

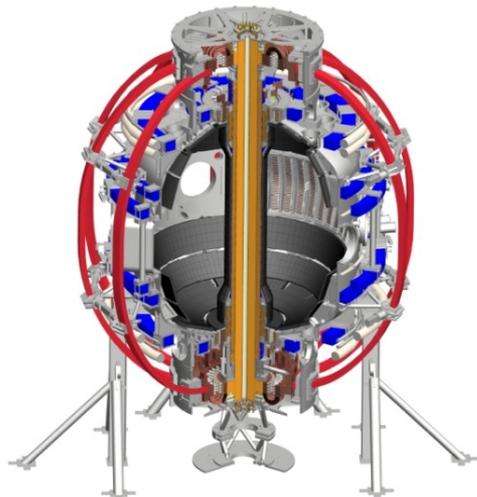
Internal Amplitude, Structure and Identification of CAEs and GAEs in NSTX

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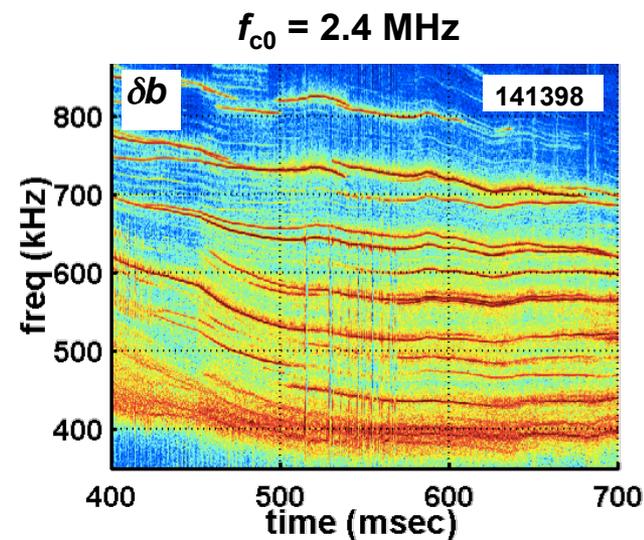
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Summary

- High frequency Alfvén Eigenmodes (AE) excited by beam ions in NSTX \Rightarrow can also be excited in ITER & FNSF by beam ions & α 's
 - correlate with enhanced core electron thermal transport
 - posited cause: resonant interaction in presence of multiple modes
- Measurements reveal two kinds of mode
 - (1) broad structure, peaking toward core with significant edge $|\xi|$:
mostly $f < \sim 600$ kHz, $n = -6 - -8$, smaller core $|\xi|$ & larger edge δb
 - (2) strongly core localized with vanishing edge $|\xi|$:
mostly $f > \sim 600$ kHz, $n = -3 - -5$, larger core $|\xi|$ & smaller edge δb
- Local dispersion relations used with f & n to identify modes
 - (1) broad structure modes are *global AEs (GAE)*: f evolves consistently with shear dispersion relation & cannot fit in CAE “well”
 - (2) strongly core localized modes are *compressional AEs (CAE)*: f evolves inconsistently with shear dispersion relation & can fit in CAE “well”
- Amplitude and number of modes consistent with posited cause of enhanced core electron thermal transport

High frequency AEs commonly excited by beam ions in NSTX: Possible implications for burning plasmas

- High f AEs ($f/f_{c0} > \sim 0.2$) commonly observed in NSTX with reflectometers & edge δb
- Excited by Doppler-shifted resonance with beam ions
 - Edge δb_θ toroidal array typically shows $|n| < \sim 15$, propagation counter to beam ions ($n < 0$)
- High f AE activity correlated with enhanced χ_e
- Other significant effects on plasma
 - shown to cause fast-ion transport
 - postulated to cause ion heating
- Can be excited by beam ions and α 's in ITER & FNSF
 - investigation in NSTX furthers predictive capability for burning plasmas



High frequency AEs proposed as cause of observed χ_e enhancement [D. Stutman et al., PRL 102 115002 (2009)]

- Enhanced χ_e observed in core of NSTX beam-heated H-mode plasmas
- High f AE activity correlates with enhanced χ_e
- $f \sim f_{be} \sim 600$ kHz \Rightarrow resonant orbit modification
 - $f_{be} \equiv$ trapped electron bounce frequency
- High f AEs identified as GAEs
- GAE core localization expected \Rightarrow active in region of enhanced χ_e
- Orbit modeling \Rightarrow significant χ_e enhancement from multiple modes

[N. N. Gorelenkov et al., Nucl. Fusion 50, 084012 (2010)]

– threshold at ~ 15 modes

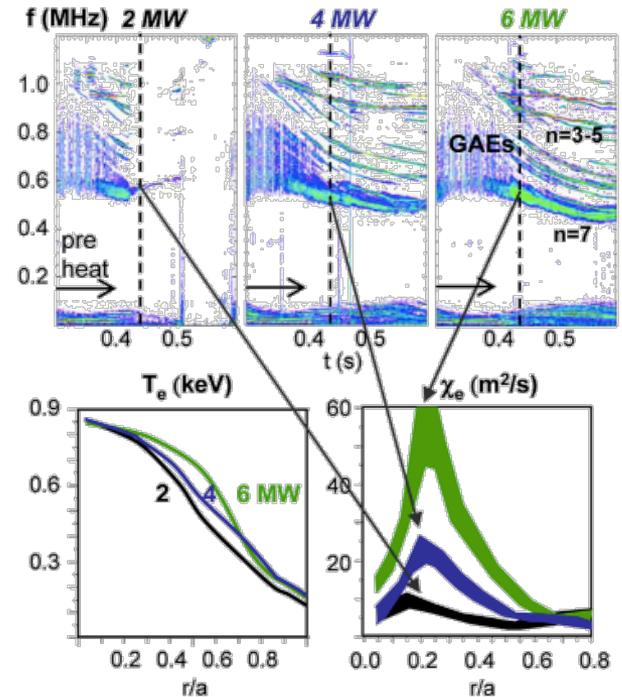
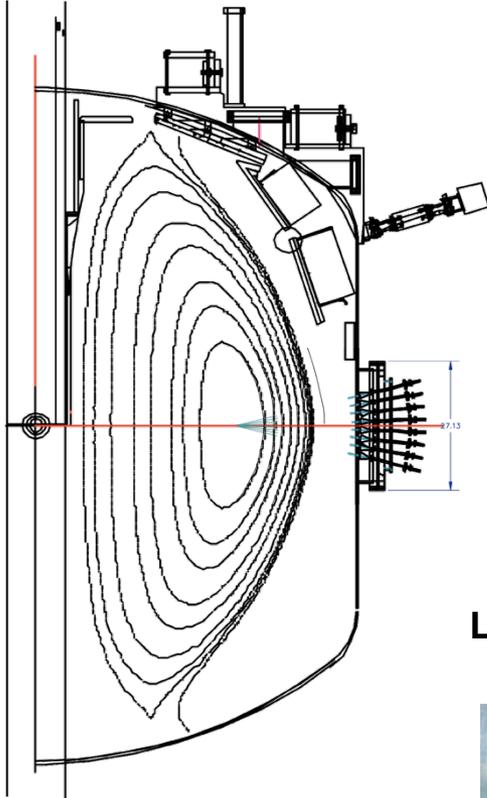


FIG. 3 (color online). Correlation between GAE activity, T_e flattening, and central χ_e increase in NSTX H modes heated by 2, 4, and 6 MW neutral beam, at $t \sim 0.44$ s. Within the uncertainties, the q , n_e , and $\omega_{E \times B}$ profiles are the same in all discharges at the time of the transport correlation [13].

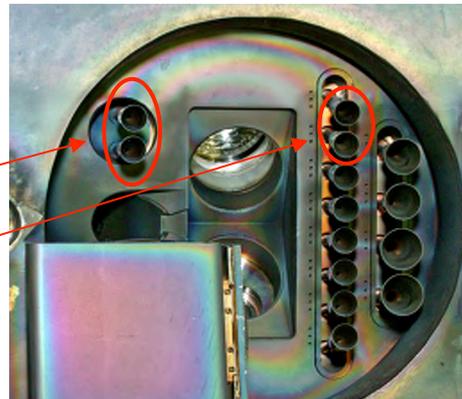
AE radial structure measured with array of reflectometers

NSTX cross-section



- Two arrays: “Q-band” & “V-band”
 - Q-band: 30, 32.5, 35, 37.5, 42.5, 45, 47.5 & 50 GHz
 - V-band: 55, 57.5, 60, 62.5, 67.5, 70, 72.5 & 75 GHz
- Arrays closely spaced (separated $\sim 10^\circ$ toroidal)
- Single launch and receive horn for each array
- **Horns oriented perpendicular to flux surfaces \Rightarrow frequency array = radial array**
- Cutoffs span large radial range in high density plasmas ($n_0 \sim 1 - 7 \times 10^{19} \text{ m}^{-3}$)

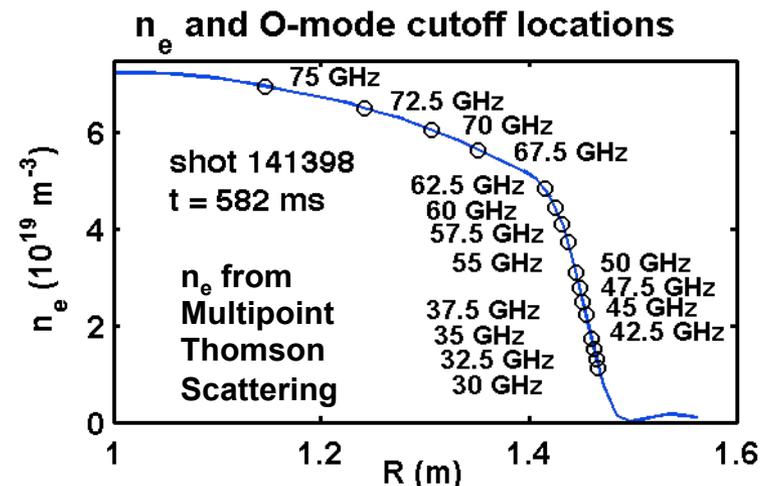
Launch and Receive Horns
(Interior View)



30-50 GHz

55-75 GHz

(not shown: horns modified to optimize for frequency range)



Reflectometers used to measure local AE density fluctuation

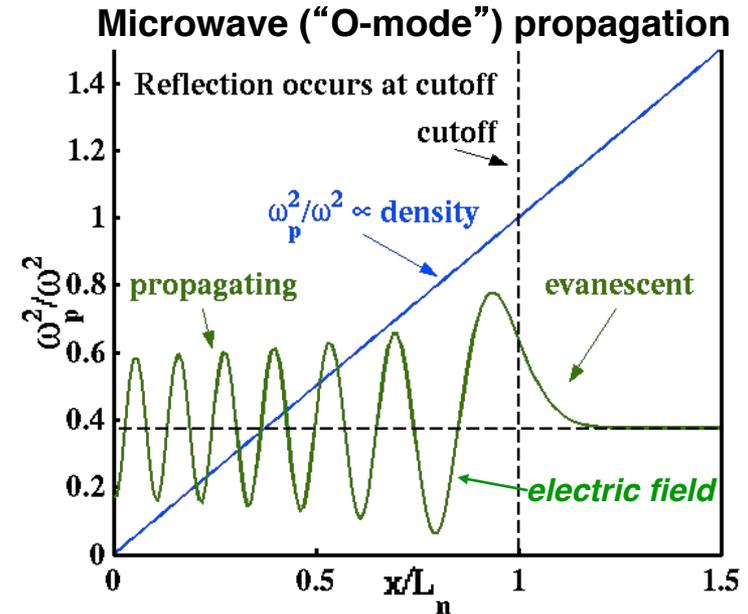
- Microwaves propagate to “cutoff” layer, where density high enough for reflection ($\omega_p = \omega$)

- Dispersion relation of “ordinary mode” microwaves: $\omega^2 = \omega_p^2 + c^2k^2$,
 ω_p^2 proportional to density ($\omega_p^2 = e^2n_0/\epsilon_0m_e$)
- $k \rightarrow 0$ as $\omega \rightarrow \omega_p$,
microwaves reflect at $k = 0$

- Reflectometer measures path length change of microwaves reflected from plasma

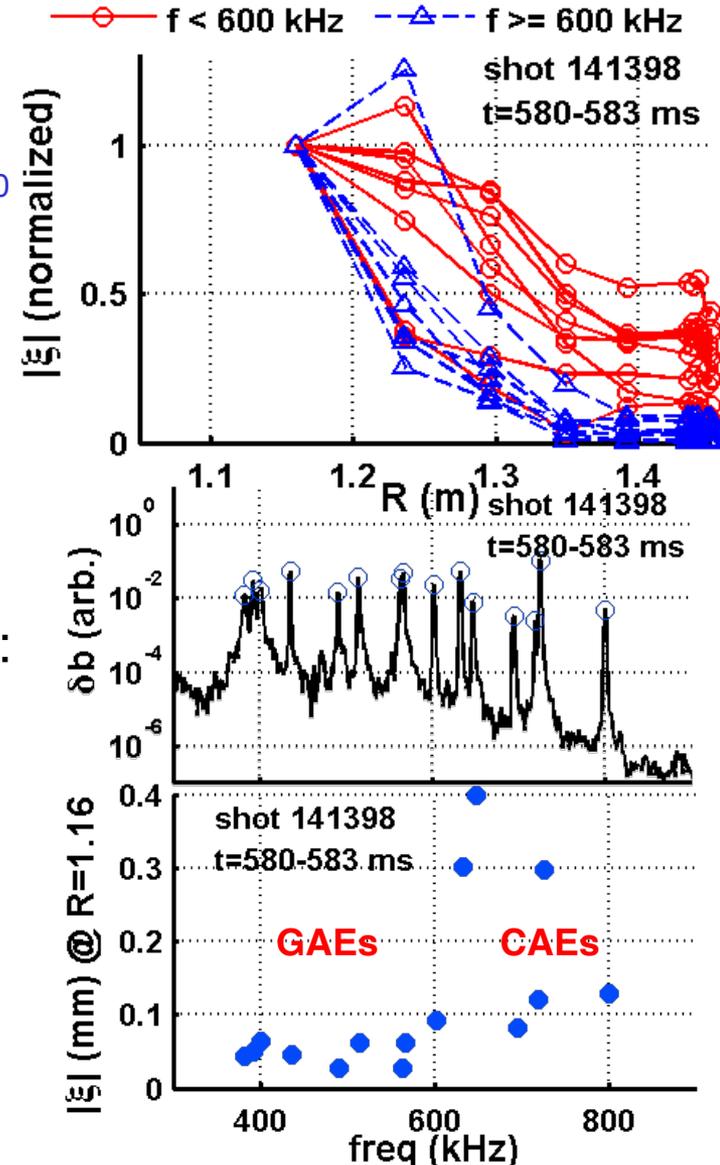
- phase between reflected and launched waves changes ($\delta\phi$)

- for large scale modes, cutoff displaces due to δn at cutoff \Rightarrow “effective displacement” $\xi \equiv \delta\phi/2k_{vac}$ approximates cutoff displacement



Measurements reveal **two kinds of high frequency AEs** in H-mode beam-heated plasmas

- *Effective displacement* (ξ) measured at **16 radii** with reflectometer array
 - shear AEs: ξ dominated by displacement of ∇n_0
 - compressional AEs: compressional δn contributes to ξ
- Toroidal mode number (n) measured with δb_θ edge toroidal array
 - 12 locations, irregular spacing ($\Delta\phi$)
 - $10^\circ \leq \Delta\phi \leq 180^\circ \Rightarrow$ resolves $|n| \leq 18$
- Modes structures tend to fall in two categories:
 - (1) **broad structure**, peaking toward core with significant edge $|\xi|$
 - mostly $f < \sim 600$ kHz, $n = -6 - -8$
 - typically larger core $|\xi|$ & larger edge δb
 - (2) **strongly core localized**, vanishing edge $|\xi|$
 - mostly $f > \sim 600$ kHz, $n = -3 - -5$
 - typically larger larger core $|\xi|$ & smaller edge δb



Modes can be identified as CAEs or GAEs via mode number and frequency evolution

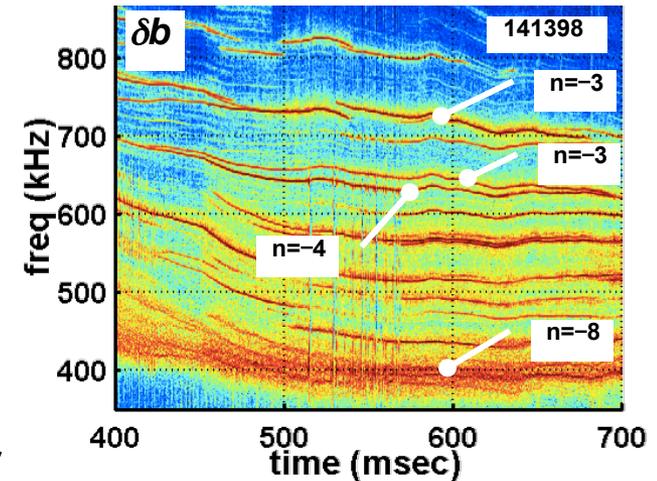
- Dispersion relation parameters measured:
 - q_0 and B_0 from equilibrium reconstruction using magnetic field pitch from Motional Start Effect
 - n_{e0} measured via Multipoint Thomson Scattering
 - Alfvén velocity, $v_{A0} = B_0/(\mu_0\rho_0)^{1/2}$
 - $\rho_0 = m_D n_{e0}$, $m_D = \text{Deuterium mass}$
 - Toroidal rotation frequency, f_{ROT0} , from Charge Exchange Recombination Spectroscopy
- For GAEs, expect $f(t)$ consistent with local shear Alfvén dispersion relation, but not CAEs

$$f_{GAE} = \frac{k_{\parallel} v_A}{2\pi} + n f_{ROT}, \quad k_{\parallel} \approx \frac{1}{R} \left| \frac{m}{q} - n \right|$$

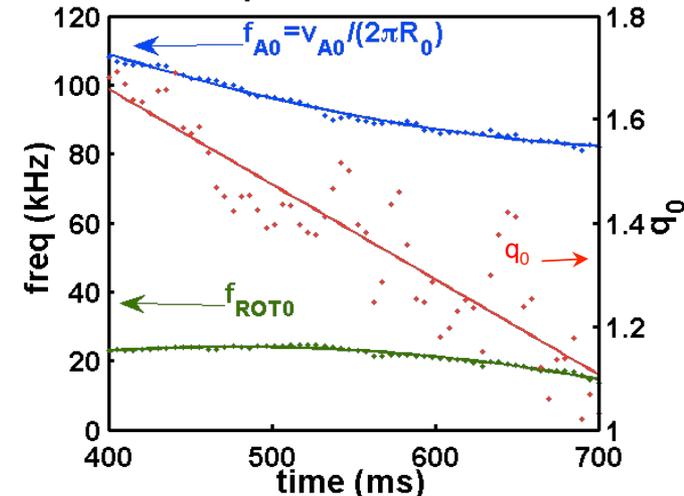
- Expect CAEs to fit in CAE “well”, but not GAEs
 - compressional Alfvén waves propagate ONLY where: $\left(\frac{n}{R}\right)^2 v_A^2 - (\omega - n\omega_{ROT})^2 < 0$
 - “wavelength” in R - Z plane must fit inside “well”

$$\lambda_{R-Z} = \frac{2\pi}{k_{R-Z}} = 2\pi \left((\omega - n\omega_{ROT})^2 - \left(\frac{n}{R}\right)^2 v_A^2 \right)^{-1/2}$$

AE frequency evolution



Equilibrium trends

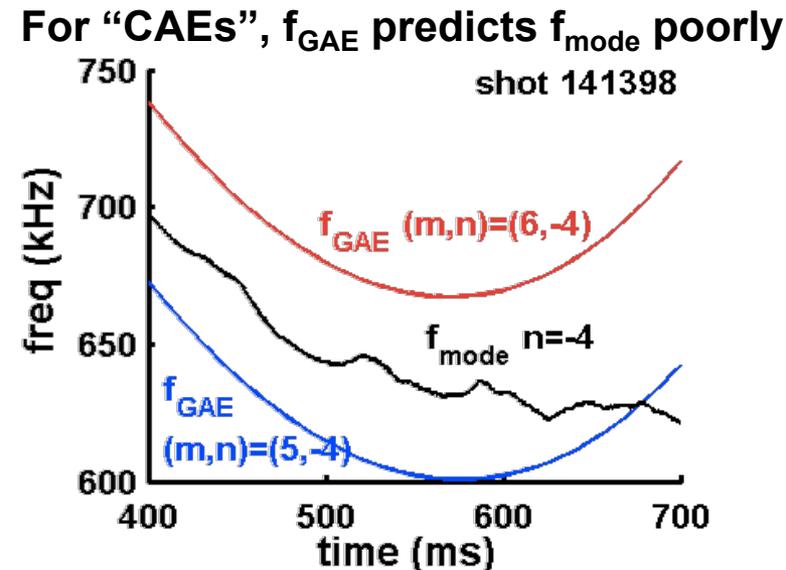
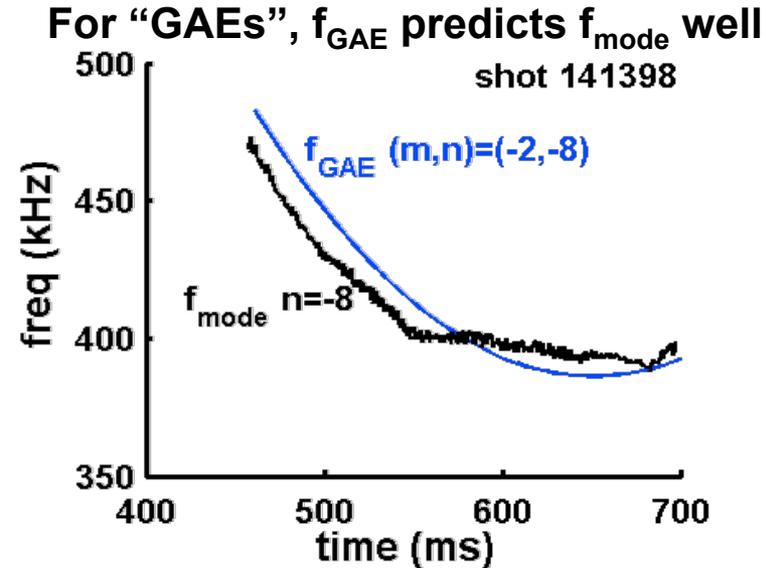


Sensitivity of f_{GAE} to q_0 helps distinguish CAEs & GAEs

- GAEs are shear Alfvén:

$$f_{GAE} = \frac{k_{\parallel} v_A}{2\pi} + n f_{ROT}, k_{\parallel} \approx \frac{1}{R} \left| \frac{m}{q} - n \right|$$

- $f_{GAE}(t)$ sensitive to m/q_0 if $|m| \gg 1$
- q_0 varies substantially (1.7 – 1.1) over $t = 400 - 700$ ms
- Modes with $f < \sim 600$ kHz, $n = -6 - -8$:
 $f(t) \sim f_{GAE}(t)$
 - $|n| \gg 1 \Rightarrow$ low $|m| \Rightarrow f_{GAE}$ insensitive to q_0
- Modes with $f > \sim 600$ kHz, $n = -3 - -5$:
 $f(t)$ NOT consistent with $f_{GAE}(t)$
 - low $|n|$, high $f \Rightarrow$ high $|m| \Rightarrow$ strong q_0 sensitivity



For identification as CAE, sufficiently wide & deep “well” must exist for mode with measured f and n

- For $n \neq 0$, compressional Alfvén “well” formed:
 - compressional Alfvén waves propagate ONLY where:

$$\left(\frac{n}{R}\right)^2 v_A^2 - (\omega - n\omega_{ROT})^2 < 0$$

- CAE “wavelength” in R - Z plane must fit inside “well”

$$\lambda_{R-Z} = \frac{2\pi}{k_{R-Z}} = 2\pi \left((\omega - n\omega_{ROT})^2 - \left(\frac{n}{R}\right)^2 v_A^2 \right)^{-1/2}$$

- For observed modes, f & n used to determine well width and λ_{R-Z}

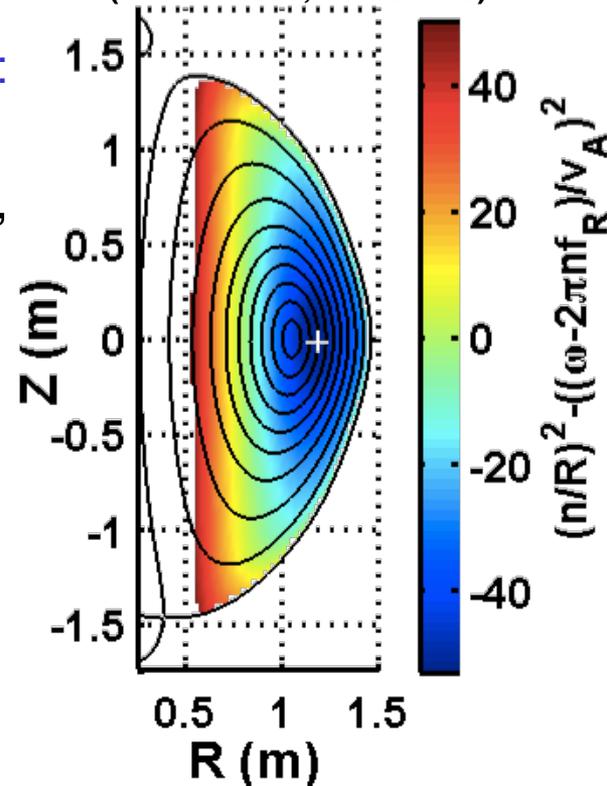
- λ_{R-Z} calculated at deepest point in well
- Width (ΔR) determined in midplane

- Modes with $f > \sim 600$ kHz, $n = -3 - -5$ sufficiently wide and deep

- Modes with $f < \sim 600$ kHz, $n = -6 - -8$ do not fit in “well”

- For some f & n , $(n/R)^2 v_A^2 - (\omega - n\omega_{ROT})^2 > 0$ everywhere
- For some f & n , $\lambda_{R-Z} \gg \Delta R$

CAE “well” for $f = 633$ kHz, $n = -4$
(shot 141398, $t = 582$ ms)



Amplitude and number of modes consistent with ORBIT modeling prediction for enhanced χ_e

- ORBIT modeling indicates significant χ_e enhancement due to resonant electron interaction of multiple modes
 - [N. N. Gorelenkov et al., Nucl. Fusion 50, 084012 (2010)]
 - total fluctuation level needed to explain χ_e enhancement: $\alpha = \delta A_{\parallel}/B_0 R_0 = 4 \times 10^{-4}$
 - χ_e scales strongly with $\alpha \Rightarrow$ bursty fluctuations give more χ_e than would expect from r.m.s $\alpha \Rightarrow$ should evaluate time dependence carefully
 - threshold at ~ 15 modes
- For modes with $f < 600$ kHz, calculated r.m.s. $\alpha = 3.4 \times 10^{-4}$ in core, **consistent with prediction for necessary fluctuation level**
 - for shear Alfvén modes: $\xi_r = \delta B_r / i k_{\parallel} B_0 = \alpha R_0 k_{\theta} / k_{\parallel}$
 - ξ_R estimated by reflectometer $|\xi|$ @ $R = 1.16$ m
 - k_{\parallel} estimated from f using shear Alfvén dispersion relation
 - $k_{\theta} = m/r$, using m estimated from $k_{\parallel} = |m/q - n|$, taking $q = q_0$ and $r = 1.16$ m $- R_0$
 - Future comparison must account for bursty fluctuation level
- Number of modes (including CAEs) is 15, **consistent with prediction for necessary fluctuation level**
- Model needed for CAE effect on χ_e

Future Work

- Extend ORBIT modeling to include CAEs in prediction of χ_e enhancement
- Use mode structure measurements to guide inputs to ORBIT modeling
- Investigate effects of CAEs and GAEs on fast-ion transport using ORBIT modeling with measured mode structures
- Compare CAE/GAE amplitude and structure measurements with theory predicting ion heating

Conclusions

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