

Influence of q profile on Tearing Stability & Error Field Sensitivity

by Richard Buttery¹
with Stefan Gerhardt², Rob La Haye¹,
Jong-Kyu Park², Steve Sabbagh³

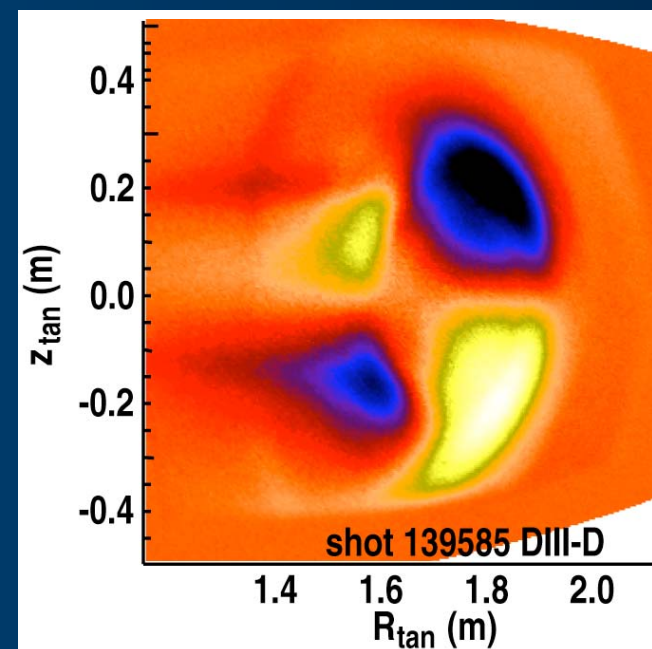
Presented to the
NSTX Research Forum, March 2011

¹General Atomics, USA

²Princeton Plasma Physics Laboratory, NJ.

³Columbia University, NY.

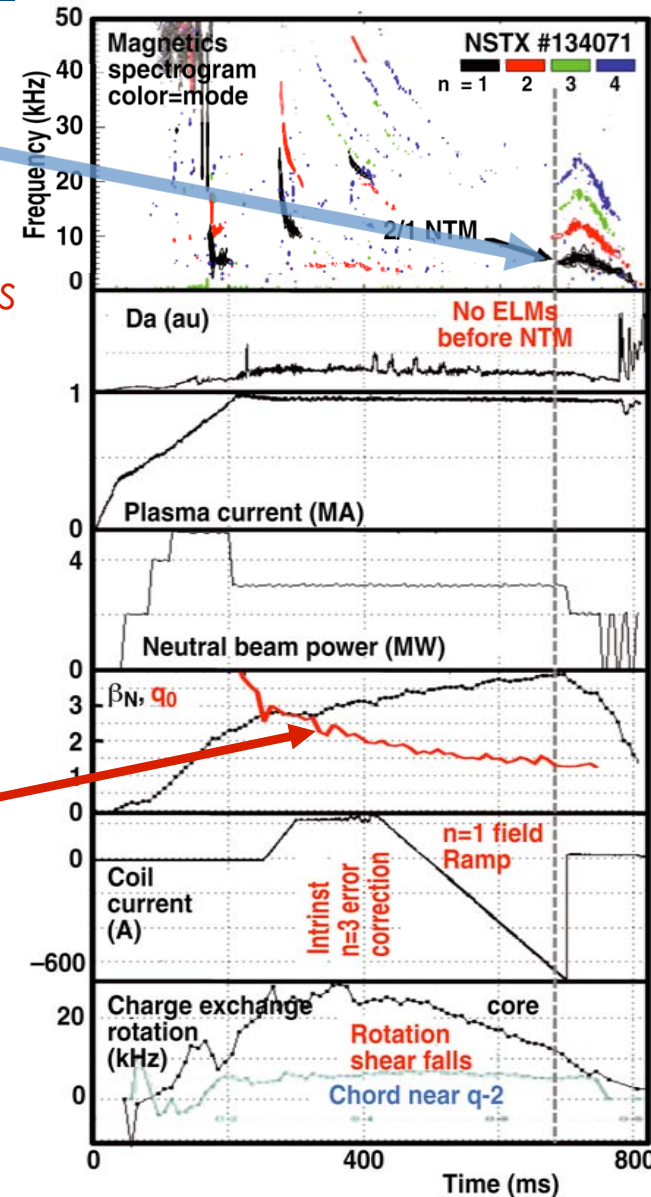
Work funded by the US DOE.



Tearing Modes are Critically Dependent on the q Profile

- **2/1 modes come out of the noise**
 - Intrinsic tearing instability, driven by dJ/dR
 - Performance limit that depends on q profile
 - *Likely source of variation in previous scaling studies*
- **Error field thresholds depend on TM stability**
 - EF brakes plasma accessing TM instability ($\leftarrow q$)
 - May further depend on q profile if plasma response amplifies fields differently
- **Need to probe both tearing β limit & error field threshold (2 effects) vs q profile**
 - Exploit natural q profile evolution on NSTX
 - Ramps in β or **error field**; Vary ramps to scan q
 - Tune to control n_e or access higher q_{\min}

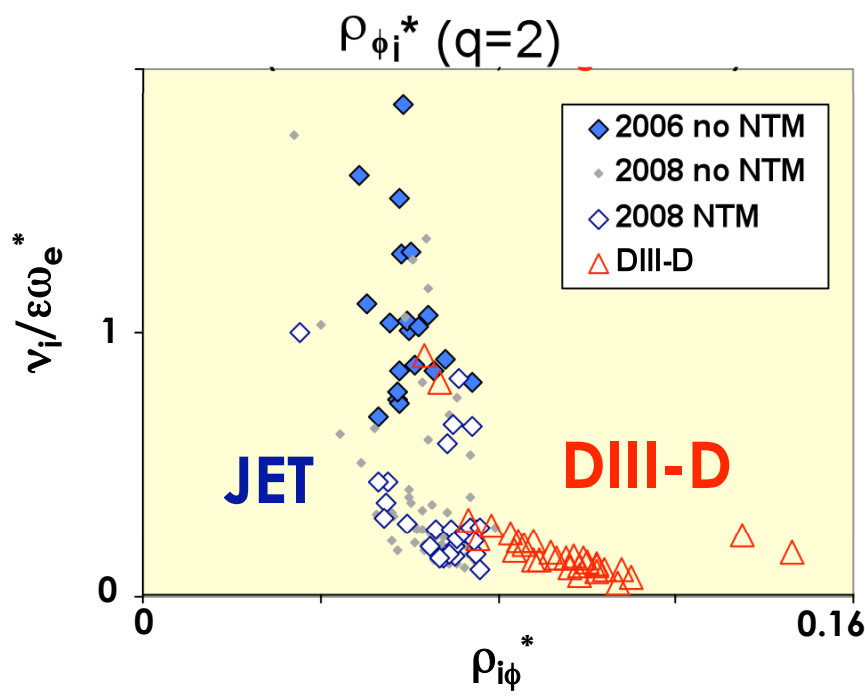
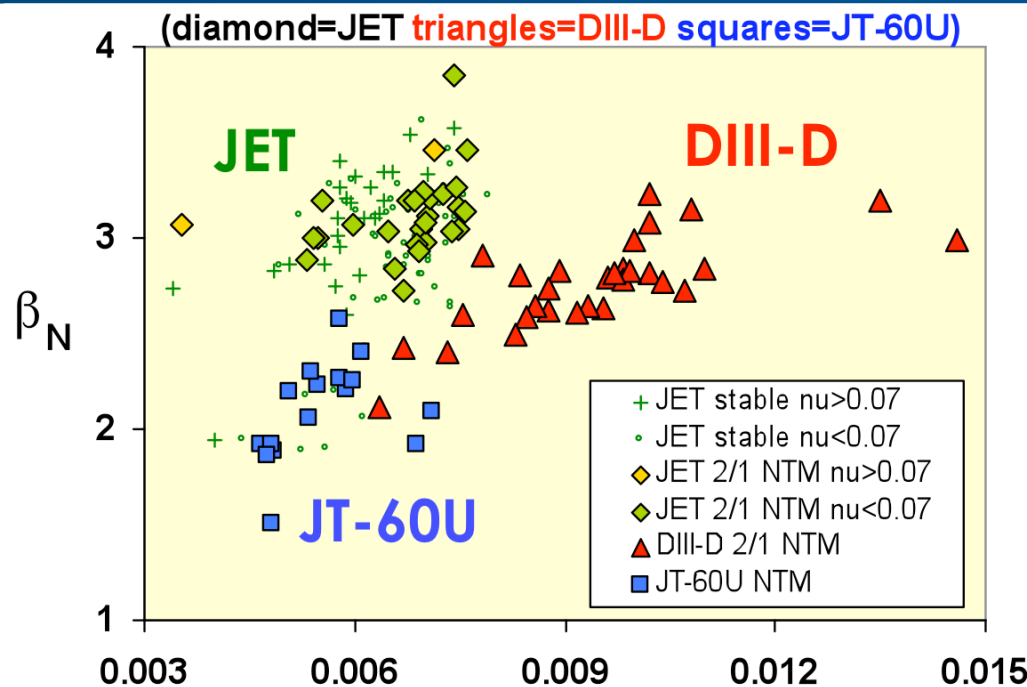
This is key to developing regimes for future devices & understanding tearing physics in general



- **Extra slides for background or discussion...**

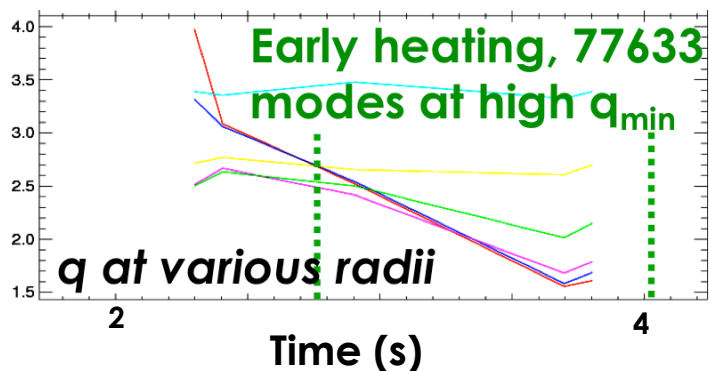
JET Hybrid Plasmas Sit Above β Limit of Other Devices: Other parameters coming into play – q profile?

- JET sits above DIII-D and JT-60U trends
 - JT-60U lower rotation \rightarrow lower β_N
 - But DIII-D high rotation
 - Possible collisionality role? No:
 - JET unstable at \diamond low ν^*
 - But stable at $+$ high and \circ low ν^*
- \rightarrow Collisionality provides 'access condition' for NTM
- Enables q profile modification
 - Can change Δ'
 - **q profile is the parameter to test...**



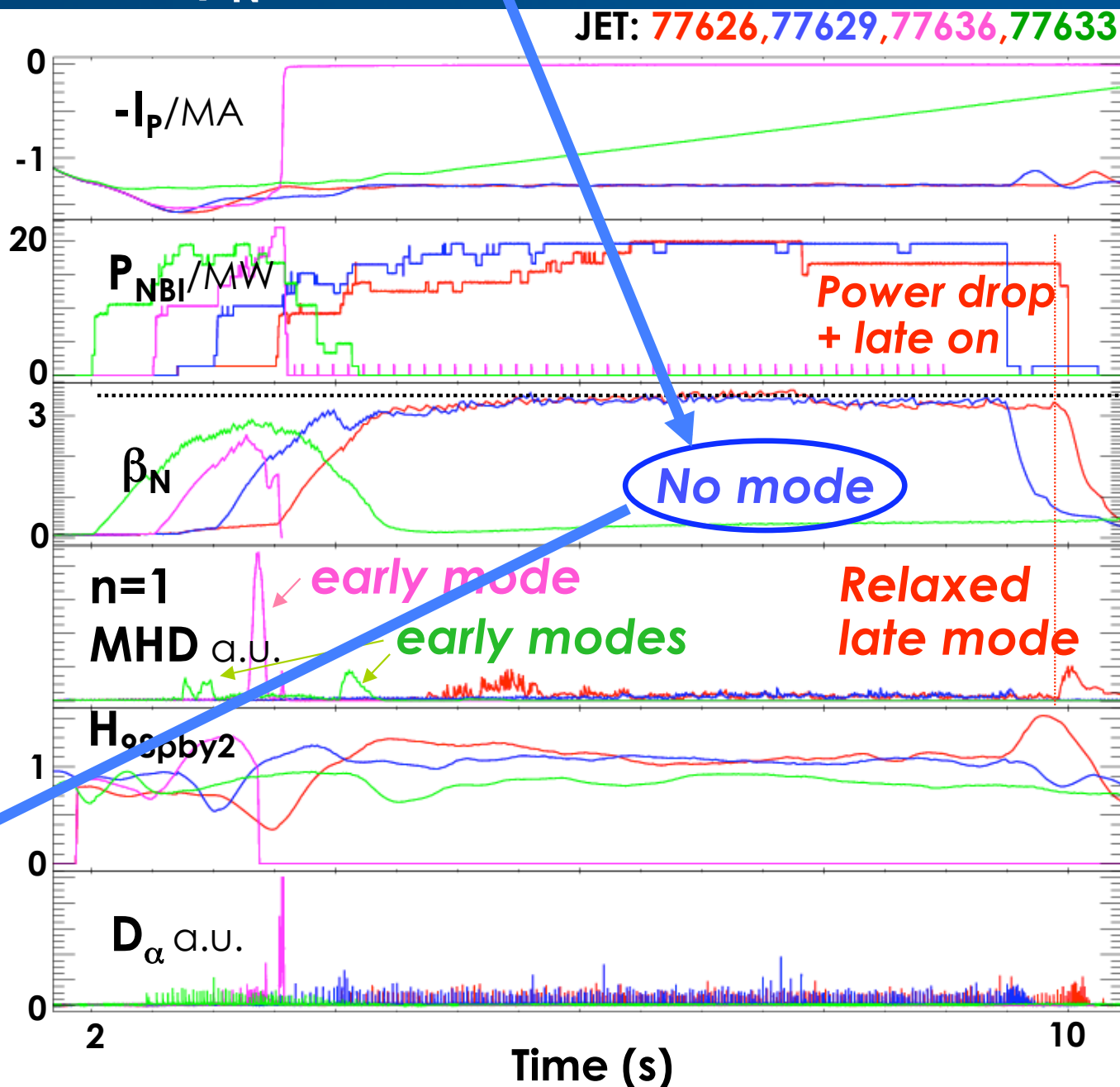
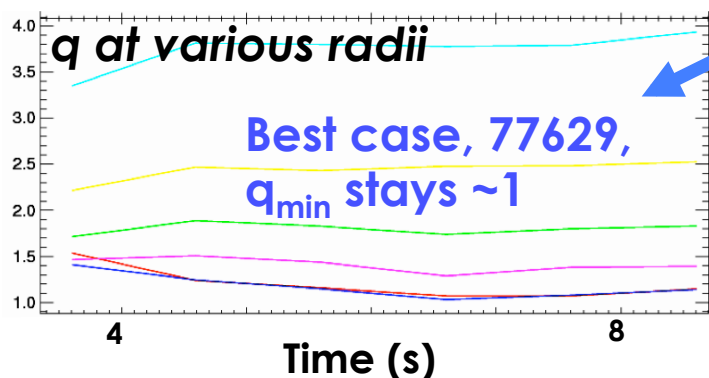
JET shows 'just right' degree of relaxation needed to maintain stability at high β_N

- Mode if profiles too 'advanced':

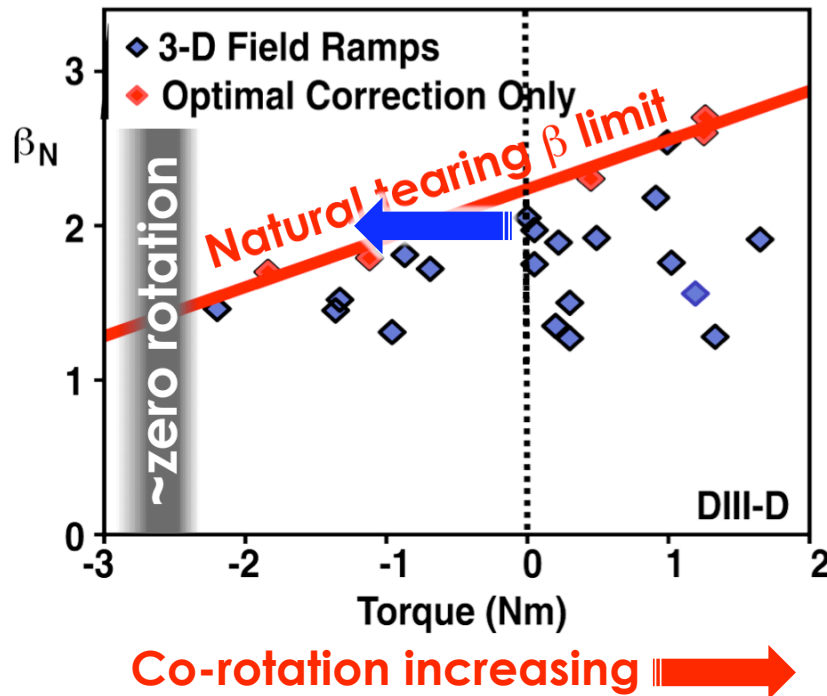


- Fully relaxed plasma also less stable

- Mode at lower β_N or occurs later

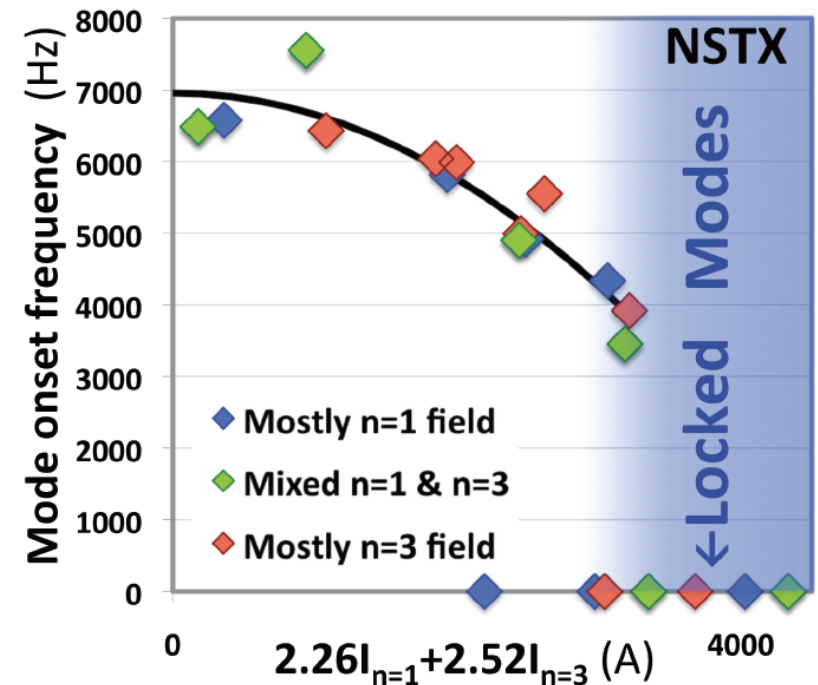


Background: Error Fields Access Tearing Instability by Lowering Rotation Shear



- DIII-D shows operational relationship between “natural” & “error field” tearing modes

- NSTX shows connection of rotating and locked mode onset mechanisms



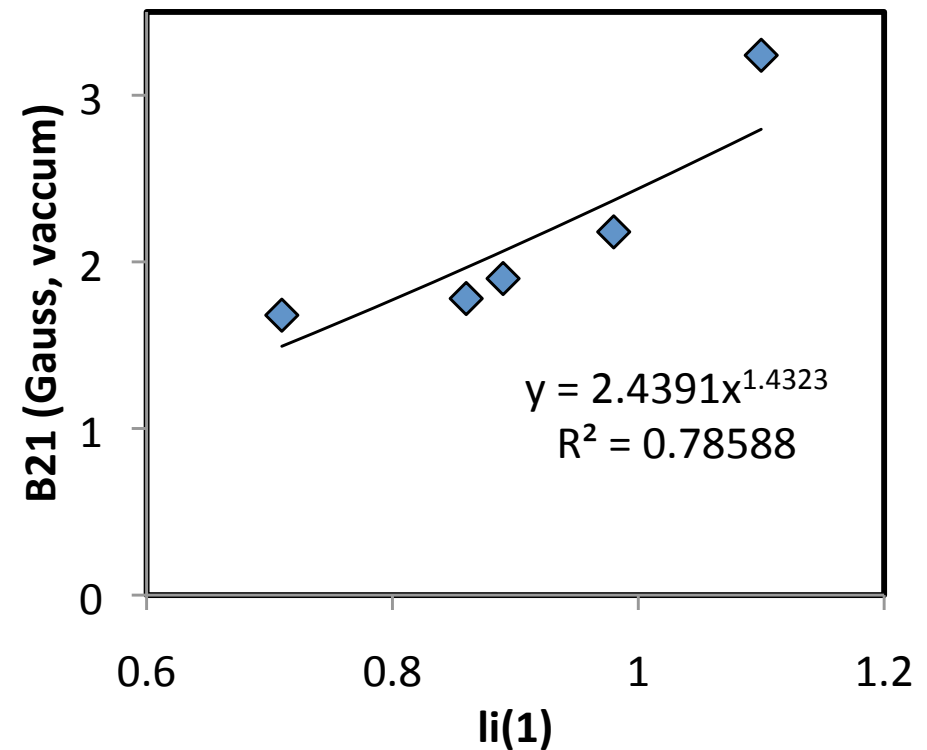
Error Field Thresholds Depend on J Profile

- Data from Ohmic plasmas JET:

- Fast current ramp flattens q and moves $q=2$ further in

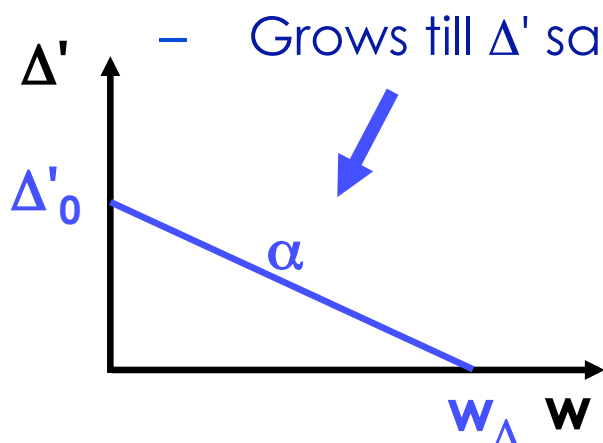
Table 4. The (2,1) field (at the $q = 2$ surface) required for the error field mode in low- l_i (2.5 MA, 2.5 T) pulses compared with the standard value corrected for density variation and intrinsic error

Pulse	l_i	Threshold (G)
Average of standard l_i pulses	1.1	3.24
44254	0.89	1.90
44255	0.86	1.78
44256	0.98	2.18
44258	0.71 (8 MW ICRF)	1.68



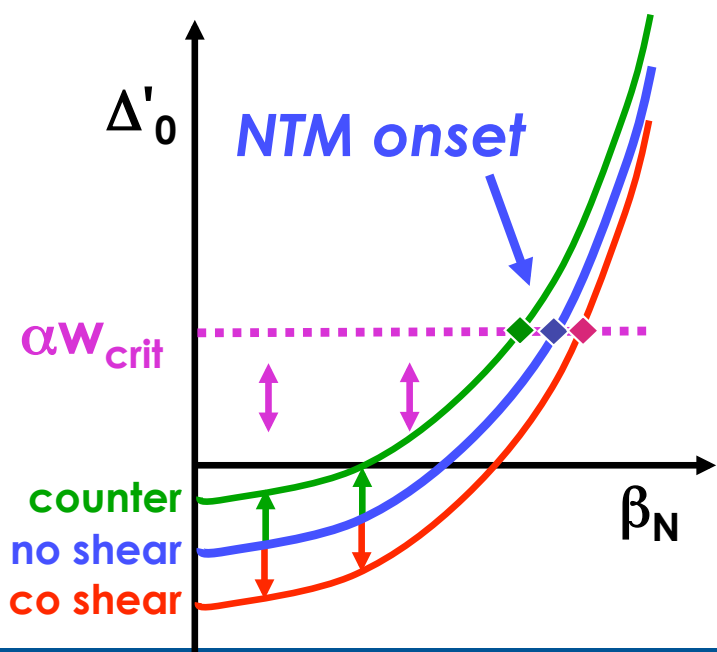
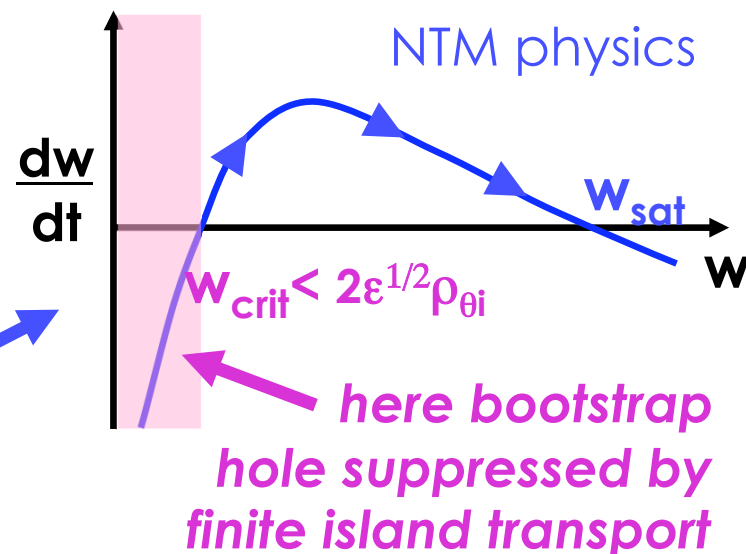
Possible 'Minimal' Δ' Model of Tearing Mode Triggering

1. Positive Δ' excites a small island



2. Growth becomes "neoclassical" if island big enough:

$$w_{\Delta} > w_{\text{crit}} \Rightarrow \Delta'_0 > \alpha w_{\text{crit}}$$

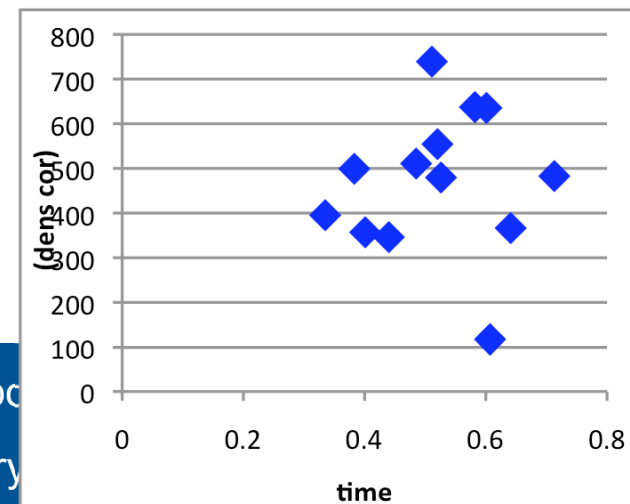
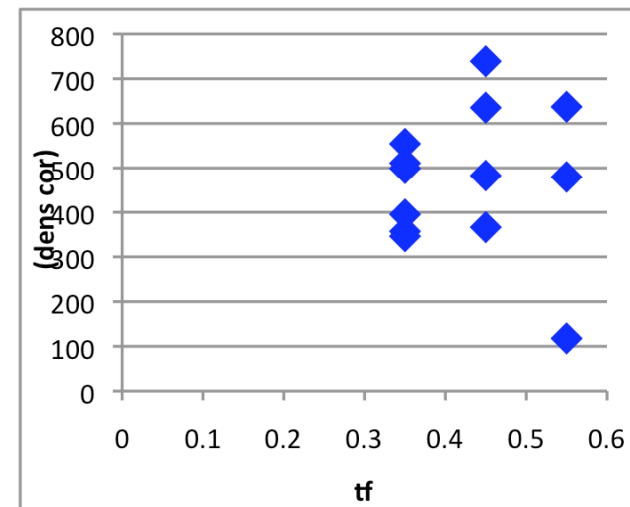
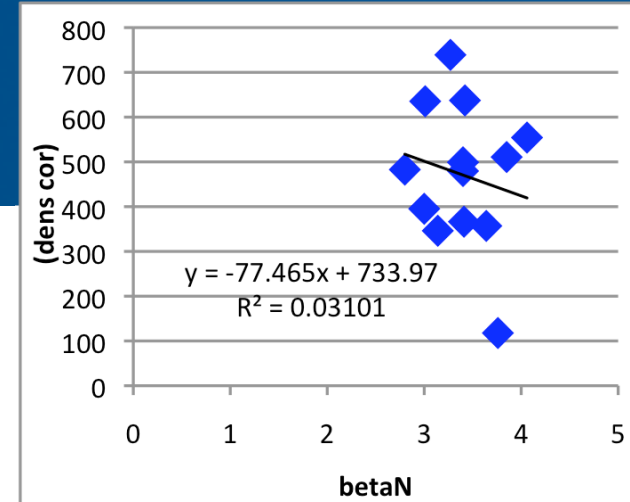
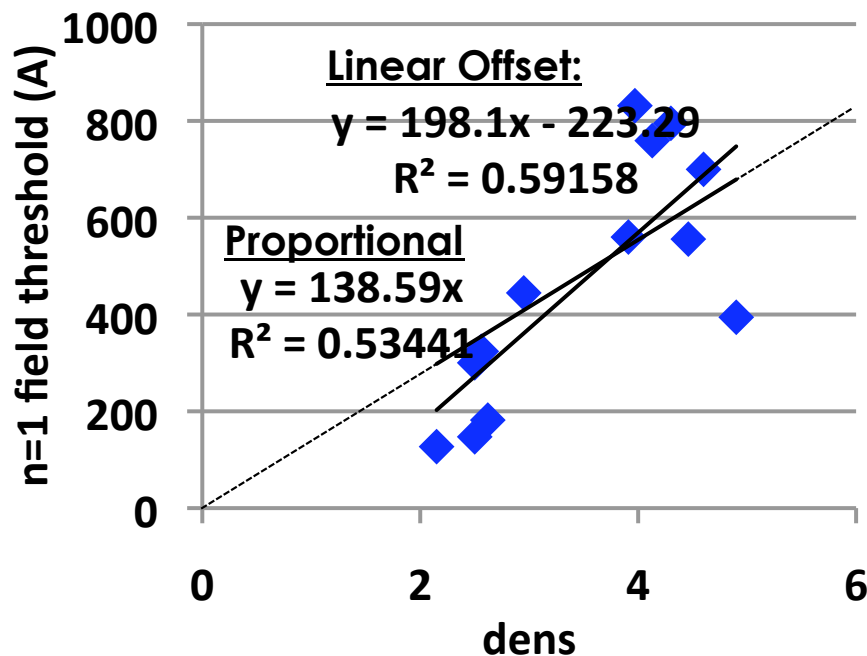


3. Δ'_0 is function of rotation shear and β_N

- **Increases/decreases** in rotation shear will change tearing mode onset β_N
- ρ^* variation introduced through w_{crit}
- **but note much harder to excite mode at low β_N away from Δ' pole**

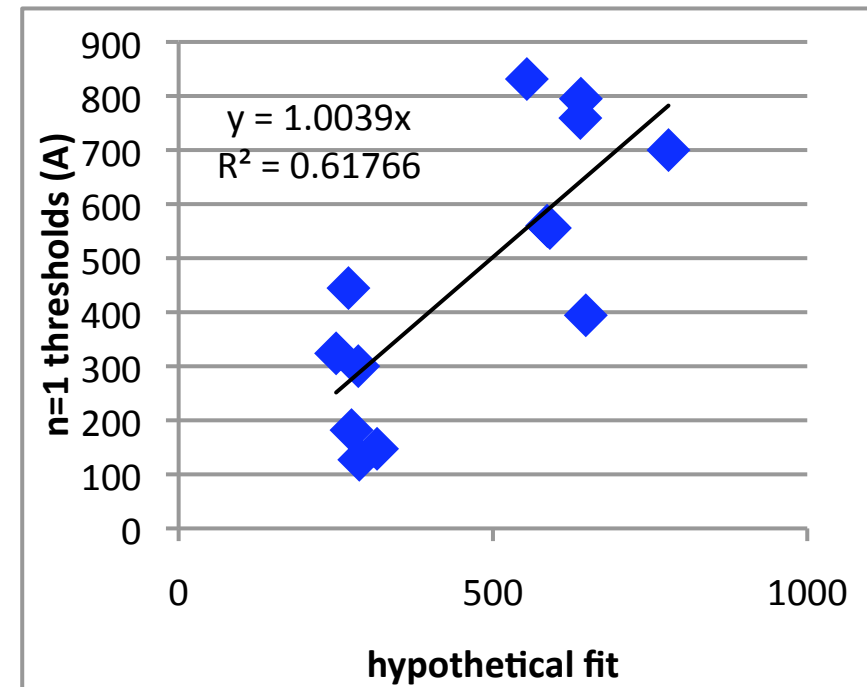
2010 NSTX EF Scaling Study Shows Considerable Scatter

- Use offset linear density fit to correct out density variation
 - No obvious trend in other variables now! ➔
 - Can we do better based on phenomenology?...



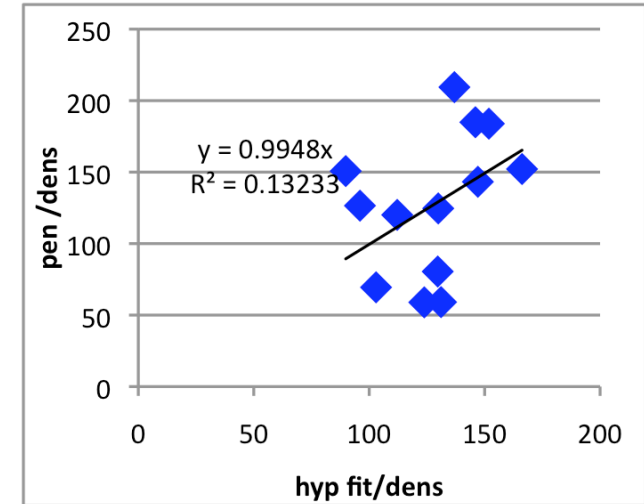
NSTX 2010: Make a fit based on intuition

- **Hypothesize power law form constructed:**
 - Positive density dependence seems clear
 - Shot phenomenology shows less or no error field needed if higher β_N – suggests negative β_N exponent
 - Arbitrary TF coefficient
- **Start from this and vary coefficients by hand to minimise residual**
 - *Actually get a better fit than regression fitting!*
- **Form found:**
$$I_{\text{pen}} \sim n_e \beta_N^{-1.25} B_T^{0.6}$$
 - Can we constrain more than one variable?

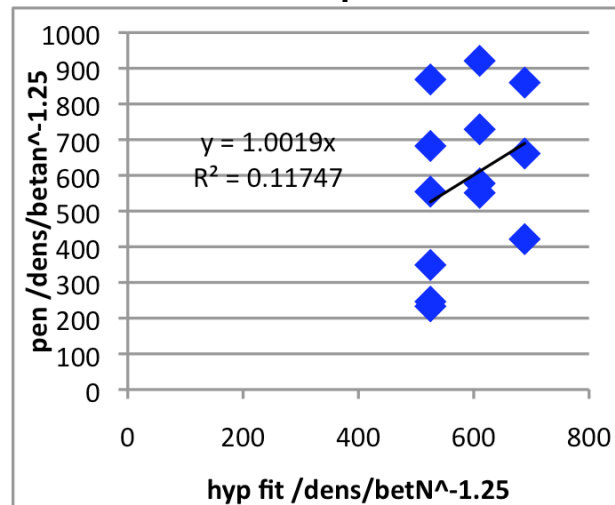


NSTX 2010: Is there a residual dependence in the fit?

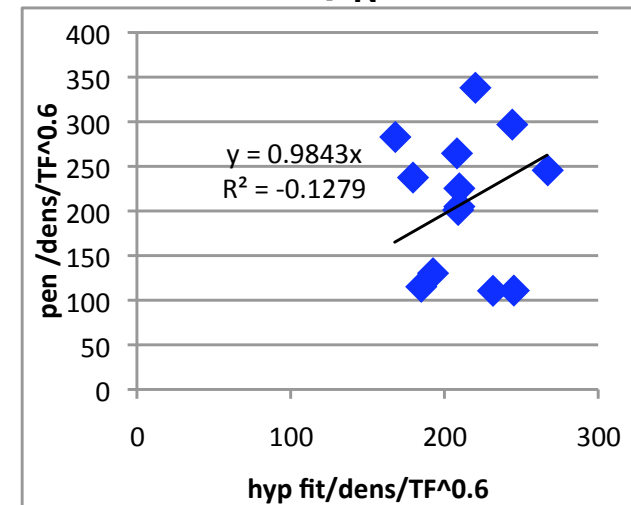
- Stripping out density dependence → leaves weak correlation
 - Further analysis shows might be B_T or β_N ,
 - but neither is well constrained & there may be no further trend!
- Possible further hidden variables?
 - Keep looking!
 - q profile, MHD?



Remaining B_T variation:



Remaining β_N variation:



Governing Physics – á la old Ohmic theory...

Penetration is about overcoming the plasma rotation

- **Modes form when resonant surface is braked by resonant response to EF to half it's natural frequency**
 - Tiny static island induced by EF
 - Viscous forces try to keep bulk plasma rotating slipping past the island - *this opposes island growth*
 - Torque exerted through island and viscosity to brakes plasma
 - *N=3 NTV effects assist this process?*
 - If rotation slows enough, island can grow, increasing torque and bifurcating to a locked mode state
 - Threshold scales as $B_{\text{pen}} \sim B_T \omega_0 \tau_A (\tau_{\text{rec}} / \tau_v)^{1/2}$
 - *ω_0 often taken to be electron diamagnetic rotation*
- **Criteria could also be regarded/generalised as condition for when we approach rapid rotation change**
- **Critical elements are:** what determines ω_0 ; whether plasma response changes; and how readily plasma rotation is overcome