

Stability considerations for optimizing ST geometry

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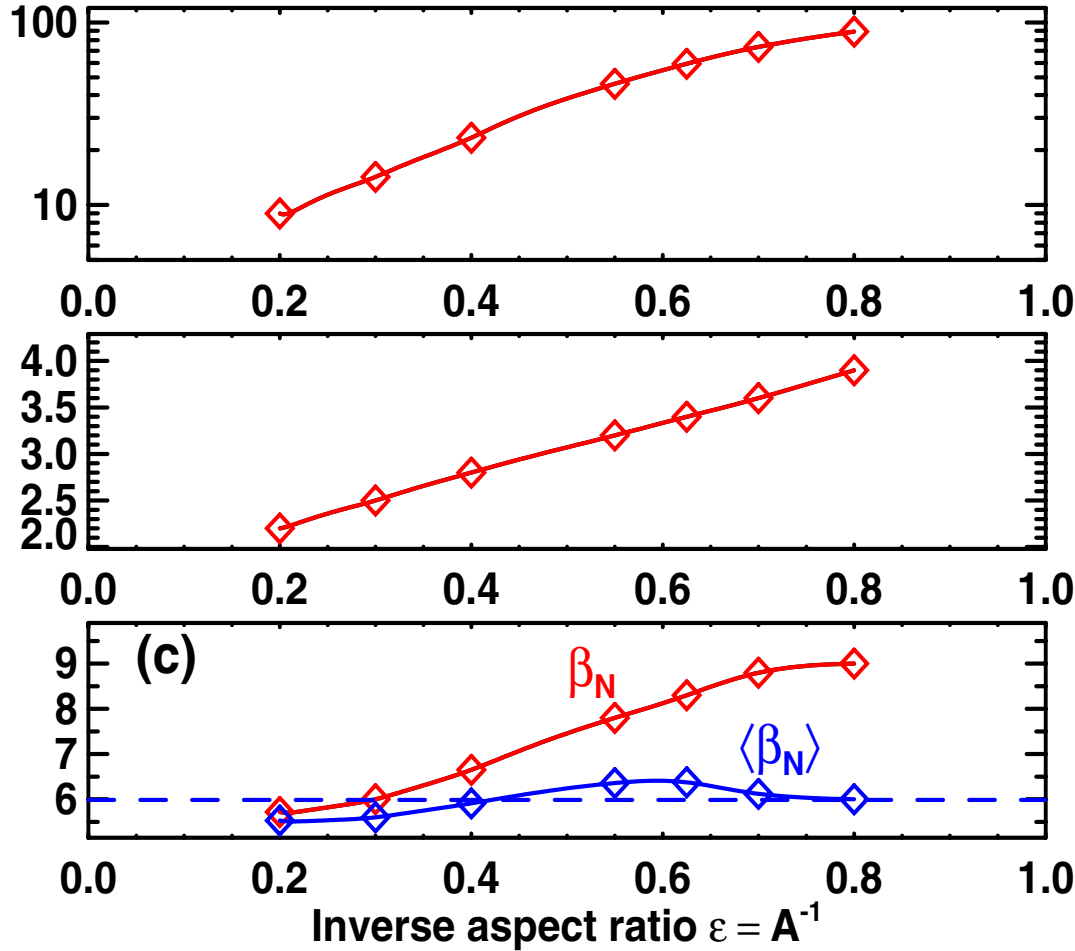
Princeton Plasma Physics Laboratory

P_{fusion} scalings for fixed R_0

- Combining Troyon and BS scalings \Rightarrow
$$\beta_t(\%) = \varepsilon^{1/2} C_{\text{BS}} (1+\kappa^2) (\beta_N)^2 / 8 f_{\text{BS}}$$
- $B_{t0} = B_{\text{MAX}}(1 - \varepsilon - \Delta_{\text{SHIELD}}/R_0)$
 $\Delta_{\text{SHIELD}} = \text{inboard shield thickness}$
- $V_{\text{plasma}} \propto R_0^3 \varepsilon^2 \kappa$
- $P_{\text{fusion}} \propto \beta_t^2 B_{t0}^4 V_{\text{plasma}}$

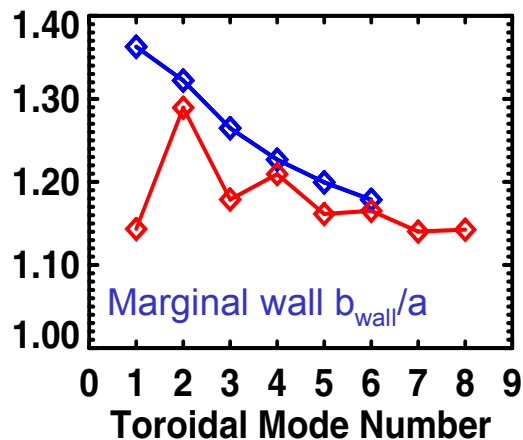
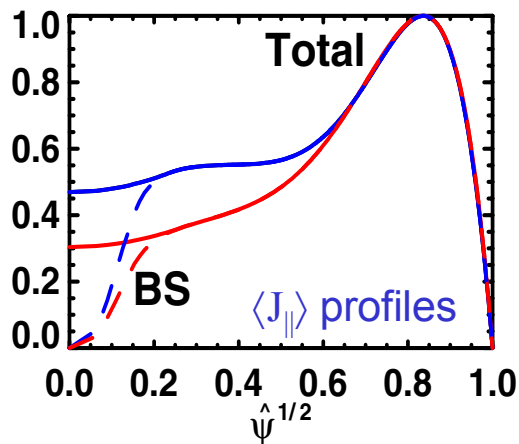
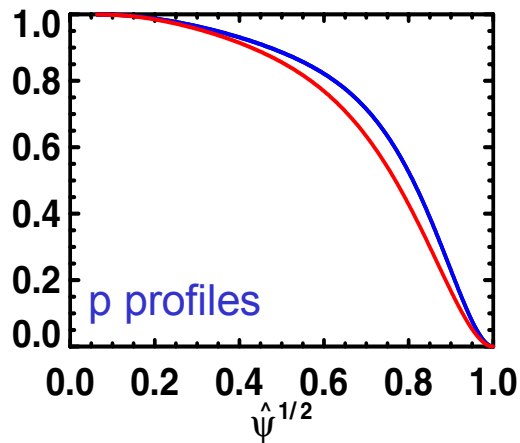
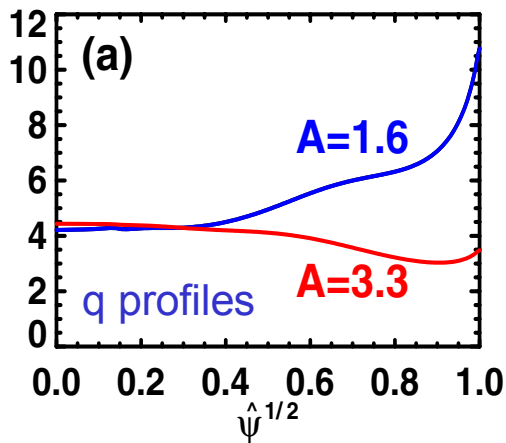
How do κ and β_N limits vary with aspect ratio?

β limits with wall stabilization, $f_{BS}=99\%$



- Factor of 10 increase in β_t from $A=5$ to $A=1.25$
 - Result of increased κ , β_N , ε
- κ increases from 2 to 4 over same range of aspect ratio
 - With-wall $n=1$ stability limits maximum elongation, assuming $n=0$ is stabilized
 - $\kappa \rightarrow 4 \Rightarrow$ very low $li = 0.1-0.2$
- β_N approaching 9 possible near $A=1.3-1.5$
- **Higher β_N and κ at low A combine to yield highest P_f at fixed R_0 for $A=1.6$**

Profile details for wall-stabilized optimized cases

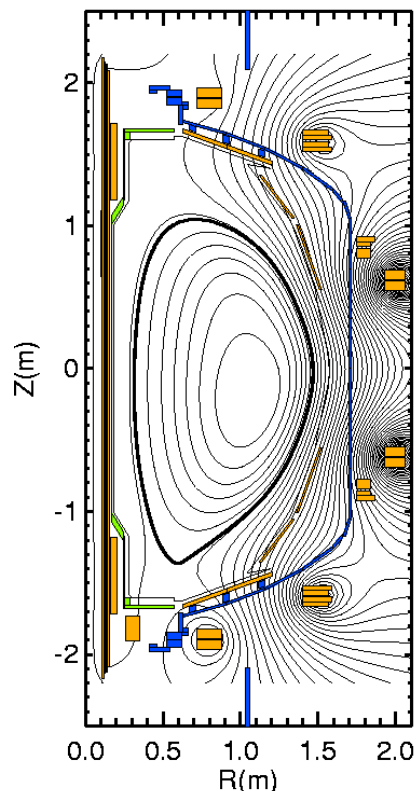


- Safety factor
 - Flat but monotonic q profile for $A < 2$
 - Reversed shear for $A > 2$
- Pressure profiles
 - Very broad, $p(0)/\langle p \rangle = 1.4-1.6$
- J profile
 - Hollow with large off-axis J_{BS}
 - Zero at edge to avoid peeling
- Wall position
 - Stable to $n=1-8$ w/ wall at 1.1
 - Intermediate- n most unstable

NSTX beginning to access “advanced” profiles

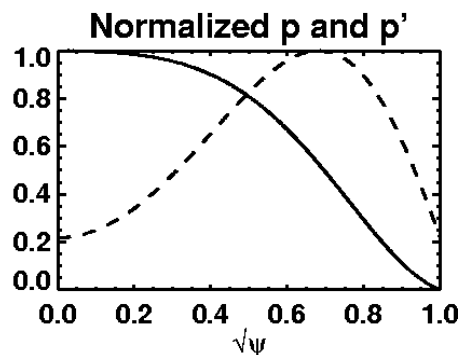
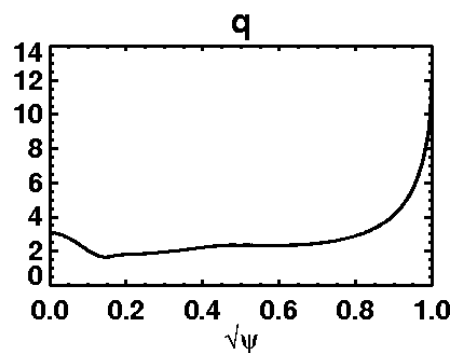
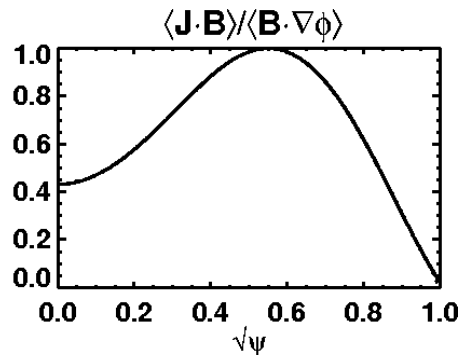


NSTX 109070 at t=529ms

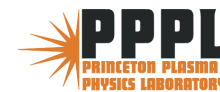


JSOLVER ID: Nea-07v0

$I_p = 0.798\text{MA}$
 $I_i = 0.601$
 $q_0 = 3.07$
 $q_{\min} = 1.65$
 $q_a = 12.2$
 $\beta_t = 18.1\%$
 $\beta_N = 6.22$
 $p_0 / \langle p \rangle = 2.02$



- EFIT02 without MSE, kinetic p, etc., but these shots appear to have:
- $\beta_N = 6.2, I_i = 0.6, q \geq 2$
 - $\beta_N / I_i > 10$
 - $\geq 1/2$ way between theoretical no-wall and with-wall limit?
- Hollow J profile
 - Flat q profile?
 - or reversed shear?
- Broad pressure profiles
 - $p_e(0) / \langle p_e \rangle = 1.8$ (H-mode)



ST reactor relies on wall stabilization and extreme κ

$$A = 1.6$$

$$\kappa = 3.4$$

$$\delta = 0.64$$

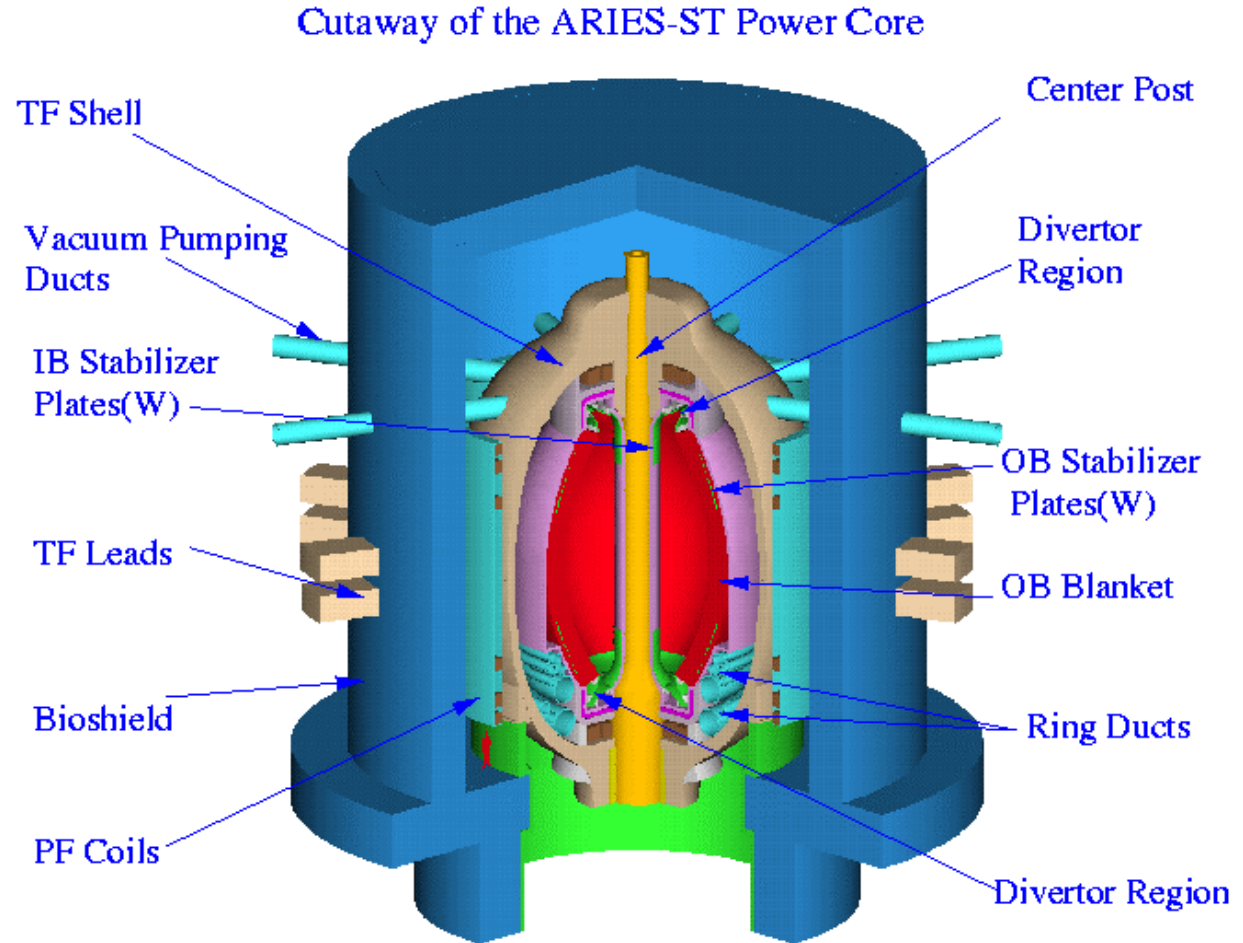
$$\beta_t = 56\%$$

$$\beta_N = 8.2$$

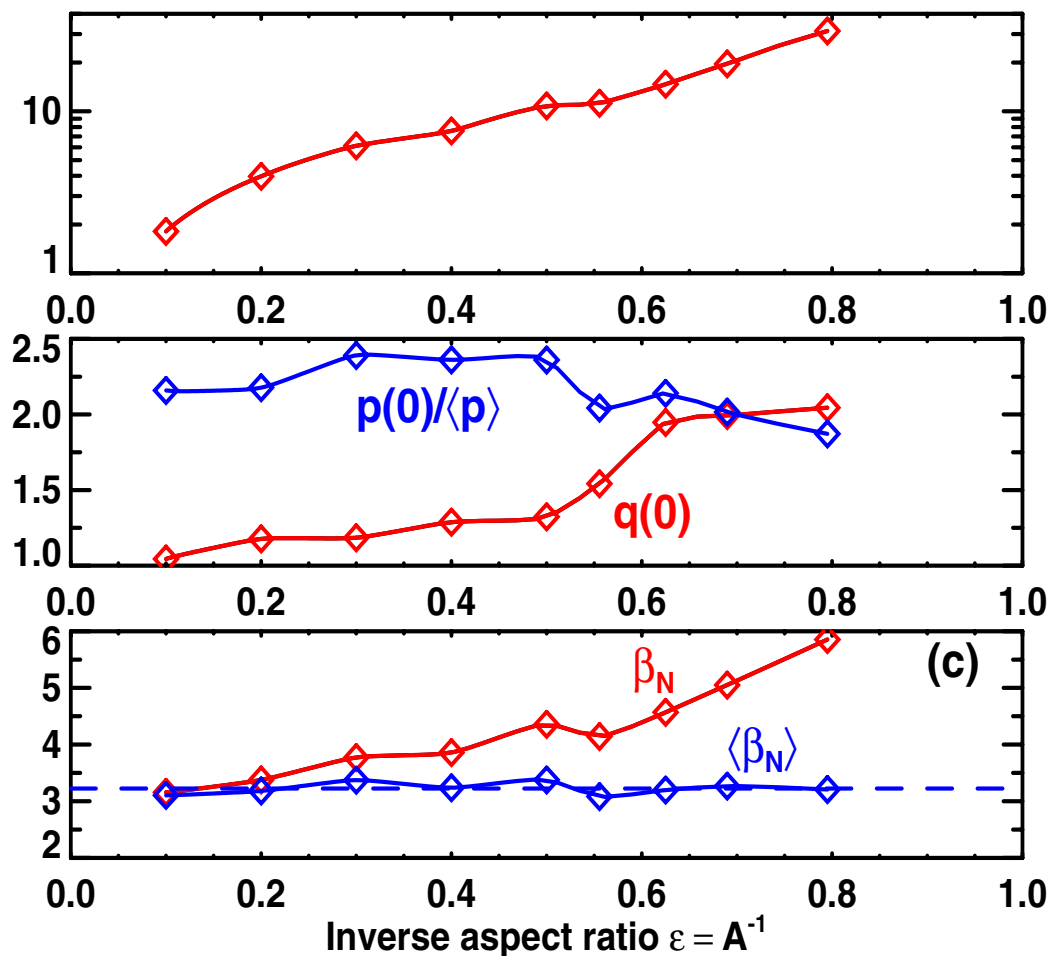
$$f_{BS} = 99\%$$

$$I_p = 35\text{MA}$$

$$p(0)/\langle p \rangle = 1.4$$

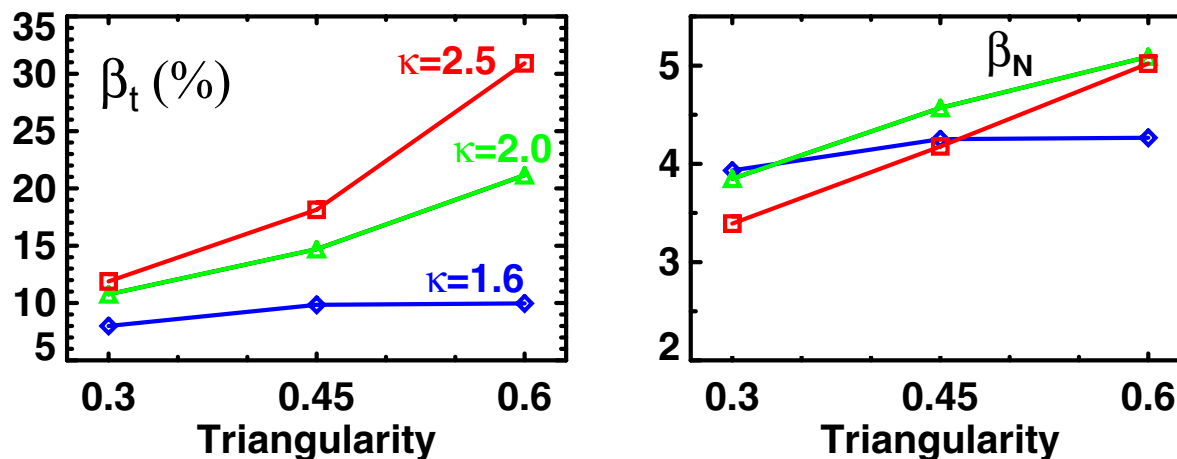


β limits *without* wall stabilization, $f_{BS}=50\%$



- **Fixed $\kappa=2.0$, $\delta=0.45$**
- Factor of 8 increase in β_t from $A=5$ to $A=1.25$
 - Result of increased β_N and ϵ
- $q(0)$ for optimal ideal stability at or above 2 for $A < 1.8$
 - Improved NTM stability
- β_N approaching 6 possible at lowest A treated ($A=1.25$)
- **Higher β_N at low A with fixed κ yields highest P_f at fixed R_0 when $A=1.8$**
 - **Including ϵ dependence of κ would lower optimal A**

β limits without wall, $A=1.6$, $f_{BS}=50\%$



- High δ crucial to no-wall stability of high κ and f_{BS} regime
 - 30% increase in β_t as $\delta=0.3 \rightarrow 0.6$ for $\kappa = 1.6$
 - **Factor of 2 increase for $\kappa=2$, $\times 2.5$ for $\kappa=2.5$**
- With $\kappa=2.5$ and $\delta=0.6$, can theoretically achieve NSTX-like $\beta_t \sim 30\%$ at higher $A=1.6$ w/o wall and with higher f_{BS}
 - Utilizing wall stabilization, $\kappa=2.5$, and $\delta=0.6$, $\beta_t \sim 40\%$ and $f_{BS} = 70\%$ are theoretically achievable – similar to lower $A=1.25$ target

Summary

- Stability \Rightarrow optimal A for max. P_{fusion} is $A=1.6-1.8$
 - Requires minimal inboard shielding, “free” non-inductive CD
 - Similar scaling results with and without wall stabilization
 - β_N limit increases naturally with increasing ϵ
 - $n=0,1$ elongation limits also increase at lower A
 - Optimal $q(0) \geq 2$ for $A \leq 1.8 \Rightarrow$ improved NTM stability
- Large increase in β_t with increased κ
 - Above $\kappa=2$, increased δ required for highest κ
 - Very broad p profiles in optimized regimes
- Optimized $A=1.6$ targets:
 - $A=1.6, \kappa=2.5, \delta=0.6, \beta_t=30\%, f_{BS}=50\%$
 - $\beta_t=40\%, f_{BS}=70\%$ possible with wall, like present target
- Can NSTX study higher A, κ, δ in next 5 years?