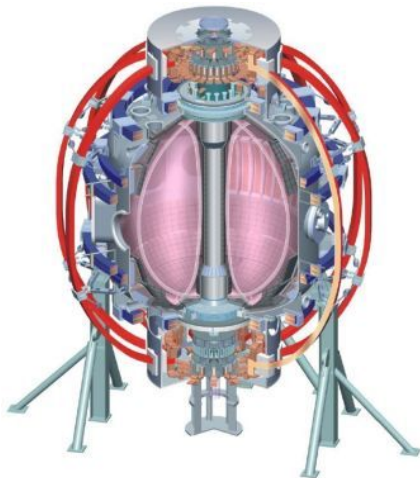


# Experimental Study of Kink-like Modes in NSTX Plasmas

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# Introduction

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**Wave number spectrum from the Mirnov coils**

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**Effective mode growth rate and real frequency**

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**Stability trend with thermal plasma and fast ion parameters**

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**Conclusions and Future work**

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# Outline

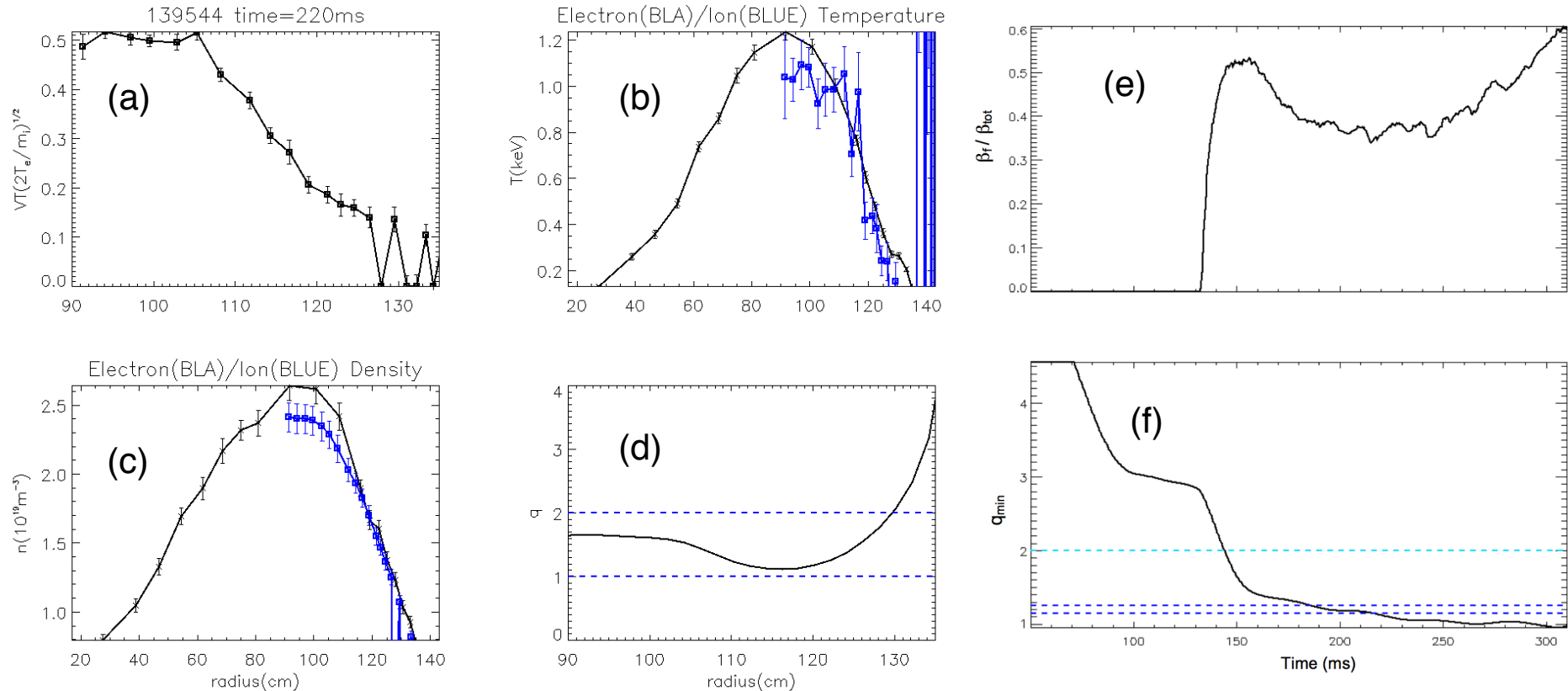
- Introduction
  - Motivations
  - National Spherical Torus Experiment (NSTX) plasma properties in the kink-like mode studies
- Non-resonant kink (NRK) and fishbone dynamics
  - Wave number spectrum from the Mirnov coils
  - Effective mode growth rate and real frequency
  - Relationship with thermal plasma and fast ion parameters
- Conclusions and future work

# Introduction- Motivation

- Internal Kink modes destabilized by energetic particles can cause particle losses and deteriorate plasma performance in toroidal fusion devices.
- NSTX primarily uses neutral beam injection (NBI) for heating and current drive, thus introducing a large super-Alfvenic fast ion population into the plasma<sup>[3]</sup>. The precessional<sup>[4]</sup> and bounce<sup>[5]</sup> resonance of the fast ions with internal kink-like modes<sup>[6]</sup> provides drive for the fishbone modes, and the consequential fast ion transport can significantly affect plasma  $\beta$  ( $= 8\pi nT/B^2$ ).
- Detailed characterization of the kink-like instabilities in NSTX plasmas can provide reference for validation and benchmark for theoretical<sup>[9]</sup> and numerical<sup>[10],[11]</sup> studies.

# Introduction- NSTX plasma properties

- $B_T \sim 0.4$  T,  $n_e \sim 3 \times 10^{19} m^{-3}$ ,  $T_e \sim T_i \sim 1.5$  keV. The flux surfaces are re-constructed using LRDFIT, constrained by Thomson Scattering (TS), charge-exchange recombination spectroscopy (CHERS) and MSE measurements.

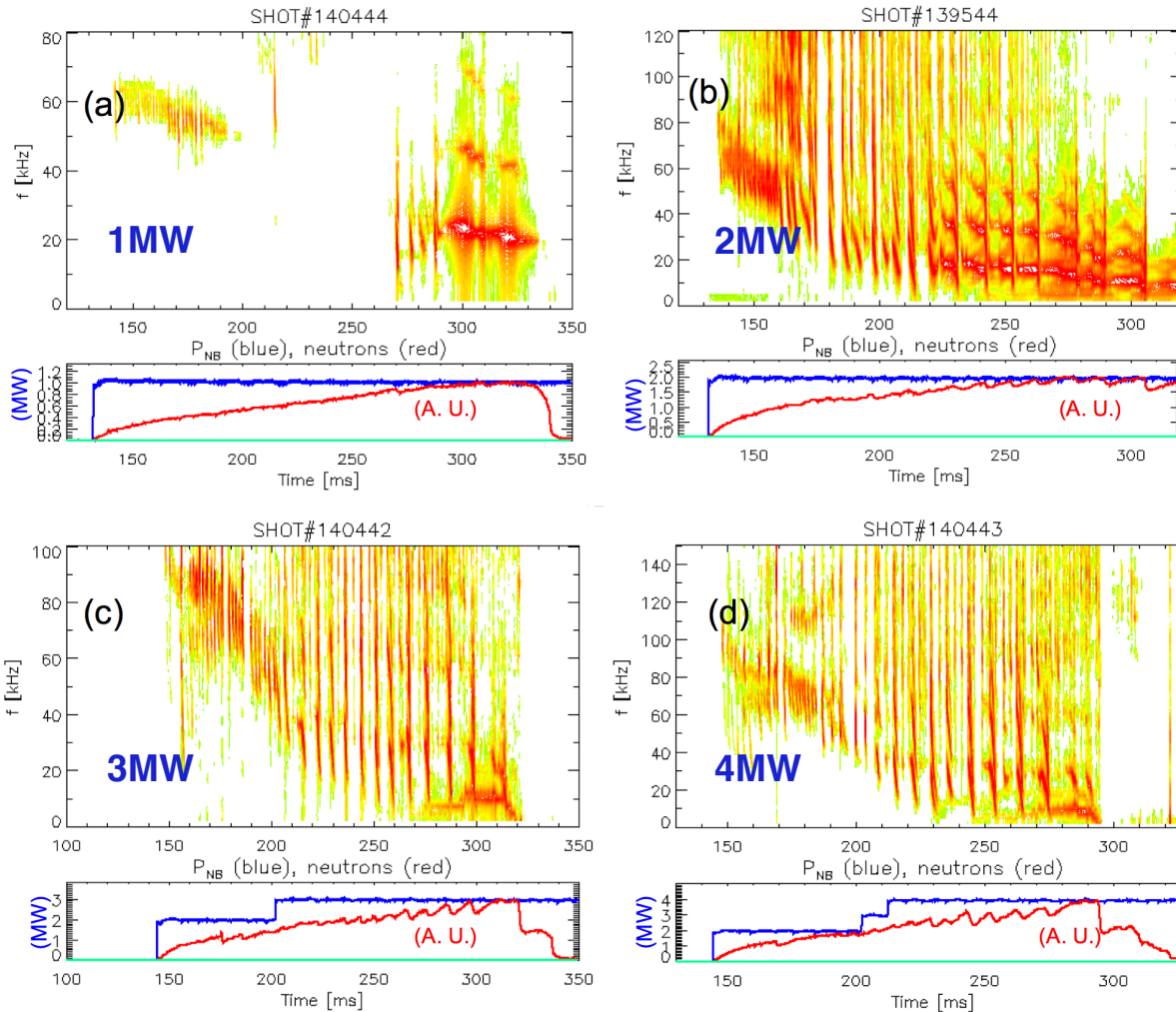


• Experimental rotation (a), temperature (b), density (c) and  $q$  (d) profile for shot # 139544 at 200 ms.

• Time evolution of  $\beta_r$  (e) and minimum  $q$  (f) from TRANSP simulation results for shot # 139544.

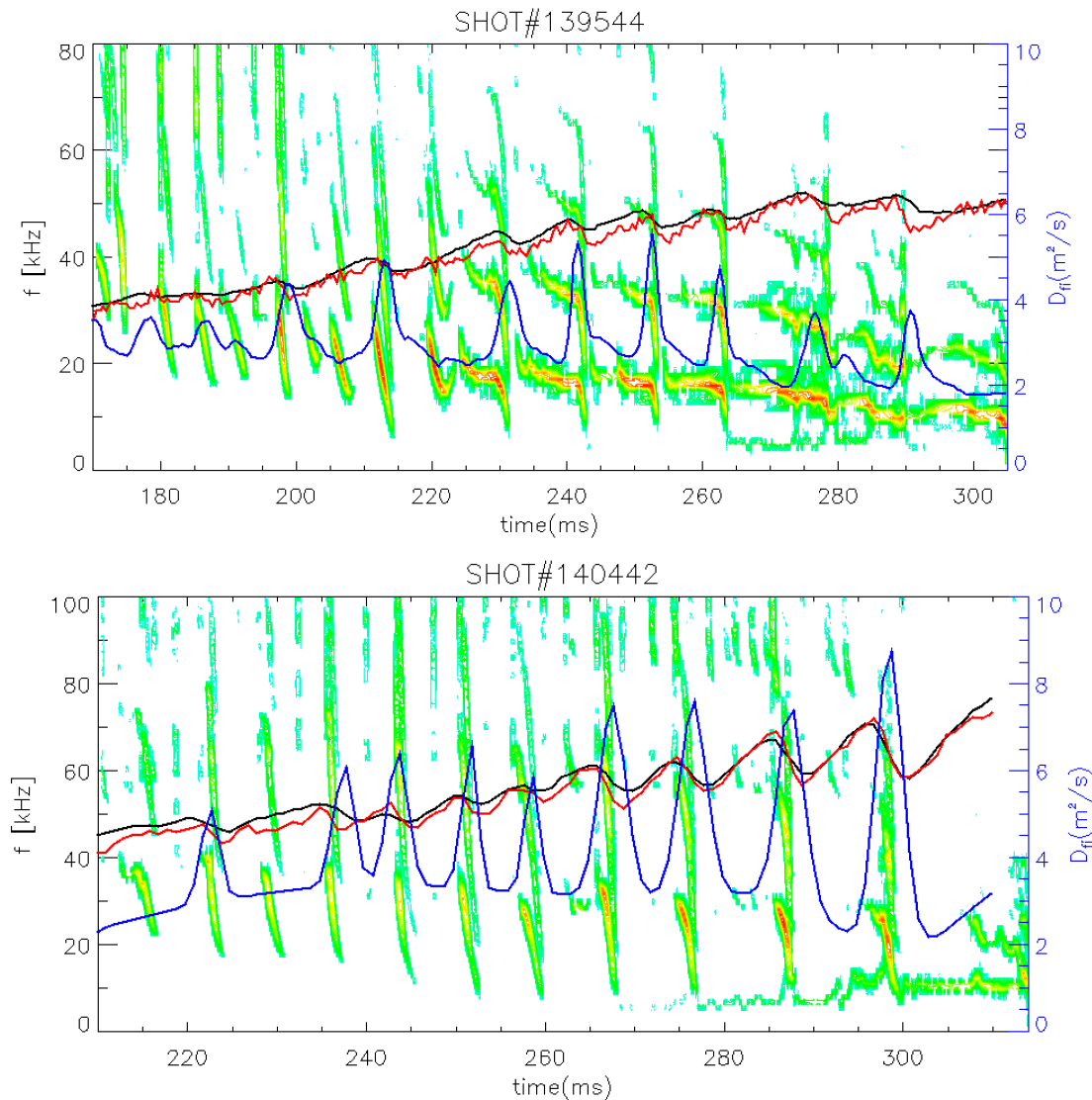
# Transition from fishbones to Non-Resonant Kink (NRK) are observed in shots with different $P_{NB}$

- Fishbone and NRK are analyzed in shots with different scenarios and NB power. Transitions from fishbones to NRK are observed.



• Spectrograms of magnetic fluctuations in shot # 140444 (a), 139544(b), 140442(c) and 140443(d), with NB power 1MW, 2MW, 3MW and 4MW, respectively.

# Bursting modes correlate with large fast ion transport events, as deduced by drops in neutron rate



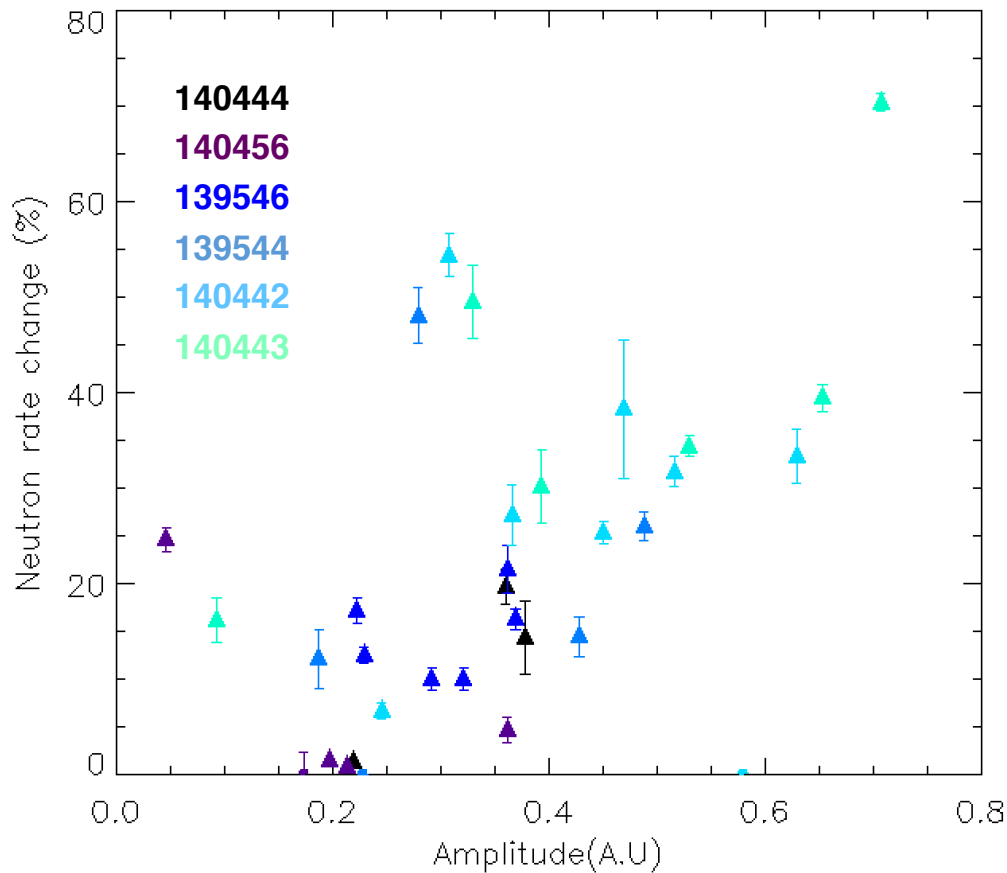
- The fast ion dynamics is simulated using TRANSP, with imposed fast ion diffusivity to match the measured neutron rates.
- Fishbone bursts correspond to large fast ion transport events, with measured neutron rate drops up to around 50%.

— Imposed diffusivity  
— Measured neutron rate  
— Simulated neutron rate

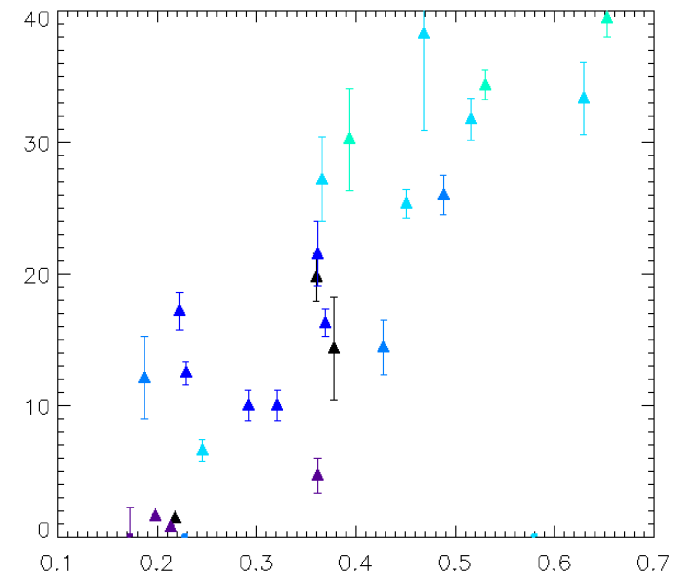
•TRANSP simulation results and spectrogram for shot # 139544 and 140442



# Fast ion transport has an increasing trend with the bursting mode amplitude



- Relationship between neutron rate change and mode amplitude for bursting events. Colors represent different shots.
- The bursting modes amplitude is measured from the Mirnov coil signals.



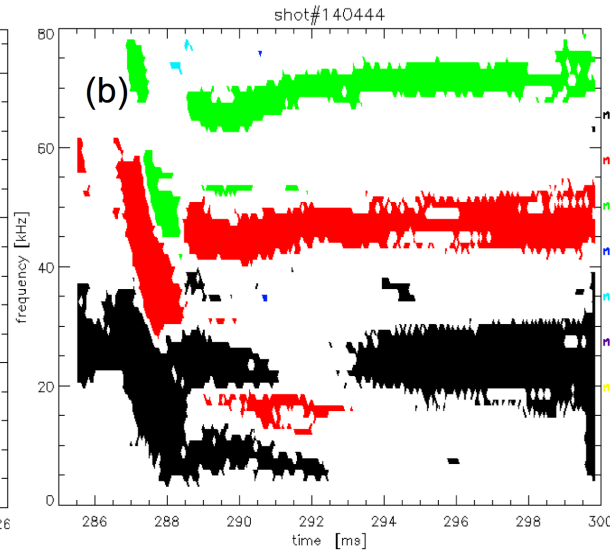
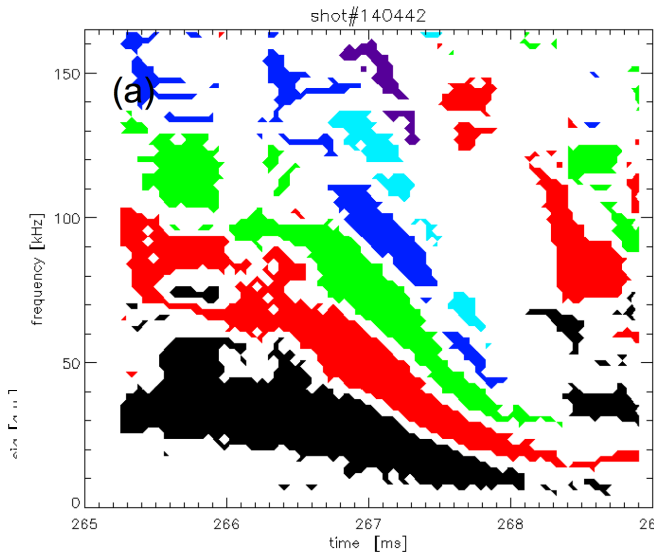
•Cropped figure for neutron rate decrease from 0-40 percent, and for mode amplitude from 0.1-0.7.

- The neutron rate decreases correlates well with the mode amplitudes, especially for the central range of both parameter (cropped figure).
- This implies that the fast ion transport rate might has a strong dependence on mode amplitude.

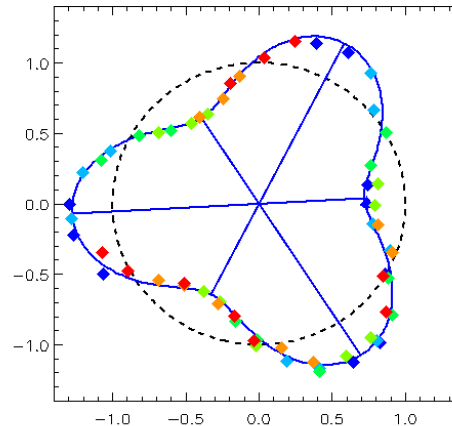
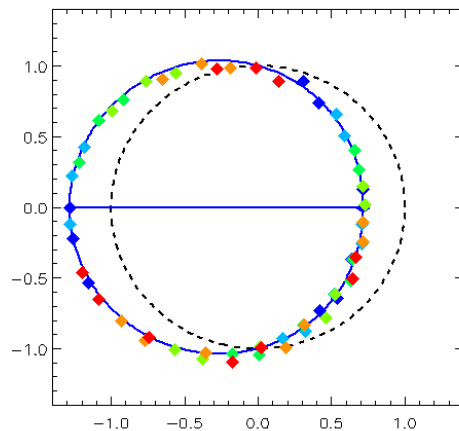


# Bursting modes and long-lived modes are identified as fishbones and NRKs

- The bursting modes with lifetime  $\sim 2$  ms and chirping frequency  $\delta f \sim 10$  kHz are identified as fishbone oscillations (a). The long-lived modes with lifetime  $\geq 10$  ms appearing near the end of the discharges are identified as kink modes (b).

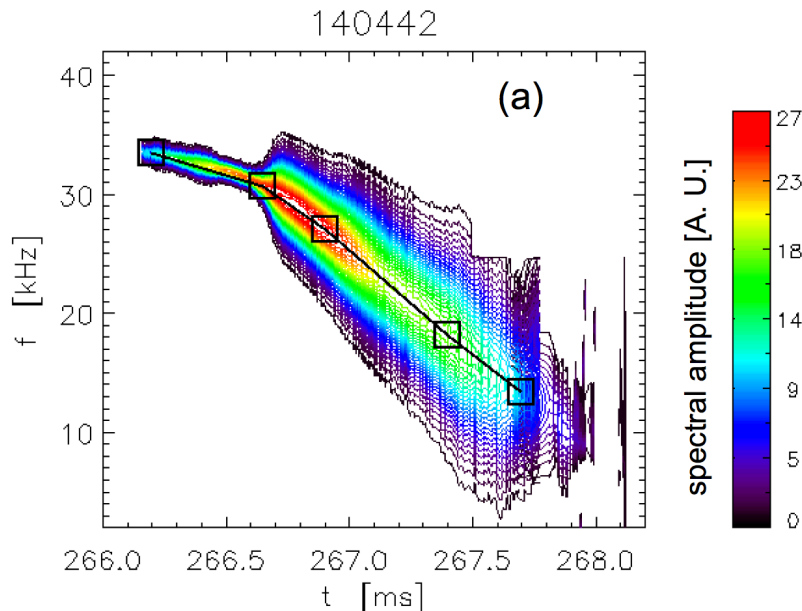


- Spectrogram of Mirnov coil signal with toroidal mode number during  $\sim 267$  ms in shot # 140442 (a), and during  $\sim 295$  ms in shot # 140444 (b)

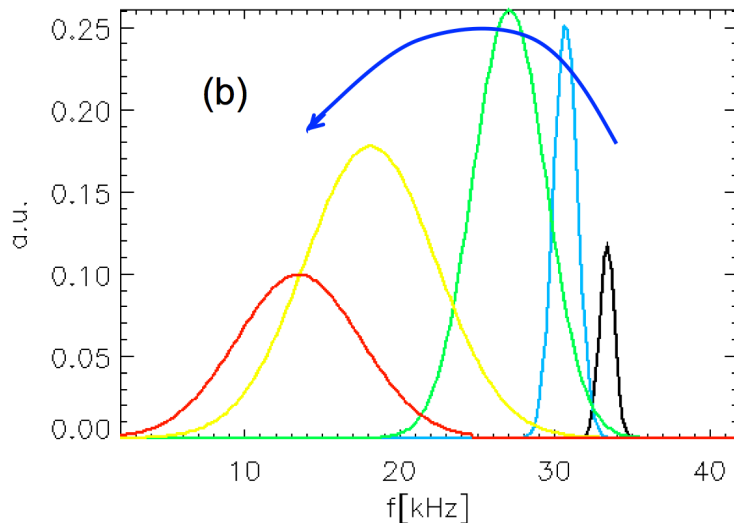


- Polar plot of the mode amplitude versus coil sensor toroidal angle fitted with a sinusoid. Data refer to the  $n = 1, 3$  fishbone harmonic at  $t = 267$  ms in shot # 140442.

# Details in fishbone frequency chirping



- The fishbone modes generally have a chirping frequency from  $\sim 30$  kHz to  $\sim 15$  kHz in the lab frame for the dominant  $n=1$ ,  $m=1$  harmonic.
- The spectrum also become broader as the frequency drops (b). This pattern repeats itself with a interval also on the time scale of  $\sim 5$  ms.



• **Details of the  $n=1$  harmonic in the chirping fishbone mode. The black squares in (a) indicate time points where the spectrum is plotted in (b).**

# Effective mode growth rate and real frequency

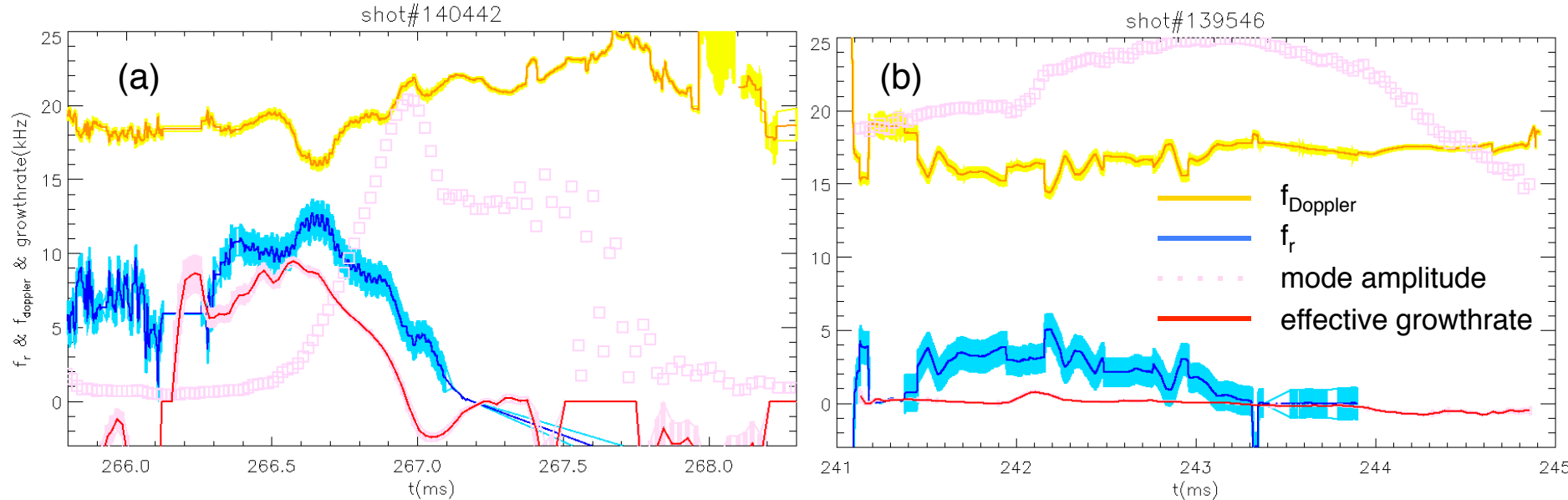
- The frequency separations between peaks with consecutive  $n$ 's are almost constant, for both fishbones and NRKs, implying different harmonics of the mode have a same real frequency on top of the Doppler shift caused by toroidal rotation<sup>[3]</sup>, i. e.

$$f_{lab,n}^{mode} = f_r^{mode} + n f_{Doppler}$$

- Linear fit can be done for the instability events in the spectrum time evolution to extract  $f_r^{mode}$  and  $f_{Doppler}$ .
- Effective growthrate is calculated by exponential fit to the mode amplitude evolution

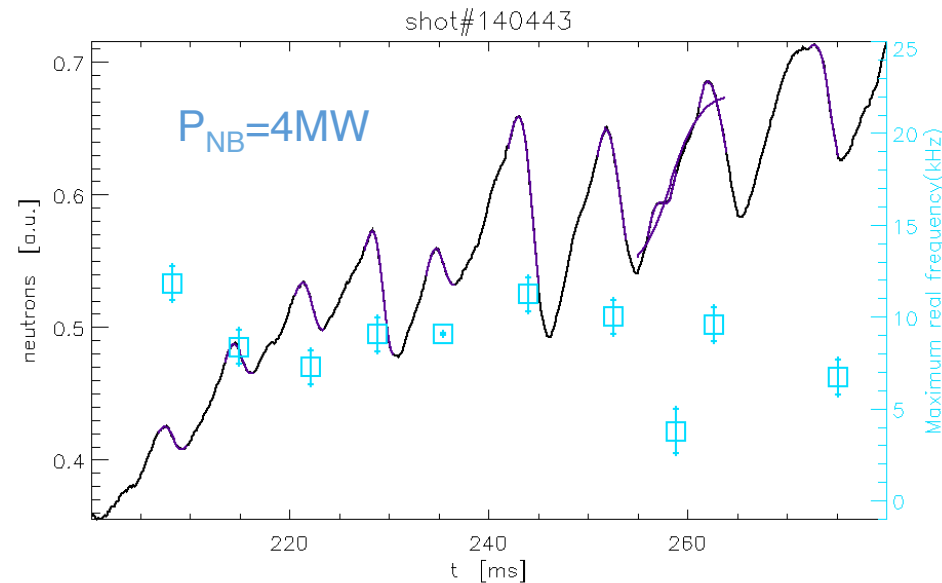
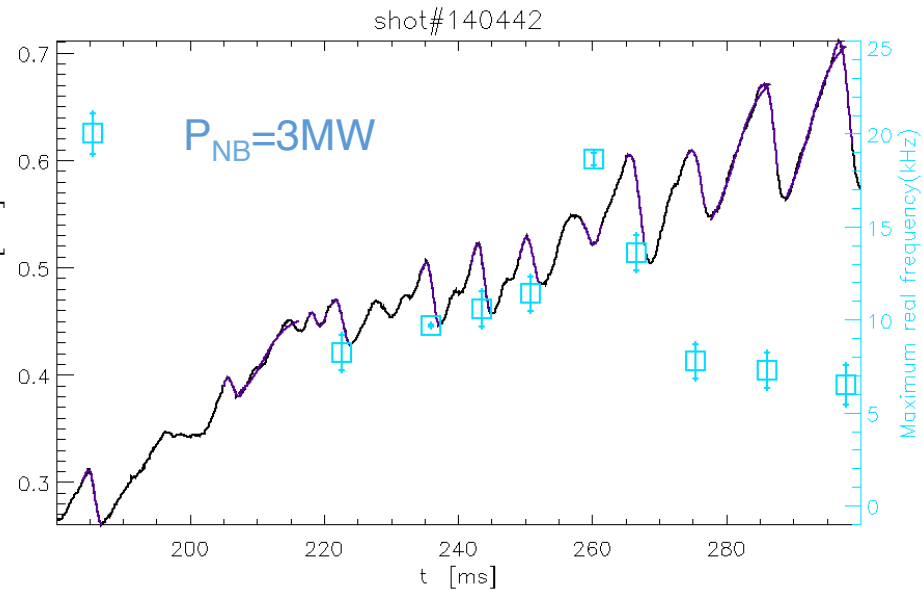
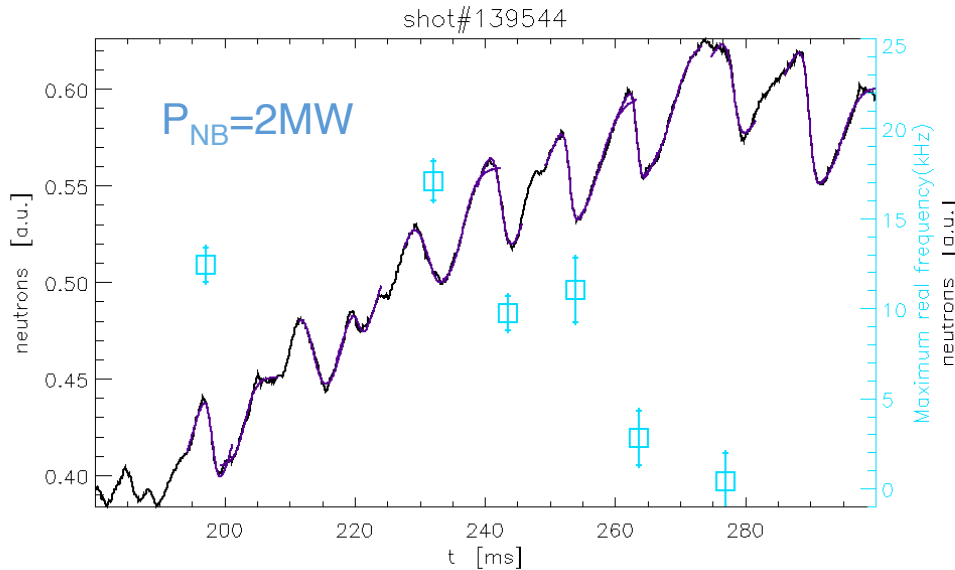
# Real frequency and effective growthrate evolution are distinctive of each type of instability (fishbone, NRK)

- Time evolution of various parameters during one fishbone(a) and kink (b) event.



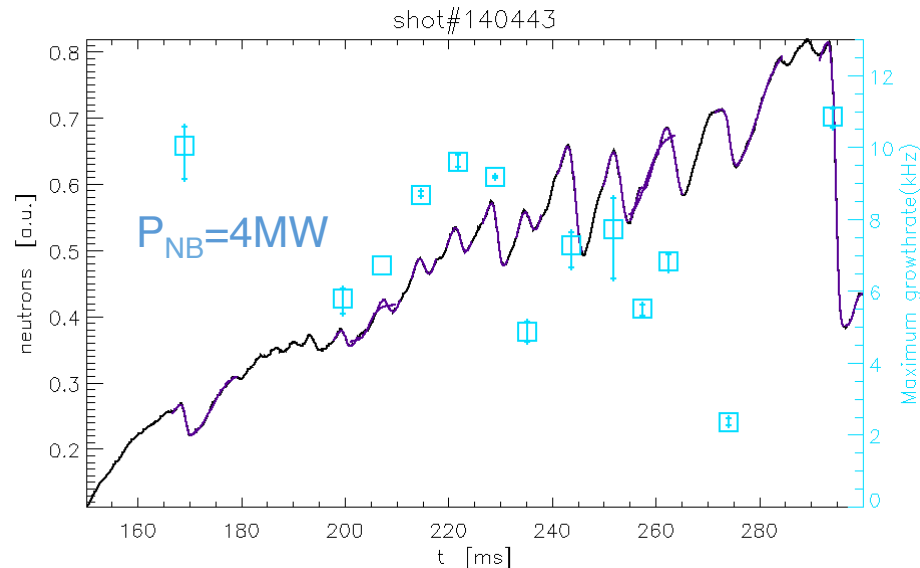
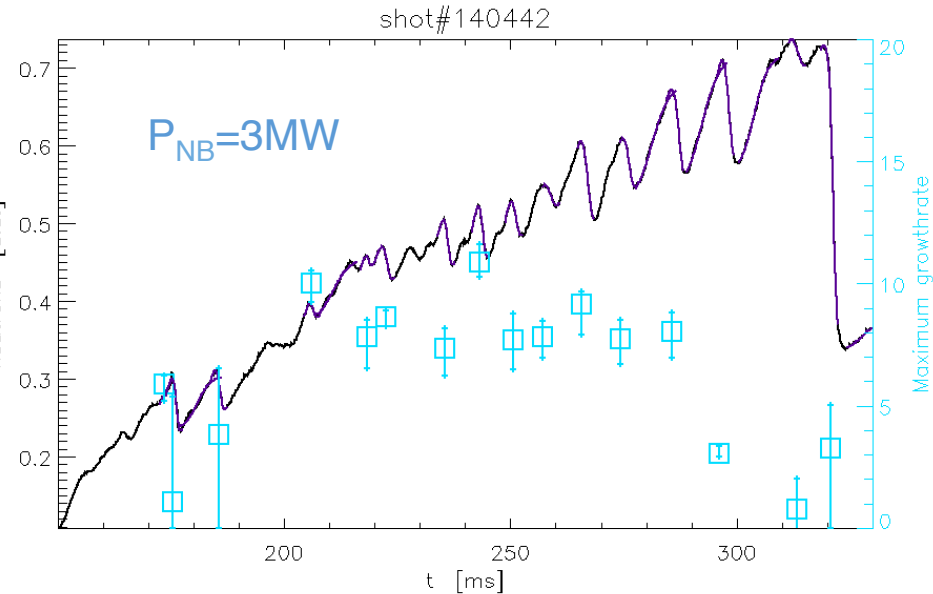
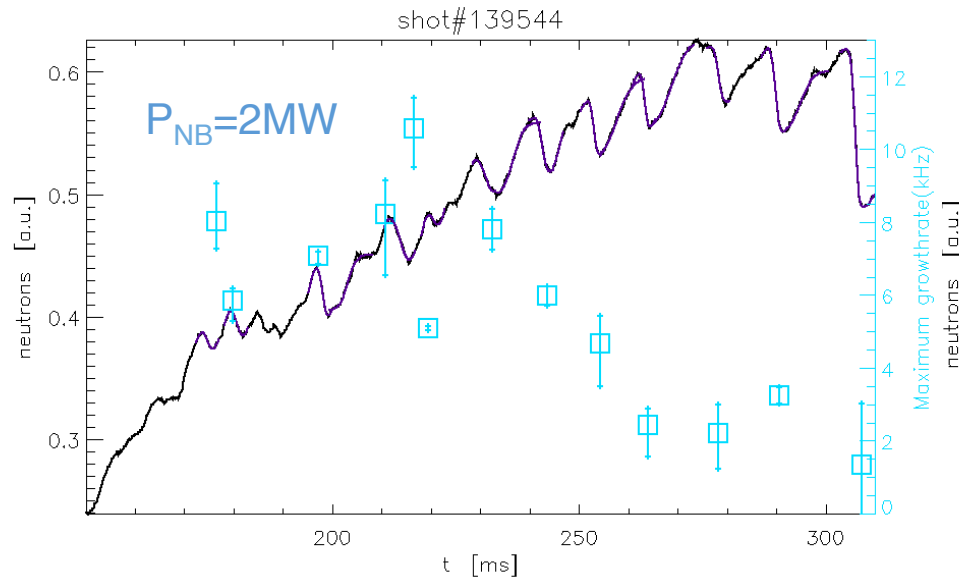
- For the fishbone mode, the real frequency drops from  $\sim 15$  kHz to 0, indicating a strong interaction with the fast ions.
- For the NRK mode, the real frequency stays almost 0, implying its ideal MHD nature. The Doppler shift frequency is of the same order of magnitude at  $\sim 18$  kHz.
- The shadow area indicate error bars for the linear fit.

# Real frequency decreases for lower $P_{NB}$ shots as the NRK regime is approached



- For each bursting fishbone event, this analysis gives a maximum mode real frequency and growthrate.
- For lower NB power shots, the mode real frequency decreases as the plasma is closer to NRK regime .

# Effective mode growthrate decreases for lower and higher $P_{NB}$ shots as the NRK regime is approached



- The maximum growthrate exhibits a decreasing trend towards the NRK regime for the discharges with NB power from 2-4 MW.

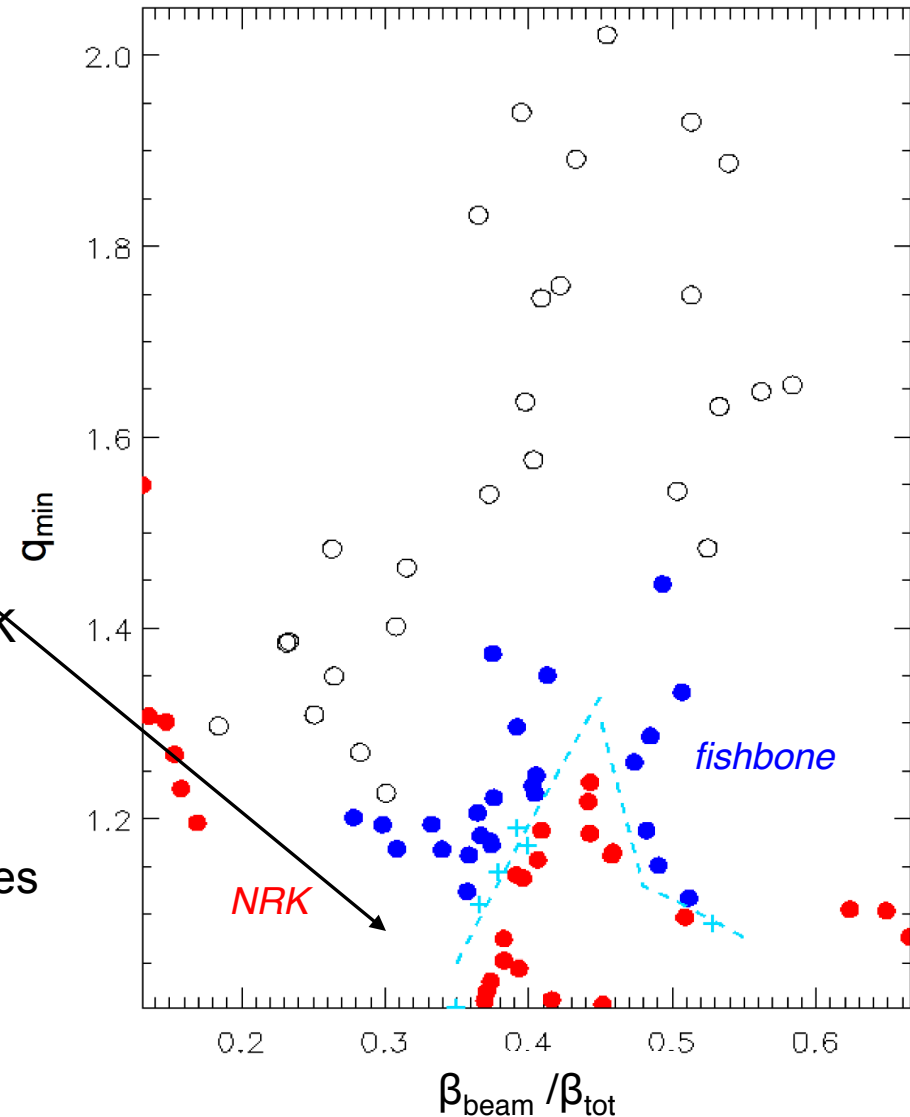
# Kink-like modes are unstable below $q_{\min} \sim 1.5$

Trends of fishbone and kink stability with selected parameters (e.g.  $\beta$ ,  $q_{\min}$ ) can be found from this database.

## Fishbone and NRK stability diagram in

### $\beta_{\text{beam}}/\beta_{\text{tot}}$ - $q_{\min}$ space

- Blue dots represent fishbone events
  - Red dots represent NRK events
  - Black circles represent no instability below 40kHz.
  - Light blue crosses represent mode transition from fishbone to NRK in different shots
- The mode could be marginal between NRK and fishbone near the transition point.
  - Above  $q_{\min} = 1.55$ , no mode is observed.
  - NRKs appear at low  $\beta_{\text{beam}}/\beta_{\text{tot}}$  values.
  - The regime around  $\beta_{\text{beam}}/\beta_{\text{tot}} \sim 0.4$  becomes most NRK unstable.
  - The fishbone events become unstable at  $\beta_{\text{beam}}/\beta_{\text{tot}} \sim 0.25$ .





# Stability diagram in different parameter spaces indicate fishbone and NRK dependence on $\beta_{\text{beam}}$

## Fishbone and kink activity diagrams in different quantity space

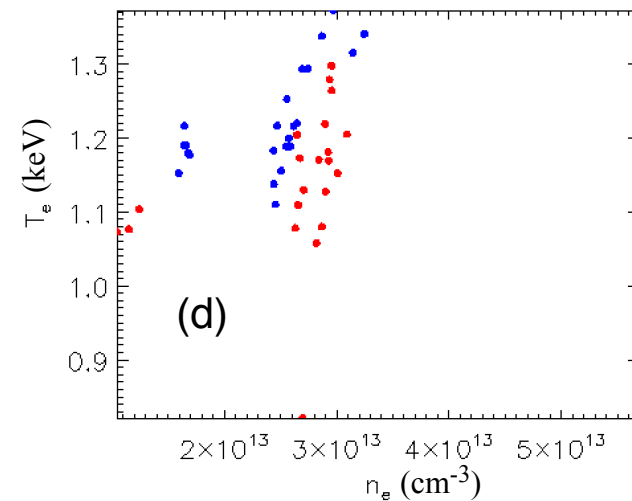
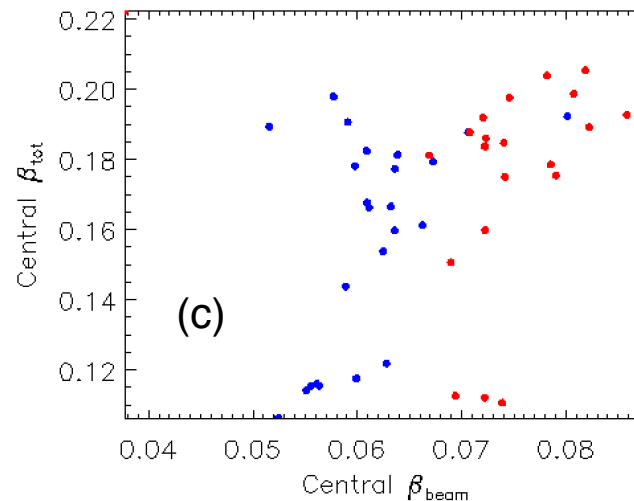
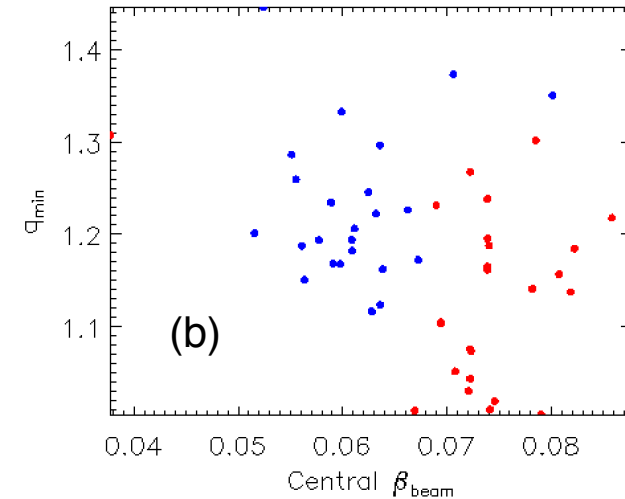
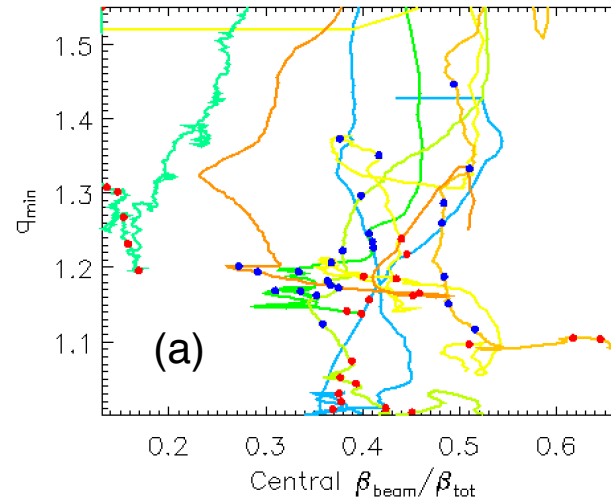
Colored lines in (a) represent time history of  $q_{\text{min}}$  and  $\beta_{\text{beam}}/\beta_{\text{tot}}$  in different shots

(a) The time evolutions of the two quantities in various shots do not have a clear trend, indicating no hidden dependence of the mode stabilities on time.

(b) The NRK is mostly unstable at higher  $\beta_{\text{beam}}$  and lower  $q_{\text{min}}$ , and the fishbones are mostly unstable at lower  $\beta_{\text{beam}}$  and higher  $q_{\text{min}}$  in the parameter regime the data base scans

(c) The instabilities depend on  $\beta_{\text{tot}}$  weakly

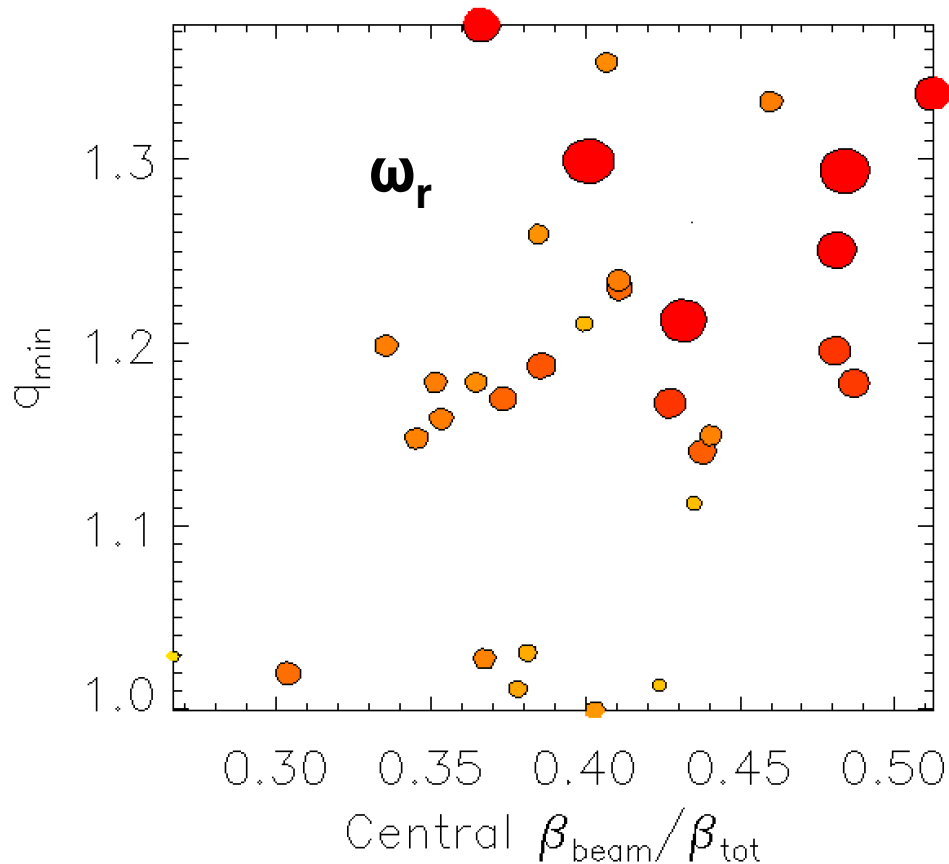
(d)  $T_e$  and  $n_e$  range is  $\sim(1,1.4)\text{keV}$  and  $(1,4)10^{19}\text{m}^{-3}$ , respectively



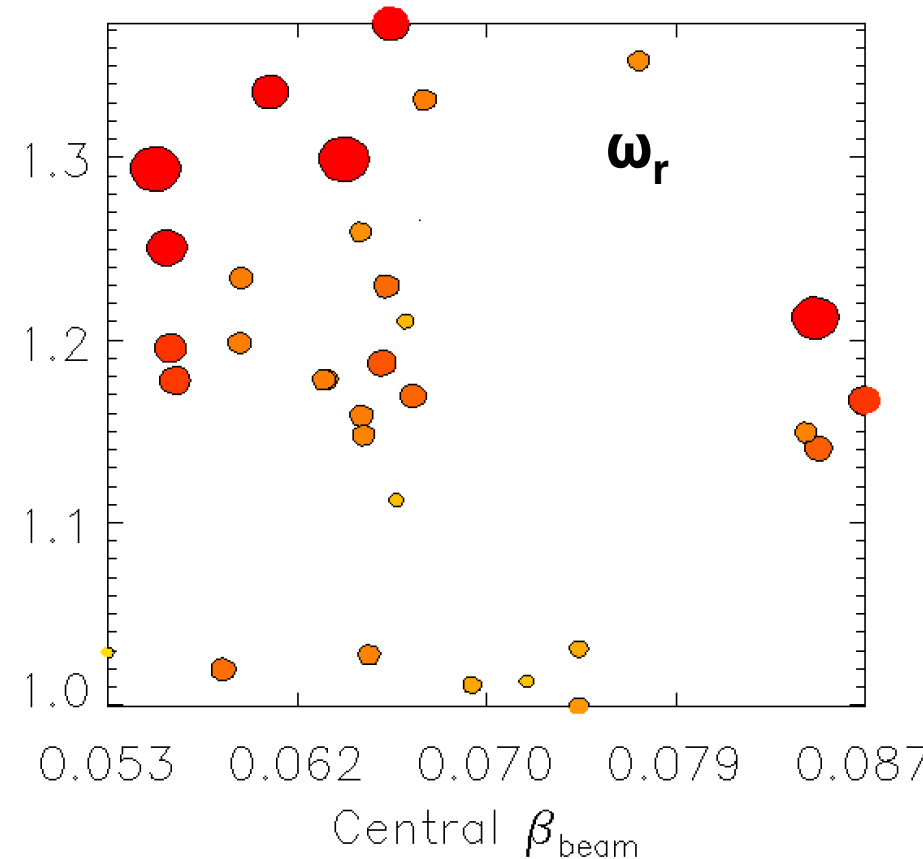
# Bursting mode real frequency has increasing trend with $\beta_{\text{beam}}/\beta_{\text{tot}}$ and $q_{\text{min}}$

Fishbone and marginal bursting mode stability diagram with mode frequency change  
Size and color of the events represent the maximum real frequency

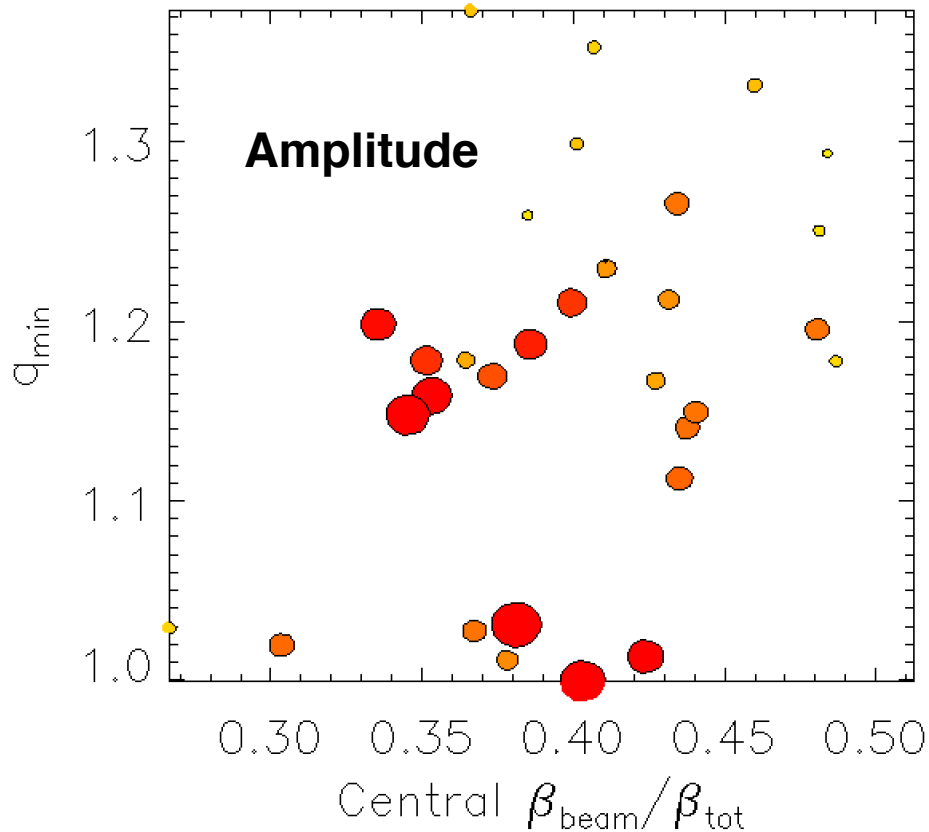
The mode real frequency increases with  $\beta_{\text{beam}}/\beta_{\text{tot}}$  and  $q_{\text{min}}$



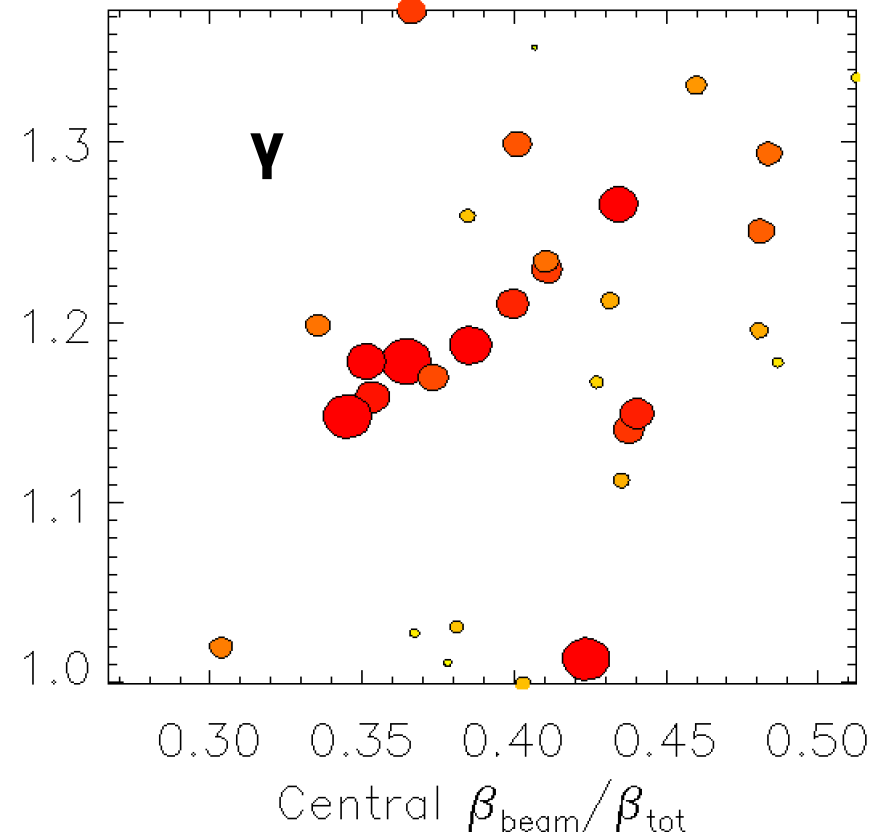
The mode real frequency depends weakly on  $\beta_{\text{beam}}$



# Mode amplitude has decreasing trend with $\beta_{\text{beam}}/\beta_{\text{tot}}$ and $q_{\text{min}}$ Effective growthrate depends weakly on either parameter



- Stability diagram with mode amplitude change indicates the mode amplitude decreases with  $\beta_{\text{beam}}/\beta_{\text{tot}}$  and  $q_{\text{min}}$



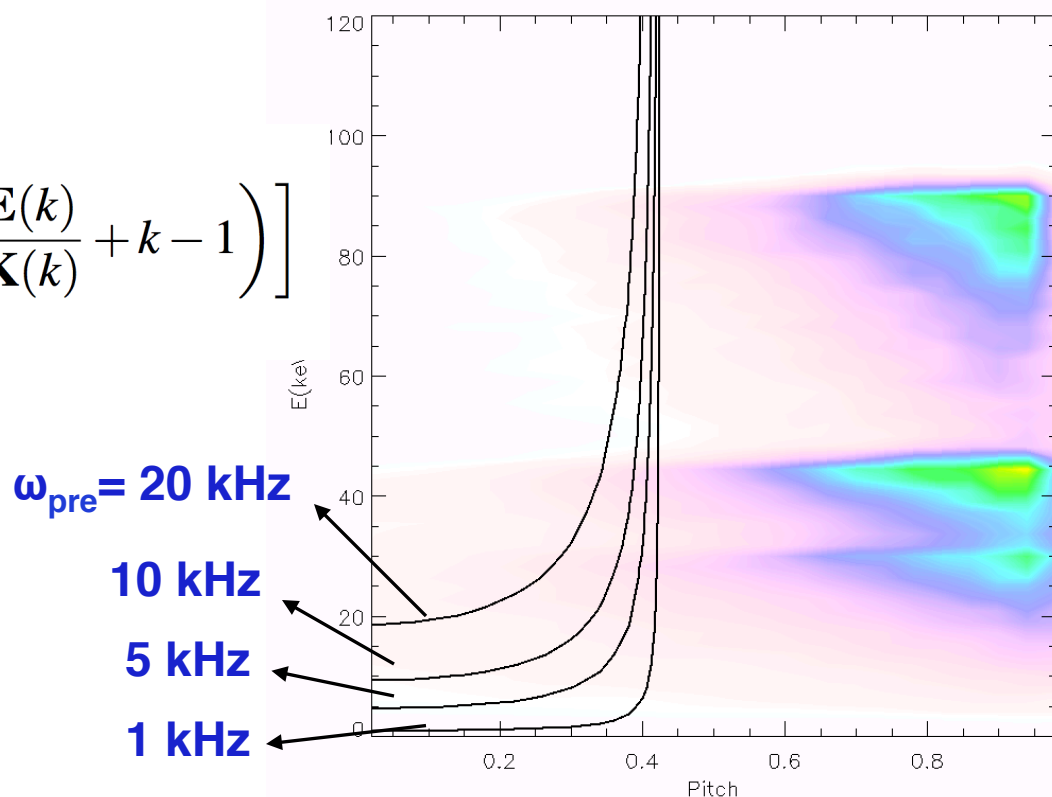
- Stability diagram with effective growth rate shows no clear trend with  $\beta_{\text{beam}}/\beta_{\text{tot}}$  and  $q_{\text{min}}$

# Dependence of mode properties on resonant fast ion parameters

- Since the dependence of mode properties shows only weak trends on global parameters, fast ions satisfying the precessional resonance condition  $\omega_r = n \omega_{pre}$  are selected. Where  $n=1$  is the dominant toroidal mode number for kink-like modes.
- The resonant fast ion  $\beta$ :  $\beta_{res} = \beta_{beam}$  integrated along the  $\omega_r = \omega_{pre}$  line in the phase space to select resonant fast ions, where  $\omega_r = 2\pi f_r$ , and  $\omega_{pre}$  is the fast ion precessional frequency given by<sup>[15]</sup>

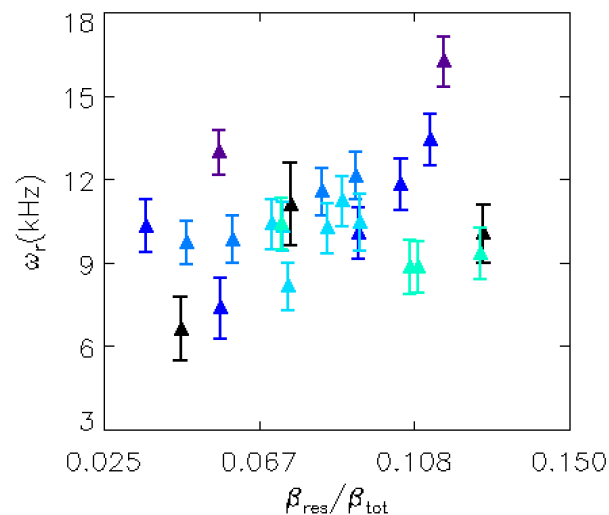
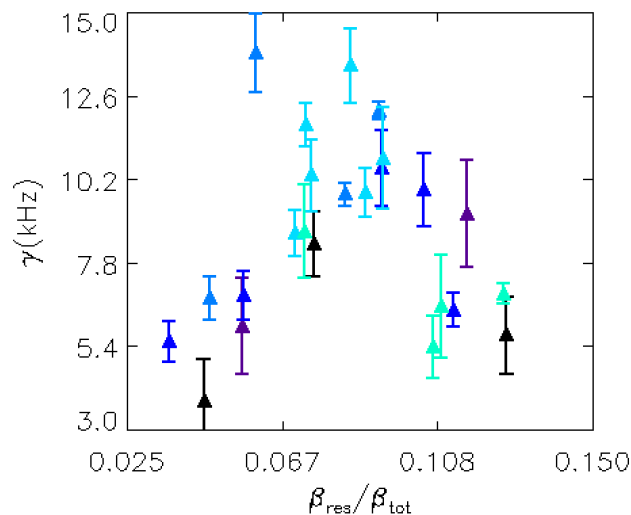
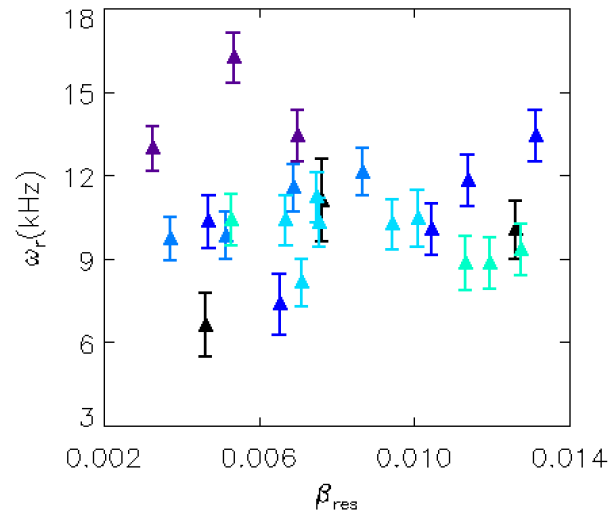
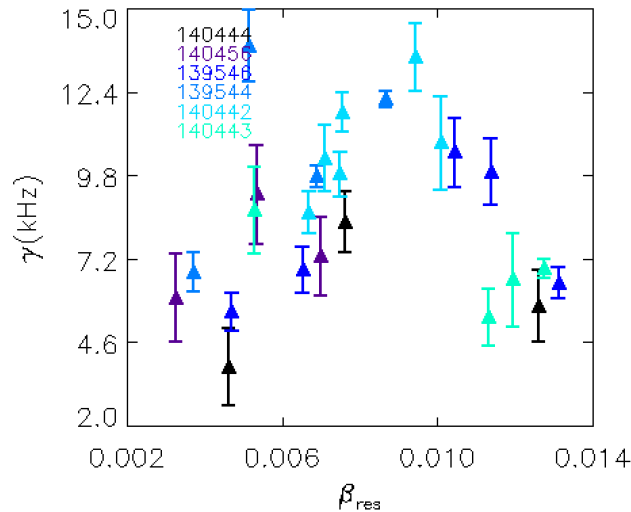
$$\omega_{pre} = \frac{2E}{R_0 B_0} \frac{q}{r} (2 - \lambda) \left[ \frac{E(k)}{K(k)} - \frac{1}{2} + \left( \frac{E(k)}{K(k)} + k - 1 \right) \right]$$

- $E$  is the fast ion energy.
- $E(k)$  and  $K(k)$  are the complete elliptic functions
- $k = (1 + \varepsilon - \lambda)/2\varepsilon$
- $\varepsilon = r/R_0$
- $\lambda = \mu B_0/E$  is a velocity space variable related to pitch angle.



Fast ion phase space distribution from TRANSP

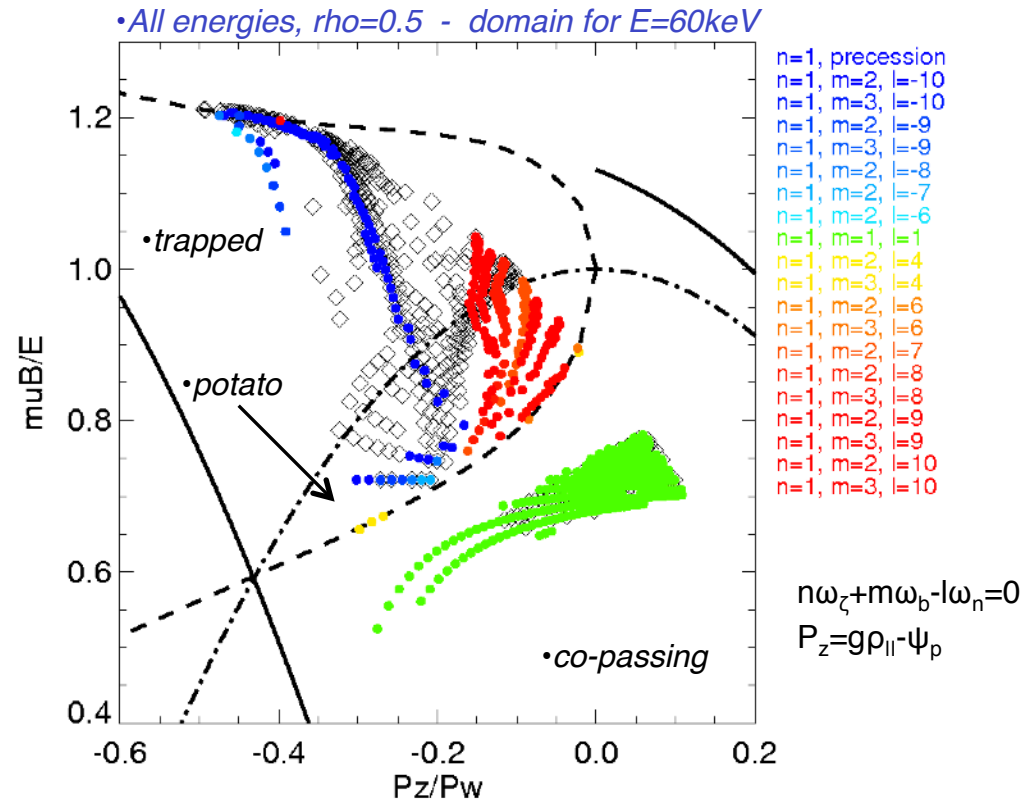
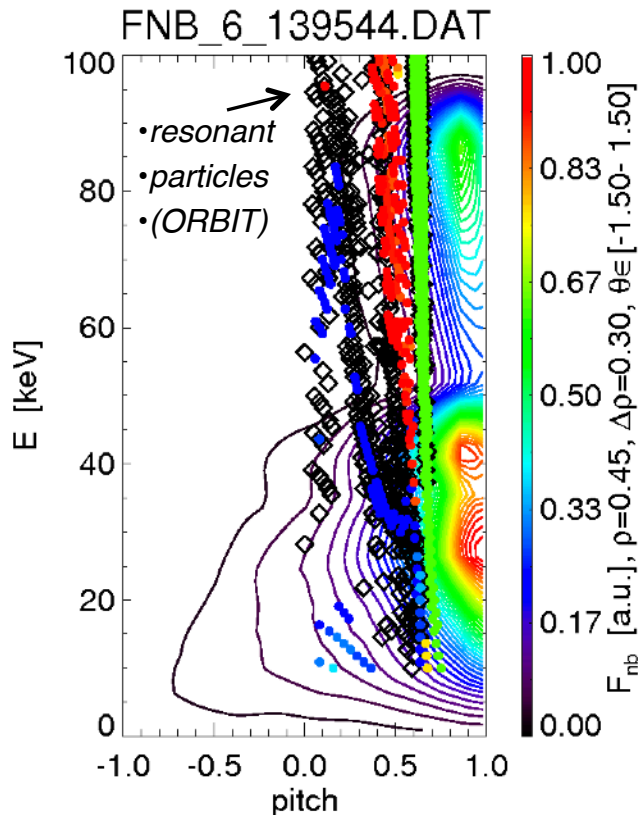
# Growthrate exhibits a general increasing trend with $\beta_{res}$



- $\beta_{res}$  is the integrated fast ion  $\beta$  along the  $\omega_r = \omega_{pre}$  line in the phase space.
- The growthrate has a increase trend with resonant  $\beta_{res}$
- except for a drop at higher  $\beta_{res}$ , corresponding to  $\beta_{res}/\beta_{tot} \sim 0.3$ .

# ORBIT code reveals multiple resonances are at play in addition to “precession” resonance

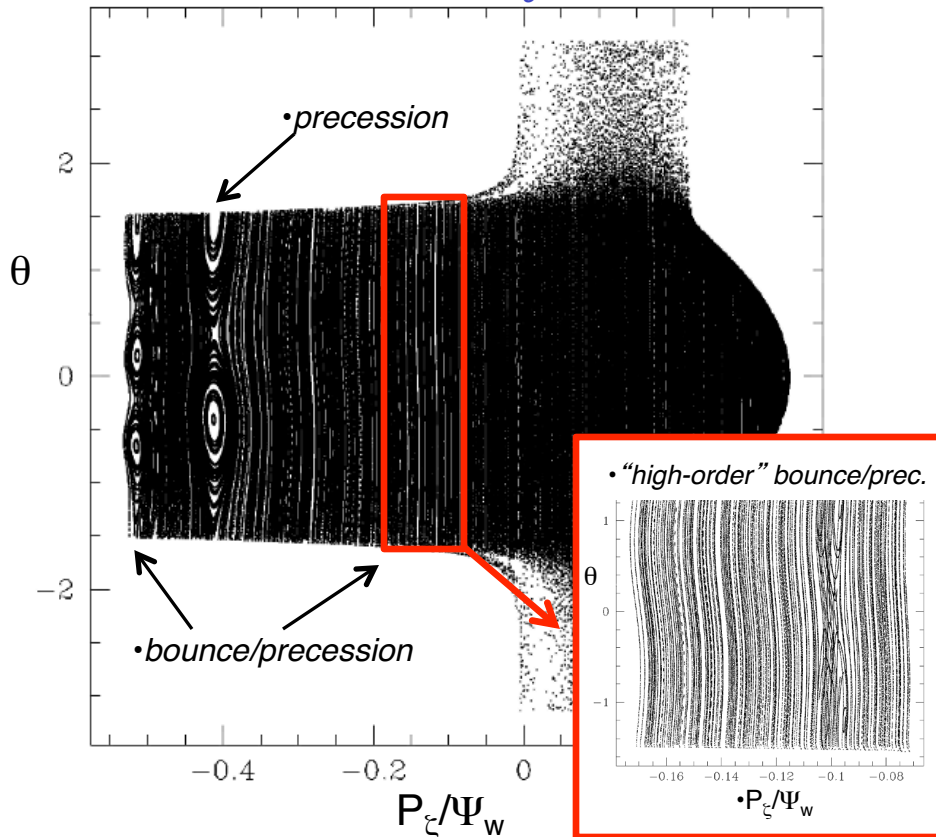
- Resonances identified through “phase vector rotation” method in ORBIT [White, PPCF **53** 085018 2011]
- Consistent with previous studies of *bounce-precession fishbones* in NSTX [Fredrickson, NF **43** 1258 2003]



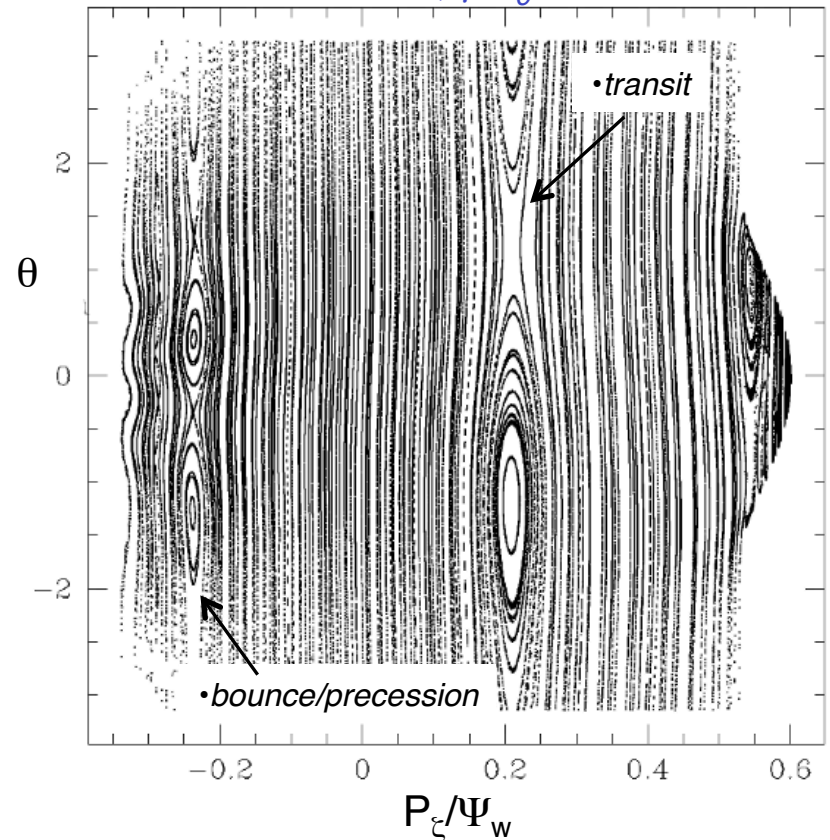
# Poincaré plots show signature of resonances over broad portion of trapped/co-passing phase space

Points are plotted in the poloidal cross section whenever  $n\zeta - \omega_n t = 2\pi k$

$E=90\text{keV}, \mu B_0/E \sim 1$



$E=90\text{keV}, \mu B_0/E \sim 0.3$



> Possible tool to compute  $\beta_{\text{res}}$  more accurately



## Summary and conclusions

- The kink-like mode stability properties and dynamics in NSTX plasmas are analyzed in this study.
- The NRK and fishbone stability diagram from the experimental data indicates that the kink-like modes appear mostly for  $q_{\min} < 1.5$
- The long lived NRK modes tend to be unstable at higher fast ion  $\beta$ .
- The bursting modes have an increased real-frequency as the minimum  $q$  and ratio of fast ion pressure and total plasma pressure increase.
- Experimental results will provide the basis for the validation and benchmark of numerical studies of the kink-like instabilities.

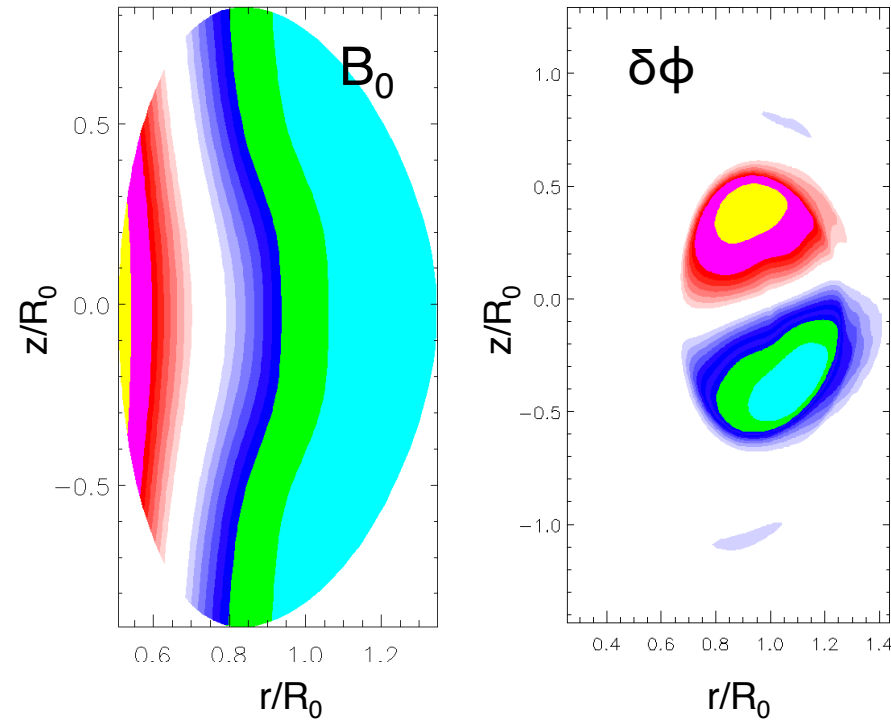
## Future work: Comparison of the database with simulations of kink-like modes on NSTX

- This experimental characterization of kink-like modes for different NBI scenarios provides reference for simulations of kink-like instabilities in NSTX plasmas for a variety of scenarios, particularly for different fast ion properties.
- Simulations with the GTC code<sup>[16]</sup> will be used to assess the kinetic effects of thermal and fast ions on the instabilities and identify regimes for which kink/fishbone activity is minimized or suppressed.
- Experimental plasma parameters from the database including the thermal equilibrium and measured fast ion profiles can be implemented and used as initial conditions.

**This work is partly supported by US-DoE  
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# NSTX equilibrium and preliminary kink simulations in GTC fluid limit

- Experimental equilibrium from shot # 124379 has been implemented in GTC.
- $q$  profile is modified to test the numerical capabilities. Simulations in fluid limit is being carried out for benchmark purposes.

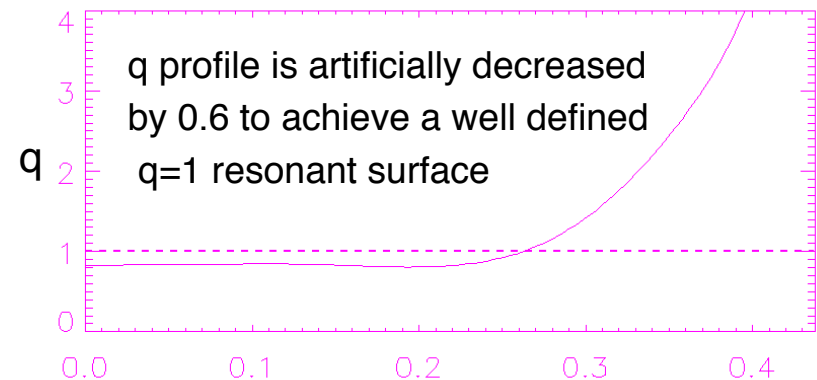
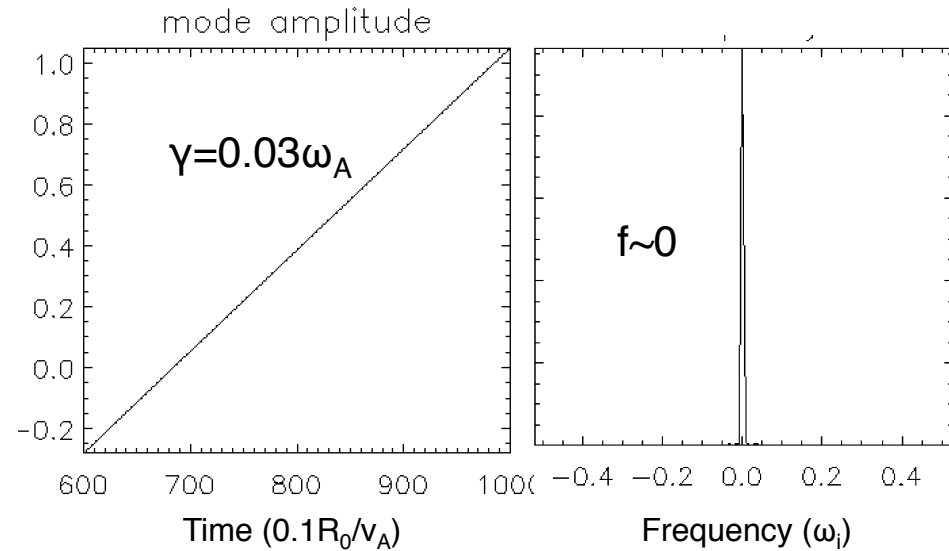


$$n_e = 9.34 \times 10^{19} \text{ m}^{-3}$$

$T_e = 879.96 \text{ eV}$  (artificially increased to  $2.3 \text{ keV}$  to match experimental total beta in fluid limit simulations)

$$R_0 = 101.83 \text{ cm}$$

$$B_0 = 4536 \text{ G}$$



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