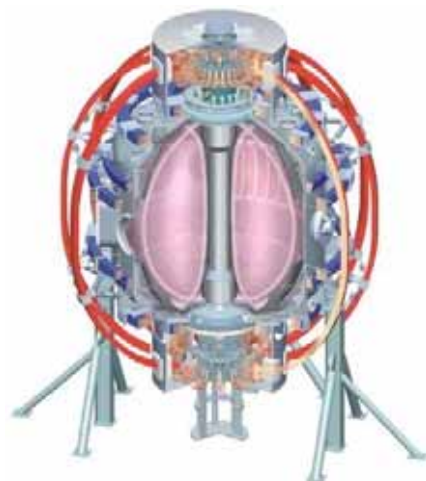


# Synthetic diagnostics for NSTX simulations

**Francesca Poli**

*S. Ethier, W. Guttenfelder, TS Hahm, S. Kaye,  
E. Mazzucato, Y. Ren, D. Smith, W. Wang  
and the NSTX Research Team*

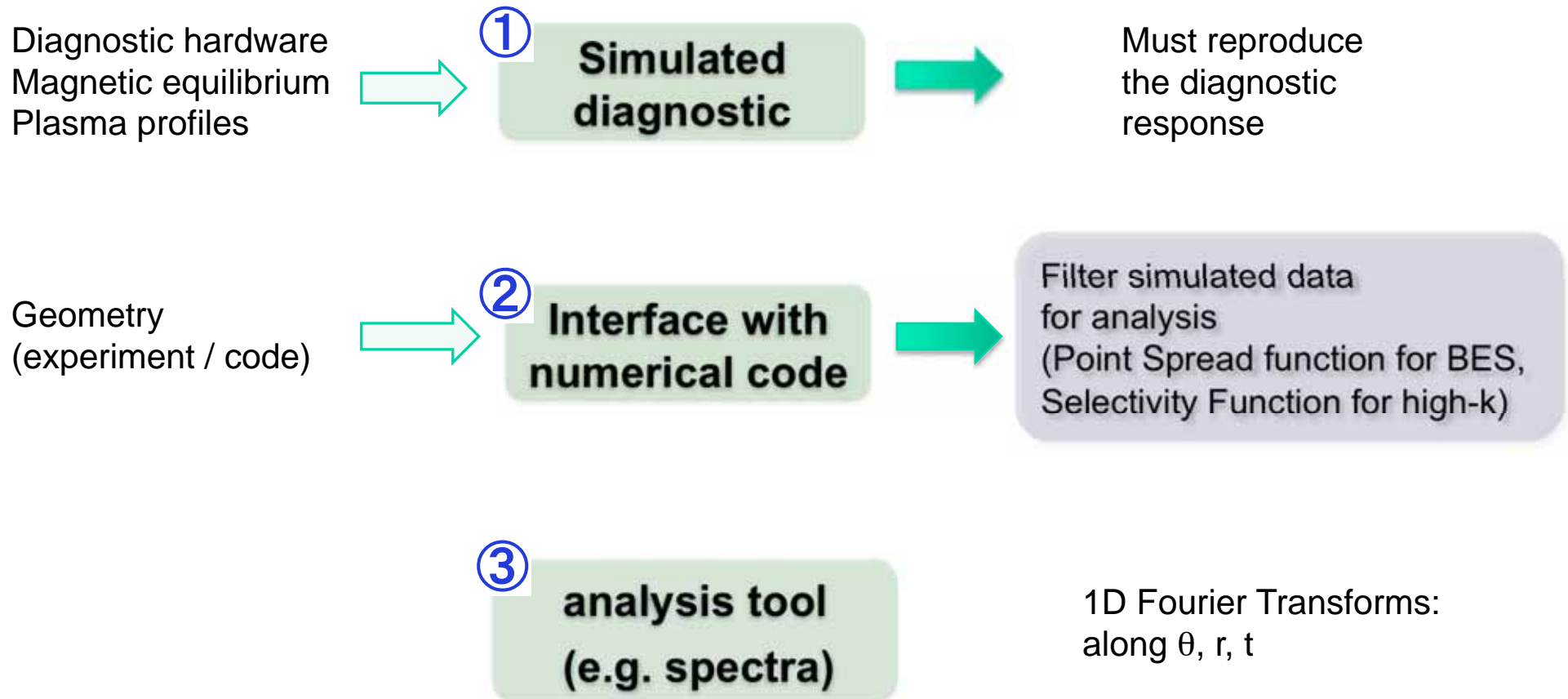
**November, 30<sup>th</sup>, 2010**



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POSTECH  
ASIPP  
ENEA, Frascati  
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ASCR, Czech Rep  
U Quebec

# General (and basic) structure of a synthetic diagnostic

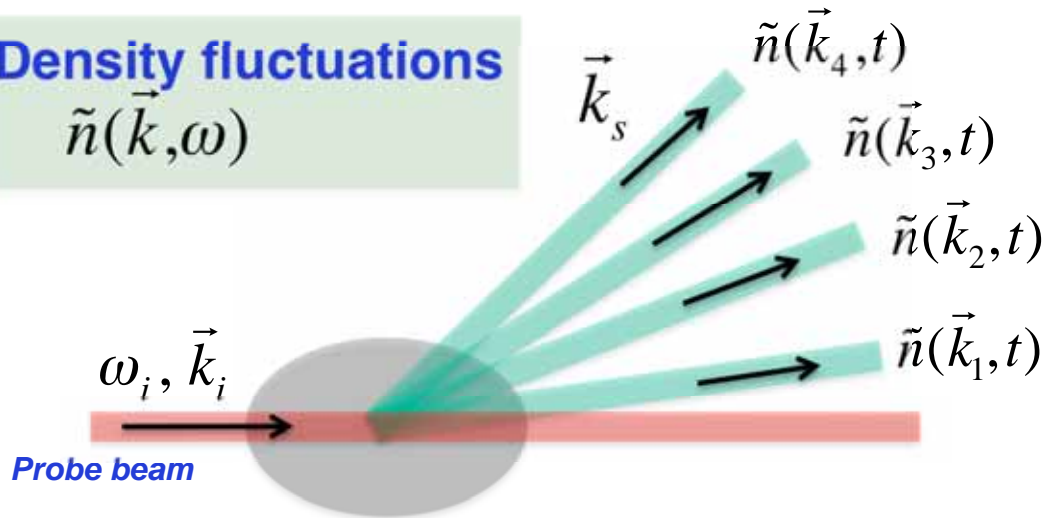


- modular structure
- should be transportable to different numerical codes and adaptable to other diagnostics

# The synthetic high-k aims at reproducing the real diagnostic

Density fluctuations

$$\tilde{n}(\vec{k}, \omega)$$



High-k scattering measures  $\{k_{\perp}\}$

$$\vec{k} = \vec{k}_s - \vec{k}_i$$

$$\omega_i \gg \omega \quad \Rightarrow \text{Small } \theta_s$$

$$k = 2k_i \sin(\theta_s / 2)$$

$$\mathbf{E}_i(\mathbf{r}, t) = \mathbf{E}_i(\mathbf{r}_{\perp}) e^{i(\mathbf{k}_i \cdot \mathbf{r} - \omega_i t)}$$

Fourier Transform of density fluctuations weighted by the beam intensity

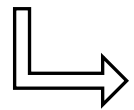
$$\mathbf{E}_s(\mathbf{v}_s) = \frac{r_e}{x} e^{i\mathbf{k}_s \cdot \mathbf{x}} (\hat{S}\hat{S} - \mathbf{1}) \cdot \int_{T'} dt' \int_V d^3 r' \mathbf{E}_i(\mathbf{r}_{\perp}) e^{i(\omega t' - \mathbf{k} \cdot \mathbf{r})} \tilde{n}(\mathbf{r}', t')$$

Direction & amplitude of  $k_s$

Amplitude profile of beam  
(size of the scattering volume)

# Present status of the synthetic high-k

MDS tree



**Beam tracing** ①

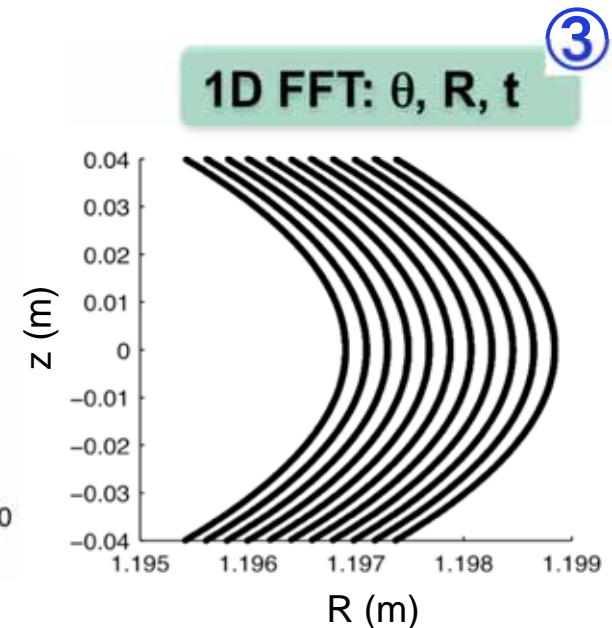
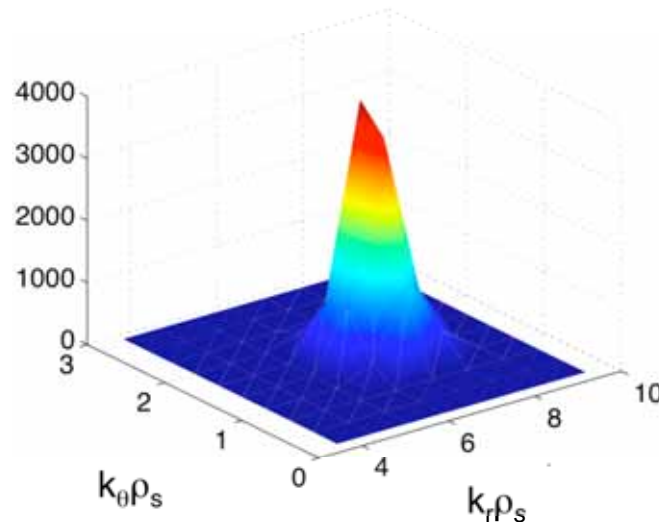
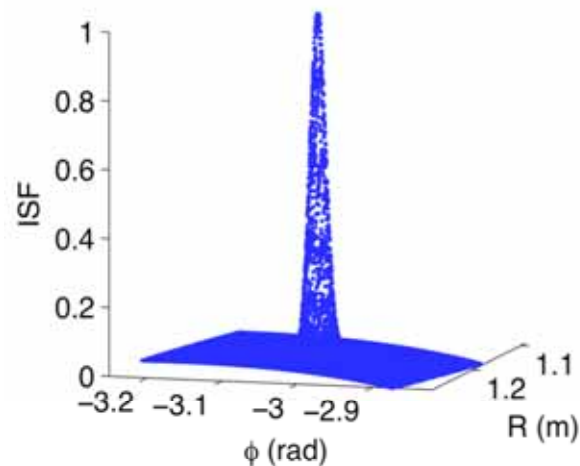


**Write input files**



• interface with GYRO ②  
• interface with GTS

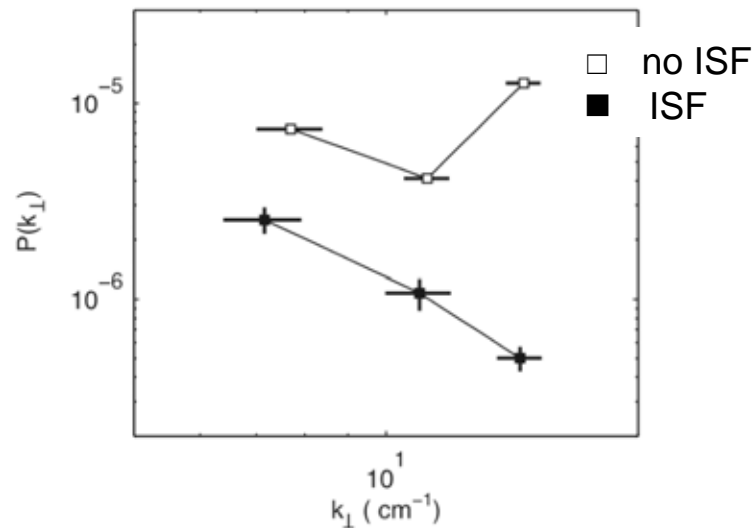
- Uses EFIT/LRDFIT equilibrium + TS profiles
- run complex ray tracing eqs. for probe+receiving beam
  - localize 3D scattering volume
  - compute the instrumental selectivity function
  - produces a  $(k_r, k_\theta)$  filter for the simulated spectra



# The spectral slope is mainly affected by 2 effects

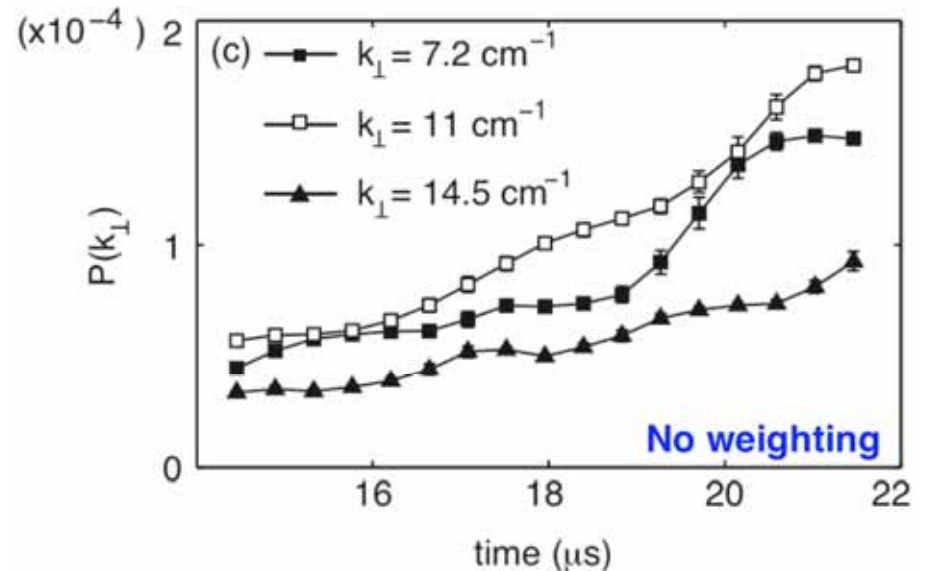
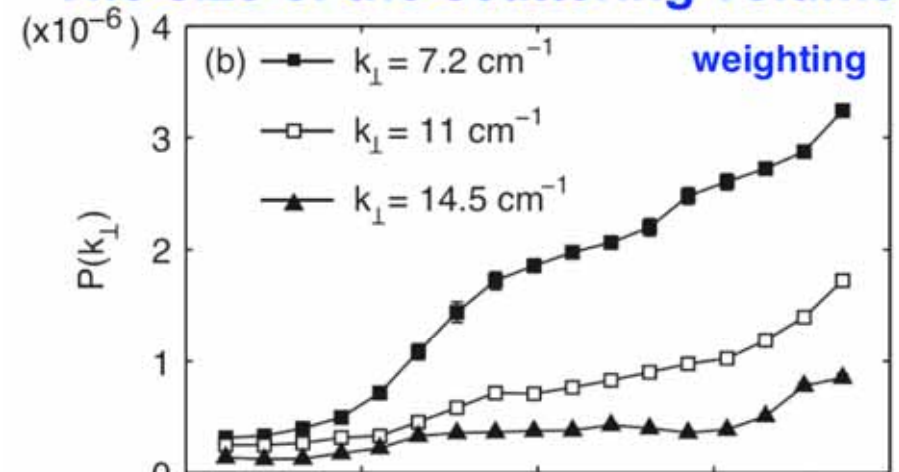
## Geometrical effects in the collection efficiency

$k_{\perp} \sim 7.5 \text{ cm}^{-1}$	1
$k_{\perp} \sim 11 \text{ cm}^{-1}$	87%
$k_{\perp} \sim 15 \text{ cm}^{-1}$	65%



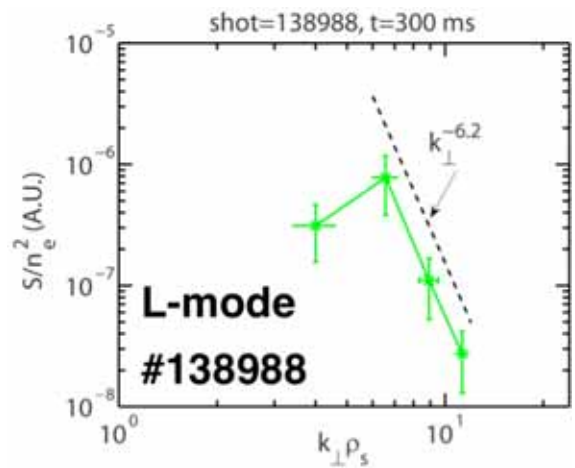
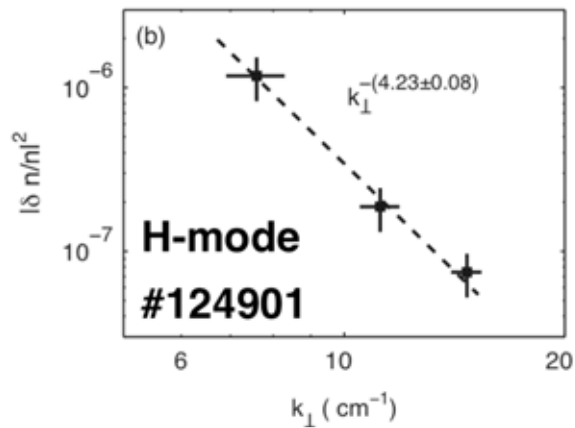
Some contribution to the spectrum slope comes from the experimental setup

## The size of the scattering volume

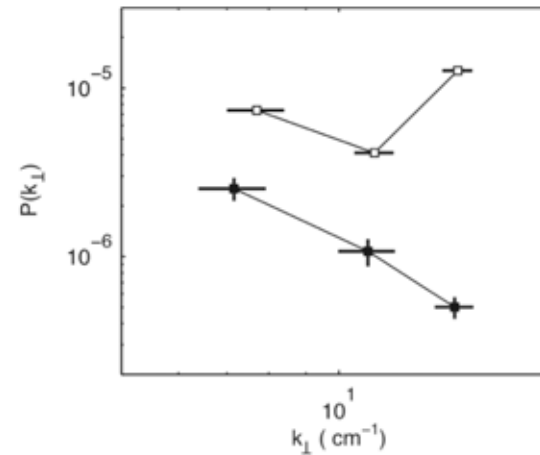


# Geometrical effects are not sufficient to reproduce measurements

## Experiments

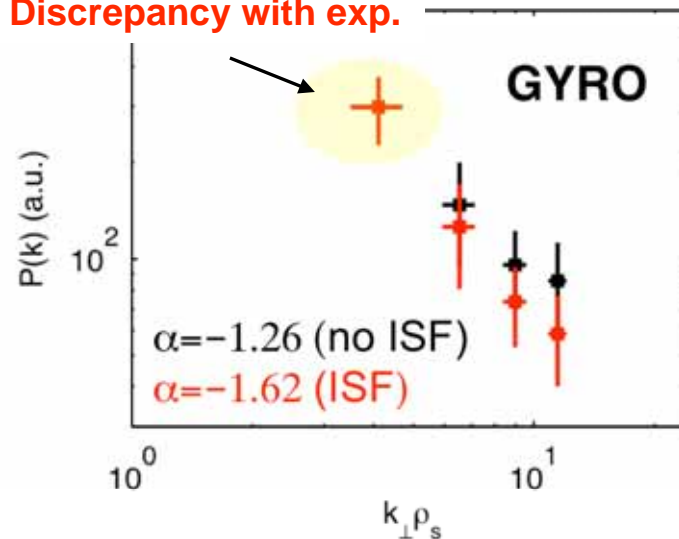


## Simulations



**GTS**

Discrepancy with exp.



**GYRO**

## Future directions and timescales

1. Benchmark of the synthetic high-k
  - Option 1: energy calibration => not feasible in the short time scale
  - Option 2: design an alternate simple experiment
  - Option 3: simulate a calibration experiment
2. Code verification and validation against experiments
  - Given: the high-k measures in a range of  $(k_r, k_q)$  where ETG spectra are maybe not significant and other instabilities can play a role
  - Can we identify a set of experiments for V&V (it would be useful to have high-k combined with other turbulence diagnostics) ?
3. Can we use these same simulations to predict the optimal layout for the second-generation high-k ?

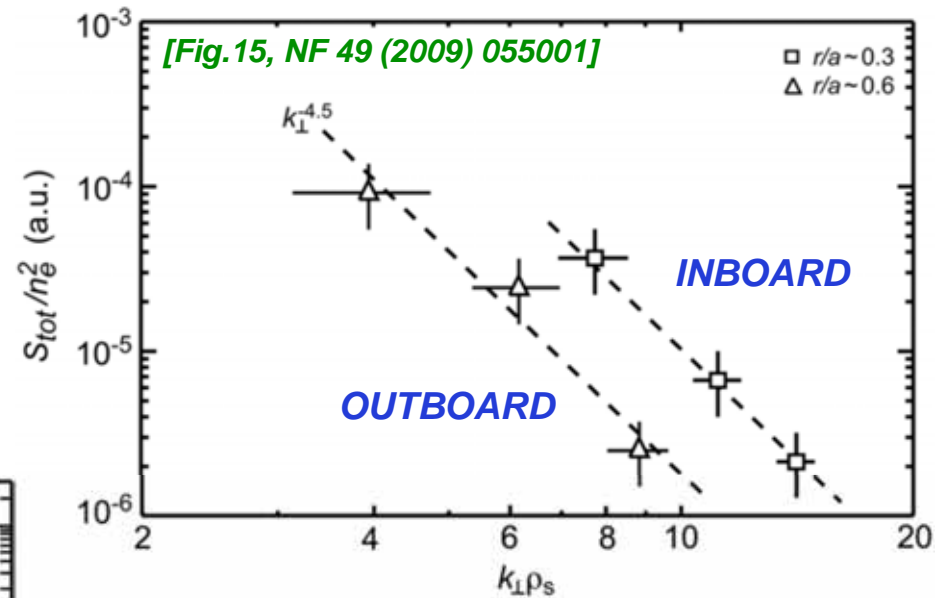
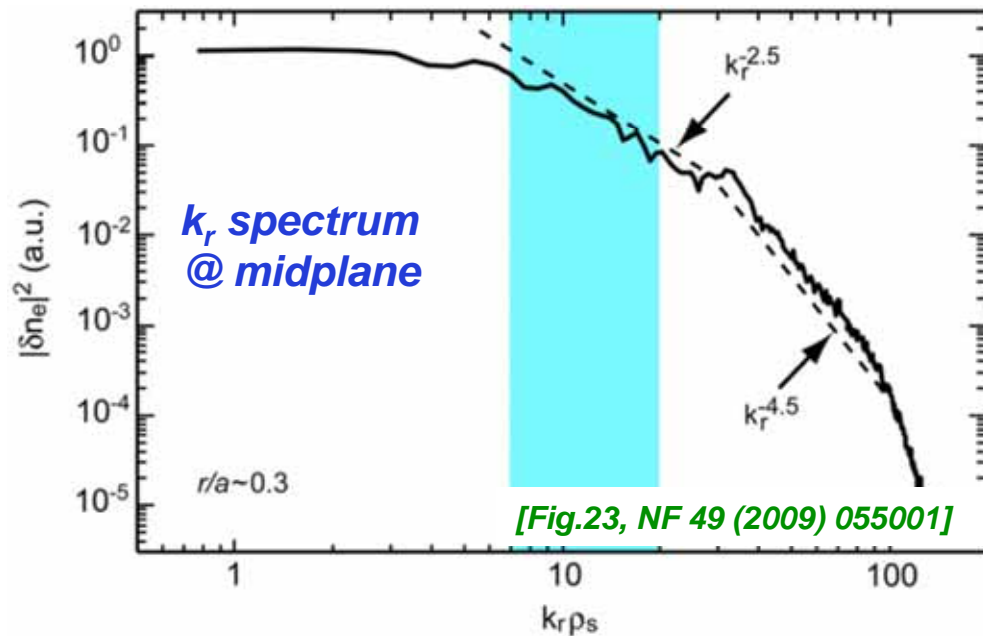
# BACKUP SLIDES



# A direct comparison may lead to fortuitous agreement

$P_{HK}(k_{\perp}^j, \omega)$      *Discrete in  $k_{\perp}$*   
    *Good statistics in  $\omega$*

$P_{SIM}(k_r, k_{\theta}, \omega)$      *Wide range in  $(k_r, k_{\theta})$*   
    *Poor statistics in  $\omega$*



**What has been overlooked ?**

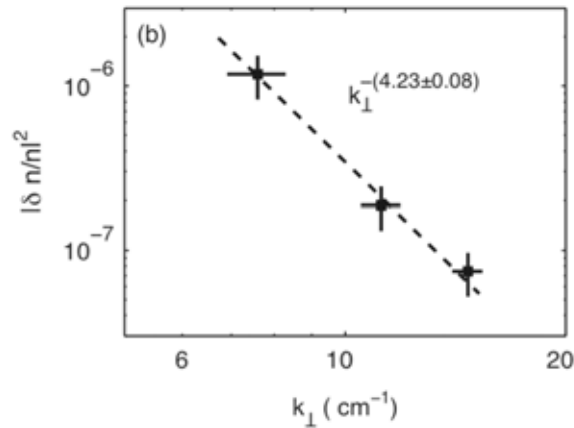
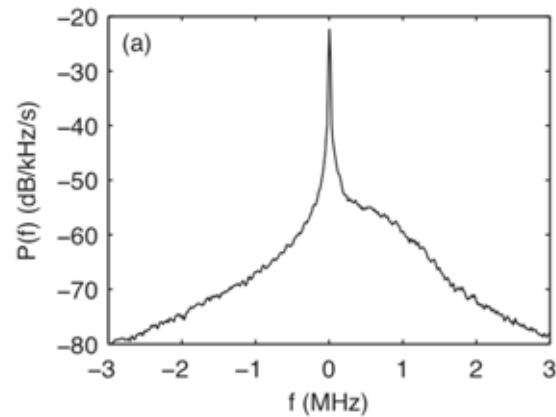
- **selection of  $(k_r, k_{\theta})$**
- **scattering volume**
- **instrumental transfer function**

# Two cases study: L-mode and H-mode plasma

## Turbulence spectra from the high-k scattering diagnostic

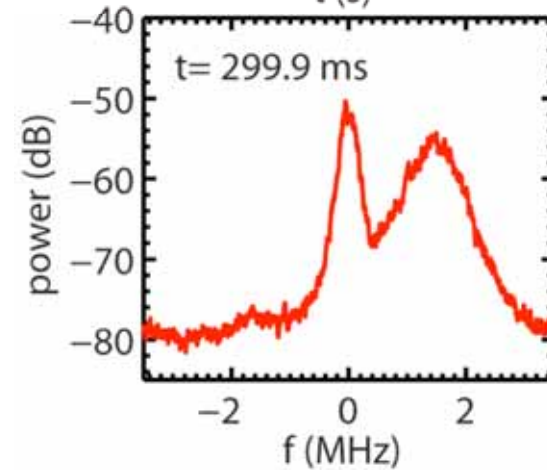
#124901 **H-mode**

t = 300 ms,  $\Delta t=10$ ms

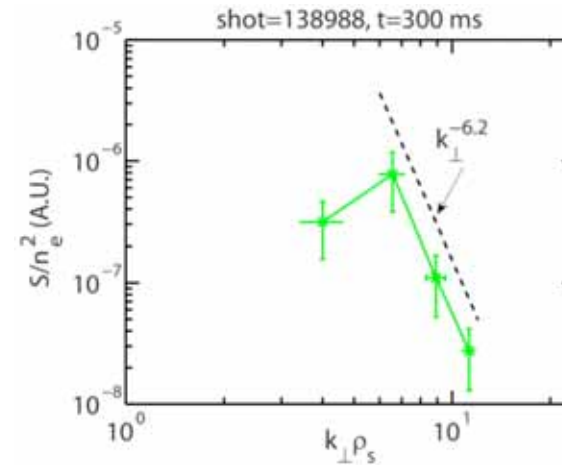


#138988 **L-mode**

t = 300 ms,  $\Delta t=1$ ms

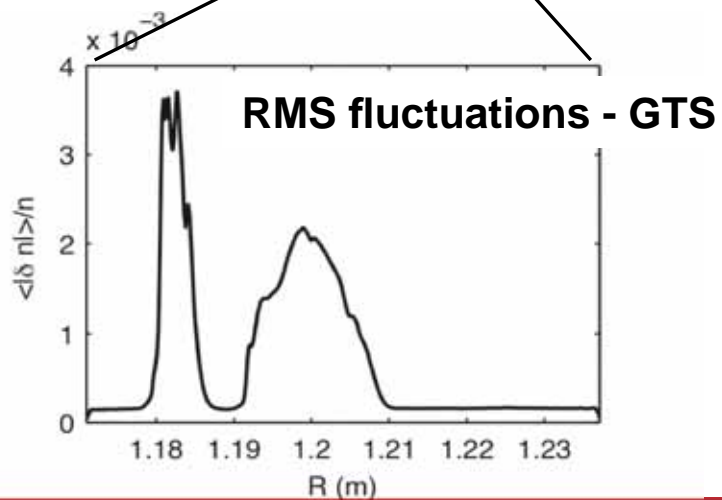
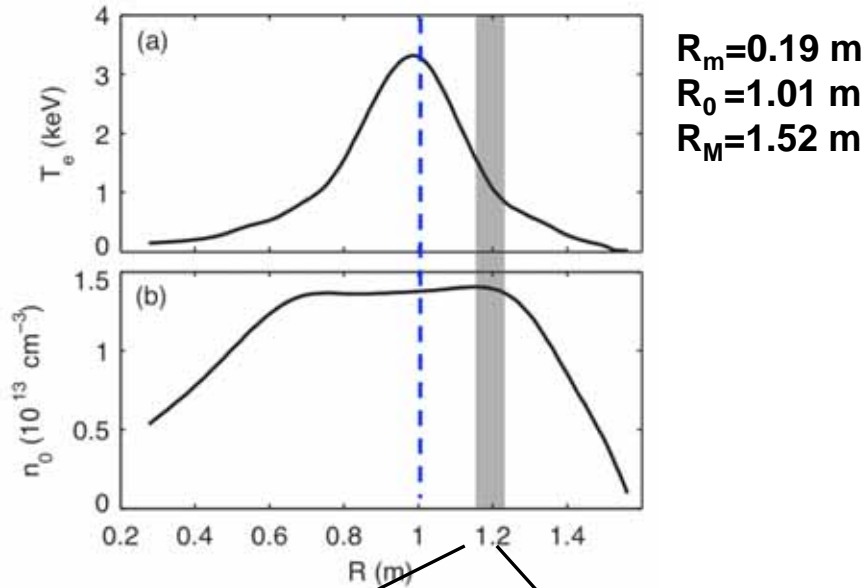


See poster BP9.67  
Y. Ren *et al*

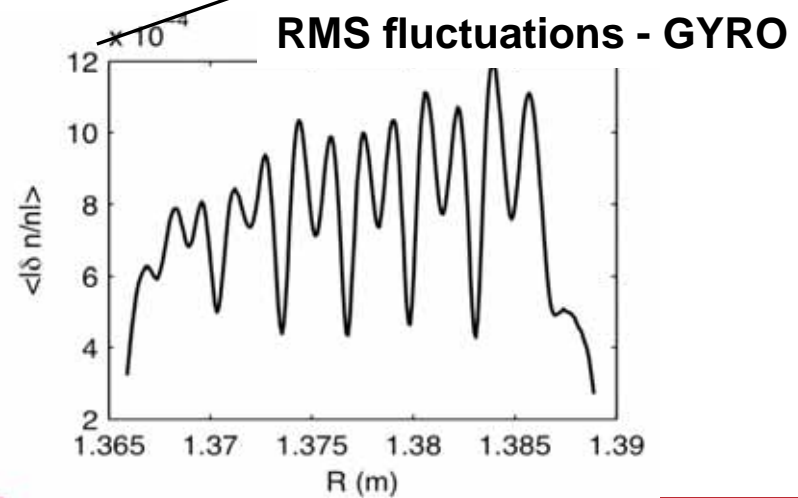
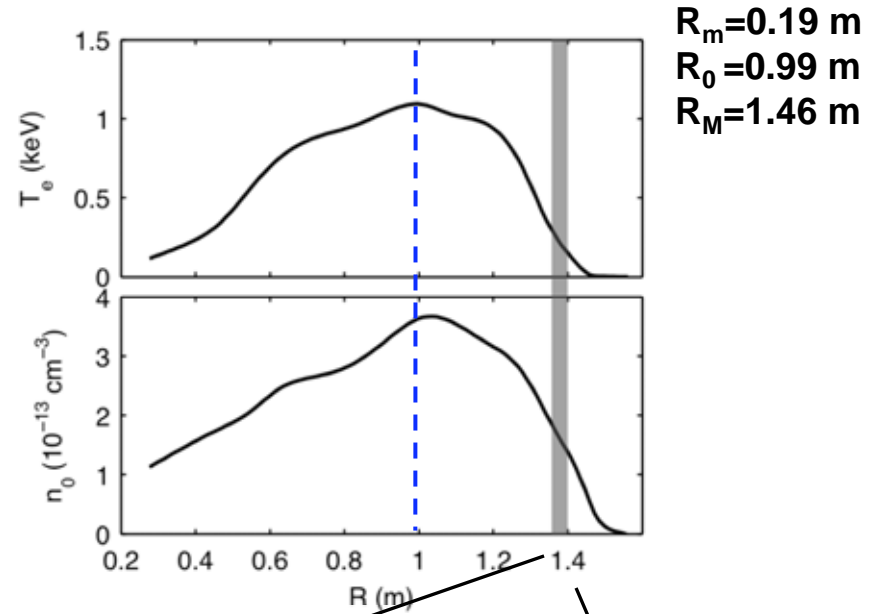


Level of fluctuations is similar, but spectra are steeper in L-mode

Measured profiles

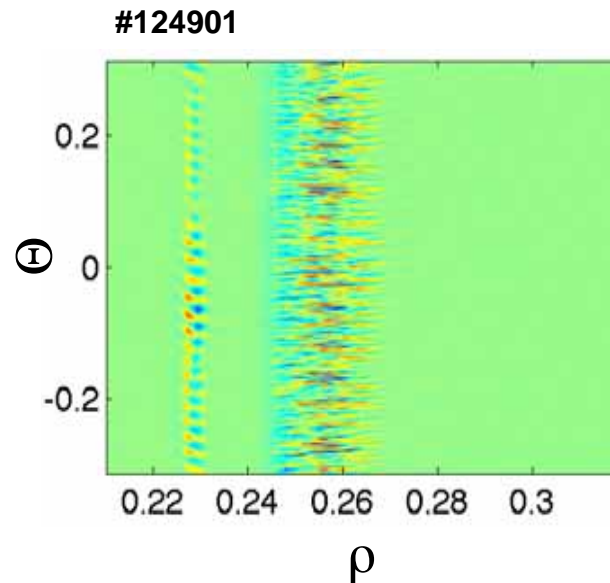
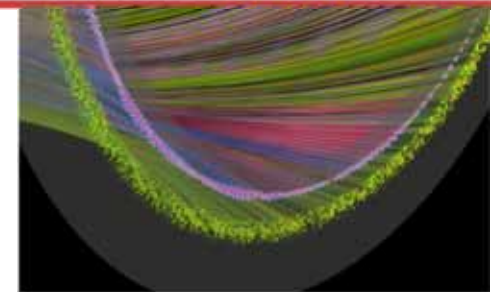


Measured profiles



# Interface with GTS\*: spectra are computed in real coordinates

[\* WX Wang et al, *Phys. Plasmas* **13** 092505 (2006) ]



Simulation using:

- numerical equilibrium
- experimental parameters
- electrostatic
- adiabatic ions

$(\rho, \theta)$  grid not regular

- $\Delta\rho, \Delta\theta$  are set by Larmor radius  $\rho_e$
- $\Delta\theta$  is regular on each flux surface, it changes between flux surfaces

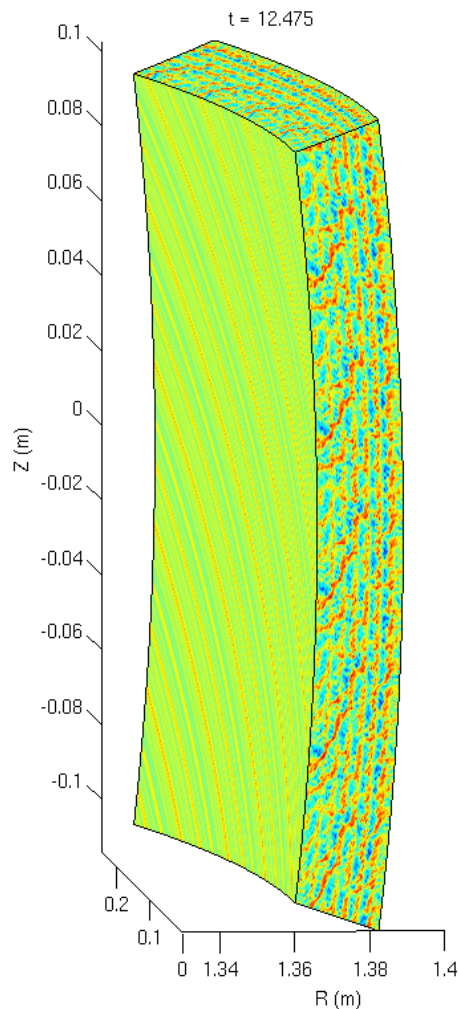
64 planes: toroidal separation comparable to scattering volume extension  
=> each plane is dealt with independently

**Compute spectra in real coordinates =>  $k$  directly compared with exps**

# Interface with GYRO\*: spectra are computed in flux coordinates

[\* J. Candy and R. Waltz, *Journal Comp. Physics*, 186-545 (2003) ]

#138988



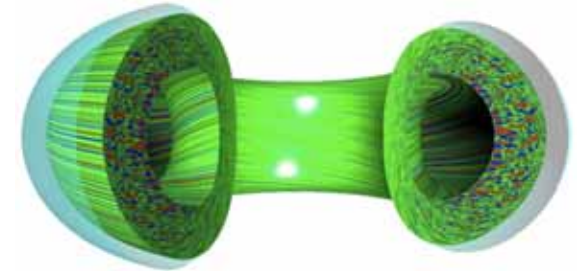
Local simulation using:

- numerical equilibrium
- experimental parameters
- finite collisionality
- toroidal flow and flow shear
- electrostatic ( $\beta_e$  is small)
- adiabatic ions (will ultimately use kinetic)

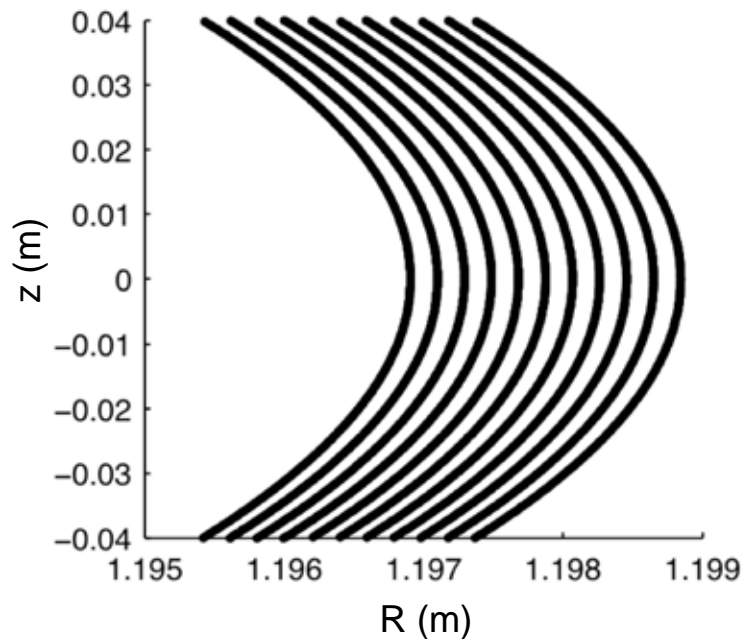
$(\rho, \theta)$  grid regular  $\Rightarrow$  compute spectra in flux coordinates

Periodicity along toroidal direction  $\Rightarrow$  need only a finite number of planes (50 for this simulation)

**$\Rightarrow$  need to convert  $k$  to physical units to compare with experiments**



## Interface with GTS: $k_\theta$ spectra are computed in real space along a pseudo-polar direction



1. Along each flux surface in real space  $(R, z)$  we construct a trajectory :

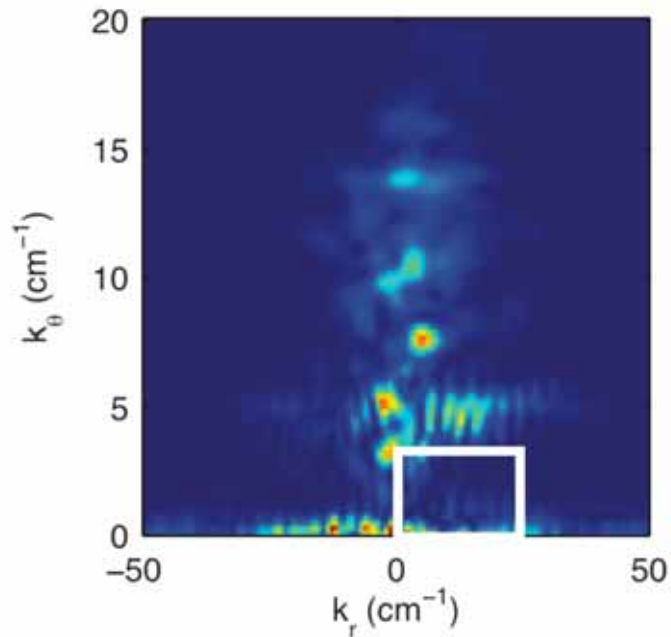
$$ds_j = \sqrt{(R_{j+1} - R_j)^2 + (z_{j+1} - z_j)^2}$$

2. Interpolate density along this trajectory using the same step for all flux surface (to have the same  $k_N$ )
3. Compute Fourier Transform using the same number of points (to have the same  $\Delta k_\theta$ )

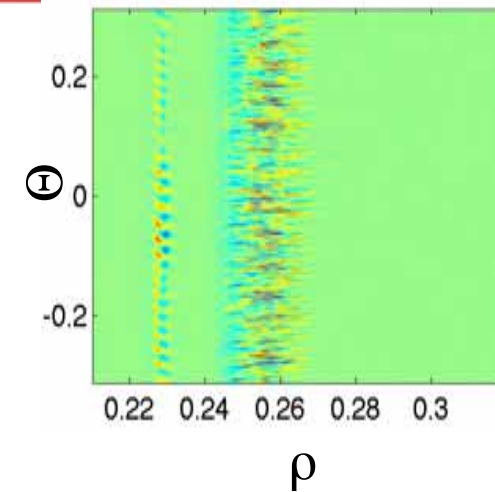
=> The Fourier components depend only on the value of  $R$  at midplane  $\tilde{n}(R_{mid}, k_\theta, t_i)$

**PROBLEM:** in order to compute the transform along  $R$ , we need to interpolate amplitude and phase of Fourier components

# Interface with GTS: density fluctuations are interpolated in flux coordinates



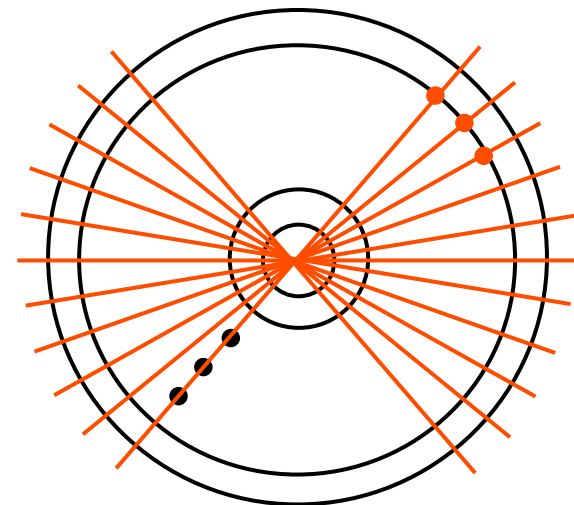
phase interpolation generates artificial structures in  $k_r$ , due to phase jumps where density structures are localized.



This issue can be overcome by pre-processing density fluctuations in flux coordinates

- interpolate along  $\rho \Rightarrow$  uniform  $\Delta R$  @ midplane
- redistribute data along  $\theta$

## NEXT STEP UPGRADE



# Block 1: Beam tracing\*

\* [ Nowak and Orefice, Phys. Plasmas 1 1242 (1994) ]

Follow propagation of a Gaussian beam  
in an anisotropic plasma

$$\vec{E}_i(\mathbf{r}, t) = \mathbf{E}_i(\mathbf{r}_\perp) e^{i[k_0 S(\mathbf{r}) - \omega_i t]} \quad S = R + iI$$

$$\begin{cases} R(x, y, z = 0) = 0 \\ I(x, y, z = 0) = -\frac{x^2 + y^2}{k_0 a^2} \end{cases} \quad \text{Initial conditions}$$

$$\Re: (\nabla R)^2 - (\nabla I)^2 = N^2 \quad \Rightarrow \text{Leads to } D(\mathbf{x}, \mathbf{k}', \omega)$$

$$\Im: \nabla R \cdot \nabla I = 0 \quad \Rightarrow \text{Amplitude is constant along rays}$$

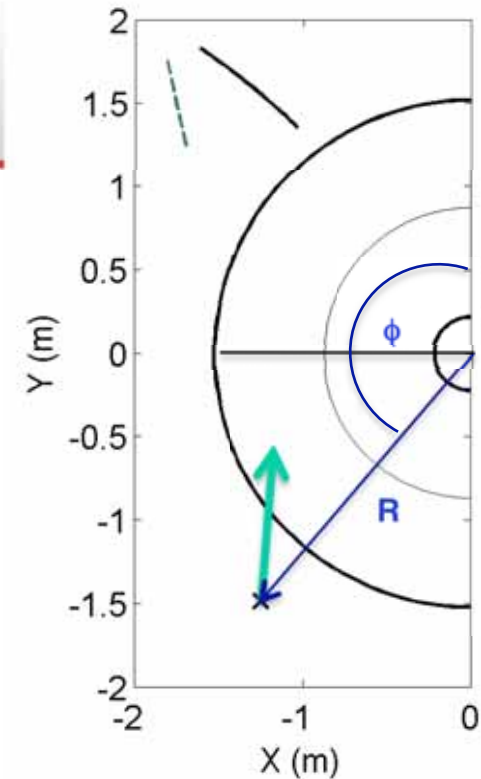
$$\mathbf{k} = \mathbf{k}' + i\mathbf{k}'' = k_0(\nabla R + i\nabla I)$$

$$\begin{cases} \frac{d\mathbf{x}}{dt} = -\frac{\partial D / \partial \mathbf{k}'}{\partial D / \partial \omega} \\ \frac{d\mathbf{k}'}{dt} = \frac{\partial D / \partial \mathbf{x}}{\partial D / \partial \omega} \end{cases} \quad \text{Ray tracing equations}$$

Solved in cylindrical geometry  $(R, \phi, z)$ , assuming an equal (and small) time step for all rays

$$D(\mathbf{x}, \mathbf{k}', \omega) \equiv (k')^2 - \left(\frac{\omega}{c}\right)^2 [n^2 + (\nabla I)^2] = 0$$

**Dispersion relation (Hartree-Fock)**





# Block 1: Beam tracing\*

\* [ Nowak and Orefice, Phys. Plasmas 1 1242 (1994) ]

The term  $(\nabla I)^2$  introduces a 'symmetry breaking'  
also in axisymmetric configurations  $\Rightarrow \partial / \partial \varphi \neq 0$

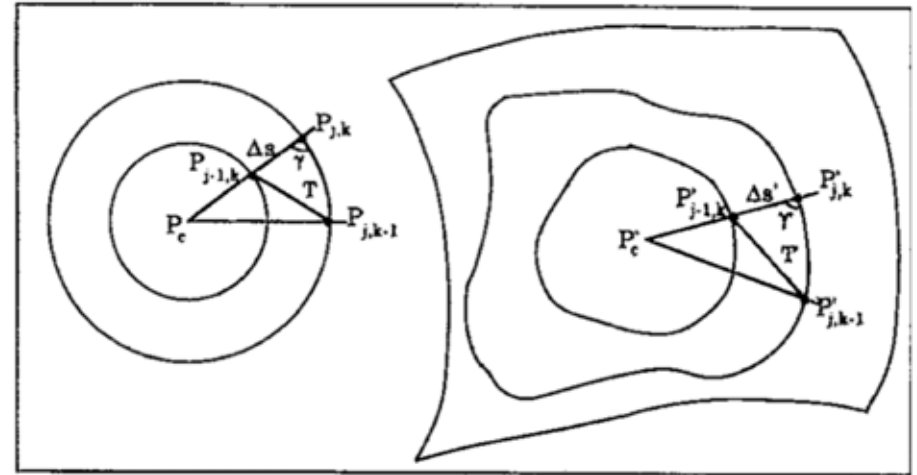
- Compute the components of  $\nabla(\nabla I)^2$  using triangulation along directions  $s_1, s_2, s_3$

From the point  $P(x, y, z) = P'_{j,k}$

$s_1$ , towards  $P_1(x_1, y_1, z_1) = P_{j,k}$  (along the ray)

$s_2$ , towards  $P_2(x_2, y_2, z_2) = P'_{j,k-1}$

$s_3$ , towards  $P_3(x_3, y_3, z_3) = P'_{j-1,k}$



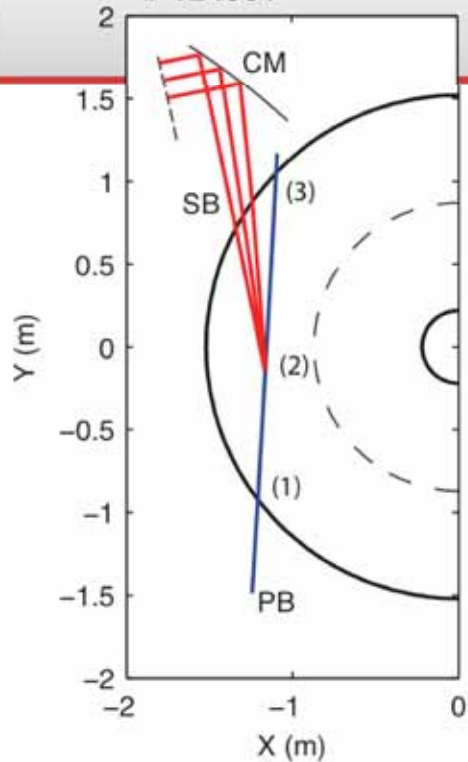
[ Fig.2 from Nowak and Orefice, Phys. Plasmas 1 1242 (1994) ]

$$\frac{d(\nabla I)^2}{ds_i} \equiv \frac{[\nabla I(P_i)]^2 - [\nabla I(P)]^2}{ds_i} = \frac{1}{ds_i} \left( d\varphi_i \frac{\partial}{\partial \varphi} + dR_i \frac{\partial}{\partial R} + dz_i \frac{\partial}{\partial z} \right) (\nabla I)^2$$

$$\left| \nabla I(P'_{j,k}) \right| = \left| \frac{1}{\sin \gamma(P_{j,k})} \frac{\partial I(P'_{j,k})}{\partial s'} \right| \quad \frac{\partial I(P'_{j,k})}{\partial s'} = \frac{\Delta s}{\Delta s'} \frac{\partial I(P_{j,k})}{\partial s}$$

# Negligible distortion of the wave front at the location of scattering

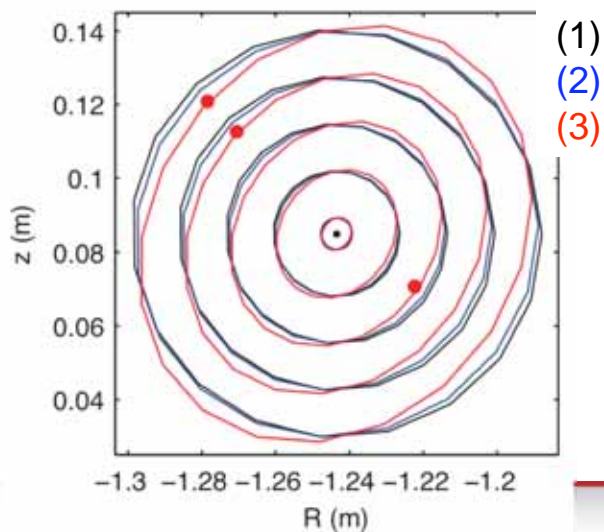
# 124901



- No appreciable spreading of the beam at the location of scattering (2) (high frequency beam)  
 => Gaussian function used as a weighting function for density fluctuations on the poloidal plane

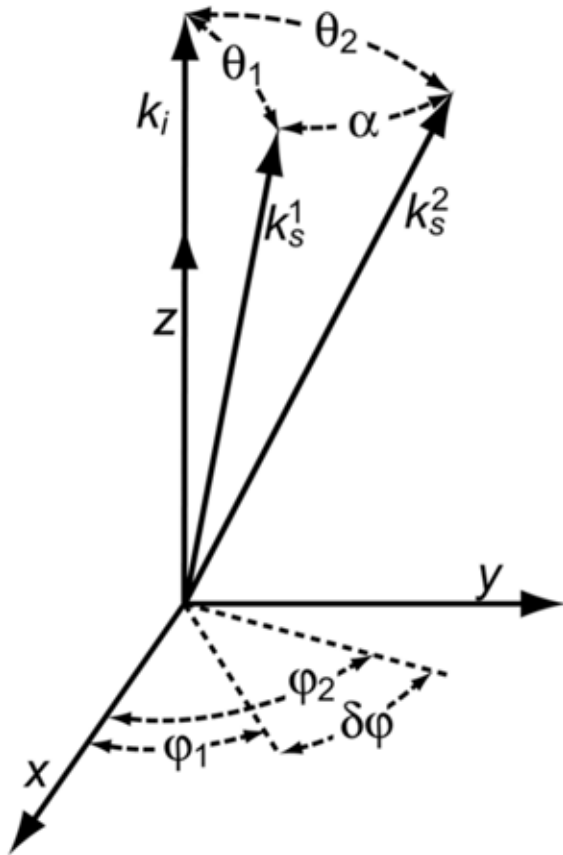
$$\int_{T'} dt' \int_V d^3 r' \mathbf{E}_i(\mathbf{r}_\perp) e^{i(\omega t' - \mathbf{k} \cdot \mathbf{r})} \tilde{n}(\mathbf{r}', t')$$

- ⇒ full beam equations not necessary for the propagation and distortion of the beam, but important for the reconstruction of the 3D Instrumental Selectivity Function and of the filtering function  $(k_r, k_\theta)$  for the simulated spectra



# The collection efficiency is optimized at tangent injection

[ E. Mazzucato, *Phys. Plasmas* 10 753 (2003) ]



$$F = \exp(-\alpha^2 / \alpha_0^2) \quad \alpha_0 = 2 / k_i a$$

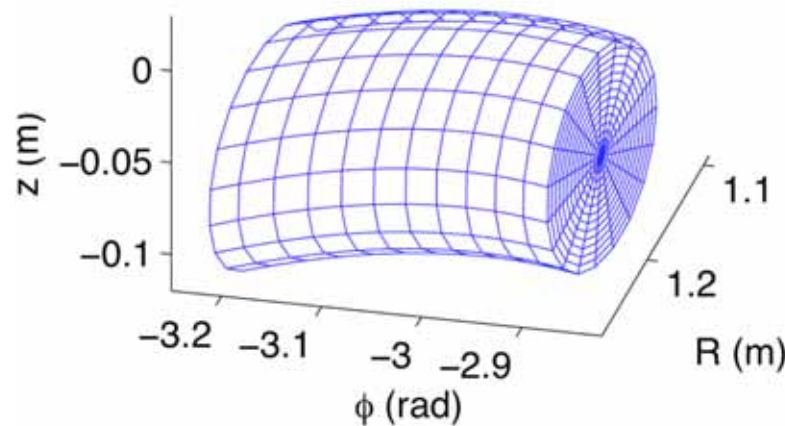
$$\alpha^2 \approx (\theta_2 - \theta_1)^2 + 4\theta_2\theta_1 \sin^2(\delta\varphi/2)$$

The collection efficiency depends on:

- the scattering angle
- direction of the magnetic field

Max efficiency for scattering along the detector line sight and for tangent injection.

# The scattering volume is highly localized in the toroidal direction

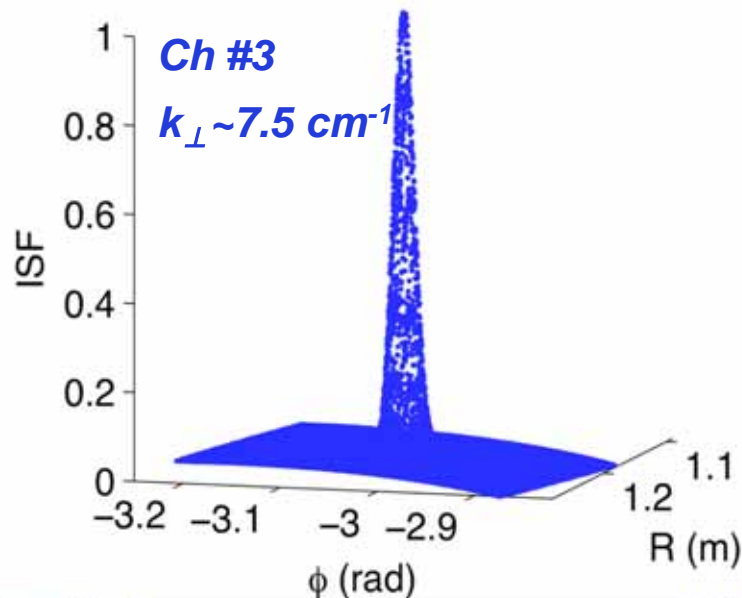


1. take a toroidal length  $L = \frac{2a}{\sin(\theta_s)}$
2. Compute the collection efficiency for all  $k_i, \theta_s$  within this volume

The Instrumental Selectivity Function (ISF) is highly localized in  $\phi$

The resolution in  $(R, z)$  is affected by the alignment of incident and scattered beam

=> Use a function for the receiving window

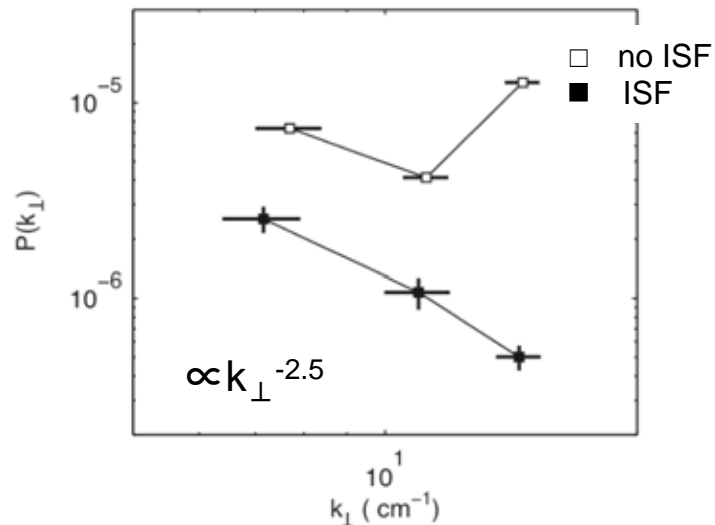
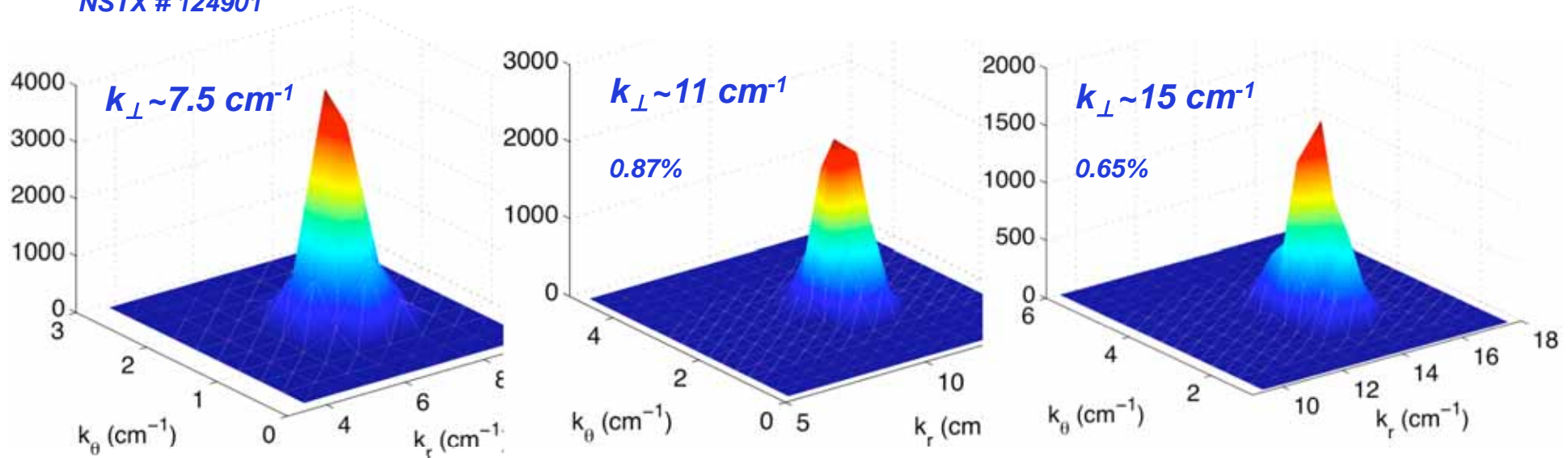


## NEXT STEP UPGRADE :

use the 3D extension of the scattering volume for the computation of spectra. Include in the interface for both GTS and GYRO

# The collection efficiency is used to reconstruct a $(k_r, k_\theta)$ filter for the simulation spectra

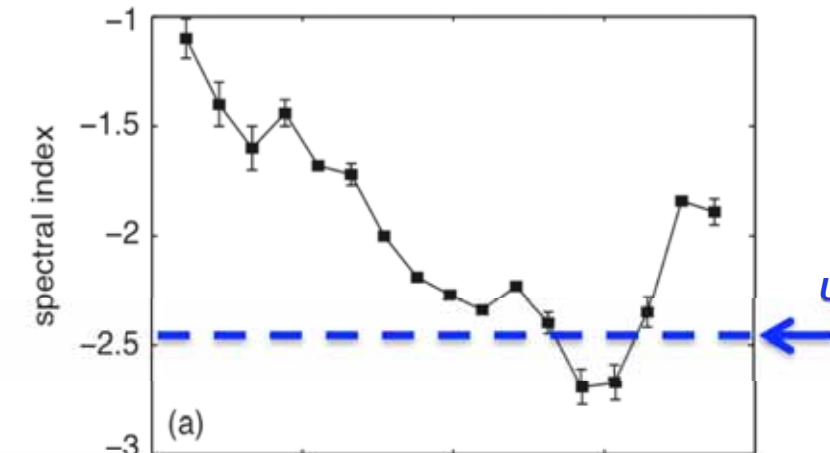
NSTX # 124901



The reconstructed  $(k_r, k_\theta)$  is important for amplitude correction of both simulated and measured spectra

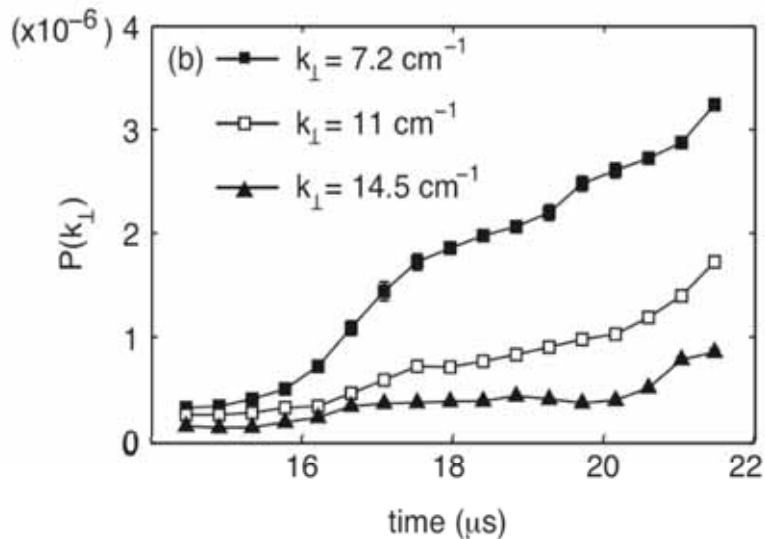
# Simulations must reach stationary phase for a meaningful comparison with experiments

From GTS simulations



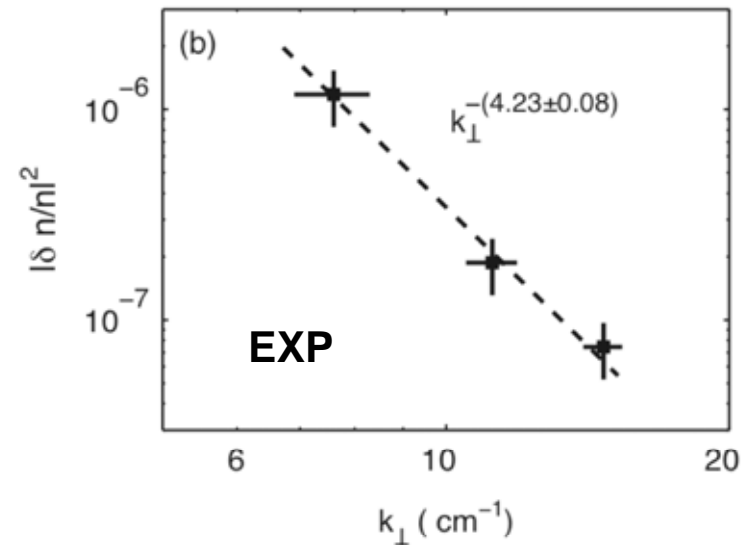
synthetic spectra become steeper  
(amplitude increases at the smallest  $k_{\perp}$ )  
But still less steep than in experiments

Using  $P(k_{\perp})$  computed at midplane



#124901

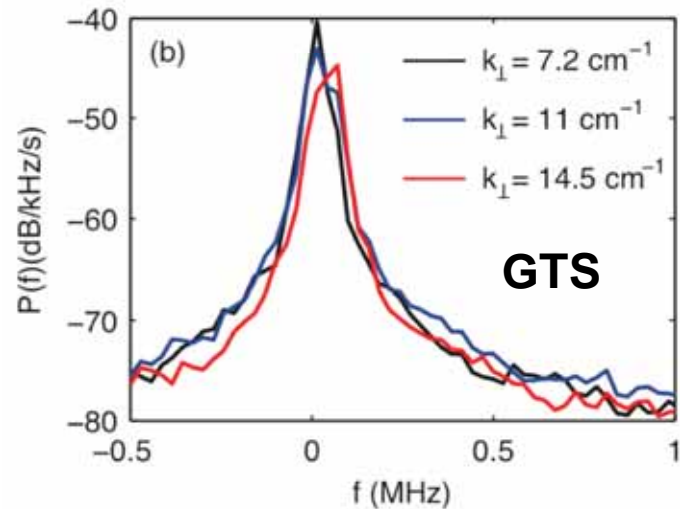
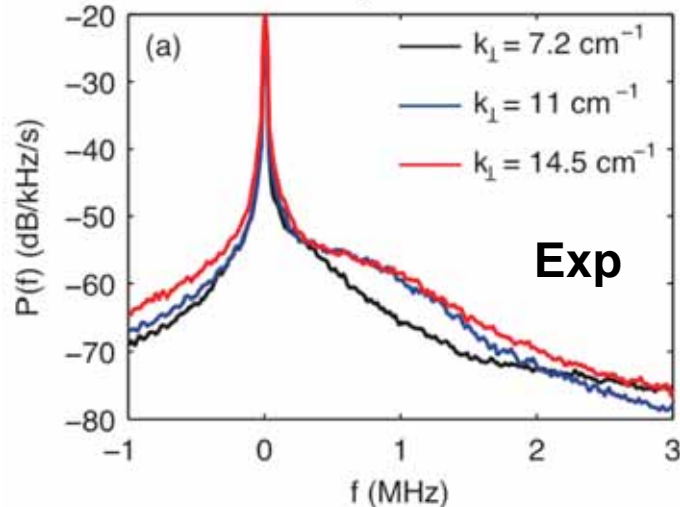
$t = 300 \text{ ms}, \Delta t = 10 \text{ ms}$



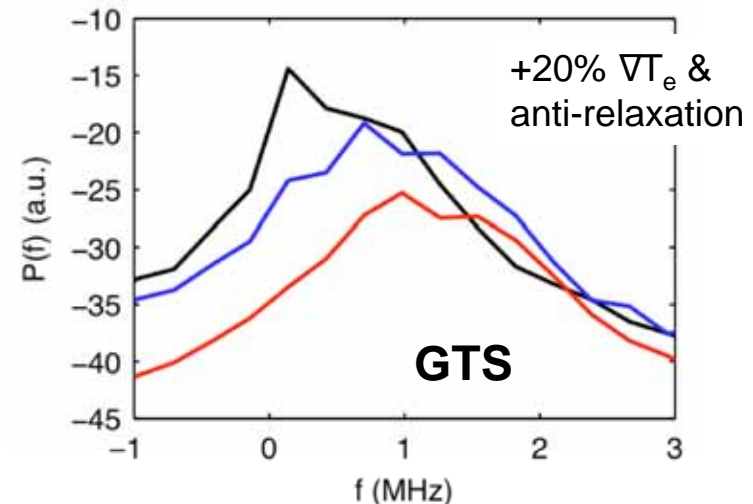
# Frequency spectra are broader in experiments

#124901

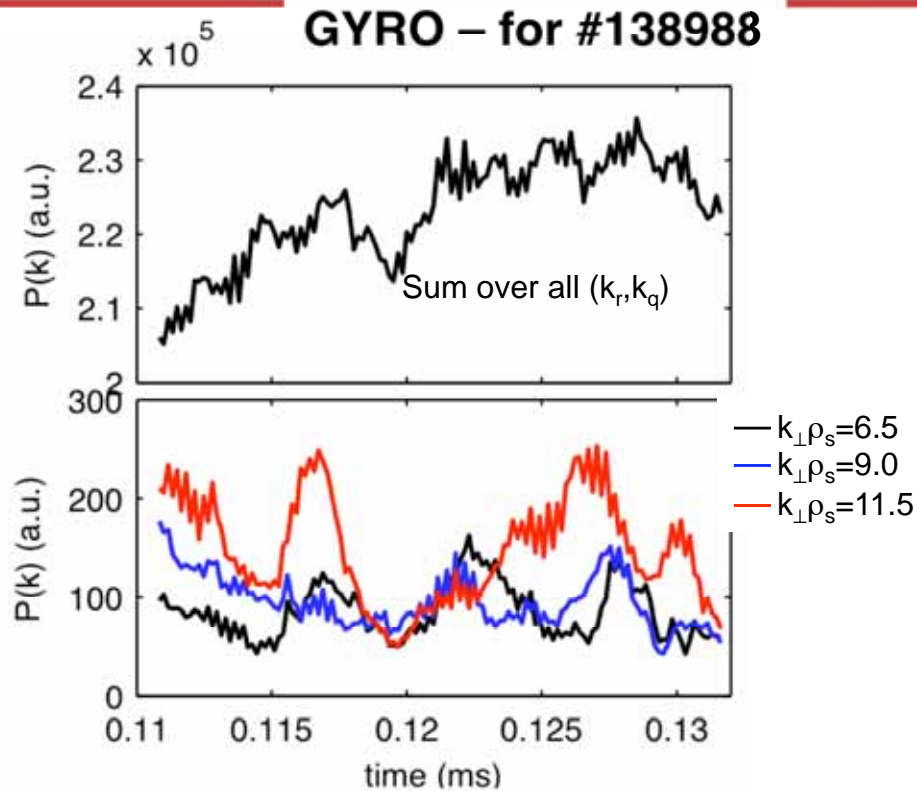
$t = 300$  ms,  $\Delta t = 10$  ms



- Peaking frequency is comparable when a Doppler shift of 500 kHz is taken into account (from rotation measurements)
- Simulated spectra are much narrower than measured spectra (left)
- Better match when  $\nabla T_e$  is increased by 20% and using an 'anti-relaxation' algorithm to maintain the gradient drive (below)



# Spectral index less steep than in experiments also in L-mode



- Level of fluctuations appears to be statistically steady
- The ISF does not affect significantly the spectral slope
- the ISF cannot reproduce the dramatic decrease in amplitude at the lowest  $k$
- Predicted ETG transport much smaller than experiment, may not be the dominant mechanism in this L-mode discharge

