MHD modeling of the Effect on n=2 RMP on Peeling-Ballooning mode in KSTAR

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Introduction

- Simulation setup - Numerical tools & Reference
- RMP driven Plasma response
 - Kink-tearing response
 - Increased pedestal transport
- RMP driven ELM crash suppression
 - Natural & RMP PBM simulation
 - Coupled RMP & PBM
 - PBM locking
- Conclusion



RMP driven ELM suppression

- **RMP driven ELM crash suppression**
 - ✓ Peeling-ballooning mode (PBM) [1,2] is the main instability resulting in large ELMs.
 - \checkmark Resonant MP (RMP) can suppress the ELM crash [3-5].
 - \checkmark Suppression has a very narrow operation window [6].

Mechanism is important for reliable ELM control

- **Increased pedestal transport by RMP application**
 - \checkmark RMP can increase the radial transport of the pedestal.
 - \checkmark It can degrade the pedestal gradient by forming the stochastic layer [7-9].







[7] R. Fitzpatrick et al., POP 5 (1998), 3325 [8] M. Heyn et al., NF 54 (2014), 064005 [9] N.M. Ferraro et al., POP 19 (2012), 056105

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RMP driven ELM suppression

• "Initial" understanding of RMP driven ELM suppression



Possible limits of 'initial' explanation

- Interesting features in RMP driven ELM crash suppression
 - ✓ PBM-like filaments remain during the suppression phase [1,2].
 - Mode structure is locked when suppression is achieved.
 - ✓ Experimental observation found the importance of $\omega_{\perp,E\times B} \approx 0$ [3].

Missing keys ?

Role of micro-instabilities Role of MHD characteristics

→ This study is focused on MHD behavior

> NL simulation including both RMP and PBM is conducted.



J. Lee et al., PRL 117 (2016), 075001
 J. Lee et al., NF 59 (2019), 066033
 C. Paz-Soldan et al., NF 59 (2019), 056012

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RMP simulation with equilibrium
- Equilibrium response

Image: Construction with PBM (w/o RMP) simulation with PBM exponse
- PBM response



Numerical tools

- JOREK (3D Nonlinear MHD simulation code) [1]
 - $\checkmark\,$ Toroidal X-point geometries with scrape-off layer is included.
 - ✓ 4-fields Reduced MHD equation [2] is used.

$$\begin{split} \frac{1}{R^2} \frac{\partial \psi}{\partial t} &= \eta(T) \nabla \cdot \left(\frac{1}{R^2} \nabla_\perp \psi\right) - \vec{B} \cdot \left(\nabla u - \tau_{\rm IC} \frac{\nabla p_{\rm e}}{\rho}\right) \quad \textit{Ohm's law} \\ \frac{\partial \rho}{\partial t} &= -\nabla \cdot (\rho \vec{v}) + \nabla \cdot (D \nabla \rho) + S_{\rho} \quad \textit{Continuity eqn.} \\ \rho \left(\frac{\partial}{\partial t} + \vec{v} \cdot \nabla\right) \left(\vec{v}_{\rm E} + \vec{v}_{||}\right) &= -\nabla (\rho T) + \vec{J} \times \vec{B} + S_{\rm v} - \vec{v} S_{\rho} + \mu \Delta \vec{v} - \nabla \cdot \vec{\Pi}_{\rm neo} \\ \frac{\partial (\rho T)}{\partial t} &= -\left(\vec{v}_{\rm E} + \vec{v}_{||}\right) \cdot \nabla \rho T - \gamma \rho T \nabla \cdot \left(\vec{v}_{\rm E} + \vec{v}_{||}\right) + \nabla \cdot (\kappa \nabla T) + (1 - \gamma) S_{\rm T} \end{split}$$



Fluid model is included w/ toroidal rotation

w/ diamagnetic effect w/ neoclassical viscosity

Ion Momentum eqn.

Energy eqn.



[JOREK grid for KSTAR]



[RMP on JOREK boundary for KSTAR, ERGOS]

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• ERGOS (Vacuum RMP field code) [3]

✓ Vacuum MP is calculated.

G. T. A Huysmans et al, PPCF 51 (2009), 124012
 F. Orain et al., POP 20 (2013), 102510
 M. Becoulet et al., Nucl. Fusion 48 (2008), 024003

Reference plasma

- Target discharge and equilibrium
 - ✓ ELM suppression discharge (#18594) [1] of KSTAR is selected
 - $\checkmark B_{\rm T} = 1.8 \text{ T}, I_{\rm p} = 660 \text{ kA}, q_0 \sim 1, q_{95} \sim 4, \beta_{\rm p} = 1.0 \text{ , } \overline{n}_{\rm e} = 3.3 \times 10^{19} \text{ m}^{-3}$
 - ✓ ELM suppression is achieved with n=2 (ϕ = 90°), $I_{\rm RMP}$ ~3.7kA RMP configuration [2].



Reference plasma - Profile & EFIT

- Kinetic profile and EFIT construction
 - \checkmark We developed GFIT & GEFIT package to construct a kinetic profile and EFIT in KSTAR.
 - ✓ Numerical/Theoretical corrections are applied to solve obstacles in theses constructions.
 - \checkmark They are in full operation at the KSTAR computing server (one of the standard tool).



[GFIT & GEFIT package, KSTAR]



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RMP driven Plasma response - Approach

- Numerical modeling of MP application
 - \checkmark Boundary condition is modified with vacuum RMP field ($\delta \psi_{\text{pol},\text{RMP}}$).

 $\psi_{\rm bdy} = \psi_{\rm bdy,0} + \delta \psi_{\rm bdy,RMP}$

- $\checkmark\,$ Vacuum field approximation is used on the boundary.
- ✓ Field penetration and the response (only n=0 & 2) are self-consistently calculated.
- Kink-tearing response is reproduced.



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Kink-tearing response - Kink

- Kink response
- Kink ↓ It has an edge localized structure. ✓ It has large deformation at X-point.
 - ✓ It results in a $v_{E \times B}$ convection layer on the pedestal.





Plasma response - Tearing

Tearing response

Tearing -

- ✓ Perturbed current shields the external field.
- $\checkmark v_{\perp e} \approx 0$ layer and finite resistivity in the edge weaken the field shielding.
 - \checkmark Field penetration occurs in the pedestal region.
 - ✓ As a result, stochastic layer is formed.



b)

0.8

0.6

0.4

0.2

0.2

 $\delta j_{\phi} (n = 2) [a.u.]$

0.8

0.6

0.4

a)

0.8

0.6

0.4

0.2

 ψ_N

 $\delta \psi_{pol} (n=2) [a.u.]$

Increased pedestal transport - Agreement

1.25

1.0

 $[n.75]{n.75}$ 0.75 0.5

0.25

- Pedestal profile degradation
 - $\checkmark\,$ Radial transport increases due to
 - $v_{\mathrm{E} imes \mathrm{B} \perp}$ convection (Kink).
 - Stochastic layer (Tearing).
 - ✓ Pedestal profile (n=0) is degraded.
 - \checkmark Density pedestal is governed by $v_{\rm E \times B, \perp}$.
 - ✓ It is consistent with the trend that density pump-out increases with kink response [1,2].
 - ✓ T pedestal shows a similar tendency in the experiment and simulation.
 - ✓ However, the decrease in \overline{n}_e from the experiment is three times larger than the simulation.



Increased pedestal transport - Disagreement

- Pedestal profile degradation
 - \checkmark Change in V_{ϕ} pedestal is also not consistent.
 - \checkmark This study does not include
 - Effect of micro-instability [1-4]
 - Magnetic flutter [5] and proper transport model [6]
 - Neoclassical Toroidal Viscosity (NTV) [7,8]
 - ✓ Γ_{E×B,MHD} can not solely explain the pump-out.
 → Role of NTV and micro instability is also important.
 - These transport mechanisms will be needed to fully explain the RMP driven profile degradation.



[1] T.M. Bird et al., NF 53 (2013), 013004[5]F.L. Waelbroeck et al., NF 52 (2012), 074004[2] I. Holod et al., NF 57 (2017), 016005[6] T. Rhee et al., NF 55 (2015), 032004[3] G.J. Choi and T.S. Hahm NF 58 (2018), 026001[7] W. Zhu et al., PRL 96 (2006), 225002[4] R. Hager et al., APS-DPP (2019), Florida, USA[8] J.-K. Park et al., POP 16 (2009), 056115



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RMP simulation with equilibrium - Equilibrium response Natural PBM (w/o RMP) simulation
RMP simulation with PBM
- PBM response

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Natural PBM simulation (without RMP)

- Linear PBM simulation
 - ✓ Linearly dominant n is $n_{\text{ECEI}} = 11 \pm 1$, $n_{\text{sim}} = 12$.
 - ✓ Poloidal velocity of mode is $v_{\theta,mode}$ ~3 km/s in both cases (ECEI & simulation).

 $\checkmark v_{\theta,\text{mode}} \approx v_{\theta,\text{E}\times\text{B}}$ (LAB, ion - diamagnetic direction) [1,2].

- Nonlinear PBM calculation
 - ✓ Mode crash is reproduced during nonlinear phase.
 - $\checkmark\,$ Large heat flux occurs with pedestal collapse.
 - $\checkmark \Delta W_{\rm ELM,sim} \approx 8 {\rm kJ} \, (\Delta W_{\rm ELM,exp} \approx 7 \pm 4 {\rm kJ}).$
 - Experimentally relevant ELM with $v_{\theta,mode} \approx v_{\theta,E \times B}$ is obtained.



- Effect of RMP on PBM
 - ✓ PBMs are affected by RMP driven plasma response via mode coupling.
 - ✓ Mode mitigation occurs with small $I_{\rm RMP}$ (≤ 2kA).
 - ✓ Mode crash suppression is achieved with $I_{\rm RMP}$ ~ 4 kA (~3.7 kA in exp.).
 - ✓ PBM suppression is reproduced with experimentally relevant RMP.





[Nonlinear evolution of MHD modes with RMPs]

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Coupled RMP & PBM

- Comparison between w/ and w/o mode coupling case
- ✓ Degraded pedestal due to RMP ($I_{RMP} = 4kA$) is included in both cases.
- Nonlinear PBM simulation w/o mode couplings shows
 A bursty behavior in its nonlinear phase
- ✓ Nonlinear PBM simulation w/ mode couplings shows
 - Mode suppression without bursty behavior
- $\checkmark\,$ Therefore, suppression of PBM with RMP is related to both
 - Reduced pressure gradient
 - Coupling of PBMs and RMP driven plasma response



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Coupled RMP & PBM



- ✓ Tearing component decrease with the mode coupling effect for $I_{\rm RMP} \le 2$ kA.
- \checkmark Magnetic island is amplified under the coupling effect when suppression is achieved.

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- ✓ Effect of mode coupling on the perpendicular flow is small.
- $\checkmark\,$ Pedestal transport is increased by the coupling effect.
 - Larger stochastic layer and pedestal transport
 - Smaller pedestal gradient (Reduced instability source)

Coupled RMP & PBM

Increased energy transfer with coupled RMP-PBM



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✓ Interaction between harmonics increases [1] with RMP.

- Amplified energy transfer between harmonics
- ✓ Vorticity U_{00} in the pedestal is reduced.
 - More evenly distributed perturbed energy among harmonics [2]

✓ Catastrophic growth of unstable mode can be prevented [3].

M. Becoulet et al., PRL 113 (2014), 115001
 H. Jhang et al., NF 57 (2017), 022006
 P.W. Xi et al., PRL 112 (2014), 085001

Coupled RMP & PBM - Suggestion

• Effect of coupled RMP-PBM



PBM locking

- Locking of mode structure
 - ✓ PBM is locked ($v_{\theta,\text{PBM}} \rightarrow 0$) when suppression is achieved (I_{RMP} ~4 kA).
 - \checkmark Similar trend is observed in the previous experiment [1, 2].
 - ✓ Mode locking (bifurcation) is one of the major differences between mitigation and suppression.
 - ✓ When mode locking occurs, $v_{\theta, \text{PBM}}$ and $v_{\theta, \text{E} \times \text{B}}$ are decoupled.

→ $v_{\theta,\text{PBM}}$: -3 → 0 km/s while $v_{\theta,\text{E}\times\text{B}}$: -3 → -8 km/s

 $\therefore v_{\theta,\text{PBM},\text{RMP}} = v_{\theta,\text{PBM},\text{woRMP}} + \Delta v_{\theta,\text{RMP}}$



[$v_{ heta, \text{PBM}}$ in ELMy and Suppressed case]



PBM locking - Role on the mode coupling

- PBM locking and mode coupling
 - Constant or sustained phase difference ($\Delta\delta$) b/w RMP and PBMs is favorable to strong mode interaction.
 - \rightarrow Keeping the spatial overlapping of mode structures
 - ✓ RMP driven plasma response is static in space. → $v_{\theta,PBM} \approx 0$ for $\Delta \delta \approx \text{const.}$
 - ✓ PBM locking may be difficult to occurs with large $v_{\theta,E\times B}$ in pedestal.

 $v_{\theta,\text{PBM},\text{RMP}} \approx v_{\theta,\text{E} \times \text{B}} + \Delta v_{\theta,\text{RMP}} \rightarrow 0$

- ✓ PBM locking and suppression are not achieved with increase $|v_{\theta,E\times B}|$.
 - → Advantageous small $v_{\theta,PBM}$ (or $v_{\theta,E\times B} \rightarrow 0$)
 - PBM locking can be an advantageous consequence or reason for one branch of ELM suppression





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Conclusion - I

- Nonlinear effect of RMP on the pedestal has been investigated.
- Kink-tearing response is observed under RMP
 - ✓ Axisymmetric equilibrium change accompanied by Kink + Tearing non-axisymmetric features.
 - ✓ Mean (n = 0) pedestal profile degradation (Kink + Tearing)
 - *T* pedestal: Stochastic layer (Tearing part)
 - $n_{\rm e}$ pedestal: $\Gamma_{\rm E \times B}$ Convective flux (Kink part)
- Additional transport mechanism is needed to fully explain the pedestal degradation by RMP.

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✓ NTV & Micro instabilities will play important role.

Conclusion - II

- Degradation of pedestal gradient may not solely explain ELM suppression.
- ELM is nonlinearly suppressed by RMP.
 - $\checkmark\,$ ELM suppression accompanied by
 - Reduced pedestal pressure gradient.
 - Mode coupling b/w PBMs and n = 2 RMP driven modes.
- Mode coupling b/w ELMs and n = 2 RMP driven modes is important.
 - Increased pedestal transport by enlarging the magnetic island
 - Prevented mode crash by increasing energy transfer b/w harmonics
- Coupling between RMP and ELMs may explain the locked filament structure during the suppression phase in Exp.



PBM locking is distinguished feature of ELM suppression.

- ✓ Good agreement with experimental observation via ECEI
- ✓ Strengthened mode coupling b/w RMP and PBM
- Favorable conditions for the mode coupling are
 - $\checkmark\,$ Plasma conditions for the PBM locking.
 - Small $v_{\theta, PBM} \rightarrow 0$ is advantageous.
 - v_{θ,E×B} ≤ v_{θ,PBM} ≤ v_{θ,E×B} + v_{θ,i*}/2 at linear phase w/o RMP.
 (Depends on the collisionality and dominant n)
- It may be correlated with the importance of $v_{\theta,E\times B} \approx 0$ in ELM suppression.



Collaboration with PPPL

- Integrated simulation with JOREK and PENTRC
 - \checkmark Include NTV in the simulation for the particle and momentum transport.
 - $\checkmark\,$ PENTRC is connected to JOREK for the NTV calculation.
 - ✓ Work is on progress.



Thank You





Backup - RMP driven ELM suppression

- Bifurcation of poloidal mode rotation
 - ✓ Sudden bifurcation of rotation occurs at the suppression phase.
 - \checkmark The mode rotation becomes very small ($v_{ heta,mode} pprox 0$).
 - It suggests the possibility of interactions b/w RMP and PBM.
- Direct effect of RMP on PBMs
 - ✓ RMP can directly affect ELM "crash" suppression.
 - ✓ Effect of RMP on the PBMs are..
 - Linear effect of RMP induced field structure on PBM [1, 2].
 - Nonlinear MHD simulations on the RMP driven KPM [3] and ELM mitigated/suppressed case [4,5].



- Linear effect of 3D field on PBM
- Nonlinear coupling b/w RMP and PBM

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• NL simulation including both RMP and PBM is needed.

Backup - Limitation of KSTAR EFIT

Limitation of KSTAR EFIT

- \checkmark There is no standard of "good" EFIT in KSTAR.
- ✓ There are many obstacles to construct a "good" kinetic profile and EFIT.



Backup - Numerical/Theoretical compensation

- Kinetic profile correction
 - ✓ Multi diagnostic based least square fitting
 - Thomson, ECE, Inter/Reflectometry and CES
 - ✓ Various numerical filters & function based fitting
 - ✓ Theoretical model based pedestal profile
 - ELM toroidal n (n_{ECE}) and ELM size (ΔW_{ELM})
- Current profile correction
 - ✓ Theoretical model based current profile
 - Synthetic MSE vs Experimental MSE
 - Edge bootstrap current
- KSTAR parameter optimization
 - \checkmark Optimization through brutal force approach



Marginal

Backup – reference EFIT

- Kinetic profile and EFIT construction
 - ✓ GFIT & GEFIT package is developed to construct a kinetic profile and EFIT in KSTAR.
 - ✓ They are in full production at the KSTAR computing server (one of standard branch).



Numerical accuracy	Convergence: $10^{-4} \rightarrow 10^{-11}$
Experimentally relevant	Error: $N/A \rightarrow 14.5$

"Good" reference isdeveloped for the simulation.

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Backup - RMP driven ELM crash suppression

- RMP and divertor heat flux
 - \checkmark Instantaneous ELMy peak heat flux (Q_{peak}) decreases with RMP.
 - $\checkmark Q_{peak}$ is drastically reduced for $I_{RMP} \ge 3$ kA where modes are suppressed.
 - \checkmark Background heat flux increases with $I_{\rm RMP}$ due to the enhanced transport to SOL.



- PBM suppression is reproduced with experimentally relavent RMP configuration
- Suppression of PBM with RMP can be related to
 - Reduced pressure gradient



[ELMy peak divertor heat flux induced by PBMs]

Backup - Simulation setup

- Target discharge and equilibrium
 - ✓ #18594 is selected for the simulation.
 - $\checkmark B_{\rm T} = 1.8 \,{\rm T}, I_{\rm p} = 660 \,{\rm kA}, q_0 \sim 1, q_{95} \sim 4, \beta_{\rm p} = 1.0 , \overline{n}_{\rm e} = 3.3 \times 10^{19} \,{\rm m}^{-3}$
 - ✓ ELMs are suppressed with n=2 (ϕ = 90°), $I_{\rm p}$ ~3.7 kA RMP configuration [1].
 - ✓ Modified Sauter formula [2] is applied to construct the bootstrap current.

Numerical setup

- ✓ Neoclassical constraint ($v_{\rm neo}$) is applied to construct the ion-poloidal flow.
- $\checkmark v_{\theta,E\times B}$ in the pedestal region is in the <u>ion-diamagnetic</u> direction.
- $\checkmark T_i = T_e$ is assumed.
- Adaptive diffusive profile and source are used to sustain the ho, T, $v_{
 m \varphi}$ profiles.
- ✓ Spitzer-like resistivity (x40) and braginskii parallel conductivity are used.



Y. M. Jeon et al., PRL 109 (2012), 035004
 R. Hager and C. S. Chang et al., Phys. Plasmas 23 (2016), 042503