



U.S. DEPARTMENT OF

ENERGY Science

Core electron thermal transport in NSTX due to orbit stochastization by high frequency Alfvén eigenmodes

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Overview

- Stochastization of e⁻ guiding center orbits by CAEs & GAEs posited to cause thermal transport in ST core
 - CAE/GAE activity correlates with enhanced χ_e in core of H-mode NSTX beam heated plasmas [D. Stutman, PRL 2009; K. Tritz, APS DPP 2010 Invited Talk]
- Early transport simulations with guiding-center code ORBIT promising – need more realistic experimental mode inputs
- Structure and amplitude of CAE & GAE δn measured in beamheated NSTX H-mode ⇒ use for future ORBIT simulation
 - Radial structure & amplitude from inverted reflectometer array data
 - Toroidal mode numbers and frequencies from edge B-dot array
 - Modes identified local dispersion relations
- Simulation of CAEs & GAEs by HYM code compared with experiment ⇒ promise for transport prediction capability
 - substantial validation efforts needed!

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CAEs and GAEs potentially cause significant core electron thermal transport in STs

- Beam-heated spherical torus plasmas feature high frequency Alfvén eigenmodes (AE) (f > ~ 400 kHz): Compressional (CAE) & Global (GAE)
- CAEs & GAEs correlate with enhanced core χ_e in NSTX
- Resonant interaction of multiple modes with e⁻ guiding center orbits proposed to stochastize orbits, enhancing thermal transport



Testing hypothesis requires comparison of experimental transport with realistic orbit simulation

 Early transport simulations with guiding-center code ORBIT consistent with hypothesis

[N. N. Gorelenkov et al., NF 2010; K. Tritz, APS DPP meeting 2012; N. A. Crocker et al., NF 2013]

- assumed mode structures (e.g. Gaussian radial structure)
- amplitudes from interferometer & simplified analysis of reflectometer measurements
- More realistic representation of modes needed for more stringent test
 - Toroidally distributed Mirnov array: experimental spectrum with measured frequencies & mode numbers
 - δn mode structure & amplitude from inversion of reflectometer array measurements
 - Mode polarization (shear/GAE or compressional/CAE) from Mirnov & reflectometer measurements + local dispersion relations

Structure and amplitude of CAE & GAE δn measured in high performance plasma

- High frequency AEs observed in 6 MW beam-heated H-mode plasma
- High frequency AE structure
 measured with reflectometer array
- Toroidal mode numbers (n) and frequencies (f) determined using edge B-dot array
- Modes identified using:

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- measured mode structures, f & n
- local dispersion relations: CAE (compressional Alfvén): $\omega^2 = k^2 V_A^2$ GAE (shear Alfvén): $\omega^2 = k_{\parallel}^2 V_A^2$





56th APS DPP, New Orleans, LA – Core electron therm. Transp. in NSTX due to orbit stochast. by high freq. AEs, N. Crocker (10/29/2014)

Structure and amplitude of CAE & GAE δn measured in high performance plasma



- Observed modes identified as:
 - GAEs: *f* < ~ 600 *kHz*, *n* = −6 − −8
 - CAEs: $f > \sim 600 \text{ kHz}$, n = -3 -5
- GAEs and CAEs have distinct δn structural differences
 - Edge: GAE $\delta n > CAE \delta n$
 - Core: CAE δn > GAE δn

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- CAES: strongly peak toward core
- GAES: broad structure, peaking toward core;

large edge peaks \Rightarrow edge displacement + large $|\nabla n_a|$



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CAE+GAE simulation shows promise for first principles transport prediction

- Hybrid MHD (HYM) code simulates CAE structure and stability
 - 3D, coupled MHD fluid & fully kinetic fast-ions
 - realistic equilibrium

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 Simulation & experiment compared for beam heated H-mode plasma



- most unstable CAEs and GAEs have similar frequencies and mode numbers to observed experimental spectrum [see E. Belova YI1.6]
- GAEs structures compared: similar broad structures & strong edge peaking
- predictive capability for CAEs & GAEs + transport simulation
 - ⇒ predictive capability for core electron thermal transport
 - substantial model validation efforts required!

Measurement Technique

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Toroidal mode numbers and frequencies determined using edge B-dot array

- Modes appear as peaks in δb spectrum
- *n* determined from δb measured by edge toroidal array of B-dot coils



– method: find *n* that minimizes χ^2 :

$$\chi^{2} \equiv 1 - \left| \sum_{\forall \phi} \delta b e^{-in\phi} \right|^{2} / \left(N_{\phi} \sum_{\forall \phi} |\delta b|^{2} \right)$$

 N_{ϕ} =10 is number of coils.

 Smallest coil spacing is 10° ⇒ can distinguish |n| ≤ 18

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Reflectometers provide radial array of measurements

NSTX cross-section



30-50 GHz -

55-75 GHz (not shown: horns modified to optimize for frequency range)

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Two arrays: "Q-band" & "V-band"

-Q-band: 30, 32.5, 35, 37.5, 42.5, 45, 47.5 & 50 GHz -V-band: 55, 57.5, 60, 62.5, 67.5, 70, 72.5 & 75 GHz

- Arrays closely spaced (separated ~ 10° toroidal)
- Single launch and receive horn for each array
- Horns oriented perpendicular to flux surfaces ⇒ frequency array = radial array
- Cutoffs span large radial range in high density plasmas ($n_0 \sim 1 7 \ge 10^{19} \text{ m}^{-3}$)

Launch and Receive Horns



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Reflectometers measure local density fluctuation in plasma

- Microwaves propagate to "cutoff" layer, where density high enough for reflection ($\omega_p = \omega$) Microwave ("O-mode") propagation
 - Dispersion relation of "ordinary mode" microwaves: $\omega^2 = \omega_p^2 + c^2 k^2$, ω_p^2 proportional to density $(\omega_p^2 = e^2 n/\varepsilon_0 m_e)$
 - $k \rightarrow 0$ as $\omega \rightarrow \omega_p$, microwaves reflect at k = 0

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- phase between reflected and launched waves changes ($\delta\phi$)

• Wave propagation controlled by density – $\delta\phi$ depends on δn



δn determined from reflectometer measurements using synthetic diagnostic

- Synthetic diagnostic used to model reflectometer response (ξ) to δn
 - WKB path length (L) approximation:

$$L = L_0 + \xi = \int_{edge}^{\omega_P^2(R) = \omega^2} \sqrt{1 - \omega_P^2(R) / \omega^2} dR$$
$$\omega_P^2 = \omega_{P0}^2 + \delta \omega_P^2 \propto n_0 + \delta n$$

- Perturbation modeled with cutoff displacement (d_c) :
 - $-\delta\omega_{\rm P}^2 \propto \delta n(R) = \sum_i a_i d_{C,i}(R) \nabla n_0(R)$
 - Find a_i to minimize $\chi^2 = \sum_i (\xi_{i,meas} - \xi_{i,fit}) / \sigma^2_{i,meas}$

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• Fit sensitive to noise in ξ_{meas} gradient \Rightarrow smoothed $\xi_{i,meas}$ used for inversion



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Summary

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- CAE & GAE δn have distinct structural differences in beamheated NSTX H-mode
 - Radial structure & amplitude from inverted reflectometer array data
 - Toroidal mode numbers and frequencies from edge B-dot array
 - Modes identified local dispersion relations
- Future work: measurements will be used in ORBIT simulation for comparison with experimental transport
- HYM simulation of CAEs and GAEs compared
 - Unstable mode numbers and frequencies similar to experiment

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GAEs have similar structures

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