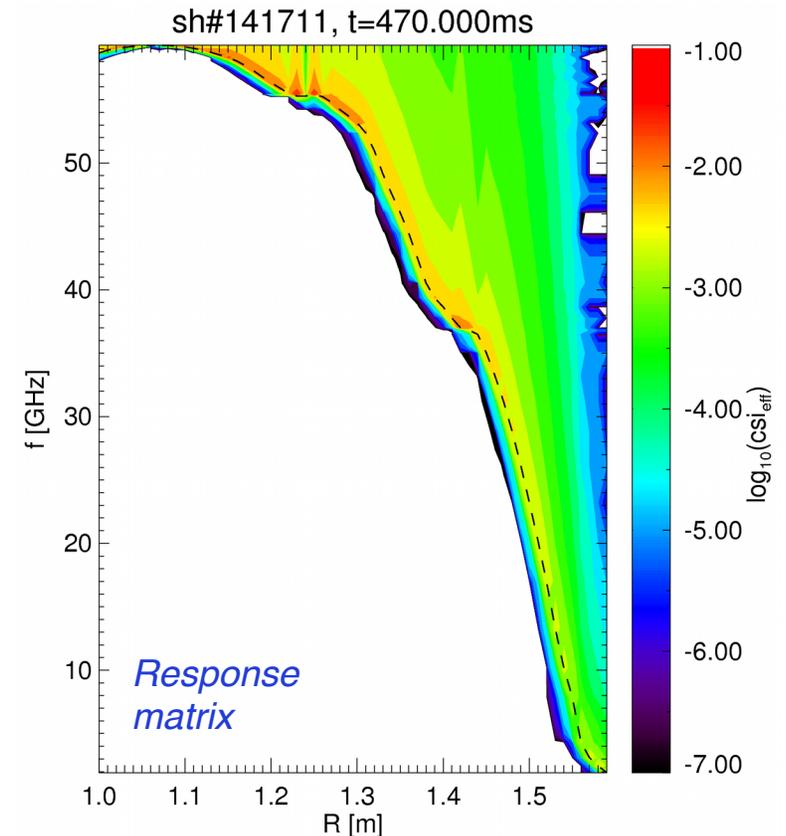
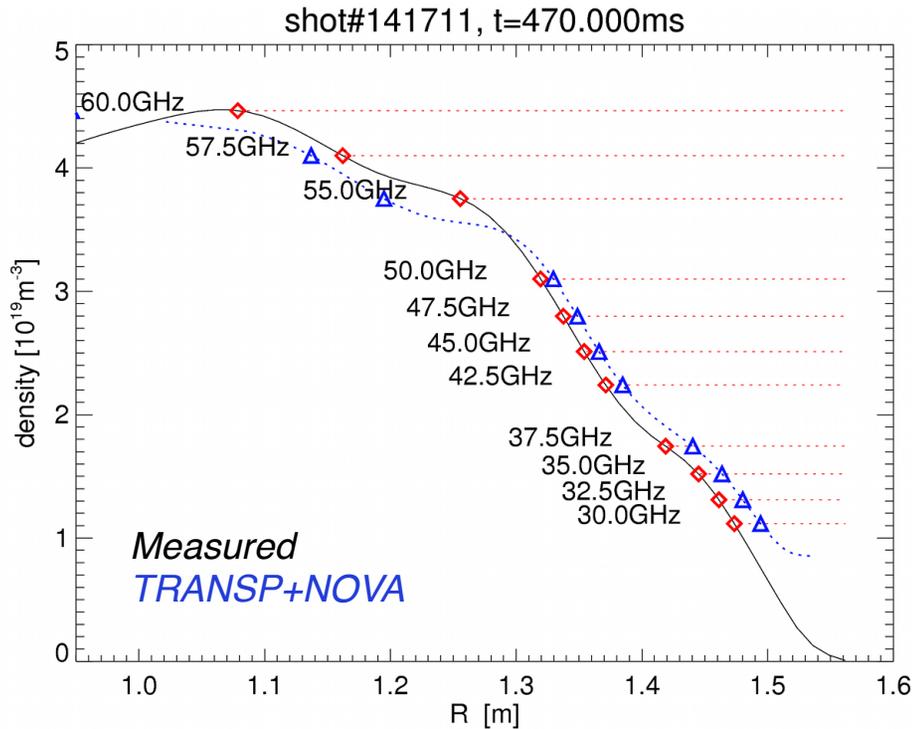


- Low-field side launchers/receivers
- Assume pure O-mode propagation

$$\Delta\Phi = \frac{2\omega}{c} \int_{x_{c.o.}}^{x_{inj}} N dx$$

$$N^2 = \frac{k^2 c^2}{\omega^2} = \frac{c^2}{\omega^2} k_{inj}^2 \left[ 1 - \frac{n(x)}{n_{c.o.}} \right]$$

# Analysis of reflectometer's data



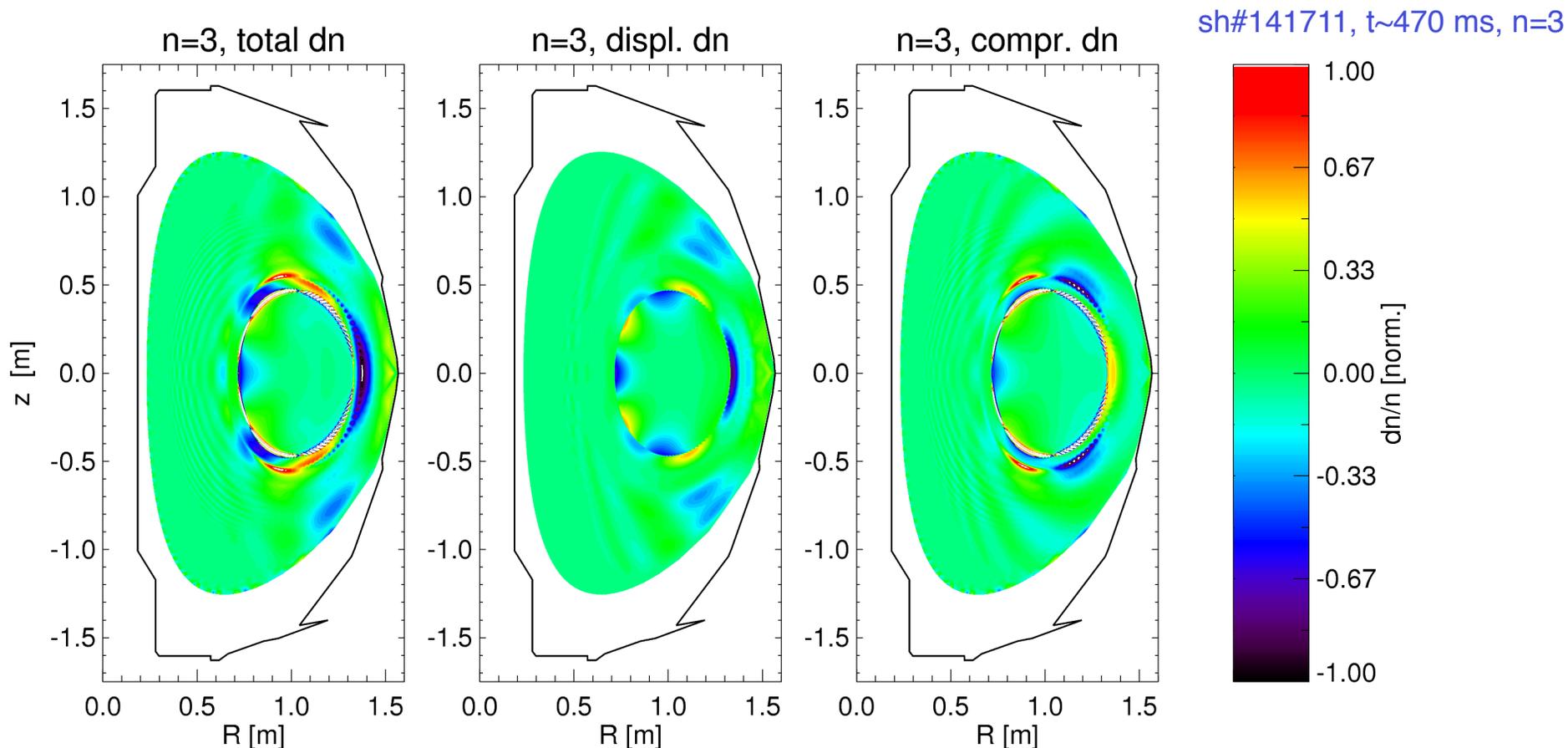
- Low-field side launchers/receivers
- Assume pure O-mode propagation

$$\Delta\Phi = \frac{2\omega}{c} \int_{x_{c.o.}}^{x_{inj}} N dx$$

$$N^2 = \frac{k^2 c^2}{\omega^2} = \frac{c^2}{\omega^2} k_{inj}^2 \left[ 1 - \frac{n(x)}{n_{c.o.}} \right]$$

- Invert data by using *response matrix*,  $M : \Delta\Phi_i = M_{ij} \delta n_j$
- Find total  $\delta n$ , then filter around each mode's frequency
- OK for small (<3%)  $\delta n$
- Assumptions (pure O-mode, linear, ...) likely to break down for large perturbations

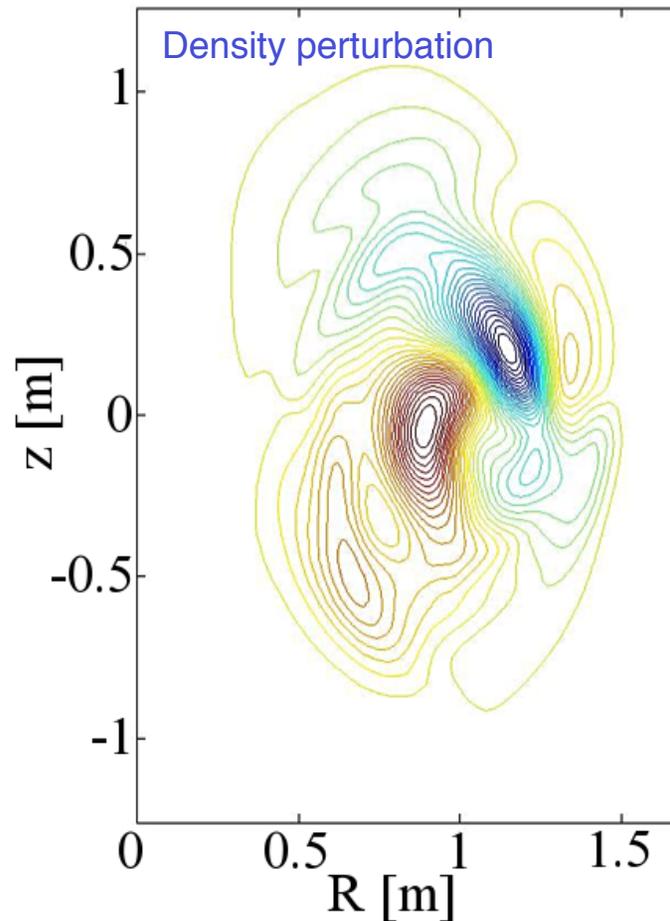
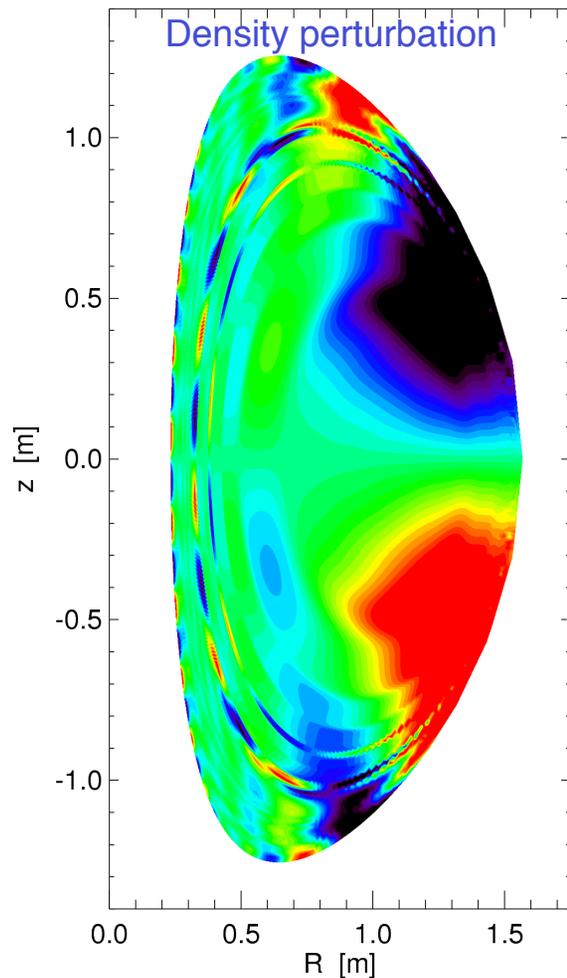
# NOVA analysis reveals significant contribution to density perturbation from compressional term



- Compressional term is significant
- Impact interpretation of reflectometer's data, etc.

$$\frac{\delta n}{n} = \nabla \underline{\xi} - \underline{\xi} \cdot \frac{\nabla n}{n}$$

# MHD unstable $n=1$ kink also found through self-consistent M3D-K code



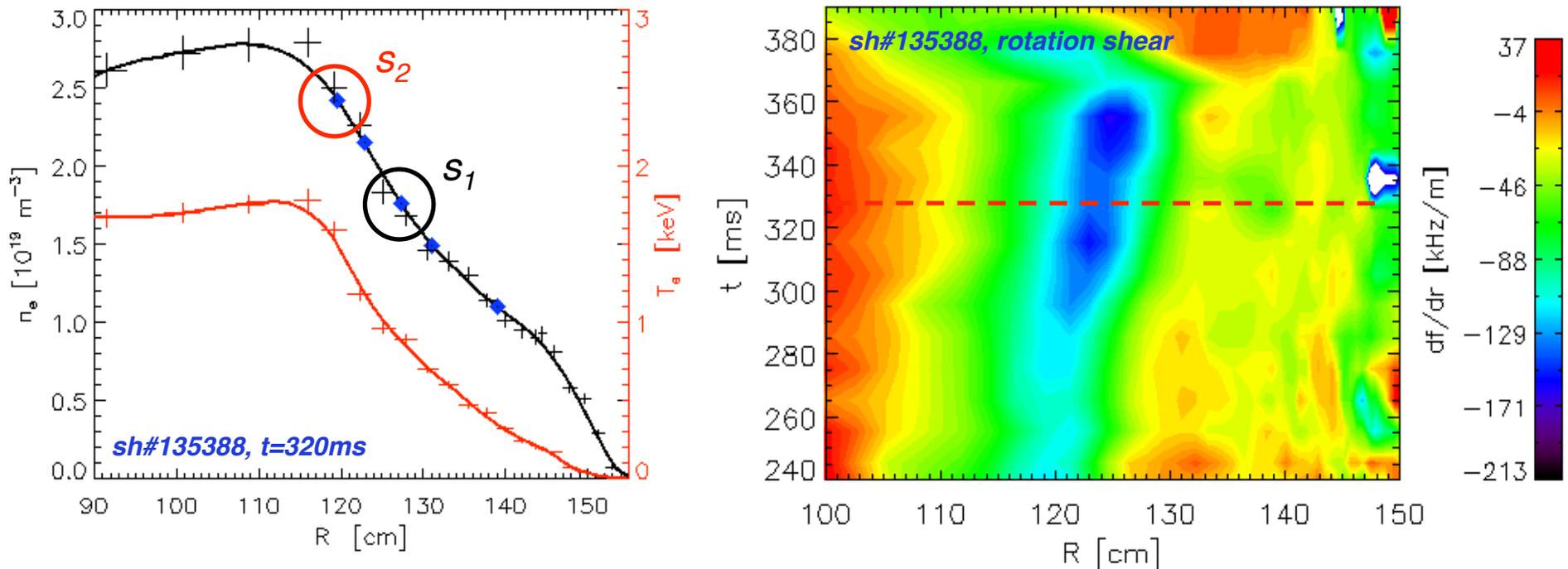
## *M3D-K:*

- *Realistic geometry (spherical tokamak)*
- *Experimental parameters and profiles (interface with TRANSP)*
- *Global; linear/nonlinear*
- *Non-perturbative fast ion effects (i.e., can model EPM) – not used here*
- *Plasma rotation is included*

**Fu, TTF 2011**

- Structure is different between NOVA and M3D-K
- Support hypothesis of marginally stable ‘kink’, destabilized during avalanche

# Multi-channel reflectometer is used to look for decorrelation of TAE across rotation shear layer

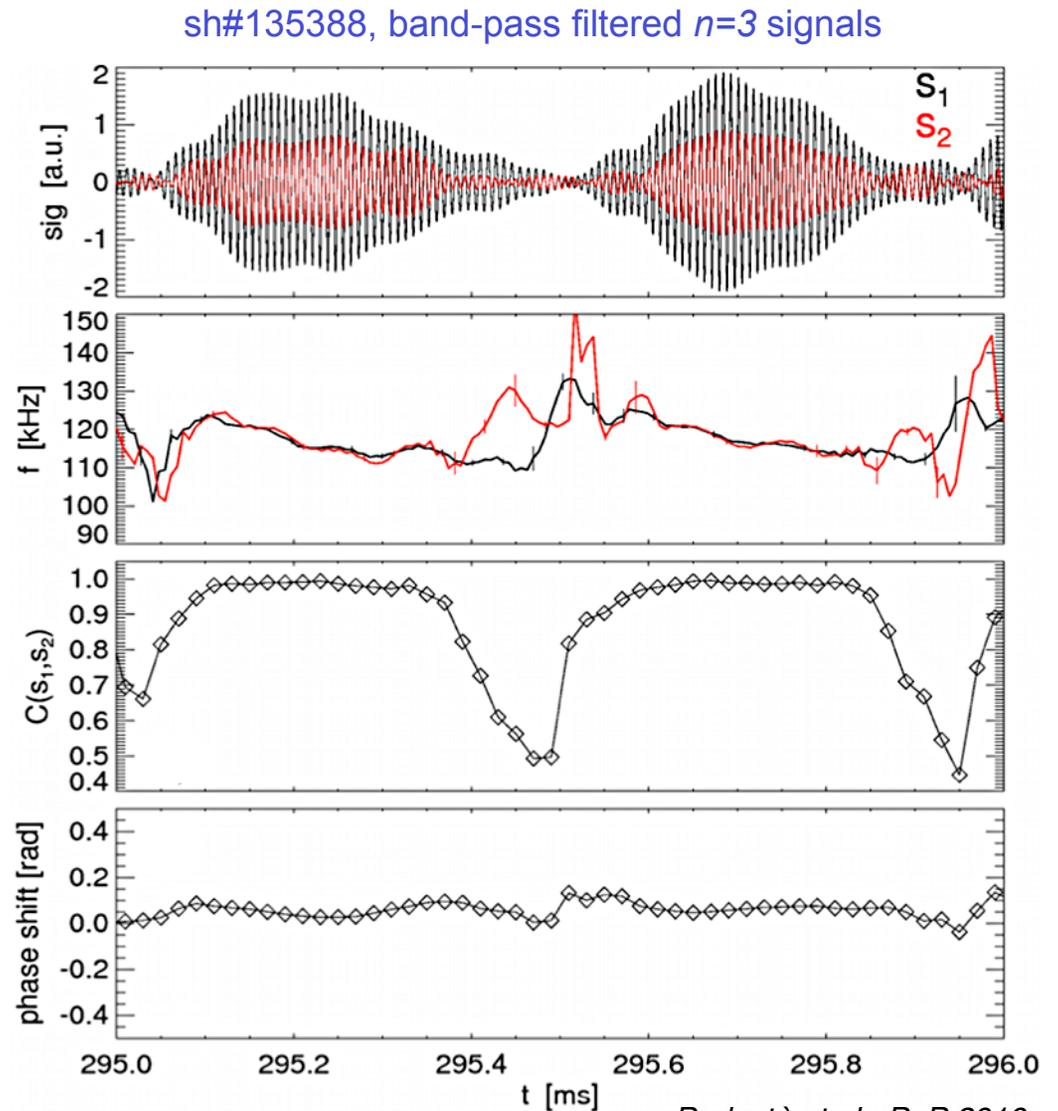
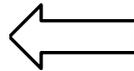
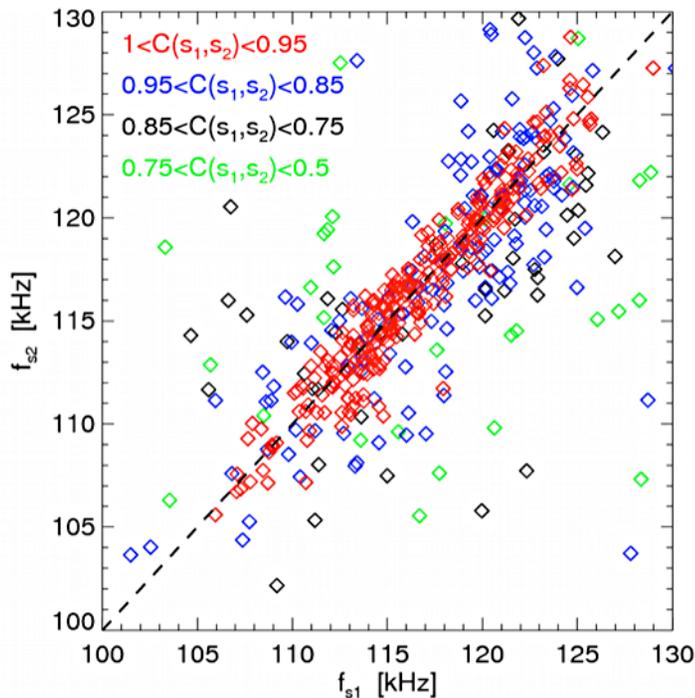


## Procedure:

- Band-pass filter signals around mode frequency (ex.  $n=3$ )
- Reconstruct frequency, amplitude evolution
- Get cross-correlation
- Obtain cross-phase between channels from time delay

# Results from reflectometer show no evidence for spatial decorrelation of the modes across shear layer

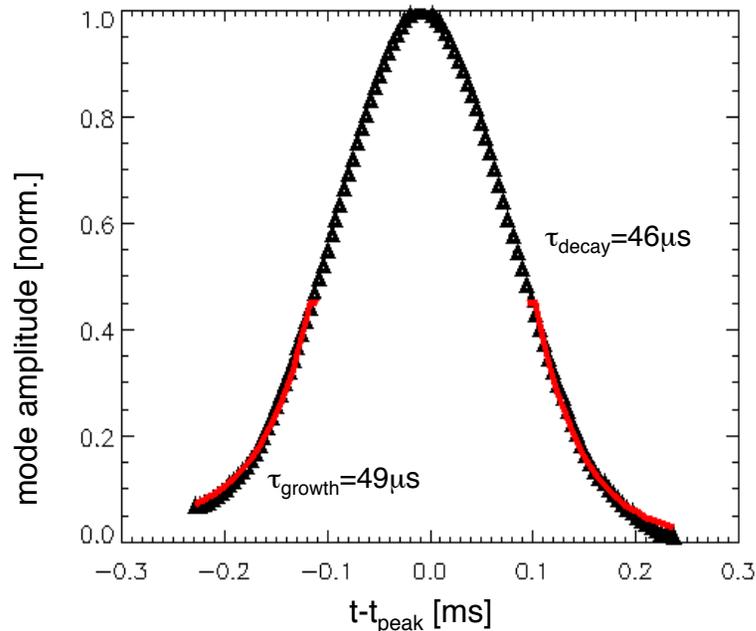
- No difference in measured frequency
- Mode starts decaying when cross-correlation is still  $\sim 1$
- No systematic cross-phase variation during chirps



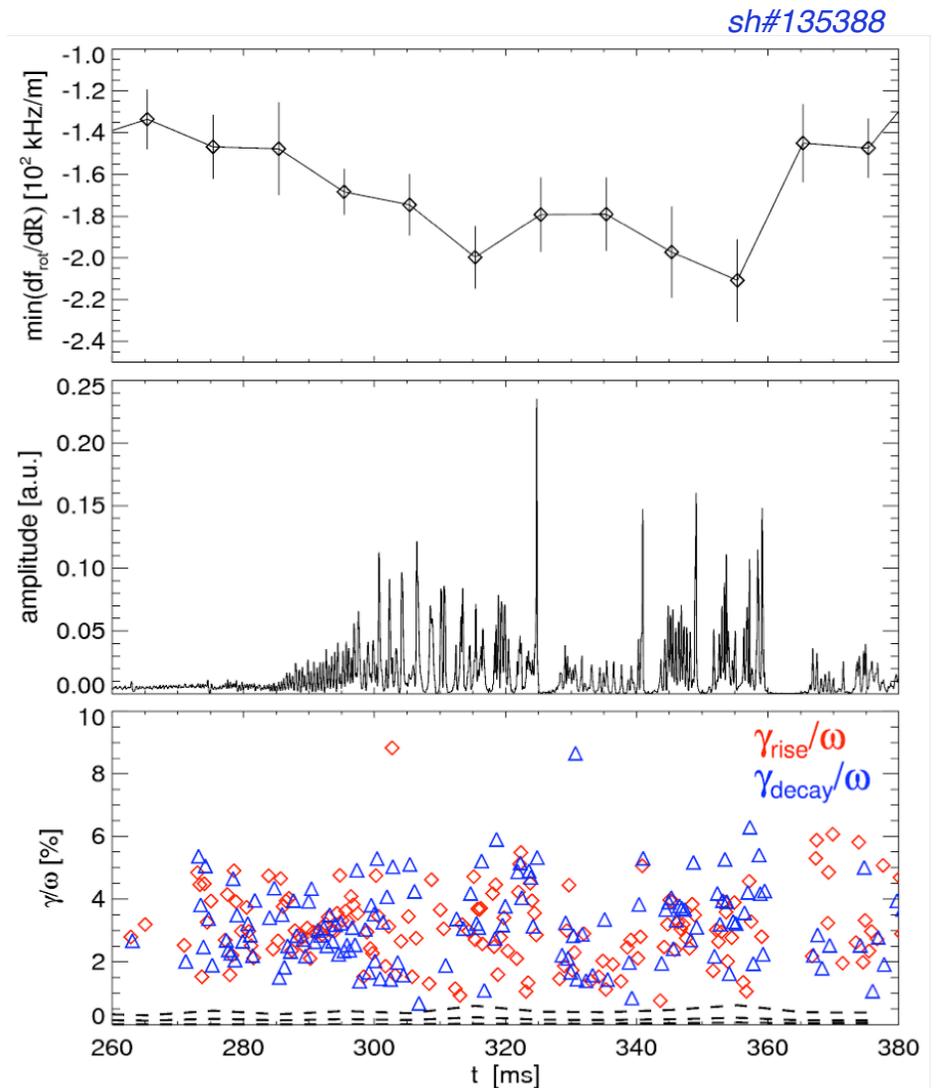
Podestà et al., PoP 2010

# No temporal correlation is observed between rotation shear evolution and mode amplitude rise/decay rates

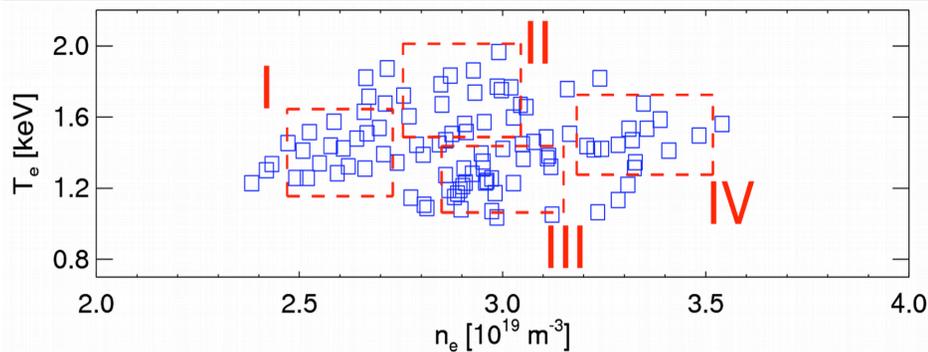
- Effective rise/decay rates calculated from exponential fit (B-dot data)



- Shear increases in time
- No correlation with inferred rates

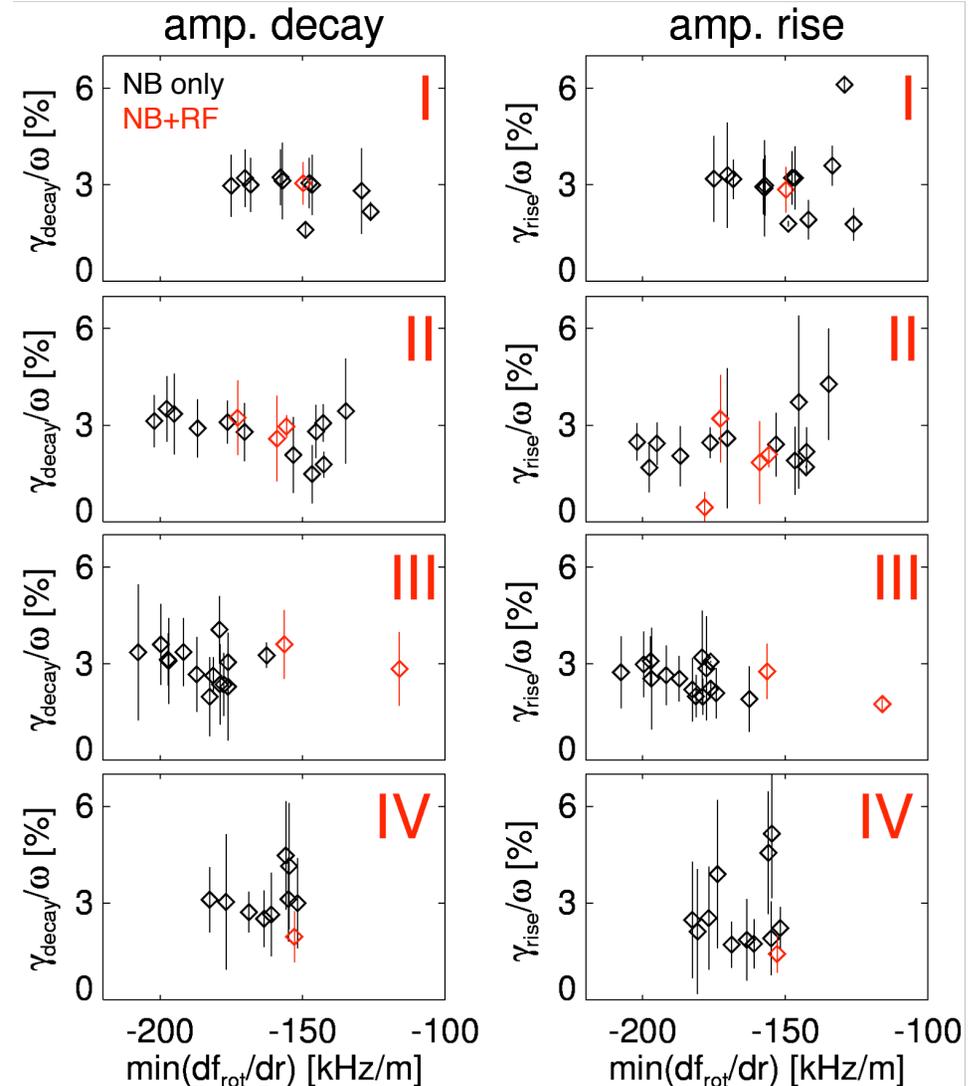


# Statistically significant ensemble does not show any clear trend of rise/decay rates on rotation shear

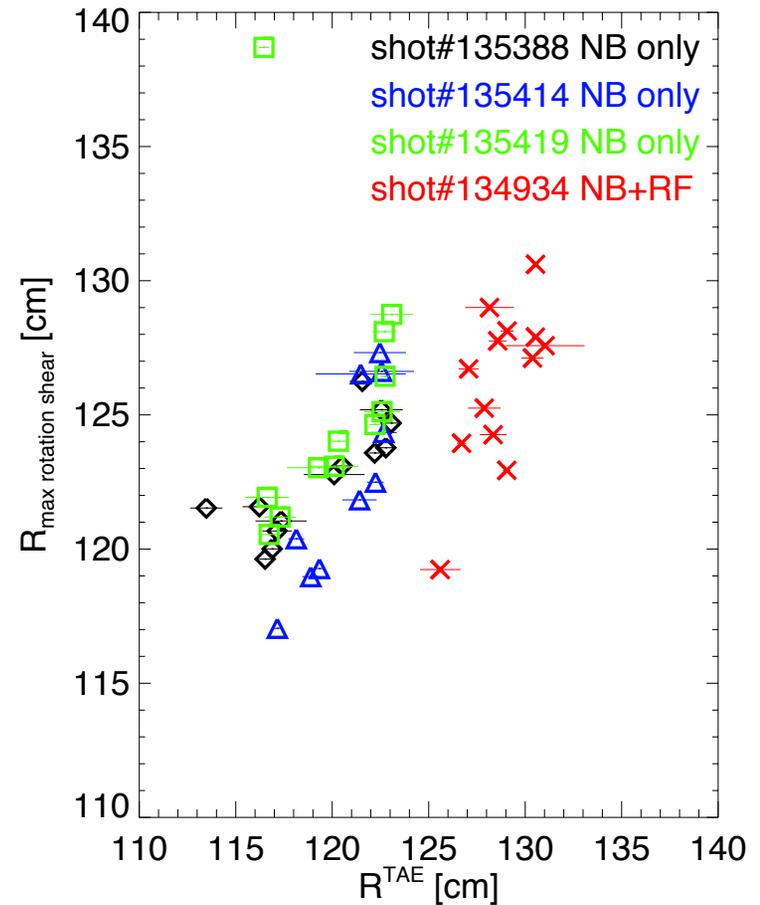
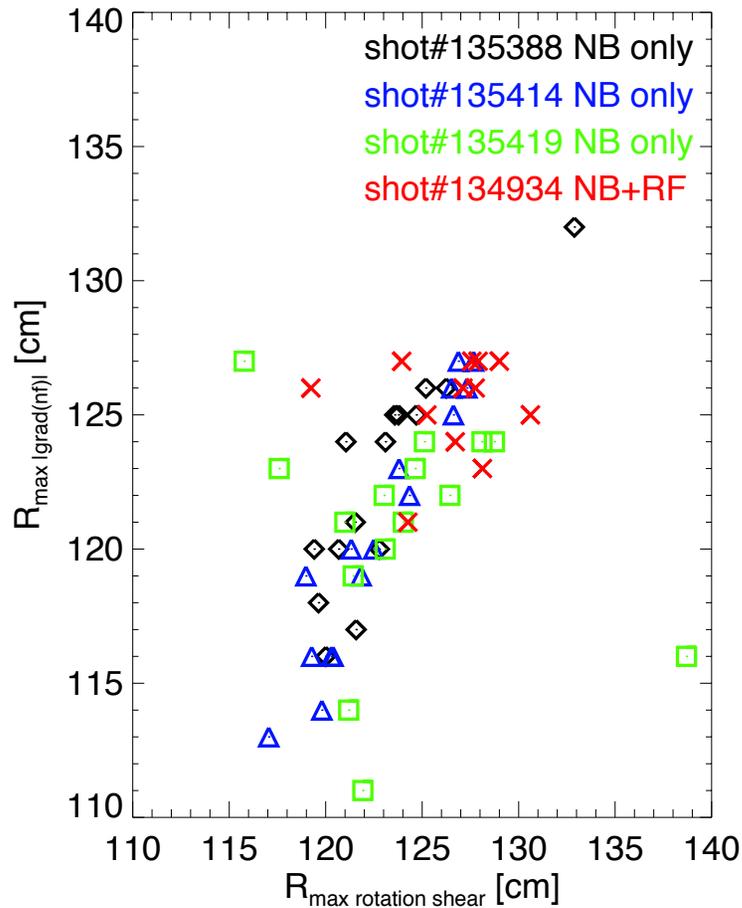


- Database of 10 discharges
- Group data with similar  $n_e$ ,  $T_e$ 
  - Similar damping on thermal plasma
- No simple dependence on injected NB power,  $T_e$ ,  $n_e$ , ...
- Trends hidden by changes in  $q$  profile, gap structure, ... ?

$n=3$  mode, 10 ms average

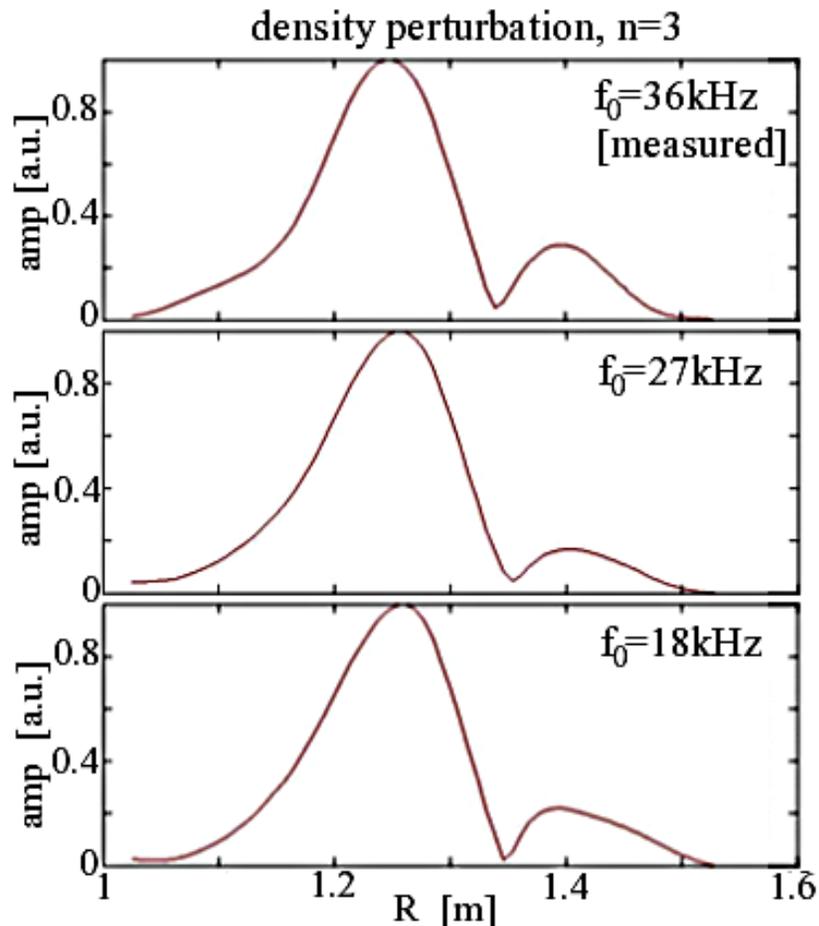


# Additional RF power marginally successful in decoupling fast ion, TAE and thermal plasma dynamics



- May explain slight differences between NB-only and NB+RF

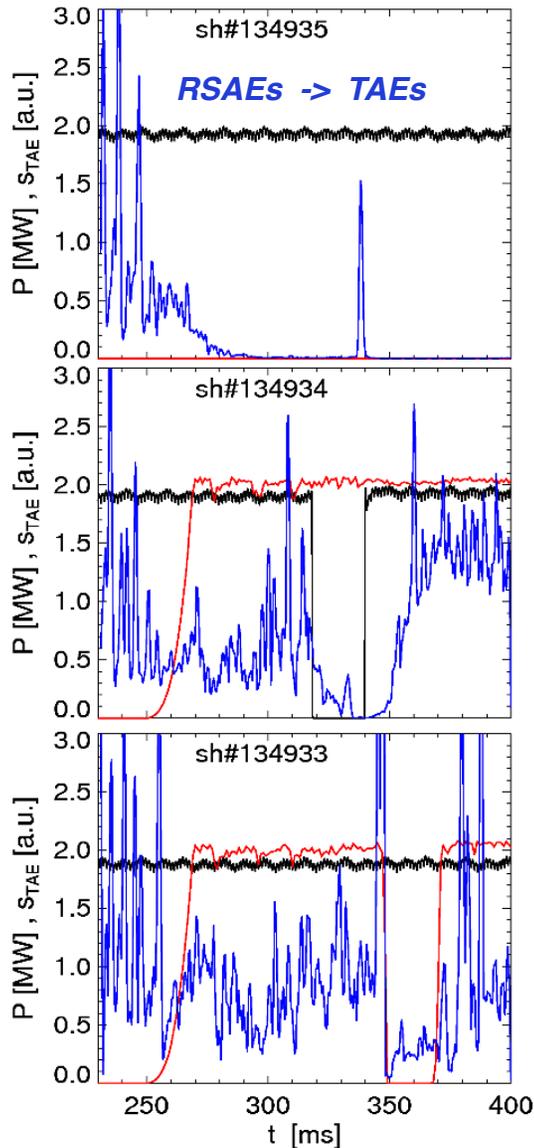
# Preliminary results from M3D-K also show little effects of rotation on TAE structure



- No fast ion effects included
- Scale rotation profile from measured  $f_0=36$  kHz down to  $f_0=18$  kHz (50% reduction)
- Mode peak location, structure do not change substantially

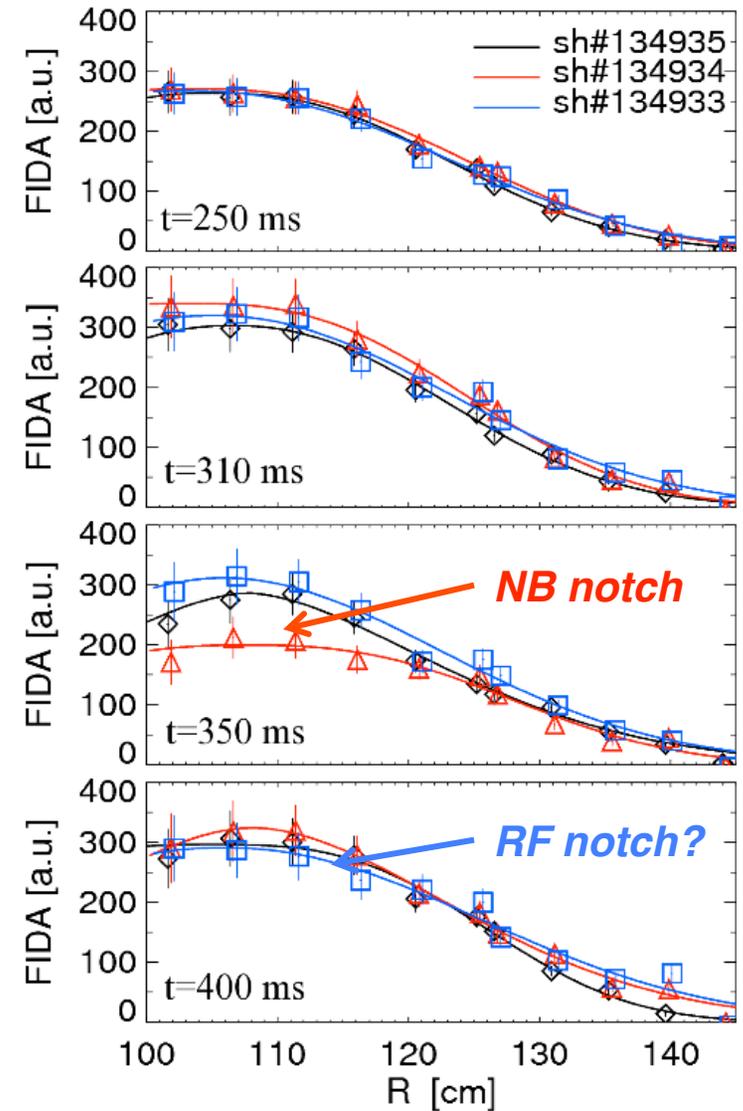
*Fu, TTF 2011*

# Fast ion population is key parameter to destabilize TAEs; subtle details hard to get experimentally...



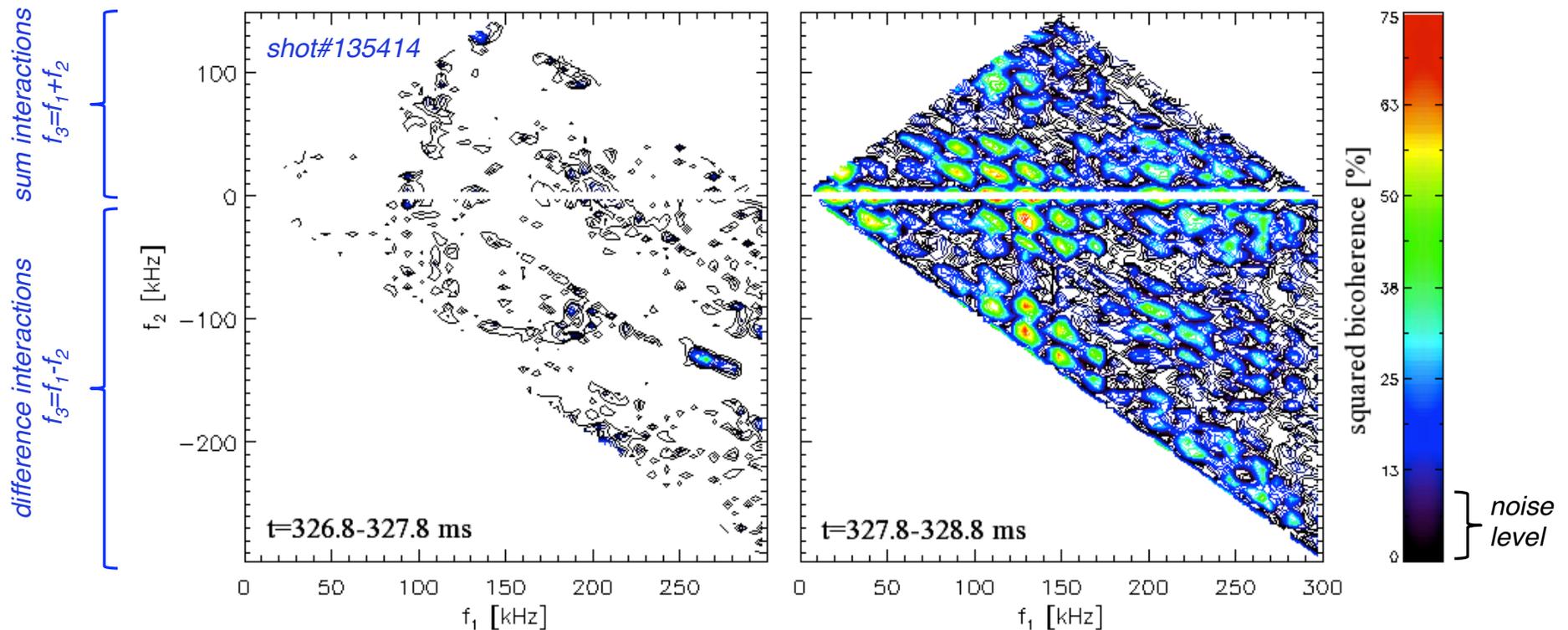
**NB only**  
**NB+RF, NB notch**  
**NB+RF, RF notch**

- Marginal variations in  $n_f(R)$ ,  $\text{grad}(n_f)$  from FIDA, except for 100% change in source
- Can not differentiate between role of  $\beta_{f.i.}$  and radial gradient
- OK to look at trends



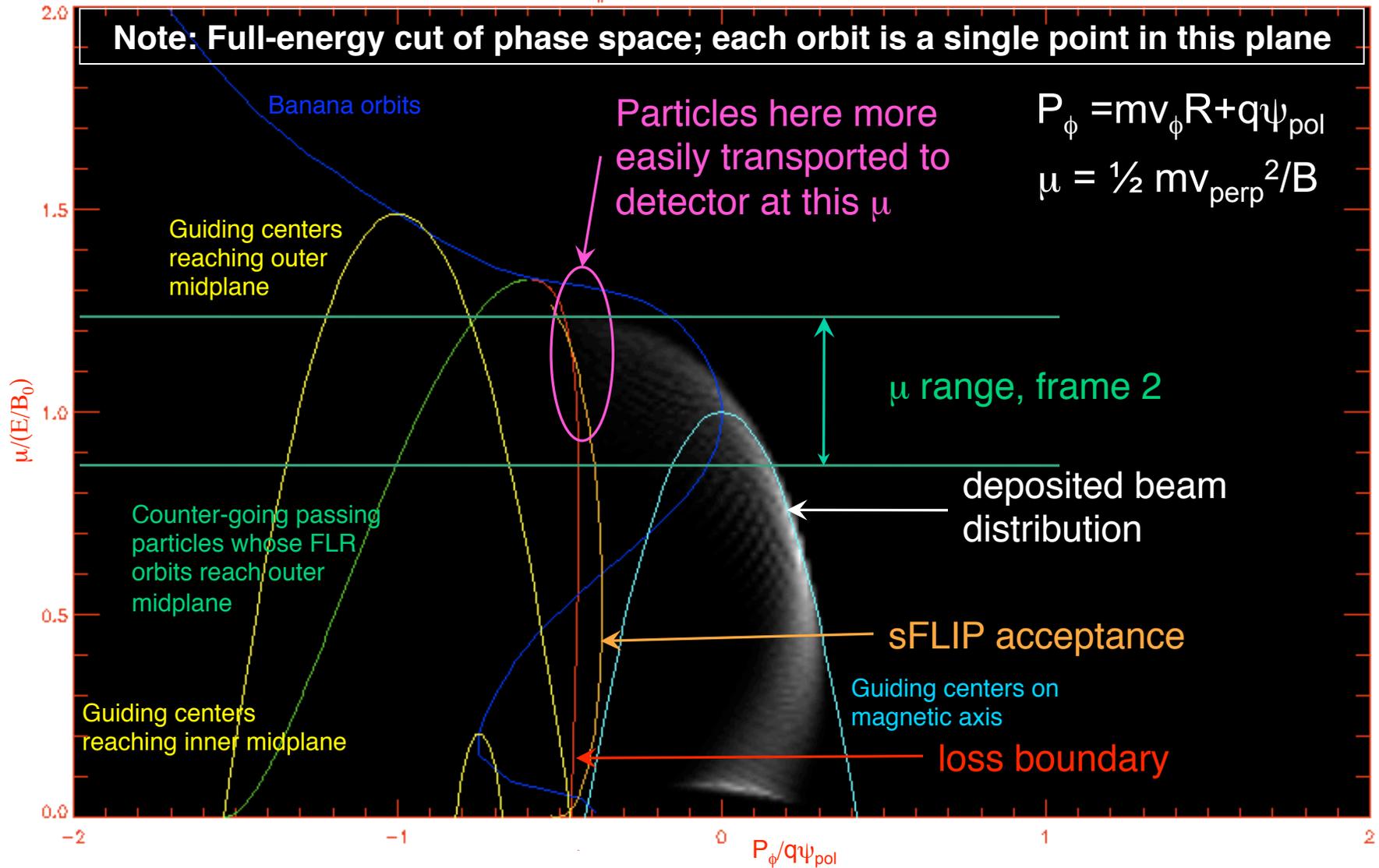
# Bicoherence suggests coupling between modes at play during large bursts

- High bicoherence >70% measured during burst
  - Average over 11 Mirnov coils distributed toroidally over 360°
  - Indicative of sum/difference interactions between modes
  - Both TAEs and low-frequency modes participate

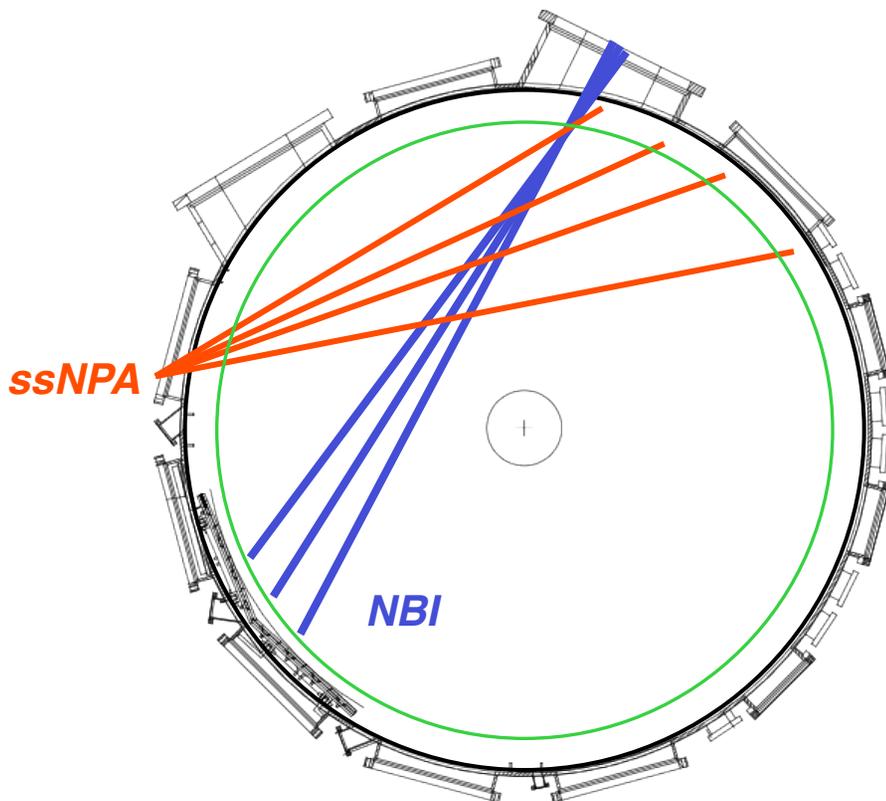


# Proximity of beam ions to sFLIP detector at high $\chi$ (i.e. high $\mu$ ) indicates why loss appears there first

shot#: 141707a shotTime: 485

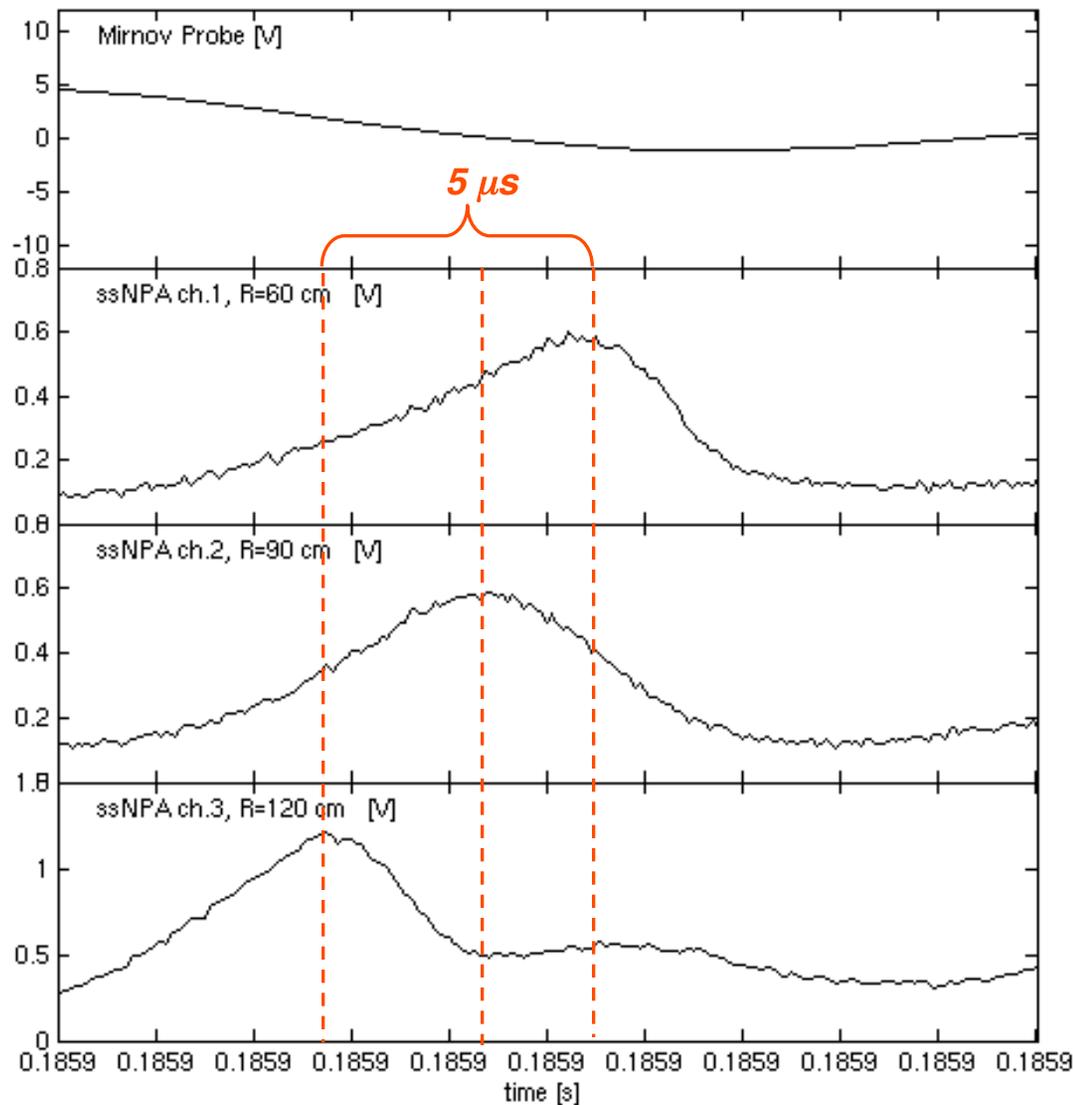


## Solid State NPA diagnostic on NSTX operated in “current mode” during FY-10 for high temporal resolution data on mode-induced fast ion losses



- Measurement of flux of energetic neutrals
- 4 lines of sight on the NBI
  - $R_{\text{tan}} = 60, 90, 100, 120 \text{ cm}$
- Pinhole & Silicon photodiode detector (AXUV)
- Aluminum foil (150nm) blocks light, SXR, low energy neutrals (<10 keV)
- Detected neutrals generated by Charge Exchange of fast ions with **beam** and/or **edge** neutrals

# 'Fishbone beacon' observed during transient fast-ion losses associated with chirping modes



- Fast frequency chirping instabilities (e.g. TAE) accompanied by periodic bursts in ssNPA signals
- Fast ion loss cone, rotating in phase with the mode, is inferred based on time delay between ssNPA channels
- Burst appear at different phases in different channels

# Open Issues

- How to scale present experiments to future devices (ITER), burning plasmas?
  - Code validation, multi-machine comparison are the key
    - > Linear codes (NOVA)
    - > Quasi-linear models, self-consistent codes (M3D-K)
    - > Investigate wave-fast ion interaction (ORBIT, SPIRAL)
    - > *Improve stability calculations*
  - But: conditions will be very different, e.g.  $F_{f.i.}(r,v,t)$  from alpha's (+NB, RF, ...)
    - > E.g. need better understanding of role of spatial vs. velocity gradients
  - Parallel effort: develop control tools
    - > Act on NB deposition, q-profile? Active antennas?
- Combine different diagnostics/techniques; develop phase-space models to interpret results consistently