



# Full Wave Simulations of Fast Wave Scrape-off Layer Losses of NSTX/ NSTX-U and a Comparison with DIII-D/C-Mod/EAST

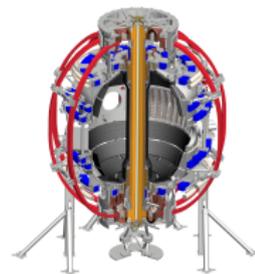
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- Motivations
- AORSA simulations including SOL plasma for NSTX and NSTX-U
  - Brief description of the full wave code AORSA
  - Computation of SOL power losses vs. edge density in NSTX with “collisional” damping as a proxy
  - NSTX-U case projections
- Extension to “conventional” tokamaks with higher aspect ratio
  - DIII-D (mid/high harmonic fast wave regime)
  - Alcator C-Mod and EAST (IC minority heating regime)
- Discussion
  - IC minority heating vs. HHFW regime
  - Magnetic pitch angle
- Conclusions and future plans

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## Previous NSTX studies of heating efficiency showed large amounts of HHFW power missing from plasma core

- Interaction between the RF antennas and the SOL plasma is of crucial importance in determining the overall performance of RF in a tokamak
  - all frequencies: LH, IC, HHFW, . . . , and helicon waves
- In NSTX:
  - Strong interactions between HHFW and SOL plasma [Hosea PoP 2008, Perkins PRL 2011]
  - Up to 60% of the power possibly lost to SOL
  - Larger SOL losses for high density in front of the antenna
- Other machines (Alcator C-Mod, ASDEX-U, EAST, JET, Tore Supra, . . . )
  - Impurity contamination & transport
  - Impact of RF on SOL plasma
  - . . .

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# Full wave code AORSA: wave field modeled with linear wave equation

- Full field wave equation:  $\nabla \times \nabla \times \mathbf{E} - \frac{\omega^2}{c^2} \boldsymbol{\varepsilon} \cdot \mathbf{E} = 4\pi i \frac{\omega}{c^2} \mathbf{J}_{\text{ext}}$
- AORSA includes the complete non-local, integral operator for  $\boldsymbol{\varepsilon}$  that is valid for “all orders” ( $k_{\perp} \rho_s > 1$ ) [E. F. Jaeger et al, Phys. Plasmas 9 (2002) 1873]
- AORSA utilizes a Fourier decomposition in  $k_x, k_y$  in the poloidal plane and a Fourier decomposition in the toroidal direction of symmetry:

$$\mathbf{E}(x, y, \phi) = \sum_{n_{\phi}} \sum_{n, m} \mathbf{E}_{n_{\phi}, n, m} e^{in_{\phi}\phi} e^{i(k_n x + k_m y)}$$

where  $x = R - R_0$  and  $y$  is the distance from the midplane

- Extended AORSA to include SOL plasma [D. Green PRL 2011]
  - Exponential decay for the SOL density to fit the experimental density data

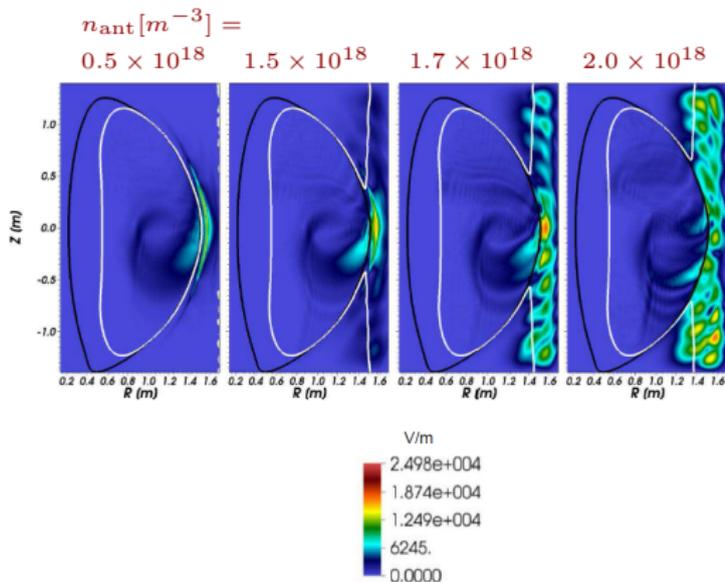
$$n_e = n_{\text{ant}} + [n_e(\rho = 1) - n_{\text{ant}}] \exp \left[ \frac{\rho - 1}{d_{\text{SOL}}} \right], \quad \rho \geq 1$$

$n_{\text{ant}}$  = density in front of the antenna

# RF field amplitude in the SOL increases as soon as the FW cut-off is removed from in front of the antenna

- For very low density the RF field is strongly localized in front of the antenna
- Standing wave appears at higher density
- Note that  $|E_{\text{tot}}|$  in the SOL is much greater than  $|E_{\text{tot}}|$  inside the LCFS and spreads out with increasing density
- Direct correlation between SOL RF field and FW cut-off location

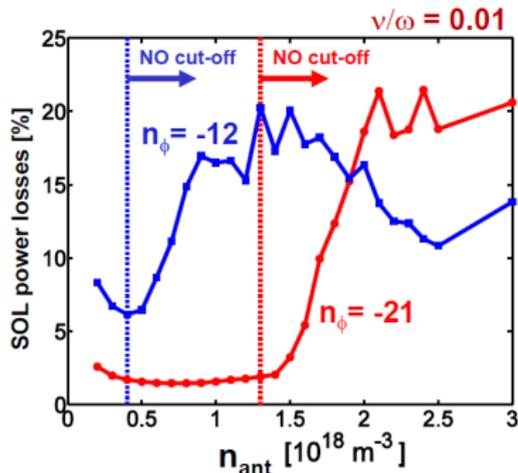
$|E_{\text{tot}}|$  for  $n_{\phi} = -21$  (# 130608)



N. Bertelli *et al*, NF 54 083004 (2014)

# SOL power losses increase from the evanescent to propagating within SOL according to the FW cut-off location

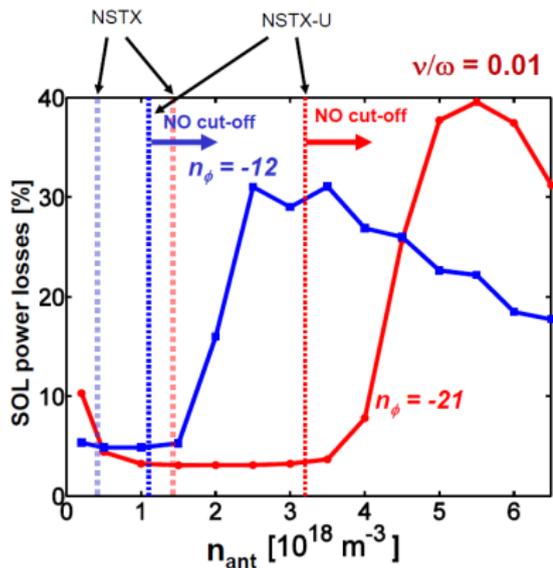
- “Collisional” damping included in AORSA as a proxy to represent the real SOL damping processes ( $\nu/\omega$  is input into AORSA)
- FW cut-off condition:  $n_{e,FWcut-off} \propto \frac{k_{\parallel}^2 B}{\omega}$
- Lower  $n_{\phi}$  ( $n_{\phi}/R = k_{\phi} \approx k_{\parallel}$ ) then transition at lower  $n_{ant}$
- For given  $n_{\phi}$ , SOL power losses increase if  $n_{ant} > n_{e,FWcut-off}$
- Agreement with some indications from the NSTX experimental observations [Hosea PoP (2008) and Phillips NF (2009)]
  - Will be further validated in the upcoming NSTX-U campaign



N. Bertelli *et al*, NF 54 083004 (2014)

# Larger evanescent region predicted at higher fields achievable in NSTX-U, favorable for future experiments

- H-mode scenario planned for NSTX-U, obtained by TRANSP simulations [S. P. Gerhardt, Nucl. Fusion **52**, 083020 (2012)]
- NSTX-U ( $B_T = 1$  T) vs. NSTX ( $B_T = 0.55$  T): transition occurs for  $\sim 2x$  higher in  $n_{ant}$
- Same relative behavior found for NSXT-U case with  $B = 0.76$  T
- NSTX-U: optimization of edge density to minimize the SOL losses and maximize the coupling to the core

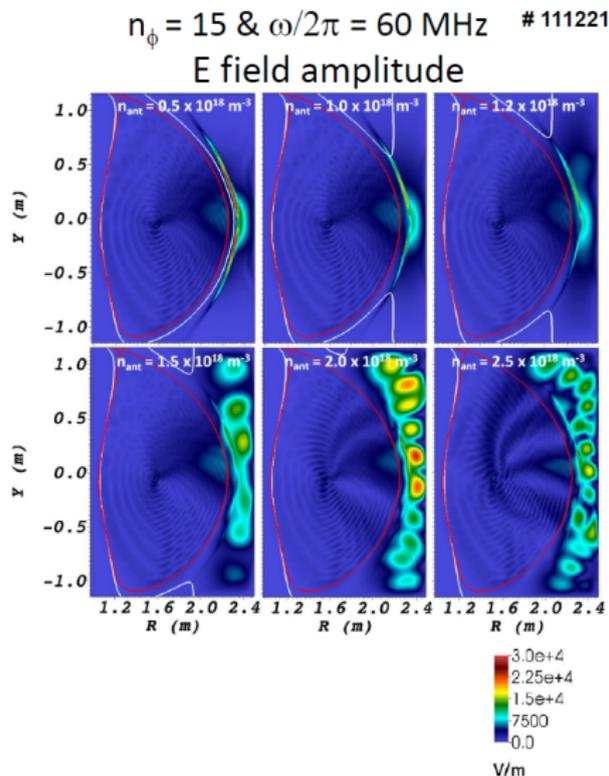


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# DIII-D results show similar E field behavior in the SOL found in NSTX and NSTX-U

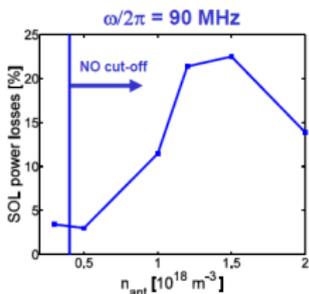
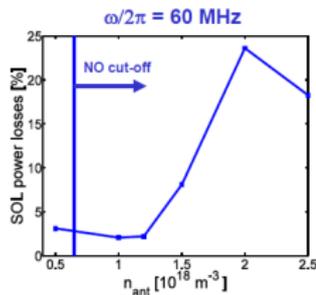
- FW heating used in DIII-D is similar to the regime adopted in NSTX/NSTX-U
- $\omega/2\pi = 60 - 120$  MHz &  $B_T = 1.3 - 2.1$  T:  
Mid/high harmonic regime ( $\omega/\omega_{c,D} = 4 - 12$ )
- E field amplitude increases when wave propagates outside the LCFS
- Same trend of E field amplitude for  $\omega/2\pi = 90$  MHz



N. Bertelli *et al*, submitted to NF (2015)

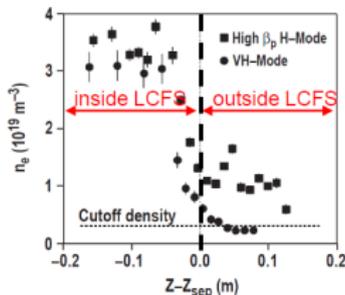
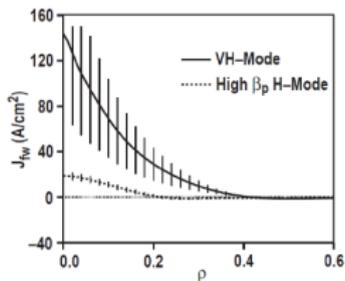
# Absorbed power in the SOL increases when the SOL density is above $n_{FW, cut-off}$ in agreement with previous DIII-D experiments

- From AORSA simulation including a damping as a proxy



- FW cut-off condition:  $n_{e,FWcut-off} \propto \frac{k_{\parallel}^2 B}{\omega}$
- higher  $\omega \rightarrow$  transition at lower  $n_{ant}$

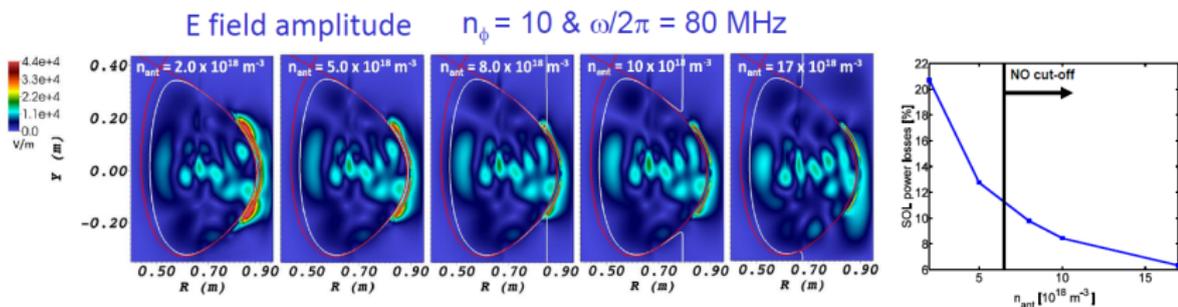
- DIII-D experiments shows large (small) FWCD in the core when SOL density is below (above) the FW cut-off density



Petty et al  
Nucl. Fusion 39 (1999) 1421

# Unlike NSTX/NSTX-U/DIII-D, Alcator C-Mod results show a decreasing of E field amplitude outside LCFS with increasing $n_{\text{ant}}$

- FW experiments in Alcator C-Mod operate in the ion cyclotron minority heating regime which differs from the mid/high harmonic regime adopted in DIII-D & NSTX/NSTX-U



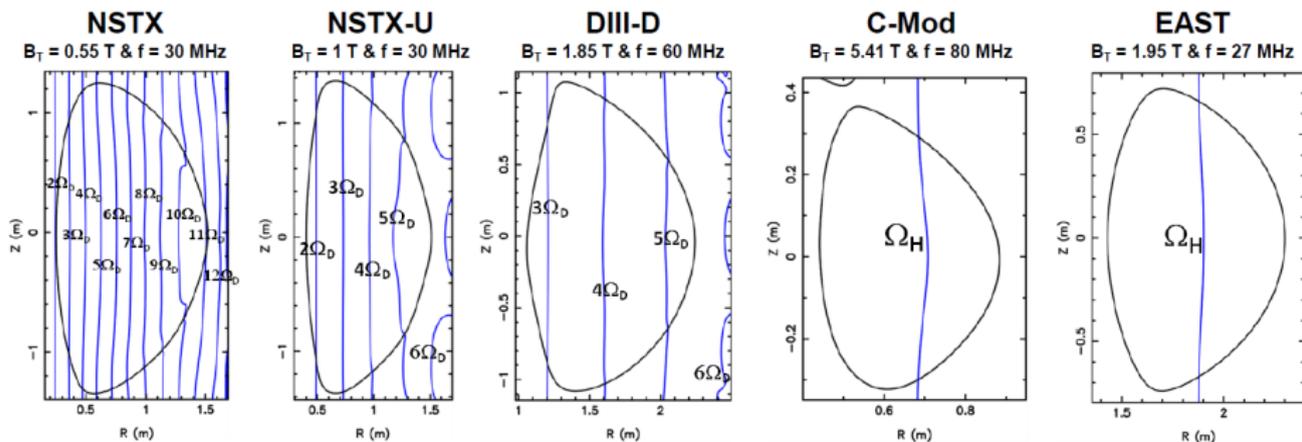
- Transition to higher SOL power losses does not appear due to different E field amplitude behavior in the SOL w.r.t. NSTX/DIII-D
- Same behavior found for EAST case
- In Alcator C-Mod and EAST, results perhaps more intuitive w.r.t. the NSTX/NSTX-U/DIII-D:
  - increase SOL density  $\Rightarrow$  enhances antenna-plasma coupling  $\Rightarrow$  lower power lost to the SOL

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# Hydrogen minority ICRH vs. mid/high harmonic ICRH regimes

**Main difference:** harmonic numbers  $\omega/\omega_{c,i}$  in the plasma and the interaction with the minority and majority ion species



No evidence in simulations of a specific role of the cyclotron resonances in the SOL plasma

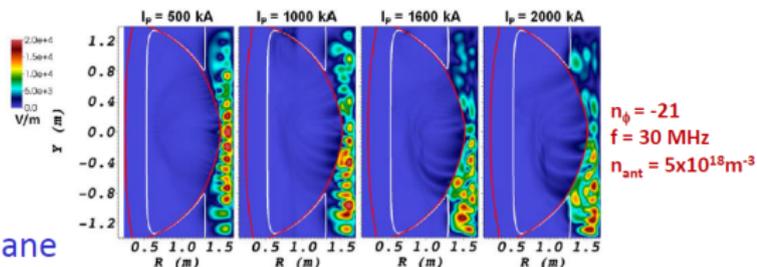
# Magnetic field pitch angle can play an important role in the E field behavior in the SOL

	NSTX	NSTX-U	DIII-D	C-Mod	EAST
$B_{T,0}$ [T]	0.55	1	1.85	5.41	1.95
$I_p$ [MA]	1	1	1.2	1	0.49
$\langle B_p / B_z \rangle$ ( $\rho=1$ )	-0.34	-0.19	-0.12	-0.10	-0.08

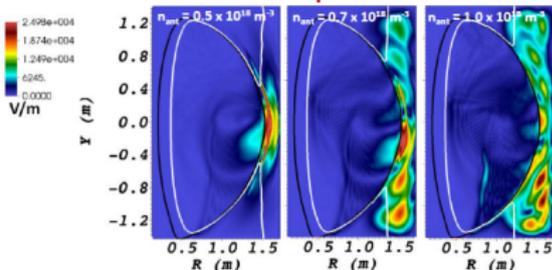
NSTX-U magnetic equilibria

$B_T = 1$  T and  $I_p = 0.5, 1.0, 1.6,$  and  $2.0$  MA  
By free-boundary equilibrium ISOLVER

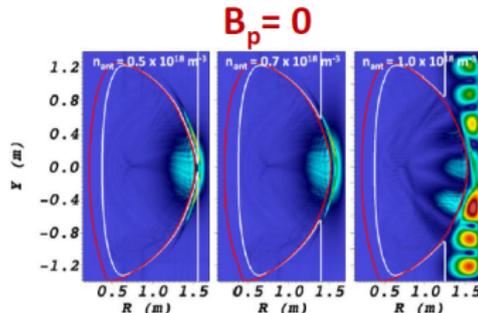
Large E amplitude still present but  
RF field moves down from the mid-plane



$B_p \neq 0$   $n_\phi = -12$  &  $f = 30$  MHz NSTX 130608



VS.



## Conclusions & future plans

- AORSA simulations show a direct correlation between the large SOL RF field, the location of the FW cut-off, and the SOL losses in NSTX/NSTX-U & DIII-D
  - SOL losses increase significantly as the wave transitions from evanescent to propagating as the density in the SOL increases
  - Agreement with experimental observations
  - NSTX-U simulations predict a wider evanescent region with lower SOL losses relative to NSTX
- Alcator C-Mod & EAST results differ from NSTX/DIII-D results
  - SOL RF field amplitude decreases when SOL density above the FW cut-off
- Magnetic pitch angle can play an important role in the behavior of SOL RF field
  
- Estimate the impact of limiter boundary in the AORSA results
- Perform AORSA runs in a reduce domain area just in front of the NSTX-U antenna (in order to have higher resolution)