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Coupled Tearing and Internal Kink Modes and Their Effect on Fast Ion Transport in NSTX

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NSTX-U / Magnetic Fusion Science meeting, Princeton, NJ (Apr. 27, 2020)

Motivation

- Low frequency modes affect tokamak operation
 - Confinement degradation [1-11], rotation slowing down [11-13], impurity transport [14]
 - Flux pumping [15]
- Fast ion interaction with kink mode is well known [10-13,16-23]
- Fast ion interaction with tearing mode is more theoretical than conclusive [25-45]
- Most works concern large aspect ratio [All but 10-13,22,23[†]]
- This paper studies coupled tearing and internal kink modes [11,28,32,46] and its effect on fast ions in NSTX

[†] On internal kink mode

Outline

- Low frequency modes appear to degrade confinement
- Synthetic soft X-ray measurement and “kick” model are implemented
- Fast ion transport by tearing and internal kink modes is modeled successfully
- Relative phase of the modes plays major role
- First principle modeling of multiple modes is needed for further analysis

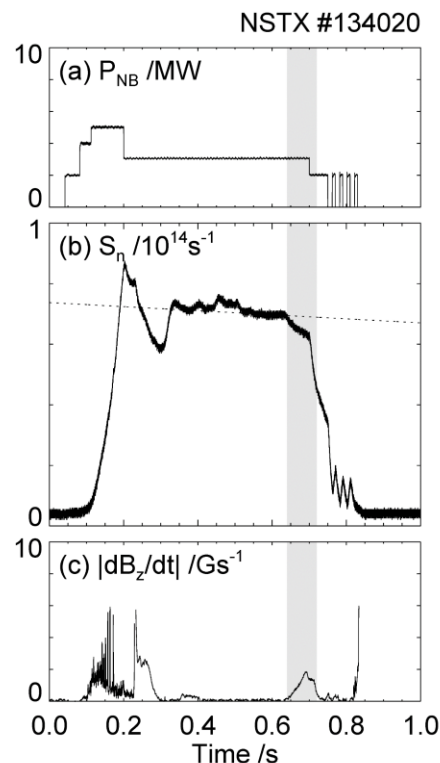
Low frequency modes affect confinement

- Instability

- Onset at peak β_N while $q_{\min} < 2$
- Neutron rate drops 20%
 - Implies loss of fast ions
- Mitigated by P_{NB} step down

- Other parameters

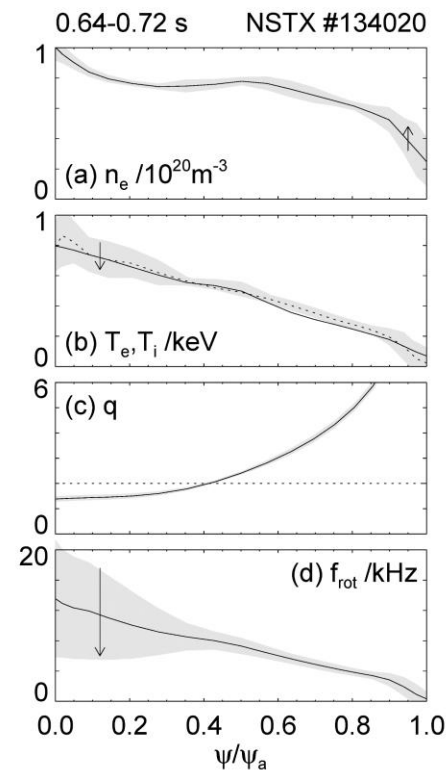
- No ELMs or AEs
- No mode locking (EF correction)
- Li conditioned for reproducibility



Low frequency modes affect core rotation

- Profiles

- Unchanged q and density profile
- Small drop in temperatures [49]
- Large rotation slowing down at core ($q < 2$) [50]

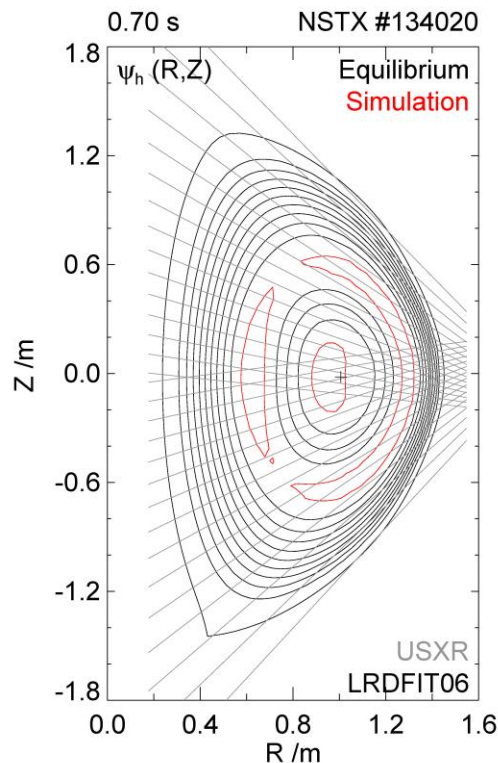


Modes are identified as tearing & internal kink

- Synthetic SXR diagnostics[†]
 - Sampled at 5 MHz [52]
 - Simulated perturbations are fit to measured emissivity[‡]
 - Best fit with 2/1 tearing mode and core $n = 1$ kink mode
 - Best fit with modes coupled in phase

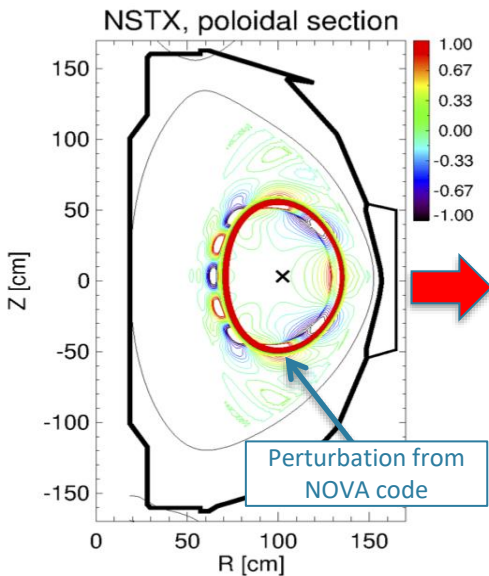
[†] See Appendix: Automation of [51]

[‡] Equilibrium from LRDFIT (MSE constrained) [23,53]

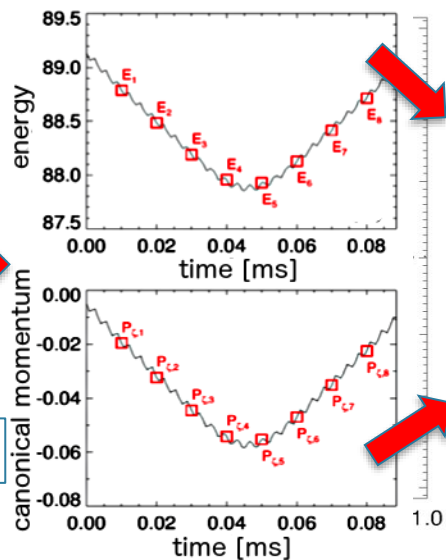


Kick model: particle-following ORBIT code used to infer transport matrix numerically

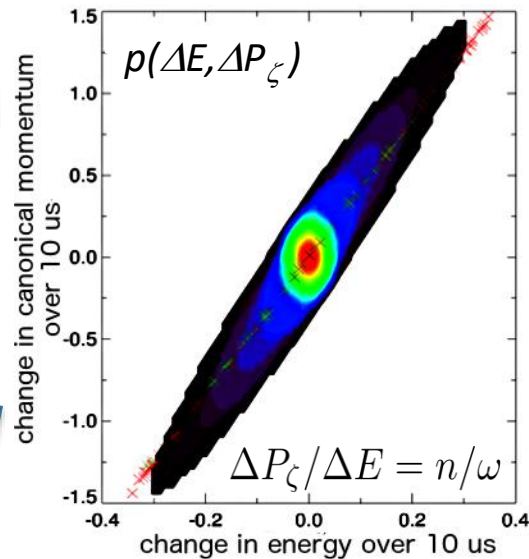
Initialize test particles uniformly in phase space



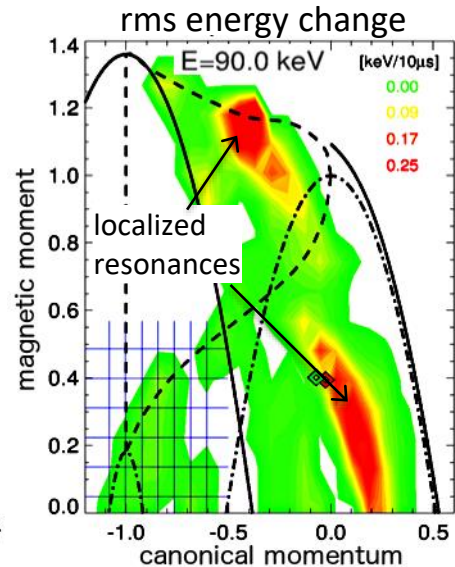
Track energy, momentum variations (*kicks*) at fixed time intervals



Combine ΔE , ΔP_ζ from same (E, P_ζ, μ) phase space bin into $p(\Delta E, \Delta P_\zeta)$



Repeat for all (E, P_ζ, μ) bins to infer 5D matrix \rightarrow input for NUBEAM: $p(\Delta E, \Delta P_\zeta | E, P_\zeta, \mu)$

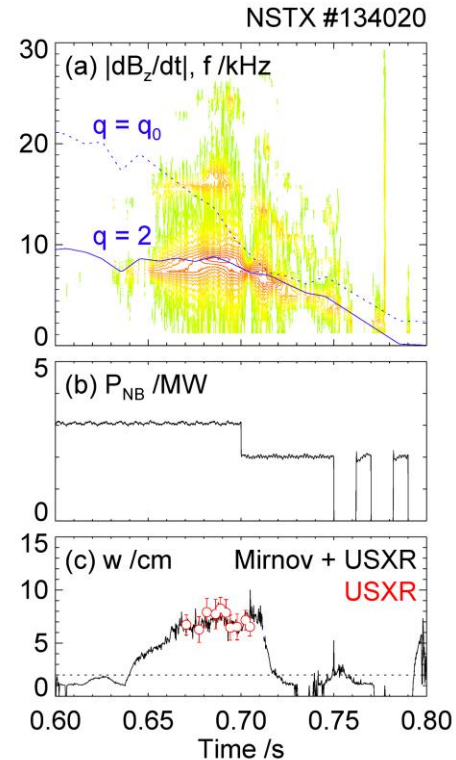


Podestà PPCF 2017



Fast ion confinement is modeled by “Kick” model

- “Kick” model [54]
 - Mode structure and amplitude
 - Experimental input
 - Mirnov coil signals scaled with synthetic SXR fits
 - ORBIT computes fast ion transport probability [55]
 - Input to NUBEAM / TRANSP [56,57]

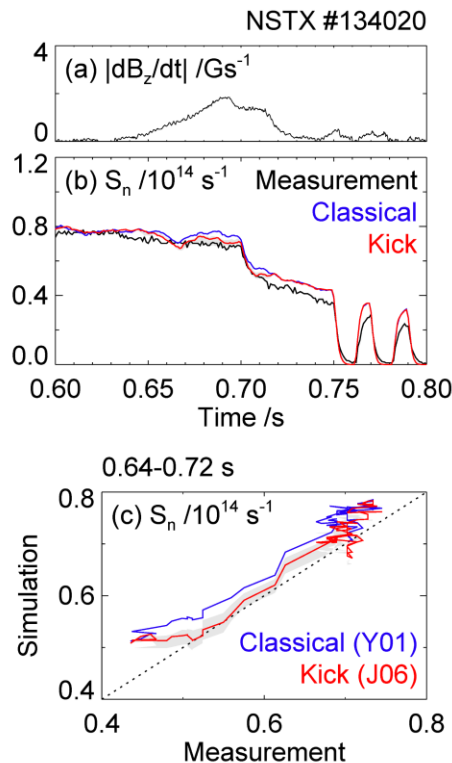


Simulation improved with inclusion of “Kick”

- Neutron rates

- Fast ions create neutrons
- NUBEAM computes fast ion dynamics from classical factors[†]
- Kick model adds the effect of instabilities
- Measured neutron rate [59] recovered by simulation with instabilities

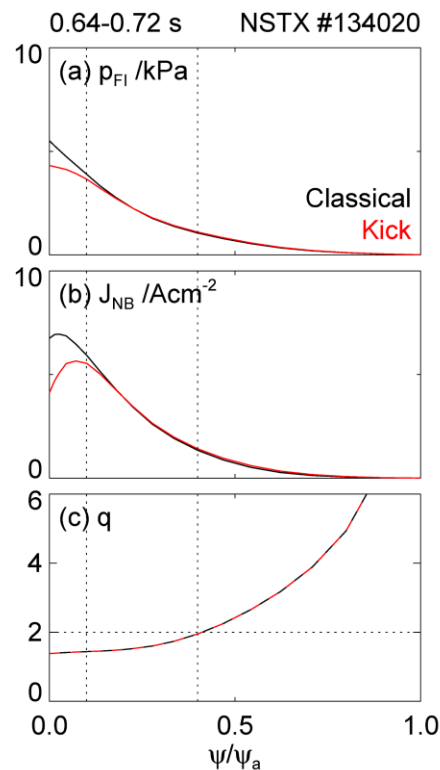
[†] Atomic physics, Coulomb collision and finite orbit effects, but not instabilities [58]



Transport is localized near resonance island

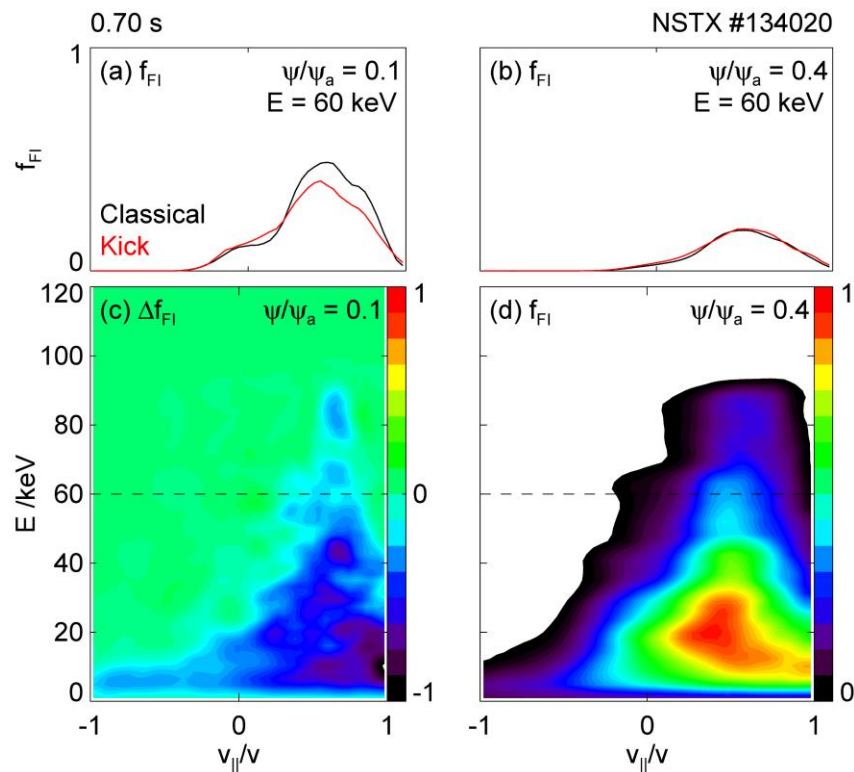
- Fast ion profiles

- Fast ion pressure drops with kick
- Neutral beam driven current drive drops with kick
- Region of drop is near core
- More interaction with resonant than tearing mode islands



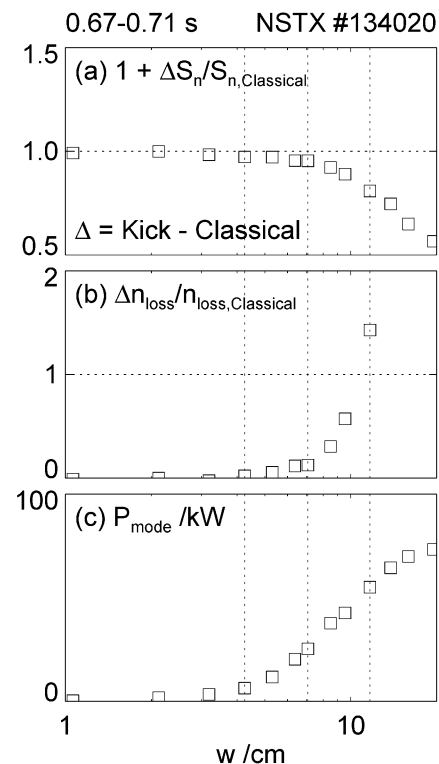
Depletion is core-localized in fast ion distribution

- Fast ion distribution
 - Extends to 90 keV (E_{inj})
 - Near core, kick depletes fast ions
 - Distribution near $q = 2$ surface is practically unchanged
 - As a result, weighted integrals of distribution drop primarily near core [24]



Transport surges at over-threshold island width

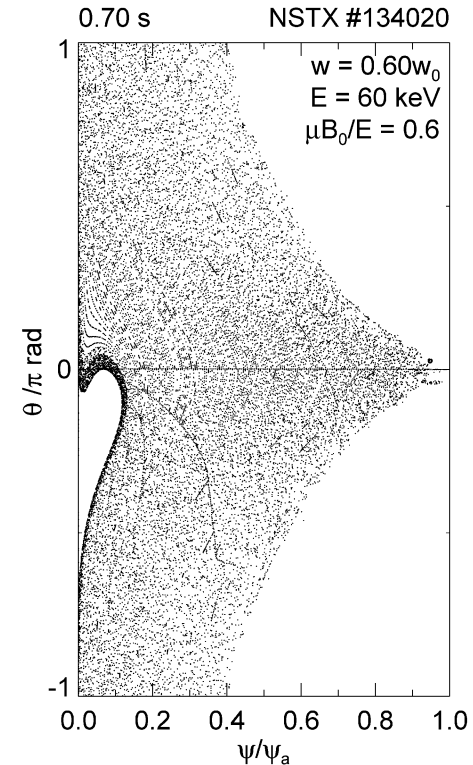
- Island width scan
 - Experimental values:
 - Island width 7 ± 1 cm
 - Kink displacement 5 ± 2 cm
 - Scanned proportionally
 - Threshold island width exists for neutron rates and losses [31]



Islands $>$ threshold turn flux surfaces chaotic (1/2)

- Poincaré plots

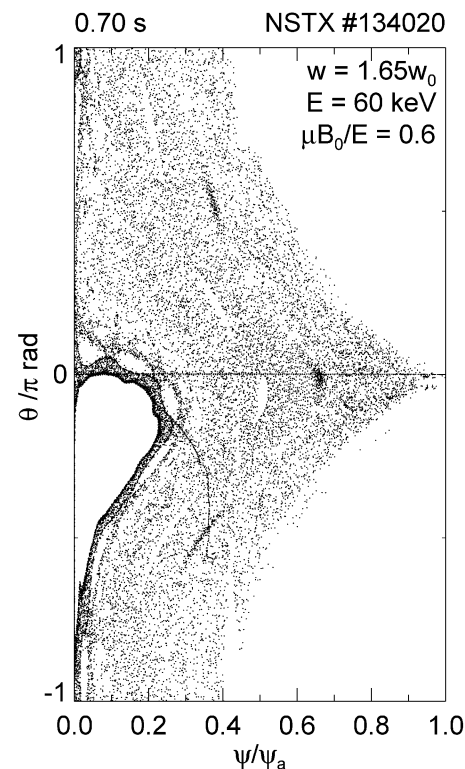
- Fast ion trajectory after round trip
- Flux surfaces are layered for islands $<$ threshold
- Flux surfaces become chaotic for islands $>$ threshold [47,48]



Islands $>$ threshold turn flux surfaces chaotic (2/2)

- Poincaré plots

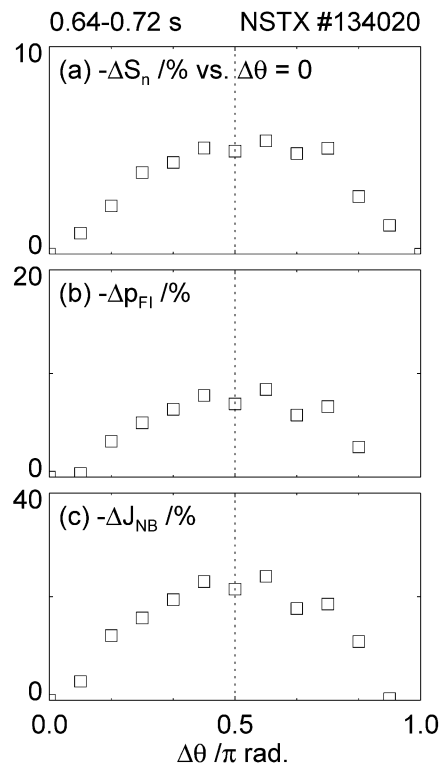
- Fast ion trajectory after round trip
- Flux surfaces are layered for islands $<$ threshold
- Flux surfaces become chaotic for islands $>$ threshold [47,48]



Transport is sensitive to relative phase of modes

- Relative phase scan
 - Experimental relation
 - In phase[†]
 - Scanned for period
 - More fast ion transport than measurement when out of phase

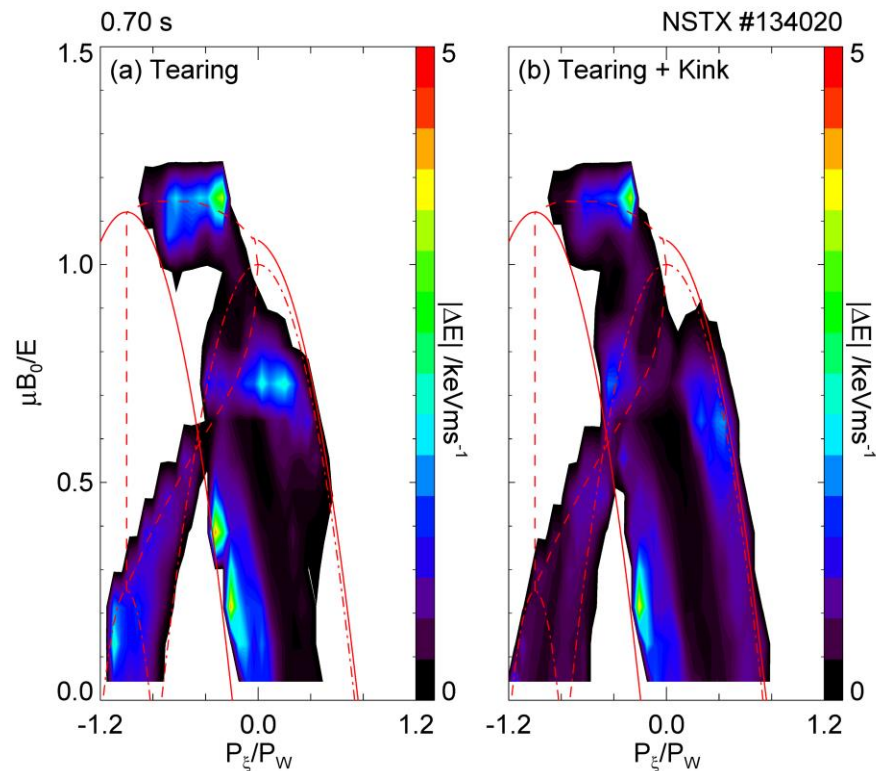
† Fixed relative phase: Islands aligned at midplane when core displaced to high field side [46]



Fast ion distribution impacts mode coupling (1/2)

- Mode coupling

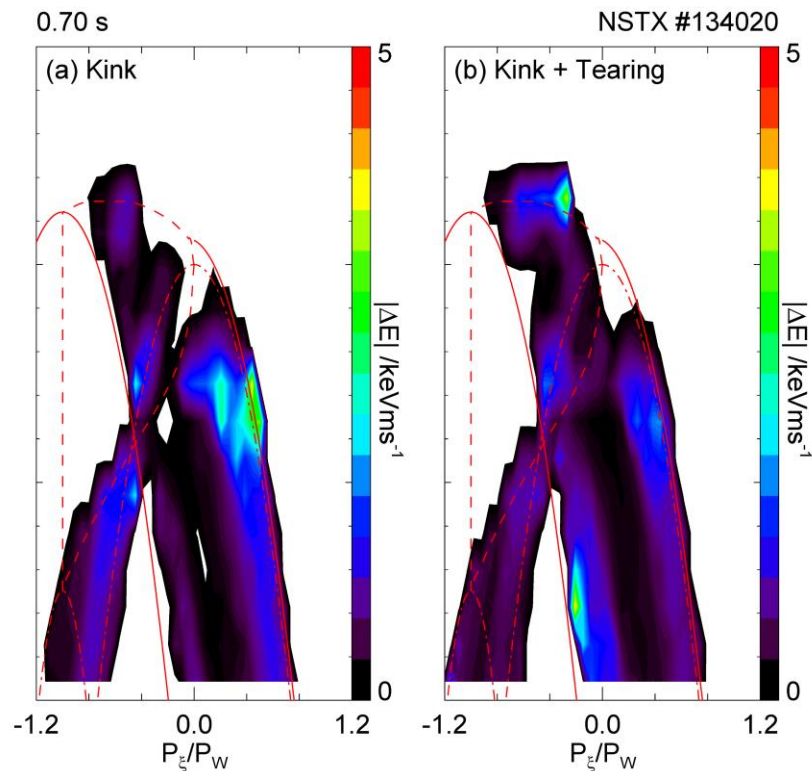
- Kick probability from tearing mode changes when internal kink mode is added [32]
- Same for internal kink mode [32]
- Fast ion impacts mode coupling, but how significant is this?



Fast ion distribution impacts mode coupling (2/2)

- Mode coupling

- Kick probability from tearing mode changes when internal kink mode is added [32]
- Same for internal kink mode [32]
- Fast ion impacts mode coupling, but how significant is this?



Conclusion

- Coupled tearing/internal kink modes is observed experimentally
- Fast ion transport by coupled modes is successfully interpreted by “kick” model
- Relative phase of modes plays major role in fast ion transport
- First principle modeling of multiple modes is needed for further analysis

Reference (inclusive)

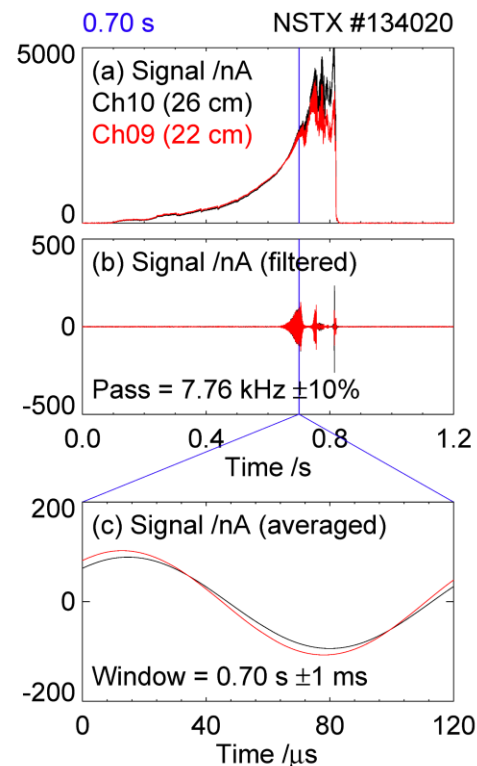
- 1) Heidbrink NF 34 535
- 2) Carolipio NF 42 853
- 3) Zweben NF 39 1097
- 4) Garcia-Munoz NF 47 L10
- 5) Gobbin NF 49 095021
- 6) Gunter PPCF 41 767
- 7) Chang NF 30 219
- 8) Poli PoP 15 032501
- 9) Zhang NF 55 113024
- 10) Cecconello PPCF 57 014006
- 11) Menard NF 45 539
- 12) Chapman NF 50 045007
- 13) Heidbrink NF 56 056006
- 14) Delgado-Aparicio NF 53 043019
- 15) Jardin PRL 115 215001
- 16) Chen PRL 52 1122
- 17) White PoF 28 278
- 18) Coppi PoFB 2 927
- 19) Porcelli PPCF 33 1601
- 20) Porcelli PPCF 38 2163
- 21) Borba NF 40 775
- 22) Pfefferle NF 54 012001
- 23) Menard PRL 97 095002
- 24) Heidbrink NF 58 082027
- 25) Forest PRL 79 427
- 26) Gude NF 39 127
- 27) Sesnic PoP 7 935
- 28) Frederickson PoP 9 548
- 29) Li PPCF 58 045012
- 30) Anderson PoP 20 056102
- 31) Bardoczi PPCF 61 055012
- 32) Liu NF in press (2020)
- 33) Konovalov SJPP 14 461
- 34) Mynick PoFB 5 2460
- 35) Mynick PRL 43 1506
- 36) Marchenko PoP 8 4834
- 37) Hegna PRL 63 2056
- 38) Cai PRL 106 076002
- 39) Cai PoP 19 072506
- 40) Cai NF 56 126016
- 41) Pritchard PoP 4 162
- 42) Brennan NF 52 033004
- 43) Halfmoon PoP 24 062501
- 44) Somlyakov PoP 2 1581
- 45) Wilson PoP 3 248
- 46) Bando PPCF 61 115014
- 47) White CNSNS 17 2200
- 48) Chirikov JNEC 1 253
- 49) LeBlanc, RSI 79 10E737
- 50) Bell, PoP 17 082507
- 51) Fredrickson RSI 1797
- 52) Stutman RSI 74 1982
- 53) Levinton, RSI 79 10F522
- 54) Podesta PPCF 56 055063
- 55) White PoF 27 2455
- 56) Pankin CPC 159 157
- 57) Hawryluk PoPTC 1 19
- 58) Goldston JCP 43 61
- 59) Roquemore, SOFE SP1-39

Appendix: Synthetic SXR diagnostics code

- **GAUNTLET: Automated FALCON**
 - Measured signals are periodically averaged
 - Low frequency modes are modeled analytically
 - Emissivity profile relates perturbation to signal
 - Fit is more sensitive to resolution than to noise
 - Fit is not sensitive to initial guess

Measured signals are periodically averaged

- USXR signal processing
 - Calibrated signals are taken
 - Filtered around mode frequency
 - Averaged each periods within fixed time window (± 1 ms)
 - Amplitude and phase extracted



Low frequency modes are modeled analytically

- Eigenfunctions for low frequency instabilities

- Tearing mode uses scaling law

$$w^2 = (16r_s/sB_\theta)\psi$$

to get helical flux

$$\psi_h = \left(\frac{B_0}{R_0}\right) \int_0^r \left(\frac{1}{q} - \frac{n}{m}\right) r dr + \psi \cos \zeta$$

where $\zeta = m\theta - n\phi + \int_0^t \omega dt$

- Kink mode uses analytic formula

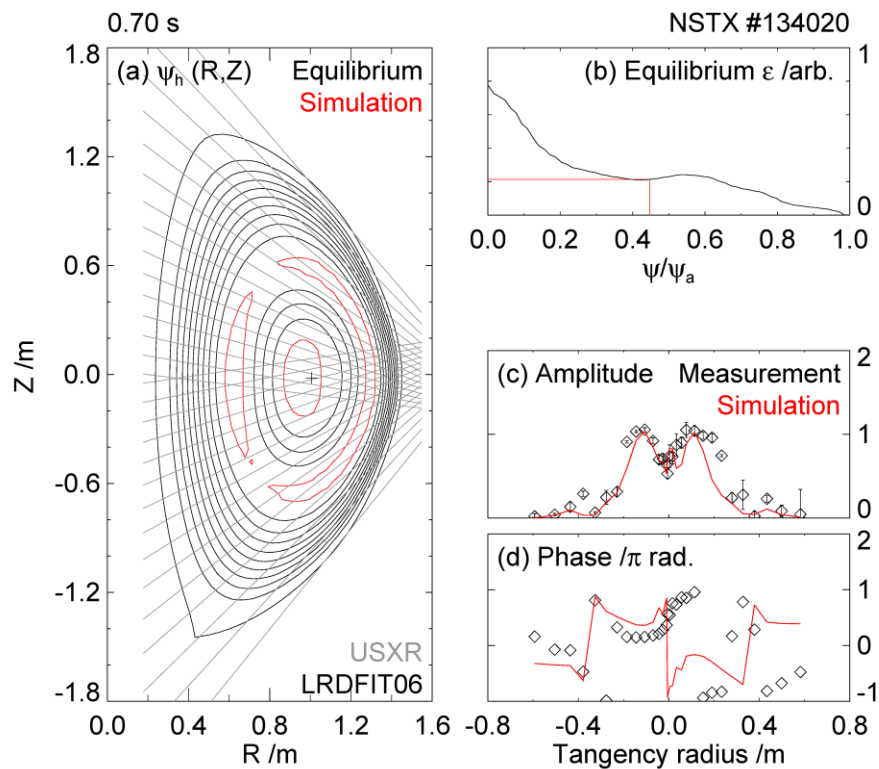
$$\xi = \delta/[1 + (a/r_k)^k]$$

to get flux displacement

- Flux translated with reconstructed equilibrium emissivity profile

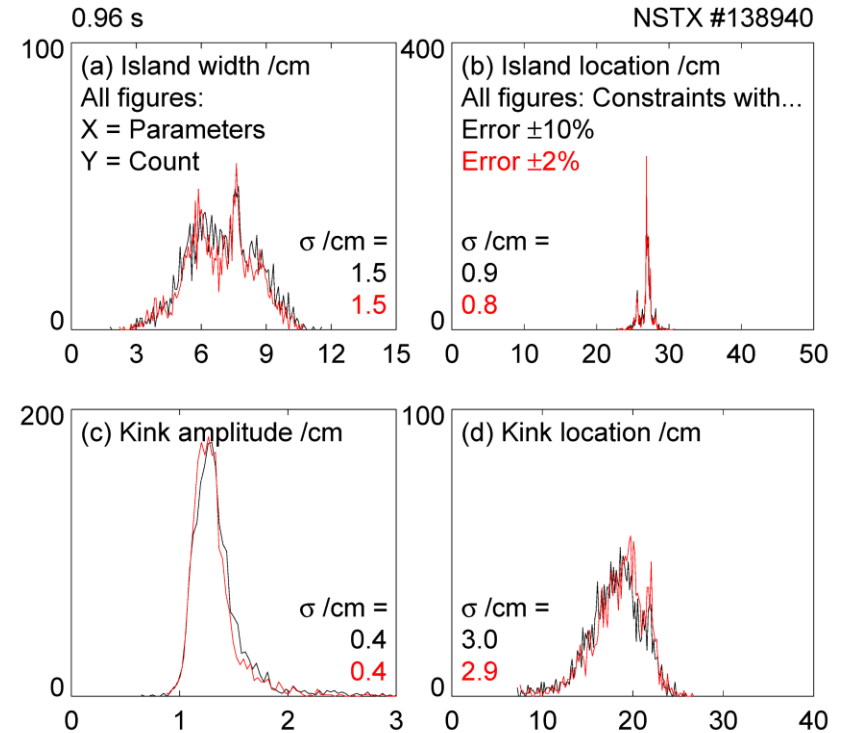
Emissivity profile relates perturbation to signal

- Soft X-ray tomography
 - Performed to the *equilibrium* emissivity
 - Provides relation of magnetic flux to emissivity
 - Analytic perturbed flux is converted to perturbed emissivity
 - Line-integrated to simulate signal and fit to the measurement



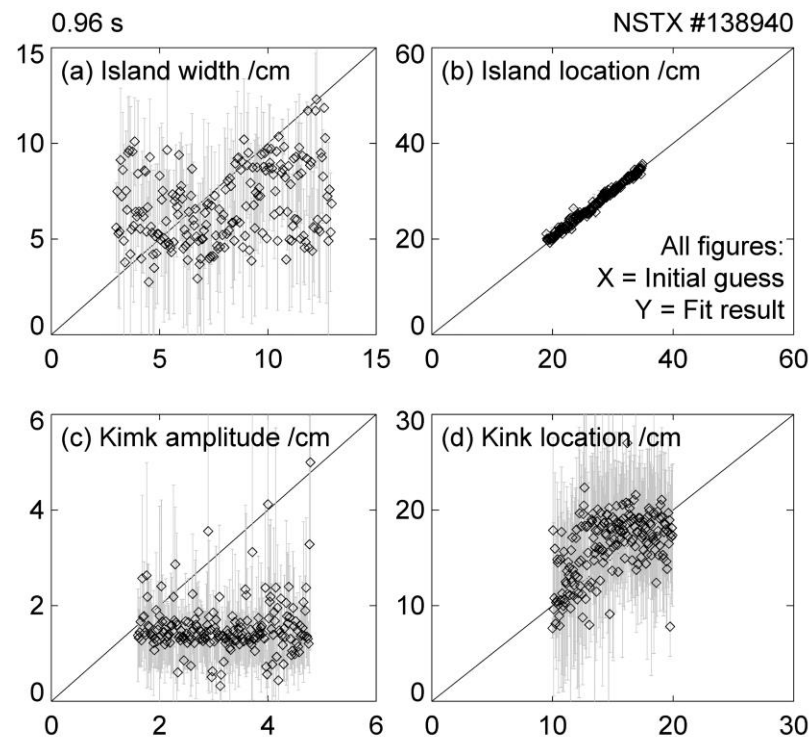
Fit is more sensitive to resolution than to noise

- Fit sensitivity to signal error
 - Nominal signal error is 2%
 - Fit uncertainty is small up to signal error of 10%;
Island width uncertainty < spatial resolution
 - Similar fit uncertainty for increasing signal error implies that fit algorithm is robust



Fit is not sensitive to initial guess

- Fit sensitivity to initial guess
 - Fit needs initial guess
 - Box scatter means fit result is independent of initial guess within error bars
 - Most can use any initial guess
 - Island location initial guess is provided from Mirnov coil, EFIT and CHERS



Backup

- Original figures
- Backup slides

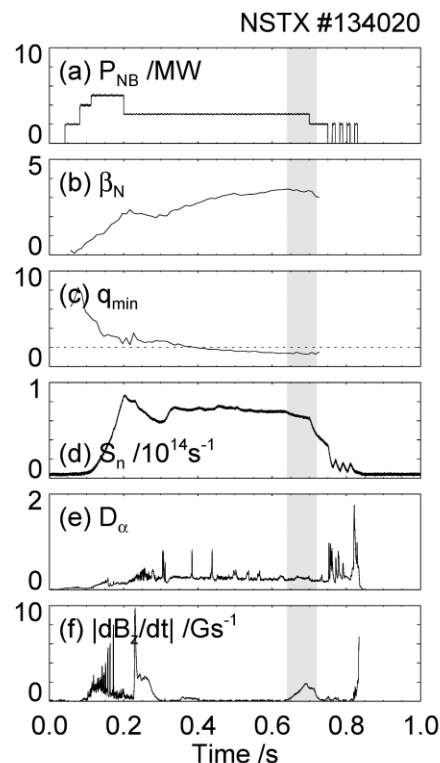
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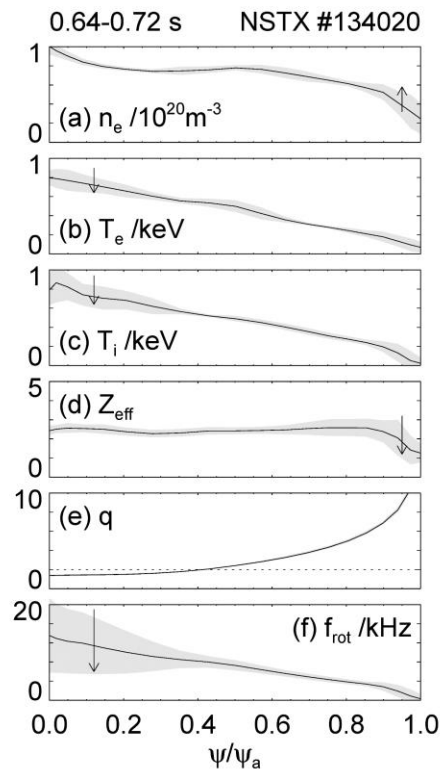
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Low frequency modes affect core rotation

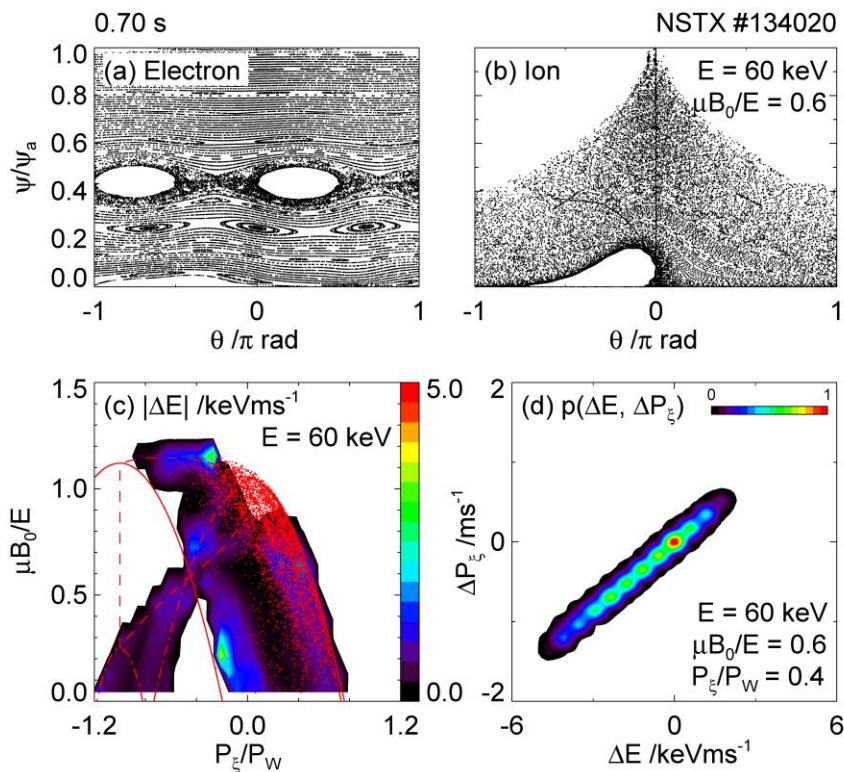
- Profiles

- Unchanged q and density profile
- Small drop in temperatures
- Large rotation slowing down at core ($q < 2$)



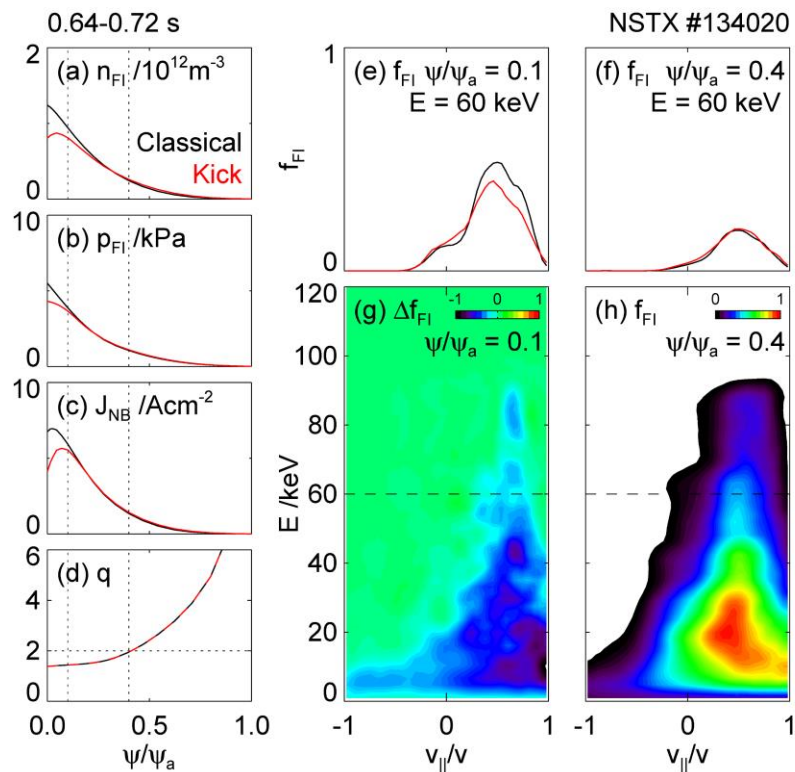
Resonant island appears near core for fast ions

- “Kick” probability
 - Deposited fast ions occupy core co-passing orbits
 - ORBIT: “Kick” for fast ions is localized near core and boundary
 - Core: Resonant island
 - Boundary: Tearing mode island
 - Deposited fast ions are kicked out from core region (= transport)



Depletion is core-localized in fast ion distribution

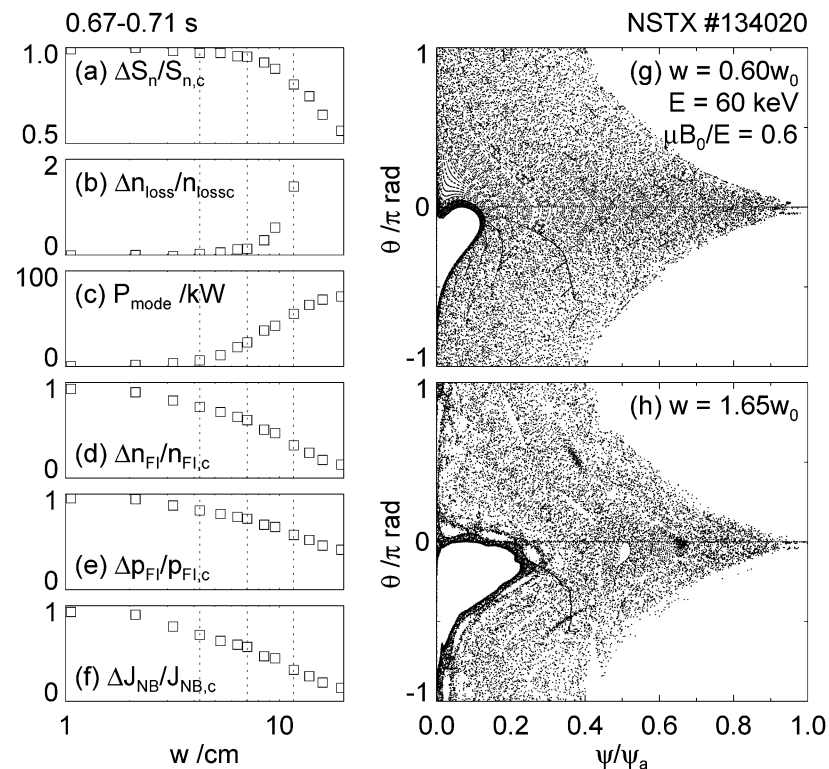
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Islands over threshold turn flux surfaces chaotic

- Poincaré plots

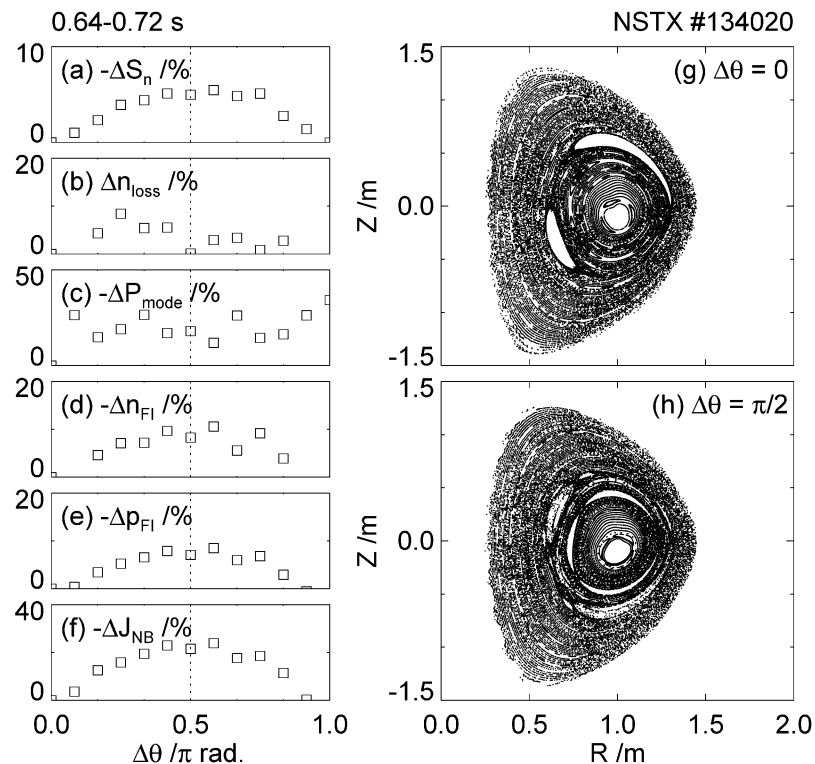
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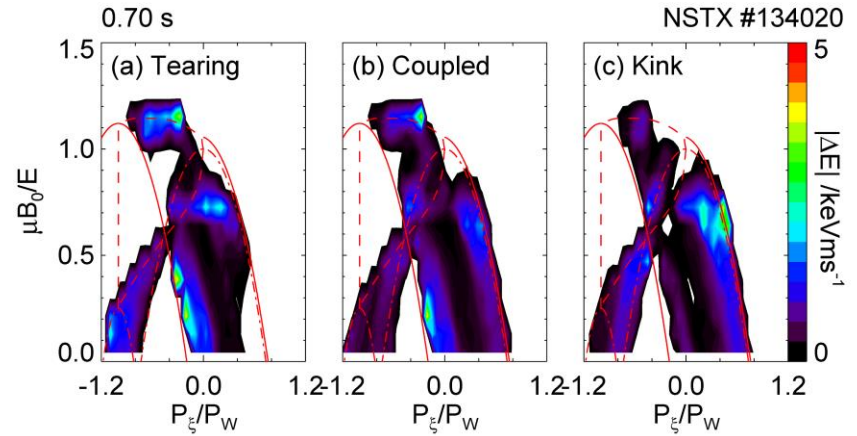
[†] Fixed relative phase: Islands aligned at midplane when core displaced to high field side



Fast ion distribution impacts mode coupling

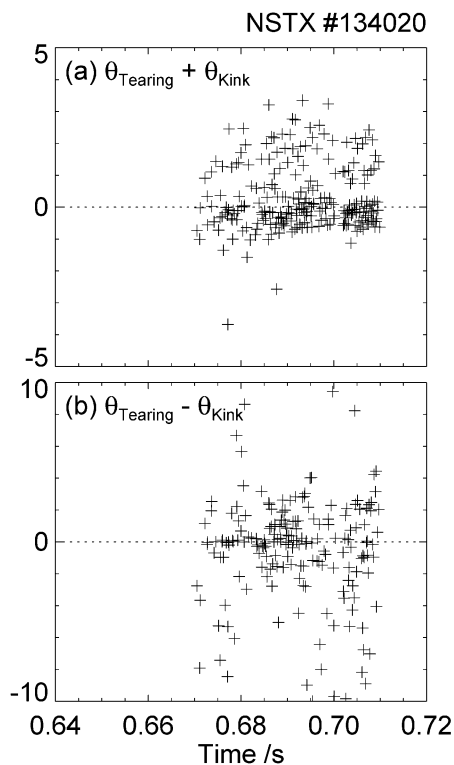
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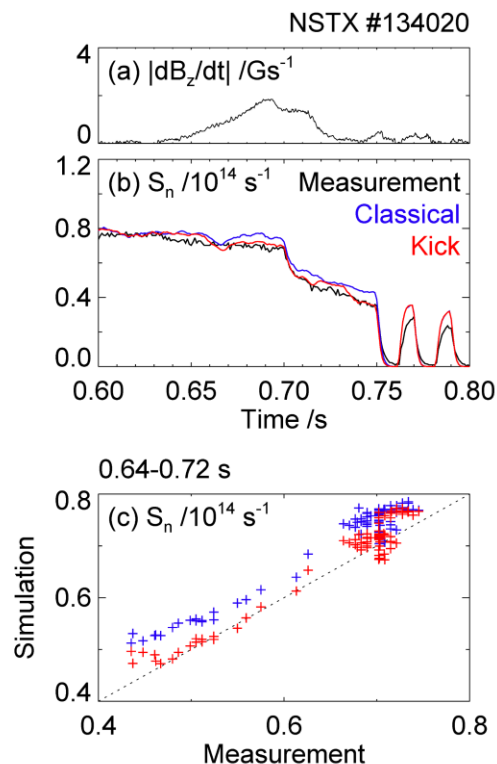
Backup – Relative phase of coupled modes

- Phase difference is constant during mode excitation
- Phase sum is constant too?



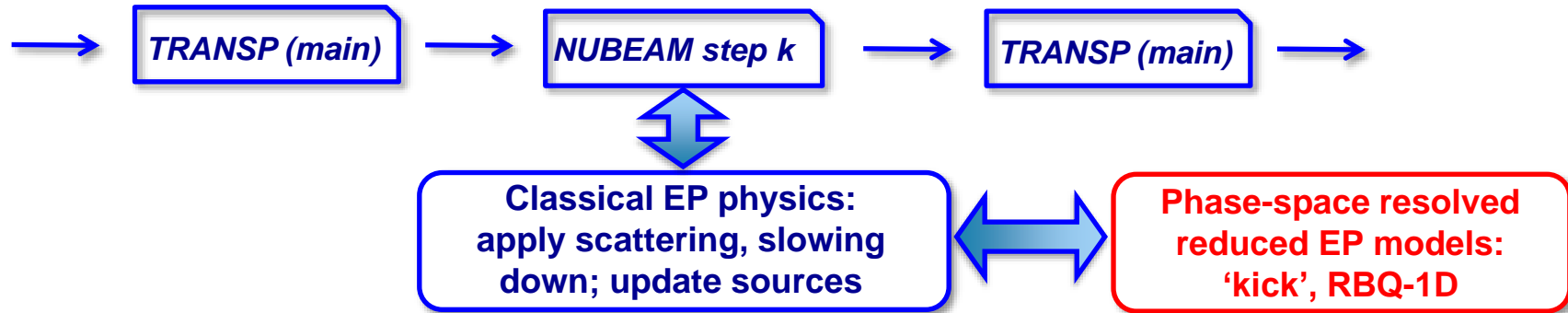
Backup – Full discharge modeling

- Modeling of 0.71 – 0.75 s
 - Tearing mode 3/1 coupled with internal kink ($n = 1$) excited
 - Transition at 0.72 s after surfaces of $q = 2$ and $q = 3$ coincide



Kick and RBQ-1D reduced models address EP transport in time-dependent integrated simulations

- NUBEAM module accounts for (neo)classical EP physics
 - Includes scattering, slowing down, atomic physics



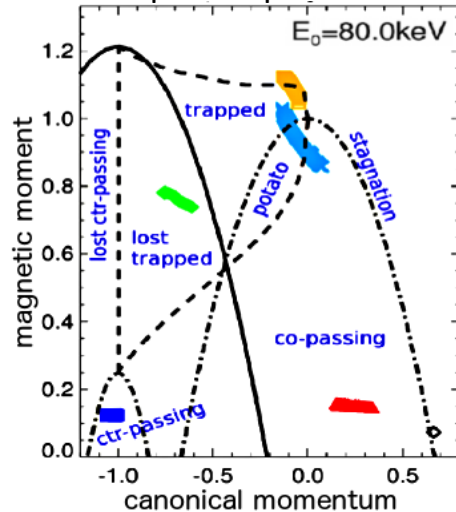
New physics-based models enable predictive capabilities

Constants of Motion variables are used to describe resonant wave-particle interaction

Each orbit characterized by:

$$\left\{ \begin{array}{l} E, \text{ energy} \\ P_{\zeta} \sim mRv_{\text{par}} - q\Psi, \text{ canonical momentum} \\ \mu \sim v_{\text{perp}}^2/B, \text{ magnetic moment} \end{array} \right.$$

- Complex orbits in real space translate in simple trajectories in phase space



Wave stability (drive):

$$\gamma \propto \omega \frac{\partial F_{nb}}{\partial E} + n \frac{\partial F_{nb}}{\partial P_{\zeta}}$$

- Resonant interactions obey simple rule:

$$\omega P_{\zeta} - nE = \text{const.}$$



$$\Delta P_{\zeta} / \Delta E \propto n / \omega$$

$\omega = 2\pi f$: mode frequency
 n : toroidal mode number

Define **transport matrix(es)** for NUBEAM:

$$p(\Delta E, \Delta P_{\zeta} | E, P_{\zeta}, \mu)$$

“Conditional probability that a particle at (E, P_{ζ}, μ) receives kicks $\Delta E, \Delta P_{\zeta}$ from wave-particle interaction”

