

*Schematic layout of top and bottom  
banners (about 5 ft wide)*

*...being professionally drafted...*

# Abstract



Tearing mode beta limits depend on a complex balance between pressure gradient 'neoclassical' drives, small island threshold effects, external triggers and underlying classical tearing stability,  $\Delta'$ .

In this study, the threshold physics is probed by:

- deploying different types of *error fields* on NSTX & DIII-D to vary the plasma *rotation profile*
- different forms of *current and heating ramp-up* on JET to vary the *current profile*

*Results suggest changes in the intrinsic tearing stability play a major role in governing beta limits, and can be affected by variations in the current profile or the rotation shear at the  $q=2$  surface*



# Underlying Physics

Tearing drives & sinks described by modified Rutherford Equation:

$$\frac{\tau_r}{r} \frac{dw}{dt} = r\Delta' + r\beta_P \left[ a_{bs} \left( \frac{w}{w^2 + w_d^2} - \frac{a_{pol}}{w^3} \right) \right]$$

*a<sub>pol</sub> from ion polarisation currents*  
*w<sub>d</sub> from finite island transport leading to incomplete flattening of pressure*

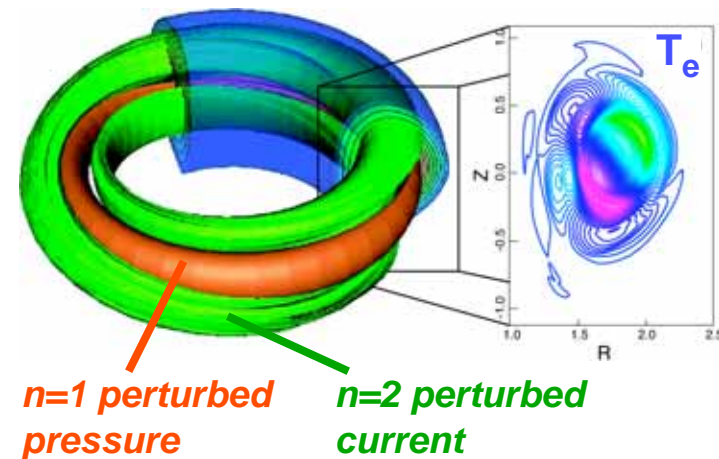
Classical tearing stability - usually negative and stabilizing for NTM

Bootstrap: main drive for the NTM

*w<sub>d</sub>, a<sub>pol</sub> terms stabilise mode at small island size*

**Leads to trigger requirement (a seed) for mode**

- **Current profile** governs basic 'intrinsic' tearing stability
- **Rotation** can enter through several mechanisms:
  - Shielding out trigger perturbation
  - Change intrinsic tearing stability
  - Small island effects e.g. *a<sub>pol</sub>*



[NIMROD, Brennan]

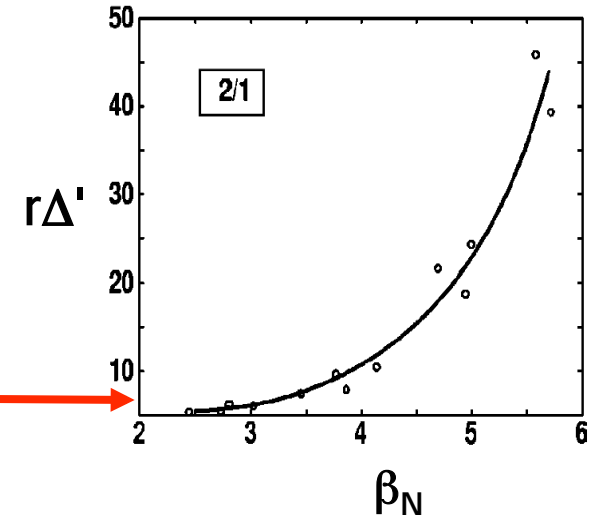
# Highest $\beta$ Limits May Be Governed by Pole in $\Delta'$

– Introducing dependency on current and flow profiles

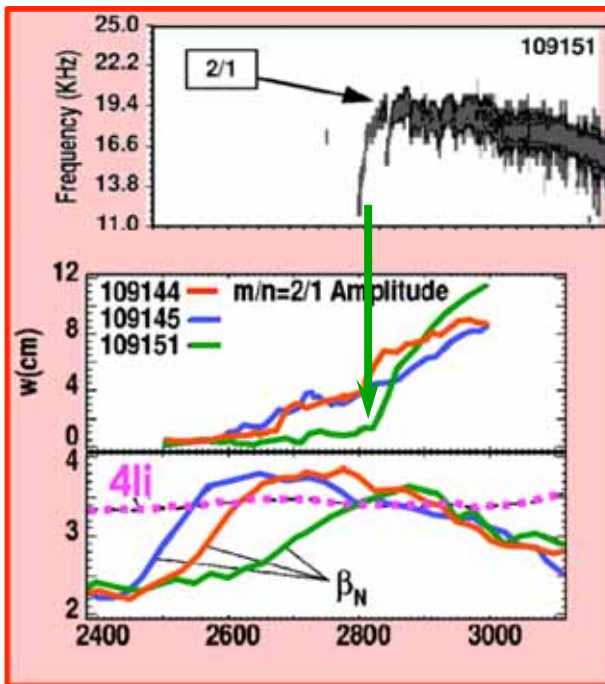
- Calculations show  $\Delta'$  rises as ideal  $\beta$  limit approached

Seedless 2/1 modes observed as  $\beta_N$  crosses ideal no-wall limit

- *Current profile governs baseline  $\Delta'$  & gives means to raise thresholds*



[Brennan et al, PP10, 1643]

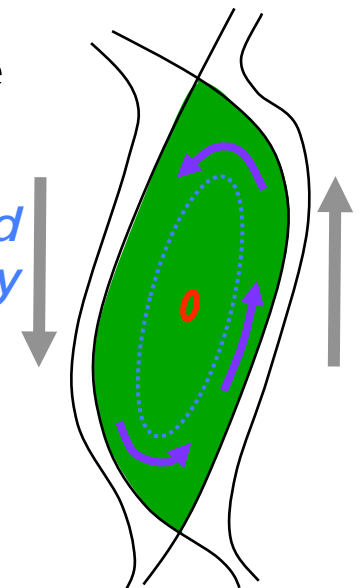


- Island stability may also be modified by flow shear:

– *Viscous coupling distorts island structure changing free energy*

- Error fields can perturb flows in the plasma

– *Response to error fields may depend on plasma stability  $\leftarrow \beta_N, \Delta'$*

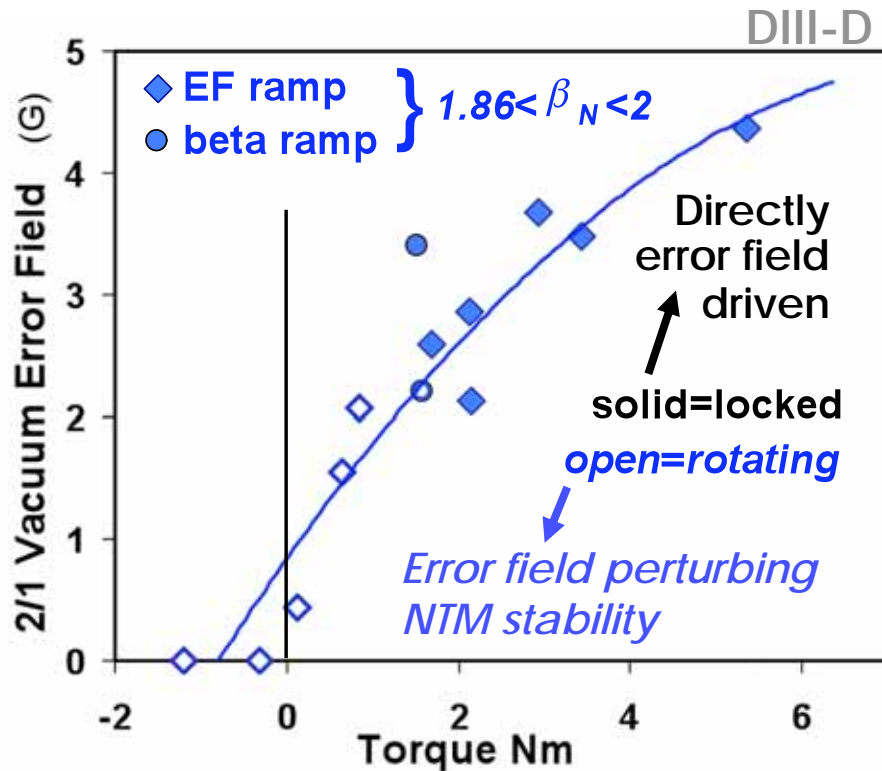




# **Role of Error Fields & Plasma Rotation**

# How do Error Fields Interact with Plasma?

*DIII-D experiments show resonant error field can act through two mechanisms to drive modes in high  $\beta$  plasmas:*

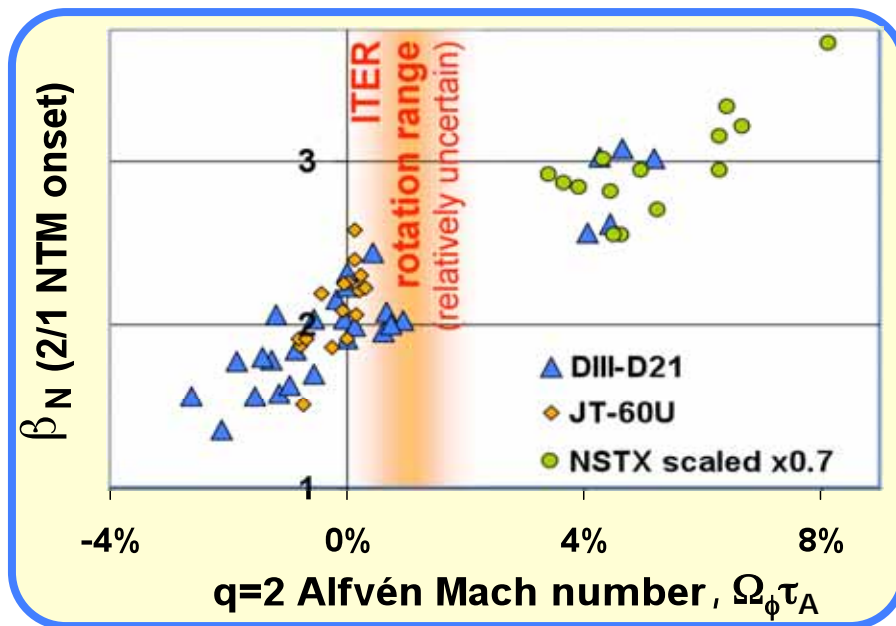


- Locked modes:
  - Influenced by proximity to
    - ideal kink beta limit?
    - classical tearing limit?
  - Role of rotation?
- Rotating modes:
  - EF perturbing classical or neoclassical stability?
    - Action through rotation or rotation shear?

→ EFs can probe NTM physics  
→ Measure error field response & correction requirements...

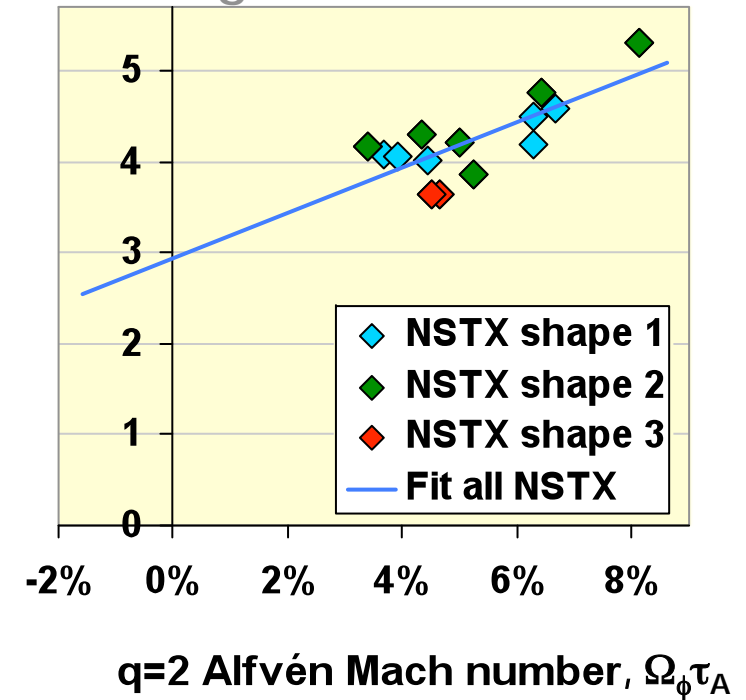
# NSTX Studies Have Shown a Rotation Effect in Error Field Interaction & Impact on NTM $\beta$ limit

- n=3 braking showed 2/1 NTM thresholds rise with rotation
  - Consistent with rotation trends from beam mixing studies on DIII-D & JT-60U:



$\beta_N$  (2/1 NTM onset)

NSTX: n=3 braking perturbs rotating 2/1 NTM beta limit



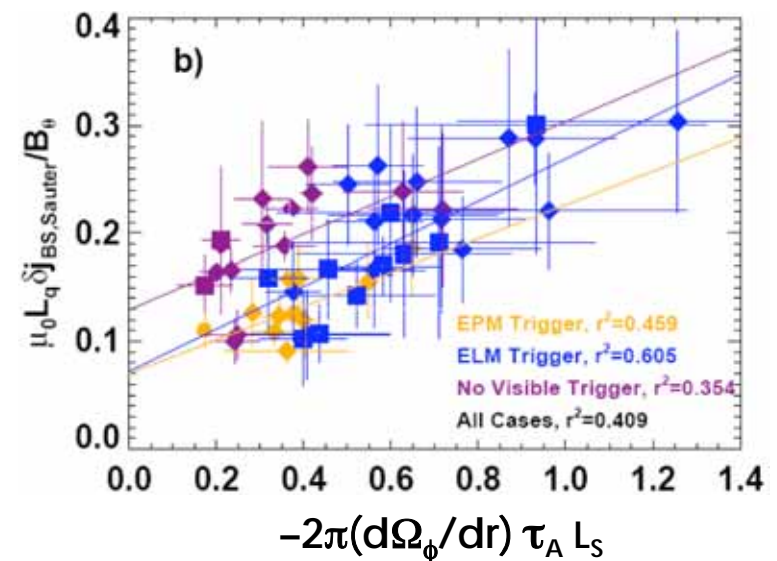
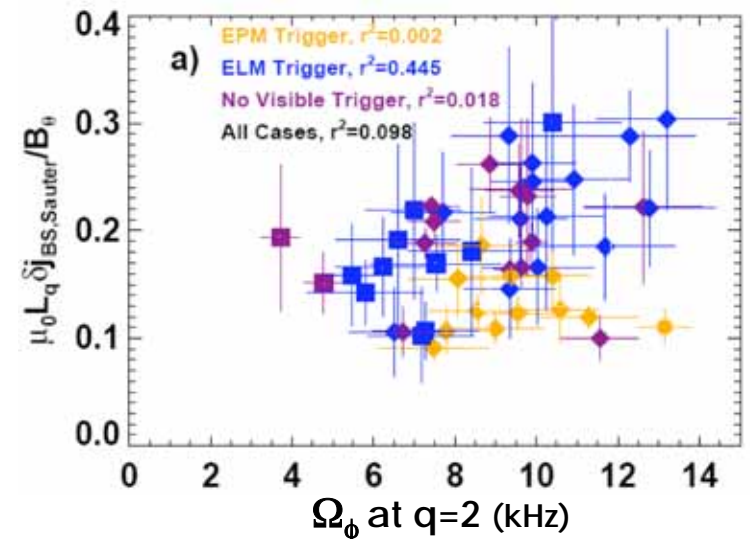
- How is rotation acting on NTM stability?
- What are practical error field limits?

# NSTX Database Study Suggested Rotation Acts Through the Local Rotation Shear at the Island

- Gerhardt analysis<sup>1</sup> compared trends for different types of NTM trigger across NSTX 2007 campaign
  - no n=1 braking in this data set

*Goal 2009: Controlled study of error field effect in constant conditions:*

- Decouple rotation roles further with n=1 and n=3 fields
- Learn about error field interaction
- *Achieved reproducible scans by tuning H mode:*
  - shape, gas, lithium



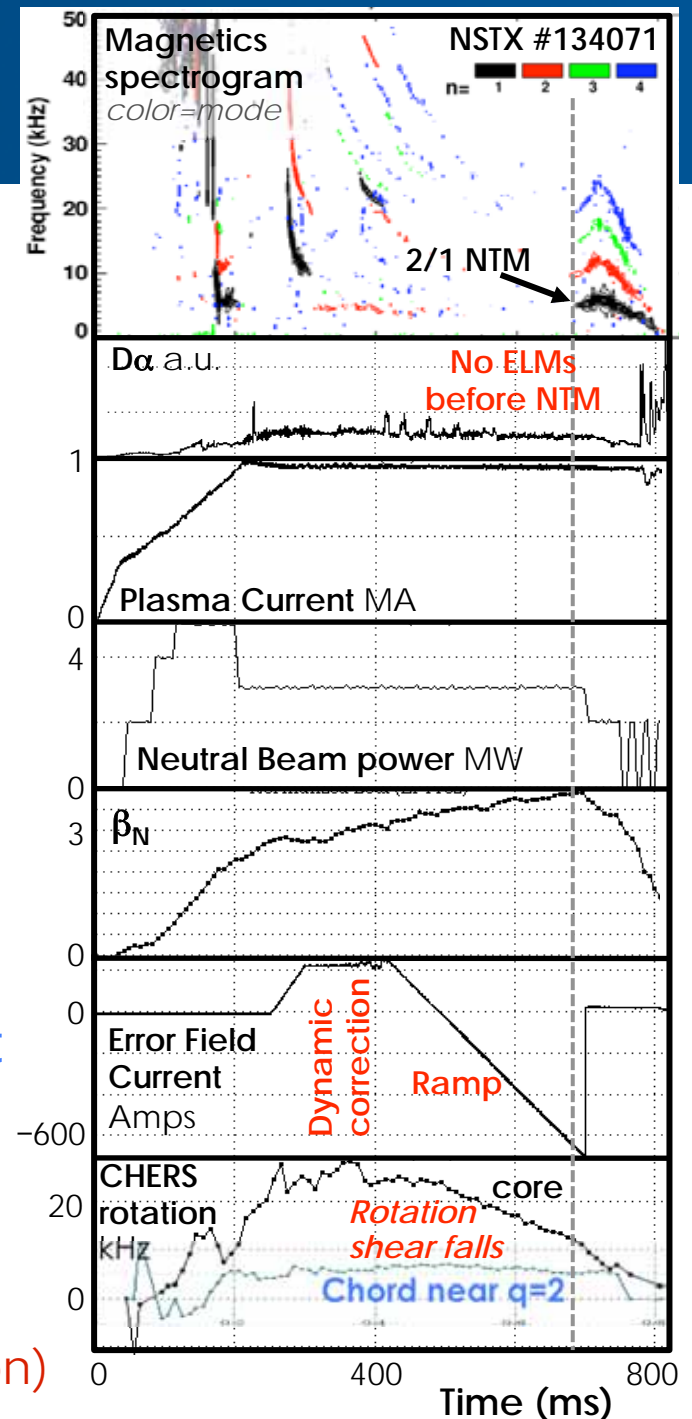


# New NSTX Experiment: Ramp Error Fields to Make Mode

- Vary ratio  $n=1:n=3$  fields shot to shot
- Typically ELMs are small (due to lithium)
- No clear NTM trigger in most shots
  - ‘Seedless’ – must be  $\Delta'$  triggered

## Other shot details:

- Early strong heating for H mode
- MHD at 300ms when  $q=2$  appears
- Reproducible conditions & front end to eliminate  $q$  profile changes shot-shot
  - From evaporating lithium each shot
- But note  $q$  relaxing towards  $q=1$  (when bad MHD would occur)
  - (Role of  $q_{\min}=1$  with EF under investigation)

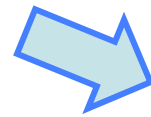


# Applied Error Fields

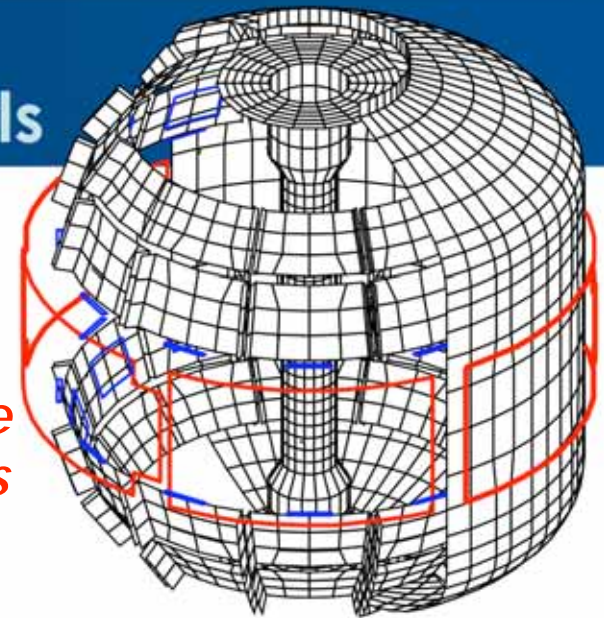
## Mix of $n=1$ & $n=3$ from Midplane Coils

- $n=1$  field computed for various shots across the scan:

- Vacuum field is  $\sim 2.5\text{G/kA}$  ( $m=2$   $n=1$  at  $q=2$  surface)
- Including plasma response from other surfaces (IPEC) raises **total field** at  $q=2$



*Midplane field coils*

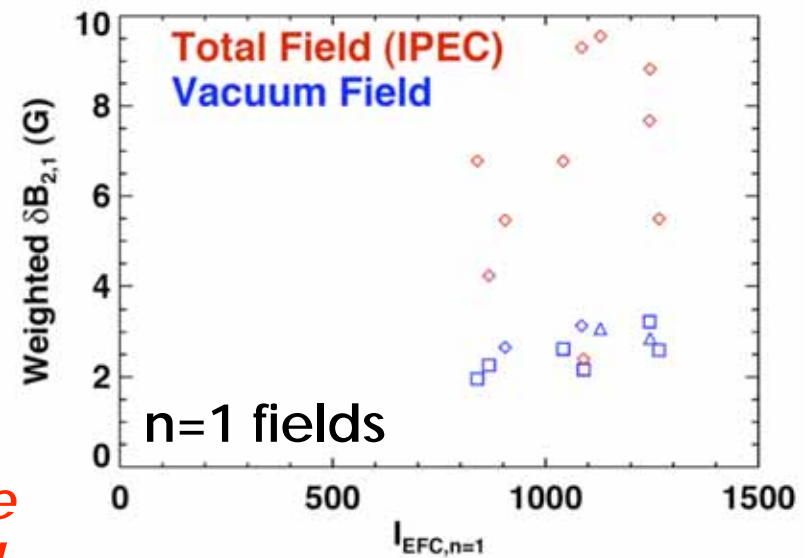


NSTX

- $n=3$ : no similar formalism to compare size (as non-resonant)

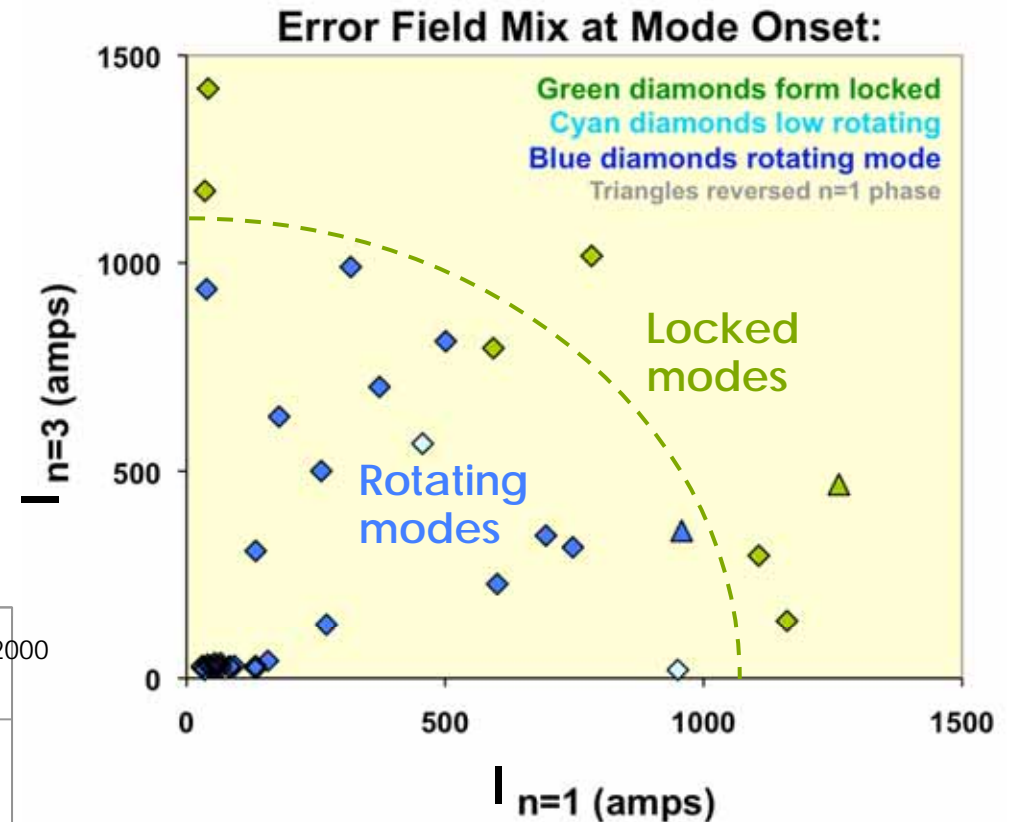
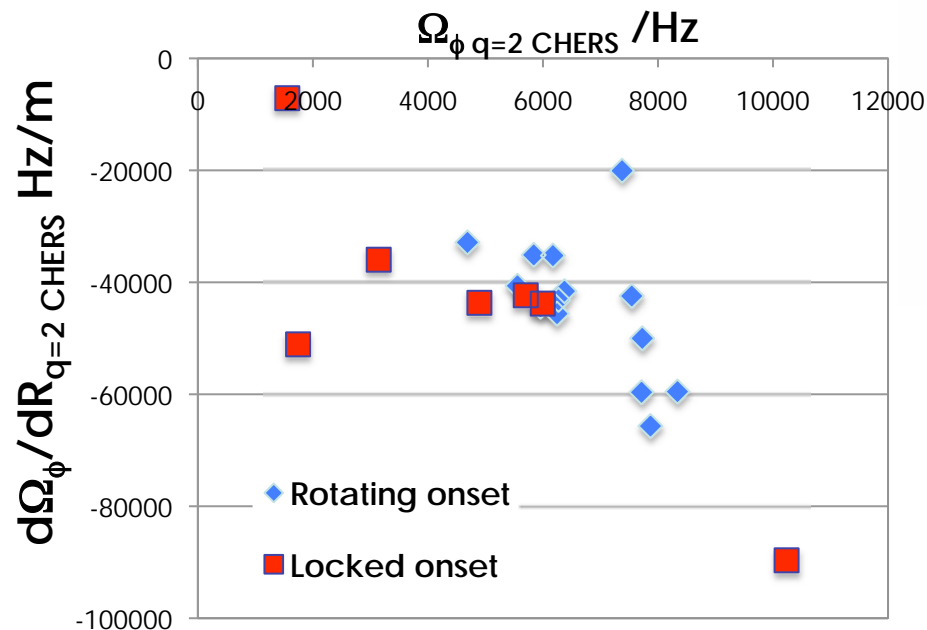
- Typical surface averaged  $|B|$  is a few Gauss
- *But may be best to compare relative magnitudes in terms of coil currents!*

- *Gives better idea of relative field strengths*



# New Experiments Perturbed $\beta$ Limit with Wide Range of Resonant $n=1$ & Non-resonant $n=3$ Fields

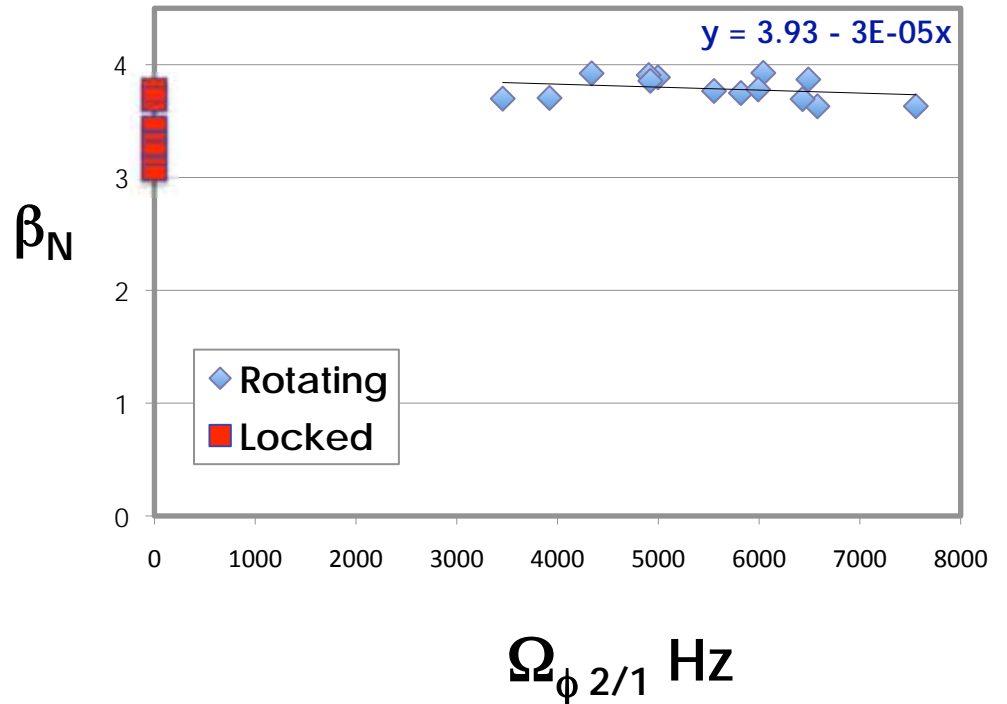
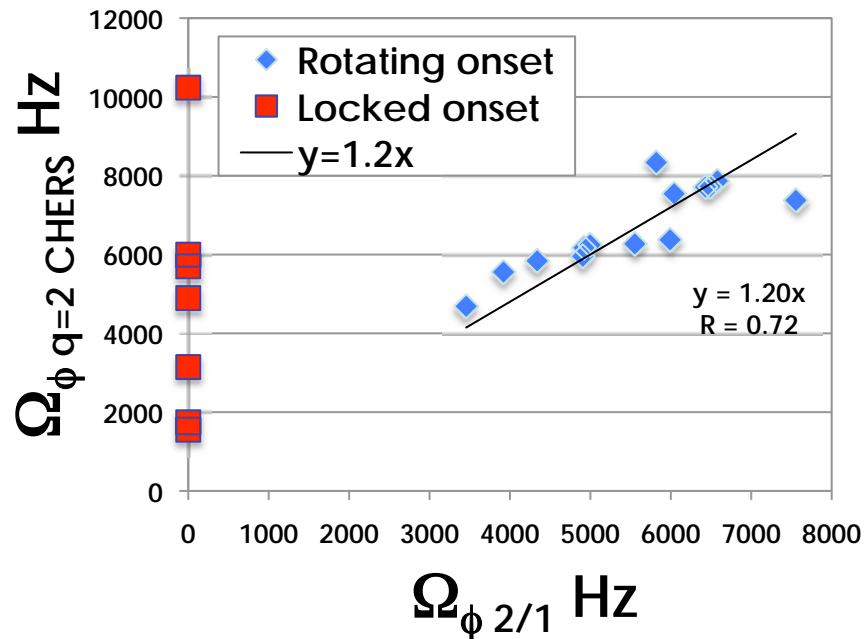
- $n=1$  and  $n=3$  fields varied up to locked mode limits (◆)
  - Locked mode threshold with roughly equal levels of  $n=1$  and  $n=3$  field current
  - Wide variation in rotation profile achieved:



- Locked modes much slower on CER but not at zero rotation

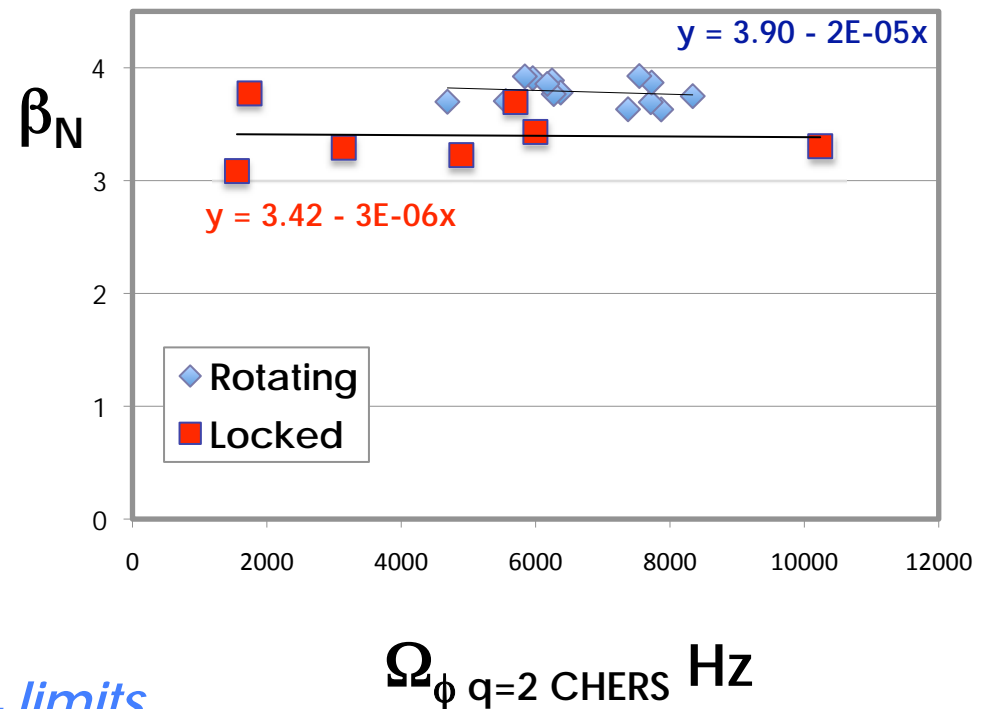
# Differences in CHERS q=2 and 2/1 mode rotation

- Mode forms locked while CHERS shows plasma rotating
  - Actual mode onset rotation is lower than CHERS
    - Coupling to ELMs?
  - Locked mode stops MHD fluid while plasma still flows



# Mode Forms at Lower $\beta_N$ when Locked

- Locked mode threshold is 0.5 lower in  $\beta_N$ 
  - May be partly confinement reduction
  - stripped out for rest of this analysis (J-KP analyzing locked mode physics<sup>1</sup>)
- Rotating mode shows no rotation dependence!

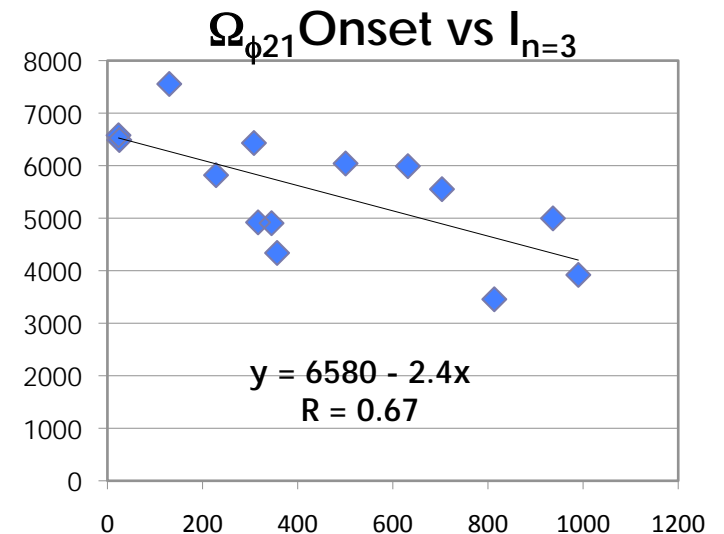
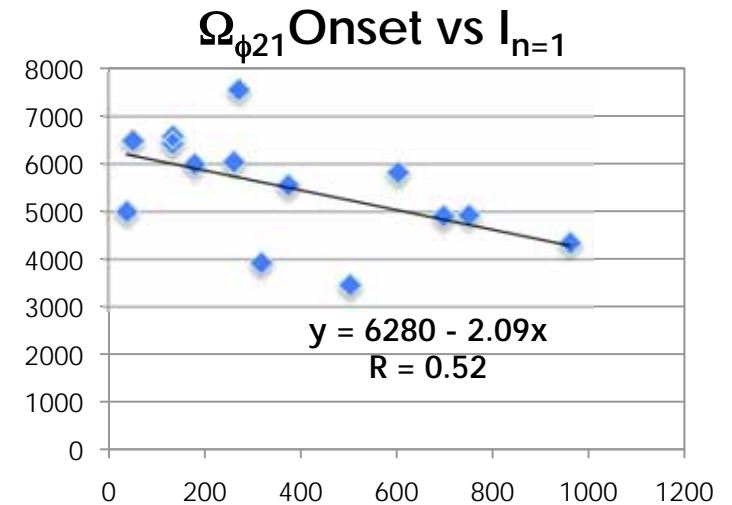
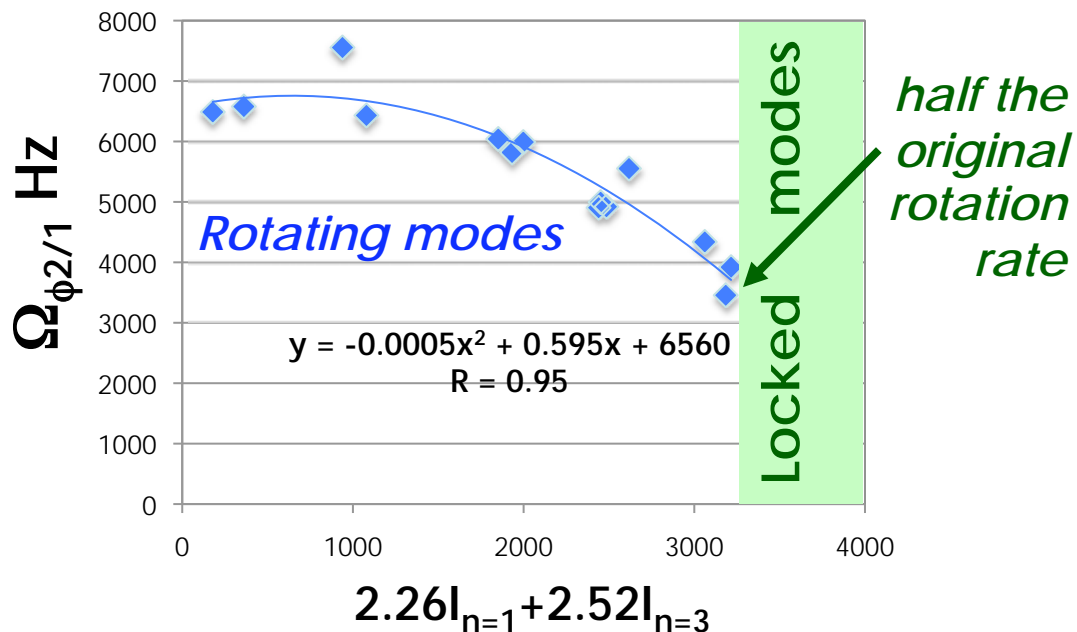


- *Generally below no-wall  $\beta_N$  limits*
- *But need to look at drives in local parameters & understand what we really varied*
  - *How does braking impact rotation and mode drives?*

[<sup>1</sup>Poster: PP8.00051, Jong-Kyu Park]

# Braking Effect: n=1 & n=3 Contribute Similarly to Braking

- Both n=1 and n=3 brake plasma
- Best fit is combination of similar levels of n=1 and n=3 currents:
  - $\Omega_{\phi 21} = 7500 - (2.26I_{n=1} + 2.52I_{n=3})$
  - *Good correlation for braking:*

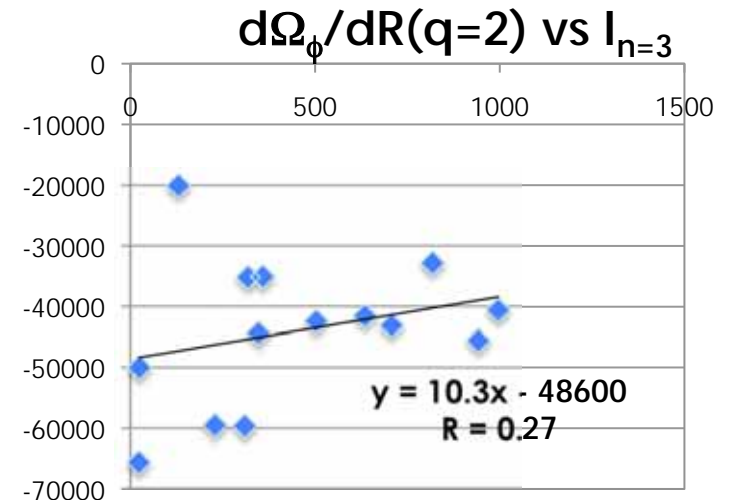
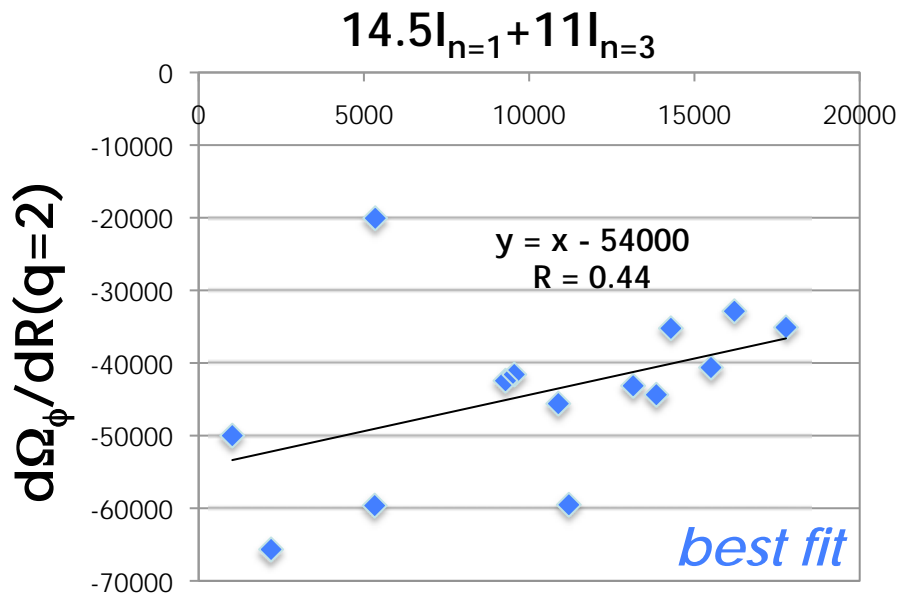
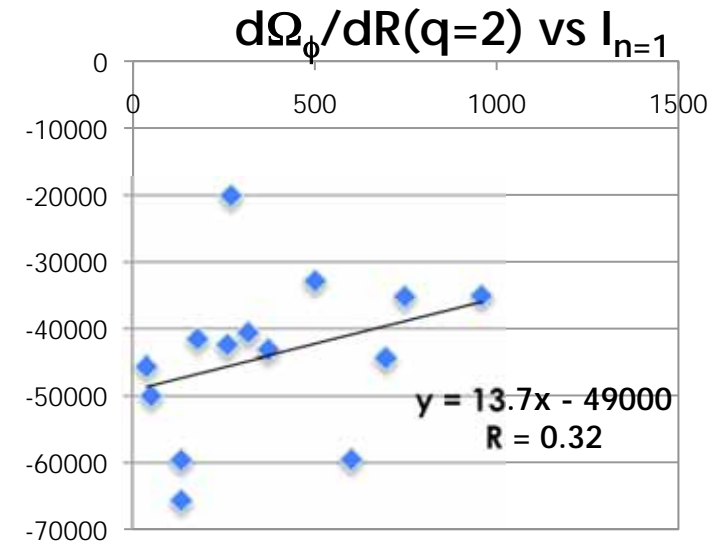


✓ *Matches Fitzpatrick theory: Penetration at half natural rotation rate.*

# Rotation Shear Much More Variable Over The Scan

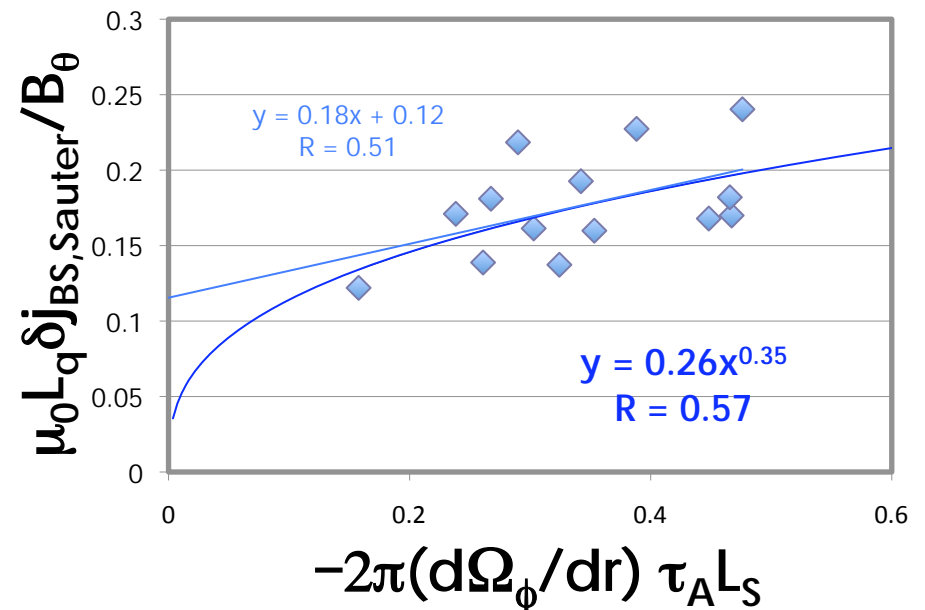
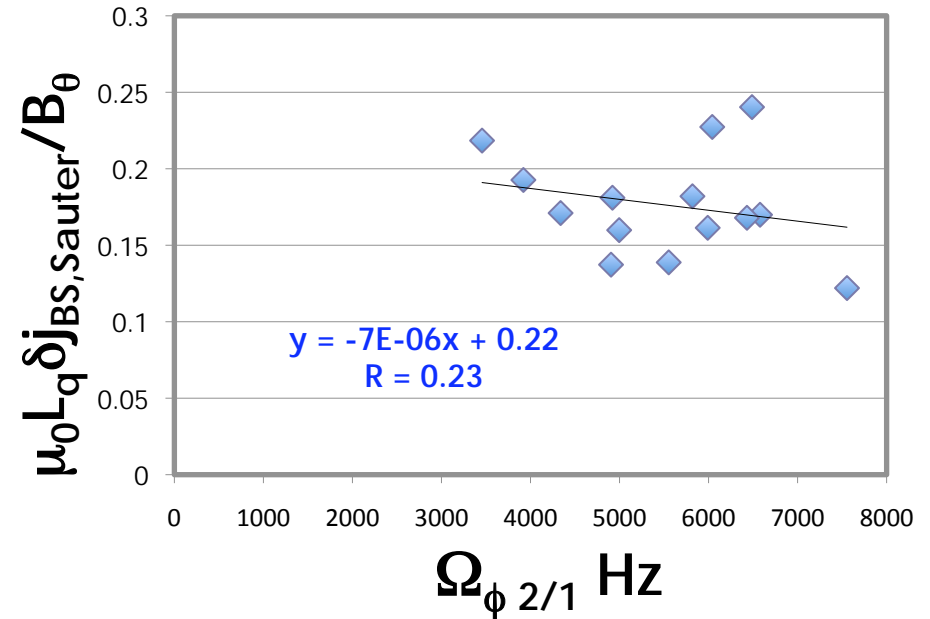
– *provides opportunity to decouple from rotation trend*

- Rotation shear more scattered than simple dependence on  $n=1$  &  $n=3$ 
  - Although both forms of braking reduce rotation shear – *best fit*:
    - $d\Omega_{\phi 21}/dR = -54000 - (14.5I_{n=1} + 11I_{n=3})$
  - Can decouple rotation shear from rotation effects – *which governs NTM?*



# Bootstrap Drive Measure of NTM Threshold Suggests Dependence Through Rotation Shear

- No measurable trend with rotation!
  - Weak positive correlation with normalized rotation shear
    - Lowest thresholds at low rotation shear
    - Highest thresholds at high rotation shear
    - Best 'fit' is power law
- This correlation in the 'most noisy' parameters suggest physics is right:*
- *Rotation impact is through shear changing  $\Delta'$*
- No correlation if fit  $\beta_N$  instead
  - Fit vs rotation & rotation shear offers little improvement





# Conclusions on Rotation & Error Fields

- NTM threshold dependence on rotation comes through **flow shear** impact at the rational surface
  - Confirms previous database study in controlled conditions
  - Correlations with rotation completely stripped out!
    - *Suggests changes to inherent plasma stability at the tearing resonant surface play an important role in determining mode onset*
- Threshold between rotating & locked mode regime at half natural plasma rotation
  - $\beta$  limit for rotating modes reduced below this
  - Locked modes above this (à la Fitzpatrick)
- Locked mode cases exhibit confinement degradation *before* mode onset, and have a lower  $\beta_N$  limit
- Both  $n=1$  resonant braking and  $n=3$  non-resonant braking have similar effects on plasma and mode



# **Role of the Current Profile**

# JET Hybrid Plasma Sit Above $\beta$ Limit of Other Devices: *Other parameters coming into play – q profile?*

- JET sits above DIII-D and JT-60U trends

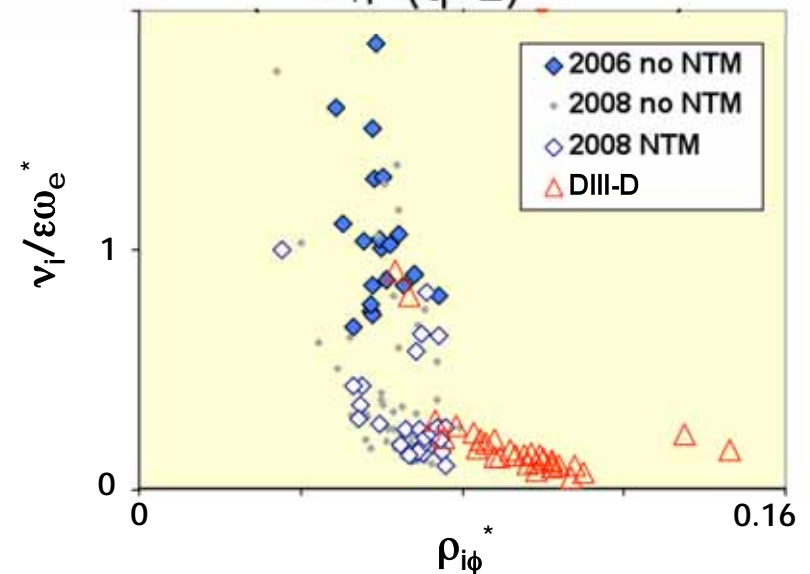
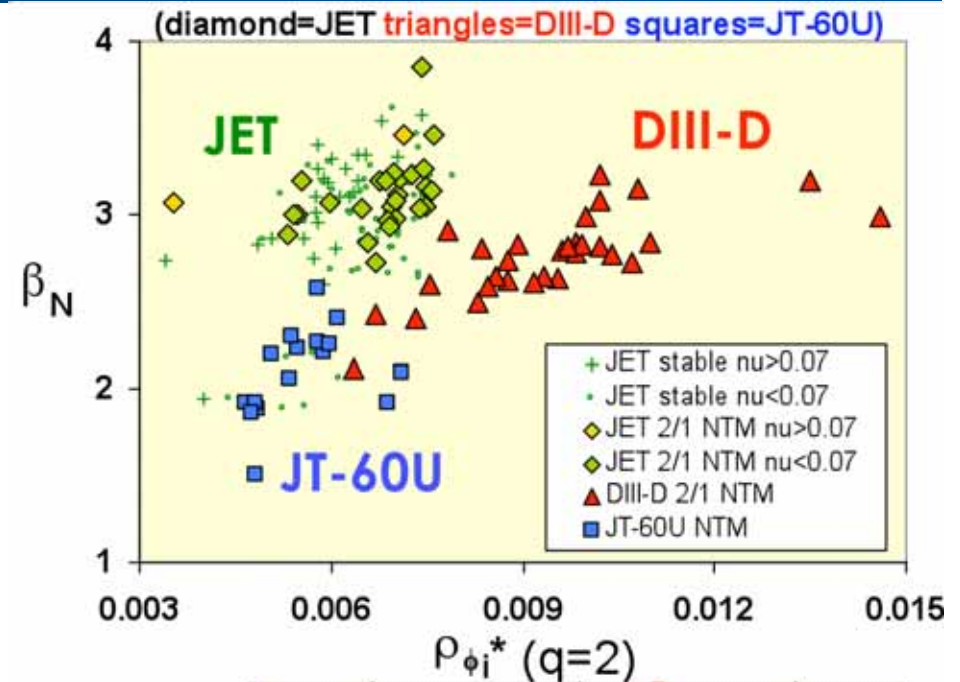
- JT-60U lower rotation  $\rightarrow$  lower  $\beta_N$
- But DIII-D high rotation

- Possible collisionality role? No:

- JET unstable at  $\blacklozenge$  low  $\nu^*$
- But stable at  $+$  high and  $\circ$  low  $\nu^*$

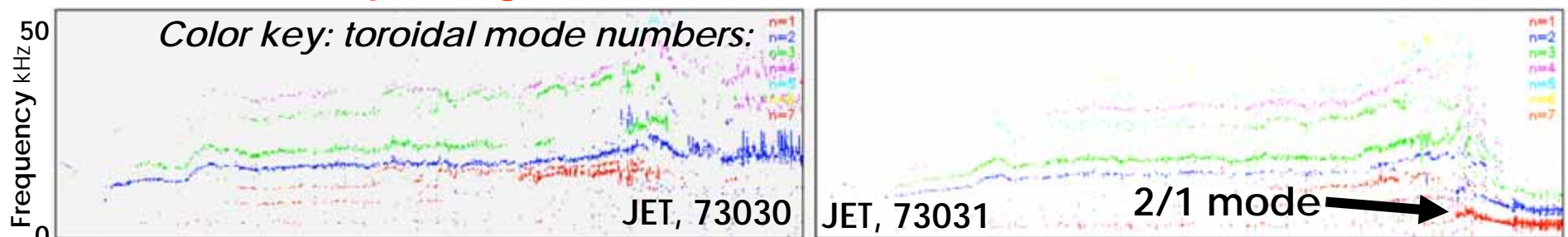
$\rightarrow$  Collisionality provides 'access condition' for NTM

- Enables q profile modification
- Can change  $\Delta'$
- *q profile is the parameter to test...*

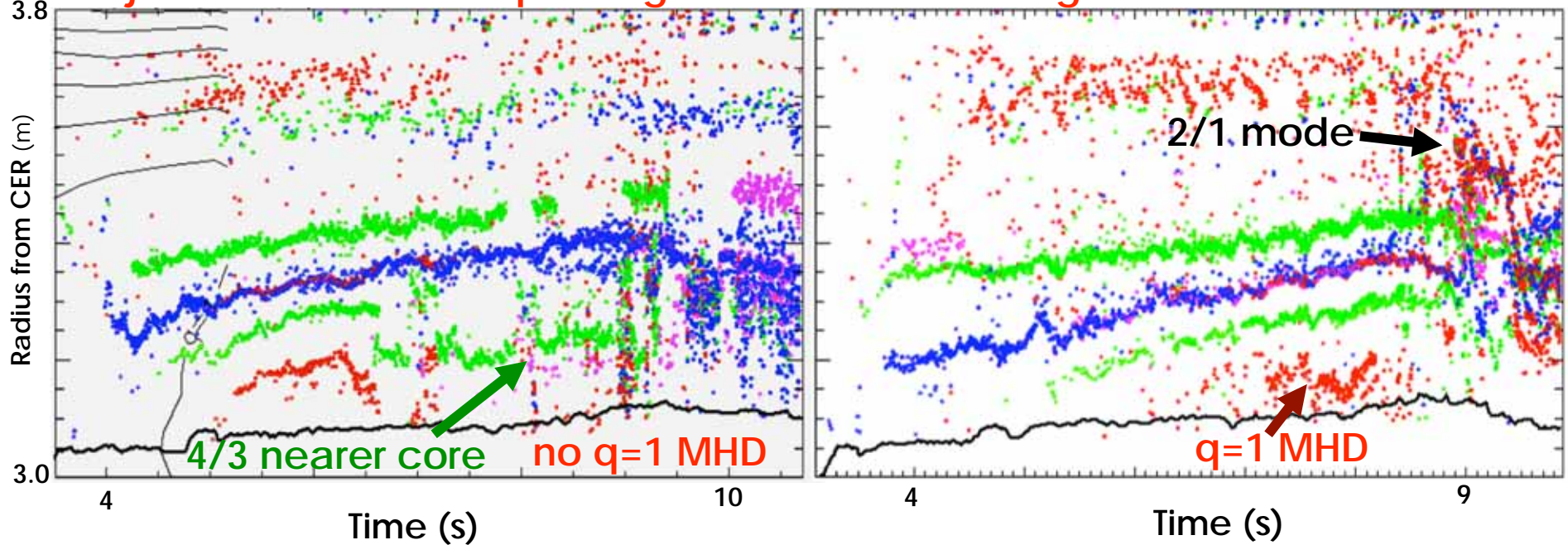


# Difference in MHD Markers Indicates $q$ Profile Change Correlating with NTM Stability Change

Mode number spectrograms:



Project mode number spectrogram onto radius using CHERS measurements:



→  $q_0$  lower in 2/1 case NTM

# Exploring q profile role in controlled scans

q profile varied with three techniques:

JET: 74631-74639

– current overshoot

- J in 'outer third'

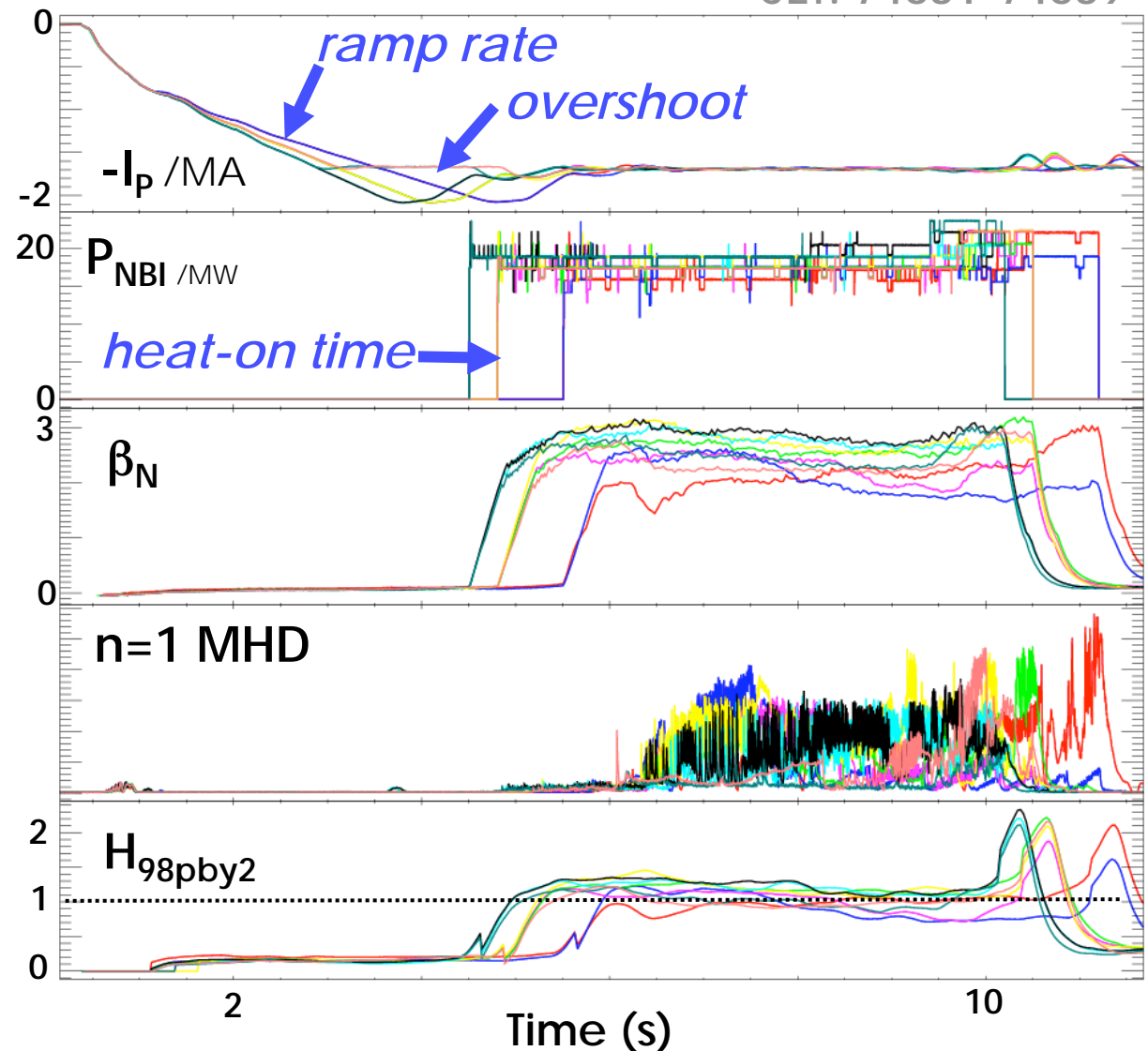
–  $I_p$  ramp up rate & beam-on time

- $q_{\min}$  value

→ *Impacts H factor*

*These 'performance' shots skirted stability limit*

→ *Raise power to access 2/1 NTM...*

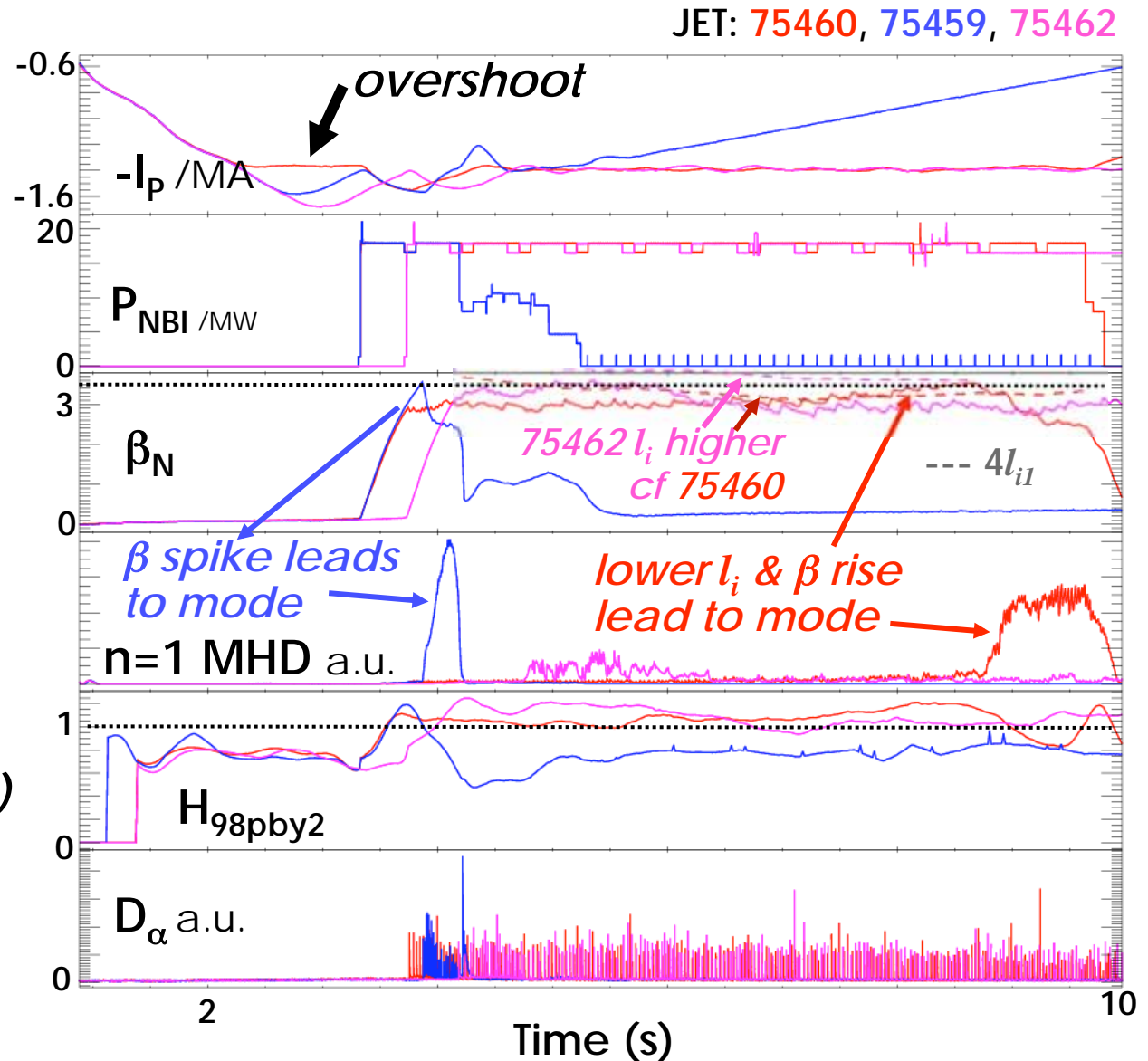


# Discharges show a $\beta_N$ threshold for the mode & q profile dependence (1: $I_p$ overshoot scan)

## Vary $I_p$ overshoot

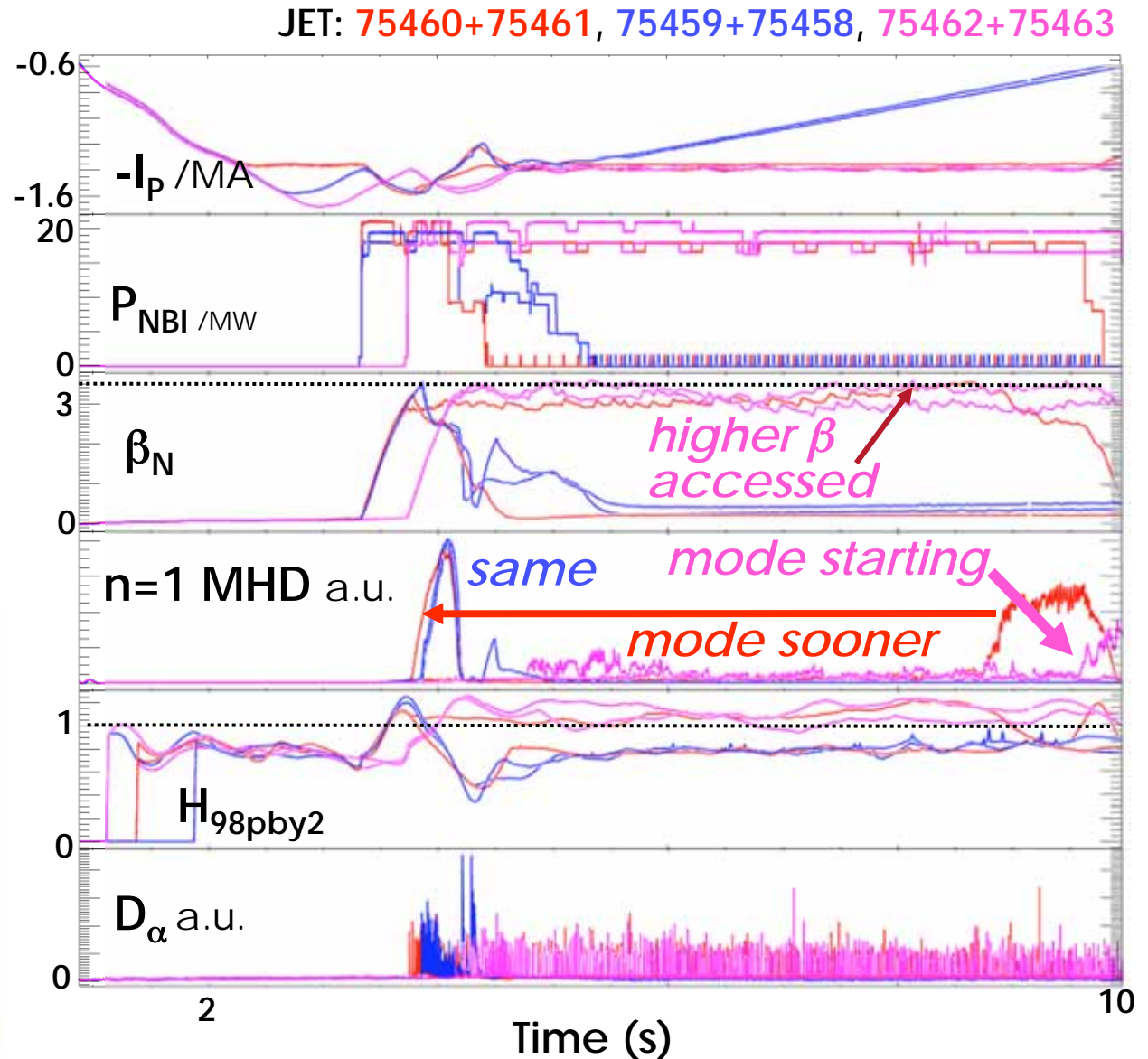
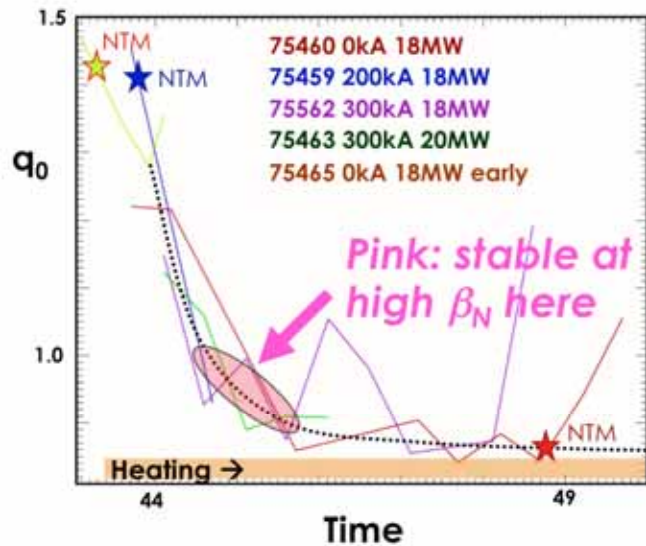
- *No overshoot:*  
→ *late mode*  
*as beta rises?*
- *Modest overshoot:*  
→ *prompt mode*  
*with ELM free*  
*high  $\beta_N$  spike*
- *Strong overshoot:*  
→ *No 2/1 mode*  
*despite early high  $\beta_N$*   
→ *q profile effect on*  
*stability (red cf pink)*

FYI: JET q profile evolves on timescale of seconds, once a strongly heated plasmas is established



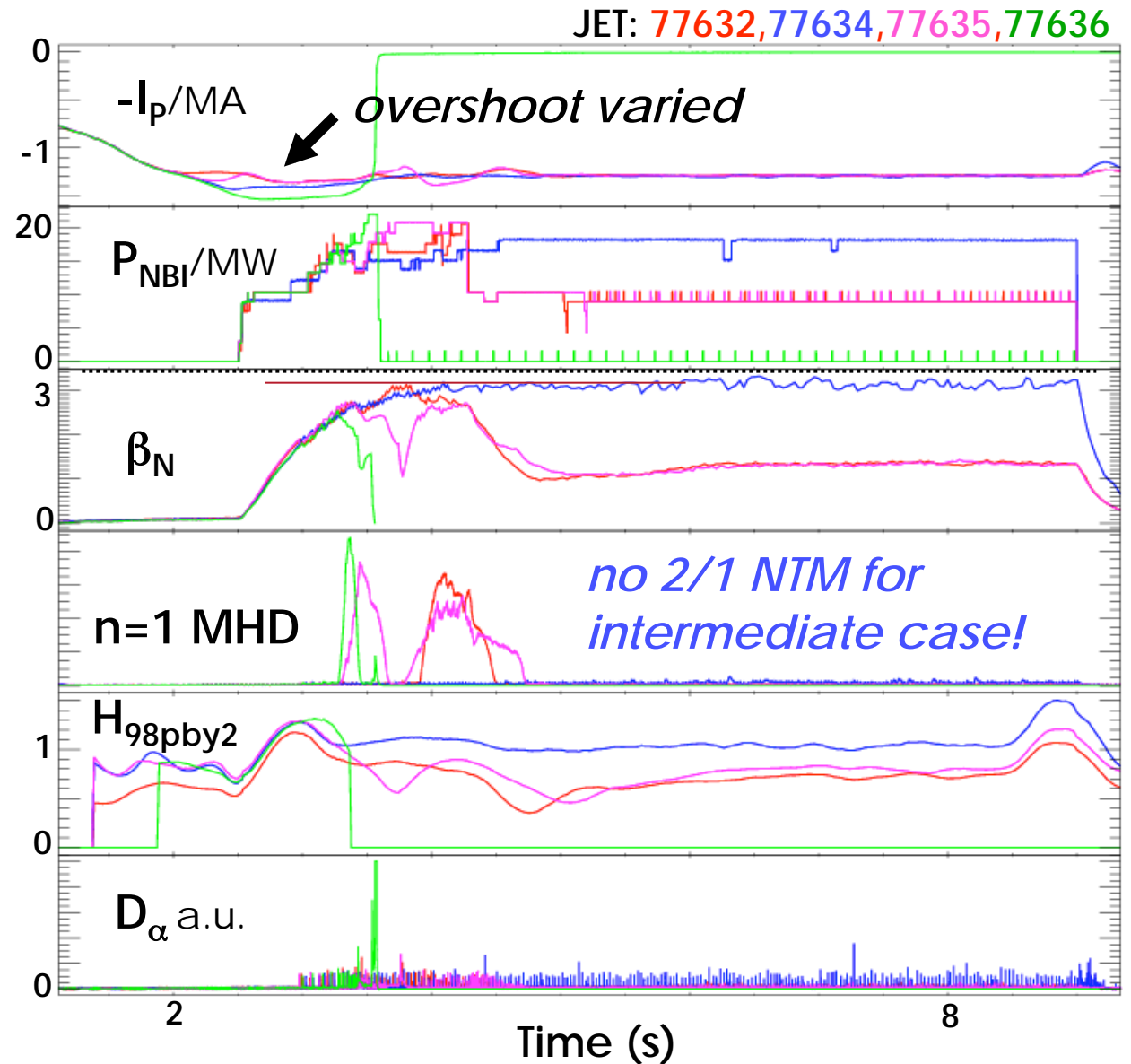
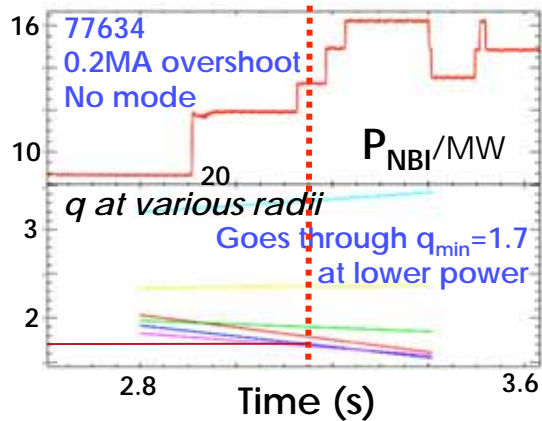
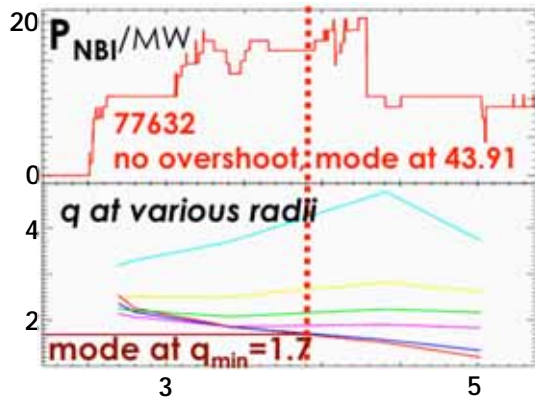
# Discharges show a $\beta_N$ threshold for the mode & q profile dependence (2: with increased power)

- *No overshoot:*  
→ mode sooner as  $\beta_N$  higher
- *Modest overshoot:*  
→ no change same  $\beta_N$  trajectory
- *Strong overshoot:*  
→ Mode at previously stable  $\beta_N$ , once q profile evolved:



# Possible Optimal Degree of Current Overshoot

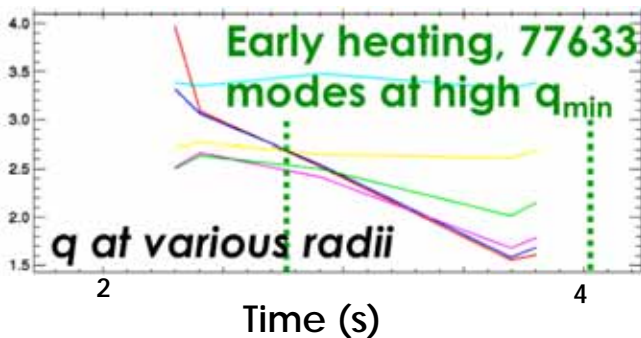
- *Beta feedback to avoid peak in ELM free phase*
- MSE data limited
  - *$q_{min}$  time history may play role:*





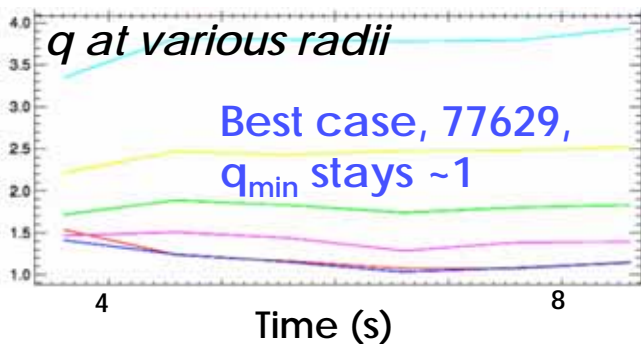
# Heating timing scan shows 'just right' degree of relaxation needed

- Mode if profiles too 'advanced':

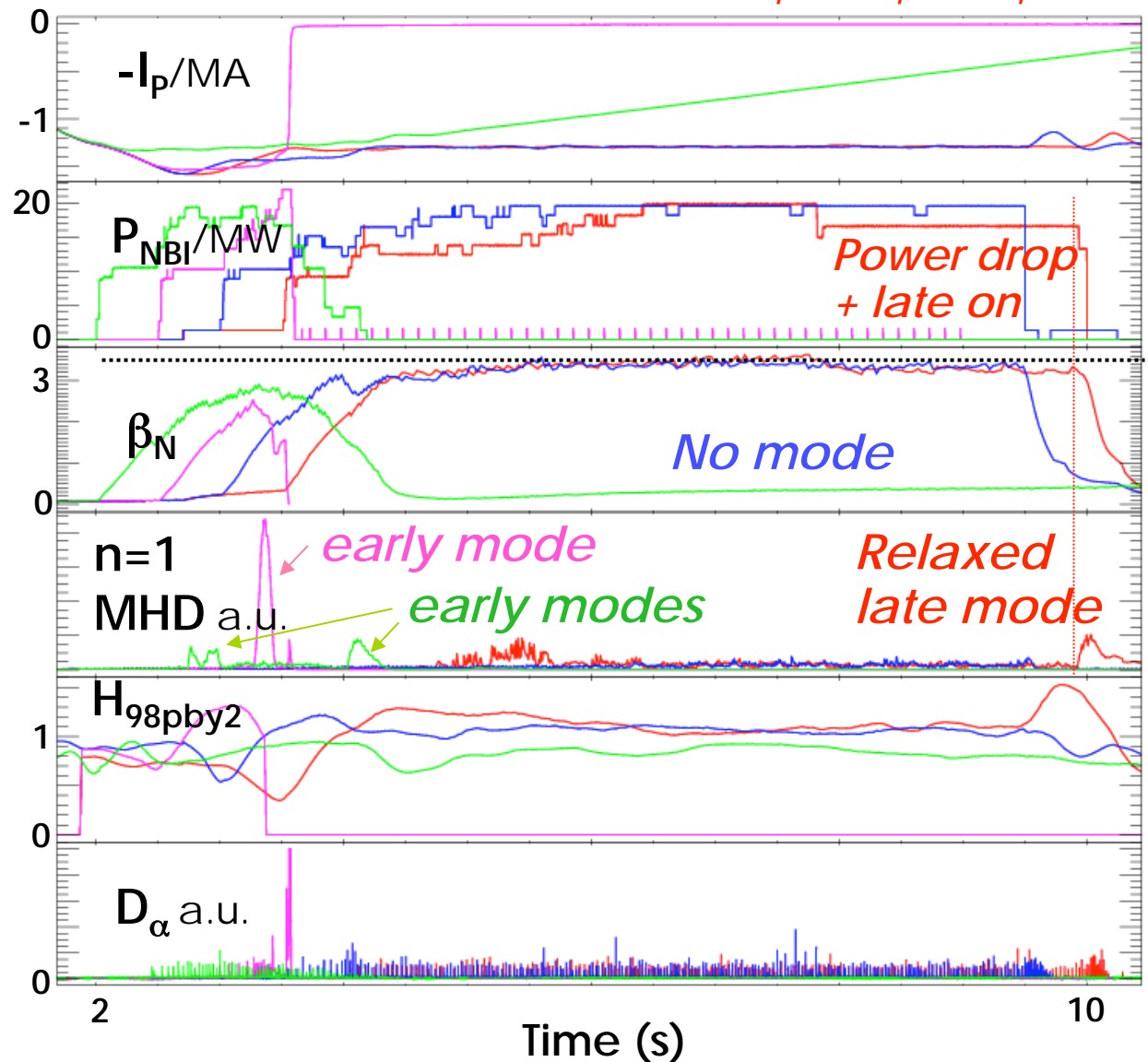


- Fully relaxed plasma also less stable

- Mode at lower  $\beta_N$  or occurs later



JET: 77626, 77629, 77636, 77633



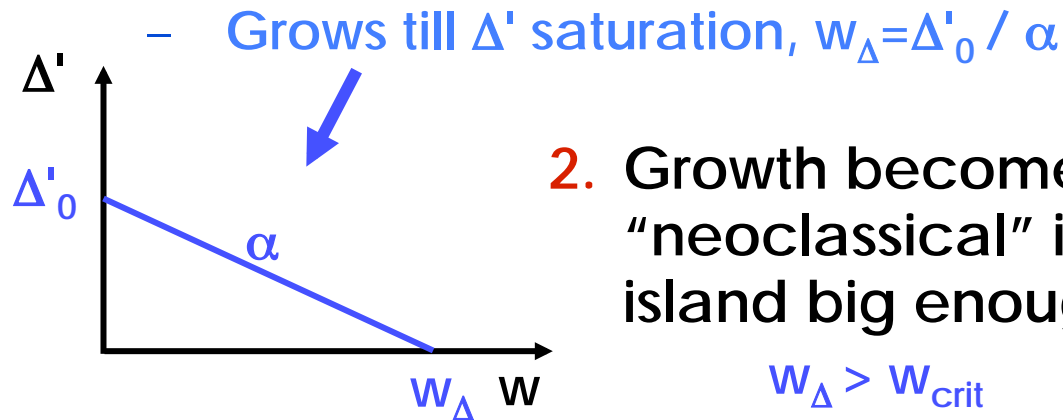
# Conclusions on q Profile Role & Generally

- JET shows increased stability to 2/1 NTM cf other devices
  - Possible origin in q profile dependence
- q profile is observed to play a major role in 2/1 NTM threshold
  - Varying heating timing or  $I_p$  overshoot impacts mode onset
  - Allowing plasma to relax (by waiting or lowering power) can lead to mode at lower  $\beta_N$
  - More 'advanced' q profiles ( $q_{\min} < \sim 2$ ) are more unstable
- It seems that a 'just right' degree of relaxation is needed to maintain stability

A common picture is emerging whereby 2/1 NTM thresholds are predominantly governed by changes in underlying tearing stability of the plasma, and that this can be influenced by manipulating **current profile** or **flow shear**, leading to *risks from error fields and low torque* and *opportunities through q and flow profile tuning*.

# 'Minimal' $\Delta'$ seeding model to explain observations

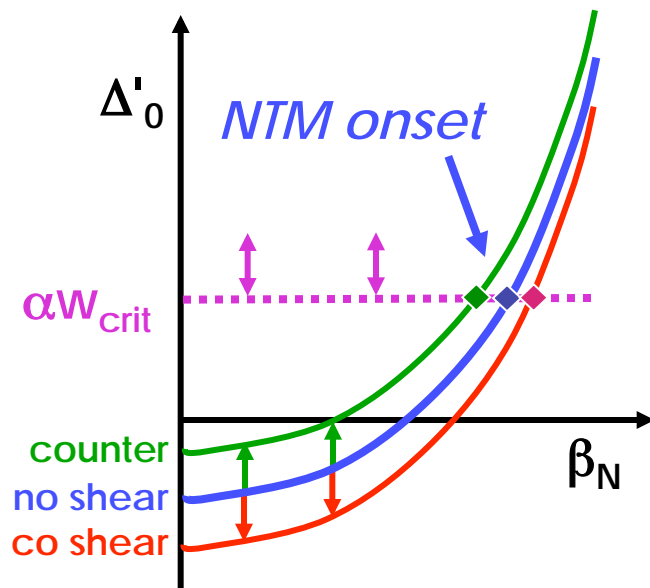
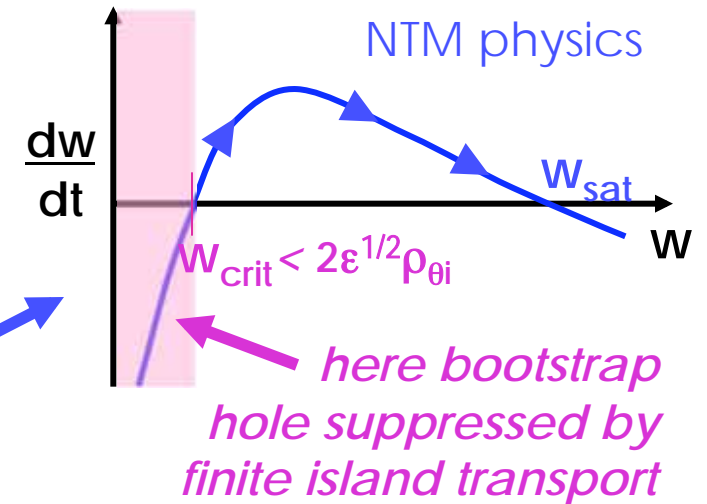
## 1. Positive $\Delta'$ excites a small island



## 2. Growth becomes "neoclassical" if island big enough:

$$w_\Delta > w_{\text{crit}}$$

$$\Rightarrow \Delta'_0 > \alpha w_{\text{crit}}$$



## 3. $\Delta'_0$ is function of rotation shear and $\beta_N$

- **Increases/decreases** in rotation shear will change tearing mode onset  $\beta_N$
- Similarly, **q profile** changes base  $\Delta'$
- $\rho^*$  variation introduced through  $w_{\text{crit}}$
- *but note much harder to excite mode at low  $\beta_N$  away from  $\Delta'$  pole*

# Affiliations



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