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# Abstract

The resistive wall mode (RWM) can be stabilized by maintaining the plasma toroidal rotation frequency ( $\omega_\phi$ ) above a critical rotation frequency ( $\Omega_{\text{crit}}$ ). Recent experiments on NSTX seek to determine  $\Omega_{\text{crit}}$  and rotation profile effects through actively braking plasma rotation by the application of external magnetic fields. Results from these experiments indicate that maintaining  $\omega_\phi$  at the  $q = 2$  surface above  $\omega_A/4q^2$  is a necessary condition for RWM stability where  $\omega_A$  is the local Alfvén frequency. This result is in agreement with a theoretical model derived from a drift-kinetic energy principle. Similarity experiments with DIII-D are being performed to examine the aspect ratio dependence of the  $\Omega_{\text{crit}}$  scaling. When  $\omega_\phi$  at the  $q = 2$  surface drops below  $\Omega_{\text{crit}}$ , the growth of internal kink/ballooning modes can prevent the RWM from terminating the discharge. A small beta collapse which drops  $\Omega_{\text{crit}}$ , accompanies this mode growth allowing a recovery of RWM rotational stabilization while maintaining  $\beta_N > \beta_N^{\text{no-wall}}$ .

\*Work supported by U.S. DOE contracts DE-FG02-99ER54524 and DE-AC02-76CH03073



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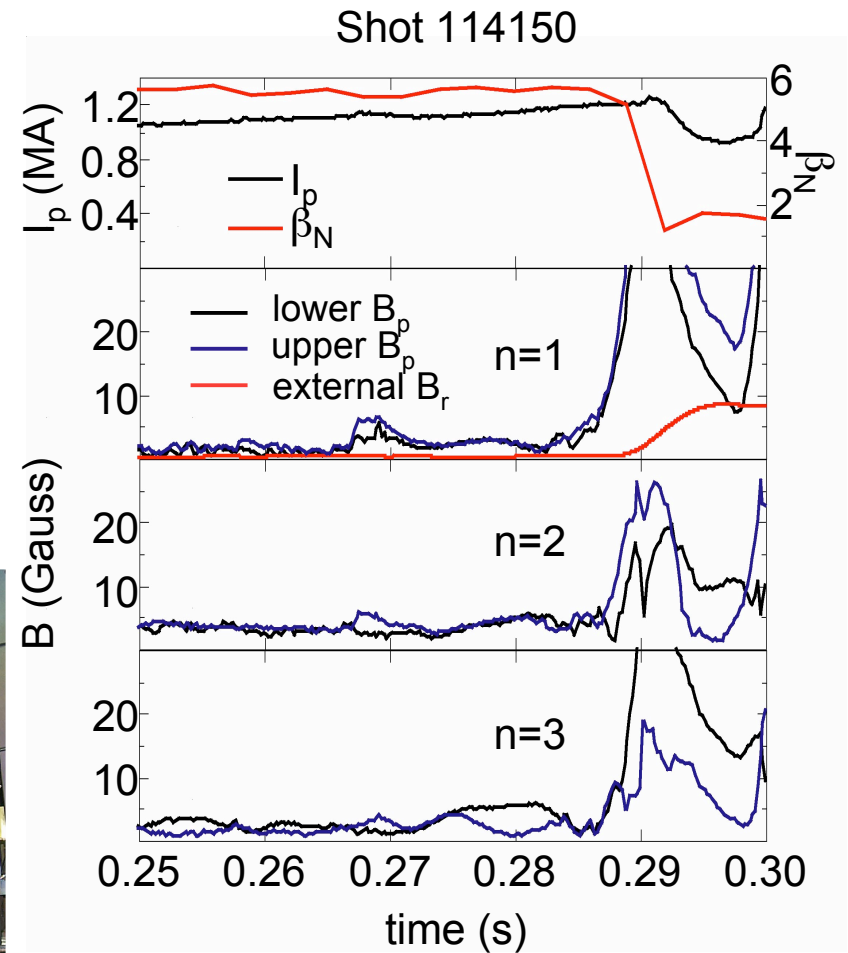
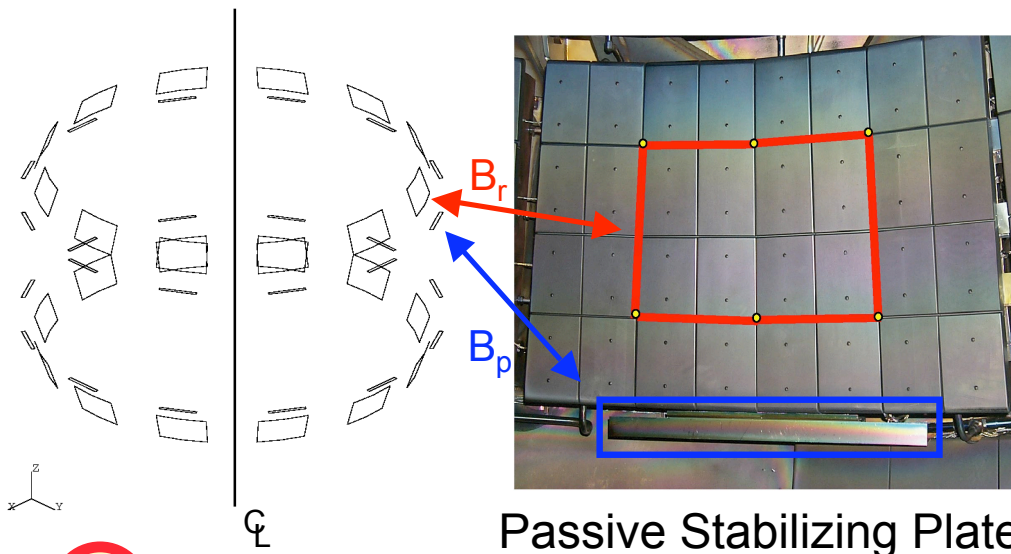
# RWM Can Limit Sustainable Pressure in Current and Future Fusion Devices

- Current fusion experiments which operate with  $\beta_N > \beta_N^{\text{no-wall}}$  experience RWMs
- RWM can be stabilized by plasma rotation
  - Feedback control has also been demonstrated
- Future devices will have low rotation so may be more susceptible to RWMs
  - Understanding of the critical rotation required for RWM stability is important to design these devices correctly
- RWM can be stabilized by combination of toroidal rotation and dissipation
  - several dissipation mechanisms have been proposed
    - sound wave
    - ion Landau damping
    - Alfvén continuum
  - rotation can affect dissipation strength
  - critical rotation frequency ( $\Omega_{\text{crit}}$ ) is minimum rotation required for stability

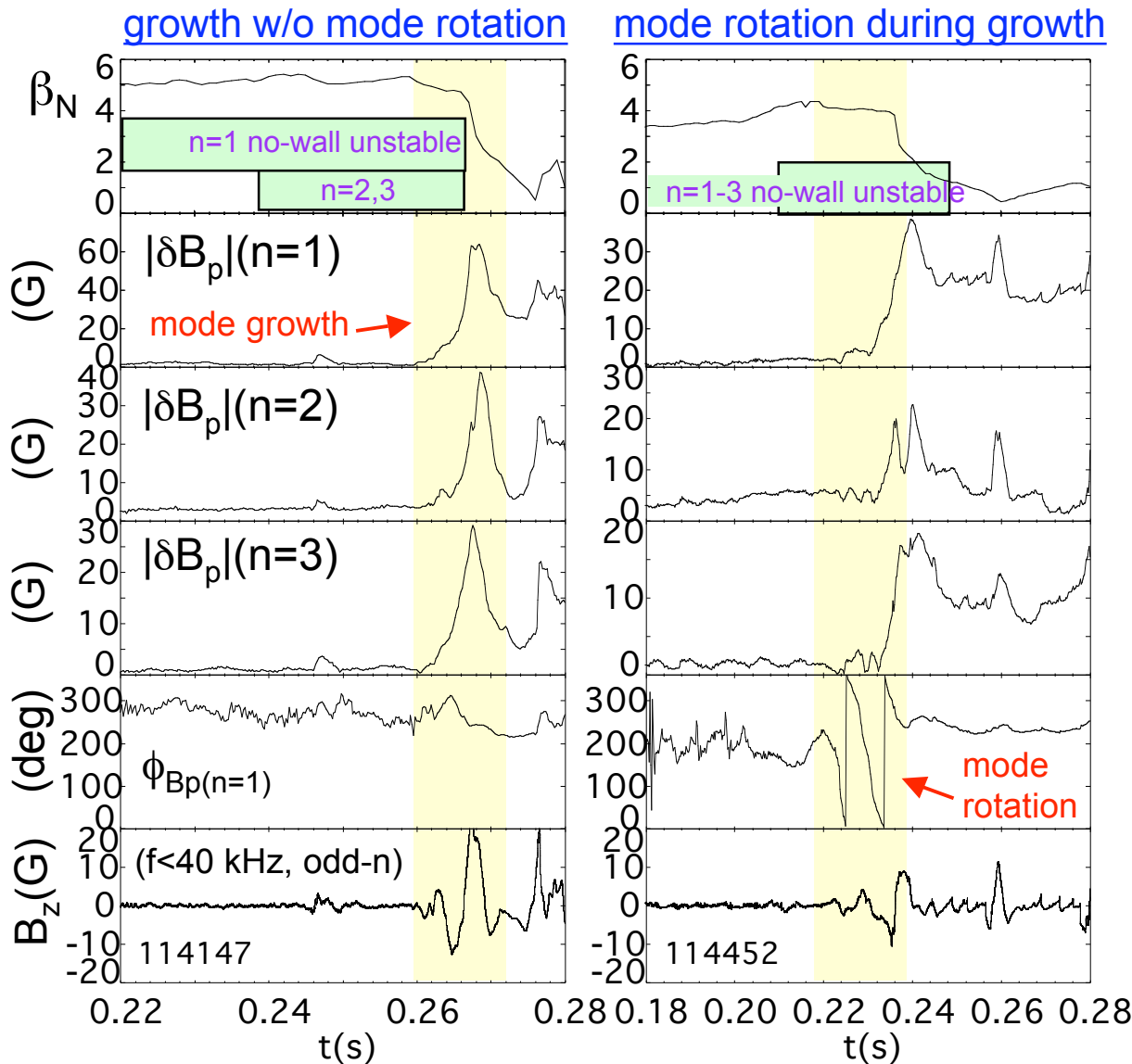


# Internal Sensor Array Used for RWM Detection

- Internal toroidal arrays of  $B_p$  and  $B_r$  sensors installed
  - 5 kHz digitization rate
  - instrumented to detect  $n = 1 - 3$
- Measured coil currents used for background subtraction
  - ~2 Gauss noise level achieved
  - allows real time mode detection
- SVD mode detection is robust



# Unstable RWM Dynamics Follow Theory



- Unstable  $n=1-3$  RWM observed\*
  - ideal no-wall unstable at high  $\beta_N$
  - $n > 1$  theoretically less stable at low  $A$
- F-A theory / experiment show
  - mode rotation can occur during growth
  - growth rate, rotation frequency  $\sim 1/\tau_{wall}$ 
    - $\ll \text{edge } \Omega_\phi > 1$  kHz
  - RWM phase velocity follows plasma flow
  - $n=1$  phase velocity not constant due to error field
- Low frequency tearing modes absent



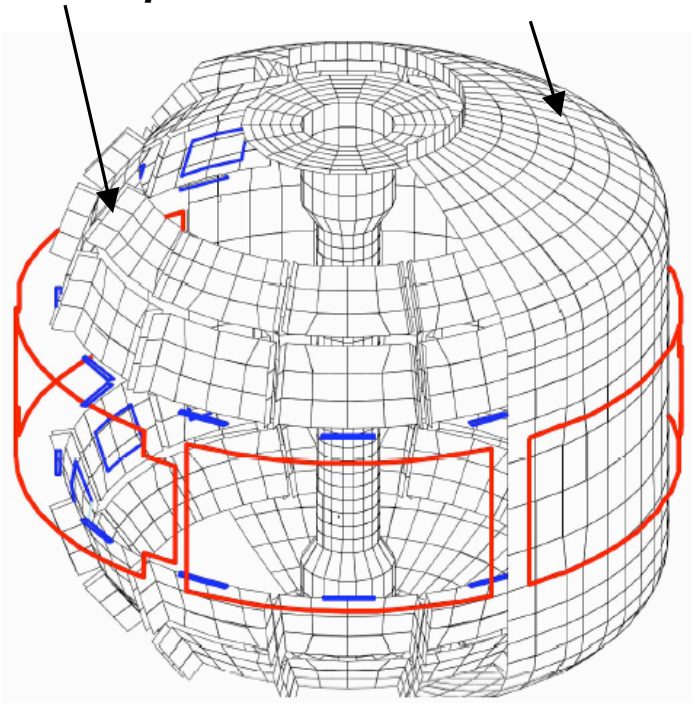
\*S.A. Sabbagh, et al., IAEA FEC 2004 paper EX/3-2; submitted to NF



# New Coils and Power Supplies Provide Greater Flexibility to Study $\Omega_{\text{crit}}$

*Copper passive  
conductor plates*

*SS Vacuum  
Vessel*

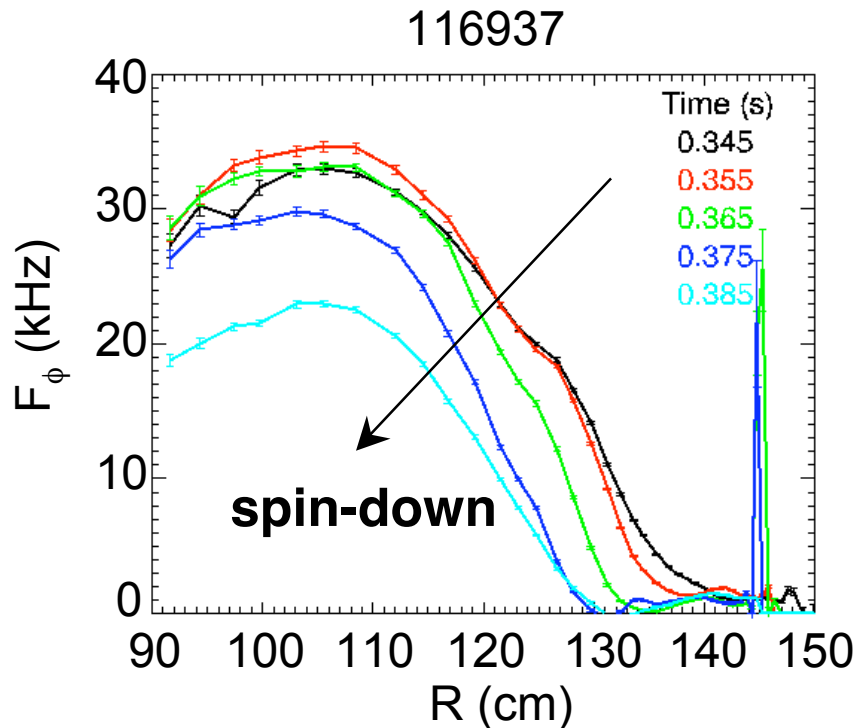


*VALEN Model of NSTX (J. Bialek)*

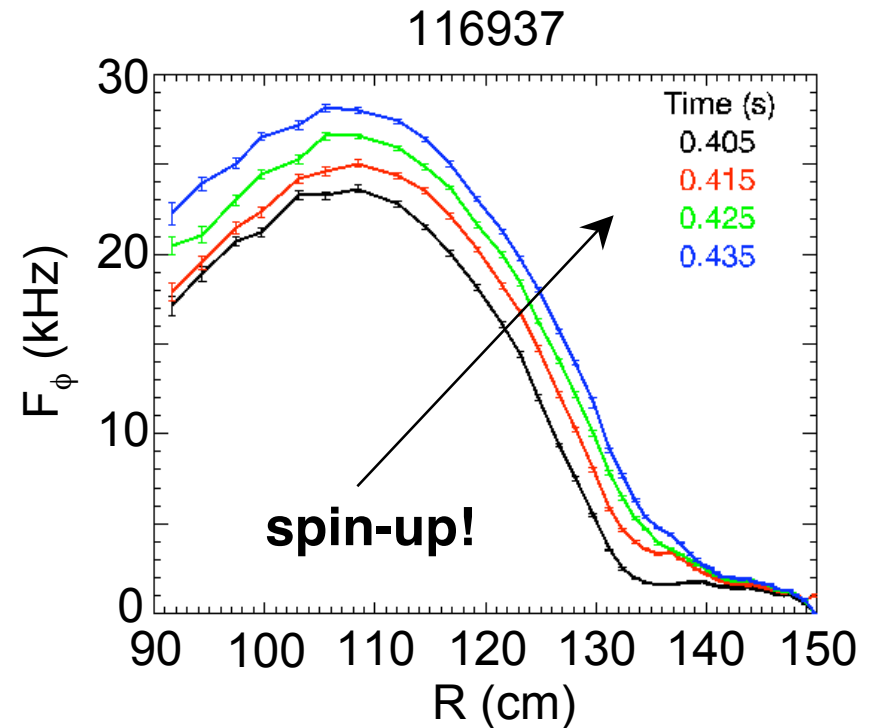
**6 ex-vessel midplane control coils**

- **RWM/EF coil and SPA capabilities:**
  - 3 opposing coil pairs in anti-series (n=1,3)
    - n=2 interconnection also possible
  - 3 independent SPA circuits - 3.3 kA, 7.5 kHz
  - Can produce 10-15 G n=1 resonant  $B_{\perp}$  at q=2
- **Uses for NSTX:**
  - investigate  $\Omega_{\text{crit}}$  profile by perturbing  $\omega_{\phi}$
  - investigate RFA
  - investigate error field correction
  - future active RWM stabilization

# External Field Application Allows Rotation Control



n=3 DC (1.1kA) external  
field applied

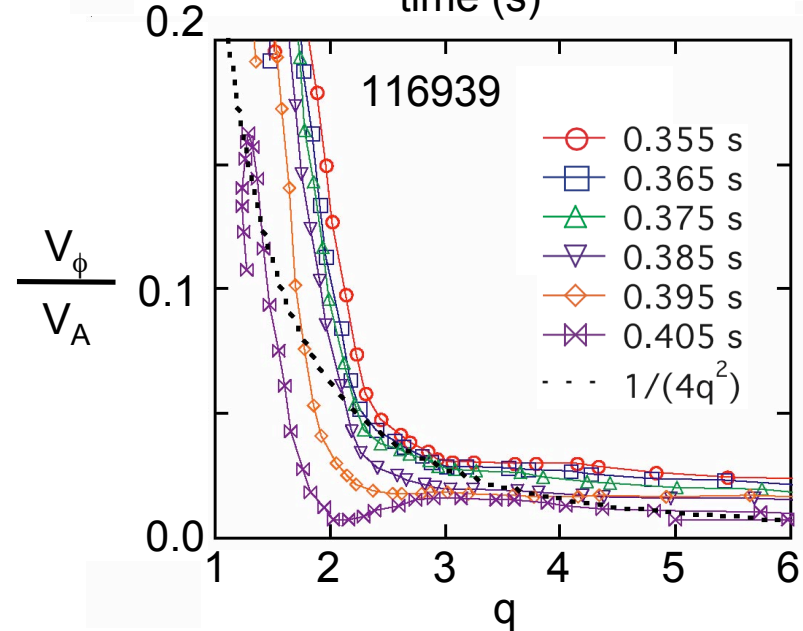
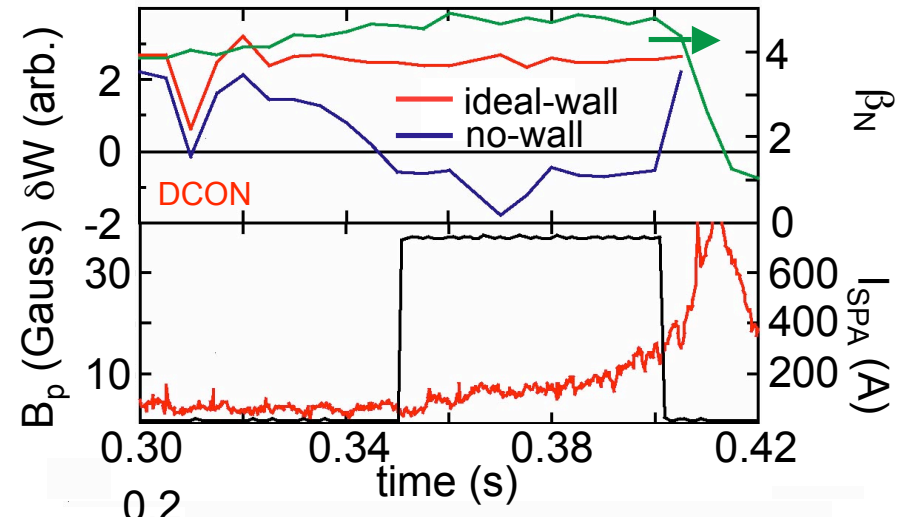


external field shut  
down

- Control over rotation allows more careful examination of the rotation profile effects on RWM stability

# Resonant Field Amplification Observed With Application of External $n = 1$

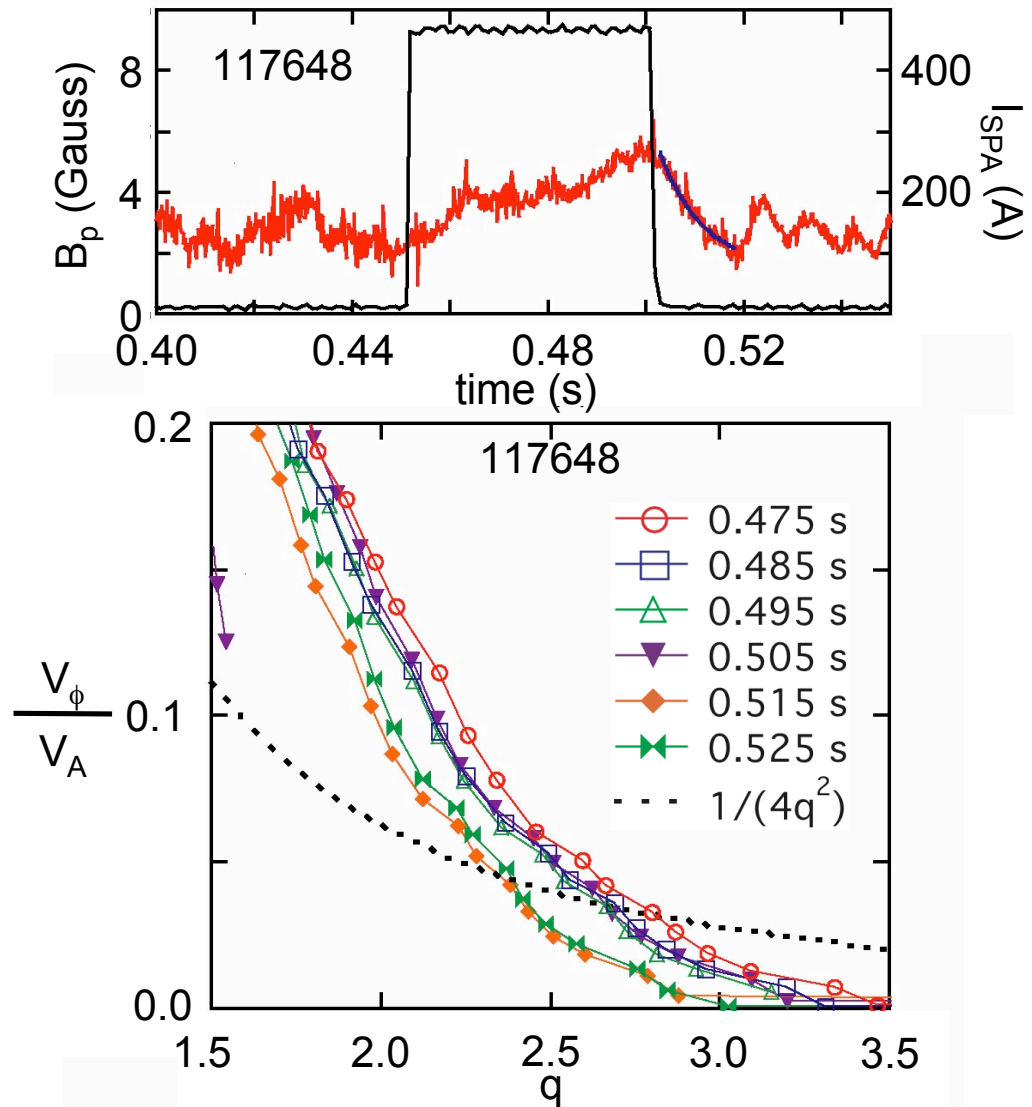
- Resonant field amplification (RFA) when  $\beta_N > \beta_{N \text{ no-wall}}$ 
  - amplification of external perturbations by *stable* RWM
  - predicted by theory\*
  - Ideal MHD stability  $\delta W$  from DCON (A.H. Glasser)
- RFA observed until rotation braking destabilizes mode
  - unstable growth after significant rotation damping
  - edge rotation remains stabilizing
  - low rotation at multiple low-order rational  $q$  surfaces



\*Boozer, A.H., *Phys. Rev. Lett.*, **86** 5059 (2001)

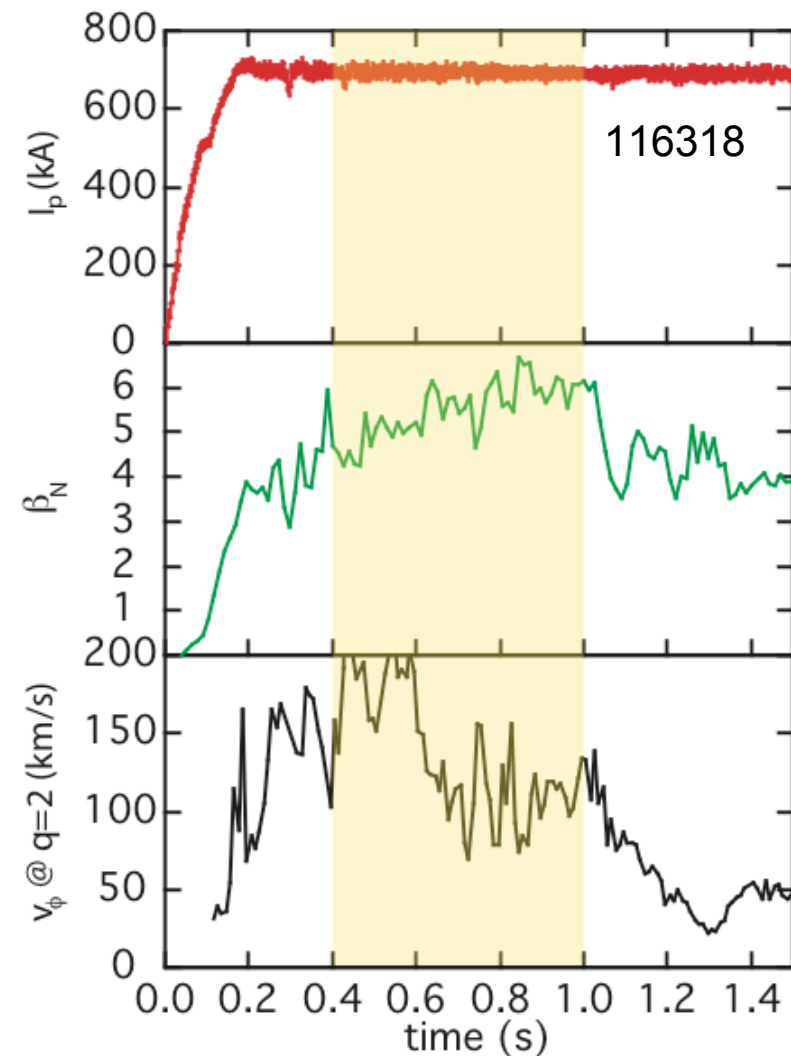
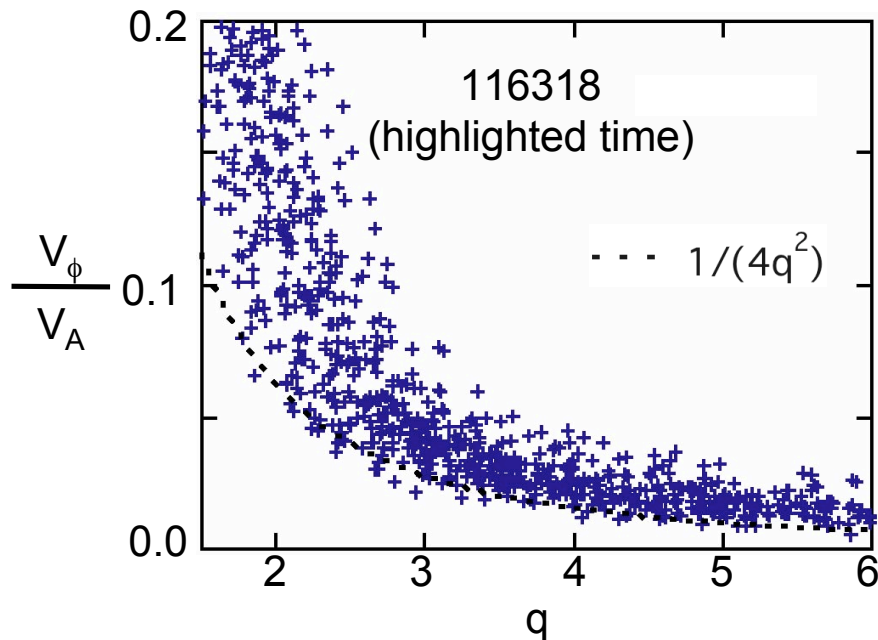
# RFA Decays When External Field Turned Off Before RWM Destabilization

- rotation remains high at some low-order rational  $q$  surfaces
  - near zero rotation outside  $q = 3$  ( $\psi_N \sim 0.65$ )
- field amplitude below threshold
  - $\sim 20$  Gauss causes unstable mode growth and disruption
- 9.1 ms decay time measured



# High Toroidal Rotation Across Entire Profile Allows Sustained High $\beta_N$

- Entire rotation profile stays high during high- $\beta$  period
  - Alfvén speed normalization &  $q$  dependence from drift-kinetic theory
- Trend observed in numerous discharges



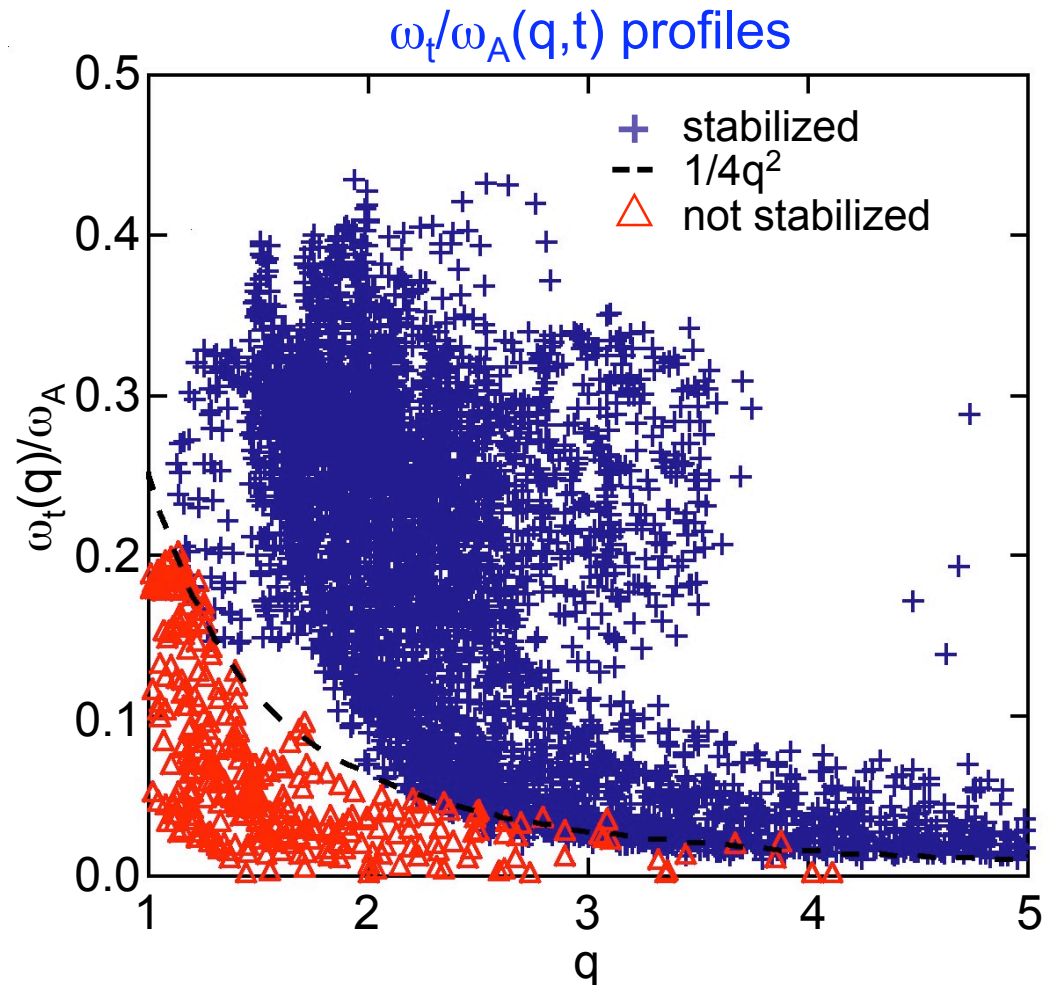
# 2004 Data Supports $1/q^2$ Scaling of Critical Rotation Frequency

- Scaling from two stability classes:
  - stabilized  $\Rightarrow$  no RWM for  $t \gg \tau_{\text{wall}}$  when  $\beta_N > \beta_{N \text{ no-wall}}$
  - not stabilized  $\Rightarrow$  collapse after a few  $\tau_{\text{wall}}$  when  $\beta_N > \beta_{N \text{ no-wall}}$

- Bondeson-Chu drift-kinetic model\* agrees with observed scaling

- trapped particle effects weaken stabilizing ion Landau damping
- toroidal inertia enhancement becomes more important
- Alfven continuum damping gives:

$$\Omega_{\text{crit}} \equiv \frac{\omega_t}{\omega_A} = \frac{1}{4q^2}$$

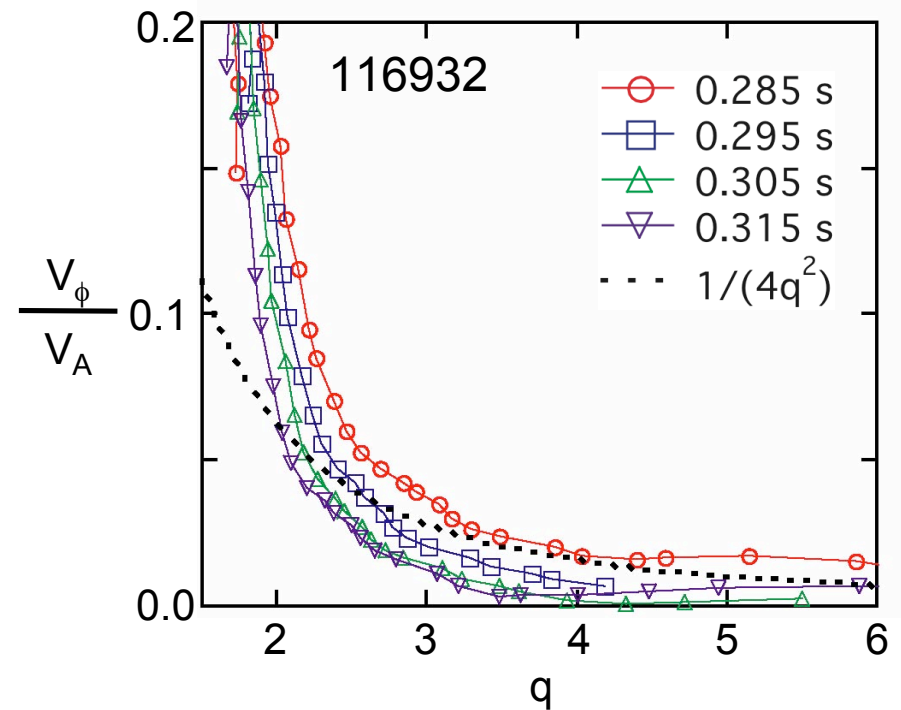
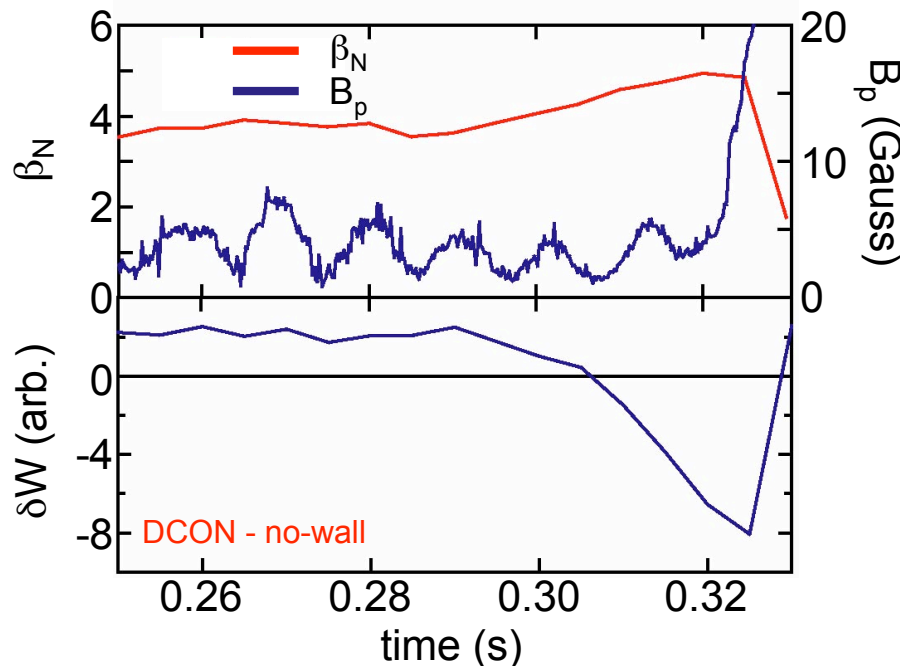


\*Bondeson, A., Chu, M.S., *Phys. Plasmas* **3** 3013 (1996)  
 & Sontag, A.C., et al., *Phys. Plasmas* **12** 056112 (2005)



# High Core Rotation Insufficient to Stabilize RWM

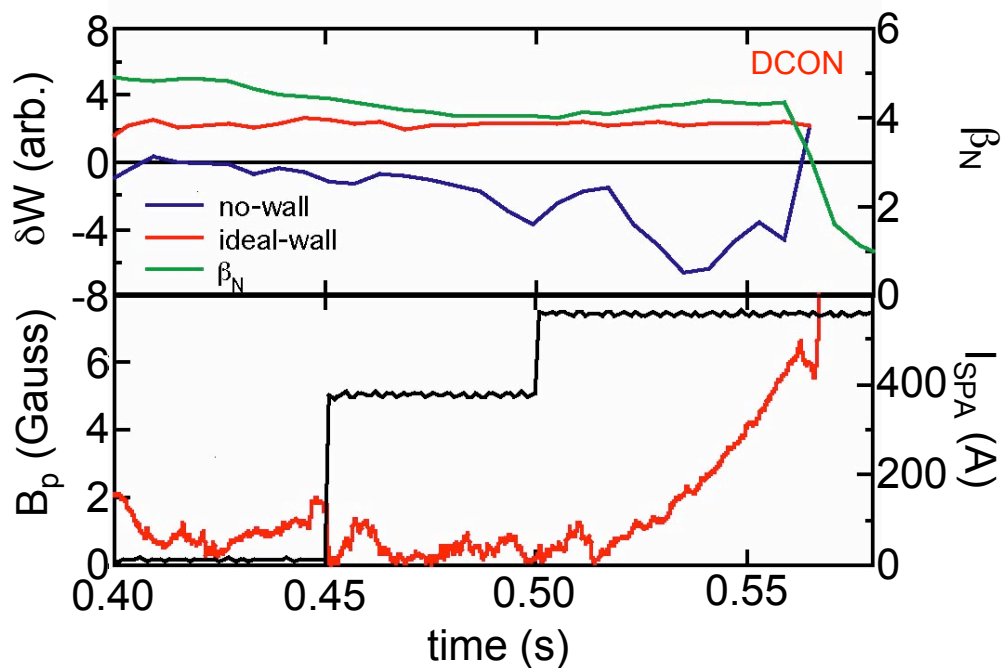
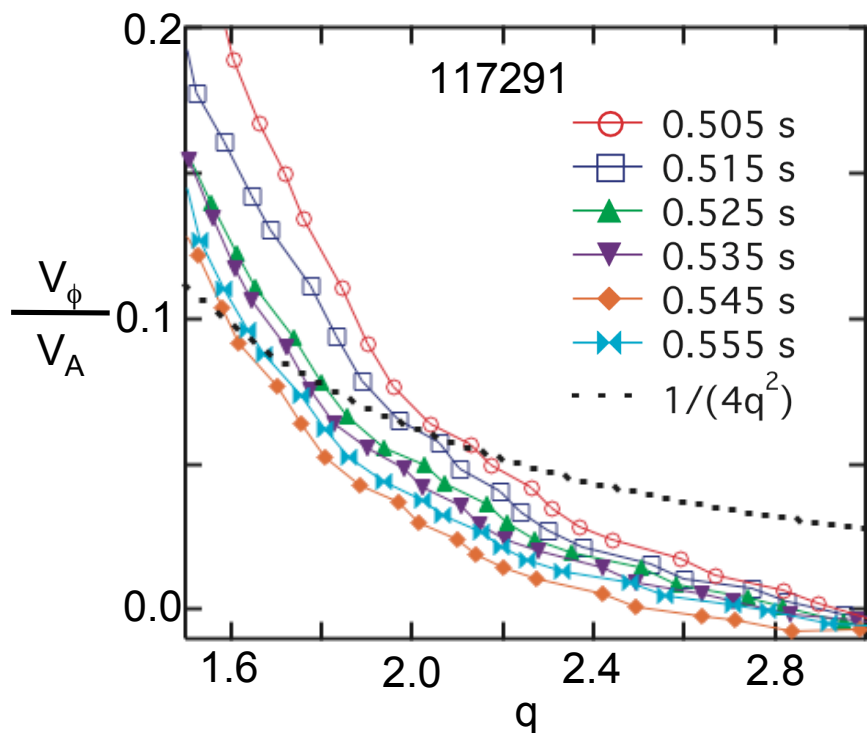
- Low edge rotation when no-wall limit exceeded
- RWM growth causes further rotation damping
  - ~15 Gauss threshold after which collapse is inevitable
- Important question: What is the critical rotation profile?





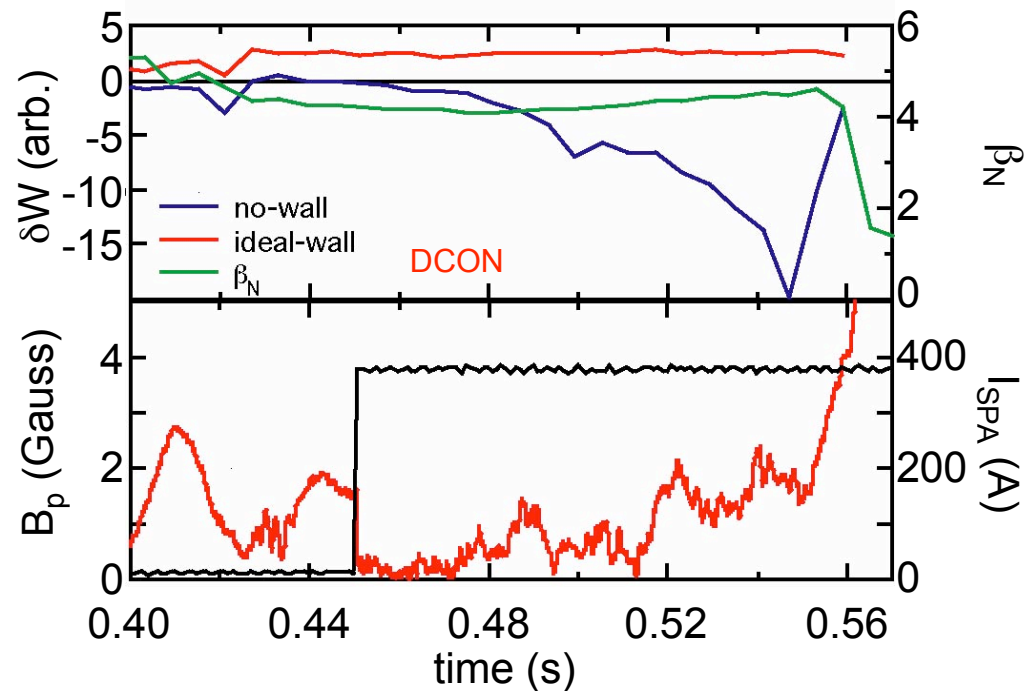
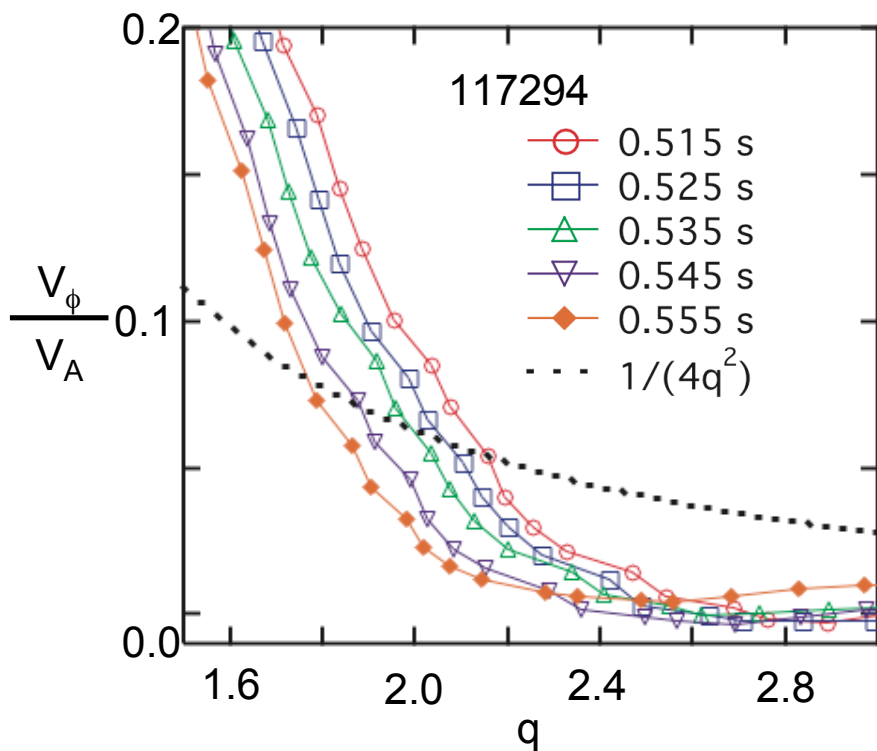
# Rotation on Higher Order Rational Surfaces Not Required for RWM Stabilization

- Plasma remains RWM stable with near zero rotation outside  $q = 3$ 
  - Stable with near zero rotation outside  $\psi_N = 0.62$
  - growth coincides with low rotation inside of  $q = 2$

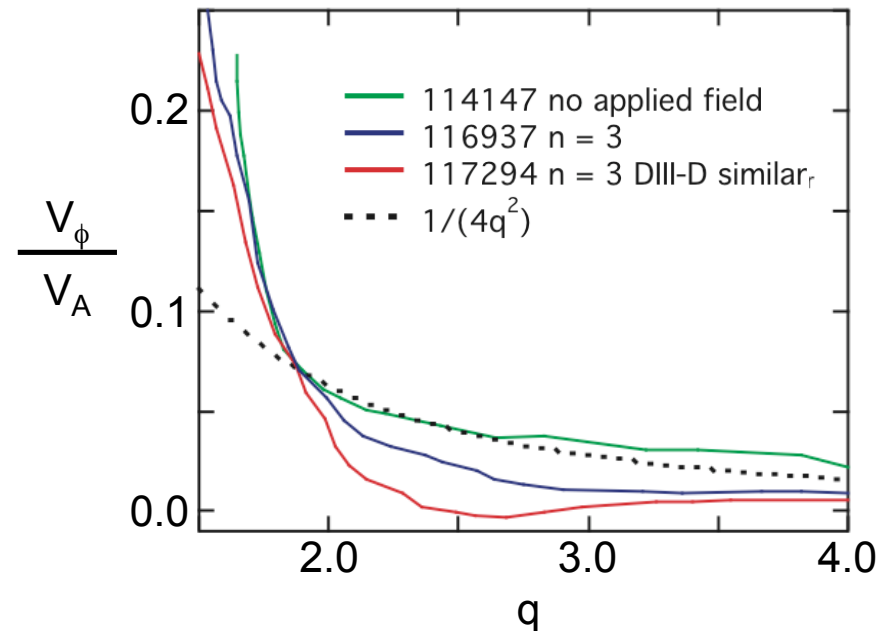
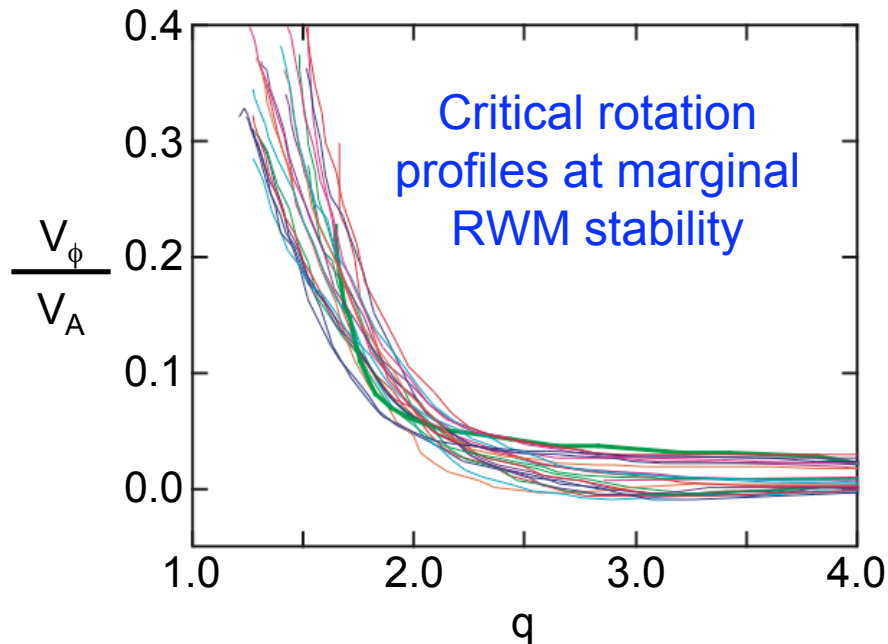


# Similar Discharges Survive Longer With Lower Rotation @ $q = 2$ Surface

- No unstable growth until  $\sim 20$  ms after rotation drops at  $q = 2$
- Higher  $\delta W$  & lower applied field than 117291
  - factors beyond rotation at  $q = 2$  need consideration



# Significant Variation Observed in Marginal Rotation Profiles



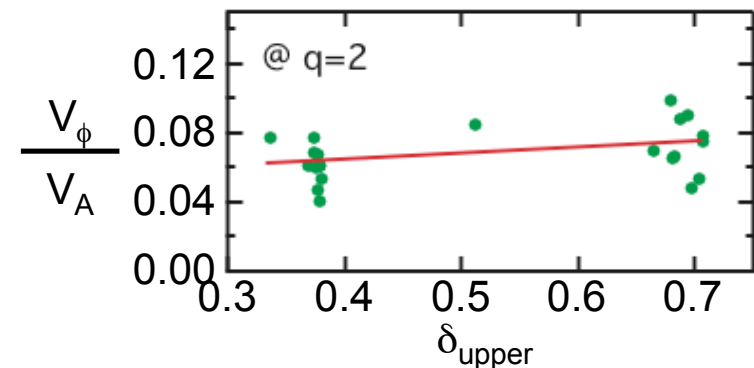
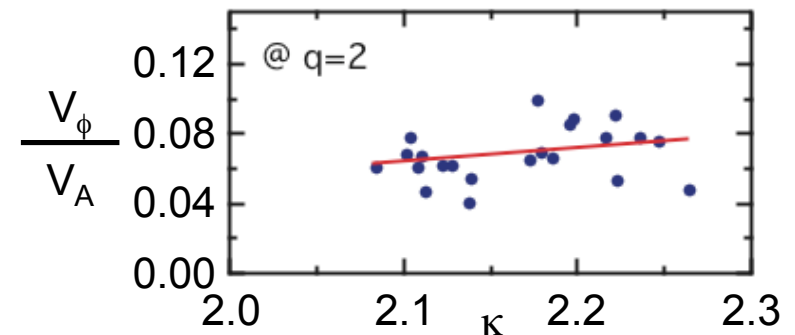
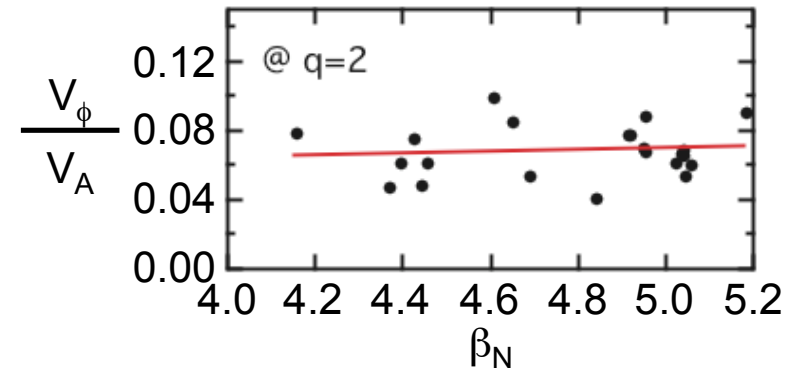
- Each case is last profile before unstable RWM growth observed
- Shot with no applied field has entire profile near or above  $1/4q^2$
- n=3 applied field used to alter rotation profile
  - rotation in edge of plasma suppressed
- $q = 2$  region appears significant but not definitive

# Marginal Stability Shows Weak Dependence on Plasma Parameters

- Rotation shows no scaling with  $\beta$ 
  - no-wall limit varies significantly shot-to-shot
  - need to check against  $C_\beta$

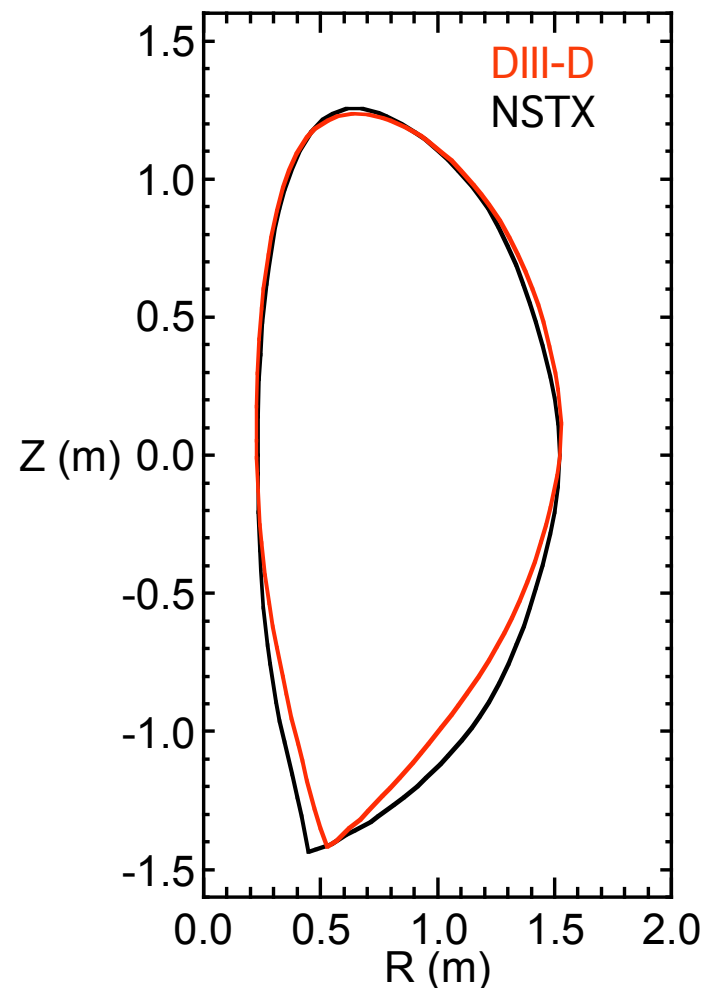
$$C_\beta = \frac{\beta - \beta_{no\ wall}}{\beta_{ideal\ wall} - \beta_{no\ wall}}$$

- Weak variation with plasma shape
  - need to normalize out influences of shape on no-wall limit



# DIII-D Shape Reproduced to Examine A Scaling of $\Omega_{\text{crit}}$

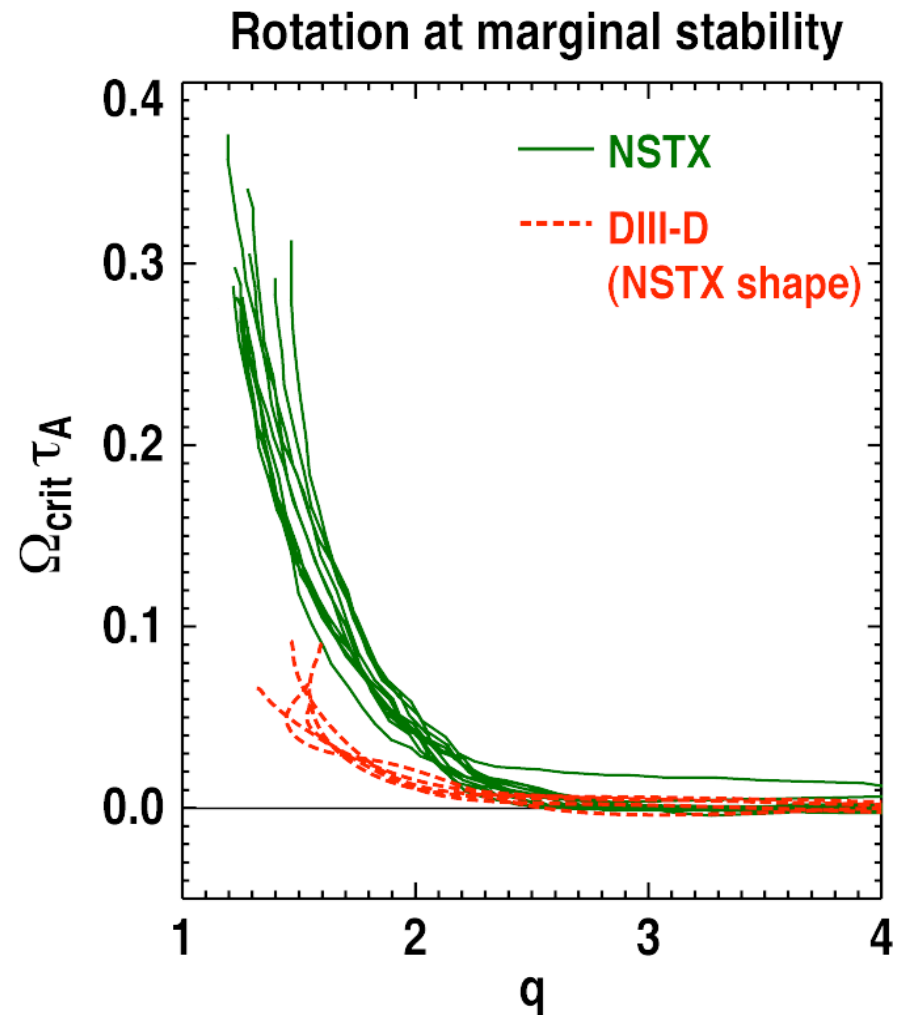
- Including neoclassical viscous dissipation in RWM dispersion relation\* leads to inverse aspect ratio dependence of  $\Omega_{\text{crit}}$
- Previous comparisons used different techniques to determine  $\Omega_{\text{crit}}$ 
  - Active braking on NSTX allows more straightforward comparison
- DIII-D shape matched in NSTX with  $\beta_N > \beta_N^{\text{no-wall}}$ 
  - q &  $\beta$  scans performed



\*Shaing, K.C., Phys. Plasma **11** 5525 (2004)

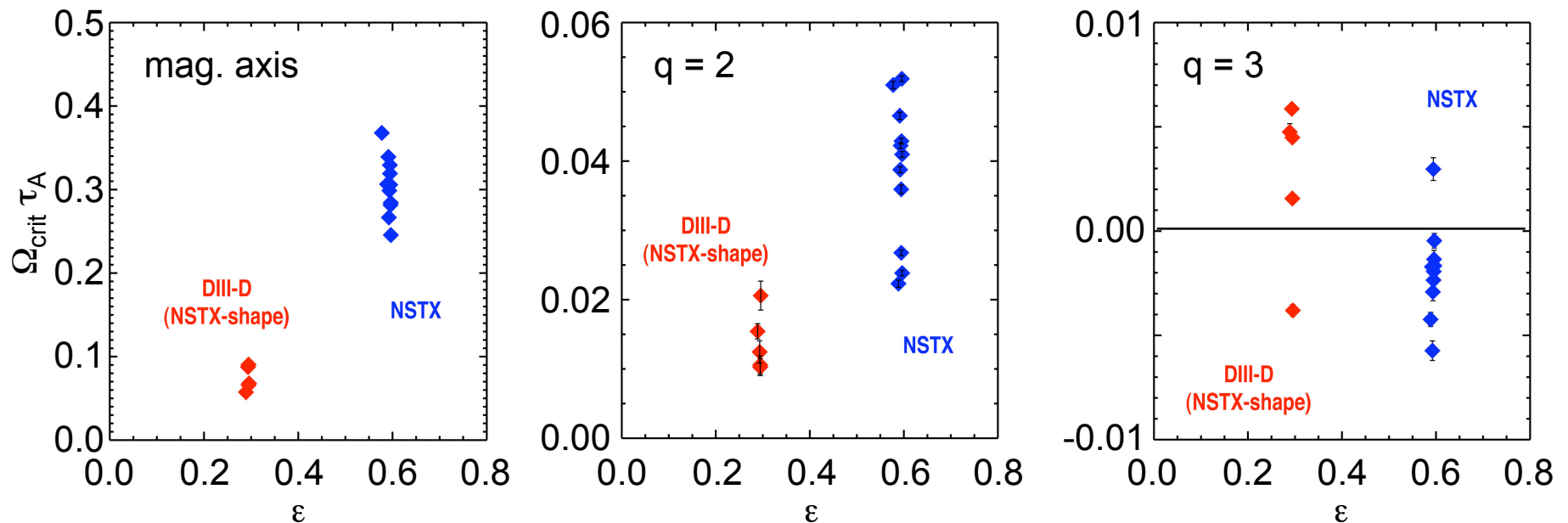
# More Rotation Required for RWM Stability in NSTX

- Comparison of marginal profiles in similar shaped discharges
- Low rotation edge doesn't affect stability
- NSTX has higher rotation throughout region which determines stability



# Similarity Experiment is Examining RWM Stability Variation with A

- Profile effects being studied
  - NSTX has higher rotation at  $q = 2$  and in the core
  - very low rotation at  $q = 3 \Rightarrow \Omega_{\text{crit}}$  cannot depend on  $q = 3$
- Large data spread (especially NSTX)
  - subjectivity in determining start of unstable growth
  - 10 ms averaging time for rotation measurement





# Sound Speed Normalization Removes Aspect Ratio Dependence

- Coupling to sound waves is one possible dissipation mechanism

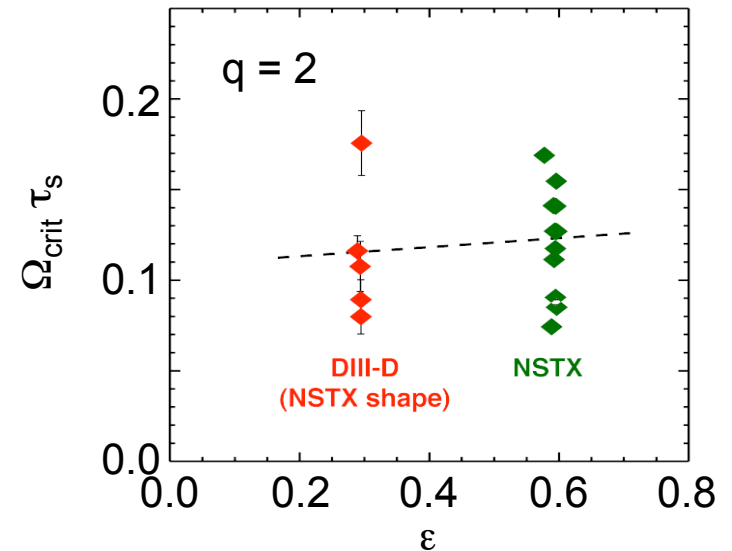
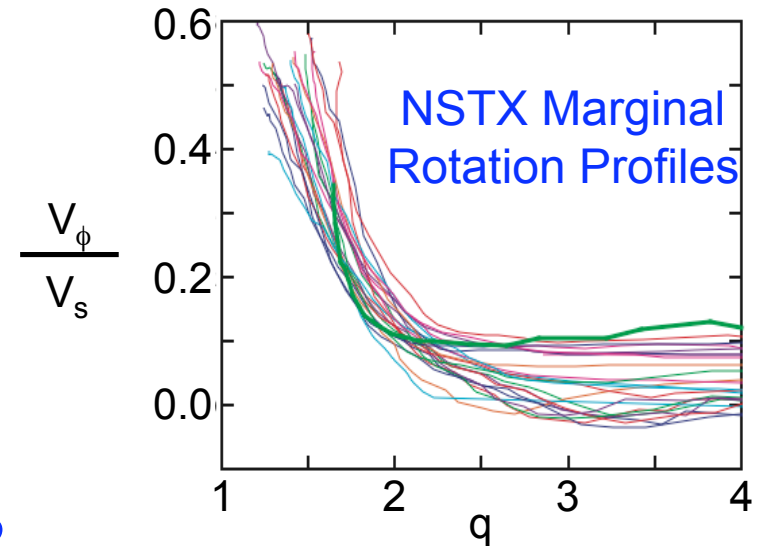
- depends on sound speed

$$V_s = \sqrt{\frac{kT_e + \gamma kT_i}{m_i}}$$

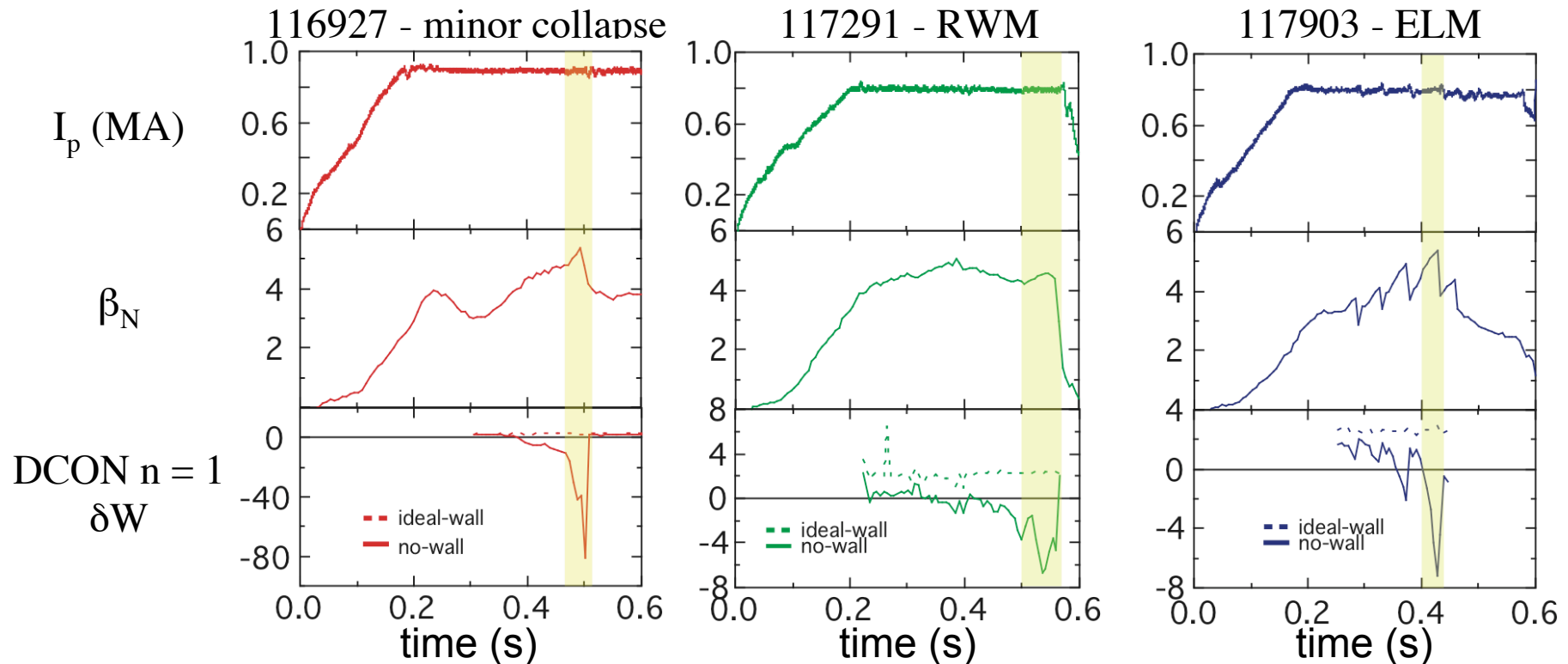
- Critical rotation variation at  $q = 2$  reduced with  $V_s$  normalization

- consistent with significant dissipation due to sound waves

*Numerical calculations of relative magnitudes of sound and Alfvén wave dissipation needed*



# Minor $\beta$ Collapse Has Effects on Plasma Similar to Both RWM and ELM

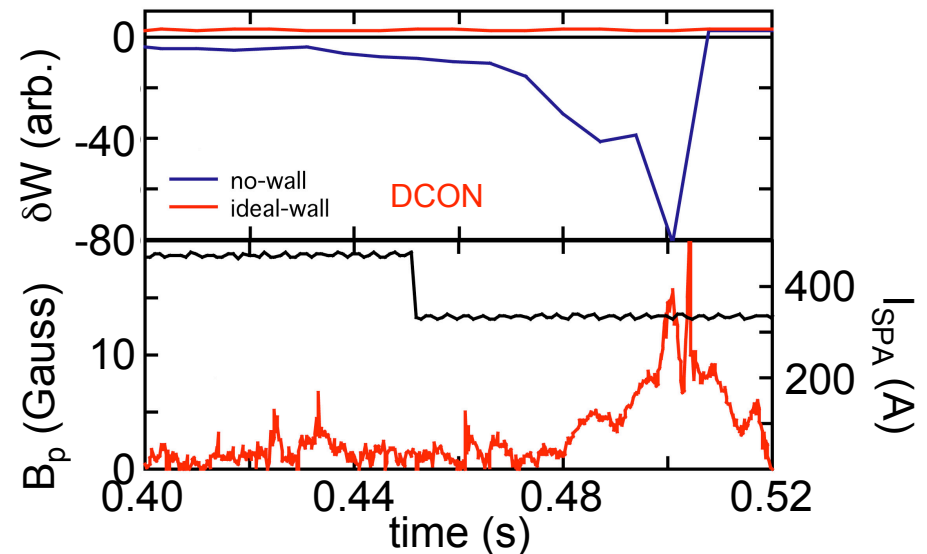
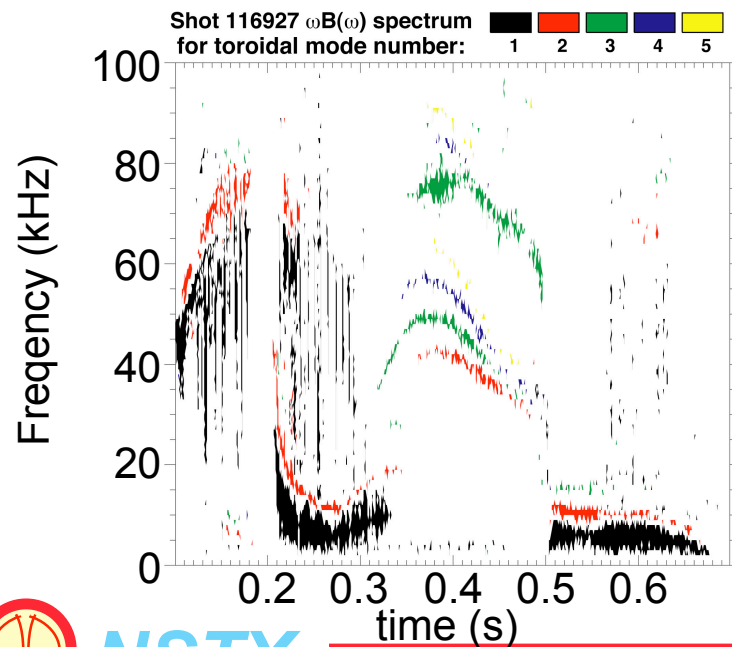
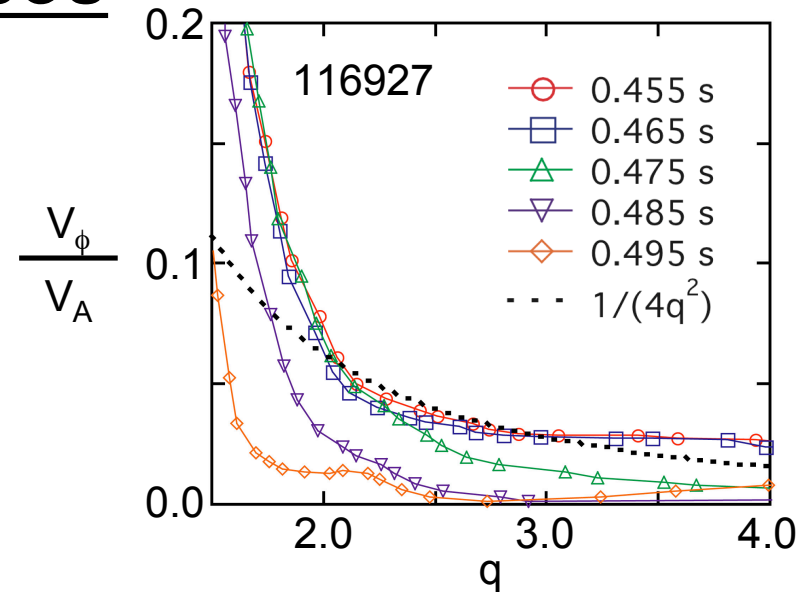


- RWM leads to disruption
- Type I ELM causes  $\beta$  drop, but plasma recovers
- Minor collapse has smaller  $\beta$  drop than RWM, but no recovery

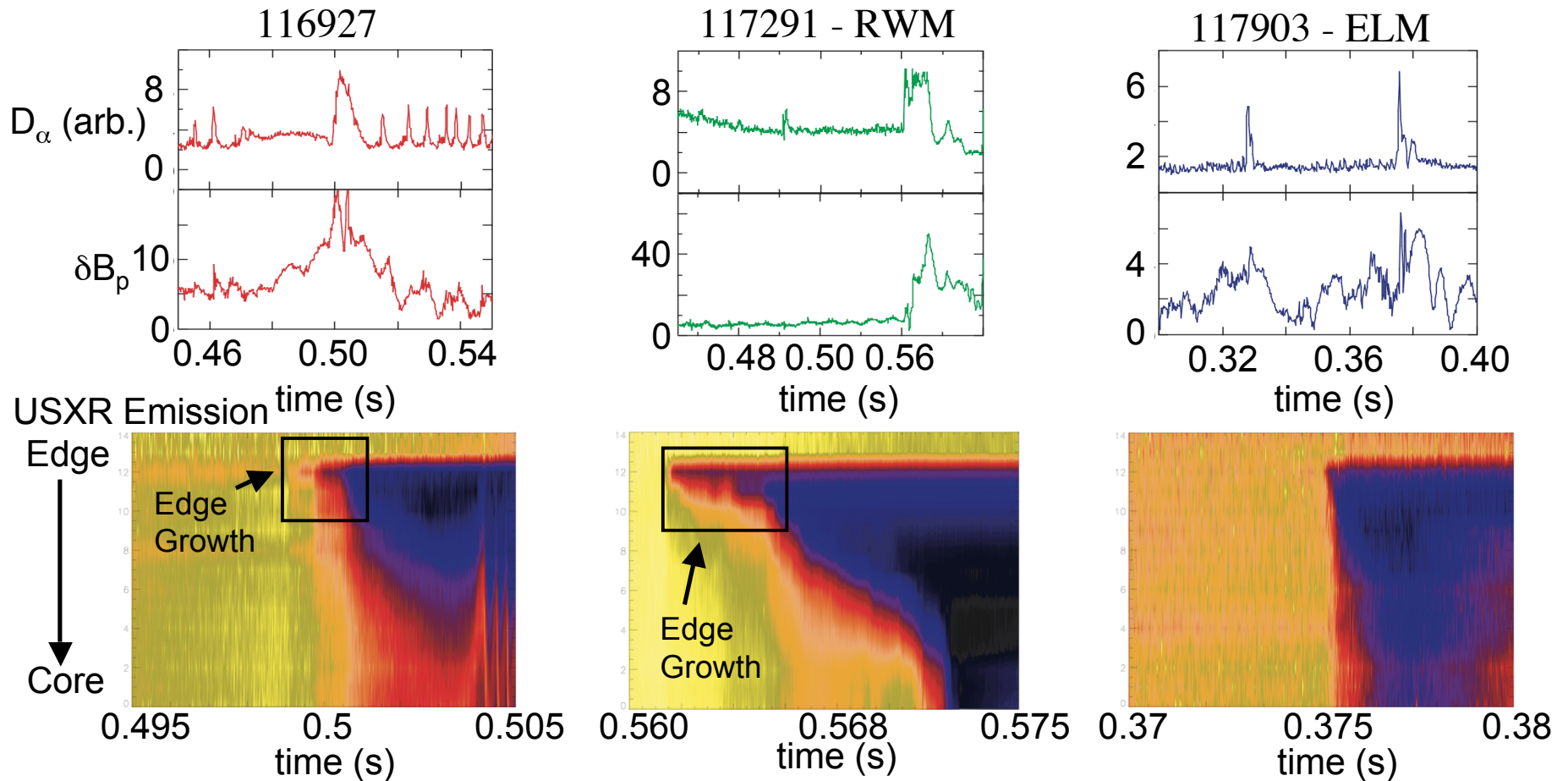
□ *must examine in more detail to classify this collapse*

# RWM Characteristics Observed During Smaller $\beta$ collapses

- Typical RWM causes disruption
- Some smaller collapses could be due to non-disruptive RWM
  - slow mode growth observed in internal sensors
  - growth rate and onset consistent with RWM
    - $\sim 10$  ms growth time
    - low rotation well inside  $q = 2$
- Growth of tearing mode removes unstable drive



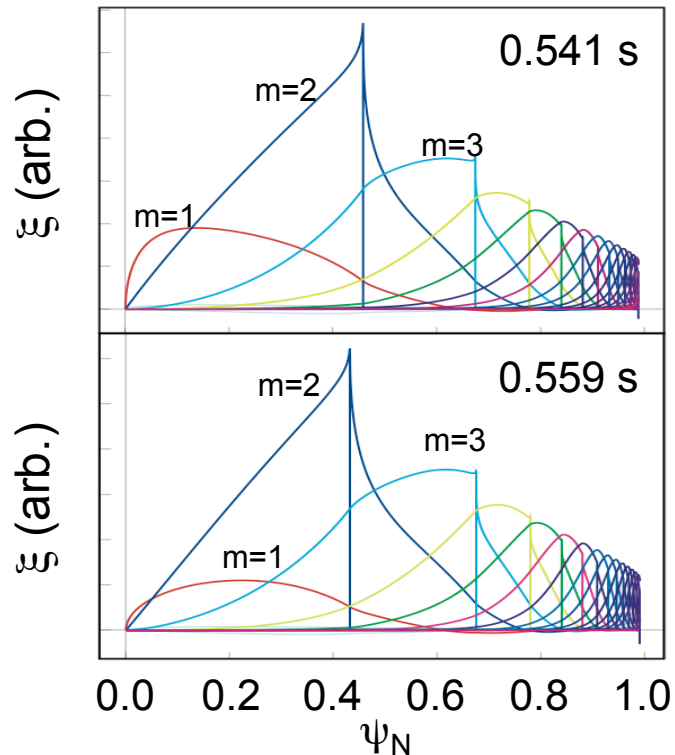
# Minor $\beta$ Collapse Dynamics Support RWM



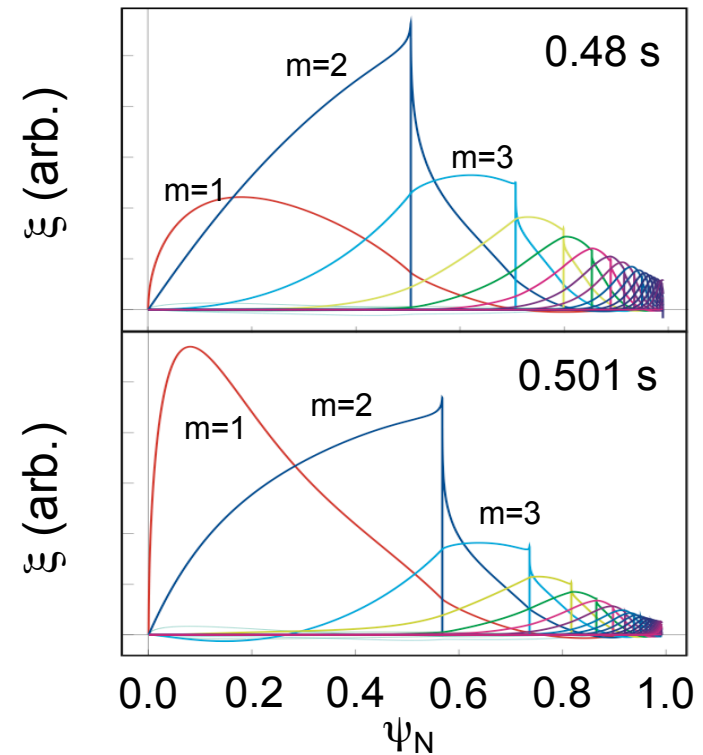
- SXR data shows initial mode growth at edge then slow penetration
  - high  $\delta W$  for 116927 causes faster growth than 117291
- ELM much more rapid than both 116927 & 117291

# DCON Shows Mode Structure Internalizing

117291 Poloidal Mode  
Eigenfunctions



116927 Poloidal Mode  
Eigenfunctions



- 116927 becomes Mercier unstable in core
- Large internal perturbation provides ideal trigger for tearing mode
  - reduction in  $\beta$  removes unstable drive for RWM

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# Summary

- Active coils allow detailed study of RWM physics
  - rotation control
  - RFA studies - MHD spectroscopy
- Examining rotation profile effects indicates rotation at outer  $q$  surfaces not required for RWM stability
  - RWM stable discharges produced with low or negative rotation outside  $q = 3$
  - core rotation (inside  $q = 1.5$ ) alone cannot stabilize RWM
- DIII-D similarity study under way to determine aspect ratio effects on RWM stability
  - low-A requires higher rotation
  - $V_s$  normalization removes aspect ratio dependence
- Growth of internal modes can halt RWM collapse
  - internal kink/ballooning modes can trigger tearing modes, removing unstable drive for RWM

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# Reprints



**NSTX**