



# Parametric dependencies of low-k turbulence in NSTX H-mode pedestals (P7-18)

David R. Smith<sup>1</sup>, R. Fonck<sup>1</sup>, G. McKee<sup>1</sup>, R. Bell<sup>2</sup>, Y. Chen<sup>3</sup>, A. Diallo<sup>2</sup>, B. Dudson<sup>4</sup>,  
S. Kaye<sup>2</sup>, B. LeBlanc<sup>2</sup>, R. Maingi<sup>5</sup>, S. Parker<sup>3</sup>, B. Stratton<sup>2</sup>, and W. Wan<sup>3</sup>

<sup>1</sup> *University of Wisconsin-Madison, Madison, WI, USA*

<sup>2</sup> *Princeton Plasma Physics Lab, Princeton, NJ, USA*

<sup>3</sup> *University of Colorado, Boulder, CO, USA*

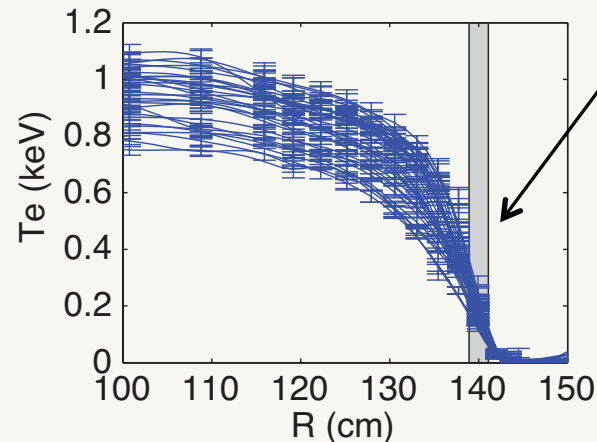
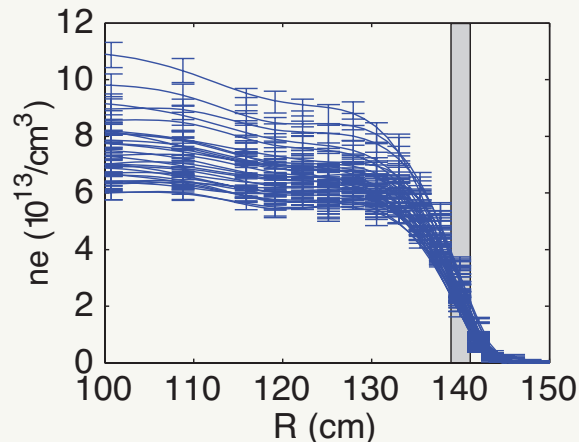
<sup>4</sup> *University of York, York, UK*

<sup>5</sup> *Oak Ridge National Lab, Oak Ridge, TN, USA*

24<sup>th</sup> IAEA Fusion Energy Conference  
San Diego, CA, USA  
October 8-13, 2012

# What are the characteristics and parametric dependencies of pedestal turbulence in NSTX? Can simulations reproduce the observations?

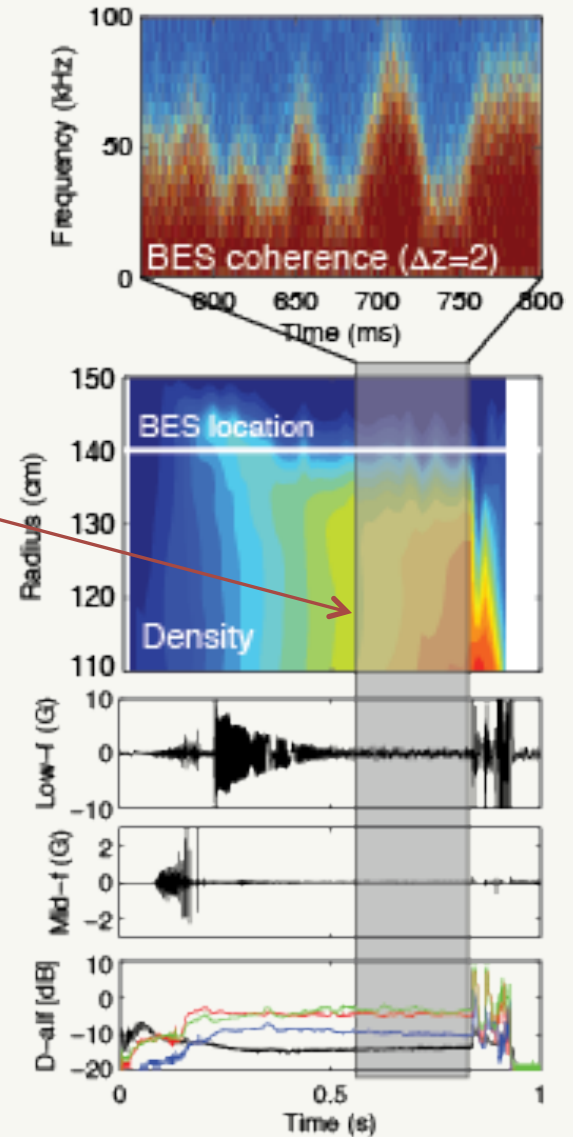
- Global confinement predictions for ITER depend upon accurate edge and pedestal models
  - ST edge parameters are among the most challenging regimes for plasma turbulence simulations: steep gradients, large  $\rho^*$ , high  $\beta$ , strong shaping, strong beam-driven flow
- We measure **pedestal turbulence** parameters in NSTX H-mode plasmas during **ELM-free, MHD quiescent** periods
  - Poloidal correlation length, wavenumber, and decorrelation time
  - Identify parametric dependencies ( $\nabla n_e$ ,  $\nabla T_i$ , etc)
- In addition, we compare measurements to **pedestal turbulence simulations** (GEM and BOUT++)



measurements from multiple discharges in outer region of pedestal

# Outline

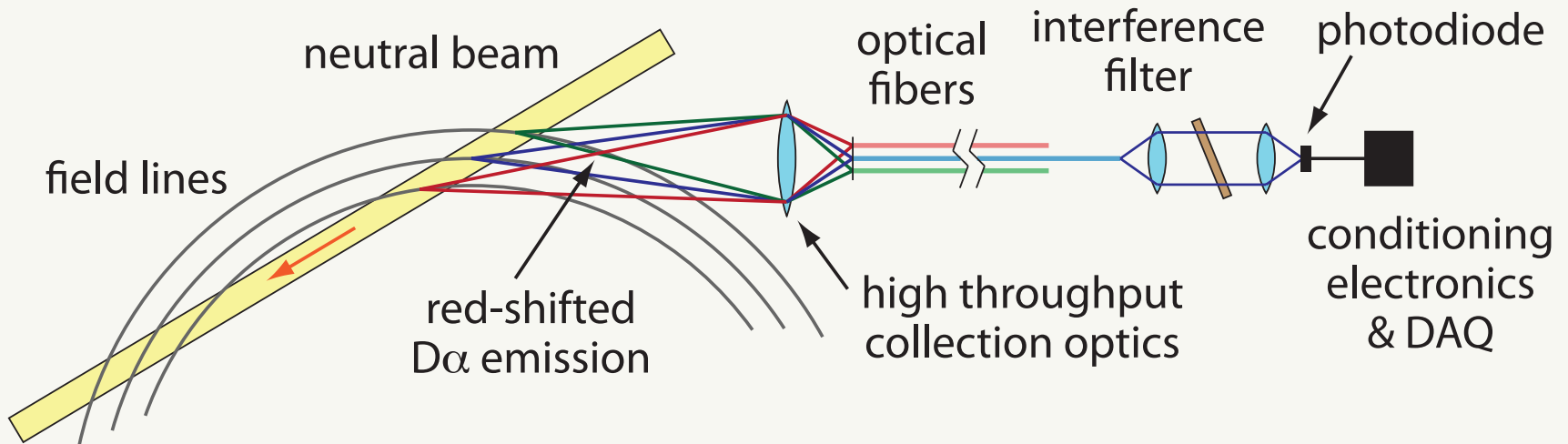
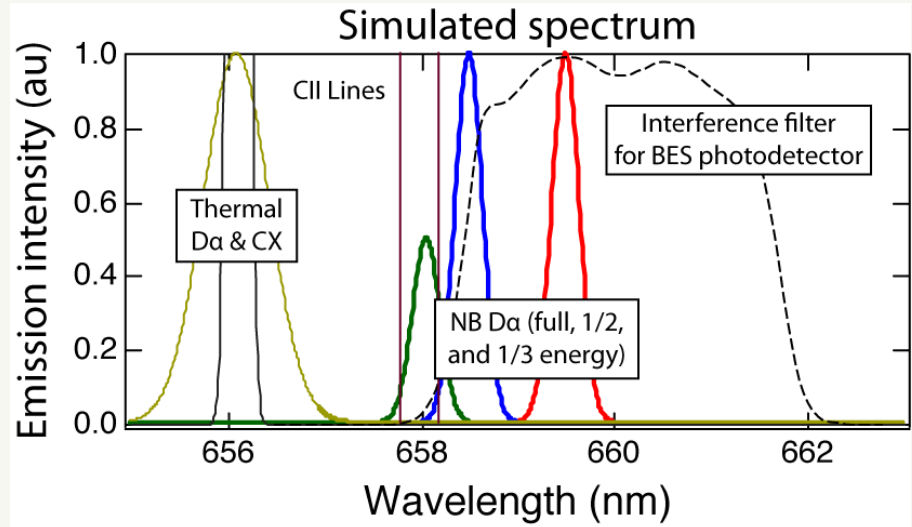
- Beam emission spectroscopy (BES) diagnostic on NSTX
- Pedestal turbulence measurements and parametric dependencies
  - ELM-free, MHD quiescent periods
- Fluid and gyrokinetic simulations of pedestal turbulence
- Future work and summary



# BES measures Doppler-shifted $D_{\alpha}$ emission ( $\lambda_0=656$ nm) from neutral beam particles

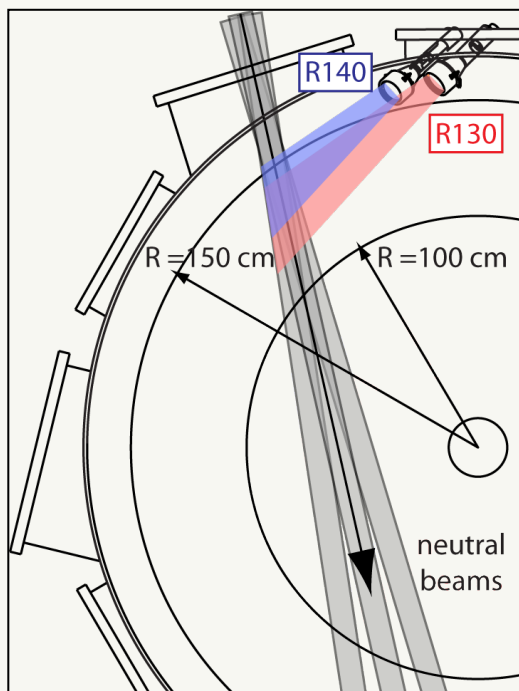
$$\frac{\delta I_{D\alpha}}{I_{D\alpha}} = \frac{\delta n}{n} \times C(E_{NB}, n, T_e, Z_{eff})$$

$\delta I_{D\alpha}$ : neutral beam  $D_{\alpha}$  emission  
 $\frac{\delta n}{n}$ : density fluctuation  
 $C \approx 1/2$

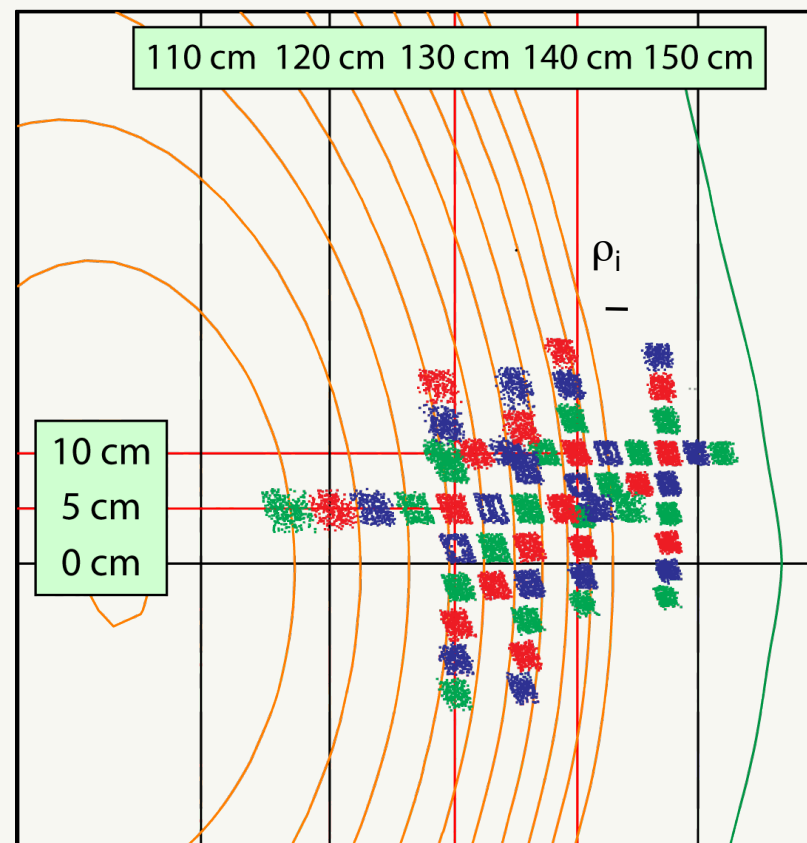


# The beam emission spectroscopy (BES) system on NSTX measures fluctuations on the ion gyroscale

- Presently 32 detection channels
- 56 sightlines in radial and poloidal arrays spanning core to SOL
- 2 MHz sampling with digital AA filter
- $k_{\perp}\rho_i \leq 1.5$  & 2-3 cm spot size
- Field-aligned optics with high throughput (etendue = 2.3 mm<sup>2</sup>-ster)



## 56 BES sightlines in radial and poloidal arrays

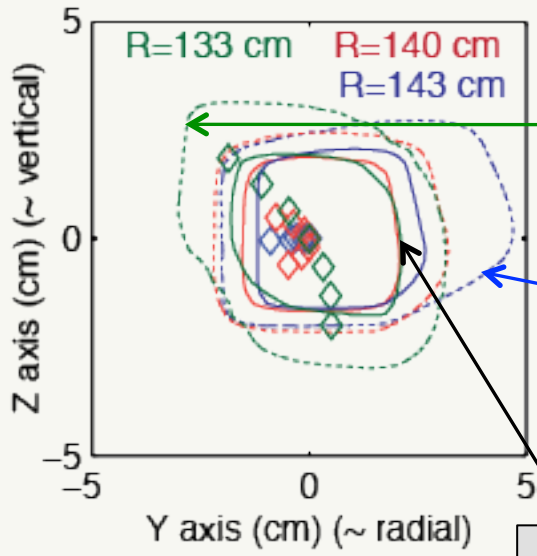
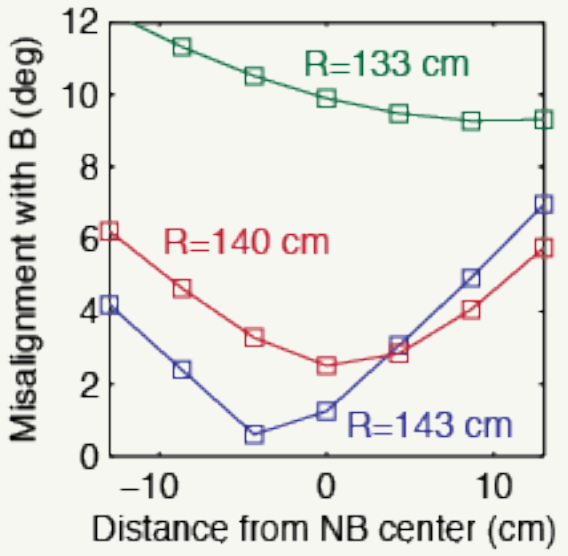
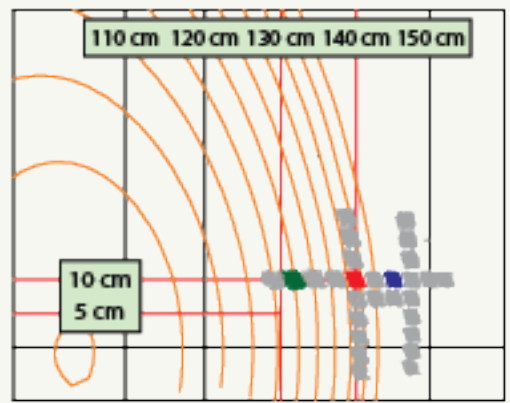
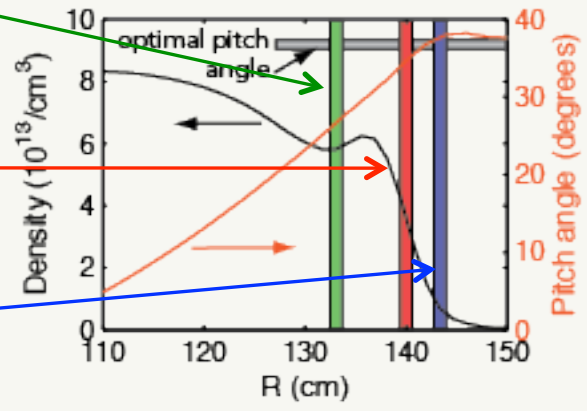


# Point spread function calculations indicate image distortion from atomic state lifetimes and field line geometry are negligible

field line misalignment

nearly optimized

low density region

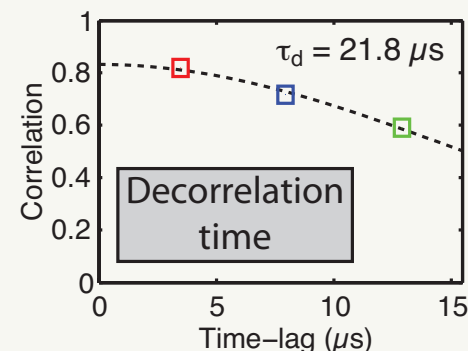
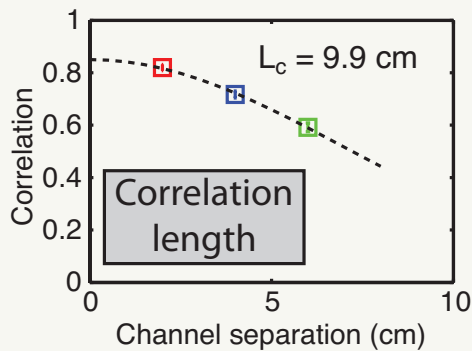
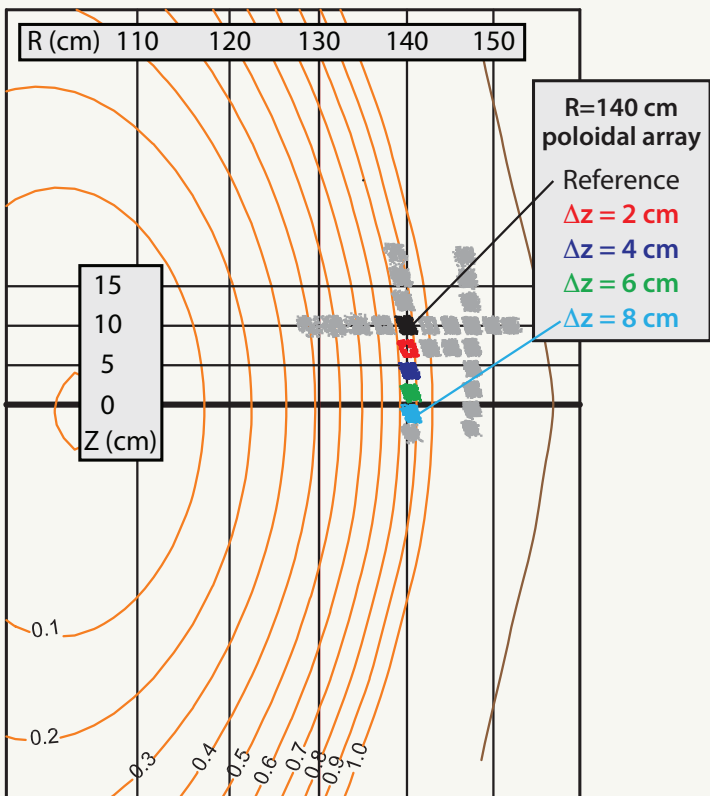
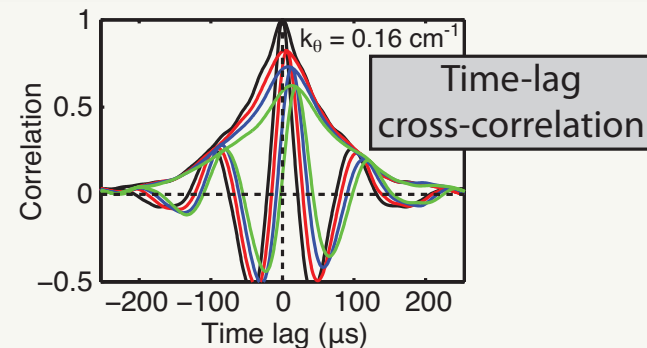
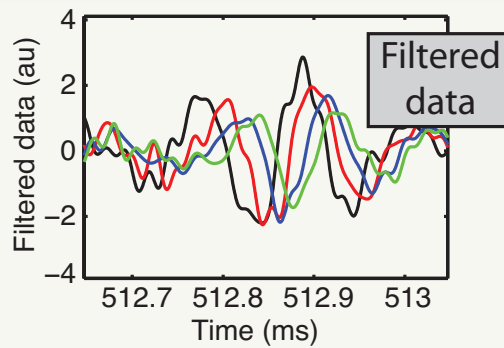
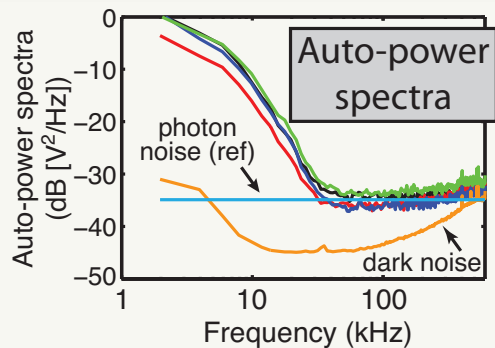


distortion from misalignment (dashed=10% of peak int.)

distortion from atomic state lifetimes

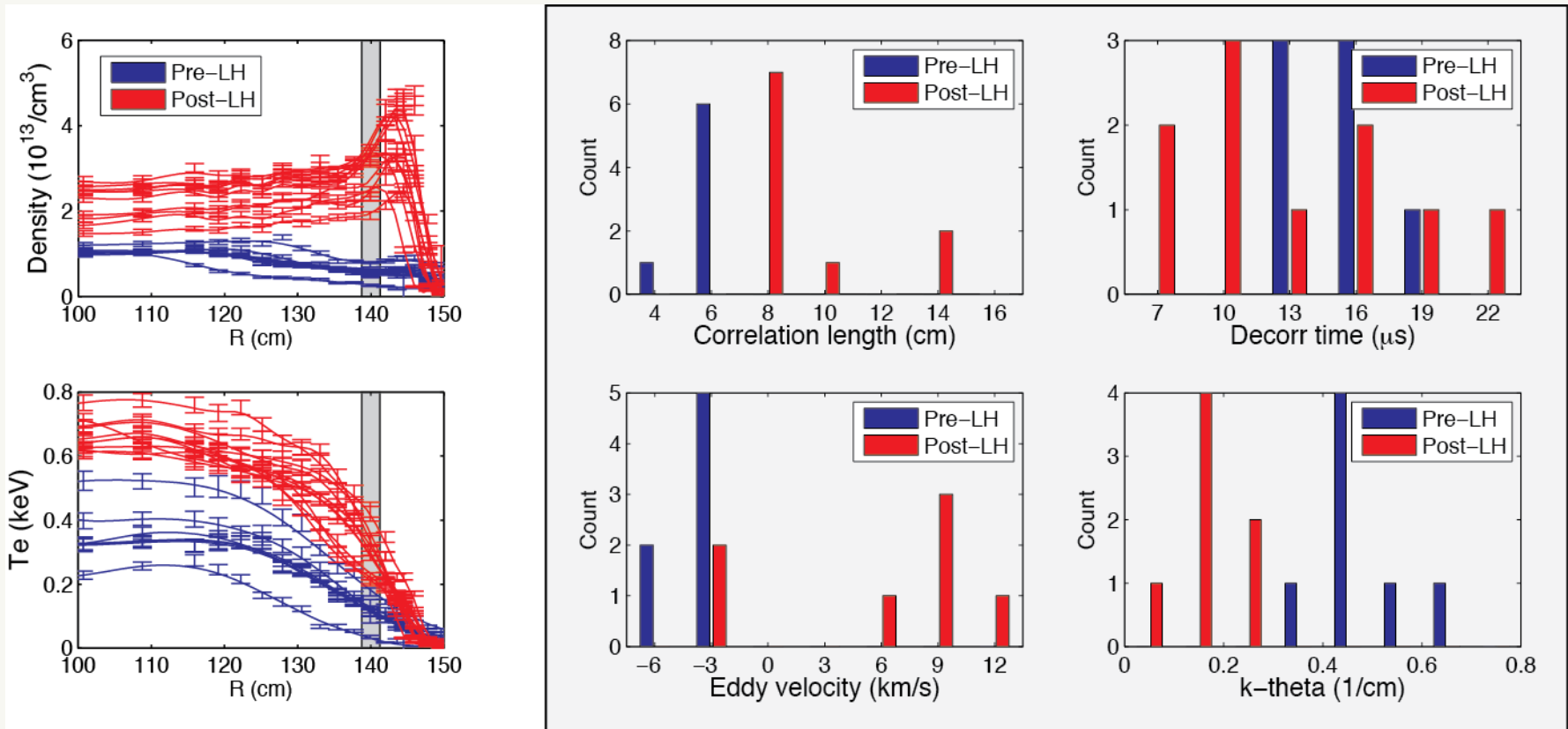
FWHM distortions (solid line) are ~10%

# We measure poloidal correlation lengths ( $L_c$ ), poloidal wavenumbers ( $k_\theta$ ), and decorrelation times ( $\tau_d$ ) with BES



- Filtered data shows eddy propagation
- Turbulence quantities calculated from time-lag cross-correlations

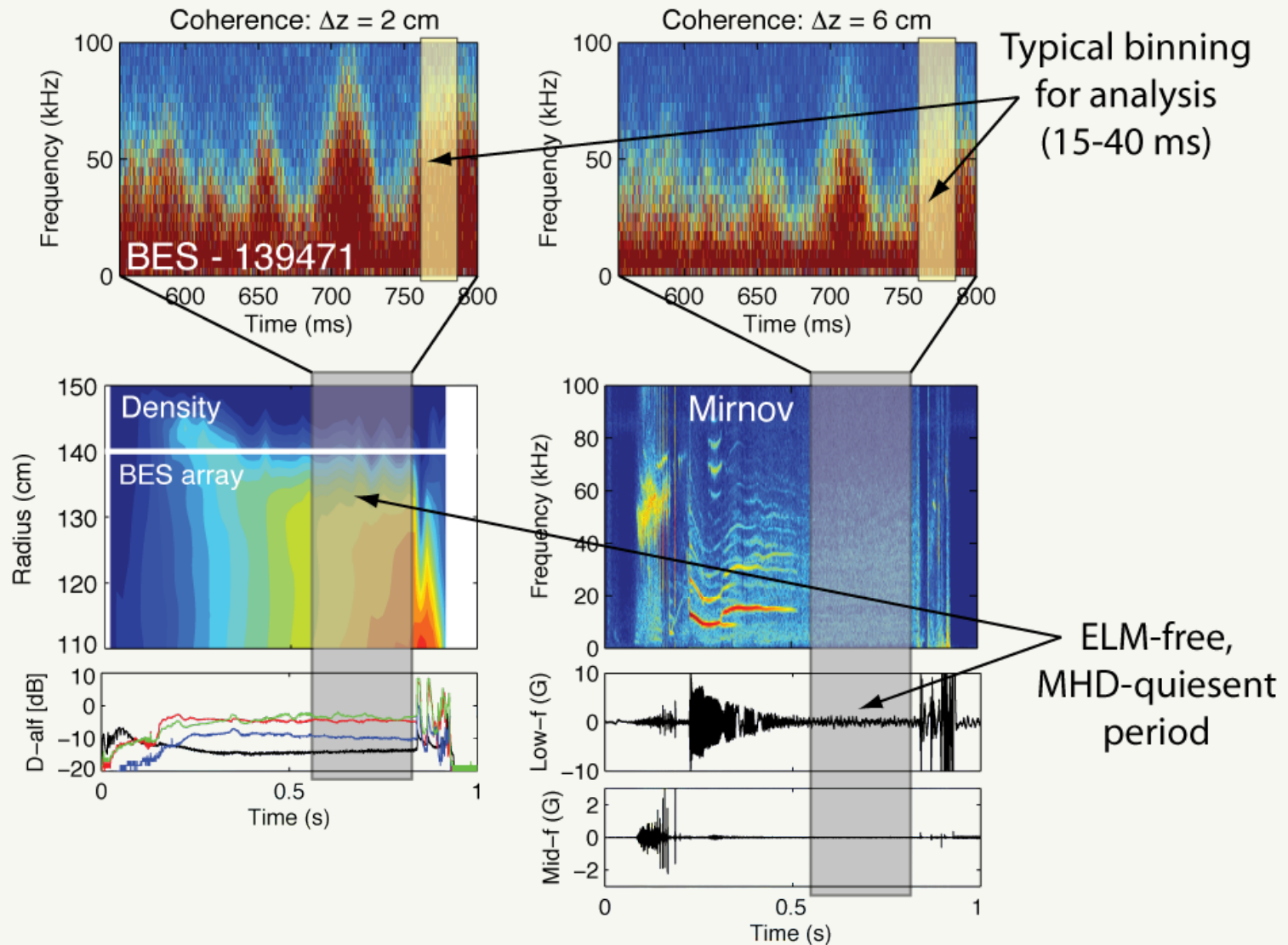
# At the LH transition, $L_{\text{pol}}$ increases and $k_{\theta}$ decreases



Also, measurements suggest eddy advection in lab frame shifts from *electron* to *ion* diamagnetic direction



# Pedestal measurements show complex turbulence activity in H-mode during ELM-free, MHD quiescent periods



# Questions about pedestal turbulence to ask and answer with BES measurements

- What are typical  $L_c$ ,  $k_\theta$ , and  $\tau_d$  values in the H-mode pedestal during ELM-free, MHD quiescent periods?
- How do  $L_c$ ,  $k_\theta$ , and  $\tau_d$  change with plasma parameters?
  - $\nabla n_e$ ,  $\nabla T_i$ ,  $q/\hat{s}$ ,  $\nu_e$ ,  $\beta_e$ ,  $n_{ped}$ , etc.
- Can we connect observations to edge turbulence simulations?
  - GEM, XGC1 or BOUT++?

# Pedestal turbulence measurements and plasma parameters from ELM-free, MHD quiescent H-modes were gathered in a database

## Database details

- 129 entries from 29 discharges

$$B_{T0} = 4.5 \text{ kG}$$

$$I_p = 700\text{-}900 \text{ kA}$$

15-45 ms averaging

- Turbulence parameters

$$L_c/\rho_i \sim 12$$

$$k_\theta \rho_i \sim 0.2$$

$$\tau_d/(a/c_s) \sim 5$$

$$\tau_d \omega_{pi}^* \sim 0.15$$

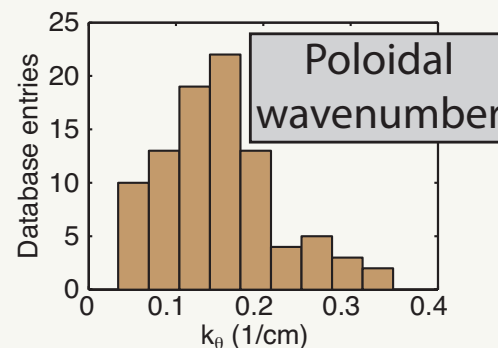
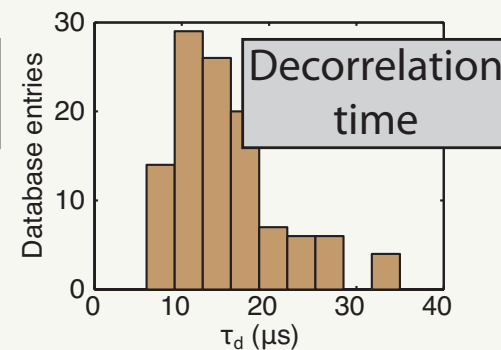
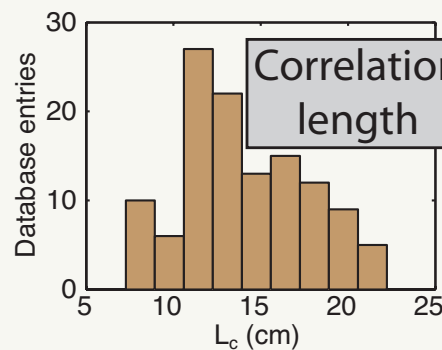
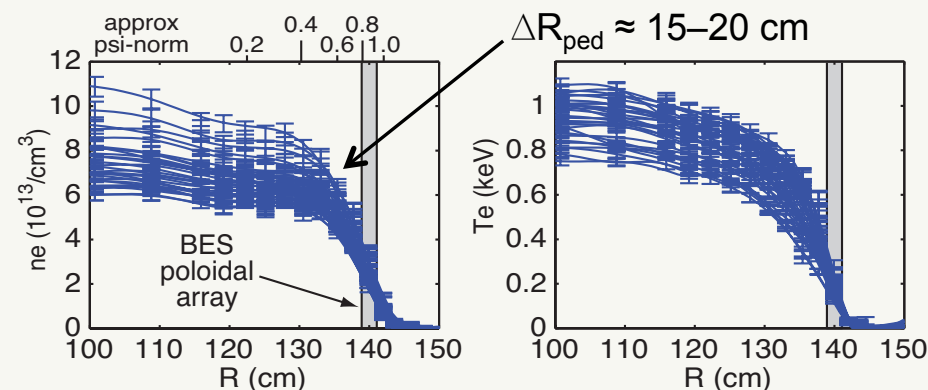
- Plasma parameters

– generally 50%-300% variation

–  $n_e, \nabla n_e, T_e, \nabla T_e, T_i, \nabla T_i, v_t,$

$\nabla v_t, q, \hat{s}, v_e, v_i, \beta, \beta_e, n_{ped},$

$\Delta R_{ped}, \delta_r^{sep}$



# A search algorithm identifies regression models; models exhibit **similar scalings** despite different parameter compositions

$$\frac{\hat{y} - \bar{y}}{\sigma_y} = \sum \alpha_k \frac{x_k - \bar{x}_k}{\sigma_{xk}}$$

turbulence parameters
scaling coefficient
plasma parameters

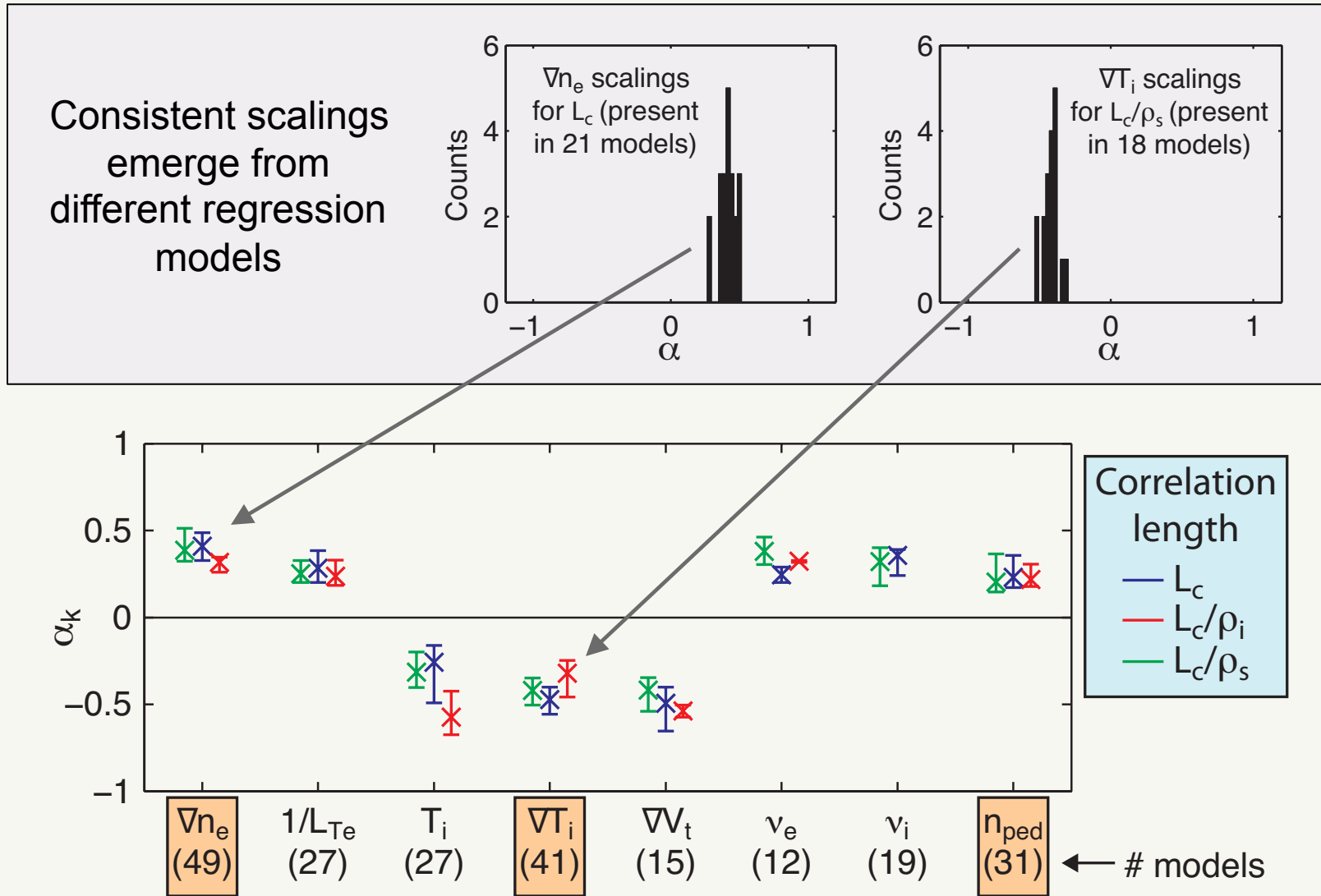
- Algorithm adds or removes  $x_k$  in model to find local minimum in model error
- Many models (local minima) exist** in high dimensional  $x_k$  space
- Screen models to ensure high statistical quality
  - Statistical significance ( $\alpha_k$  t-statistics)
  - Multicollinearity (variance inflation factor)
  - Error normality (Studentized residuals)

Regression models exhibit **similar scalings** despite different parameter compositions

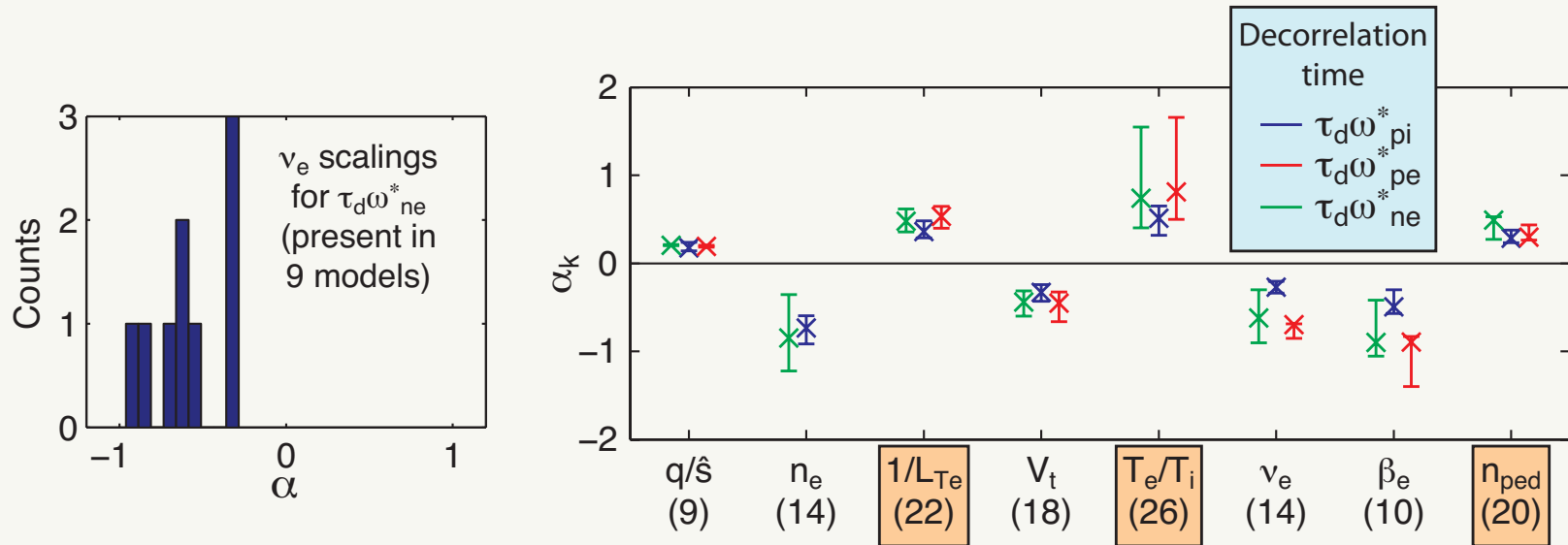
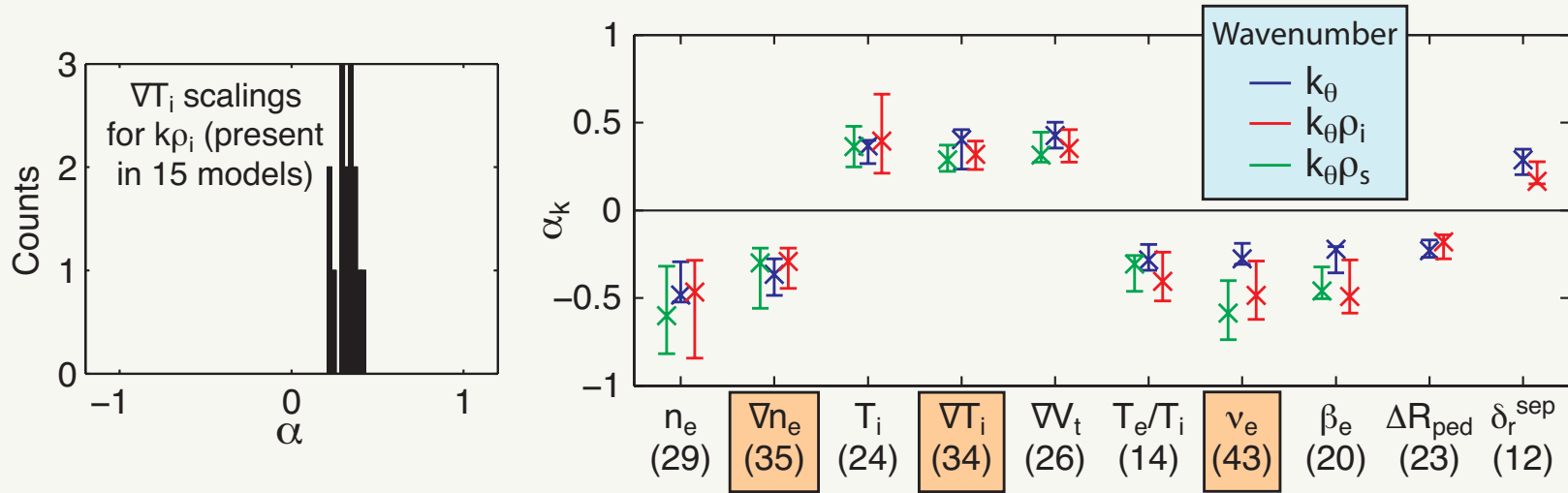
TABLE III:  $\alpha$  coefficients for a subset of  $L_c/\rho_s$  models

Model	$\alpha_k$ coefficients of parameters in model							
	$R^2$	$\nabla n_e$	$T_e$	$T_i$	$1/L_{Ti}$	$\nabla V_t$	$\nu_e$	$n_{ped}$
0.63	0.28	–	–0.20	–0.29	–	0.31	–	–
0.63	0.34	–	–	–	–0.37	0.30	–	–
0.61	0.46	–0.21	–	–	–0.38	–	–	–
0.60	–	–	–	–	–0.47	0.38	0.24	–
0.60	–	–	–0.22	–0.35	–	0.40	0.15	–
0.55	–	–0.24	–	–	–0.55	–	0.36	–

# $L_c$ increases at higher $\nabla n_e$ , $1/L_{Te}$ , $v_e$ , and $n_{ped}$ ; decreases at higher $T_i$ , $\nabla T_i$ , and $\nabla v_t$



# $k_\theta$ scalings consistent with $L_c$ scalings; $\tau_d$ scalings provide additional insight



# Parametric scalings point to **TEM turbulence** and possibly **KBM** or $\mu$ -tearing turbulence in NSTX H-mode pedestal

Parametric dependencies are ...

most consistent with **TEM turbulence**

- $\nabla n_e$  ( $L_c$  and  $k_\theta$ ) and  $1/L_{Te}$  ( $\tau_d$ ) scalings are consistent with TEM;  $T_e/T_i$  and  $v_e$  scalings show mixed agreement

partially consistent with **KBM turbulence**

- $\beta_e$  scalings ( $k_\theta$  and  $\tau_d$ ) are consistent with KBM;  $\nabla n_e$ ,  $\nabla T_i$ , and  $1/L_{Te}$  show mixed agreement

partially consistent with  **$\mu$ -tearing turbulence\***

- all  $\beta_e$  and  $v_e$  scalings are consistent with  $\mu$ -tearing, but  $1/L_{Te}$  scaling for  $\tau_d$  is inconsistent
- \* NSTX core  $\mu$ -tearing simulations indicate BES is not sensitive to  $\mu$ -tearing, but pedestal simulations show tearing-parity instabilities

least consistent with **ITG turbulence**

- $\nabla n_e$  and  $\nabla T_i$  ( $L_c$  and  $k_\theta$ ) and all  $v_e$  scalings are inconsistent with ITG;  $T_e/T_i$  scalings ( $k_\theta$  and  $\tau_d$ ) show mixed agreement

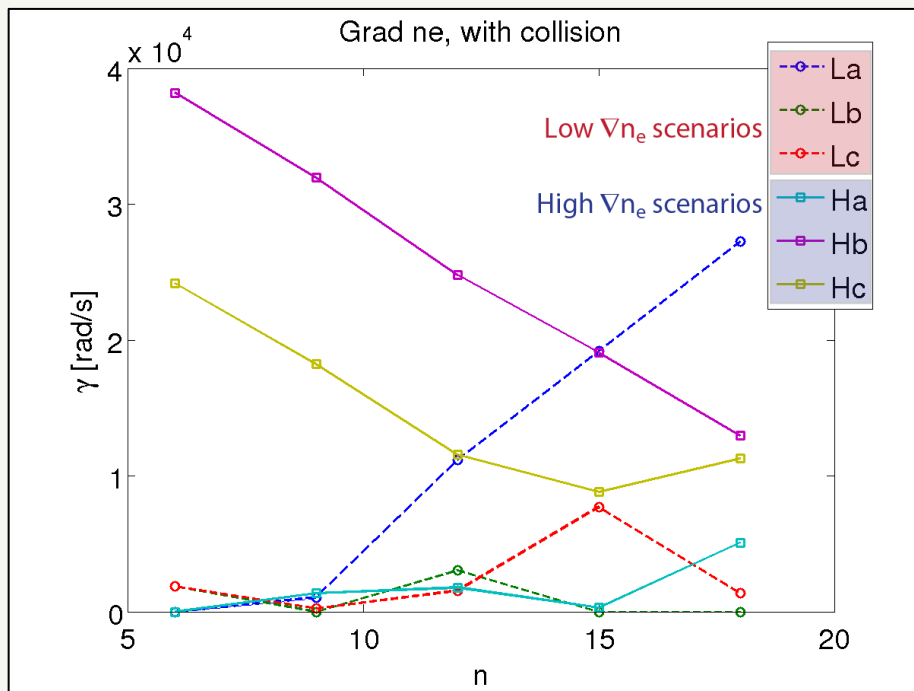
# Parametric scalings also consistent with equilibrium and zonal $E \times B$ flows

- $\nabla v_t$  scalings for  $L_c$  and  $k_\theta$  point to turbulence suppression by **equilibrium  $E \times B$  flow shear**
  - $L_c$  decreases and  $k_\theta$  increases at higher  $\nabla v_t$
- Collisionality scalings are consistent with turbulence reduction via **zonal flows**
  - $\tau_d$  decreases and  $L_c$  increases at higher  $\nu$
- **Pedestal height** ( $n_{ped}$ ) increases at larger  $L_c$  and  $\tau_d$ 
  - Consistent with empirical relationship between wider pedestals and larger turbulent structures (Z. Yan et al., PoP 18, 056117 (2011))

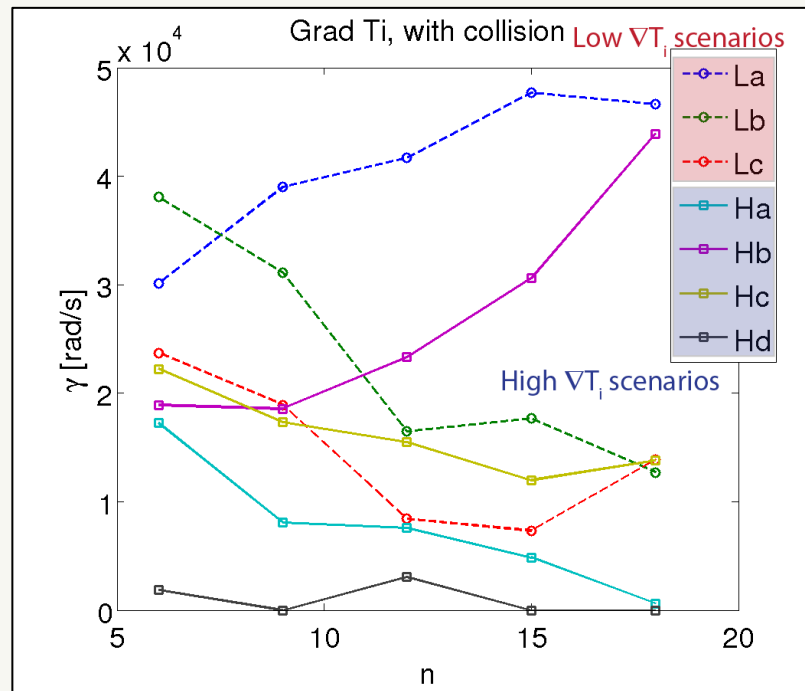


# Linear growth rates from GEM gyrokinetic simulations show scalings consistent with measured $L_c$ scalings

GEM simulations with  $6 \leq n \leq 15$  and  $k_\theta \rho_s \sim 0.2$  indicate instabilities are **electromagnetic**, destabilized by **collisions**, and exhibit both **ballooning** and **tearing parity**



5 of 6  $\nabla n_e$  scenarios indicate low-n growth rates increase at higher  $\nabla n_e$

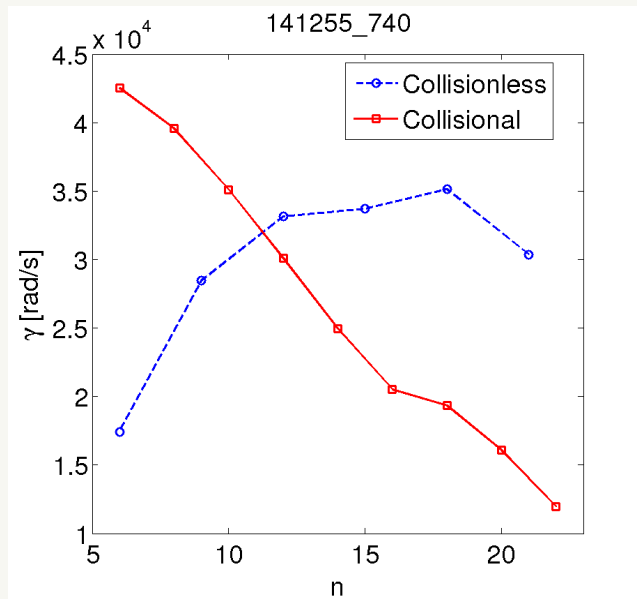


7 of 7  $\nabla T_i$  scenarios indicate low-n growth rates decrease at higher  $\nabla T_i$

GEM  $\gamma$  dependencies on  $\nabla n_e$  and  $\nabla T_i$  are consistent with measured  $L_c$  scalings

# GEM simulations point to tearing parity mode structures and highlight the importance of collisions

With collisions,  $\gamma$  rises at low- $n$  and drops at high- $n$



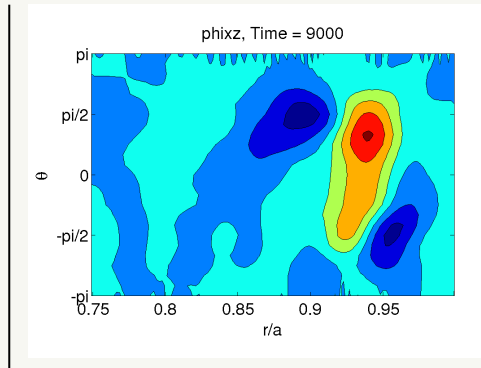
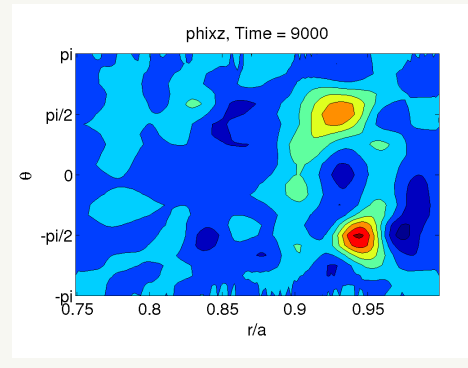
Consistent with measured scalings that show higher  $L_c$  and lower  $\tau_d$  at higher  $\nu$

$\phi$  contours

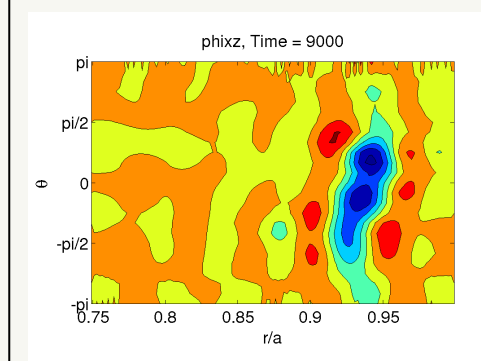
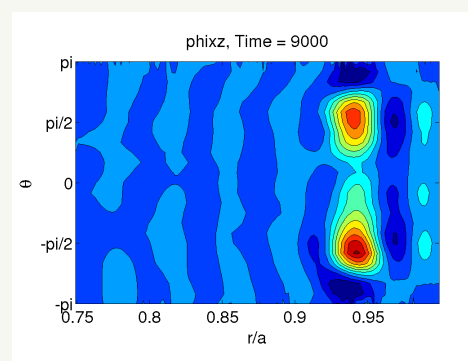
Collisionless

Collisional

$n=6$



$n=24$

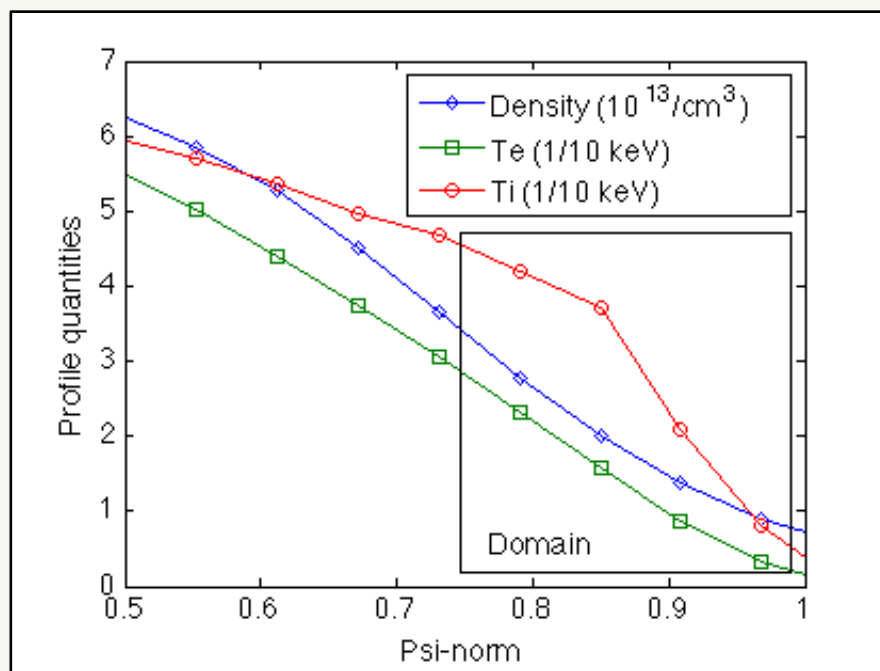


even parity

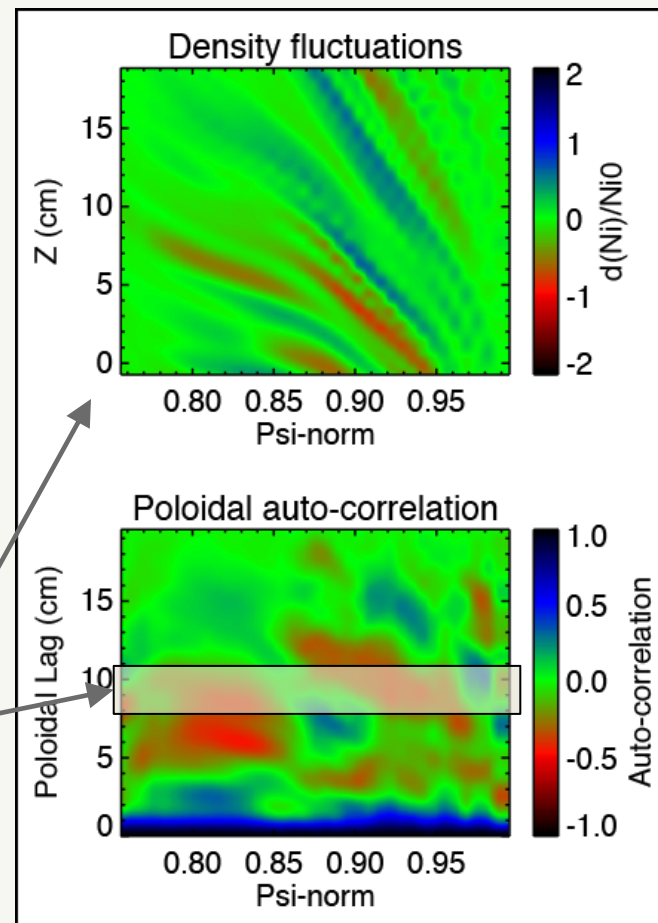
likely tearing parity

# $L_c$ and $k_\theta$ from BOUT++ pedestal simulations compare favorably with measurements

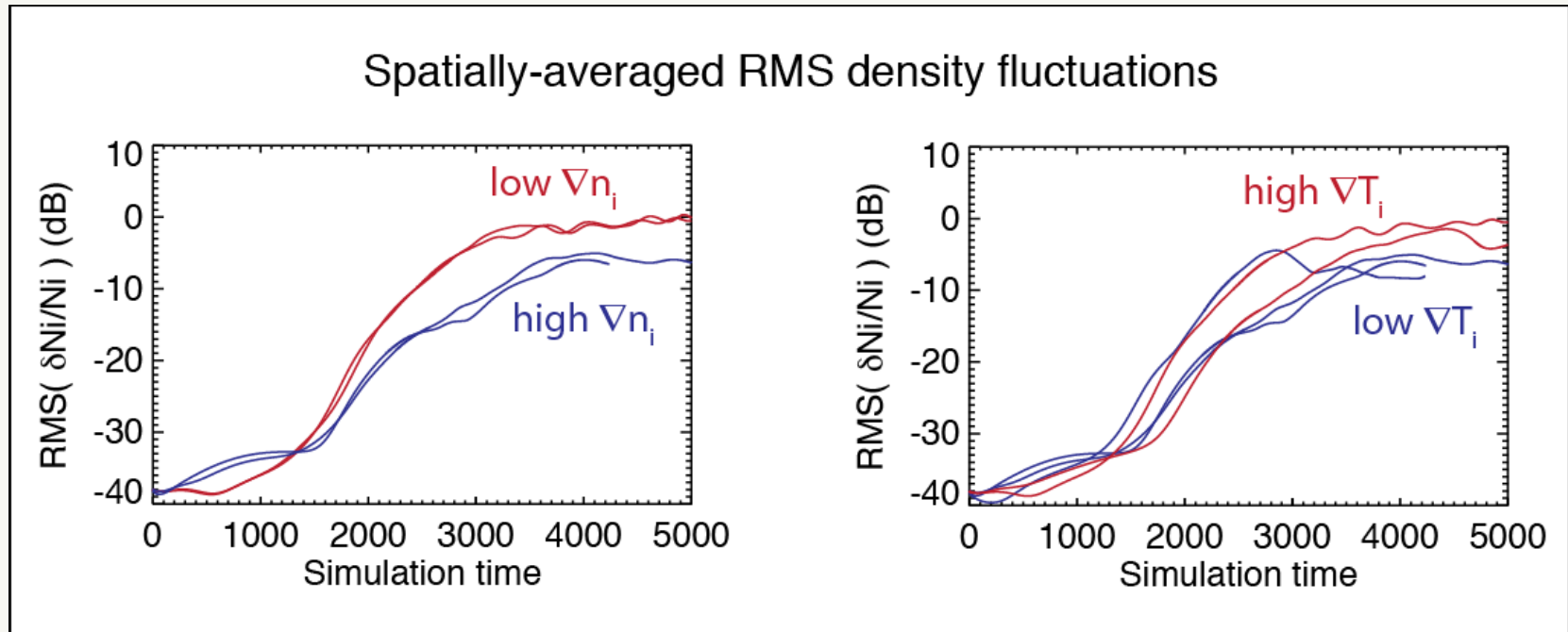
Initial value 3D Braginskii fluid simulations evolve  $n_i$ ,  $\omega$ ,  $j_{\parallel}$ ,  $A_{\parallel}$ ,  $T_i$ , and  $T_e$  with collisionality,  $E \times B$  advection, field line curvature, and drive terms for  $j_{\parallel}$  and  $\nabla P$ . Simulations do not include toroidal rotation and parallel advection.



$L_c/\rho_i \sim 8$  is in line with measurements, but  $k_\theta \rho_i \sim 0.7-1.4$  is higher than measurements



# BOUT++ parameter scans point to larger fluctuation amplitudes at **lower** $\nabla n_i$ and **higher** $\nabla T_i$



Note that measurements indicate  $L_c$  increases at **higher**  $\nabla n_i$  and **low**  $\nabla T_i$

# Future work

- Fluctuation amplitudes
  - Radial dependence
  - Parametric dependencies
- Radial correlation length analysis
- Radial and poloidal wavenumber spectra
- Flow fluctuations and time-delay estimation
  - Predator-prey model between flow fluctuations and turbulence parameters
- Fluid simulations with parallel advection and  $V_{\text{tor}}$

# Summary

- Pedestal model validation is critical for ITER, and ST edge parameters are among the most challenging regimes for turbulence simulations
- We measured pedestal turbulence parameters in NSTX H-mode plasmas during ELM-free, MHD quiescent periods
  - $L_c/\rho_i \sim 12$        $k_\theta \rho_i \sim 0.2$        $\tau_d/(a/c_s) \sim 5$
- Parametric dependencies for pedestal turbulence measurements are most consistent with **TEM turbulence** and partially consistent with **KBM and  $\mu$ -tearing turbulence**
- **GEM** gyrokinetic simulations show higher  $\gamma$  at higher  $\nabla n_e$  and lower  $\nabla T_i$   
→ **consistent** with measured  $L_c$ 
  - Collisions increase  $\gamma$  at low- $n$  → **consistent** with measured scalings
- **BOUT++** Braginskii fluid simulations show **saturation amplitudes** that decrease with  $\nabla n_i$  and increase with  $\nabla T_i$  → not consistent with scalings

# Pedestal turbulence measurements

# Pedestal turbulence parametric dependencies in ELM-free, MHD quiescent H-modes



# Preliminary pedestal turbulence simulations (gyrokinetic and Braginskii fluid)