

Two-dimensional Hell Doppler shift image measurement in QUEST

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Introduction

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- Visible (or converted visible) light emission of two-dimensional profile is easily obtained by fast cameras, and the technology progress of the fast camera during recent decade is amazing.
- Fast cameras on many devices had shed much new light on the complex nature of plasma phenomena.
- And now, the qualitative analysis are needed to treat the image data.

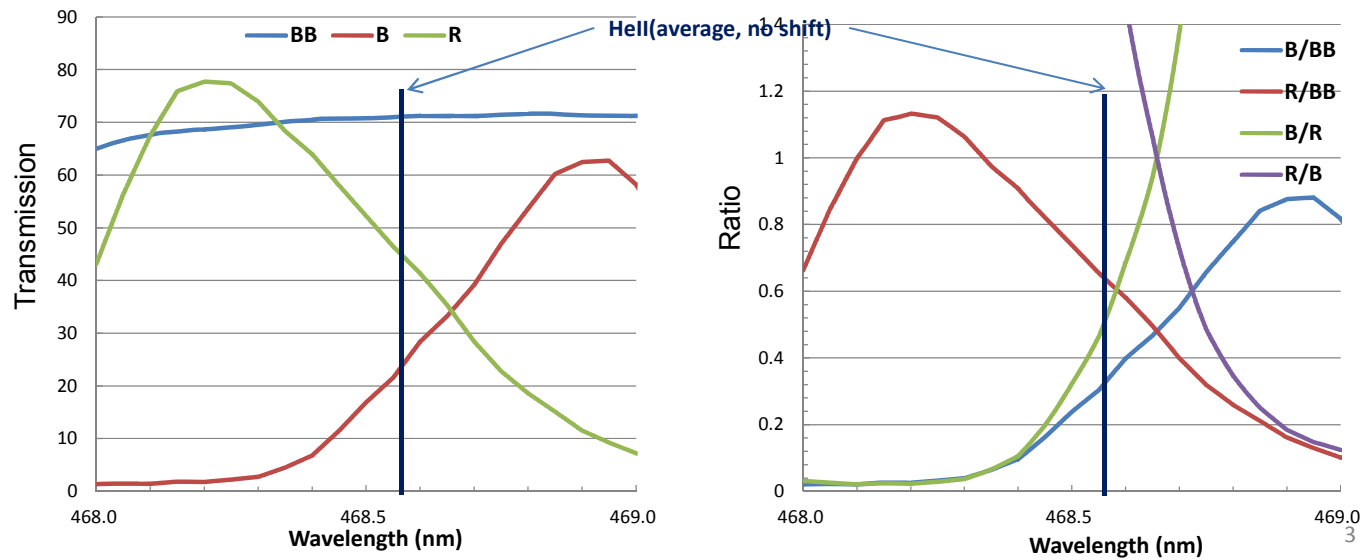
- On the other hand,
- 2D Ion flow (or ion velocity) profile is also very useful information for understanding plasma physics.
- However, 2D ion flow profile measurement is not fully developed up to now.

- SWIFT (Shifted Wavelength/Interference Filter Technique) is easy to extend to 2D measurement for getting the ion flow profile.
- Therefore, this time we tried to measure Hell Doppler shift along the toroidal direction in QUEST plasma using a fast camera, several optical filters for Hell and an image intensifier.
- The original idea is SWIFT, and we modify this method.

Principle of Doppler shift measurement

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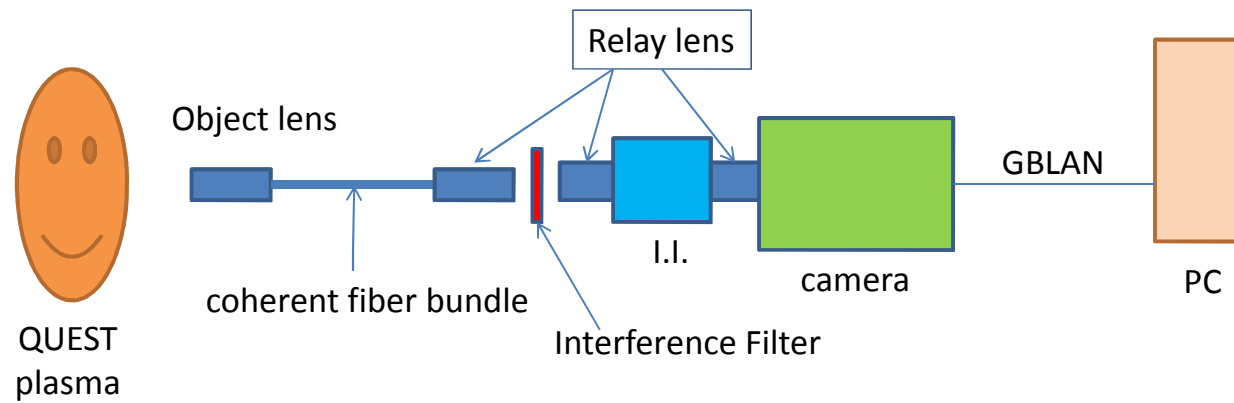
- Target line is HeII (this time).
- Various IF for target line are used (Blue edge, Red edge, Broad-Band at this time).
- The transmission of each filter depends on the wavelength.
- If the ratio of the transmission of each filter is a single-valued function of the wavelength, Doppler shift will be determined.



Fast camera with the Image Intensifier

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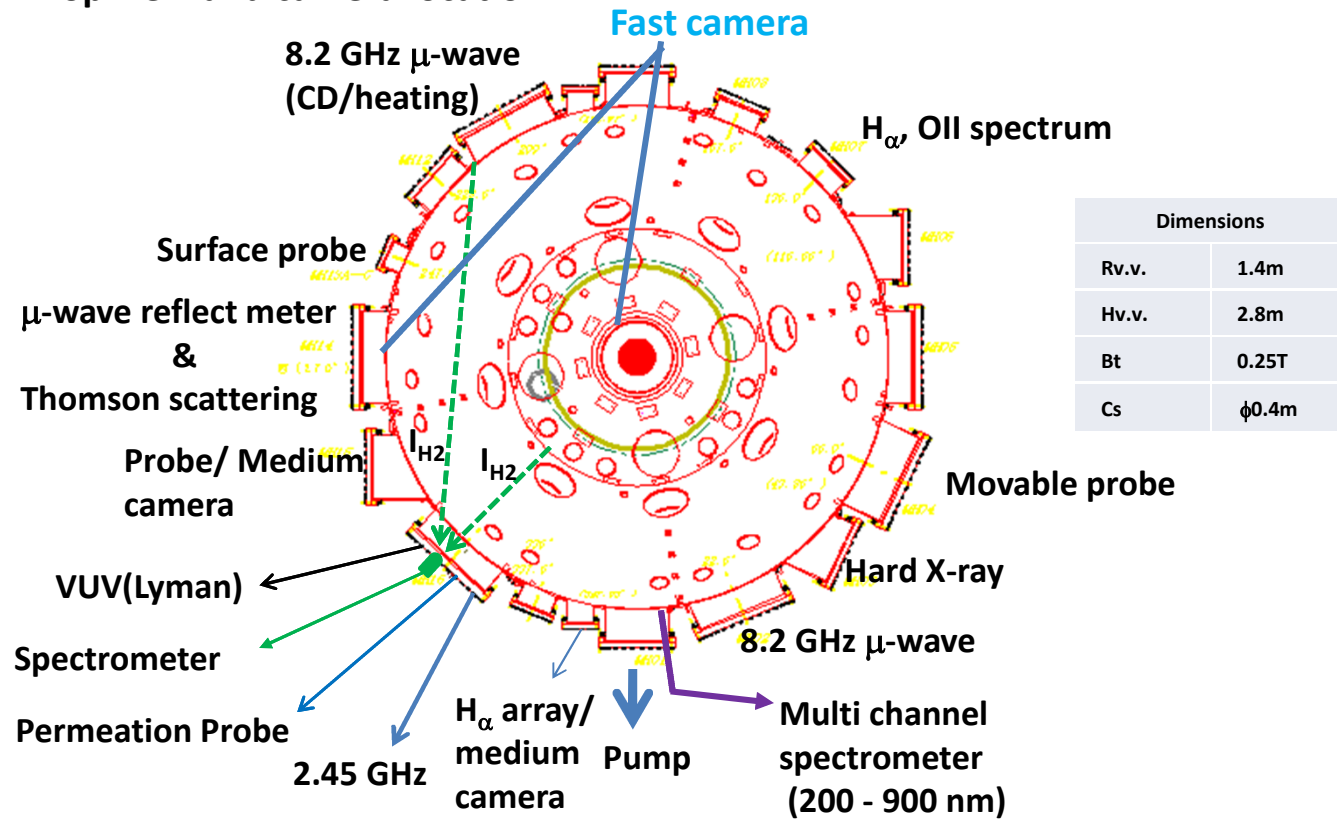
- A coherent fiber bundle was used for wide application.
- The image intensifier was used due to lack of photons.



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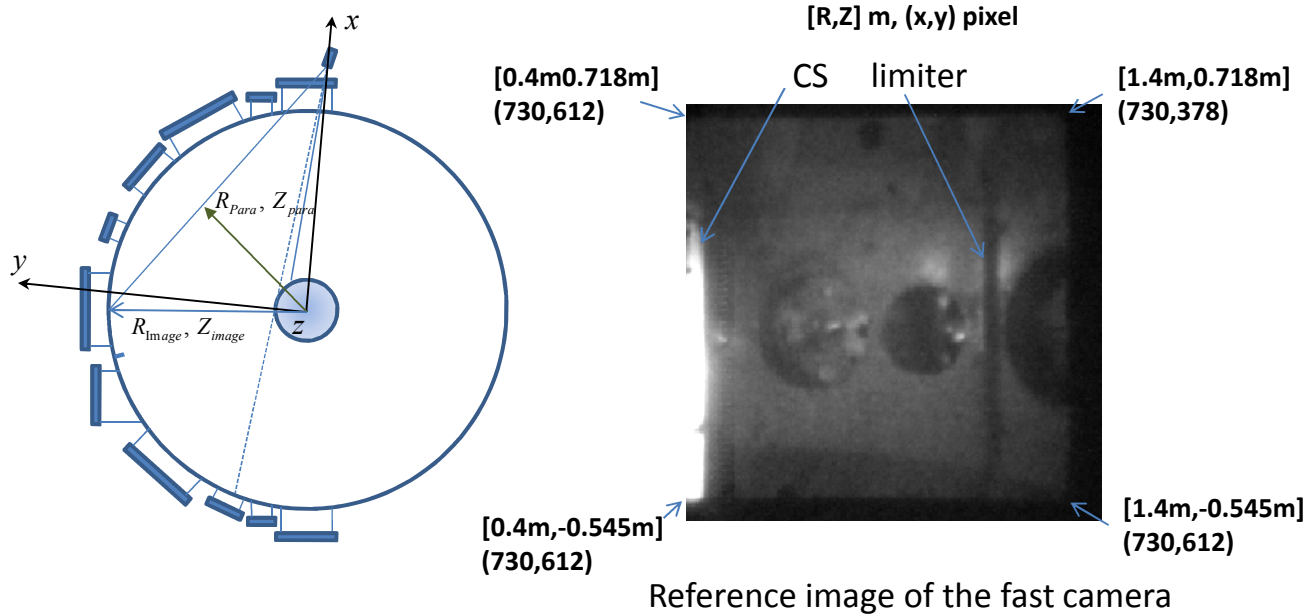
- Top view and camera location



Description of the coordinates for analysis

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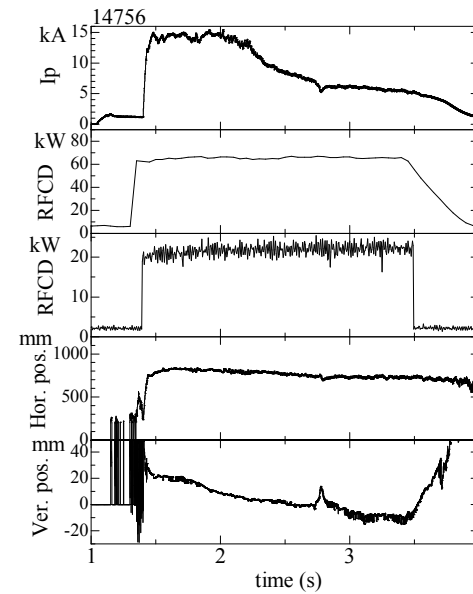
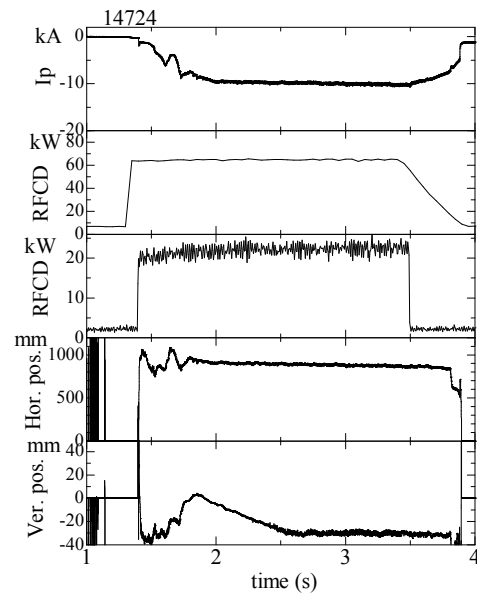
- The location of the fast camera is set to x-axis, and the center of the center stack is the origin.
- Z-axis is height, and right-hand side coordinate is used.



QUEST PLASMAS

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- Waveforms of RF current drive plasmas, two samples are shown.
- Normal $I_p < 0$.

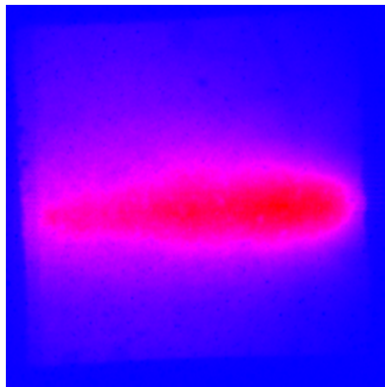


Images with optical filters – Normal I_p –

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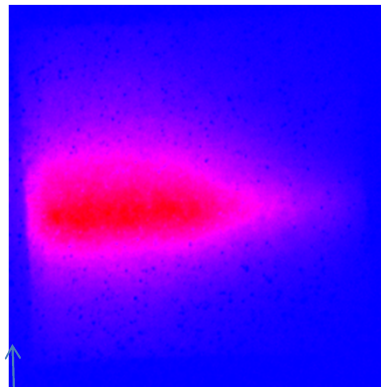
- Measurement was done with shot by shot due to single camera.
- #14724-#14726, $I_p = -10\text{kA}$, raw image (average of 0.1s images), 1000FPS

#14724, 2.0-2.1s average



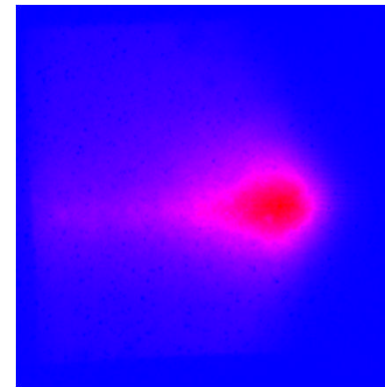
BB filter

#14725, 2.0-2.1s average

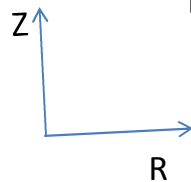


R filter

#14726, 2.0-2.1s average



B filter



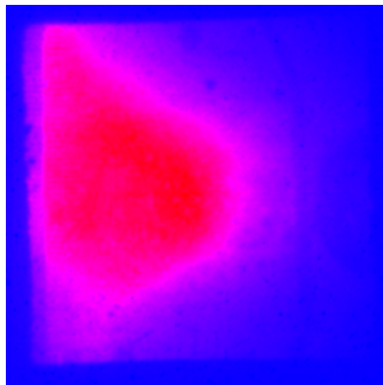
The average of 100 images is taken to remove noise. Intensity is auto scale.
Plasma image is tilted a little, but the size is the same as that of the reference.

Images with optical filters – Reversed Ip –

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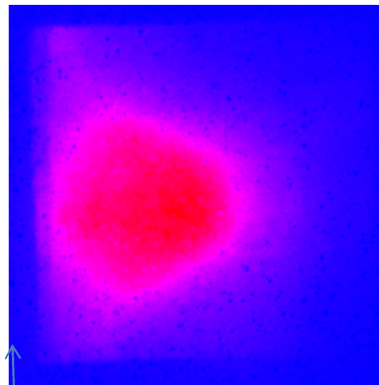
- #14756-#14758, $I_p=15\text{kA}$, raw image (average of 0.1s images), 1000FPS

#14758, 1.6-1.7s average



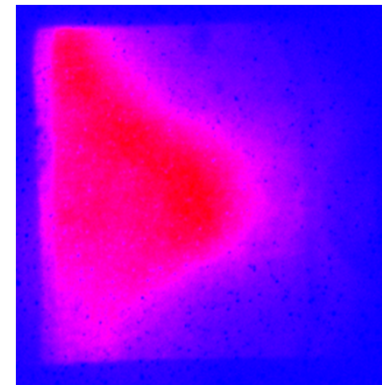
BB filter

#14756, 1.6-1.7s average

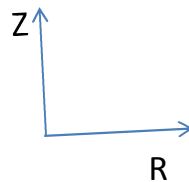


R filter

#14757, 1.6-1.7s average



B filter

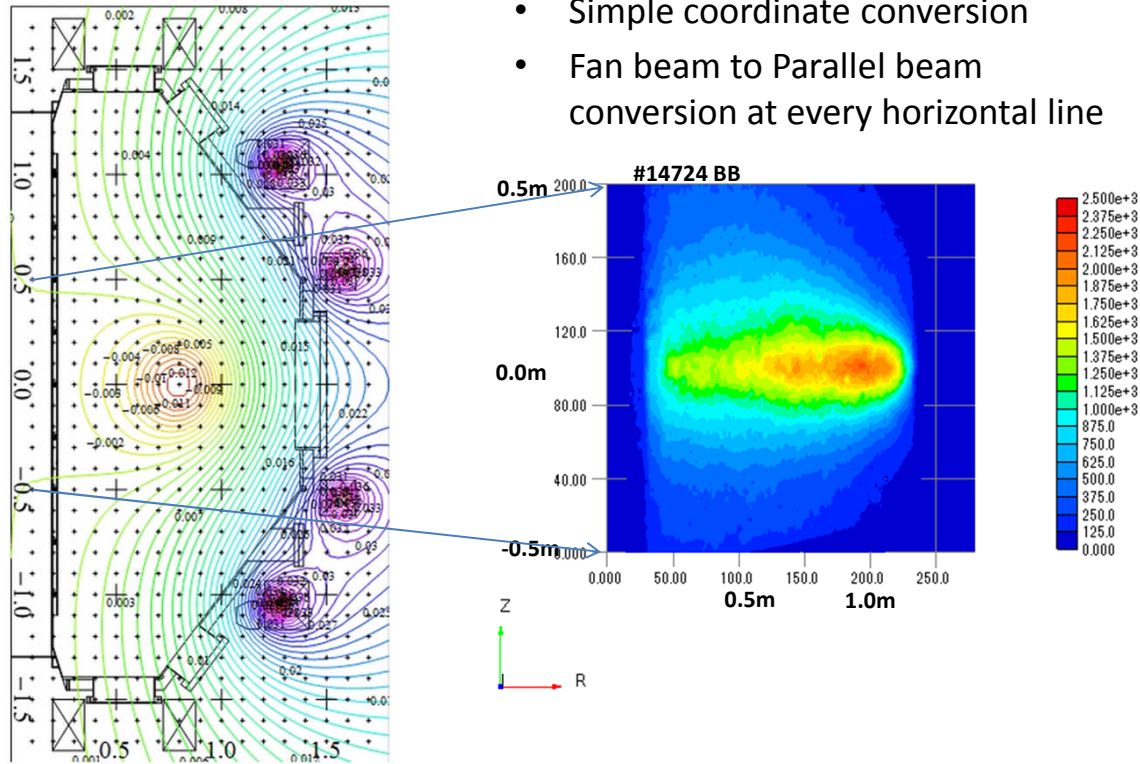


The average of 100 images is taken to remove noise. Intensity is auto scale.
Plasma image is tilted a little, but the size is the same as that of the reference.

Hell emission profile and magnetic flux cal.

- #14724 Limiter configuration (normal Ip)

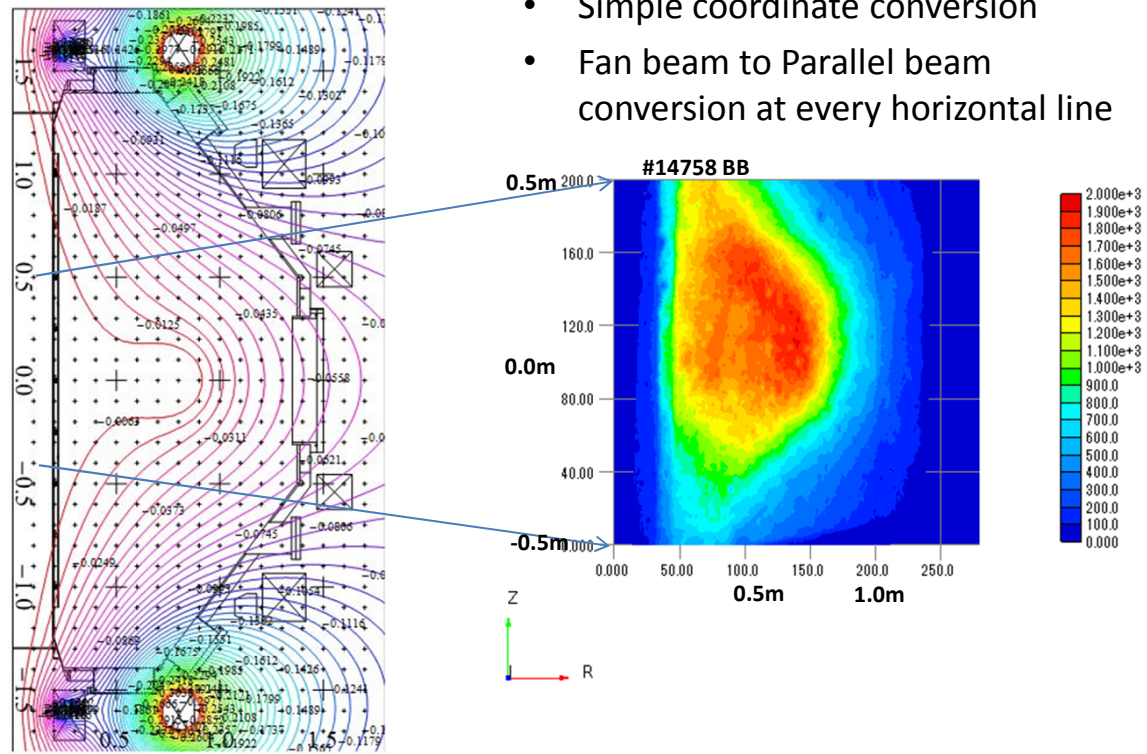
- Simple coordinate conversion
- Fan beam to Parallel beam conversion at every horizontal line



Hell emission profile and magnetic flux cal.

- #14756 Inner null configuration (reversed Ip)

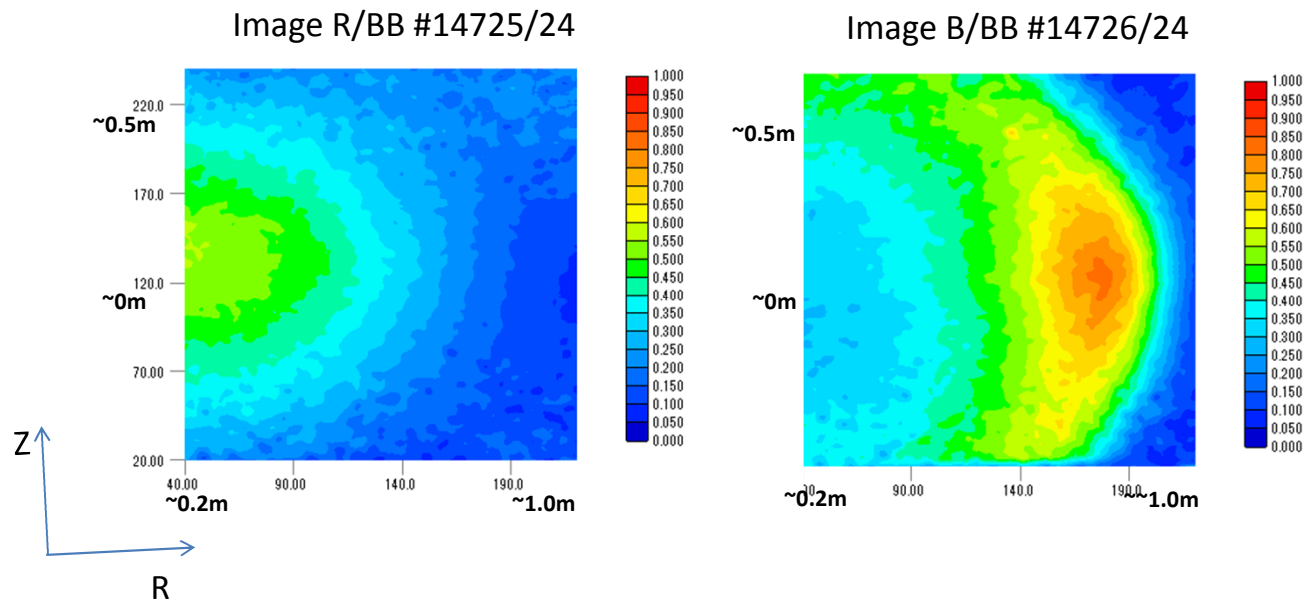
- Simple coordinate conversion
- Fan beam to Parallel beam conversion at every horizontal line



Ratio image with R, B, BB

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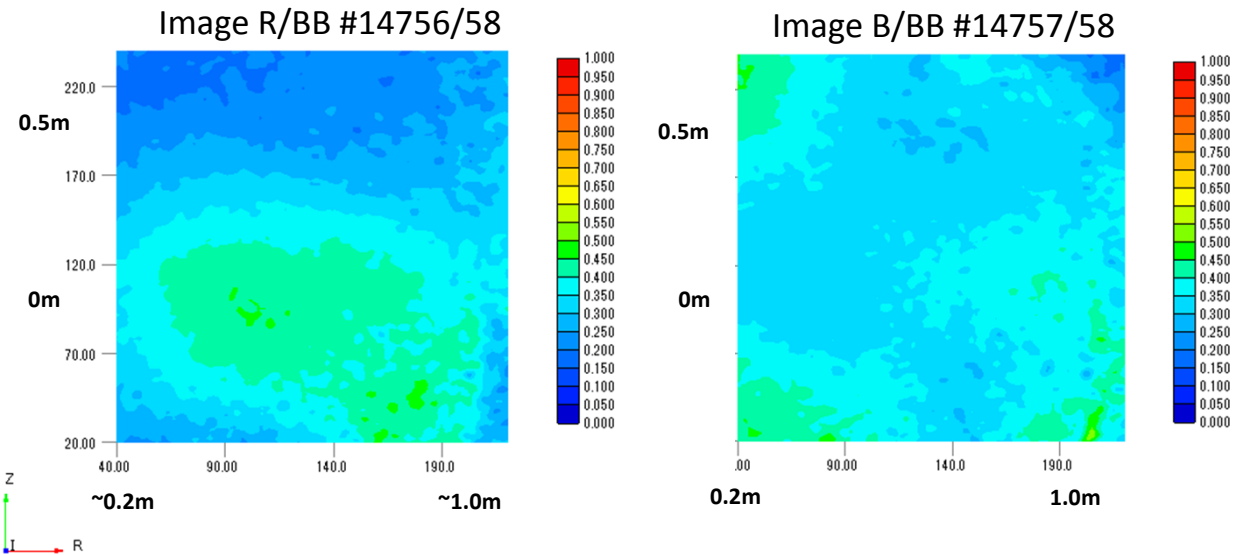
- Using the average raw image (R/BB and B/BB image)
- Limiter configuration (normal Ip)



Ratio image with R, B, BB

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- Using the average raw image (R/BB and B/BB image)
- Inner null configuration (Reverse Ip)



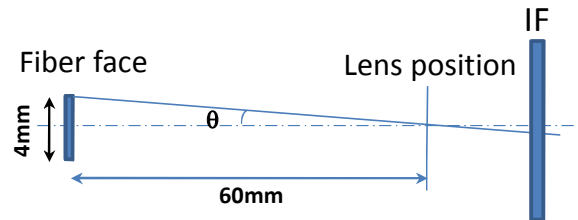
How to convert the image taken by this system to ion flow map

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- Even though target plasma was thin ($\sim 10^{18}\text{m}^{-3}$), using Image Intensifier and fast camera with 1000 FPS Hell emission profile was observed.
- It seems that the ratio of Hell emission using various filters and time average of 0.1s were useful.
 - Conversion of fan beam to parallel beam may be useful.
 - Hell emission patterns were different in two types of discharges.
- To estimate the Ion velocity from these images, the calibration procedure is needed to get zero ion flow (offset).
- An idea is that plasma of no current may give us the offset information on Hell flow.
- Before this procedure the incident angle dependence should be included.

Transmission dependence of the Incident angle

- Transmission of IF depends on the incident angle.
- Focal length of the lens at the fiber exit is $\sim 60\text{mm}$, and the fiber face size is $4 \times 4\text{mm}$, and the size of each fiber is $10\mu\text{m} \times 10\mu\text{m}$.



- There is well known formula on the wavelength shift due to the incident angle.

$$\lambda = \lambda_{\max} \sqrt{1 - \left(\frac{n_0}{n_e} \sin \theta \right)^2}$$

- Therefore, transmission of the same wavelength should be the concentric circle in the image.

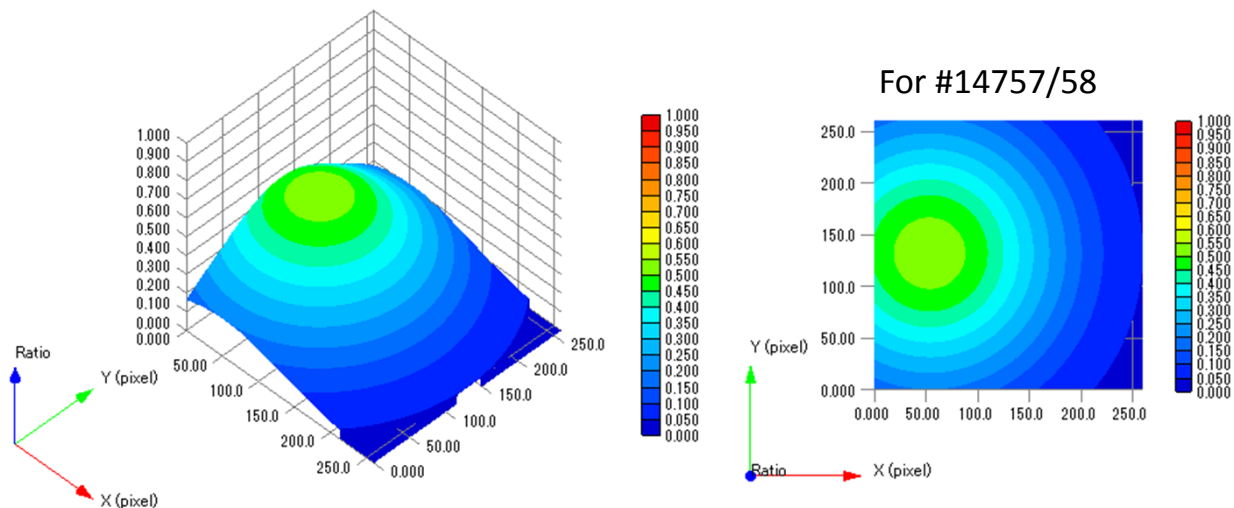
$$\Delta\lambda = \lambda_{\max} \left[1 - \sqrt{1 - \left(\frac{n_0}{n_e} \right)^2 \left(1 - \frac{1}{\tan^2 \theta} \right)} \right], \quad \tan \theta = \frac{0.01X(\text{fiber})}{60}$$

$$\text{if } \theta \ll 1, \quad \Delta\lambda \approx \frac{1}{2} \left(\frac{n_0}{n_e} \frac{0.01}{60} \right)^2 \lambda_{\max} X^2, \quad \sin \theta \approx \tan \theta$$

Calibration curve (surface)

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- According to the previous formula, the transmission calibration curve was made. Typical calculation result is shown .
- The incident angle to the pixel depends on the length between the pixel and the optical center of IF.
- As a results, on the top view the concentric circle was given under the assumption of that BB filter has no effect on the incident angle.

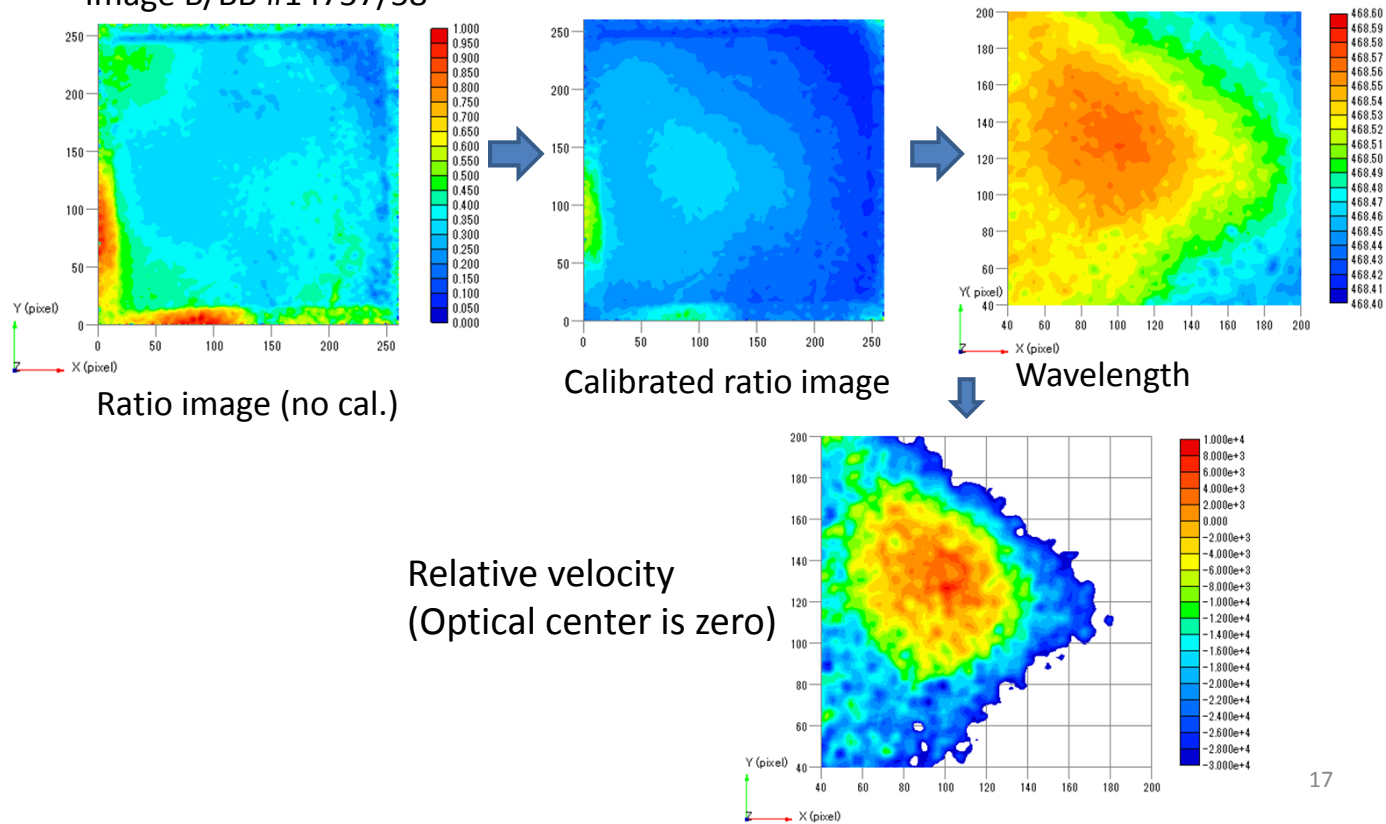


Convert to wavelength, velocity information - Inner null configuration -

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- Use calibration curve and convert the ratio image to wavelength image.

Image B/BB #14757/58

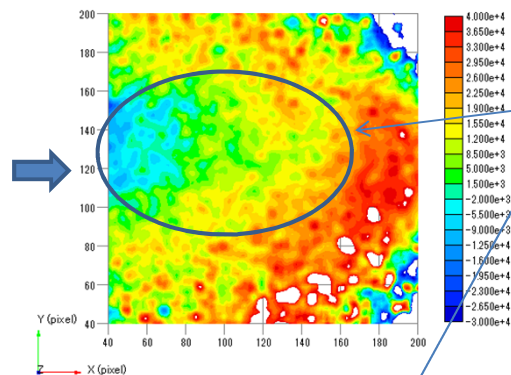
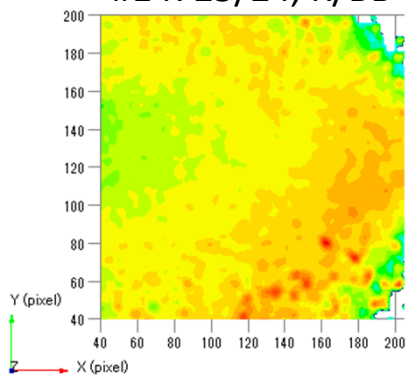


Wavelength, velocity information

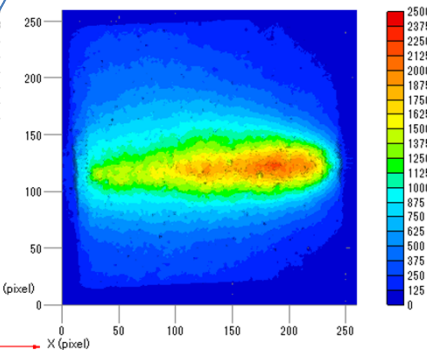
- Limiter configuration -

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- #14725/24, R/BB

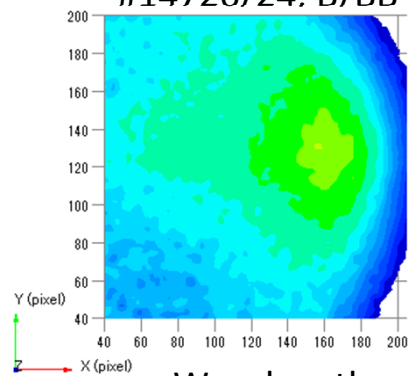


Bright region

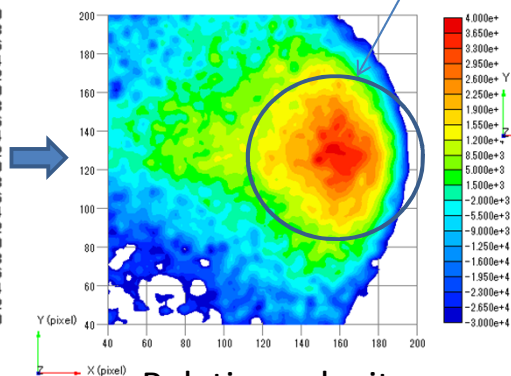


Hell emission

- #14726/24, B/BB



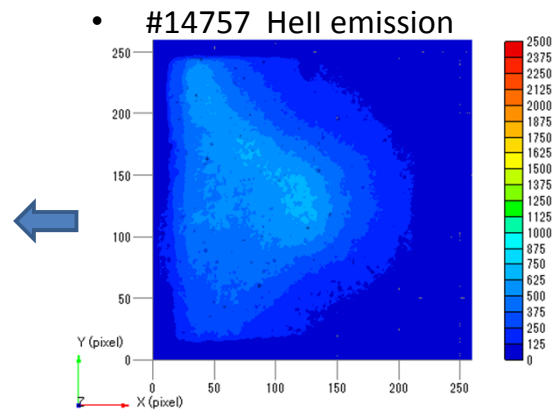
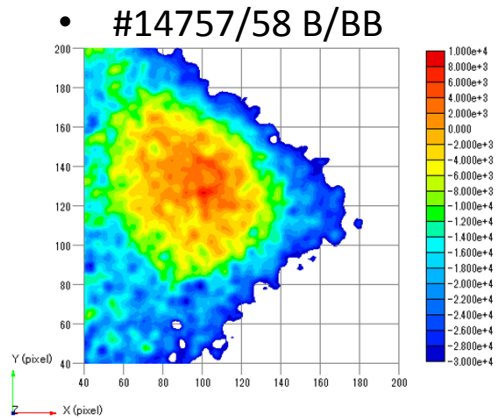
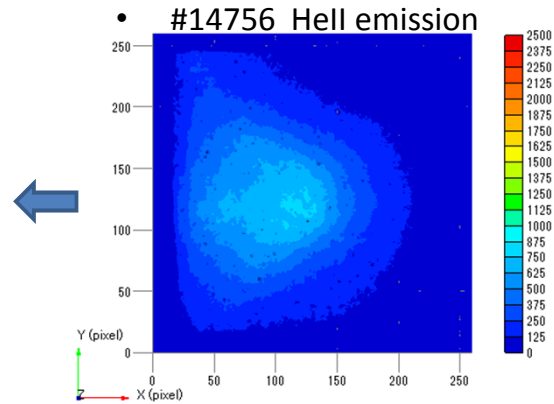
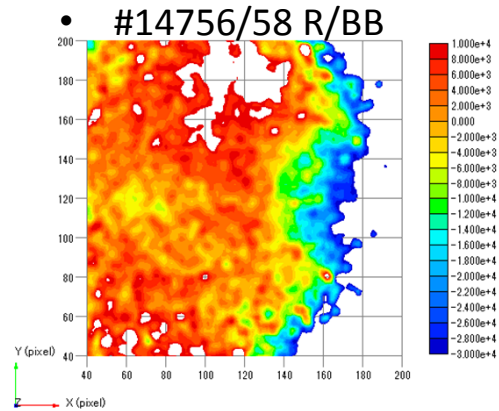
Wavelength



Relative velocity

Velocity information - Inner null configuration -

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Relative velocity

Discussion

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- Wavelength (velocity) profile obtained by this measurement is somewhat larger than that expected, because RF CD plasma was used here.
- This may be caused by
 - Adjustment ← IF was changed by manual
 - Lack of photons
 - Accuracy of the transmission curve of IF?
- Steps to improvement
 - Use more precise optical equipment
 - Take Longer average time at steady state plasma
 - or get high density plasma
 - Check the transmission curve
 - or Use other IF?

Conclusion

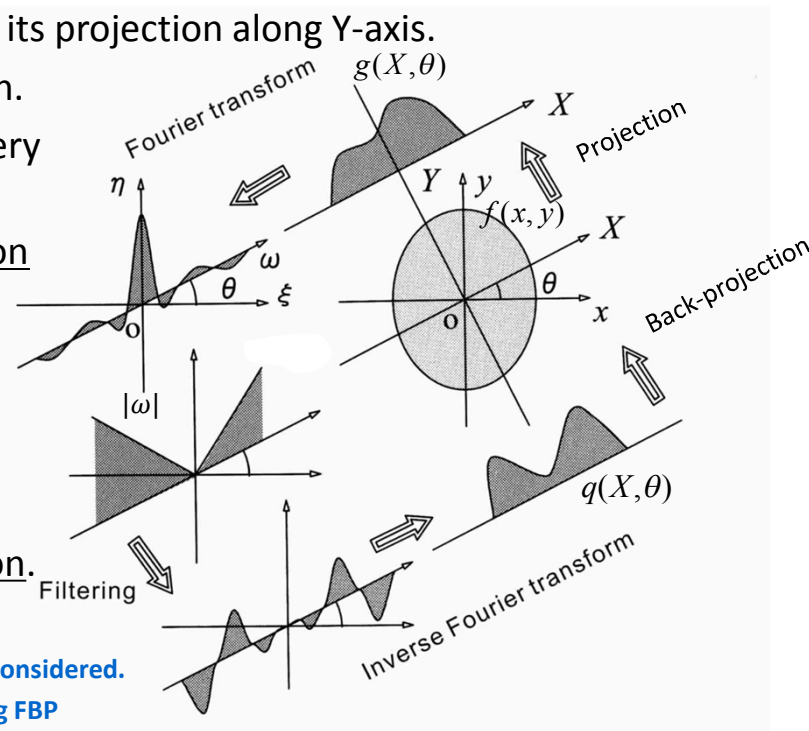
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- Two dimensional ion flow measurement system using Hell optical filters was demonstrated in QUEST.
- Under several plasma conditions with He gas puff the various ion flow profiles were observed (two cases were shown).
 - The obtained ion flow profile seemed to change with the magnetic configuration.
 - However, calculated ion velocity has somewhat ambiguity, and the reference light source (zero ion flow) is needed.
- In the near future we will improve this system with taking precise adjustment and performing the elaborate calculation.
 - To get ion flow profile from the images FBP method will be used with the assumption of toroidal symmetry.

FBP (Filtered Back-Projection) Method

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- FBP is well known method and it is widely used as the reconstruction method of CT in the medical field to resolve the original object.
- $f(x,y)$ is the object, and $g(X,\theta)$ is its projection along Y-axis.
- $|\omega|$ is used as the filter function.
- It is very simple, and also it is very fast using FFT.
- Use FBP to get the initial solution for 2D line emission profile.
- Central horizontal line of the image reconstructed by FBP should be the exact solution.
- At other lines in the image give us an approximated solution.
- **The effect of the elevation angle should be considered.**
- **Need fan-para beam conversion before using FBP**



Description of FBP method

- Projection $g(X, \theta)$ is the line integral of $f(x, y)$

$$g(X, \theta) = \int_{-\infty}^{\infty} f(x, y) dY$$

- Double Fourier Transform of $f(x, y)$ is

$$F(\xi, \eta) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) e^{-i(\xi x + \eta y)} dx dy \quad \begin{cases} \xi = \omega \cos \theta \\ \eta = \omega \sin \theta \end{cases}$$

$$= F(\omega \cos \theta, \omega \sin \theta) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) e^{-i\omega(x \cos \theta + y \sin \theta)} dx dy$$

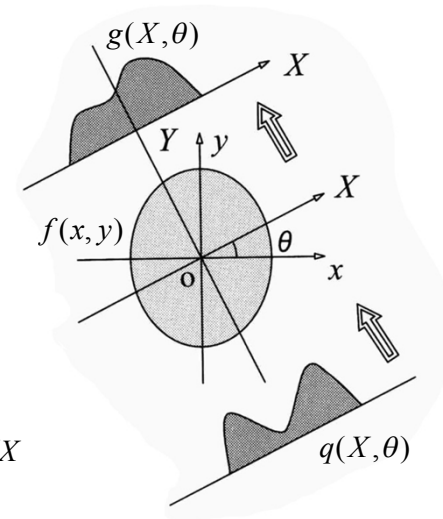
$$X = x \cos \theta + y \sin \theta, \quad dx dy = dX dY$$

$$= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) e^{-i\omega X} dX dY = \int_{-\infty}^{\infty} \left[\int_{-\infty}^{\infty} f(x, y) dY \right] e^{-i\omega X} dX = \int_{-\infty}^{\infty} g(X, \theta) e^{-i\omega X} dX$$

$$f(x, y) = \frac{1}{(2\pi)^2} \int_0^{2\pi} \int_0^{\infty} F(\omega \cos \theta, \omega \sin \theta) e^{i\omega(x \cos \theta + y \sin \theta)} \omega d\omega d\theta = \frac{1}{2(2\pi)^2} \int_0^{2\pi} \int_{-\infty}^{\infty} F(\omega \cos \theta, \omega \sin \theta) e^{i\omega X} |\omega| d\omega d\theta$$

$$q(X, \theta) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \left[\int_{-\infty}^{\infty} g(X, \theta) e^{-i\omega X} dX \right] |\omega| e^{i\omega X} d\omega \quad \text{filtering}$$

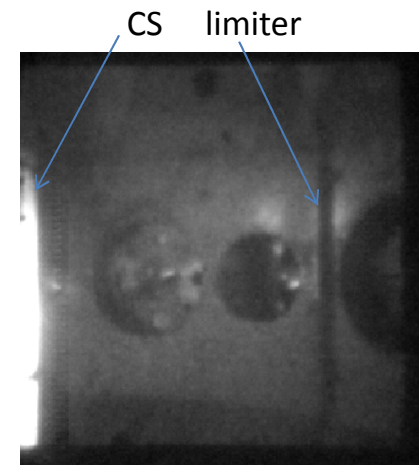
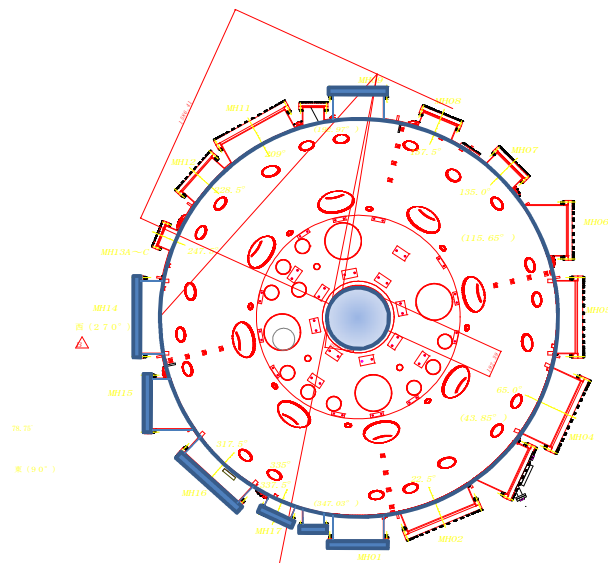
$$f(x, y) = \frac{1}{4\pi} \int_0^{2\pi} q(X, \theta) d\theta \quad \text{Back-projection}$$



Description of the coordinates for analysis

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- The location of the fast camera is set to x-axis, and the center of the center stack is the origin.
- z-axis is height, and right-hand side coordinate is used.



Reference image of the fast camera

