

# Synthetic Aperture Microwave Imaging on MAST and NSTX-U

S. J. Freethy<sup>1</sup>, K. J. Brunner<sup>1,2</sup>, J. Chorley<sup>1,2</sup>, D. Thomas<sup>1,3</sup>, V. F. Shevchenko<sup>1</sup>, J. Urban<sup>4</sup> and R. G. L. Vann<sup>3</sup>

1 EURATOM/CCFE Fusion Association, Abingdon, Oxfordshire, OX14 3DB, UK

2 Centre for Advanced Instrumentation, Department of Physics, Durham University, Durham, UK

3 York Plasma Institute Department of physics, University of York, York, YO10 5DD, UK

4 Institute of Plasma Physics, Academy of Sciences of the Czech Republic, Prague

# Outline

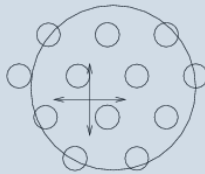
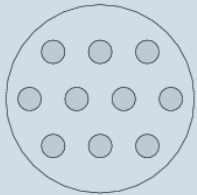
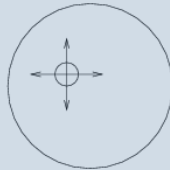
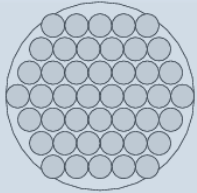
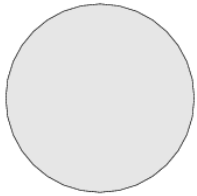
- Introduction and motivations – S. J. Freethy
  - Introduction to SAMI
  - Introduction to EBW emission
  - Results from MAST
- Reflectometry and backscattering – D. Thomas
  - Multiple reflectometers
  - Backscattering and Doppler shifts
- Technical developments and upgrade – J. Brunner
  - FPGAs
  - The SAMI digitiser
  - FPGA/GPU data “real-time” data processing

# Outline

- Introduction and motivations – S. J. Freethy
  - Introduction to SAMI
  - Introduction to EBW emission
  - Results from MAST
- Reflectometry and backscattering – D. Thomas
  - Multiple reflectometers
  - Backscattering and Doppler shifts
- Technical developments and upgrade – J. Brunner
  - FPGAs
  - The SAMI digitiser
  - FPGA/GPU data “real-time” data processing

# SAMI is a thinned array

For imaging microwaves you can use...



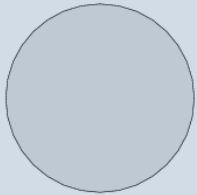
Physical aperture

Visibility aperture

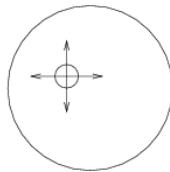
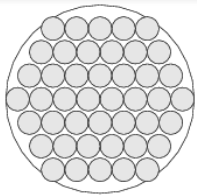
- A lens or mirror element steered by moving the element,
- or used to focus image onto an array of detectors.
- A traditional phased array is a filled aperture of phase sensitive antennas.
- Beam is steered through phase control of elements
- High signal to noise, but high redundancy
- A thinned array makes use of the spatial incoherence of the source to remove redundancies, making images of the same fidelity with much fewer elements
- Beam is steered through phase control of elements
- Beam steering replaced by Fourier Transform

# SAMI is a thinned array

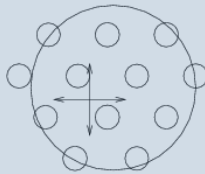
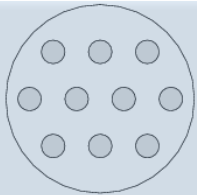
For imaging microwaves you can use...



- A lens or mirror element steered by moving the element,
- or used to focus image onto an array of detectors.



- A traditional phased array is a filled aperture of phase sensitive antennas.
- Beam is steered through phase control of elements
- High signal to noise, but high redundancy



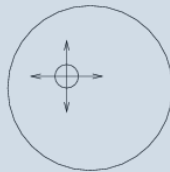
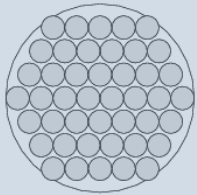
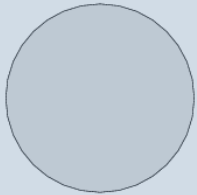
- A thinned array makes use of the spatial incoherence of the source to remove redundancies, making images of the same fidelity with much fewer elements
- Beam is steered through phase control of elements
- Beam steering replaced by Fourier Transform

Physical aperture

Visibility aperture

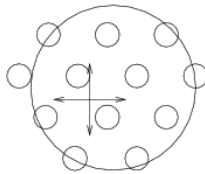
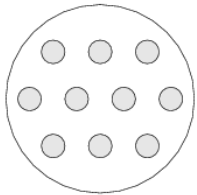
# SAMI is a thinned array

For imaging microwaves you can use...



- A lens or mirror element steered by moving the element,
- or used to focus image onto an array of detectors.

- A traditional phased array is a filled aperture of phase sensitive antennas.
- Beam is steered through phase control of elements
- High signal to noise, but high redundancy



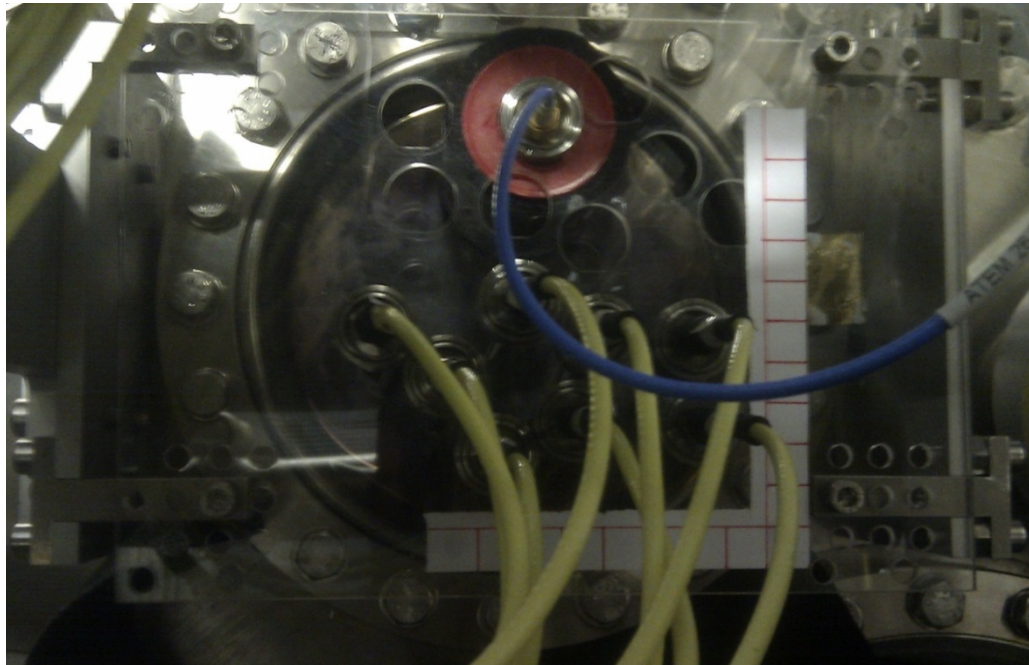
- A thinned array makes use of the spatial incoherence of the source to remove redundancies, making images of the same fidelity with much fewer elements
- Beam is steered through phase control of elements
- Beam steering replaced by Fourier Transform

Physical aperture

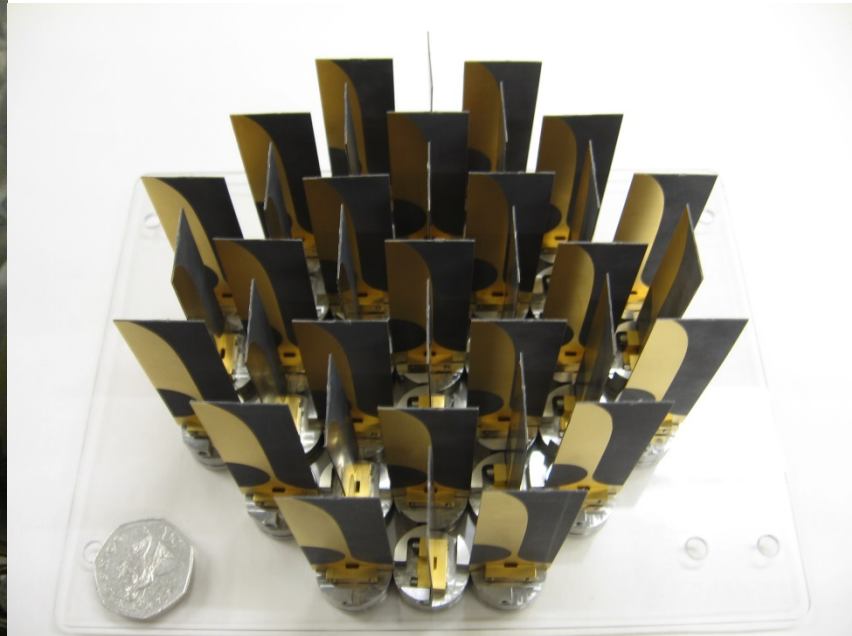
Visibility aperture

# SAMI array

8 Antenna array installed on MAST



36 Antenna array for illustration

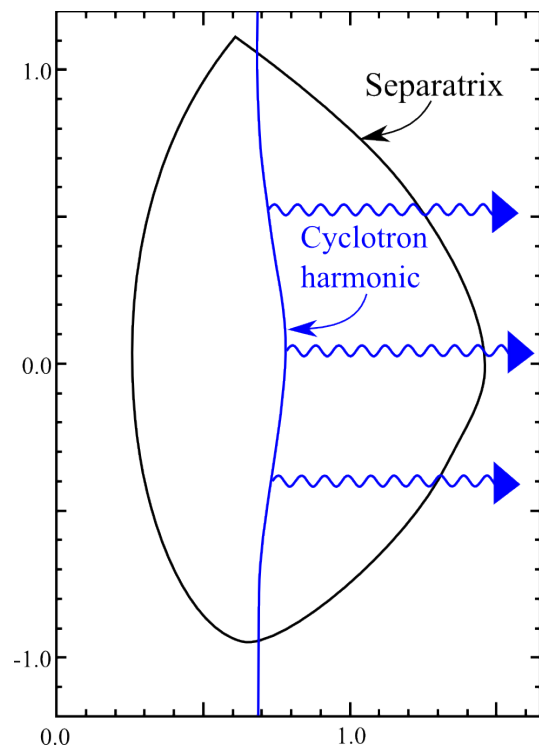


Linear polarised, very broadband PCB based antenna

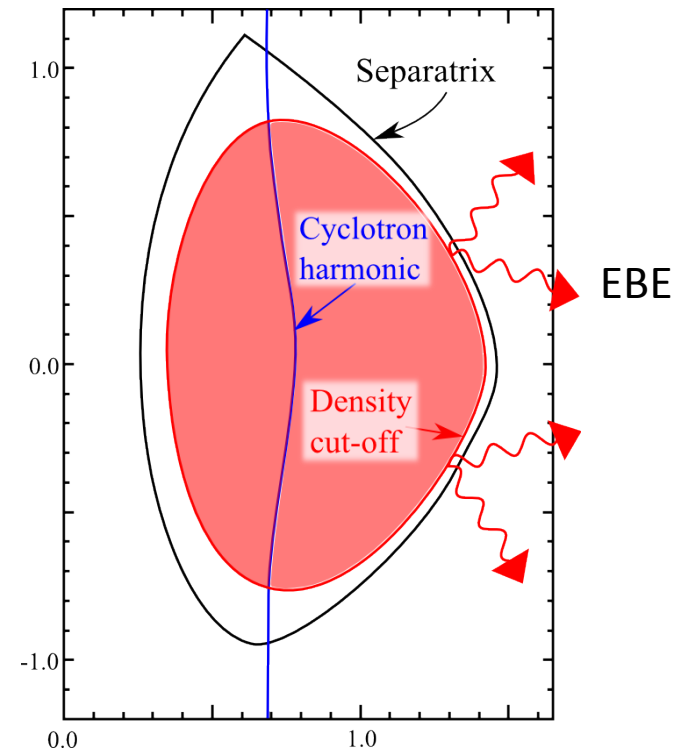
Array has wide field of view -> small antenna spacings

# Emission from over-dense machines

- Most conventional tokamaks emit thermal radiation from Cyclotron harmonics
- High beta machines tend to have their harmonics covered by cut-offs



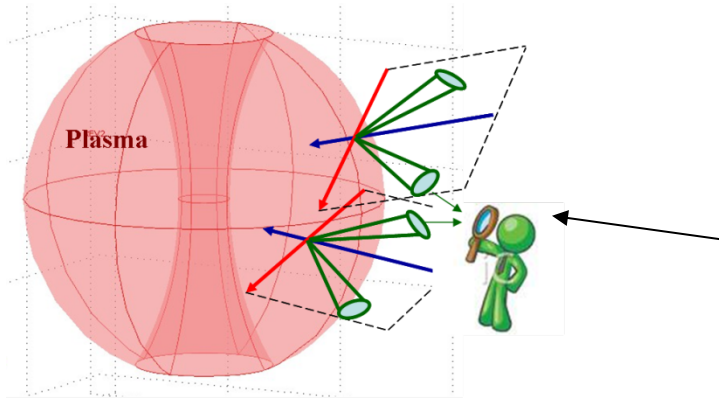
Under-dense -> Normal ECE



Over-dense -> mode converted emission



# Mode converted emission

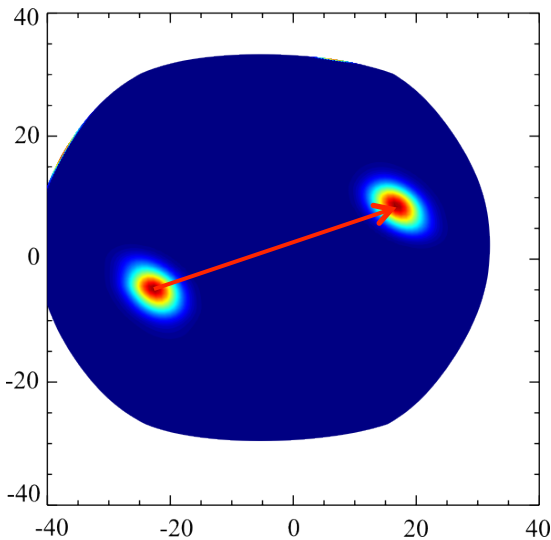


- The dependence of the Mode Conversion (MC) on the incident angle to the field means the emission is anisotropic.

- The MC'd emission takes the form of narrow angular cones.

- When all emission is considered, it appears as two spots on the plasma density surface along the magnetic field line.

- Mode conversion happens at different layers in the plasma for different frequencies, so we may diagnose different radii



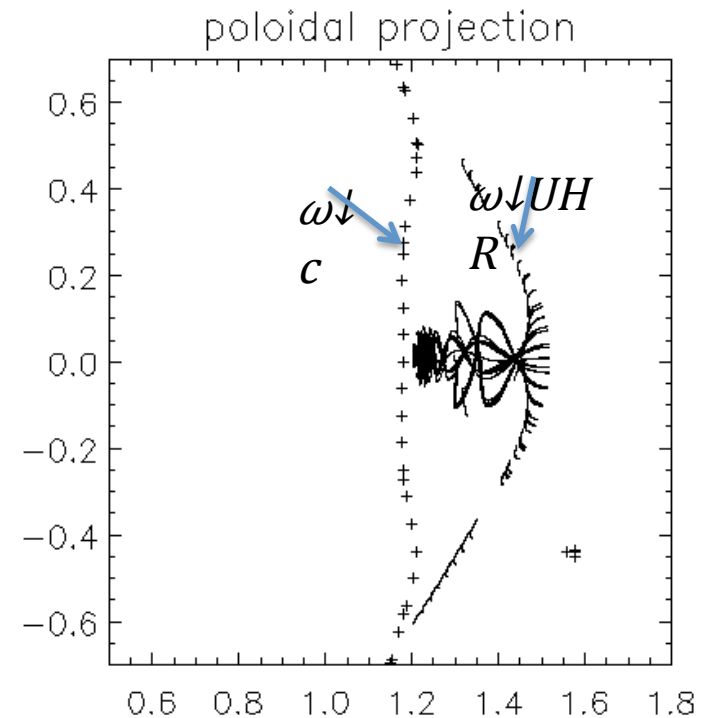
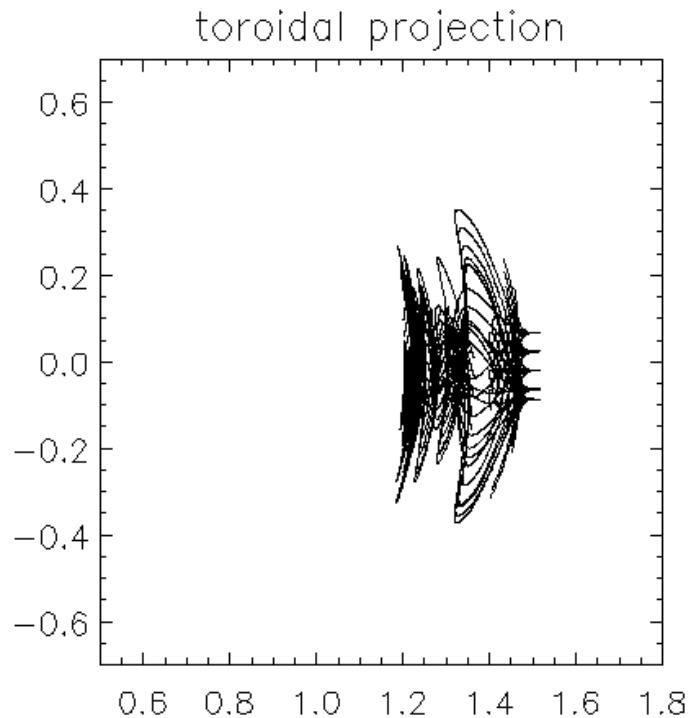
# Mode Converted Emission

- The brightness-temperature of the emission is the product of the brightness-temperature of the EBW at source and the mode conversion coefficient.

$$T_{\text{obs}} = T_{\text{EBE}} \tau_{\text{mc}}$$

# Ray tracing shows strong off-midplane Doppler broadening

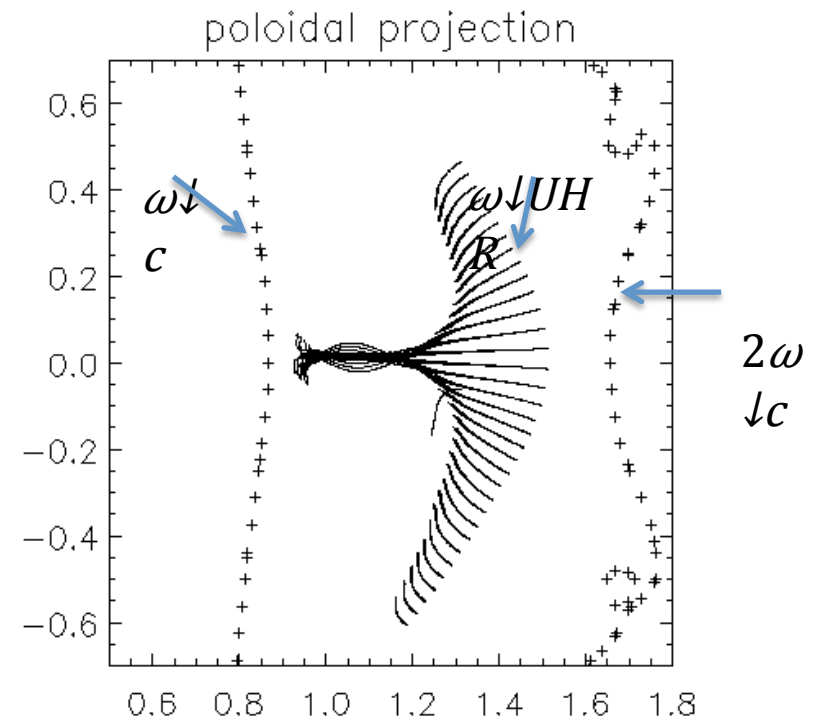
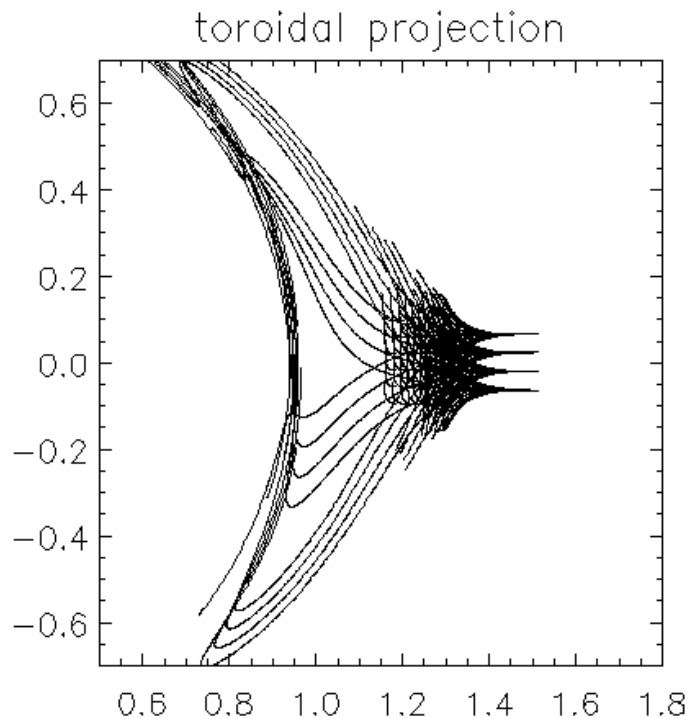
11GHz example – Only rays on the midplane originate at the cyclotron harmonic



Off midplane, the rays originate from the colder outer regions

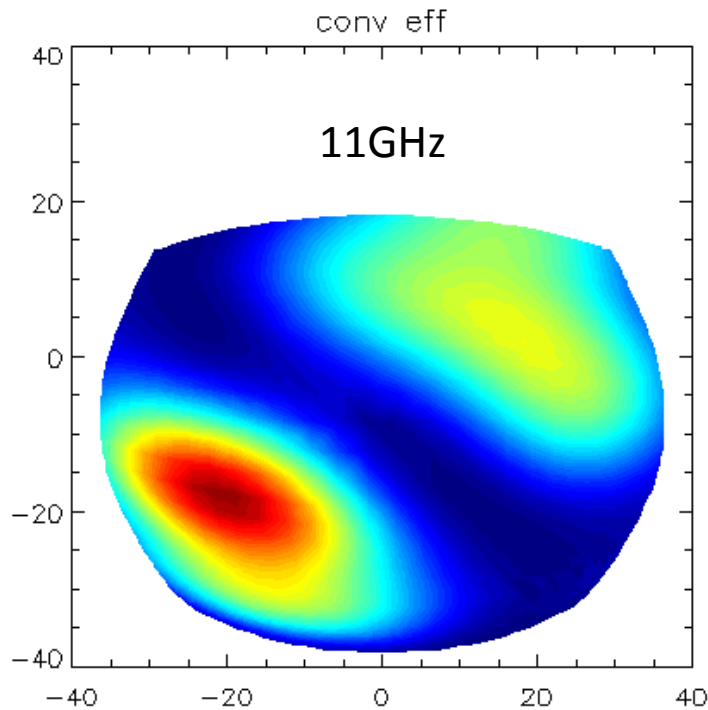
# Maximum penetration between harmonics

15GHz example – Maximum penetration of *off midplane* rays happens between harmonics

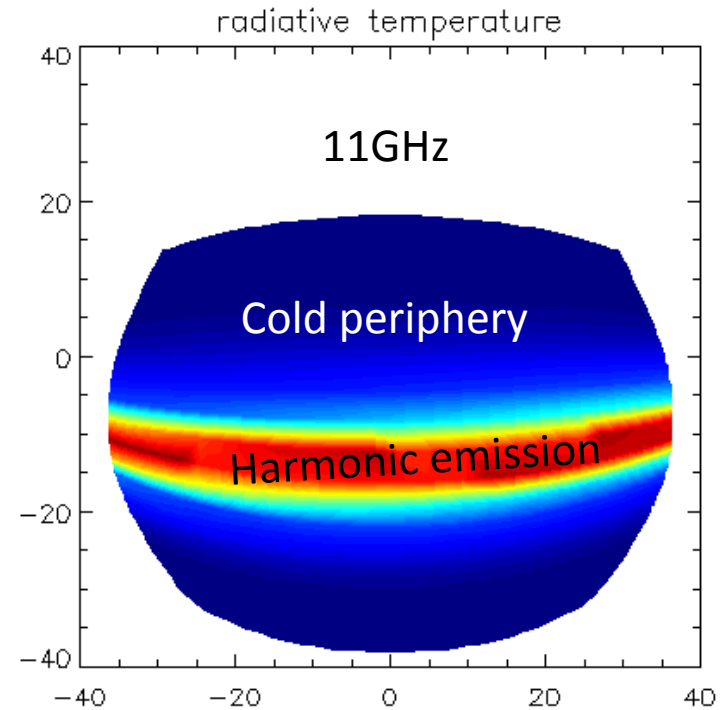


# Radiative temperature effect

Performing AMR simulations we can see that, for low frequencies, the wave refraction dominates the observable emission profile.

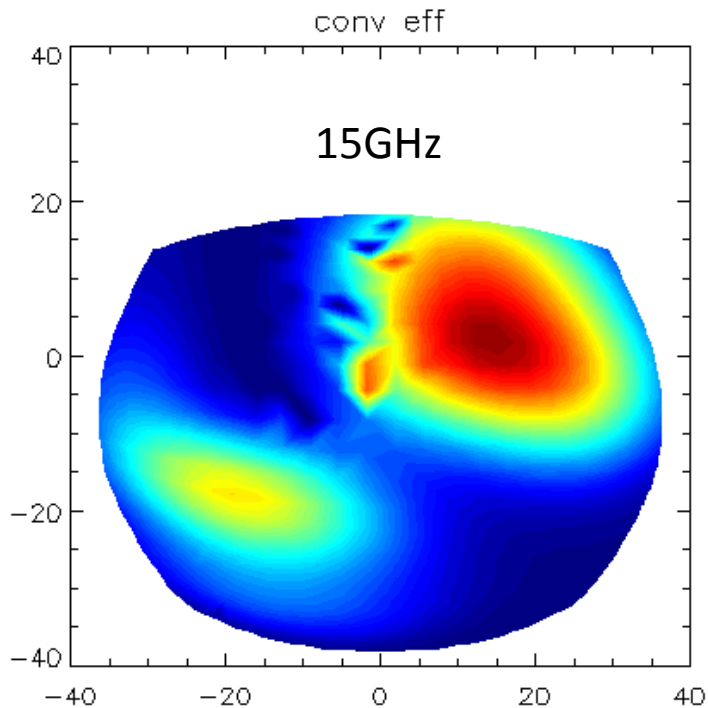


X

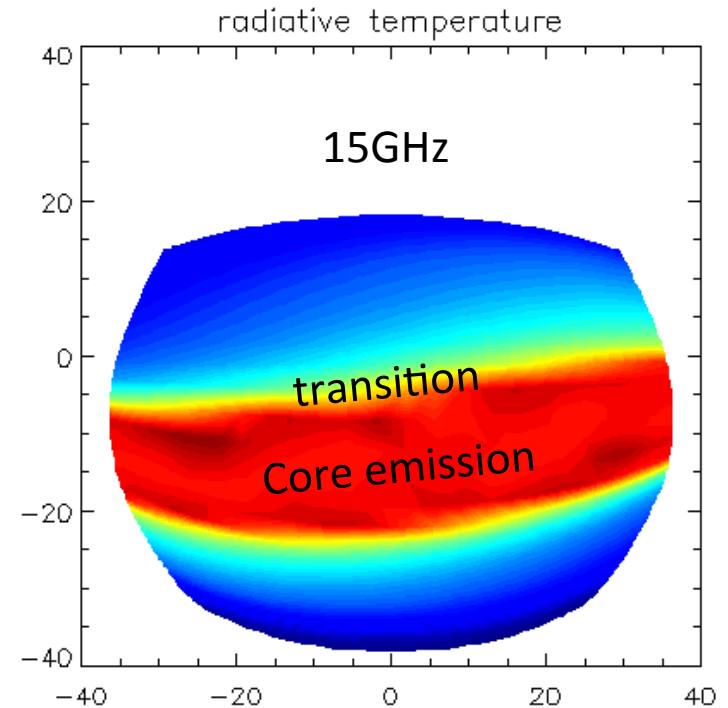


# Radiative temperature effect

In between the harmonics, the effect is less pronounced, but still present.

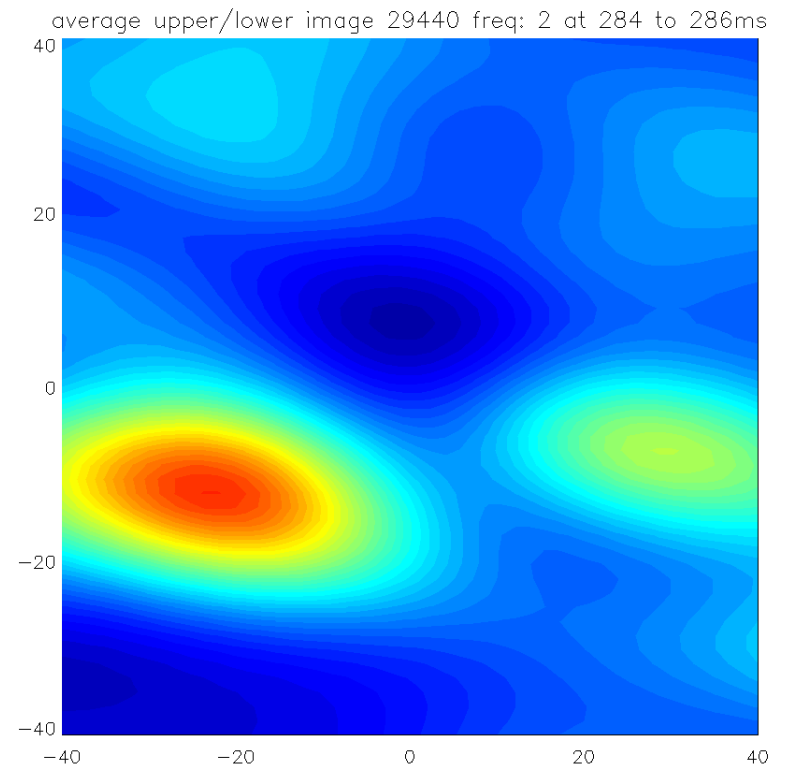
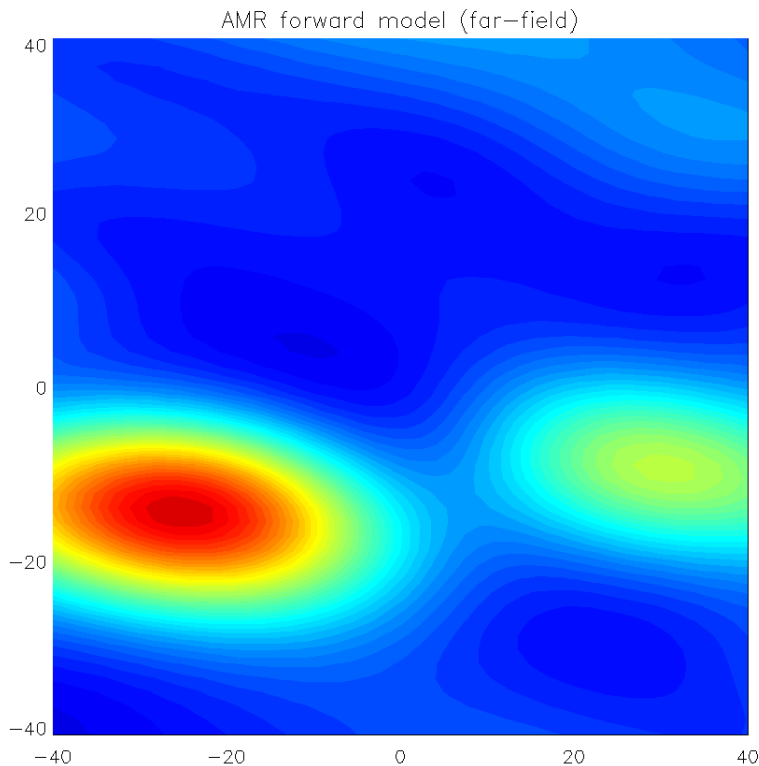


X



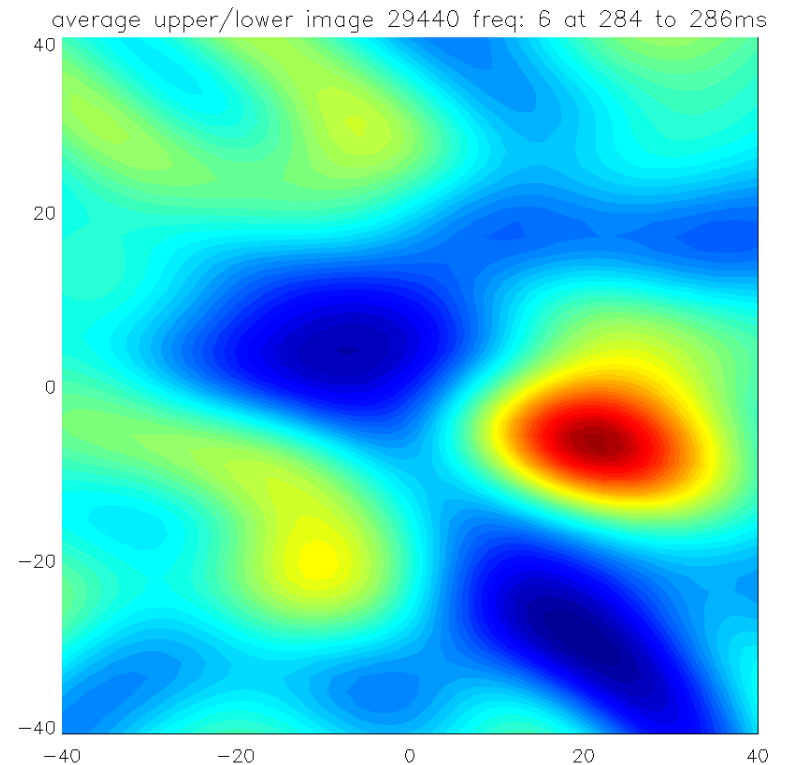
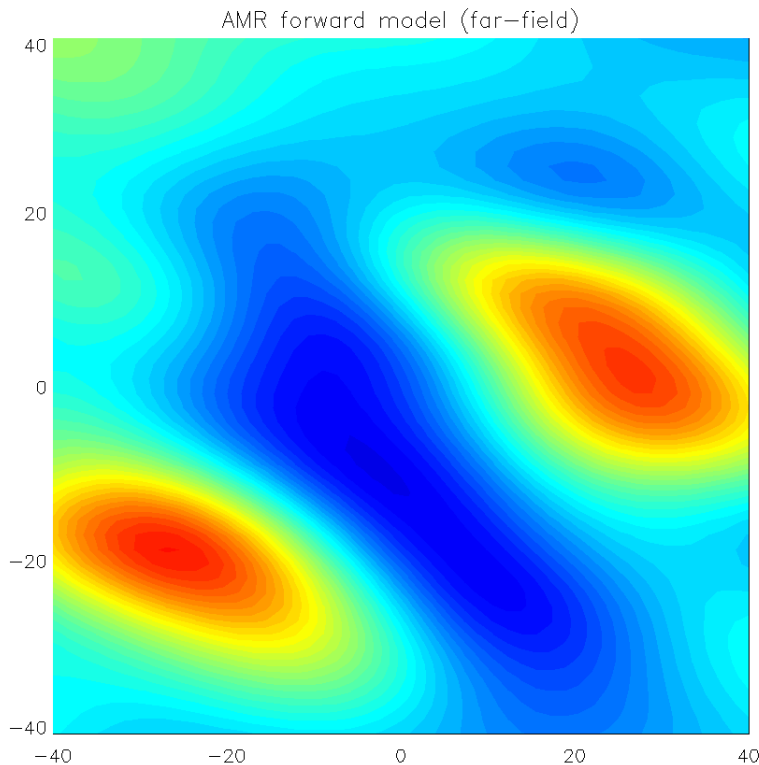
# Forward model 11GHz

Excellent agreement between convolved AMR emission and observed emission



# Forward model 15GHz

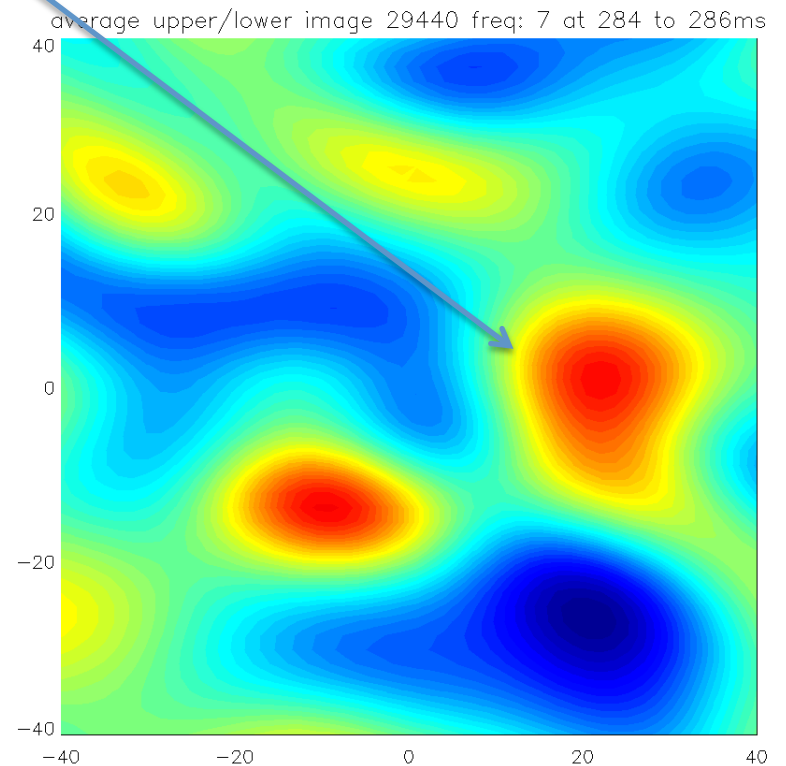
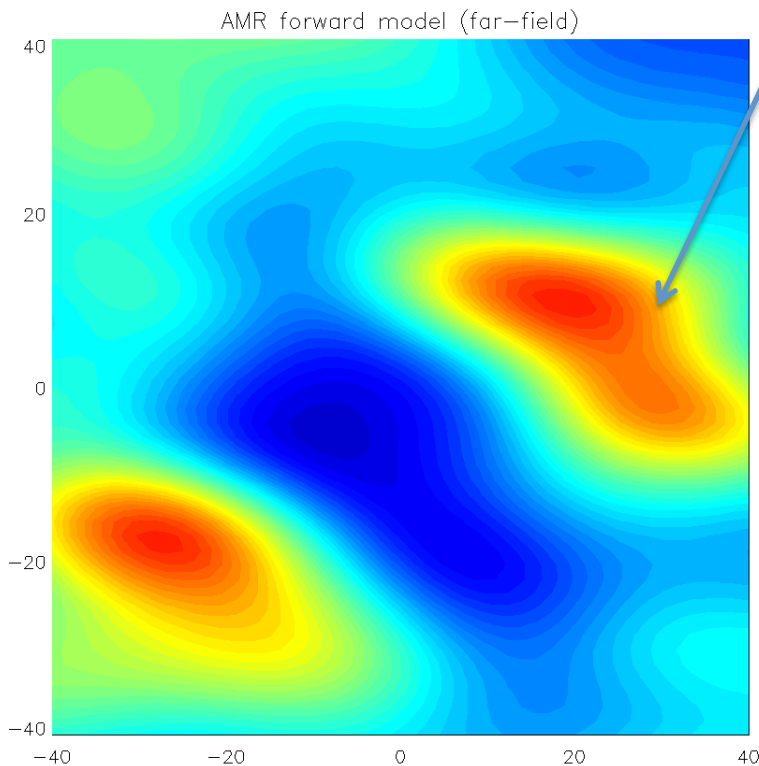
Less good agreement at higher frequencies.  
“Pitch” is consistently flatter than predicted





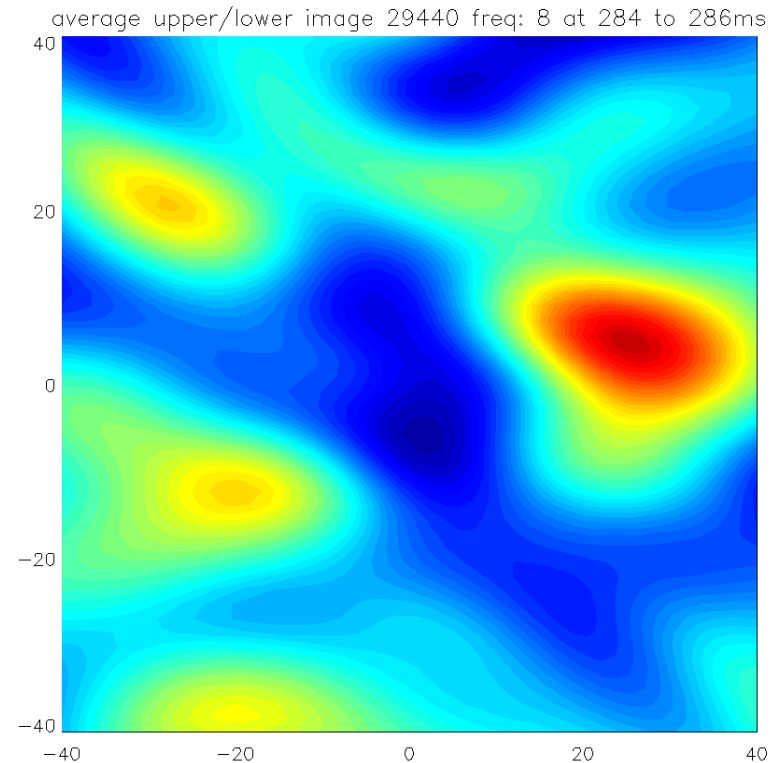
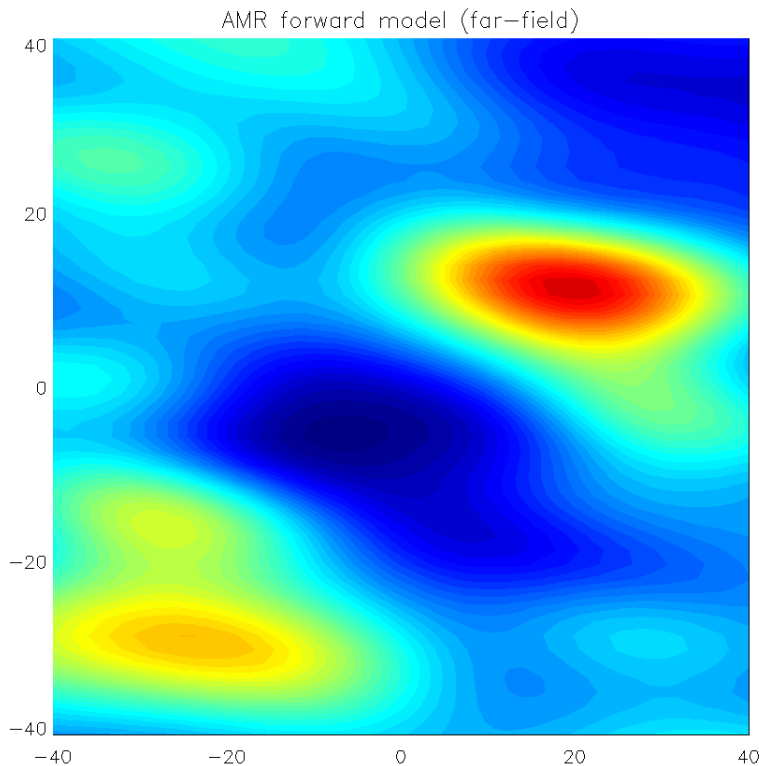
# Forward model 16GHz

Elongation of observed upper window, due to emission window splitting in two



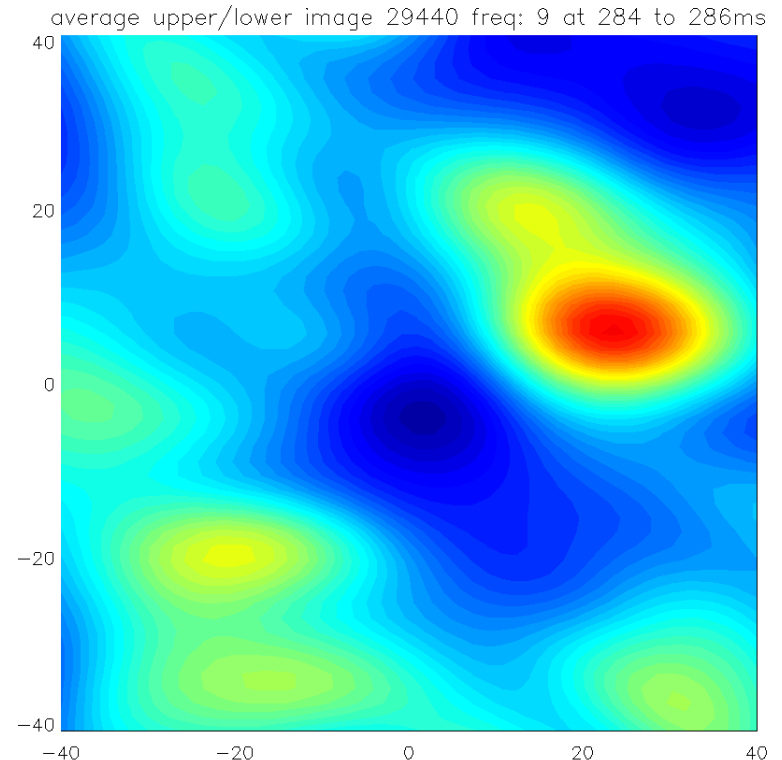
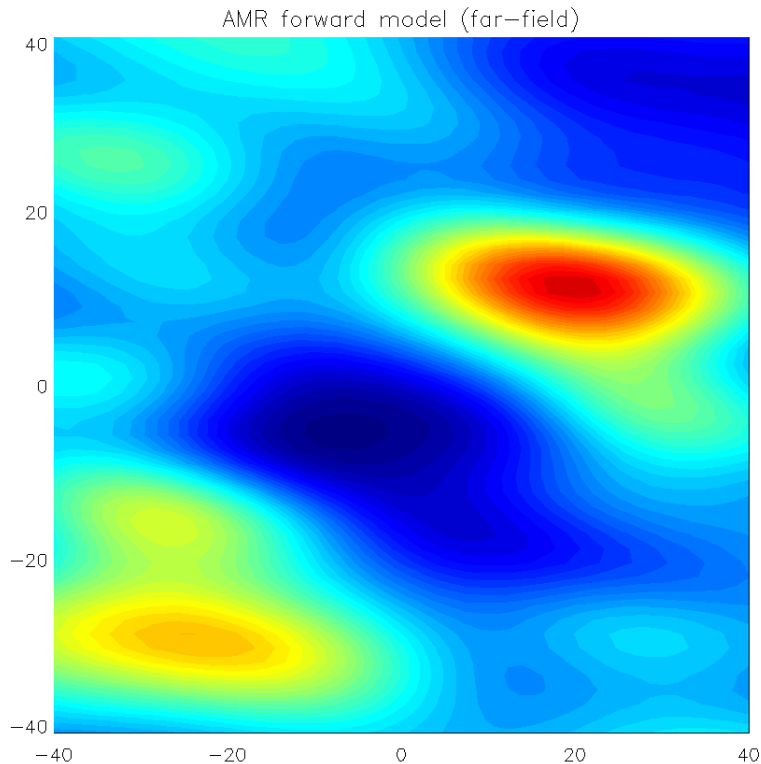
# Forward model 17GHz

Right hand window moves up off the midplane signalling 2<sup>nd</sup> harmonic emission beginning to take over. Hotter, fundamental emission is seen only off midplane.



# Forward model 18GHz

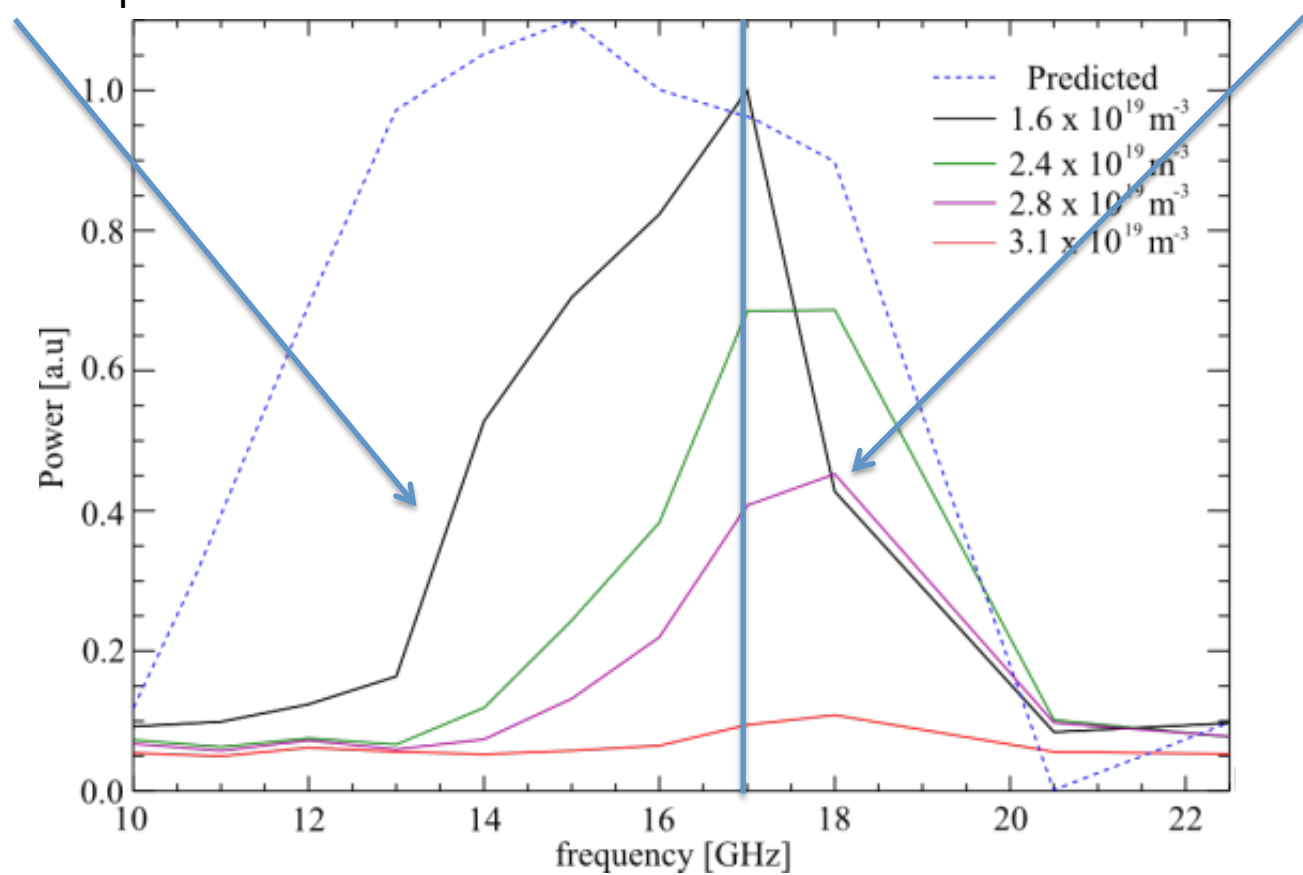
Continuing to higher frequencies, the midplane emission shuts down entirely as the 2<sup>nd</sup> harmonic begins to overlap with the UHR



# Density dependence of emission

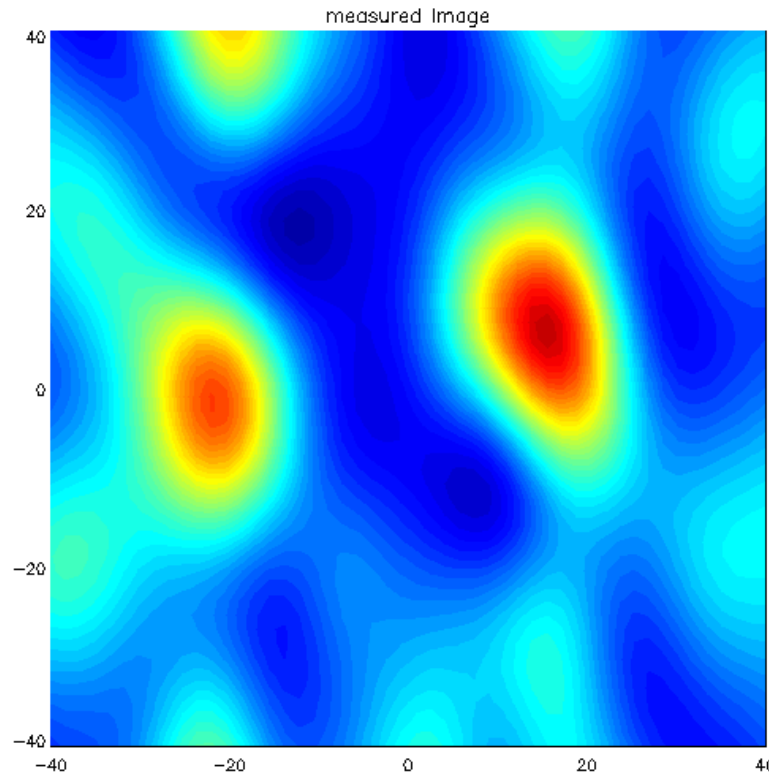
Scooped lower frequencies

Peak emission moves to higher frequency



# Array on midplane

$n_e = 1.6e19 \text{ m}^{-3}$

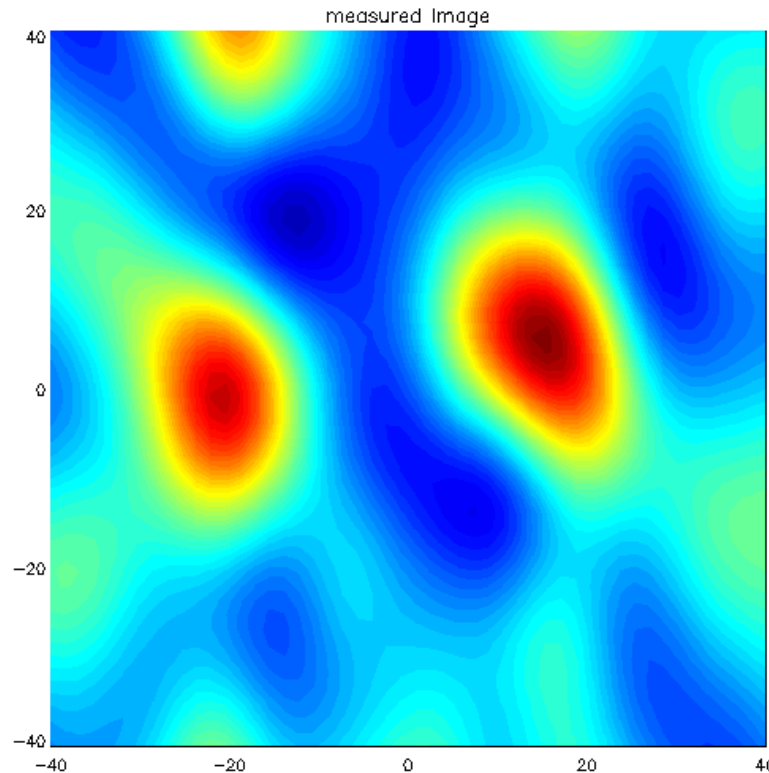


Clear trend of decreasing  
apparent pitch with  
increasing  $n_e$ .



# Array on midplane

$n_e = 2.4e19 \text{ m}^{-3}$

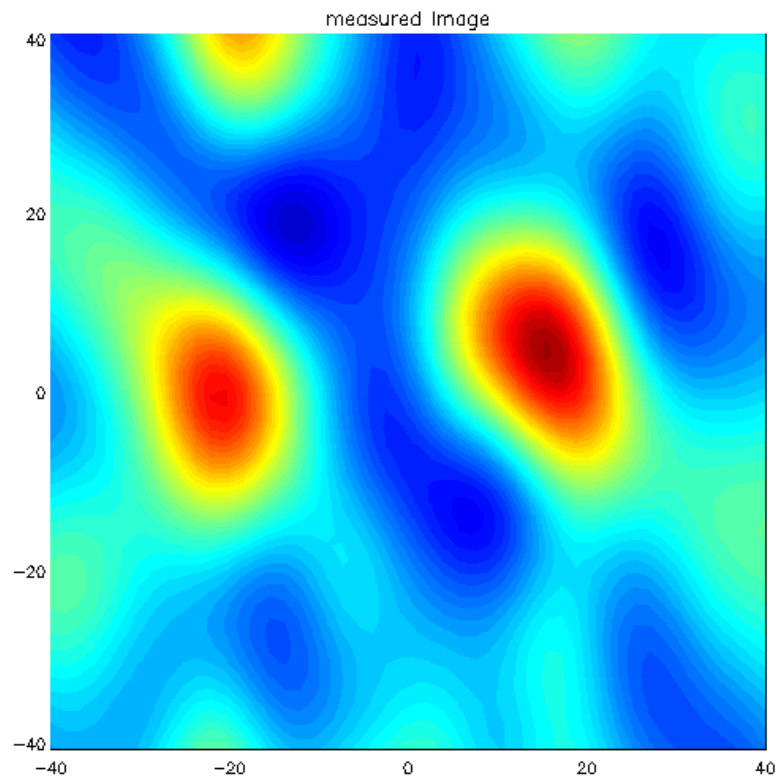


Clear trend of decreasing  
apparent pitch with  
increasing  $n_e$ .



# Array on midplane

$n_e = 2.8e19 \text{ m}^{-3}$

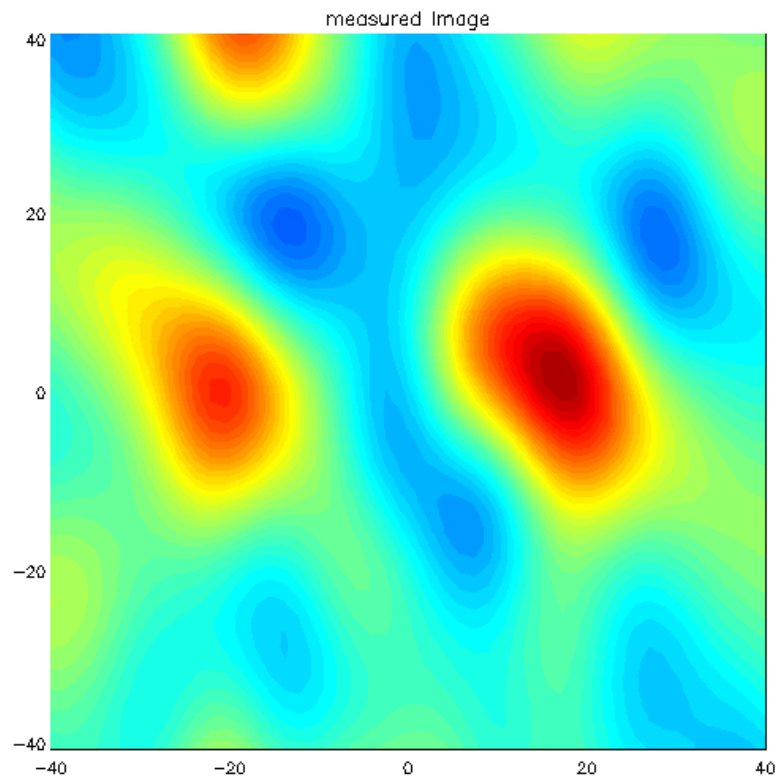


Clear trend of decreasing  
apparent pitch with  
increasing  $n_e$ .



# Array on midplane

$n_e = 3.1e19 \text{ m}^{-3}$

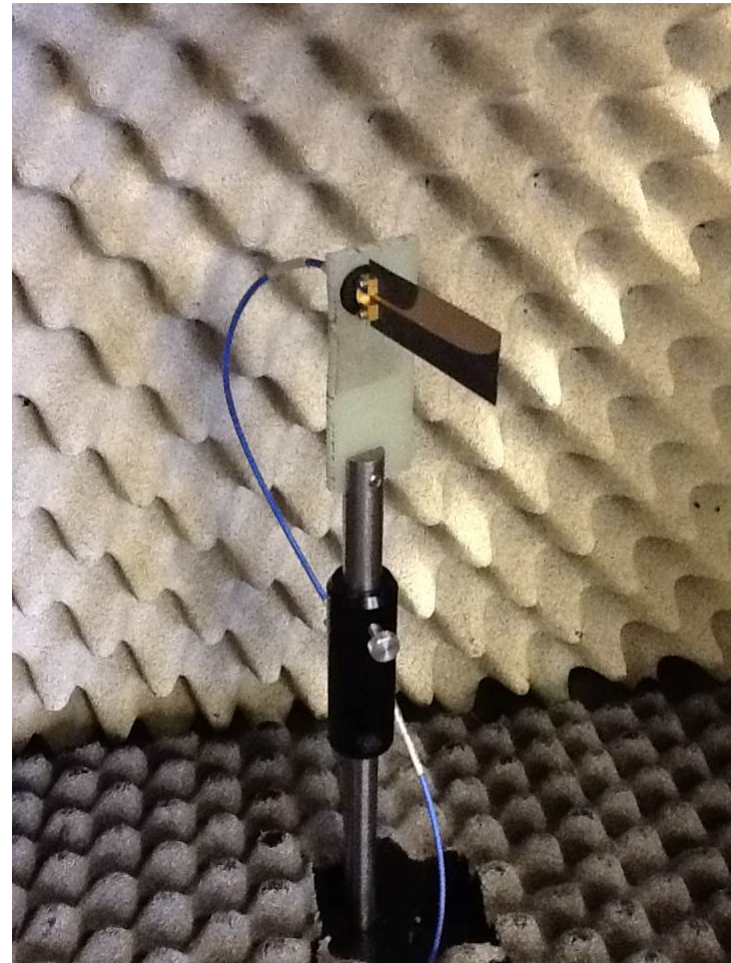
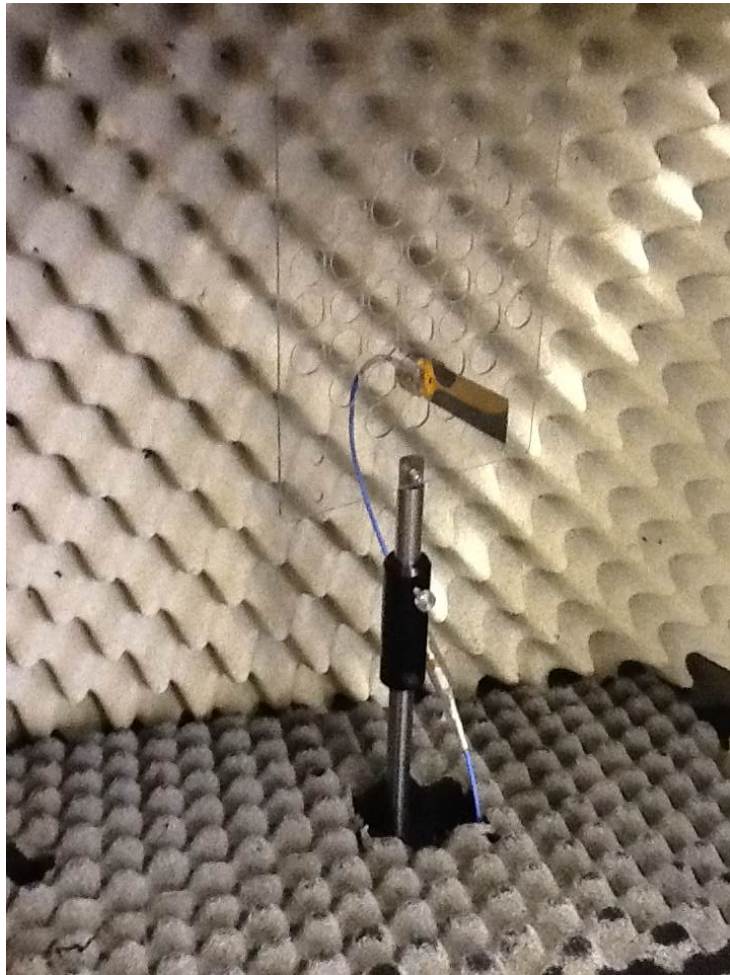


Clear trend of decreasing apparent pitch with increasing  $n_e$ .





# Single antenna setups

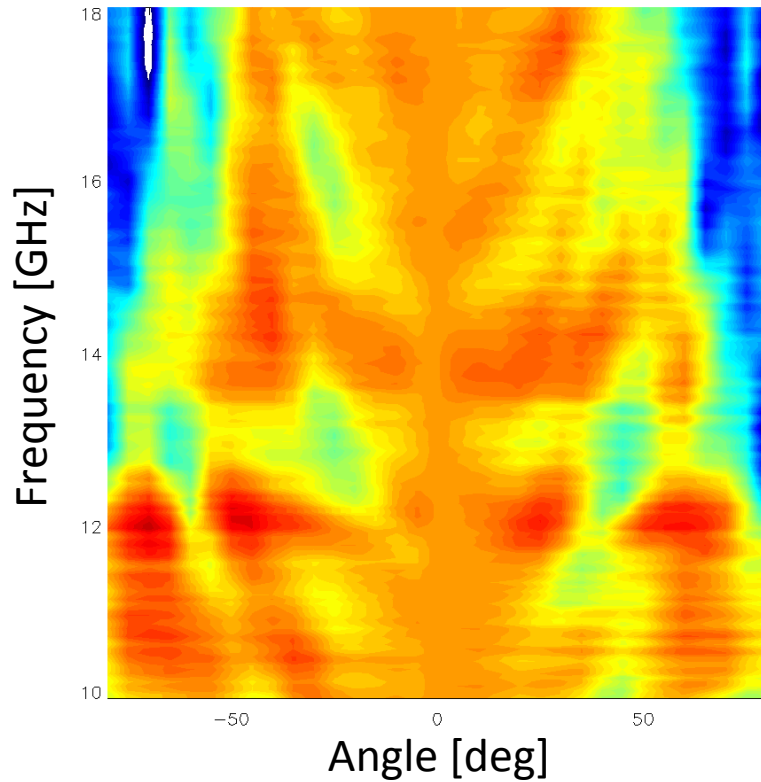


# Normalised straight ahead and power in dB

Colour range = -15dB – >5 dB

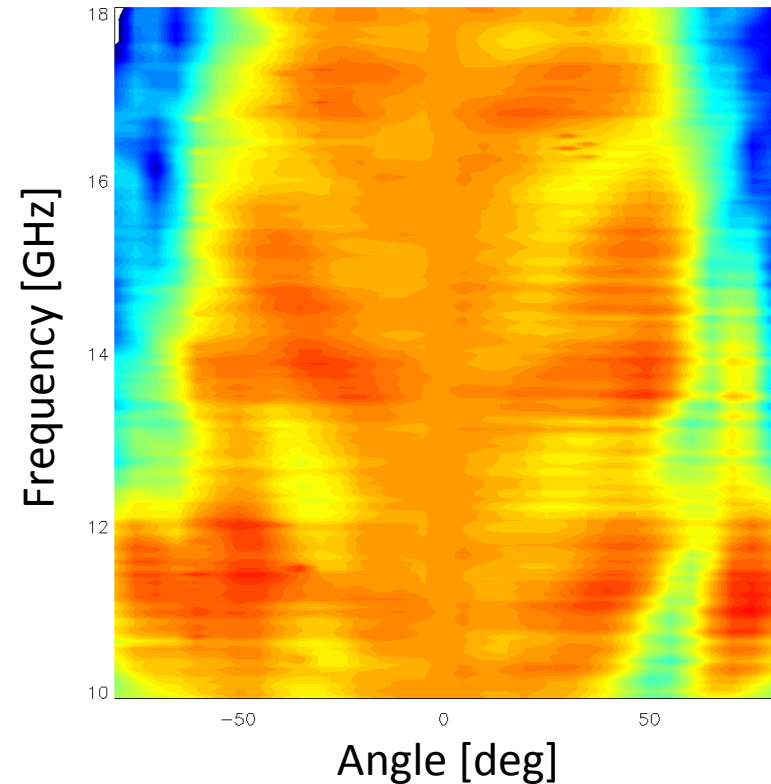
## With holder

with holder



## No holder

with no holder

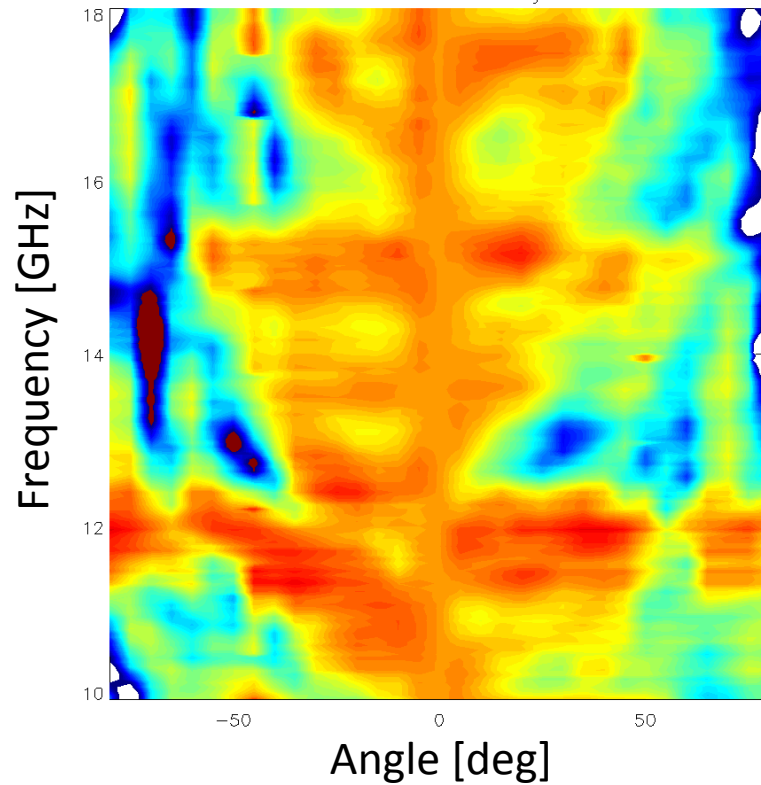


# Antenna comparisons

Colour range = -15dB – >5 dB

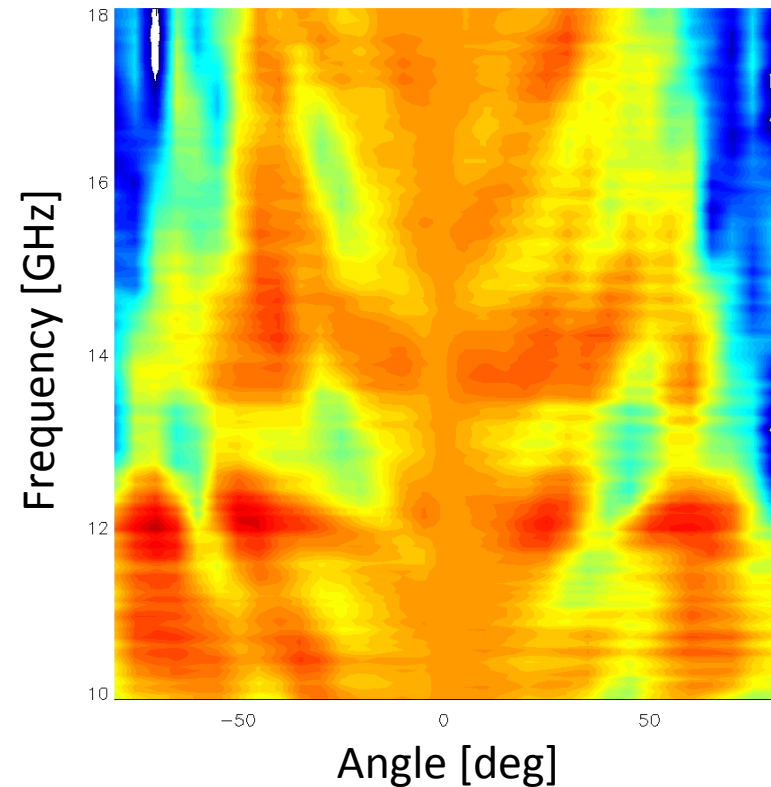
## Antenna 4 in array

antenna 4 in array



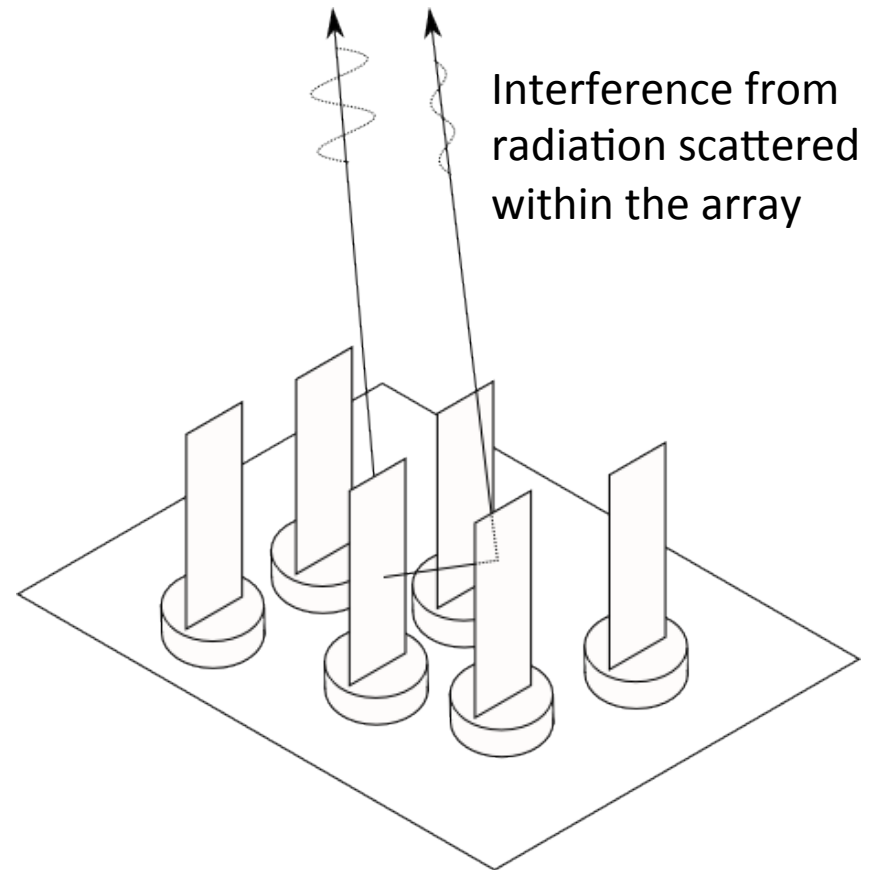
## Single antenna

with holder



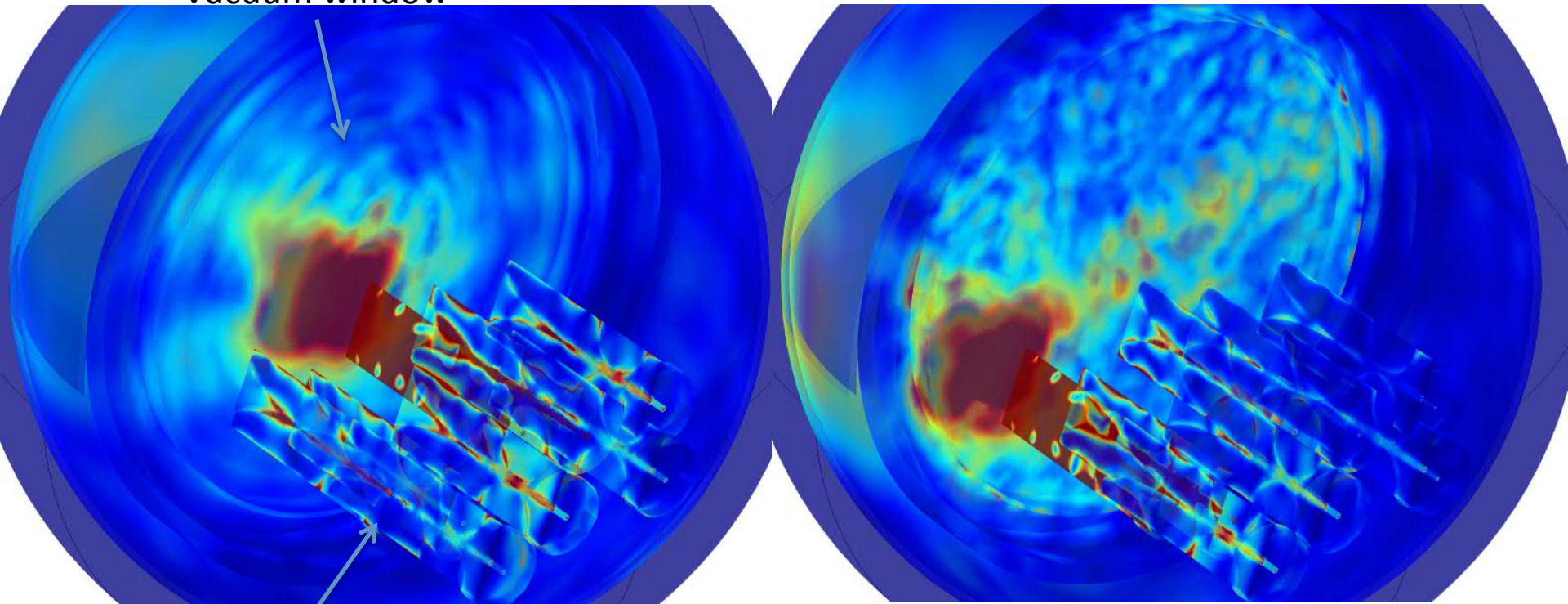
# 3D array effects distort antenna beam patterns

- The presence of other antennas distorts the beam pattern.
- The antenna cross talk is too low to be causing the issue.
- A full wave model of the array is required to diagnose and correct the problem.
- We perform modelling using a commercial package called COMSOL.



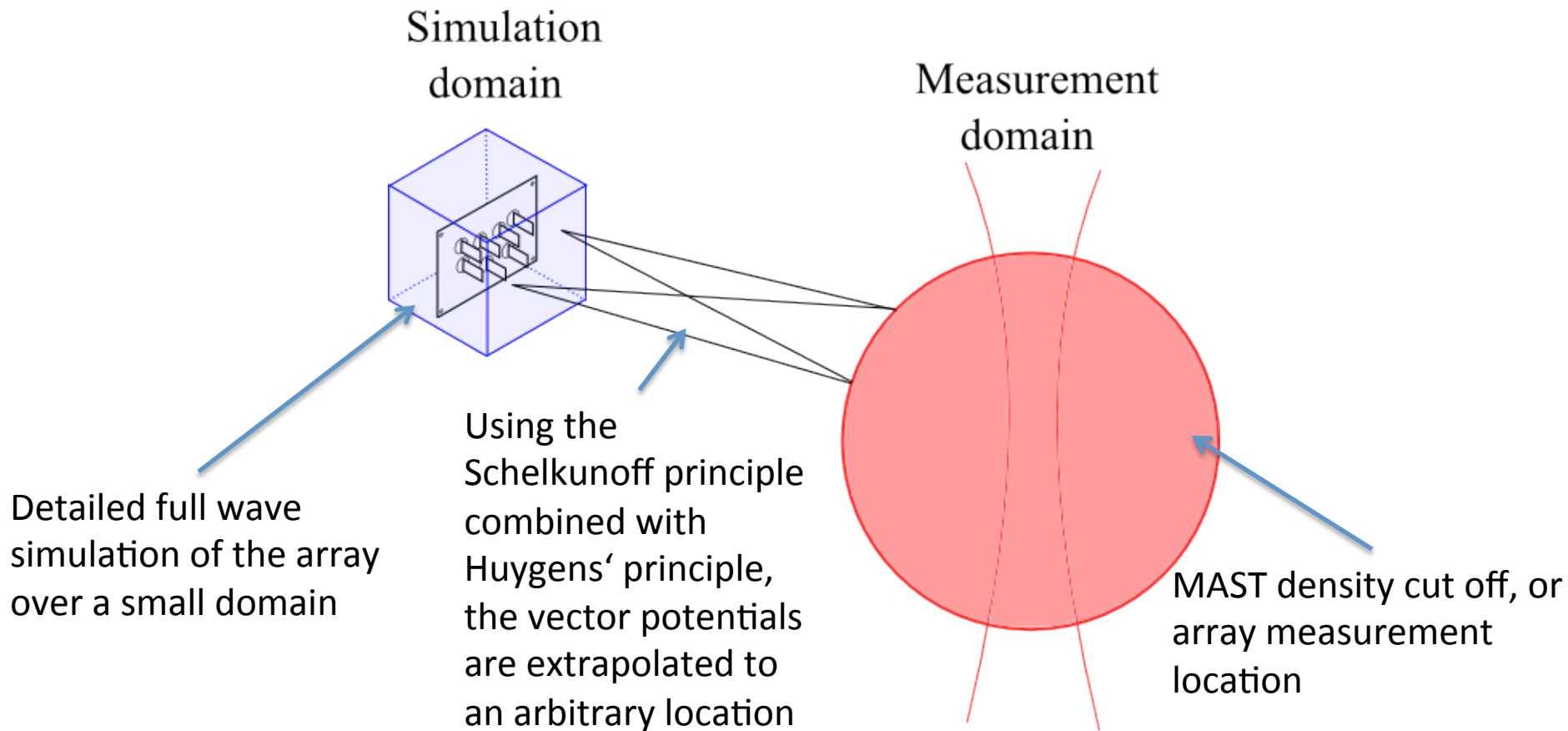
# Array modelling

Vacuum window



Antenna array

# Full wave extrapolation to measurement domain



# Future developments for SAMI



- Dual polarisation planar “sinuous” antennas
- Very stable phase centre
- Planar PCB antenna, avoids 3D field scattering effects.
- Cavity backed to control backwards pointing lobes

# Outline

- Introduction and motivations – S. J. Freethy
  - Introduction to SAMI
  - Introduction to EBW emission
  - Results from MAST
- Reflectometry and backscattering – D. Thomas
  - Multiple reflectometers
  - Backscattering and doppler shifts
- Technical developments and upgrade – J. Brunner
  - FPGAs
  - The SAMI digitiser
  - FPGA/GPU data “real-time” data processing



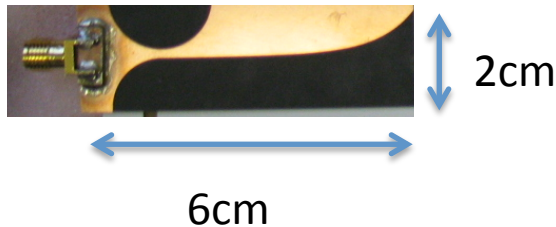
# Active Probing on SAMI



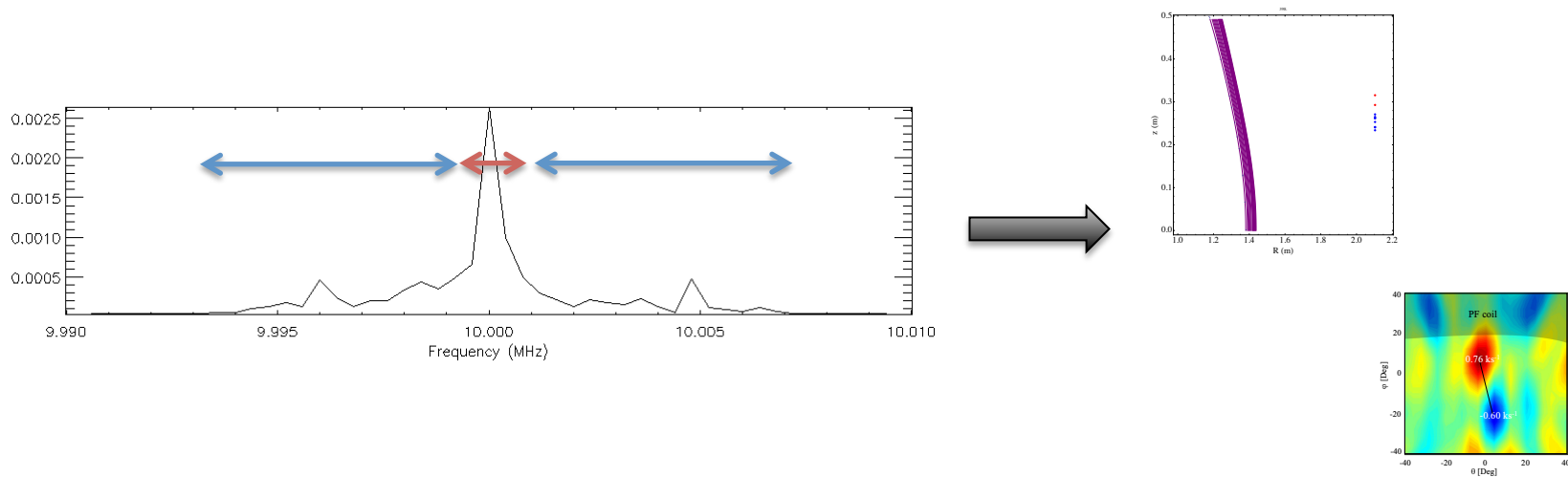
2 Active Probing Antennas

8 Receiving Antennas

- SAMI can actively probe the plasma with two different IF frequencies (10,12 MHz) simultaneously
- The back scattered signals are then received by the 8 receiving antennas
- This can be done for 16 different frequencies 10-35GHz



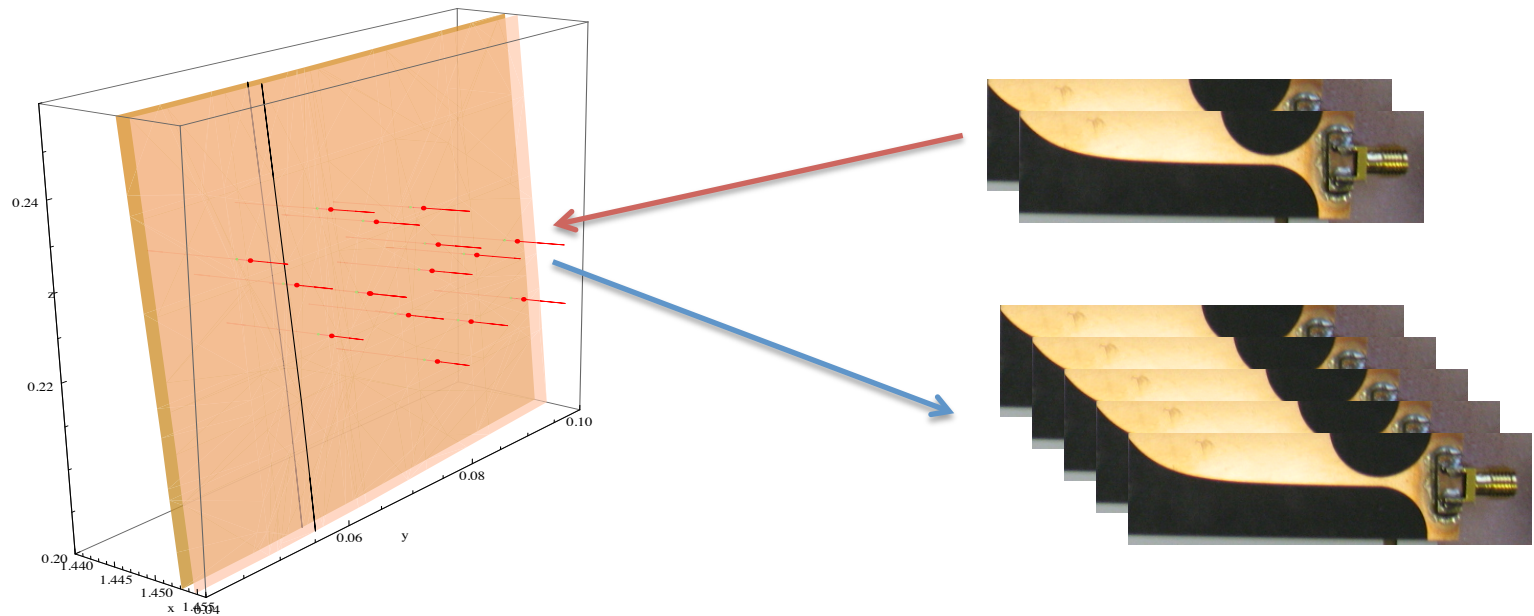
# Reflectometry using SAMI



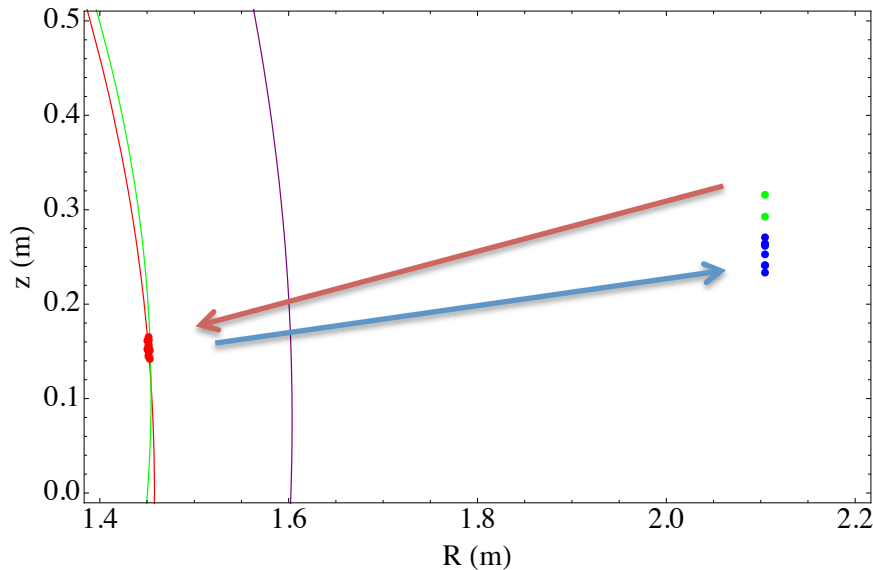
- Use a very small part of the IF frequency spectrum for reflectometry
- This is how it is possible to carry out passive and active imaging at the same time

# Reflectometry using SAMI (cont'd)

- Having 2 active probing antennas and 8 receiving antennas means that we measure 16 different phases



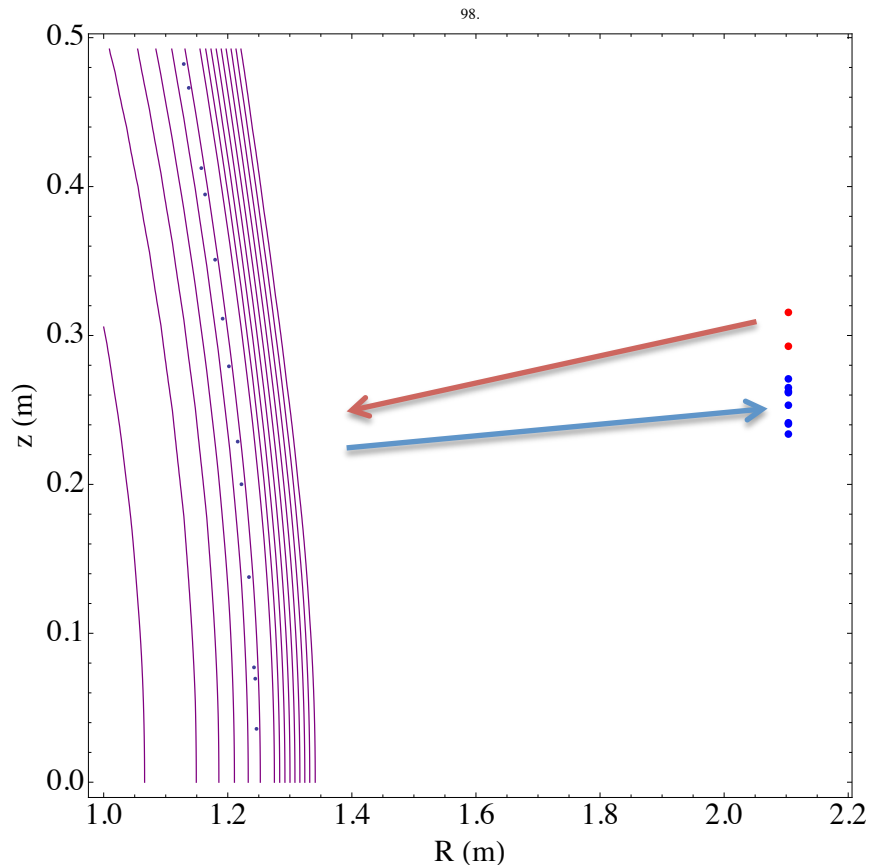
# Reflectometry fitting procedure



$$x = [R - b + (a + b \cos \theta) \cos(\theta + \delta \sin \theta)] \cos \phi$$
$$y = [R - b + (a + b \cos \theta) \cos(\theta + \delta \sin \theta)] \sin \phi$$
$$z = z_0 + k a \sin \theta$$

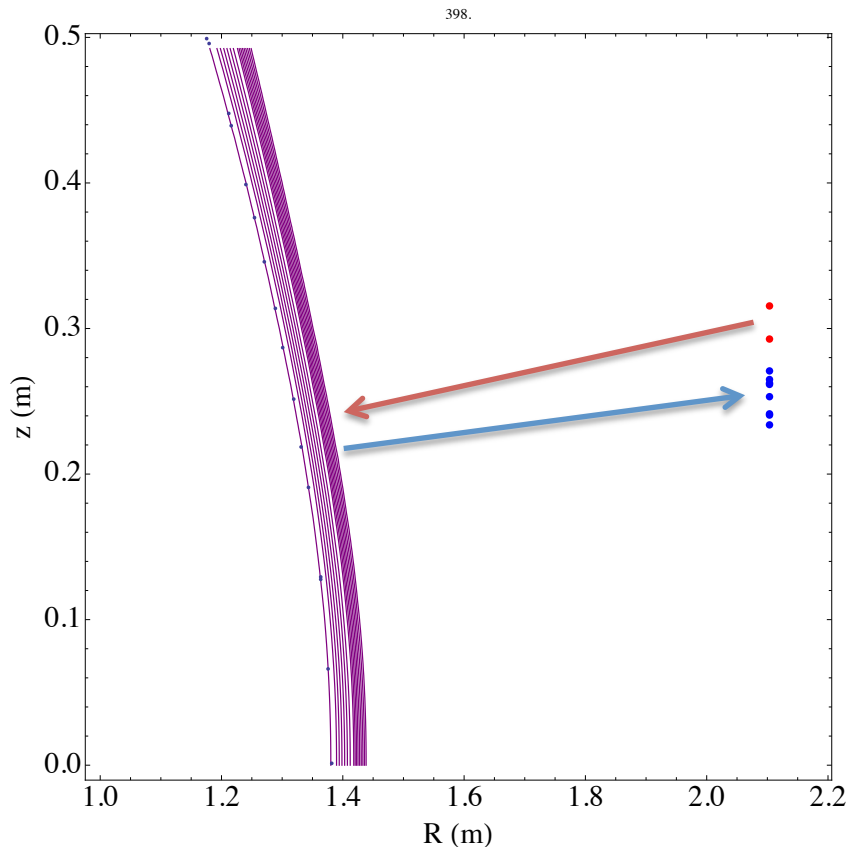
- Using the differences in the phases we numerically minimize a function until we have a best fit
- This fitting procedure has been tested on synthetic data
- Applying this fitting procedure to SAMI data is ongoing

# L-mode 98ms into MAST shot #27246



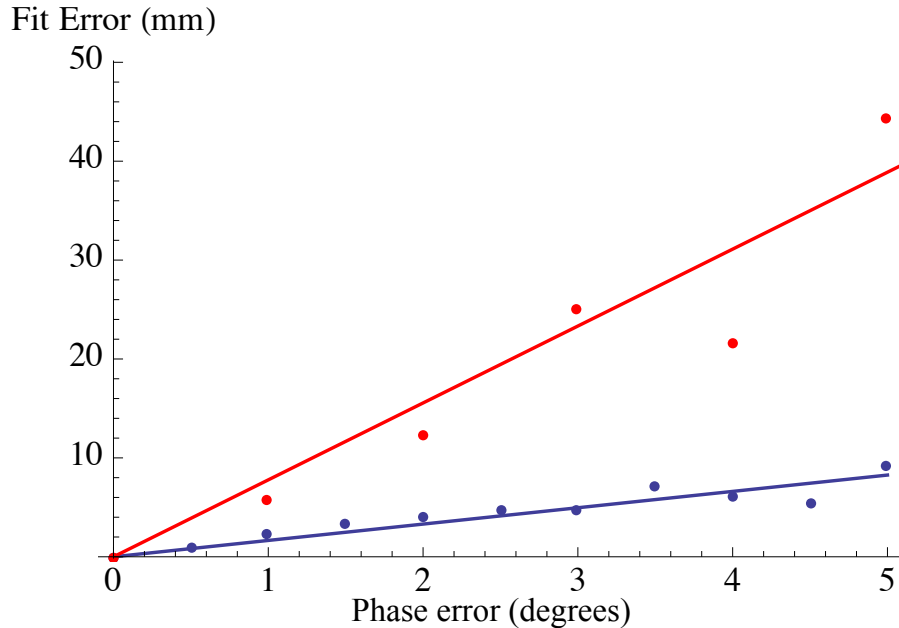
- The black dotted line represents the LCFS as calculated by EFIT
- The plasma density data is generated by Thomson Scattering along the mid-plane coupled to flux surfaces calculated by EFIT
- The red and blue dots represent the emitting and receiving antennas respectively.
- The purple surfaces represent contours where the plasma frequency is equal to one of the SAMI imaging frequencies.

# H-mode 359ms into MAST shot #27246



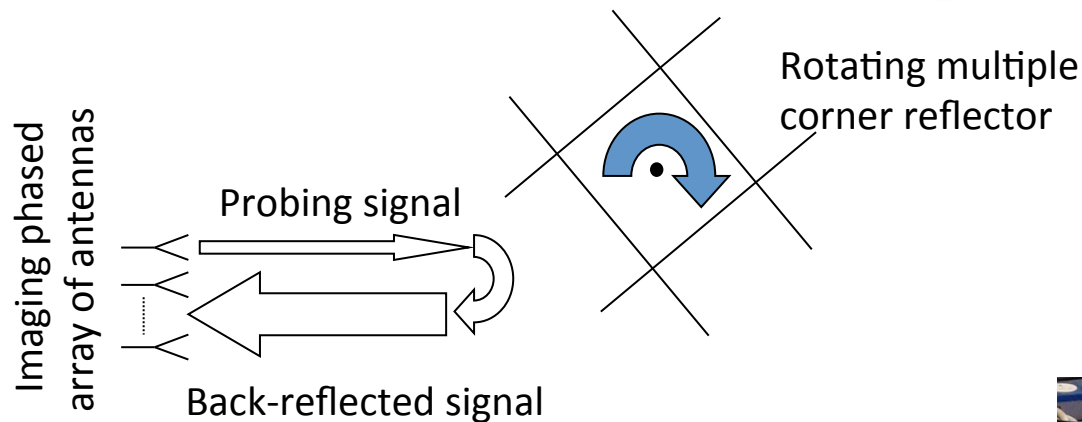
- We see that in H-mode all of the reflection surfaces are bunched up in the edge region
- This means we could get density measurements with a spatial resolution of  $\sim 3\text{mm}$  in the pedestal during H-mode.
- The accuracy at which we will be able to make these measurements is yet to be determined.

# Accuracy of fitting

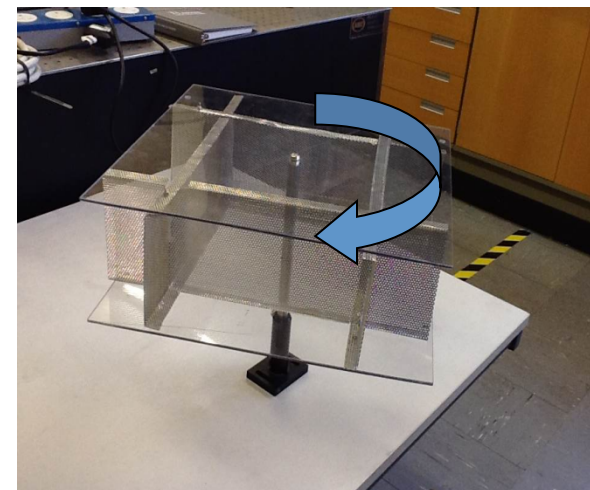


- A 2<sup>nd</sup> Active probing antenna has already been added to SAMI and a third could potentially be added in the future
- Very accurate pedestal density measurements could potentially be made

# Doppler Reflectometry test setup

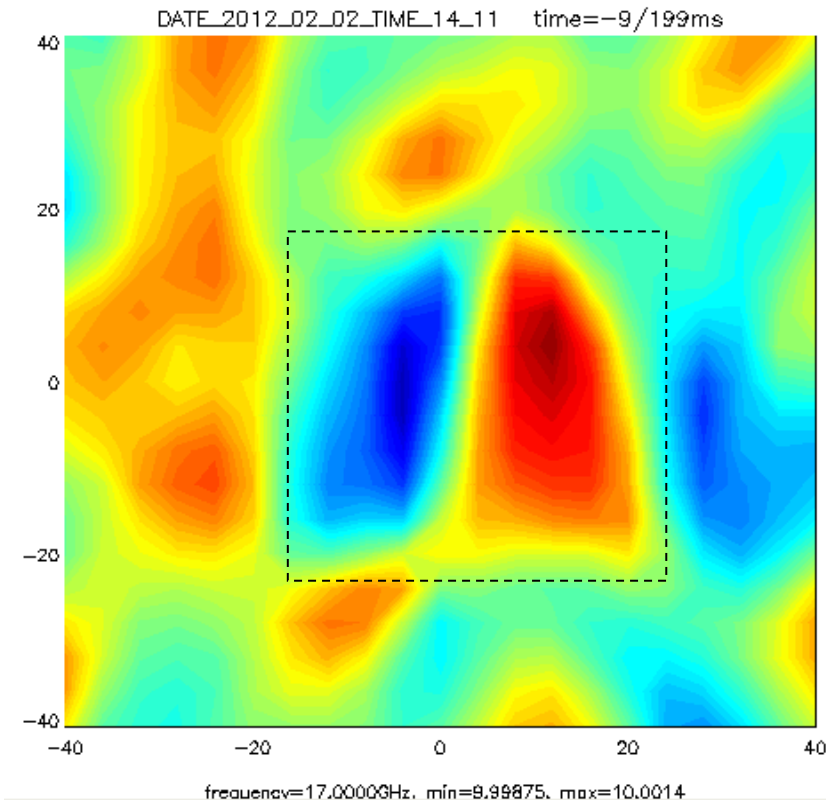


Rotating corner reflector was used in calibration





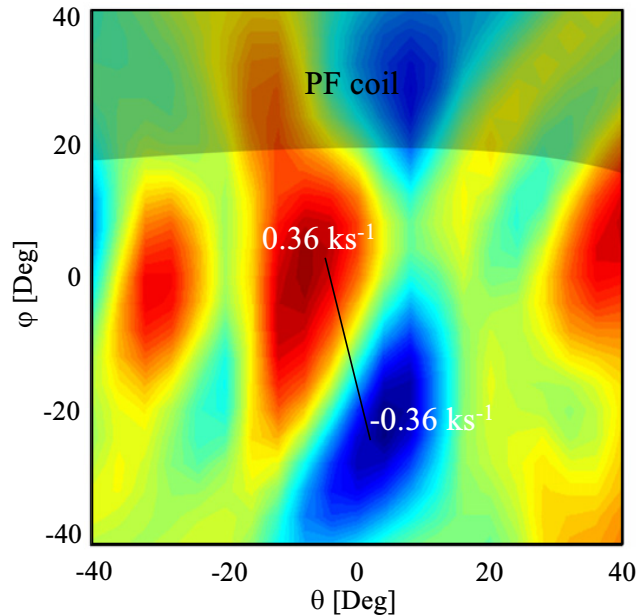
# Doppler test setup results



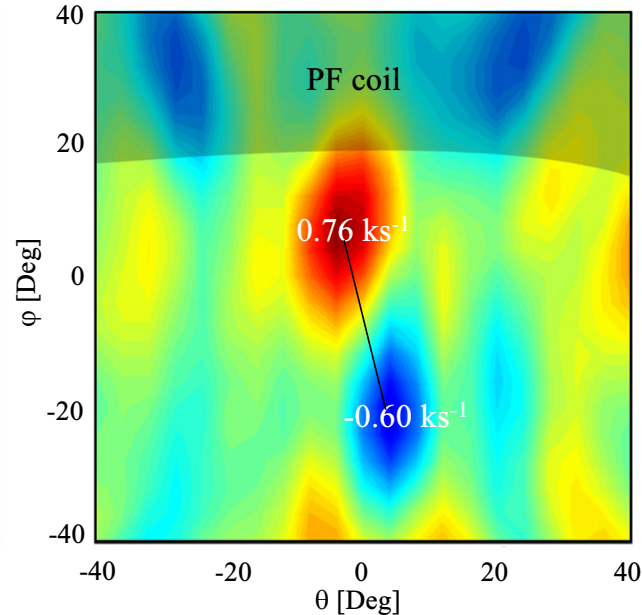
- Here we show a beam formed image of the rotating mesh at 17GHz time integrated over 200ms
- Red and blue shifted signals are apparent in the spatial locations we would expect.
- The amount of Doppler shift observed is  $\pm 250\text{Hz}$  which corresponds to a rotation rate of 3 rotations/sec consistent with the rotation speed used.

# Plasma results

13GHz

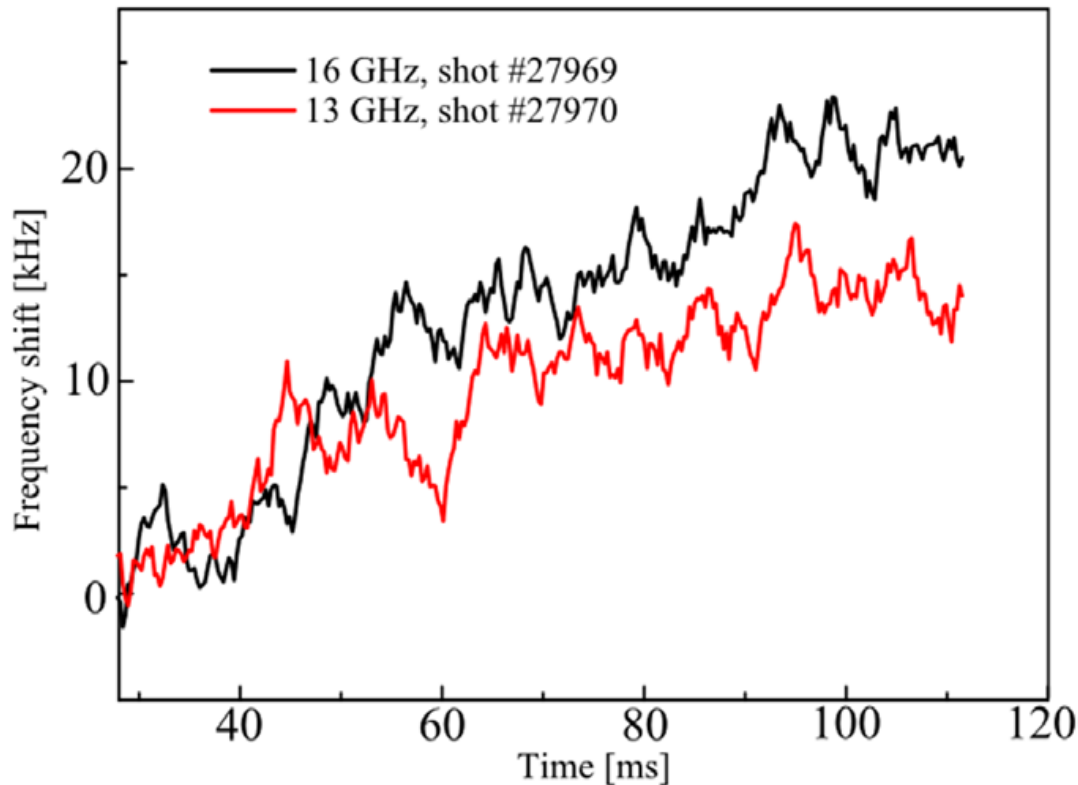


16GHz



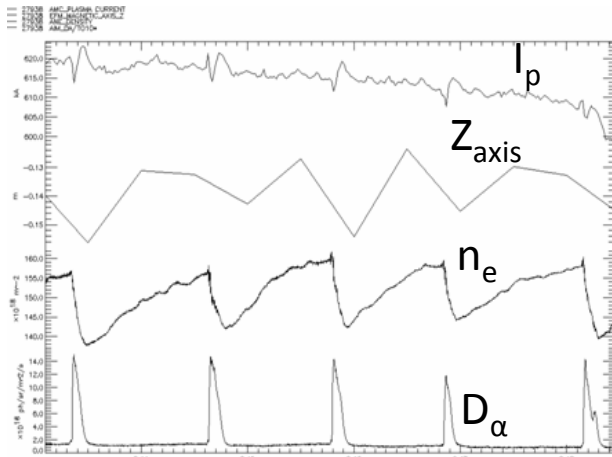
- Images averaged over 10ms at 13 and 16GHz respectively.
- The spatial structure in the Doppler shift as the observed radiation is predominantly Bragg backscattered radiation from plasma turbulent structures aligned along the magnetic field.

# L-mode spontaneous rotation

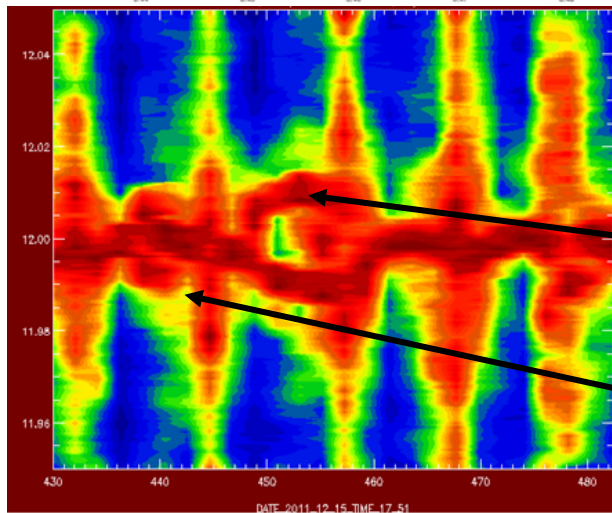


- Doppler shift as a function of time for 13 and 16 GHz.
- 16GHz is reflected from a deeper layer in the plasma.
- The 16 GHz layer is accelerated to a higher rotation velocity.

# Coherent structures in Doppler Spectrum



- Doppler back scattered (DBS) spectra plotted against time illustrate dynamics during and in between ELMs
- Coherent structures visible during ELMS



Coherent structure destroyed by ELM

Coherent structure collapsed itself

# Aims on NSTX-U using active probing

- Make high resolution density measurements in the edge region of NSTX-U plasma. Plasma  $\sim 70\text{cm}$  away on MAST,  $\sim 15\text{cm}$  away -NSTX-U relative phase difference larger. This will aid reflectometry.
- Obtain Doppler maps of NSTX-U plasma
- Resolve coherent MHD structures using the spectrum of Doppler back scattered signals

# Outline

- Introduction and motivations – S. J. Freethy
  - Introduction to SAMI
  - Introduction to EBW emission
  - Results from MAST
- Reflectometry and backscattering – D. Thomas
  - Multiple reflectometers
  - Backscattering and Doppler shifts
- Technical developments and upgrade – J. Brunner
  - FPGAs
  - The SAMI digitiser
  - FPGA/GPU data “real-time” data processing

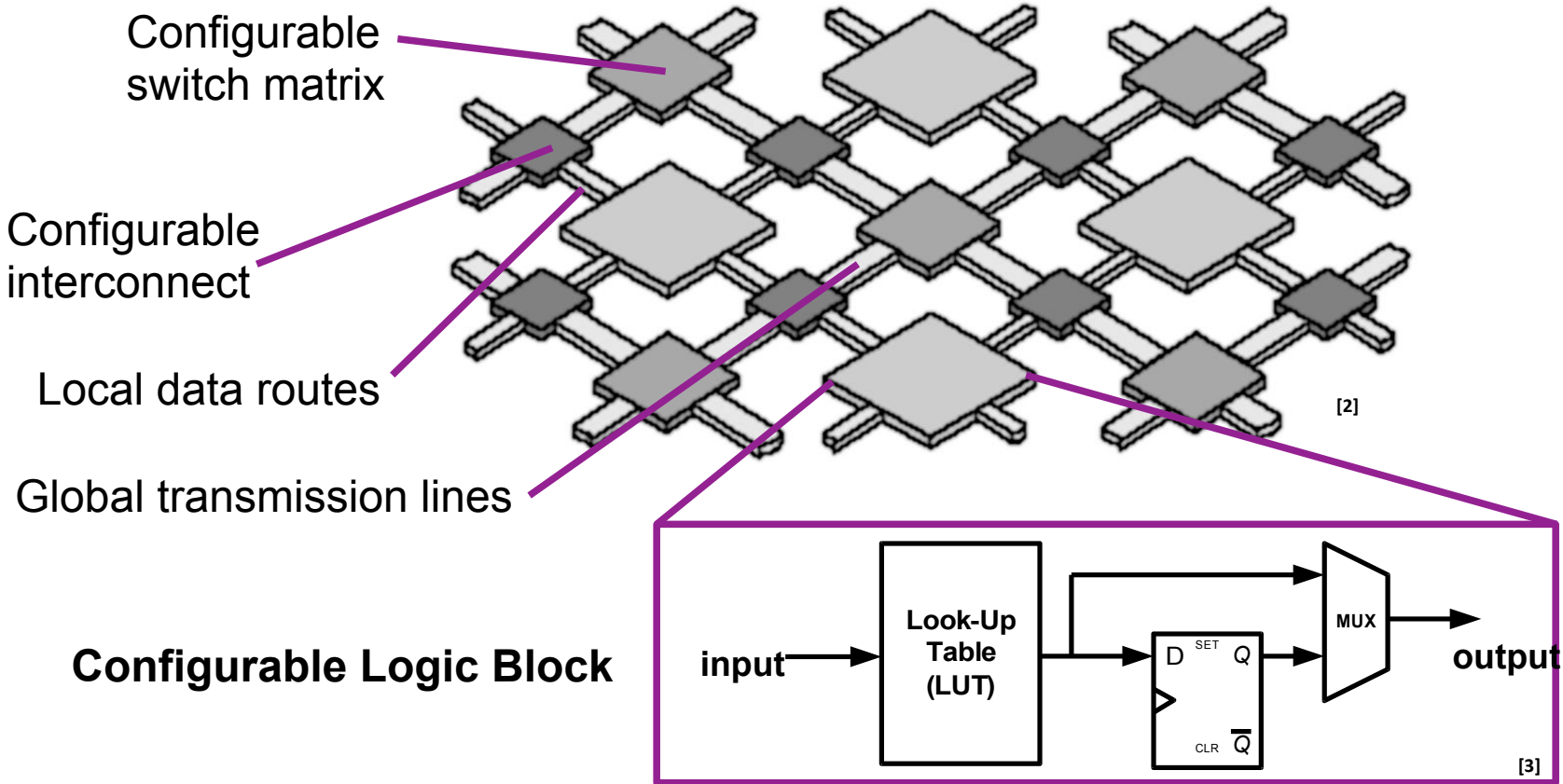
# Fast digitization for SAMI



- SAMI strongly dependent on synchronized high speed data acquisition across multiple channels
- At the same time variable configurations, i.e. active probing & passive imaging
- FPGAs enable high speed data acquisition for high bandwidth whilst allowing reconfiguration

[1] Shevchenko, V. F.; Vann, R. G. L.; Freethy, S. J. & Huang, B. K.  
“Synthetic aperture microwave imaging with active probing for fusion plasma diagnostics”  
*Journal of Instrumentation*, **2012**, *7*, P10016

# FPGA basics – the fabric

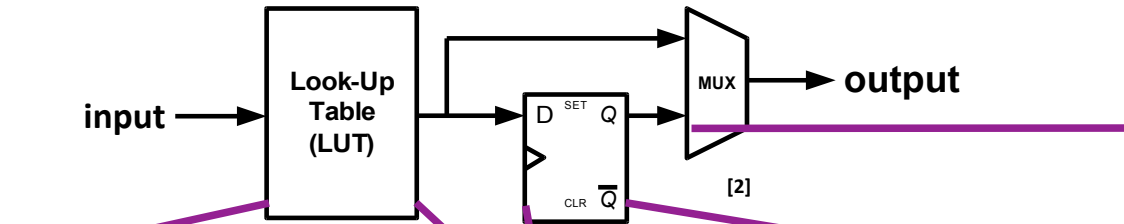


[2] "Introduction to Programmable Logic"; J. Coughlan.; RAL Technology Department, Lecture series 2007

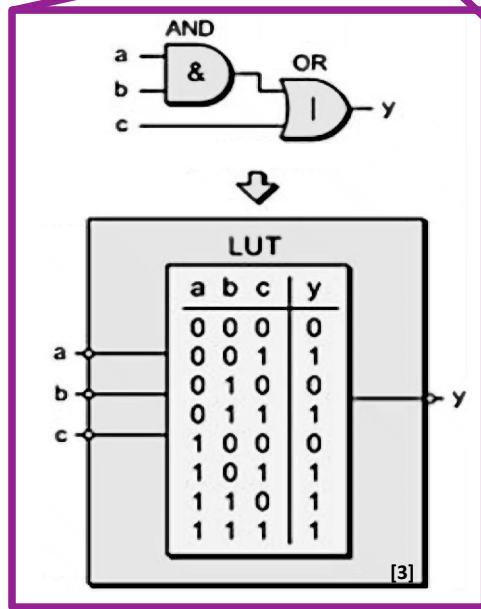
[3] "Computer Architecture I – Laboratory Exercises Background and Introduction to FPGAs"; Konstantinos Tatas; Lecture series



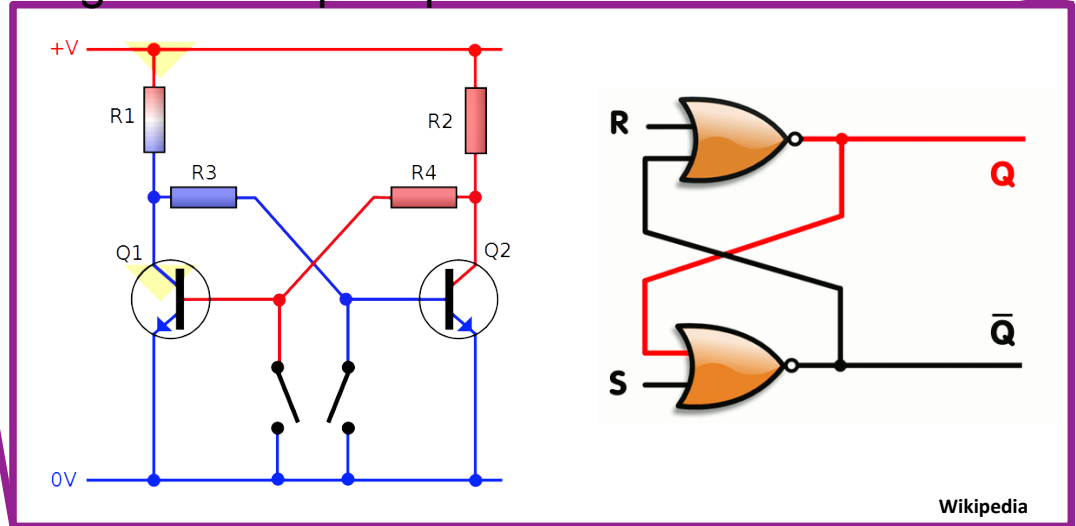
# FPGA basics – the CLB



Multiplexer is controlled and decides whether the output is registered



## Register or Flip Flop

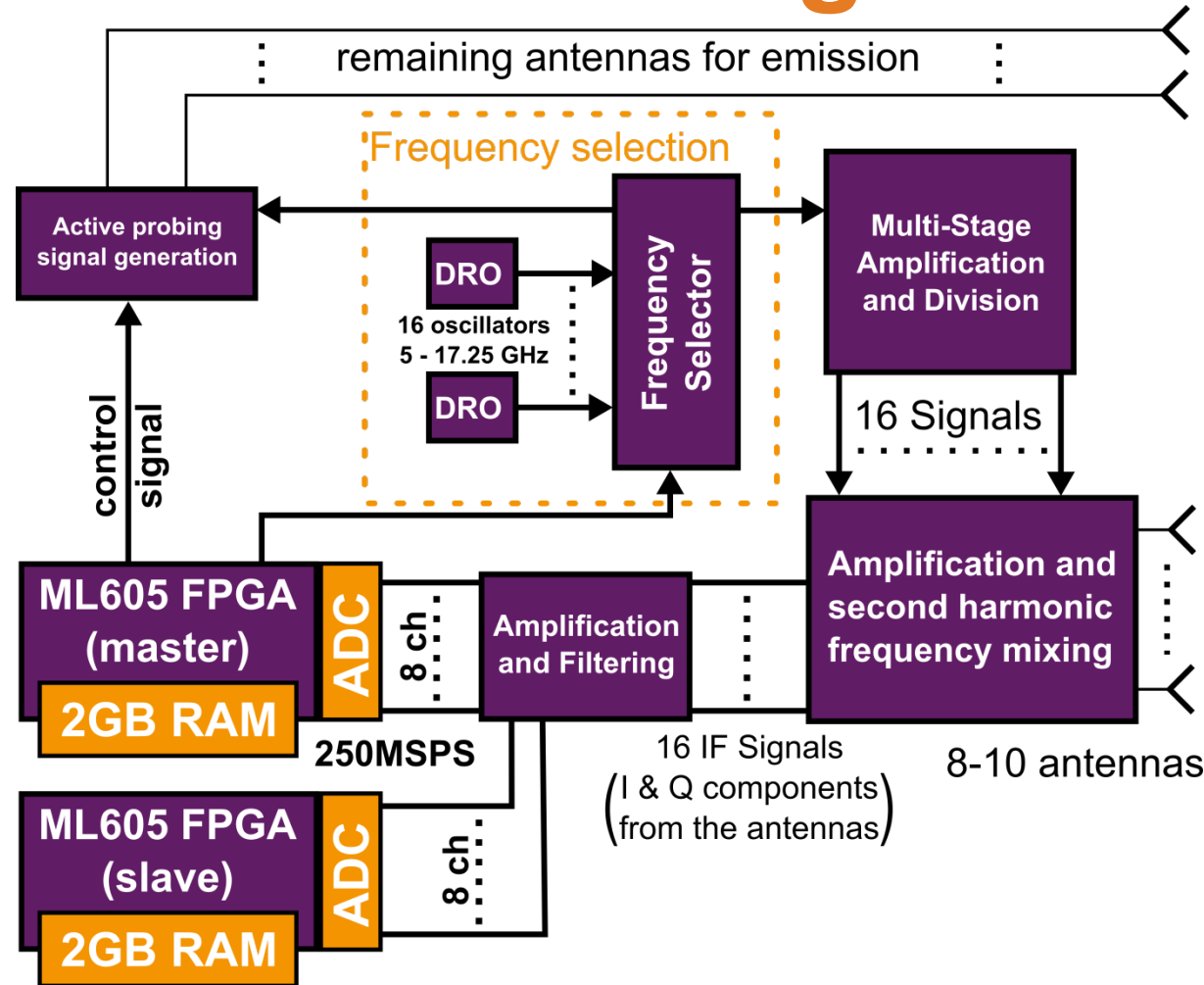


[4] "Computing Performance Benchmarks among CPU, GPU, and FPGA"; Cullinan, C. and Wyant, C. and Frattesi, T. and Huang, X.; MathWorks; Apr 2012; E-project-030212-123508

# FPGA basics – features

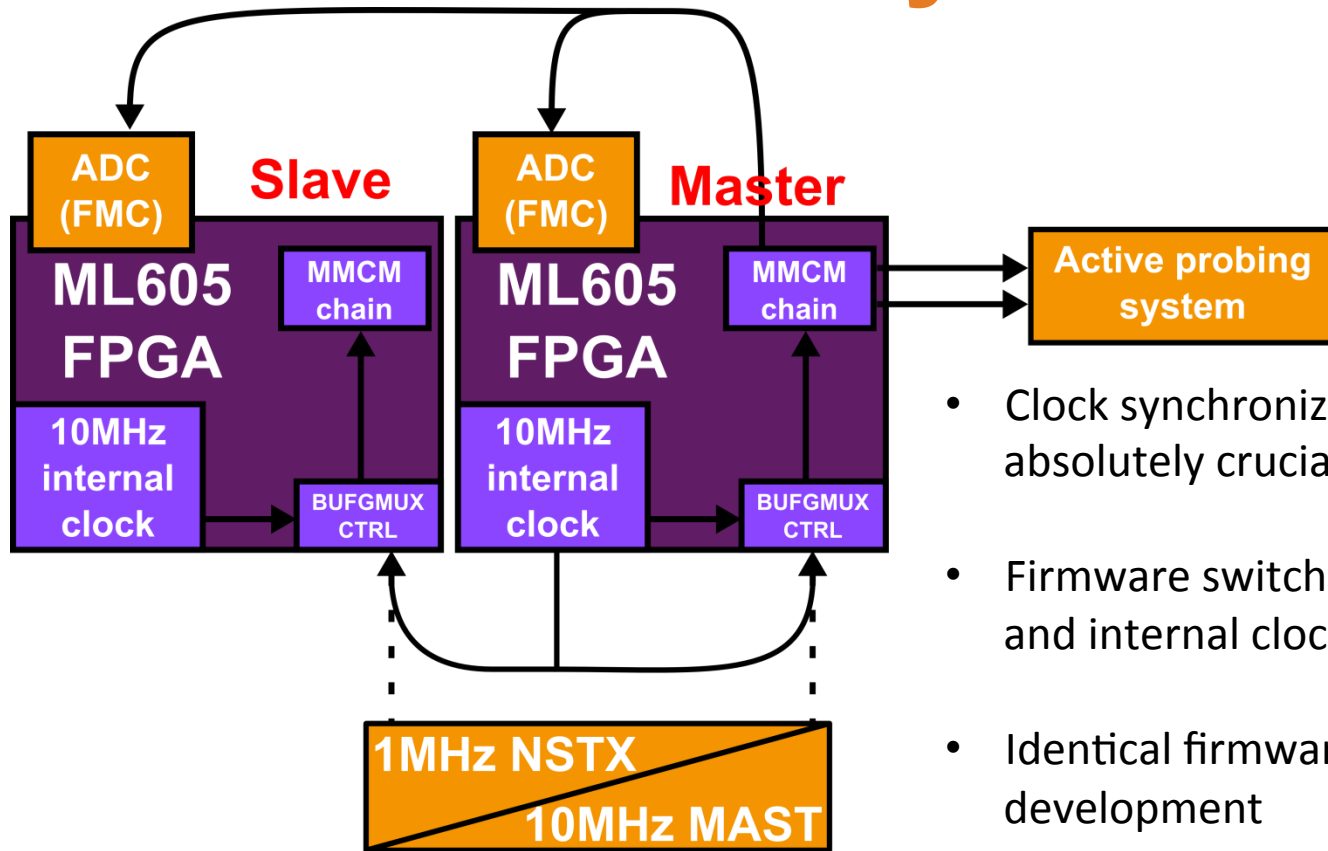
- In modern FPGAs the fabric has additional specialized blocks to enhance performance, i.e.
  - Block-RAM elements(BRAM)
  - Fast general purpose DSPs for multiplication etc.
  - Fast transceiver pins for high speed data transmission
  - Specialized delay blocks for timing
  - Dedicated Clock generation blocks

# FPGA integration in SAMI



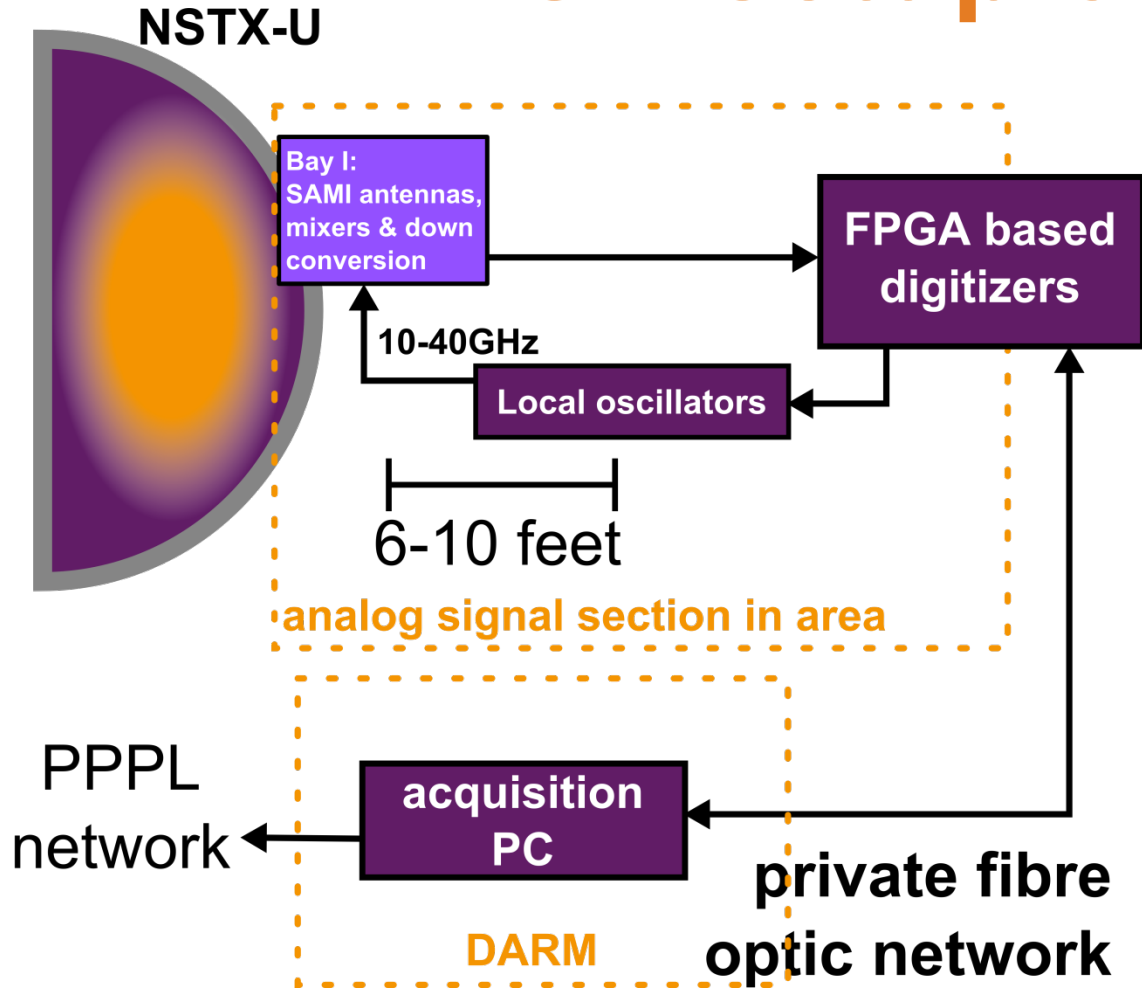
- FPGAs select frequencies from Local Oscillators (set before shot)
- FPGAs provide upconversion signal for active probing
- Currently FPGAs sample at 250MSPS with 14bit
  - 4GB of raw data on 500ms MAST shots
- running Linux on the FPGAs allows us to change the operation mode between shots

# FPGA clock synchronization

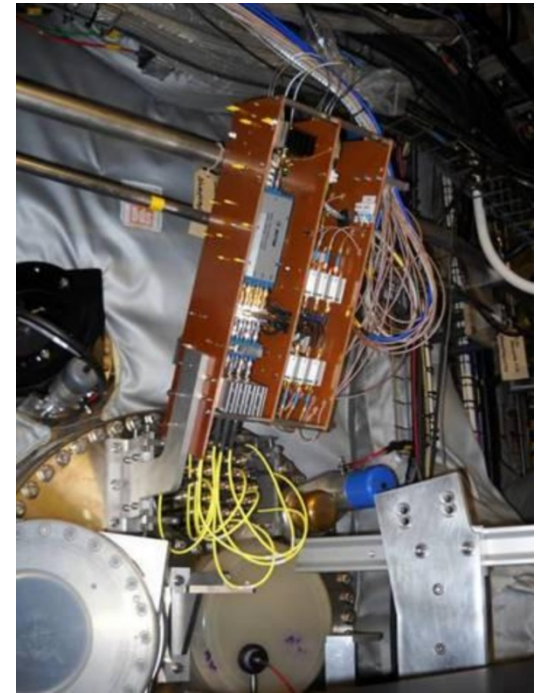


- Clock synchronization across boards is absolutely crucial for SAMI to work
- Firmware switches between an external and internal clock reference
- Identical firmware on both boards eases development
- Due to insufficiencies in reference clocks a board currently supplies the reference

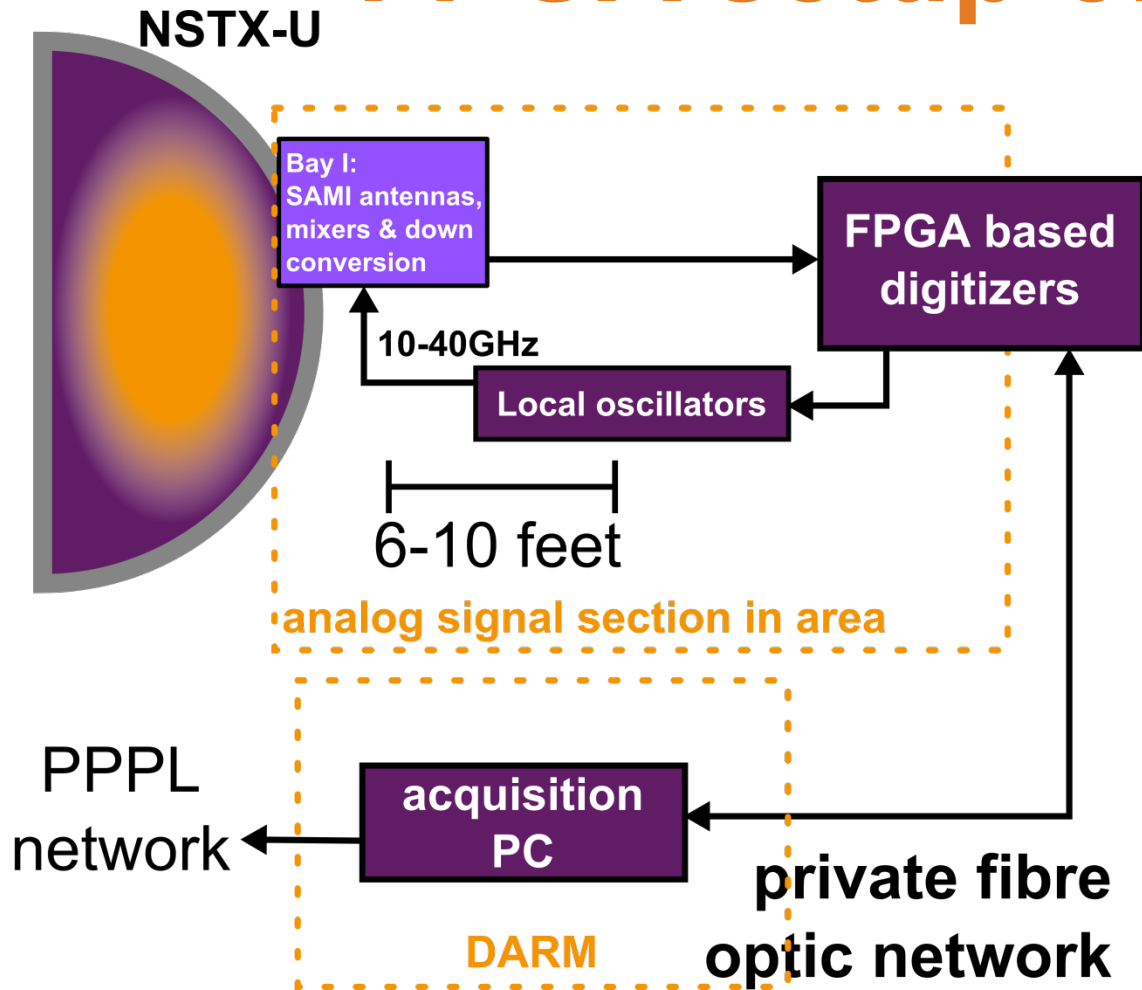
# FPGA setup on NSTX



- Antenna rack with mixers for down conversion are placed directly on the rack



# FPGA setup on NSTX

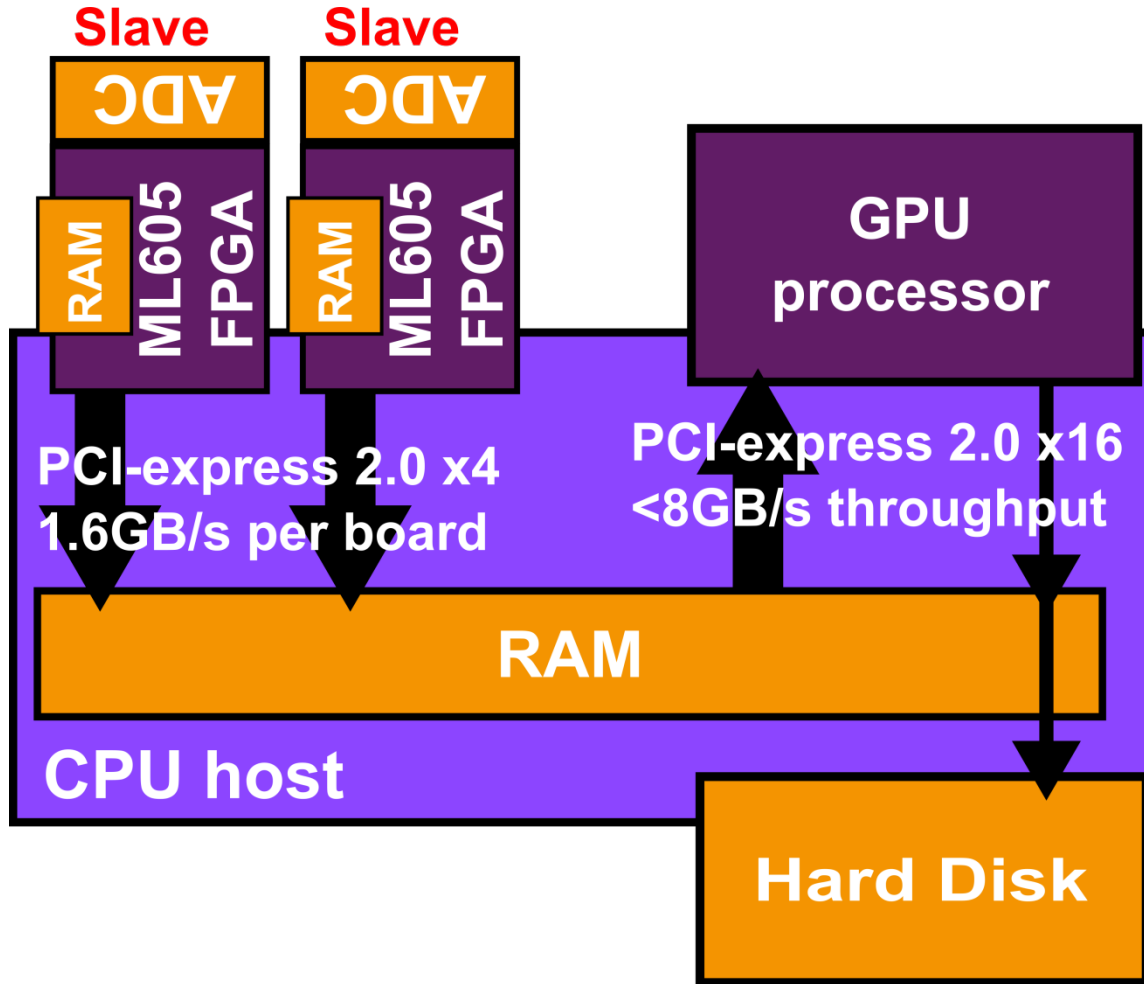


- Antenna rack with mixers for down conversion are placed directly on the rack
- Local oscillators have to stay close to the mixers
- FPGAs have a private fibre optic 100Mbit network with acquisition PC to download data and upload firmware
- The FPGA system is controlled via a webpage based on the acquisition PC

# Moving SAMI forward: new challenges

- Currently SAMI collects 4GB of data per 500ms shot, which barely fits onto the FPGAs without the capability of upgrading the memory capacity
- Bypassing all security measures transfer of data from the FPGAs currently takes 2-3min, however the transmission is not fully reliable
- Processing of that data currently takes about 15-20min: more than the avg. time between MAST shots
- Both NSTX-U and MAST-U plan on operating multiple seconds and hence will require semi-continuous acquisition and thus data streaming with faster processing
- Limits in the currently employed system force us to completely redesign data transfer and processing

# The future of SAMI



- Utilizing on board PCIe connectors transfer time could be reduced to seconds
- Streaming data into CPU host RAM directly and processing it after each shot would significantly increase SAMI operation limits
- Using GPUs to process data on the fly would reduce storage requirements



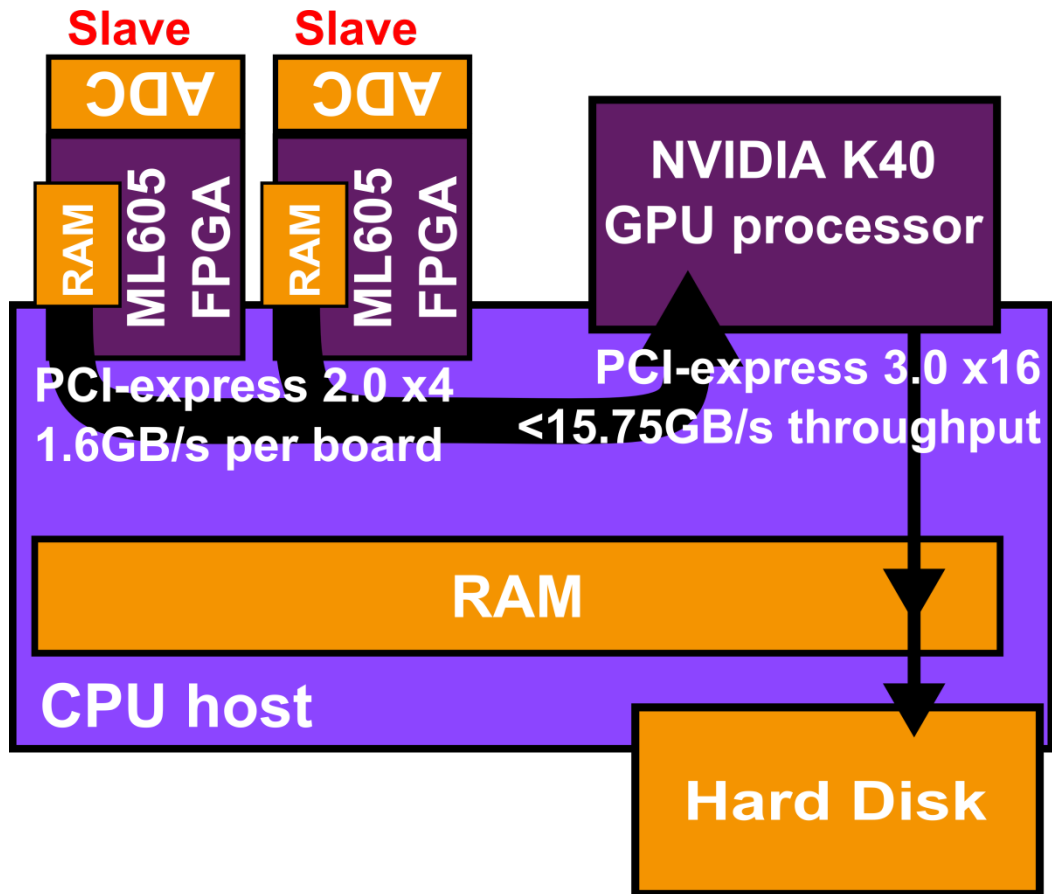
# GPU based processing

(work done by Joanne Chorley)

- Serial IDL based data evaluation takes longer than the time between shots on MAST
- Evaluation algorithm using beam forming is highly parallelizable and thus fit for GPUs
- Main problem for the GPU is memory and transfer time as the data amount doubles on read in and temporarily grows up to triple the size during processing
- Parallelizing the code and “outsourcing it to a GPU brought significant speed up

	Total Algorithm Time[s]	Reading data from Memory [s]	Compute Time(s)
IDL	1038.378	128.32 *	910.058 *
C (serial code)	464.55	88.160 *	376.39 *
CUDA (NVIDIA K40)	17.4238	11.65	5.7748

# An FPGA-GPU tandem



- To achieve maximum data transmission between GPU and FPGAs direct streaming of data between the devices is beneficial
- Treating FPGA memory as an extension to the GPU memory can bypass the CPU host and utilize the maximum speed of the PCIe bridge
- Saving only a fraction of the RAW data plus the processed data should decrease the amount of data by a factor of 2000