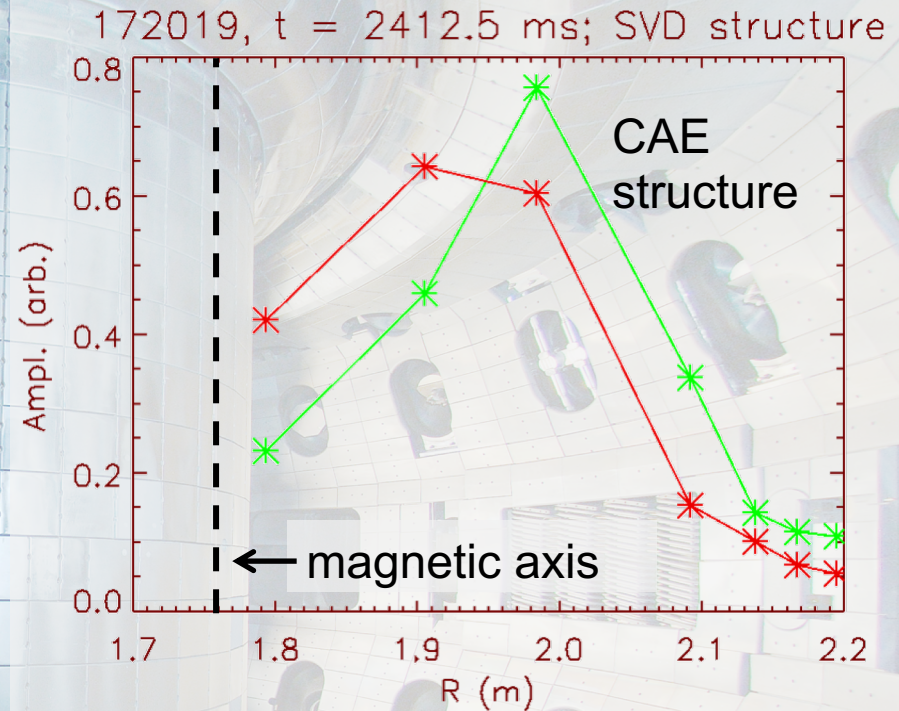


# CAE structure measurements in DIII-D

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NSTX-U/Magnetic Fusion Science Meeting  
NSTX-U/DIII-D National Campaign

Aug. 27, 2018

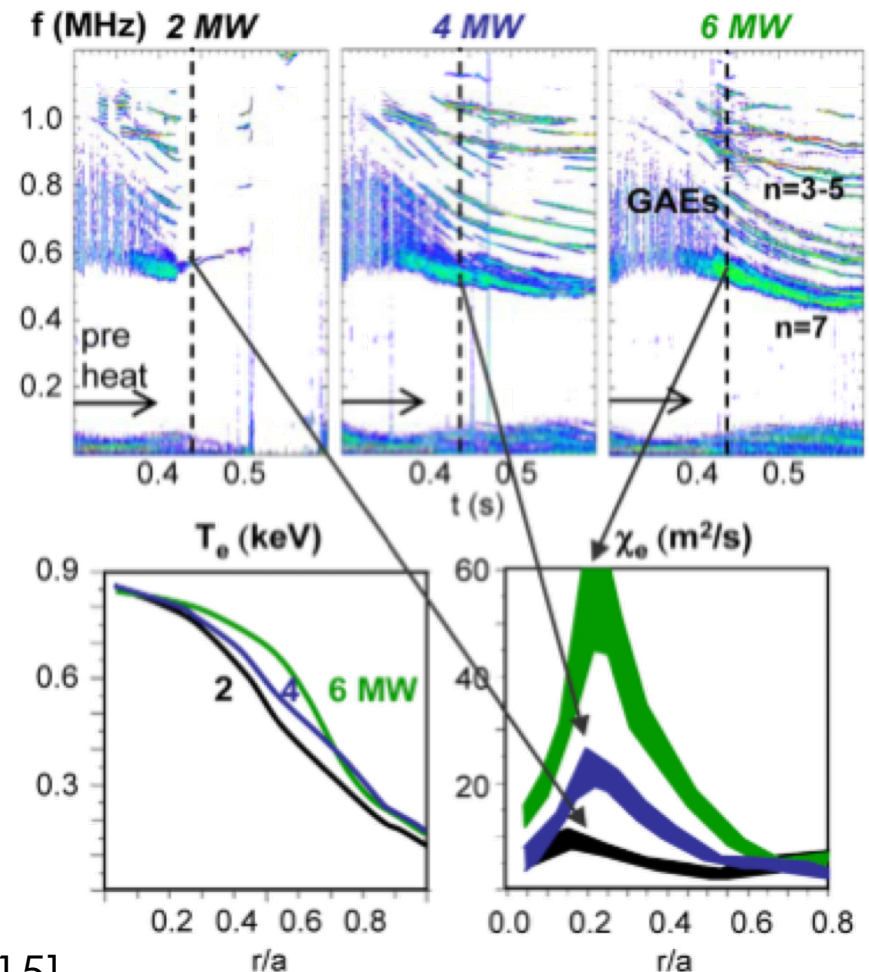


# Understanding of high frequency Alfvén activity important to transport and fast-ion diagnosis

- **Compressional (CAE) and global (GAE) Alfvén eigenmodes linked to enhanced core electron thermal transport ( $\chi_e$ ) in NSTX**
- **CAEs and GAEs are potentially powerful diagnostic for fast-ion population in burning plasma environment**
  - nominally driven by Doppler-shifted cyclotron resonance with fast ions => deeper understanding enables “MHD spectroscopy”

# CAE and GAEs linked to enhanced core electron thermal transport in NSTX

- CAE and GAE activity correlate with enhanced core  $\chi_e$  in NSTX
- Proposed mechanisms:
  - Resonant orbit stochastization => enhanced  $\chi_e$
  - CAEs/GAEs couple to Kinetic Alfvén Waves (KAWs), which channel energy out of the core



[Gorelenkov NF 2010]

[Kolesnichenko PRL 2010], [Belova PRL 2015]

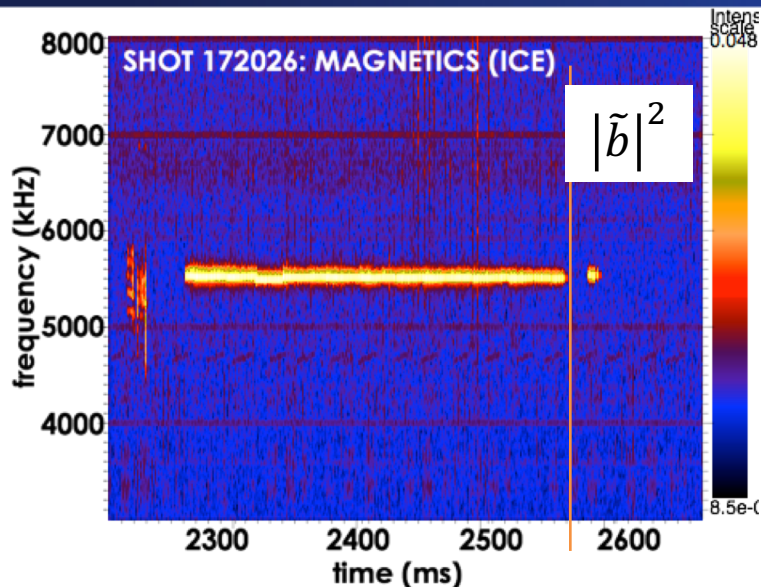
[D. Stutman PRL 2009]

# High frequency Alfvén eigenmodes driven unstable by Doppler-shifted cyclotron resonance with fast ions

- **Compressional/Global Alfvén eigenmodes (CAE/GAE) => same instability as coherent Ion Cyclotron Emission (ICE)**
  - For cyclotron resonance, [N.N. Gorelenkov NF 2003]
$$\omega - k_{\parallel} v_{b\parallel} = l\omega_c, l = \dots, -1, 0, 1, \dots$$
 [Dendy, PoP 1994]
  - $k_{\perp}\rho_b$  stabilizing in some ranges and destabilizing in others
    - Anisotropy important
    - Perpendicular instability condition requires finite orbit widths:
      - CAEs:  $1 < k_{\perp}\rho_b < 2$
      - GAEs:  $2 < k_{\perp}\rho_b < 4$
  - For CAEs,  $\omega^2 \approx k^2 v_A^2$
  - For GAEs,  $\omega^2 \approx k_{\parallel}^2 v_A^2$ 
    - Dispersion relationships modified by finite  $\omega/\omega_{ci}$  - (important to existence of GAEs)



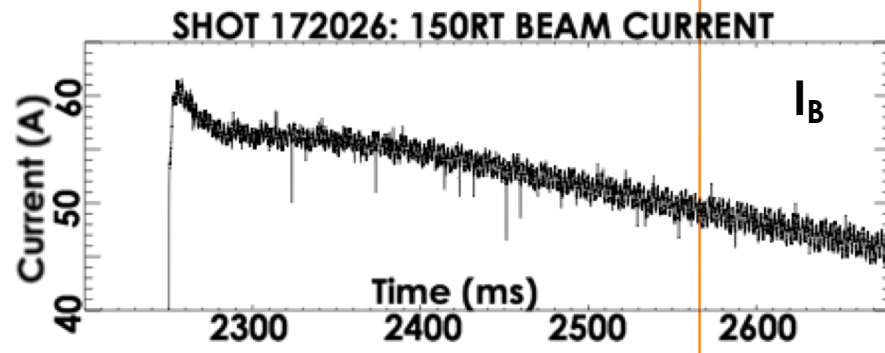
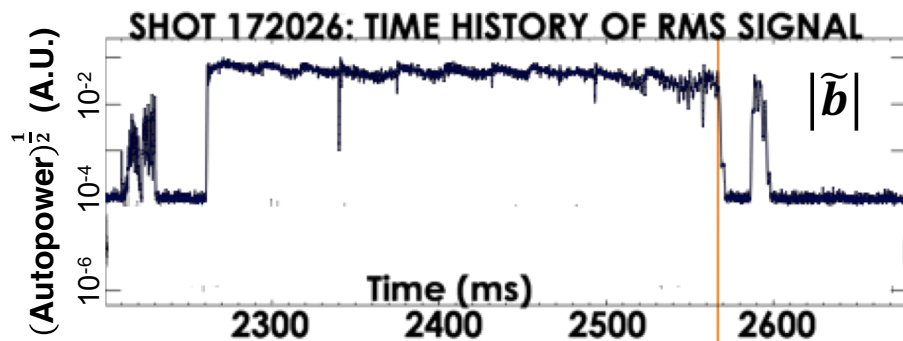
# CAE with observed beam current threshold



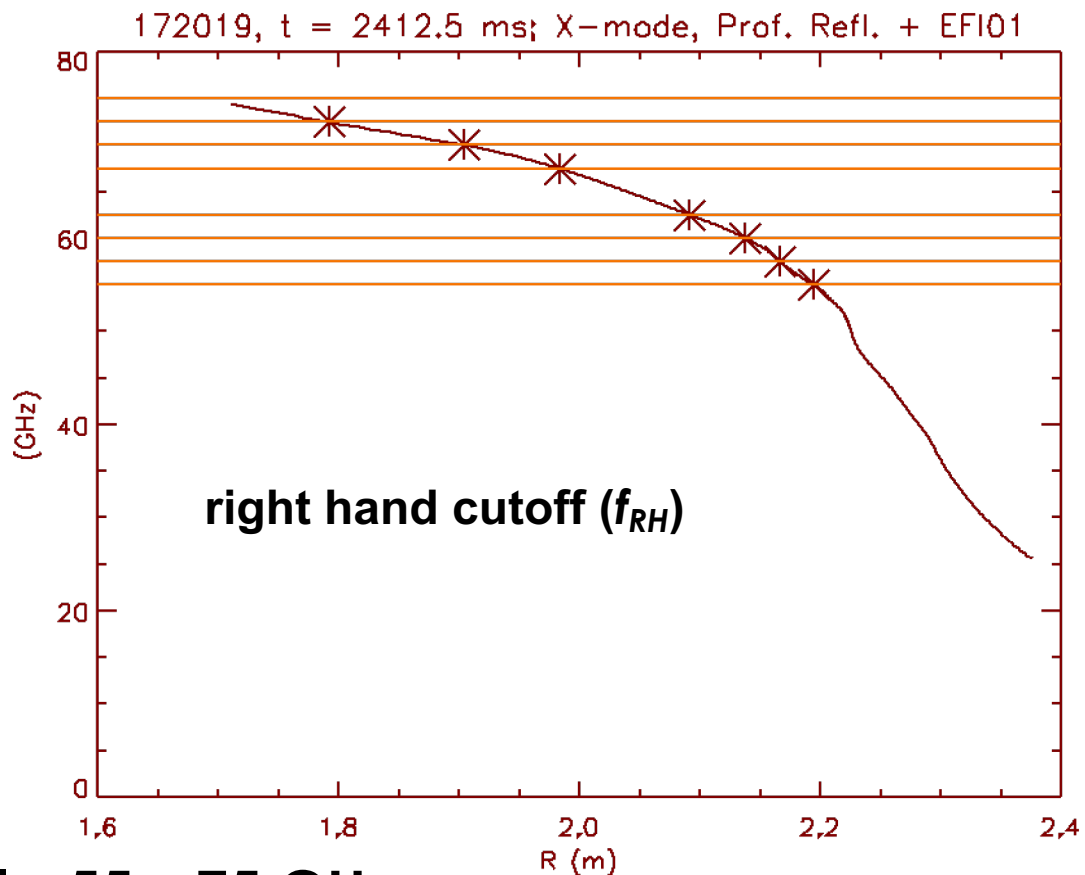
- $V_B$  constant as  $I_B$  ramped (variable perveance)
- CAEs abruptly disappears as  $I_B$  drops below threshold

caveats:

- delay in CAE start => due to beam density build-up?
- CAE reappears => due to sawtoothing?



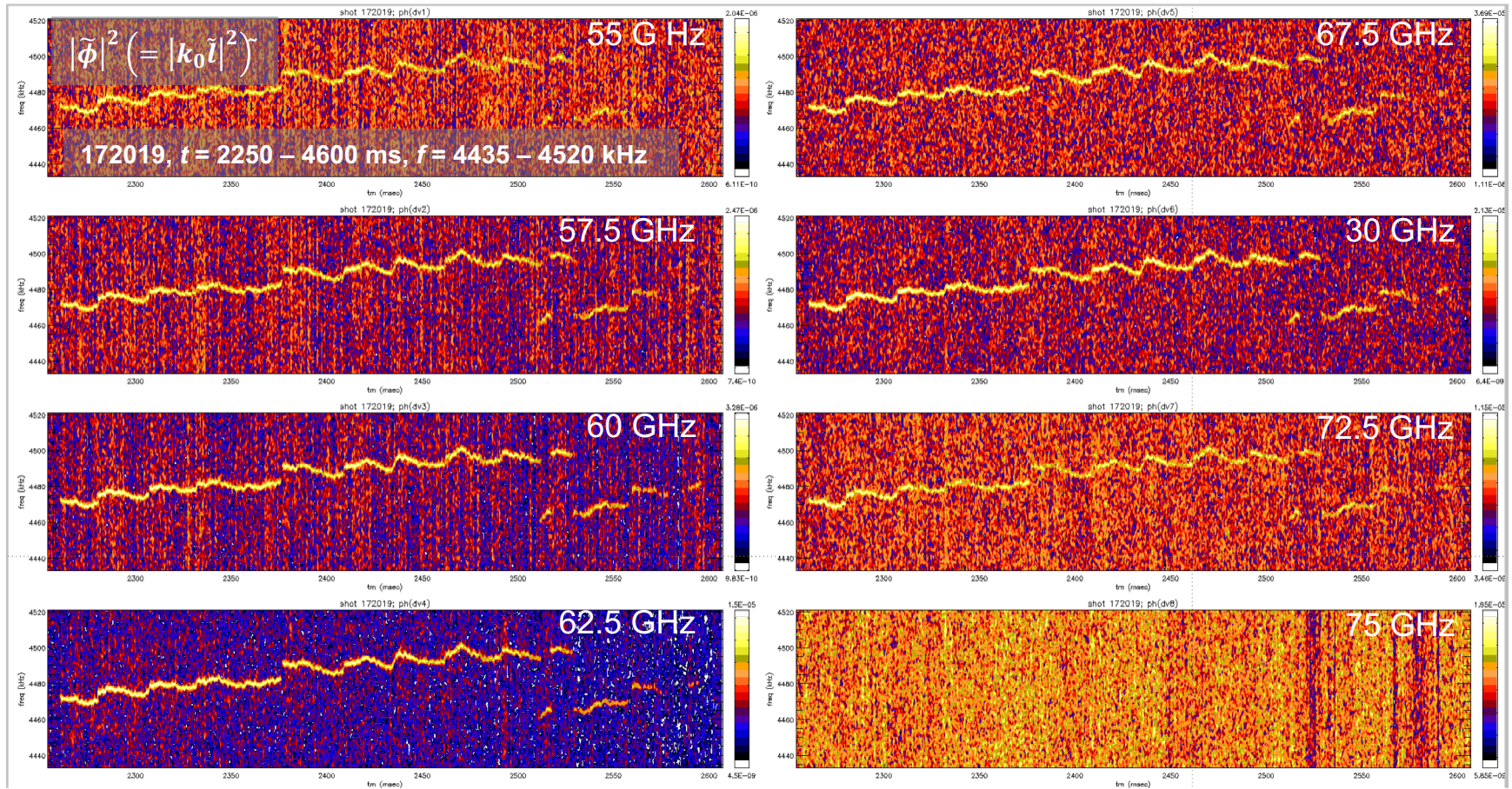
# Reflectometer array measures CAE $\tilde{n}$ across plasma



- 8 channels: 55 – 75 GHz
- X-mode or O-mode => reflection at  $f_{RH}$  or  $f_{pe}$
- global mode: path length fluctuations ( $\tilde{l}$ ) ~ from  $\tilde{n}$  @ cutoff

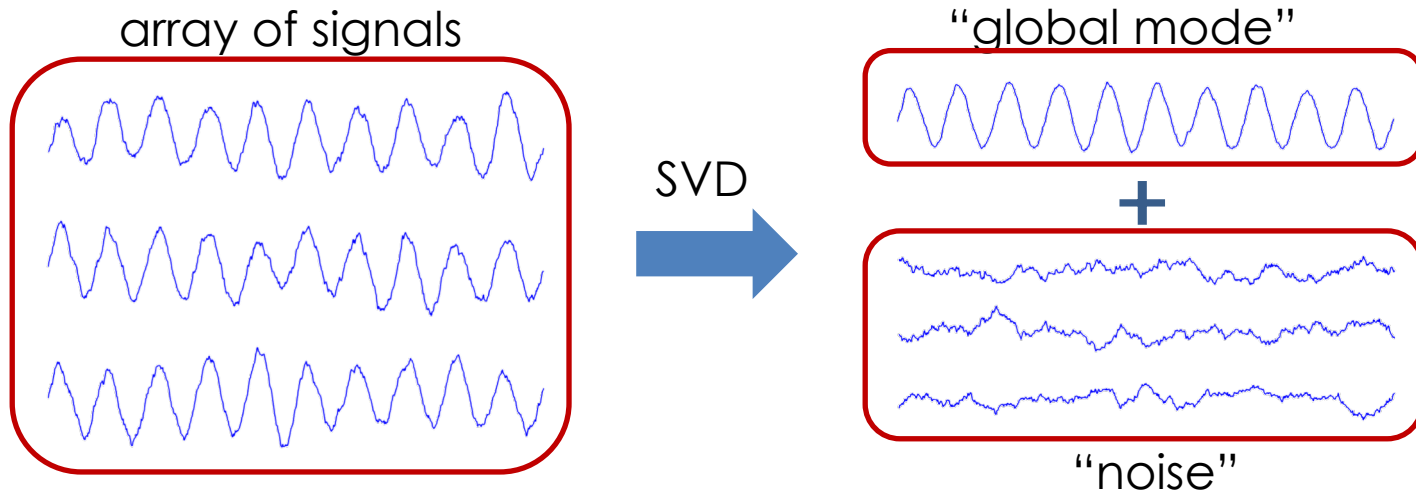


# Reflectometer array shows CAE structure is global



- Global CAE observed with reflectometers in  $I_B$  ramp at constant  $V_B$
- CAE aliased from  $f \sim 5.5$  MHz to  $\sim 4.5$  MHz (10 MHz sampling rate)

# Use singular value decomposition to isolate “global mode” from signal array



- array of signals contains global mode + noise/turbulence
- SVD separates signal matrix into global modes + noise/turbulence

$$\tilde{s}_{jk} = \tilde{s}_j(t_k) \rightarrow \sum_{m \in \text{modes}} \tilde{s}_{m0j} \tilde{s}_m(t_k) + \epsilon_j(t_k)$$

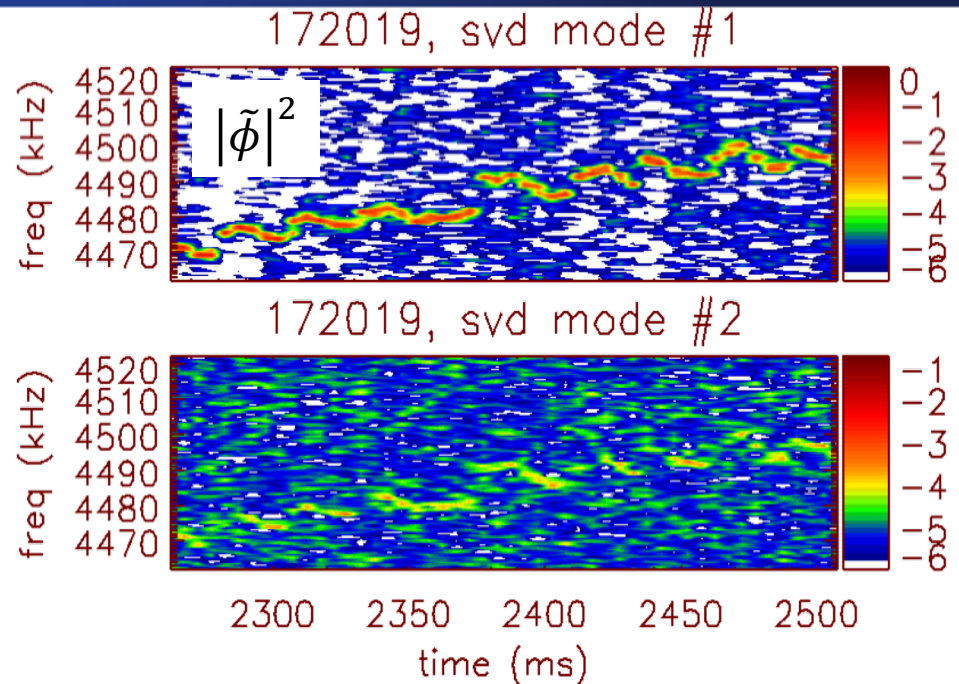
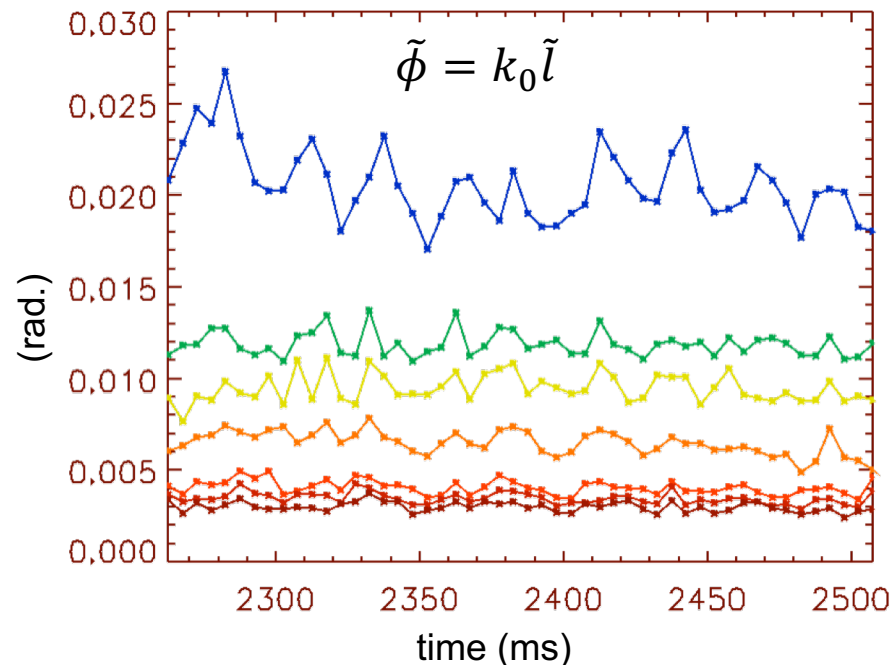
- Steps before SVD ...
  - bandpass filter signals to isolate mode
  - make signals complex  $\Rightarrow$  temporal phase factors out automatically:

- $\tilde{s}_j(t) = A(t) \cos(\theta(t) + \theta_{0j}) \rightarrow \hat{\tilde{s}}_j(t) = \frac{1}{\sqrt{2}} A(t) e^{i((\theta(t) + \theta_{0j}))} =$

$$\frac{1}{\sqrt{2}} \int_0^\infty d\omega e^{i\omega t} \int_{-\infty}^\infty dt' \tilde{s}(t') e^{-i\omega t'}$$

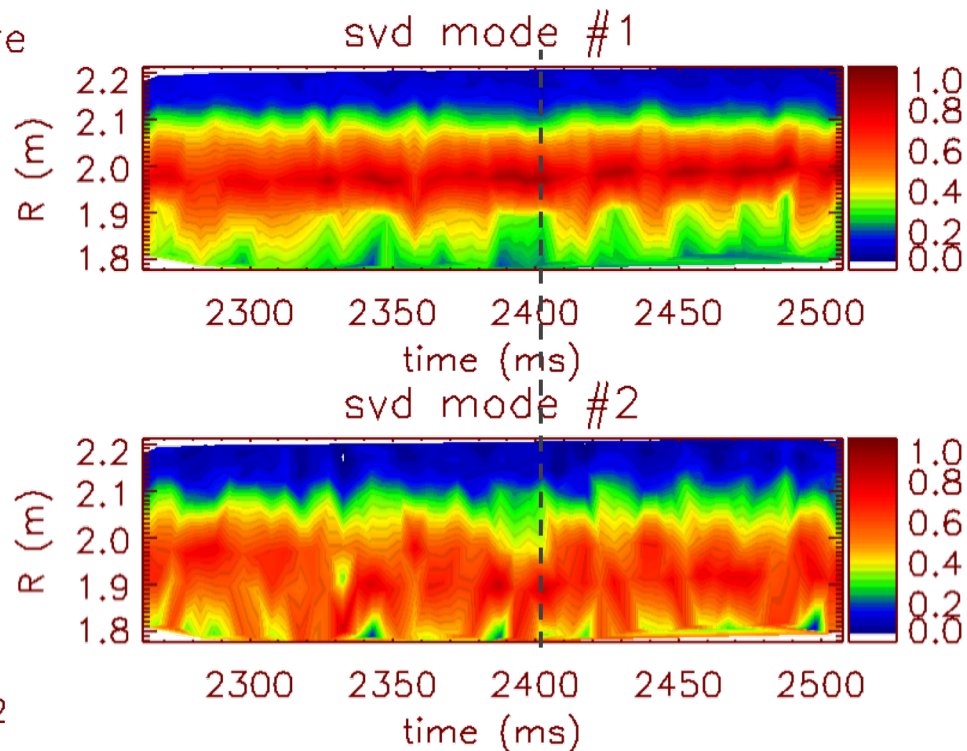
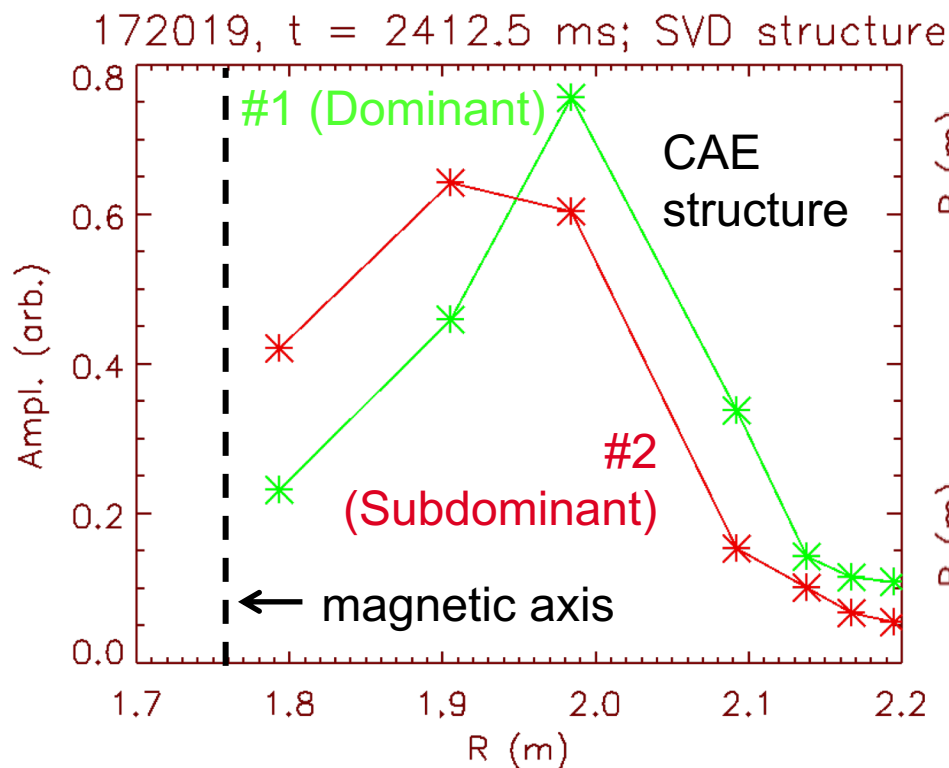


# SVD shows one dominant “mode”



- **SVD shows single dominant “mode” (~ 50 % fluctuation power)**
  - 5 ms records (no overlap), 60 kHz bandwidth
  - large amplitude subdominant mode (~ 25 % fluctuation power)  
@ ~ same frequency => Distinct modes **OR**
    - #1+#2 = single mode w/time-dependent structure (< ~5 ms modulation)?
    - #2 is SVD artifact?
- **Low amplitude components = noise/turbulence**

# Dominant SVD modes have global structure



- Modes have broad structure
- Modes peak at mid-radius ( $R \sim 2$  m)

# Conclusions

- **CAEs observed during beam current ramp at constant voltage**
- **Reflectometers observe global structure**
- **Modes peak at mid-radius ( $R \sim 2$  m)**
- **SVD analysis one dominant mode**
  - Subdominant mode @  $\sim$  same frequency  $\Rightarrow$  time-dependent CAE structure?

# Future Work

- Toroidal mode numbers from ICE toroidal loops
- Comparison with theory/simulation