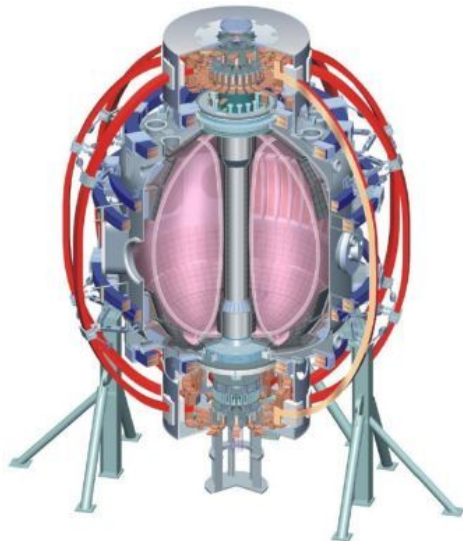


# Development of Improved Vertical Position Control

**S.P. Gerhardt, E. Kolemen**

## ASC XP Group Review

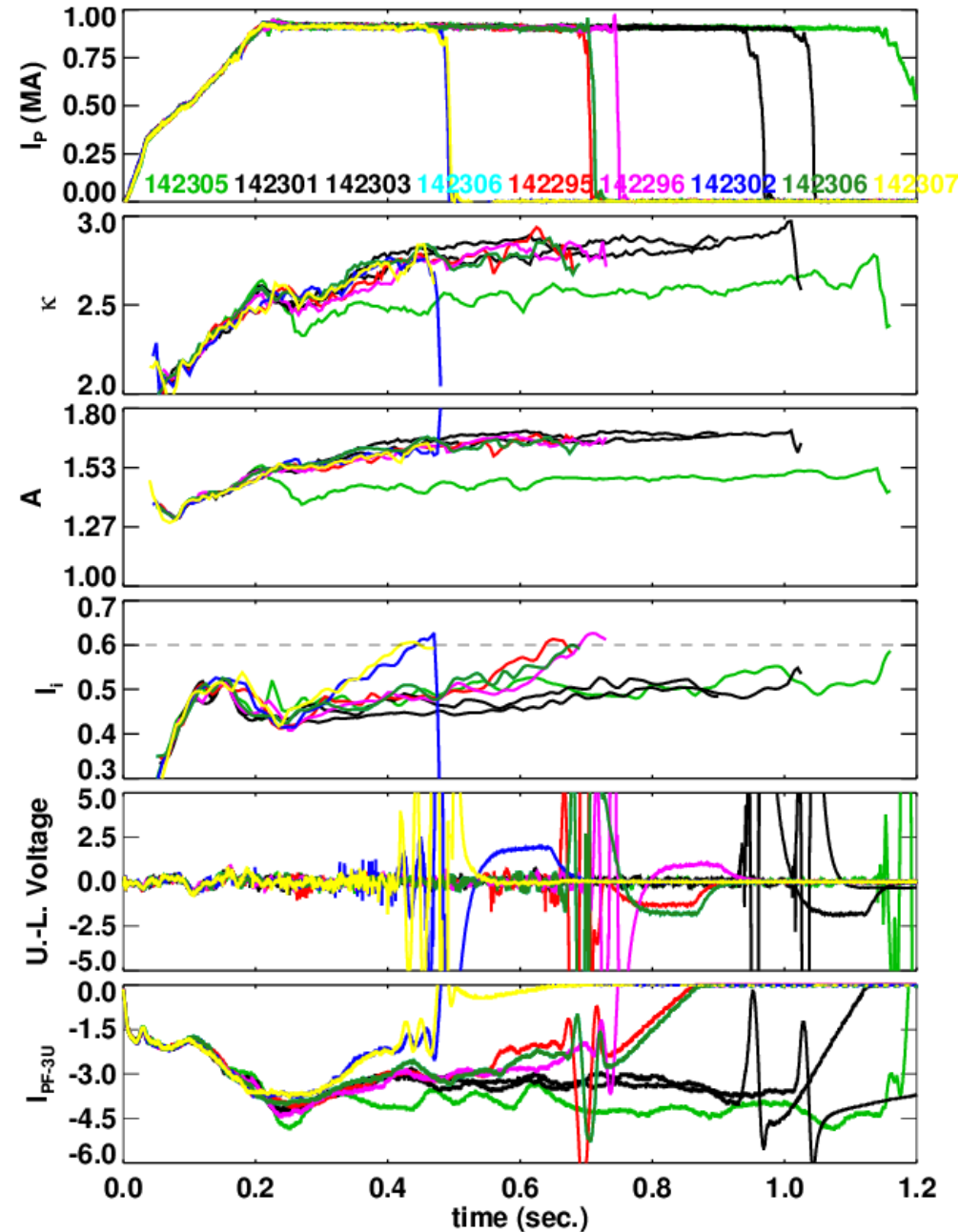
*College W&M  
 Colorado Sch Mines  
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 General Atomics  
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 MIT  
 Nova Photonics  
 New York U  
 Old Dominion U  
 ORNL  
 PPPL  
 PSI  
 Princeton U  
 Purdue U  
 SNL  
 Think Tank, Inc.  
 UC Davis  
 UC Irvine  
 UCLA  
 UCSD  
 U Colorado  
 U Illinois  
 U Maryland  
 U Rochester  
 U Washington  
 U Wisconsin*



*Culham Sci Ctr  
 U St. Andrews  
 York U  
 Chubu U  
 Fukui U  
 Hiroshima U  
 Hyogo U  
 Kyoto U  
 Kyushu U  
 Kyushu Tokai U  
 NIFS  
 Niigata U  
 U Tokyo  
 JAEA  
 Hebrew U  
 Ioffe Inst  
 RRC Kurchatov Inst  
 TRINITI  
 KBSI  
 KAIST  
 POSTECH  
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 ENEA, Frascati  
 CEA, Cadarache  
 IPP, Jülich  
 IPP, Garching  
 ASCR, Czech Rep  
 U Quebec*

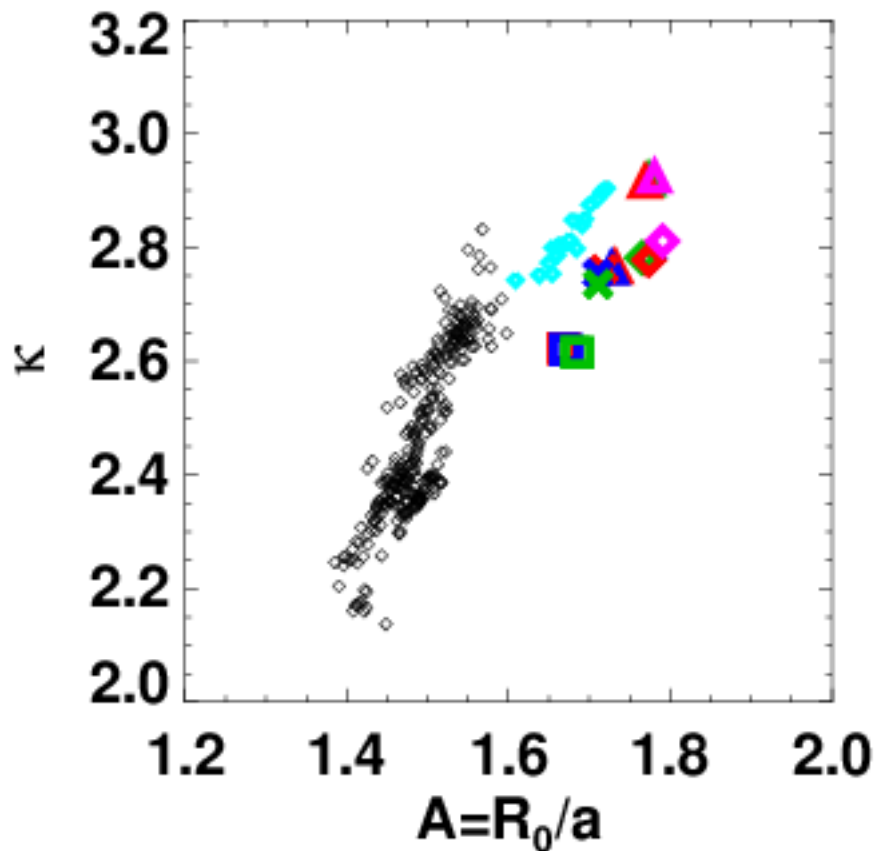
# XP in 2010 Showed that Vertical Position Control can be Lost at Higher Aspect Ratio

- 1 Fiducial (green) and 8 shots at higher aspect ratio.
  - Black cases vertically stable, the colored ones have VDEs.
- *VDE is always triggered when  $I_i=0.6$ .*
  - This is not a particularly high value.
  - Would preclude use of the scenario for many XPs.
- Other instances of vertical stability problems.
  - Egemen's squareness XP.
  - Ron Bell's DIII-D comparison XP.
  - After every nearly every locked mode and RWM.
- *Motivates improvements to the  $n=0$  controller.*

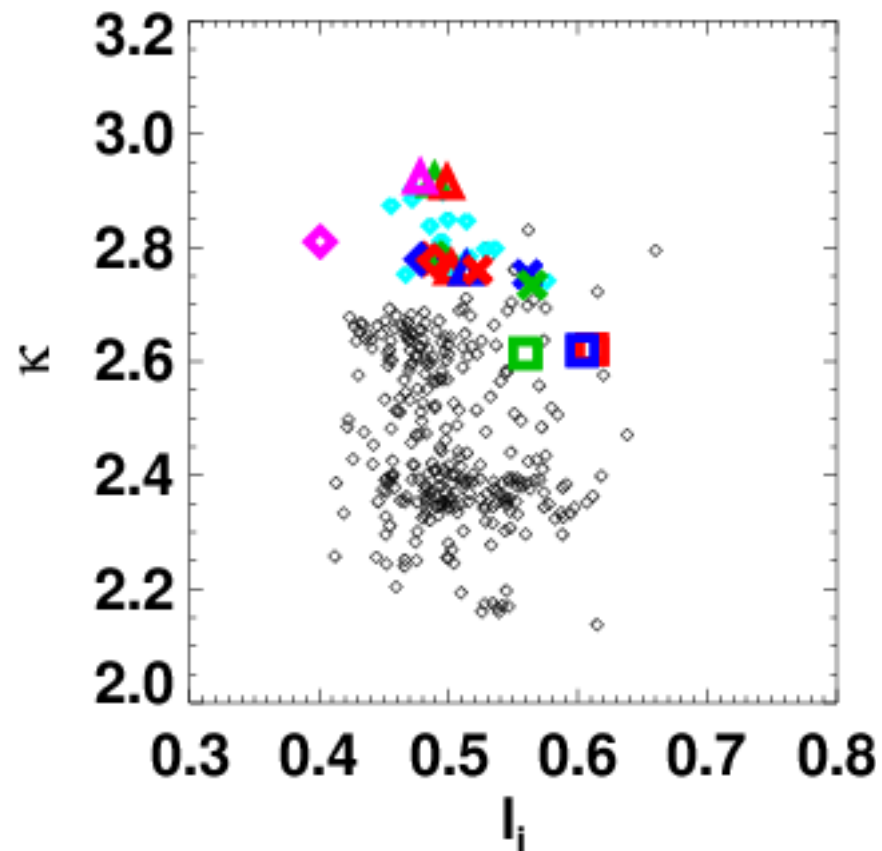


# Interesting Scenarios for the Upgrade Will Push Against These Limits

*Ask for high-kappa at even larger A.*



*Ask for high-kappa at values of  $I_i$  comparable to present values.*



# Strategy To Fix Problem

- Improve the detection of small vertical motion.
  - “dZ/dt Observer”
- Re-optimize vertical control gains with improved observer.
- If necessary, use RWM coils for vertical control.

# Vertical Position Controller is a PD Controller Using Loop Voltages for $dZ/dt$ Measurement

- Proportional controller is simply the Isoflux shape control algorithm:

$$V_{PF-3,P} = M \times PID(\text{segment error})$$

- Fast derivative controller is based on the up-down loop voltage difference.

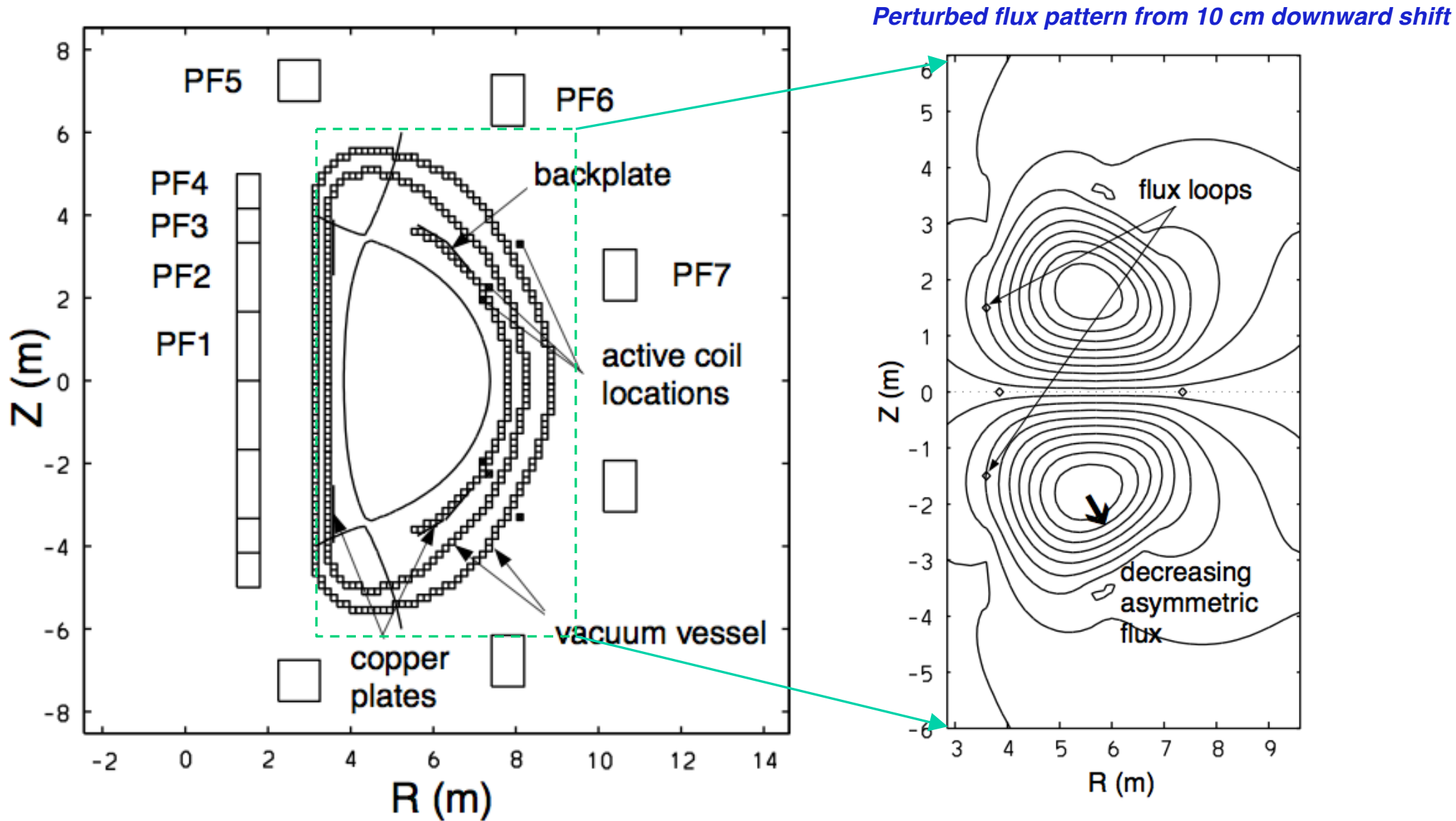
$$V_{PF-3,D} = D \times (\dot{\psi}_{Upper-Loop} - \dot{\psi}_{Lower-Loop})$$

- The underlying assumption is that the plasma vertical position can be measured by only 2 loops:

$$I_p Z_p = C \times (\psi_{Upper-Loop} - \psi_{Lower-Loop})$$

- Thesis: Using more/different loop voltages will lead to a better estimation of the plasma position.
  - Eliminate  $n=1$  pickup from random loop orientation problems.
  - More information for shapes that are distorted.
- Proper selection of measurement loops has been emphasized in the literature:
  - Ward & Hofmann, Nuclear Fusion 34, 401 (1994)
  - Pomphrey, Jardin, and Ward, Nuclear Fusion 29, 465 (1989)
  - Albanese, Coccoresse, and Rubinacci, Nuclear Fusion 29, 1013 (1989)
  - C. Kessel, et al., Nuclear Fusion 41, 953 (2001)

# Inboard Side Loops Were Chosen in a Study for ITER Control in Kessel, et al.



What is the common perturbed flux pattern for NSTX cases?



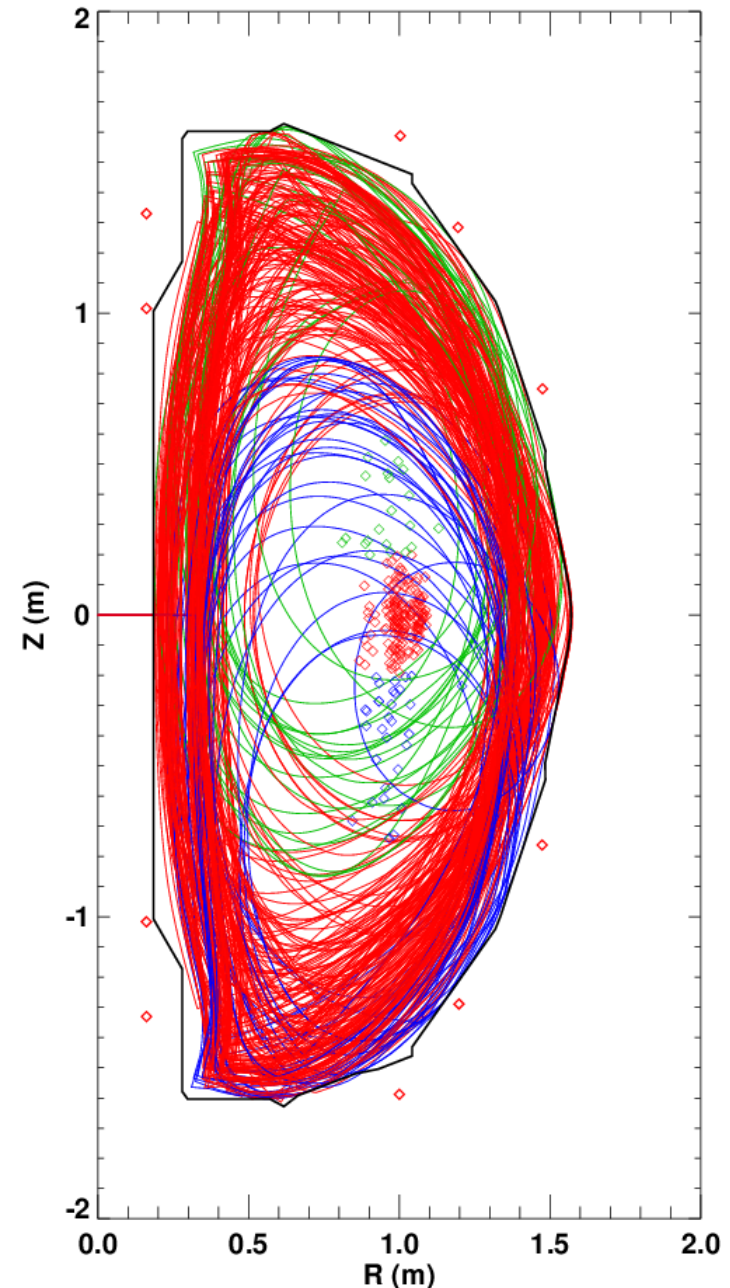
# Use a Database of Equilibria to Determine Which Loops are Best For Detecting Vertical Motion

- Consider ~290 NSTX equilibria.
  - Majority from LRDFIT and EFIT reconstructions
    - Include currents in the passive plates, mode non-rigidity.
  - Minority generated with ISOLVER
- Computed the flux at the various flux loop locations.
- Fit the magnetic axis location to a function:

$$I_P Z_P = \sum_{i=1}^{NumLoopPairs} \alpha_i \times (\psi_{Upper-Loop,i} - \psi_{Lower-Loop,i})$$

$$Z_P = \frac{\max(Z_{boundary}) + \min(Z_{boundary})}{2}$$

- Find coefficients  $\alpha$  from:
  - linear SVD solution, or
  - constrained optimization
    - Prevent any single value  $\alpha$  from becoming too large.



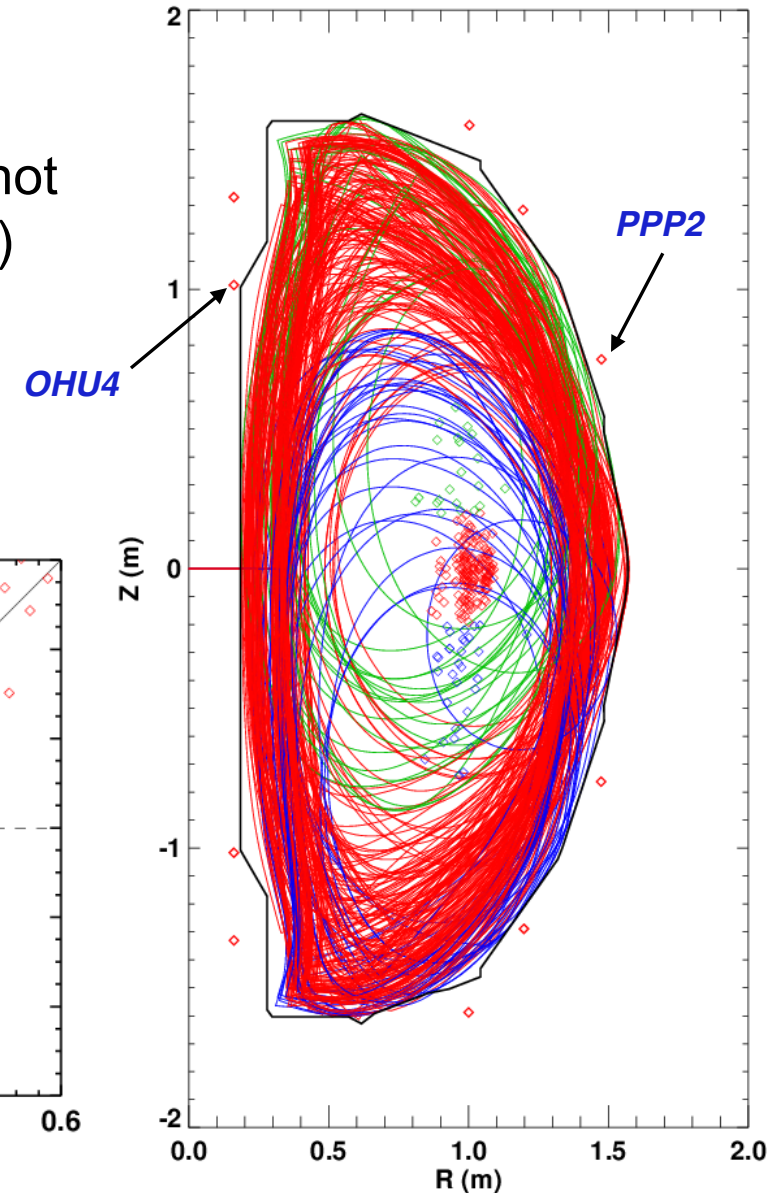
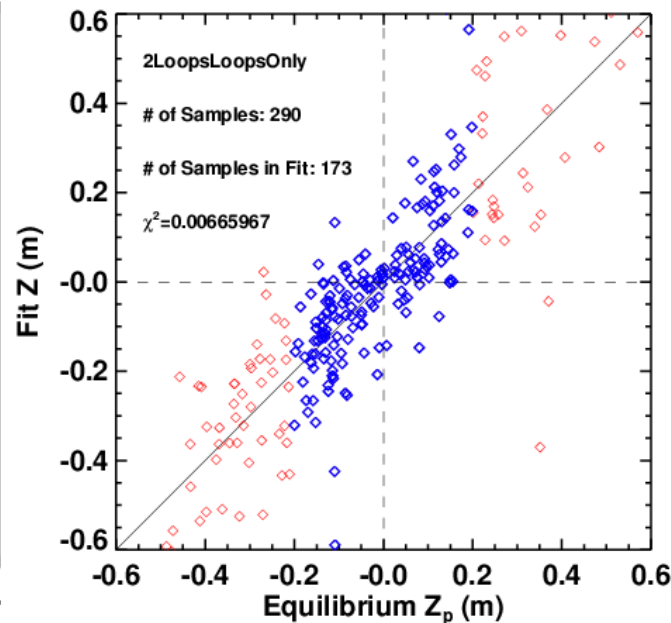
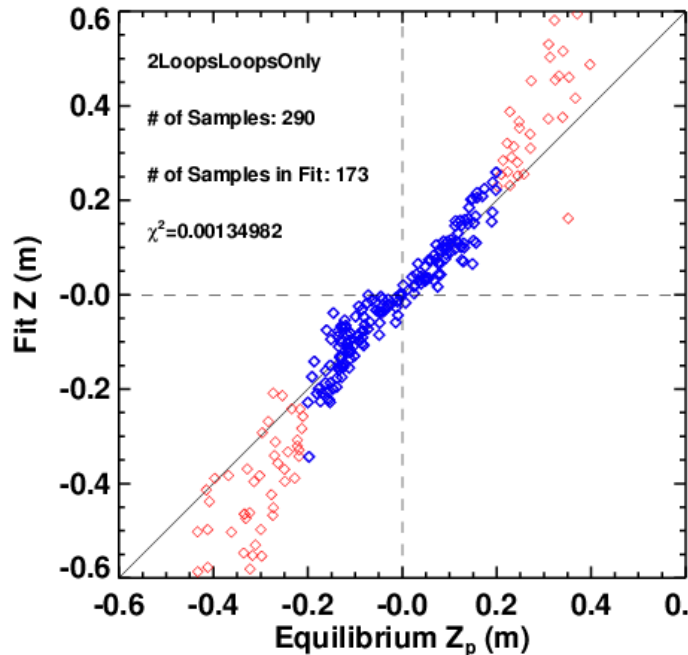


# Studies Show That Loops on the Center Column are Most Linear...But Least Sensitive

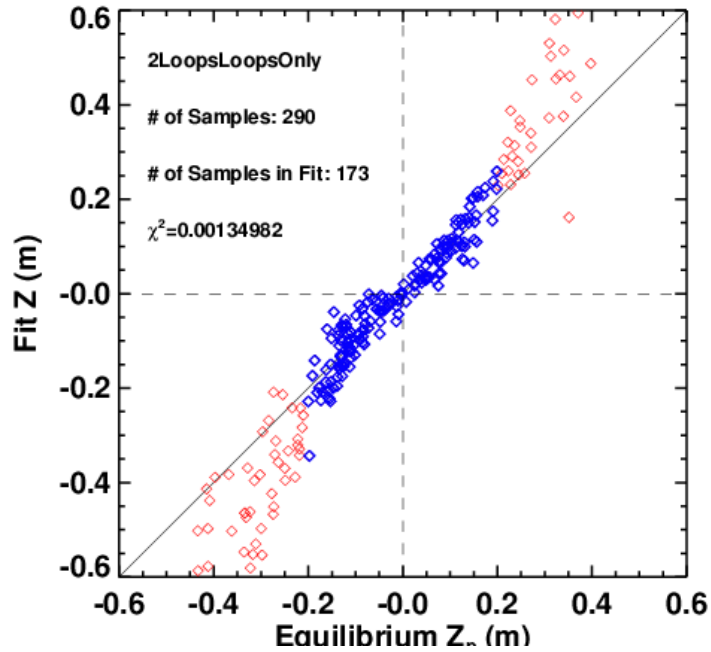
- CSC loops have less relative coupling to plates, are more linear.
  - But are much less sensitive (34 vs 2.53).
- Compromise between linearity and sensitive has not been discussed in the literature (to my knowledge)

$$\alpha_{OHU4} = -34.5$$
$$\chi^2 = 1.35 \times 10^{-3}$$

$$\alpha_{PPP2} = -2.53$$
$$\chi^2 = 6.6 \times 10^{-3}$$



# Adding More Loops With Unconstrained Fitting Allows Further Reduction of $\chi^2$ , Keeps Weight on CSC Loops

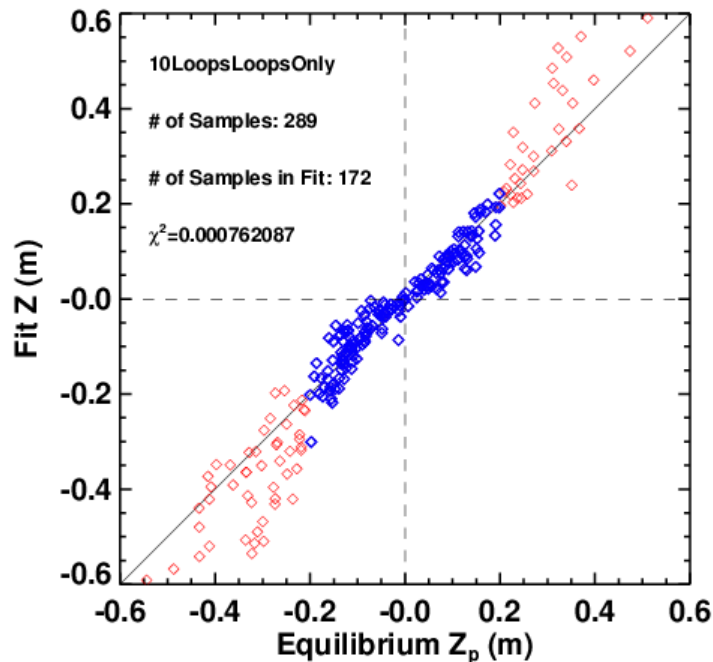


$$\alpha_{OHU4} = -34.5$$

$$\chi^2 = 1.35 \times 10^{-3}$$

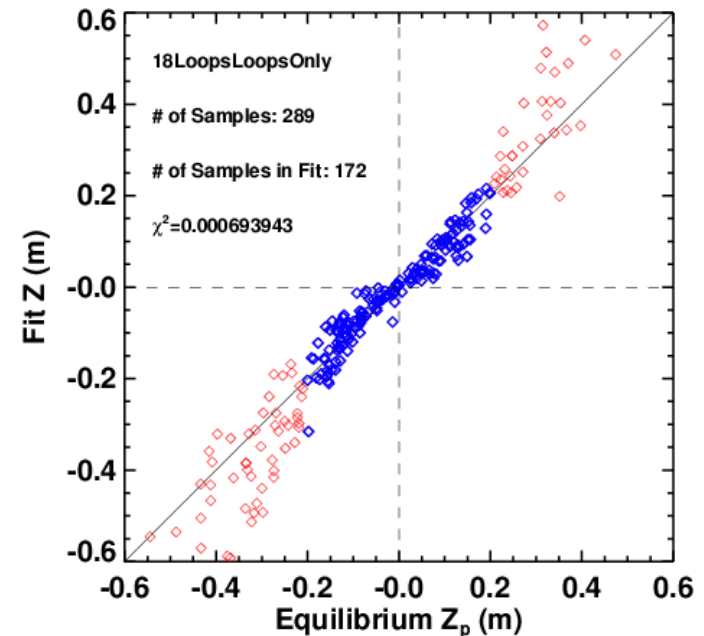
$$\alpha_{OHU4} = -29.48$$

$$\chi^2 = 6.9 \times 10^{-4}$$



$$\alpha_{OHU4} = -33.3$$

$$\chi^2 = 7.6 \times 10^{-4}$$



# Constrained Optimization Can Balance Sensitivity Against Linearity

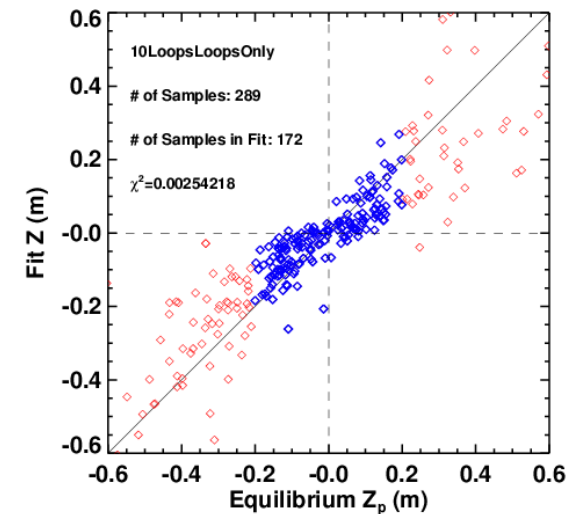
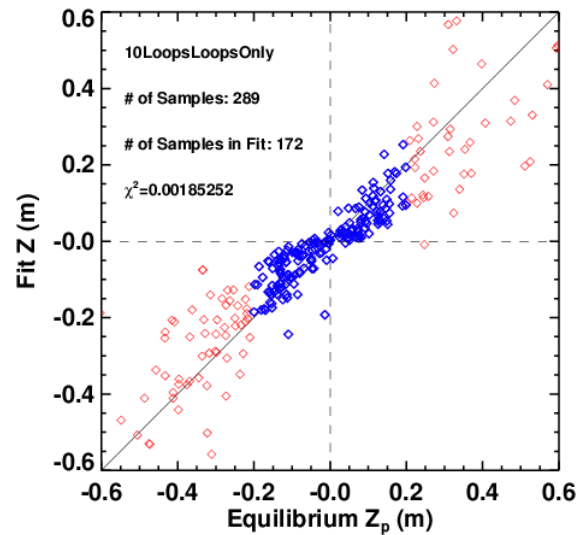
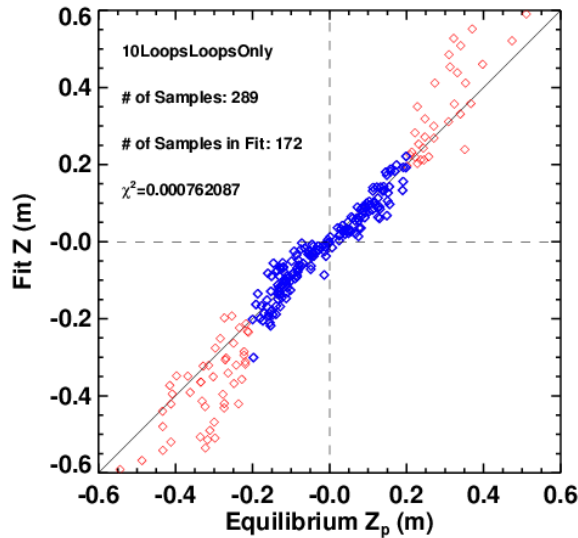
Scan of the maximum allowable weight on a single loop  
(40, 5, 2.5)

$$\begin{aligned} \alpha_{PPP2} &= 0.122 \\ \alpha_{SPP4} &= 0.169 \\ \alpha_{OHU4} &= -31.4 \\ \alpha_{OBD3} &= -0.52 \\ \alpha_{PF1A2} &= -0.29 \\ \chi^2 &= 7.6 \times 10^{-4} \end{aligned}$$

$$\begin{aligned} \alpha_{PPP2} &= -0.743 \\ \alpha_{SPP4} &= -0.107 \\ \alpha_{OHU4} &= -5.0 \\ \alpha_{OBD3} &= -0.694 \\ \alpha_{PF1A2} &= -5.0 \\ \chi^2 &= 1.85 \times 10^{-3} \end{aligned}$$

$$\begin{aligned} \alpha_{PPP2} &= -0.845 \\ \alpha_{SPP4} &= -0.408 \\ \alpha_{OHU4} &= -2.5 \\ \alpha_{OBD3} &= -0.436 \\ \alpha_{PF1A2} &= -2.5 \\ \chi^2 &= 2.5 \times 10^{-3} \end{aligned}$$

About 2.5 x better than present system



Study neglects any benefits that might come from elimination n=1 pickup.

# Strategy For Determining Loop Weighing

- There is a balance to be struck:
  - Linearity: Put all weight on inner flux loops
  - Noise immunity: Distribute weight across loops
- $n=1$  pickup (tearing and kink modes) will be stronger in some loop pairs than others.
  - Won't really know this until we see the data.
- Will pick final weight coefficients based on actual difference voltage signals.
  - Use actual voltage differences (including any noise).
  - First use coefficients from previous analysis, compare reconstructed and estimated  $d(I_p Z_p)/dt$
  - Maybe compute parameters that best map weighted sums to reconstructed  $d(I_p Z_p)/dt$ .
  - Will require a week or so of operation with all loop voltage differences functioning and data being collected.

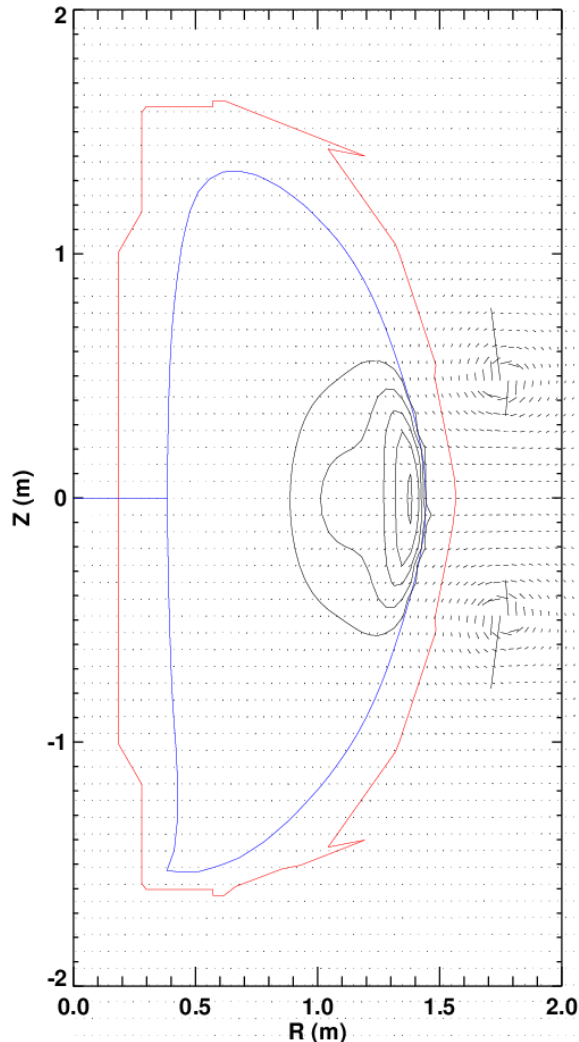
## Note on Gain Equivalences

- Present system uses a gain of 80.
  - i.e.:  $V_{VDE} = 80V_{PPP2}$
- New system will use a formulation:  $V_{VDE} = D \sum \alpha_i V_i$
- For the PPP2 loops,  $\alpha=3$ .  $V_{VDE} = D3V_{PPP2}$
- So, equivalent derivative gain is now  $80/3=27$ .

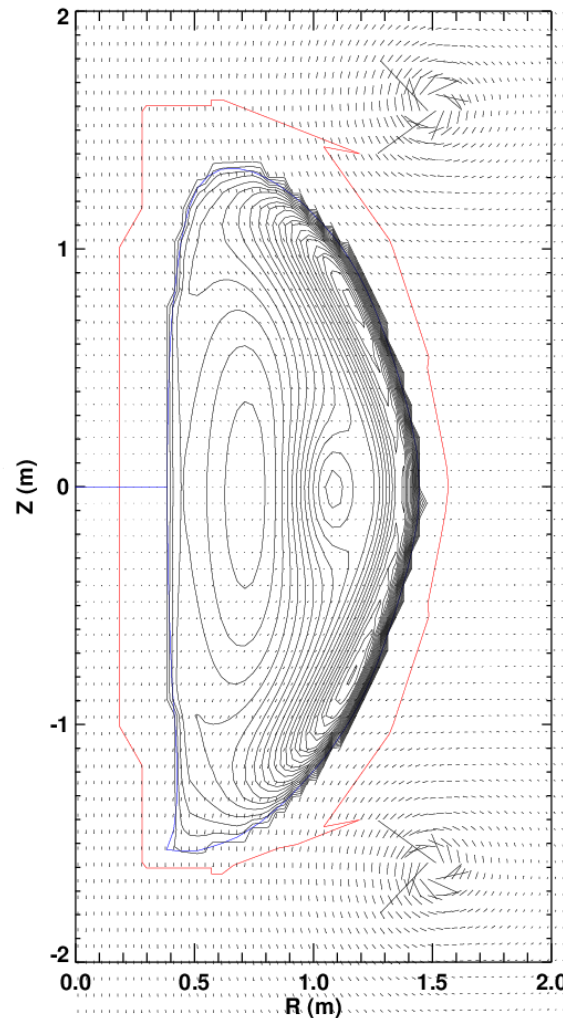
# Vertical Position Control May Be Possible With the RWM Coils

Calculate force assuming 1 amp of power supply currents  $F_Z = \sum J_\phi B_R$

**RWM Coils:  $F_Z=78$**



**PF-3 Coil:  $F_Z=1500$**



**RWM Coils make far less force for the same power supply current.**

*(ratio is not as bad for lower-elongation plasmas)*

**However....**

**1) SPA are very fast (to 3 kA in 1-2 msec)**

**2) RWM coil field may not couple as strongly to the passive plates.**

**Use this as a last resort if we have insufficient vertical control margin after other things are tried.**

# Formulation of the PCS Code

- Estimate of  $d(Z_P I_P)/dt$  :  $\frac{d(I_P Z_P)}{dt} = \sum_{j=0}^8 \alpha_j V_{UL,j}$
- Form the SPA current request:

$$I_{SPA_i}^{req}(t) = I_{SPA_i}^{OHxTF}(t) + I_{SPA_i, B_R}^{RWM}(t) + I_{SPA_i, B_P}^{RWM}(t) + I_{SPA_i}^{pre}(t) + I_{SPA_i}^{VDE}(t)$$

$$I^{VDE}(t) = -D_{RWM}^{VDE} \times LPF\left(\frac{d(ZI_P)}{dt} \tau_{VDE}\right)$$

$$I_{SPA_i}^{VDE}(t) = I^{VDE}(t)$$

- How big should D be?
  - Take a 1 MA plasma, moving 10 cm in 10 msec:
    - $d(Z_P I_P)/dt = 1 \cdot 10 / 0.01 = 1000 \text{ MAcm/sec}$
  - We want 3000 A of current for this feedback.
    - $D = 3000 / 1000 = 3 \text{ MAcm/Asec}$

# Hardware and Software Status

- dZ/dt Observer
  - Complete specification has been written, PCS programmers are looking it over.
  - Electronics for voltage differences are finished.
    - Put them in the NTC next week.
  - Changes to MDS+ tree for additional channels have been made.
- RWM coils for  $Z_{\text{axis}}$  control.
  - Specification has been written.
    - Relies on the improved dZ/dt observer for the measurement.
  - Code has been implemented as part of the 6 subunit proportional control algorithm.
    - Has not been tested.



# Run Plan (I)

- Debugging: Compare PCS calculations to identical off-line versions.
- XMP (?): Test that system is correctly coupled to the PF-3 coils.
  - Switch to new controller formulation (the  $\alpha$ s), use the same single loop pair and value of gain (27) that reproduces the old system.
  - Show that vertical controller still works.
- Day 1: Optimize gains with PF-3 as actuator, new  $d(I_p Z_p)/dt$  observer.
  - Reload vertically unstable target,  $A \sim 1.75$ ,  $\kappa = 2.9$ . Show a VDE. (3 shots)
    - Potential reload is 142301.
    - Use divertor gas injection to drive  $I_i$  up?
  - Transition to new  $d(I_p Z_p)/dt$  observer, same overall gain. Repeat. (4 shots)
    - If no VDE, then increase  $\kappa$  until a VDE occurs.
  - Increase vertical control gain until VDE is stabilized. (5 shots)
    - (or oscillation develops).
  - Contingency, do one of: (5 shots)
    - Test a second combination of loops.
      - Repeat gain scan
    - Use same combination of loops, change the shot and demonstrate benefits.
      - For instance, lower-delta target with reduced beam heating.

## Run Plan (Day 2, RWM control, if necessary)

- Turn off PF-3 vertical control and see plasma drift. (3 shots)
  - Use fiducial like target
  - Shot to reload: 141640
- Add n=0 control with RWM coils. (7 shots)
  - Scan gain using value 0.5, 1.0, 1.5, 2.0, 2.5
  - Stop scan when coil currents become too large, or VDE is stabilized.
- If VDE is stabilized, then increase inner gap until instability is achieved. (4 shots)
- Test combined PF-3 and RWM coil control to determine the new limit on aspect ratio and  $I_i$ . (4 shots)