

# Anomalous electron transport induced by multiple beam ion driven global Alfvén instabilities

N.N. Gorelenkov, E. Fredrickson, S. Kaye, R. White

*PPPL, Princeton University*

L. Delgado-Aparicio, D. Stutman, K. Tritz

*Johns Hopkins University*

A. Boozer

*Columbia University*

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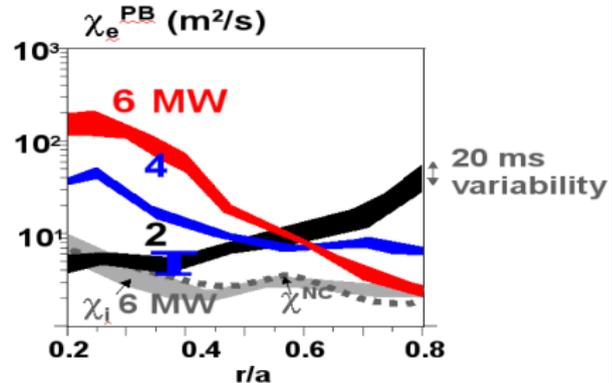
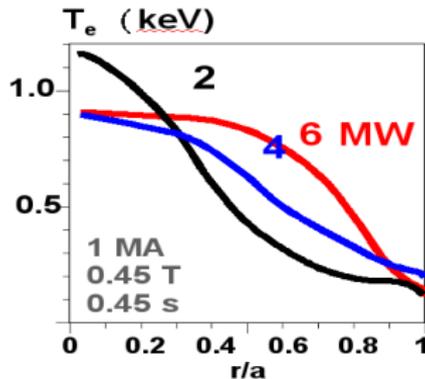


JOHNS HOPKINS  
UNIVERSITY



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## $T_e$ flattens in NSTX H-mode shots as $P_b$ increased



- $\chi_e^{PB} \geq 10 m^2/s$  inside  $r/a \leq 0.4$ , while  $\chi_i \sim \chi_i^{NC}$
- Not caused by low-f MHD or fast ion radial distribution
- E-transport correlates with GAE activity (Global shear Alfvén Eigenmode) (*Stutman, et al. PRL'09*)
- Can GAEs induce electron transport? If yes, under what conditions?

NSTX - spherical tokamak,  $B = 0.5 T$ ,  $R/a = 0.86 m/0.65 m$ ,  $P_{NBI} = 6 MW$ ,  
 $\mathcal{E}_{NBI} = 60 - 90 keV$ .

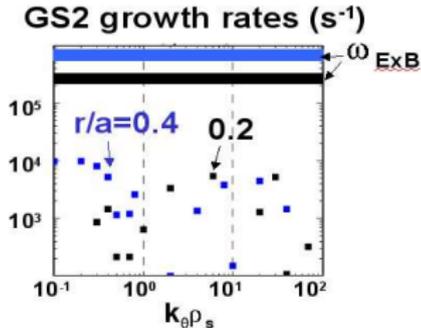
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- 1 Motivations
  - Evidence of electron transport driven by NBI
- 2 Numerical modeling
  - GAE observations and theory
  - ORBIT model for e-transport
  - ORBIT analysis with ideal MHD GAEs
  - Parallel electric field effects
- 3 Discussion and Summary
  - Simulation comparisons with experiments
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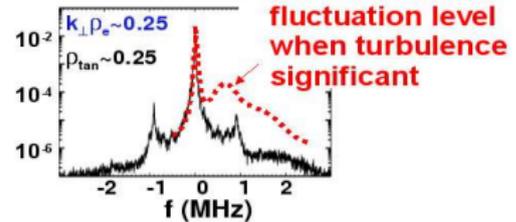
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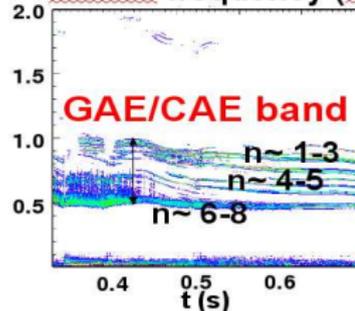
High-k power (a.u.)



- Weak high-k fluctuations
- Persistent 0.5-1.1 MHz GAE/CAEs  
 (Global and Compressional Aliven Eigenmodes)

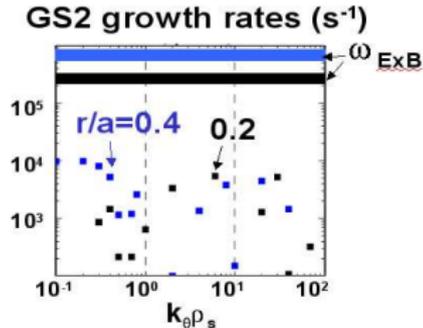
(Gorelenkov et al NF 2003)

Mirnov frequency (Mhz)

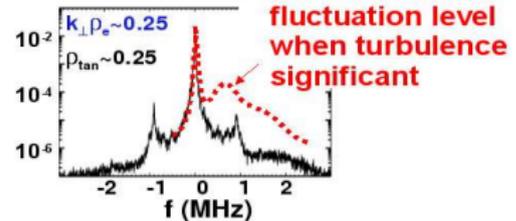


Single GAE induced  $\beta_e$  degradation was observed in W7 and explained (Kolesnichenko, PRL '05).  $E_{\parallel}$  from kinetic AW to GAE coupling is suggested to be responsible for  $\beta_e$  degradation.

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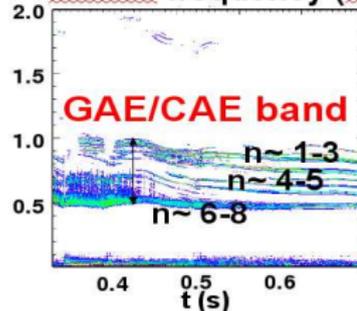
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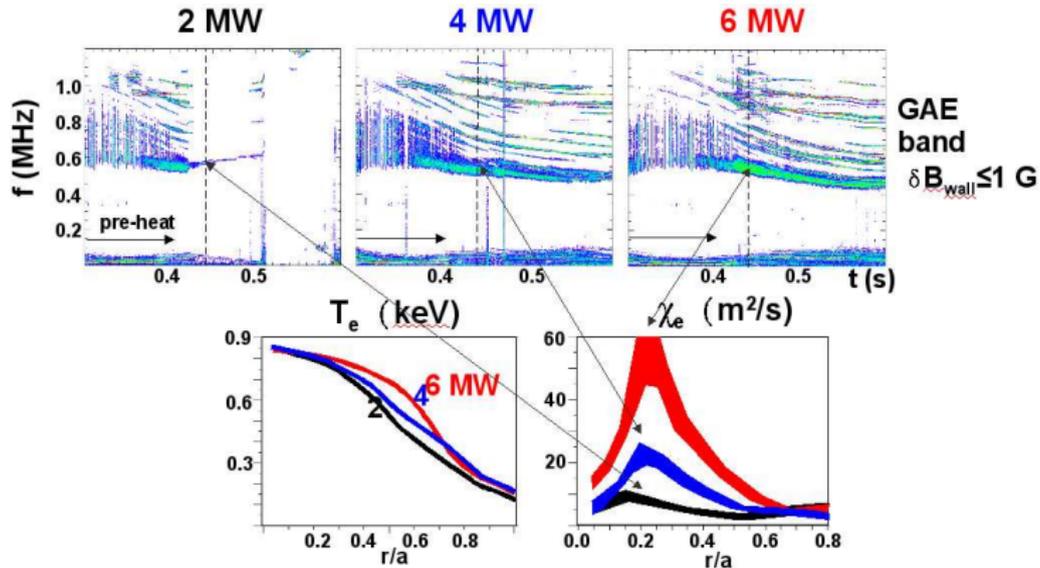
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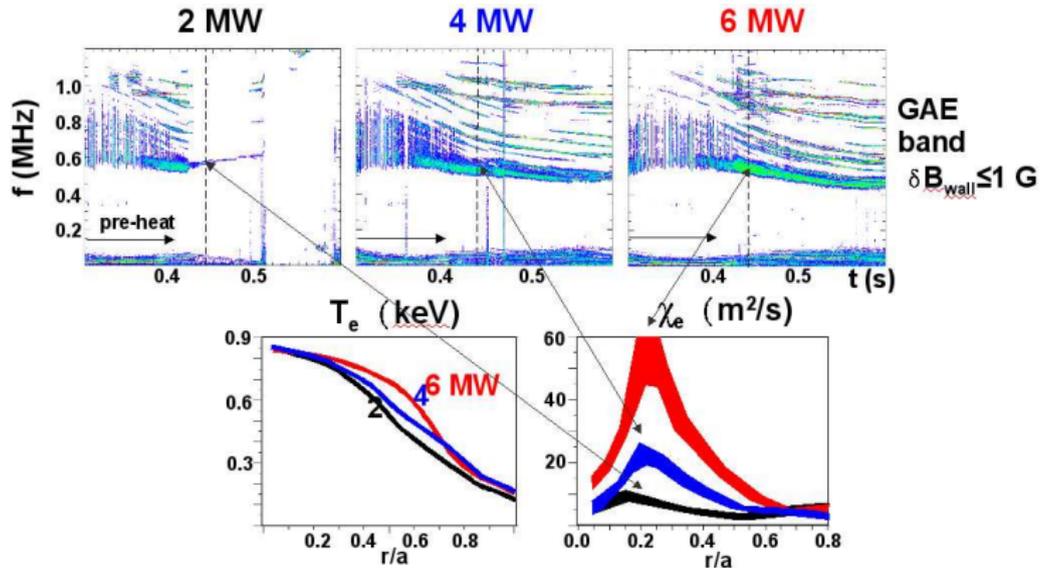
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## $T_e$ flattening (and inferred $\chi_e$ ) correlates with GAE activity



- Plasma & strong GAEs have flat  $T_e(r)$ , high central  $\chi_e > 10 m^2/sec$
- Plasma & weak GAEs have peaked  $T_e(r)$ , low  $\chi_e < 10 m^2/sec$
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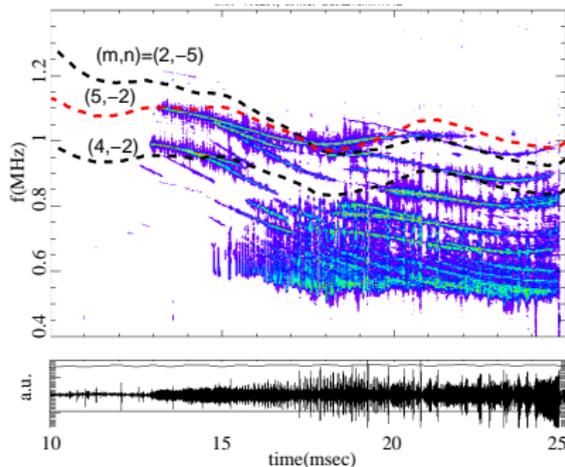


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## High-f GAE (Global shear AEs) instabilities were identified in NSTX



Dashed curves are GAE dispersion  
 $\omega_{GAE} \simeq v_{A0}(m - nq_0)/q_0R$ .

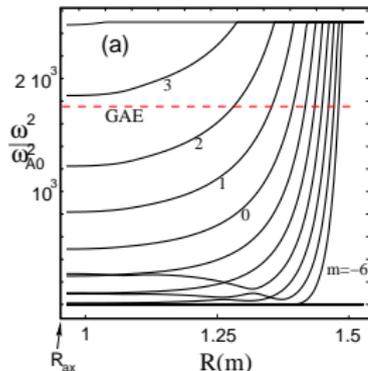
(GAEs reported by Appert, et al., *Pl.Phys.*1982; Mahajan et al. *Phys.Fluids*, 1983;  
 GAEs in NSTX, N.N.Gorelenkov, E. Fredrickson, E. Belova et al., IAEA'02, NF'03).

### GAEs in NSTX:

- observed spectrum peaks of different  $(m, n)$  modes can intersect  $\Rightarrow$  characteristic of shear AEs,
- polarization  $\delta B_{\perp} > \delta B_{\parallel}$ ,
- GAEs are driven by **fast super Alfvénic beam ions**,  $v_b/v_A \simeq 2 - 4$ ,
- multiple modes are often present
- damped on electrons
- at  $\omega < \omega_{ci}$  no interaction with thermal ions expected to affect electrons.

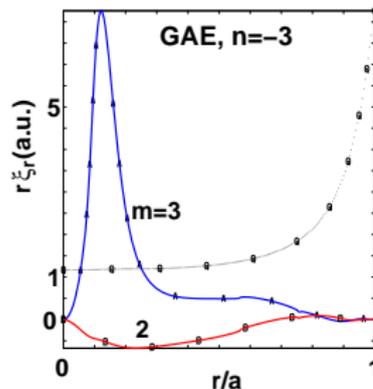
# GAEs have localized structure below each Alfvén continuum (NOVA)

Alfvén continuum



$$\omega_{GAE} \simeq v_{A0}(m - nq_0)/q_0R$$

radial structure



- Many radial modes can exist below each A-continuum line
  - Frequencies are shifted downward from the continuum up to 30%.
- Theory is extended to  $\omega_A(r)$  having minimum at  $r = 0$  (Gorelenkov, NF'03)
  - GAE radial mode width is  $\sim m^{-1}$ , dominant single  $m$  harmonic
- nonlinear hybrid code HYM GAE modeling confirms their experimental identification and theory (Belova, '09)

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## Characteristic frequencies of electron drift motion

- GAE instabilities at  $f_{GAE} \sim 500 - 1000 \text{kHz}$ , but may go higher.
- **transit (passing)** frequency  $f_{te} = \frac{1}{2\pi} \frac{v_{\parallel}}{qR} = 1.5 \text{MHz}$   $T_e = 1 \text{keV}$ ,
- **bounce (trapped)** frequency  $f_{be} = \frac{1}{2\pi} \frac{v_{\perp}}{qR} \sqrt{\frac{r}{2R}} = 430 \text{kHz}$  at  $q = 2$ ,  
 $R = 1 \text{m}$ ,  $a = 0.8 \text{m}$ ,  $r/a = 0.2$ .
- electron Coulomb scattering frequency  $\nu_e / \omega_{ce} = 3 \times 10^{-7}$   
( $\omega_{ce} = 0.7 \times 10^{11} \text{sec}^{-1}$ ), e-i collisions double this.
- thermal ion cyclotron frequency  $f_{ci} = 3 \text{MHz}$ .
- GAEs are driven by Doppler shifted cyclotron resonance of beam ions  $\omega - k_{\parallel} v_{\parallel} - \omega_{cf} = 0$ .

$f_{GAE} \sim f_{be}$  and may be  $\sim f_{te}!!!$

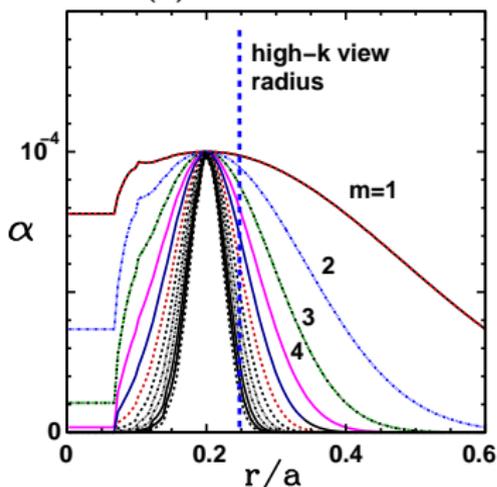
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## Employ ORBIT (White, Ph.Fl.'84) to study e-transport due to GAEs

Ideal MHD perturbation,  $E_{\parallel} = 0$   
 $\alpha(r) : \delta \mathbf{B} = \nabla \times \alpha \mathbf{B}$



Set up test GAE structures

$$\alpha = \alpha_0 e^{-m^2(r-r_0)^2/\delta r^2}$$

and  $\delta B_r/B \simeq ik_{\theta}\alpha = i\alpha m/r$ .

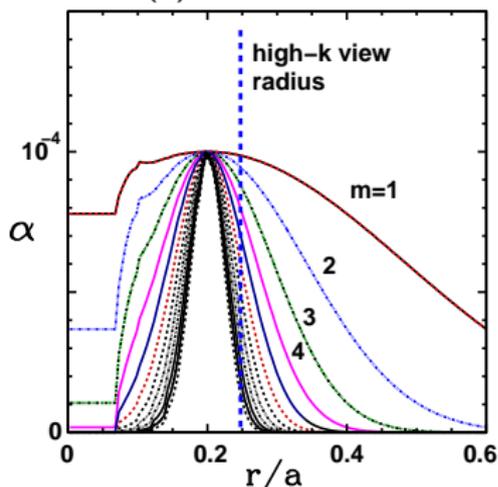
Baseline case:

- $\alpha_0/R = 4 \times 10^{-4} \Rightarrow \delta B_r/B \simeq 0.5 \times 10^{-2}$  at  $r/a = 0.2$  (mode's peak),
- up to 31 GAEs with  $n = 1 - 10$ ,  $m$  is such that  $f = 500 - 1000 \text{ kHz}$  - observed window,
- localization is close to the center - uncertainty in  $q$ -profile exist.

Use ORBIT for the *physics insight* into the driven e-transport

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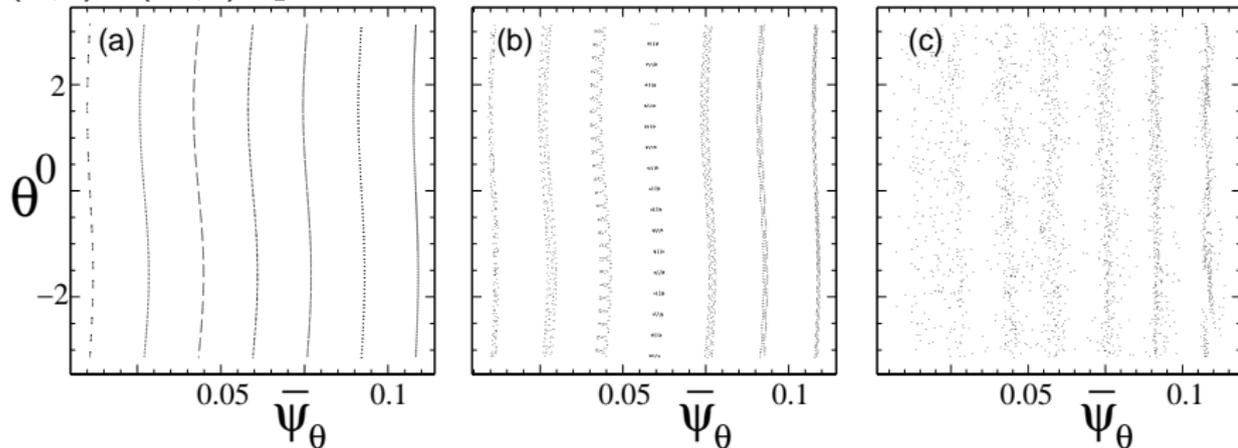
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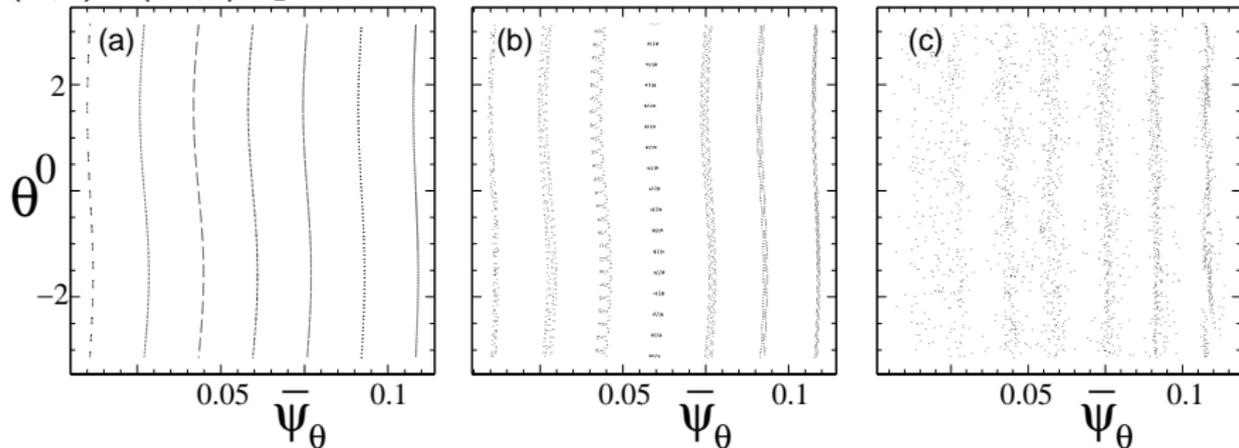
Electron Poincare map in  $\{\psi_p, \theta^0 = \omega t + n\varphi\}$  plane.  
 1 mode,  $\xi_{re} \sim \delta B_r / Bk_{\parallel}$       2 modes ( $f_1 \neq f_2$ )       $N = 20$  modes ( $f_i \neq f_j$ )  
 $(m, n) = (-3, 1); f_1 = 510 \text{ kHz}$



Multiple GAEs ( $> N = 10$ ) introduce stochasticity in electron drift motion  
 $\omega_{dr}$  or  $f_{GAE}$  dephase electron-GAE interaction

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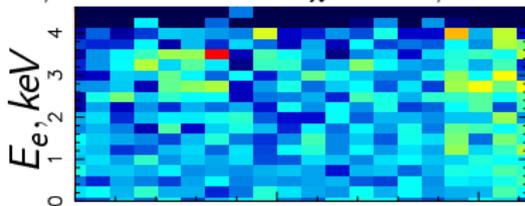


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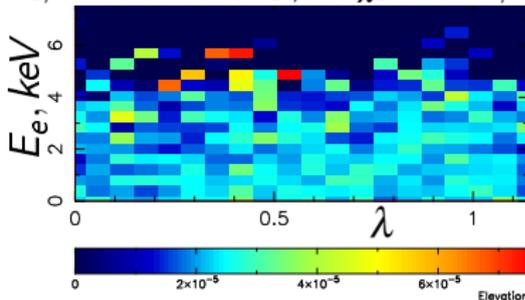
## Strong GAEs smears resonances with electrons

Compare phase space map of local  $\psi$  deviation:  $\left\langle \left| \psi^2 - \langle \psi \rangle_{\mathbf{v}^3}^2 \right| \right\rangle_{\Delta \mathbf{v}^3}$ .

$\alpha_0/R = 10^{-4}$ ,  $v_e = 0$ ,  $\chi_e < 1 m^2/s$



$\alpha_0/R = 4 \times 10^{-4}$ ,  $v_e \neq 0$ ,  $\chi_e \simeq 10 m^2/s$



Take 31 modes,  $\bar{\psi} = 0.05$ ,  $T_e = 1 \text{keV}$   
 $(\lambda = \mu B_0/E)$

### Small amplitude GAEs

- Trapped electrons are effected by GAEs ( $\lambda \simeq 1$ ) in a broad energy range.
- Passing electron can resonate via  $\omega - (k_{\parallel} + l/qR) v_{\parallel} = 0$ . (similar to Kolesnichenko, et.al, PRL'05)
- But  $\chi_e$  is too small  $< 1 m^2/sec$ .

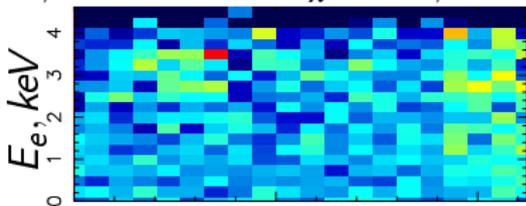
### Strong amplitude GAEs

- Pitch angle broad response to GAEs
- $\chi_e$  is larger  $\sim 10 m^2/sec$ .

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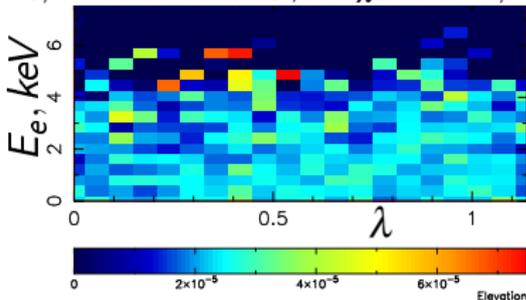


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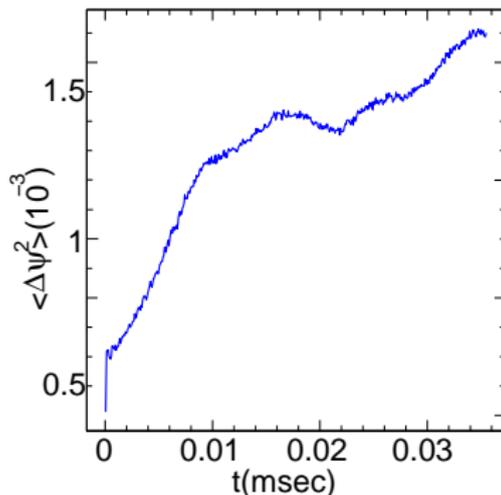
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## Use particle code ORBIT to simulate electron thermal conductivity

Load particles on one surface & Maxwellian isotropic distribution.

Look for linear “diffusive” dependence of  $\langle \psi^2 \rangle_v(t)$  over time

$\Delta t \gg qR/v_{\parallel}, \omega_{GAE}^{-1}, \omega_{dr}$ .



- introduce ambipolar potential

$$F_e = n_e \left( \frac{m_e}{2\pi T_e} \right)^{3/2} e^{-(\mathcal{E} + e\phi)/T_e}$$

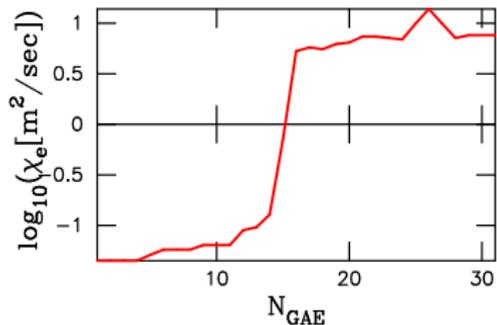
- electrons are attached to ions,  $\Gamma_e = 0$ , but can transfer energy
- $\chi_e$  is on the same order as  $D_e$

$$\frac{\chi_e}{D_e} = \frac{\langle \mathcal{E}^2 D_e \rangle}{T_e^2 \langle D_e \rangle} - \frac{\langle \mathcal{E} D_e \rangle^2}{T_e^2 \langle D_e \rangle^2}$$

- $\chi_e = 3D_e/2$  for weakly perturbed Maxwellian

## How many modes introduce stochasticity?

Baseline case  $v_e/\omega_{ce} = 6 \times 10^{-7}$ ,  $r/a = 0.245$ ,  $\alpha_0/R = 4 \times 10^{-4}$ .



At  $N_{GAE} > 16$  there is a plateau in  $\chi_e(N)$

Construct the random walk:

$$\xi_{re}^2 = \left( \frac{\delta B_r}{k_{\parallel} B} \right)^2.$$

If modes are incoherent characteristic time is smallest of  $v_{coll}^{-1}$ ,  $\tau_{pr}$ ,  $\tau_{transit}/(k_{\parallel} qR)$  (confirmed by numerics).

Then the diffusion is ( $\delta B_r/B = i\alpha m/r$ ,  $k_{\parallel} \simeq 2m/qR$ ,  $m = 3$ ,

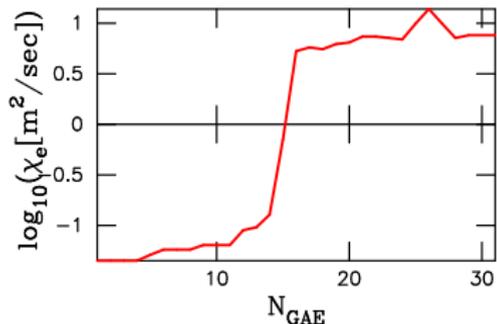
$$\tau_{transit}^{-1} = 1.5 \left( v_{\parallel}/v \right) \text{ MHz}$$

$$\chi_e = \xi_{re}^2 (k_{\parallel} qR) / \tau_{transit} = \frac{\delta B_r^2 qR}{k_{\parallel} B^2} / \tau_{transit} \simeq 25 \frac{v_{\parallel}}{v} \text{ m}^2/\text{s}.$$

This estimate gives  $D \sim \alpha^2$

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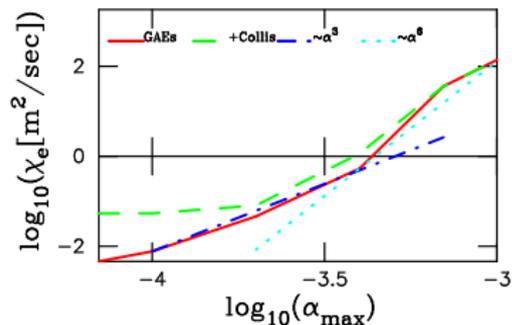
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## *e-transport strongly growth with GAE amplitude*

Baseline case  $v_e/\omega_{ce} = 6 \times 10^{-7}$  at  $r/a = 0.22$ .

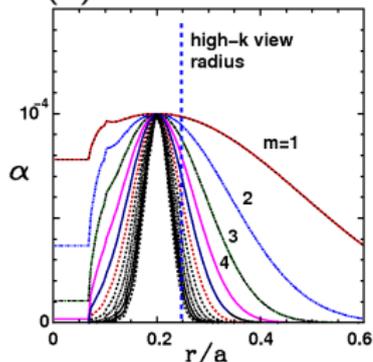


- Small amplitude  $\chi_e \sim \alpha^3$  (deviates from  $\alpha^2$ ).
- Large amplitude  $\chi_e \sim \alpha^6$  introduces intermittently strong e-transport.
- Time averaged amplitude is lower than peak amplitude, which can be above intermittent threshold.

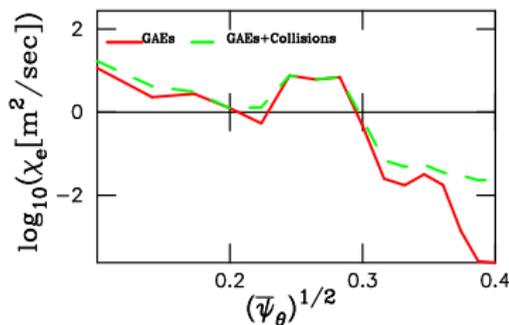
Collisions have small effects at large amplitudes.

## Radial dependence of $\chi_e$

$$\alpha(r) : \delta \mathbf{B} = \nabla \times \alpha \mathbf{B}$$



$$\alpha_0 / R = 4 \times 10^{-4}$$



Peak of  $D(r)$  is near/outside the mode amplitude peak.

Low- $m$  modes contribute more to the diffusion.

From ORBIT  $\chi_e \approx 10 m^2/\text{sec}$  diffusion we need  $\alpha > 4 \times 10^{-4}$  or  $\delta B_r / B > \sim 0.5 \times 10^{-2}$ ,

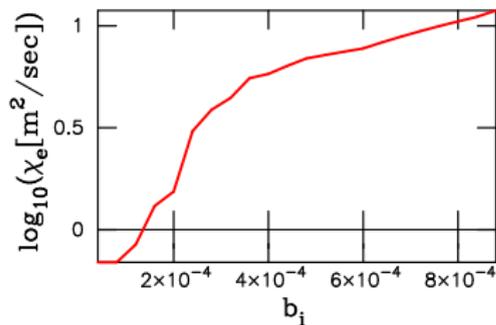
$$\frac{\xi_r}{R} \sim \alpha \frac{m}{k_{\parallel} r} \sim \frac{\alpha}{\varepsilon} \sim 10^{-3} \text{ and } \langle \delta n \rangle / \langle n \rangle \simeq \xi_r / R$$

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## Parallel electric field can strongly enhance $\chi_e$

Baseline case,  $v_e = 0$ ,  $r/a = 0.22$ ,  $\alpha_0/R = 4 \times 10^{-4}$ .



- Ideal MHD GAEs:  $E_{\parallel MHD} = 0$ ,
- Finite  $E_{\parallel} = -\nabla\Psi$  is computed perturbatively via the quasi-neutrality condition due to thermal ion FLR
 
$$\Psi = \phi_{MHD} \frac{b_i}{1 + b_i}, \quad b_i = \frac{k_{\perp}^2 \rho_i^2}{2},$$

$b_i \simeq 0.5 \times 10^{-4}$  in NSTX

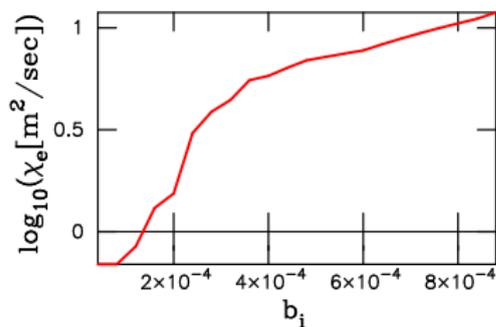
- Other sources of  $E_{\parallel}$ : two fluid effects, compressibility ( $\sim b_i$ ), beam ions:
 
$$\Psi/\phi_{MHD} = O\left(\frac{\omega_{ki,e}}{\omega}, b_i\right) \simeq b_i.$$

$$\chi_e \sim E_{\parallel}^2 \sim b_i^2 \text{ at } b_i < 3 \times 10^{-4}$$

$$\chi_e \sim E_{\parallel} \sim b_i \text{ at } b_i > 3 \times 10^{-4} \text{ as } \tau_{\parallel}^{-1} = (v_{\parallel} + eE_{\parallel} \tau_{transit}/m_e) / 2\pi qR.$$

## Parallel electric field can strongly enhance $\chi_e$

Baseline case,  $v_e = 0$ ,  $r/a = 0.22$ ,  $\alpha_0/R = 4 \times 10^{-4}$ .



- Ideal MHD GAEs:  $E_{\parallel MHD} = 0$ ,
- Finite  $E_{\parallel} = -\nabla\Psi$  is computed perturbatively via the quasi-neutrality condition due to thermal ion FLR
 
$$\Psi = \phi_{MHD} \frac{b_i}{1 + b_i}, \quad b_i = \frac{k_{\perp}^2 \rho_i^2}{2},$$

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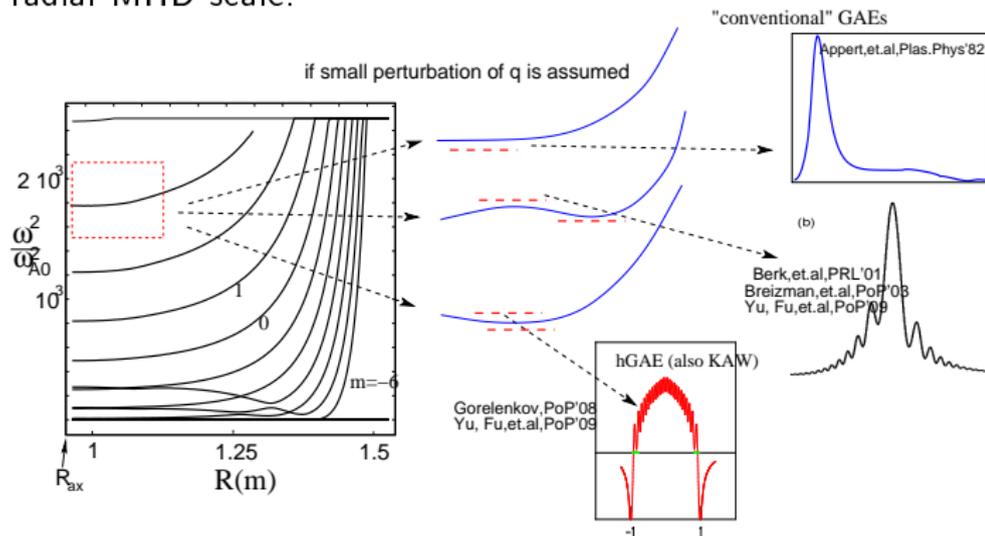
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## *Origin of parallel electric fields*

KAW couples to GAEs if  $\omega > \omega_A$  similar to stellarator GAEs (Kolesnichenko, PRL '05). Can they exist in tokamaks? Interested in long radial MHD scale.

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## Existence condition for GAEs coupled with KAW

Given  $z^2 = (r - r_0)^2 m^2 / r_0^2 S$ ,  $\varepsilon > 0$ ,  $q = q_{min} / (1 - (r - r_0)^2 / w^2)$ ,  
 GAE equation at  $\omega > \omega_A$ :

$$\lambda^{-2} \frac{\partial^4}{\partial z^4} \phi + \frac{\partial}{\partial z} (1 - z^2) \frac{\partial}{\partial z} \phi - S (1 - z^2) \phi + Q \phi = 0$$

Denoting  $\bar{\omega} = \omega R / v_A$ ,  $k_{00} = k_{\parallel} R|_{q=q_{min}}$  (Fu, et.al, PoP'06, Gorelenkov et.al, PPCF'06):

$$S = \frac{mq_{min}w^2}{r_0^2} (\bar{\omega} - |k_{00}|); \quad Q \simeq \frac{w^2}{4r_0^2} \left[ \frac{\alpha^2}{2} - \Delta' \alpha + \alpha \varepsilon \frac{q^2 - 1}{q^2} - \frac{\varepsilon}{2} (\varepsilon + 2\Delta') \right].$$

hGAEs (hybrid, global/kinetic, GAE coupled to KAW) exist with  $\omega > |k_{\parallel}|$   
 is  $Q > 2$  (Gorelenkov, PoP'08 on RSAEs)  $\Rightarrow$  flat  $q$ -profiles,  
 low\_shear,  $w > \sqrt{8}R$ .

Another branch is similar to sweeping up RSAEs if the continuum has a  
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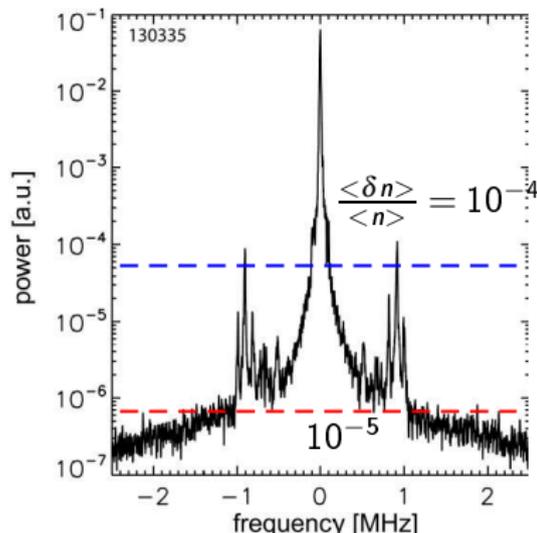
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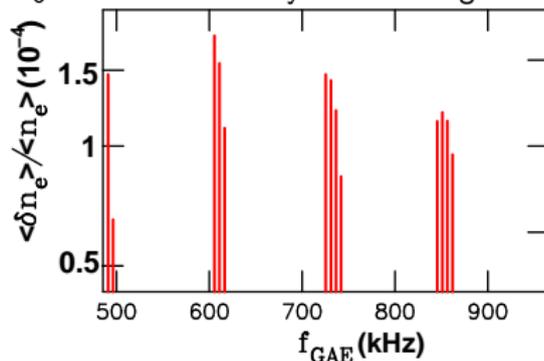
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  - Evidence of electron transport driven by NBI
- 2 Numerical modeling
  - GAE observations and theory
  - ORBIT model for e-transport
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## GAE amplitudes in experiments vs used in the (MHD) model

High-k interferometer line averaged density fluctuation spectrum,  
 $r/a = 0.25$ , 10 msec averaged

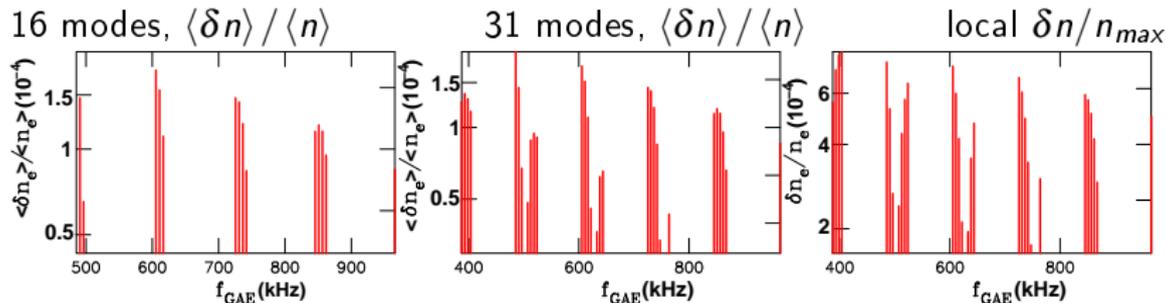


16 modes are shown from simulations  
 $\alpha_0 = 1.5 \times 10^{-4}$ . Synthetic diagnostic.



Test spectrum is different from the high-k interferometer spectrum.  
 Further studies are required to refine the simulations.

## GAE amplitude spectrum in a model



- Local density fluctuation is up to 5 times higher than line averaged.
- Resulting uncertainty can lead into even bigger uncertainty in  $\chi_e$  simulations.
- From ORBIT  $\chi_e \simeq 10 m^2 / \text{sec}$  diffusion we need  $\alpha > 4 \times 10^{-4}$  or  $\delta B_r / B > \sim 0.5 \times 10^{-2}$ ,  $\frac{\xi_r}{R} \sim \alpha \frac{m}{k_{\parallel} r} \sim \frac{\alpha}{\varepsilon} \sim 10^{-3}$  and  $\langle \delta n \rangle / \langle n \rangle \simeq \xi_r / R$ .

This is within the measured accuracy (factor 2 higher) of GAE amplitudes.

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## Qualitatively e-transport due to GAE (other \*AEs?) is expected in ST-like plasma

### Essential elements of the GAE driven electron transport in NSTX

- Strongly driven modes  $\gamma/\omega = 1 - 10\%$ .
- Strong anisotropy: beams, alphas in ST.
- Large ratio  $v_f/v_A = 2 - 4$  (ST typical).
- Weak damping.
- Multiple instabilities,  $N \geq 10$
- /  $\Rightarrow$  high  $\beta_f$  and  $\beta_f/\beta_{pl}$  are required (STs).

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## Summary

- GAEs with sufficiently strong amplitudes can induce electron transport in NSTX.
- Electron transport is due to
  - $\delta B_r/B$  caused deviation from the magnetic surface for both particles
  - multiple modes introduce stochasticity in electron motion.
- overlap of electron radial motion is the mechanism of e-transport.
- comparison with high-k interferometry shows the deficit of the observed GAE amplitudes by factor of 2 to 3 required to match the lower end of the inferred electron thermal conductivity,  $\chi_e = 10 m^2/s$ .
- $E_{\parallel}$  coming from KAW to GAE coupling can strongly enhance radial diffusion. Need to search for  $E_{\parallel}$  effects ( $\rho_i^{-1}$  scales) in experiment.