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# Sensitivity to error fields in NSTX high $\beta$ plasmas

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# Abstract

It was found that error field threshold decreases for high  $\beta$  in NSTX, although the density correlation in conventional threshold scaling implies the threshold would increase since higher  $\beta$  plasmas in our study have higher plasma density. This greater sensitivity to error field in higher  $\beta$  plasmas is due to error field amplification by plasmas. When the effect of amplification is included with ideal plasma response calculations, the conventional density correlation can be restored and threshold scaling becomes more consistent with low  $\beta$  plasmas. However, it was also found that the threshold can be significantly changed depending on plasma rotation. When plasma rotation was reduced by non-resonant magnetic braking, the further increase in sensitivity to error field was observed.

(Some figures may appear in colour only in the online journal)

## 1. Introduction

Tokamaks are almost axisymmetric, but small deviations in magnetic field exist intrinsically due to imperfections in primary magnets and surrounding conductors. It is essential to control these small deviations since they can considerably change tokamak performance. One of the worst effects of non-axisymmetric *error* field is plasma locking [1–9], which often eventually causes a plasma disruption. Error field correction (EFC), therefore, typically aims at the reduction or compensation of error field using non-axisymmetric control coils, to the level below a threshold where locking may take place. Understanding of error field threshold, or often equivalently locking threshold, is thus a prerequisite for reliable EFC.

Locking is associated with magnetic islands at the rational surfaces. It is understood by the sudden opening of islands when the electromagnetic torque by error field can overcome the compensating viscous torque [10, 11], but the possible dynamics are highly complex depending on plasma parameters [12]. Nonetheless the empirical trends for error field threshold have been found in relatively simplified fashion. The most common observation is that error field threshold increases almost linearly with plasma density. Accordingly, error field has been considered as a more important topic in ohmic plasmas, which have low  $\beta$  and low plasma density and thus can be more sensitive to error field. It has also been noted that ITER

will have a long ohmic period before the flat-top of plasma currents. For these reasons, the study of error field threshold has focused on ohmic plasmas in many devices, including DIII-D [5, 9], CMOD [6], COMPASS-D [3], JET [4], MAST [7] and NSTX [8]. In recent years, however, error field threshold in high  $\beta$  plasmas also becomes an important issue, along with new predictions for large plasma amplification of error field in high  $\beta$  plasmas.

Understanding of error field physics has been significantly improved these days, especially on the effects of plasma response to error field [13–16]. It has been shown that plasma response can largely change the field penetration by distorting the spectrum of error field and also by changing the amplitude of error field. The change in the field amplitude is expected to be large especially in high  $\beta$  plasmas through their greater amplification of the externally given magnetic field [16, 17]. That is, the actual driving field of locking can be higher than the external field, and thus the favourable density scaling in high density can be degraded and becomes unfavourable by increased  $\beta \propto nT$ . Therefore, the study of error field threshold should be extended and thoroughly investigated in high  $\beta$ plasmas as well as in low  $\beta$  plasmas.

One important question prior to the study is if error field threshold in high  $\beta$ , which often includes significant input torques by axillary heating, can be defined in the same way for low  $\beta$  and ohmic plasmas. In ohmic plasmas, error



**Figure 1.** Example of profile evolutions of (*a*) electron temperature and (*b*) toroidal rotation, during locking by external field in NSTX high  $\beta$  plasmas. One can see the temperature flattening and the rotation decrease at the q = 2/1 surface when time approaches an actual locking ~550 ms. These measurements imply that the (*m*, *n*) = (2, 1) resonant field driving islands should also be the primary measure of error field threshold.

field threshold is defined as a critical amplitude in the nonaxisymmetric components of the magnetic field to produce locking. Since many observations indicate that locking occurs by (m, n) = (2, 1) islands at the q = 2/1 resonant surface [3–8], the resonant field  $\delta B_{21}$  driving (2, 1) magnetic islands naturally becomes the measure of threshold. This is a strong reduction of complexity in error field study, from the fully three-dimensional nature of non-axisymmetric magnetic field to a mere scalar quantity [9]. The relevance of this method in high  $\beta$  should be considered, by investigating the main cause of disruption in the presence of error field.

This study found that error field can disrupt high  $\beta$  plasmas with certain threshold. Large n = 1 signals were always observed before disruptions and thus n = 1 MHD events were obviously involved. This is not by unstable kink or resistive wall mode (RWM) [18–20], as  $\beta_N$  in this study was not high enough to reach the no-wall stability limit. Our speculation is that this is by locking at the q = 2/1 resonant surface, similar to ohmic plasmas, since the evolution of electron temperature and rotation profiles indicate island opening at q = 2/1. Figure 1 is an example, as one can see the temperature flattening at the q = 2/1 surface, and more evidently, the rotation decreases and is almost locked to the frame of external error field at the q = 2/1 surface.

This clear picture was in fact not always easy to see in our experiments, due to the short period of time between locking and disruption compared with time resolution in CHERS and TS measurements, and also due to injected toroidal torques by NBI. Injected torques enable plasmas to maintain larger shielding currents, but islands would be bigger when they open due to large shielding currents. Note in general that an island size at q = m/n is proportional to  $\sqrt{\delta B_{mn}}$ , where the resonant field  $\delta B_{mn}$  driving the island is proportional to dissipated shielding currents. If (2, 1) islands are big enough to reach adjacent n = 1 rational surfaces, they can affect other (m > 2, n = 1) islands as soon as they open and thus possibly cause the wide collapse of temperature profiles in the region q > 2, as occasionally found in our study. Also in this case, rotation can be more resilient to a change due to injected torques and begin to collapse from the outside where injected torques are relatively small. In such cases, it is not clear what causes the collapse of discharges. However, this paper will assume that (2, 1) islands are still the fundamental



**Figure 2.** An example of reconstructed target equilibria in NSTX using LRDFIT (LR circuit model with Data FITting capabilities), which gives a reconstructed Grad–Shafranov equilibrium constrained by magnetic measurements, MSE,  $T_e$ -isoflux and toroidal rotation, including vessel eddy current effects [22]. The poloidal locations of EFC coils are shown on the left in 2D and on the right in 3D. EFC coils are all located at the midplane. There are six coils along the toroidal direction and the n = 1 field can be produced with almost an arbitrary toroidal phase.

drive of locking and disruption, based on many other examples, as illustrated in figure 1, and therefore error field threshold will be defined consistently across low  $\beta$  and high  $\beta$  plasmas.

The rest of the paper is organized as follows. Section 2 will describe experimental details and observations, which show clearly the increased sensitivity of plasmas to error field in higher  $\beta$ . Section 3 will describe ideal plasma calculations to explain experiments and will demonstrate the successful scaling of error field threshold across low  $\beta$  and high  $\beta$  plasmas. Section 4 will discuss the effects of plasma rotation on error field threshold and section 5 will summarize the paper.

# **2.** Experiment: error field application to high-beta NSTX plasmas

This study targeted the strongly shaped and high  $\beta$  plasmas in NSTX, as shown in figure 2. Plasmas are diverted with a lower single null with the aspect ratio  $A \sim 1.4$ , the elongation



**Figure 3.** Time trace of typical locking experiments in this study, including each (*a*) plasma current, (*b*)  $\beta_N$ , (*c*) electron density, (*d*) n = 1 signal and (*e*) applied currents for n = 1 field. The black traces are for the reference discharge, and the red and blue traces are for the low  $\beta_N \sim 3$  and the high  $\beta_N \sim 4$ , respectively. One can see the smaller threshold for the higher  $\beta_N$ , as indicated by dotted lines at the time of locking.

 $\kappa \sim 2.3$ , the triangularity  $\delta_{up} \sim 0.4$  and  $\delta_{down} \sim 0.8$ , the safety factor  $q_{95} = 8 \sim 10$  and the plasma  $\beta_N = 3 \sim 4 < \beta_{N,no-wall}$ . The n = 1 error field is produced by the 6-toroidal array of EFC [8, 21] coils at the midplane as shown in the 2D and 3D schematics in figure 2. By changing currents in EFC coils, one can measure the critical amplitude and the threshold at locking.

Error field threshold can be studied either by changing applied coil currents, as carried out in our study, or by changing plasma parameters while holding the applied coil currents. In fact, none of these methods is perfect in NSTX high  $\beta$  targets due to continuous change of several plasma parameters such as plasma density and also due to dynamic change of the intrinsic error field [8]. The change in coil currents are faster than the changes in parameters and intrinsic errors during the flat-top, but it is still necessary to estimate each dynamic parameter at each time just before locking. The effects of intrinsic errors are small but not ignorable, as will be illustrated later.

Figure 3 shows a typical sequence of our experiments in time. The same plasma current in (a),  $I_{\rm P} = 900 \, \rm kA$ , is maintained, resulting in approximately the same plasma density evolution in (c) for all three shots. One can see the plasma locking in (d) when the n = 1 EFC coil currents in (e) are increased up to each threshold, as seen in shots marked by red and blue. An important observation in these experiments is the change in the threshold, depending on  $\beta_N$ . The  $\beta_N$  is the critical parameter for plasma stability, and so for plasma responses. The  $\beta_{\rm N}$  in (b) is produced differently in experiments by differing NBI power, for example, 3 MW for black and blue traces and 2 MW for red traces. One can see clearly from the blue traces that the threshold is reduced and thus locking occurs earlier for higher  $\beta_N$ . This trend, as summarized in figure 4, has been observed in JET experiments [4] and also in recent DIII-D experiments. The greater sensitivity of plasmas to error field has been predicted in fact theoretically [17]



**Figure 4.** Summary of experimental observations for the error field threshold in external currents versus  $\beta_N$ . One can find the greater sensitivity of plasmas to higher- $\beta_N$  plasmas.

by resonant field amplification (RFA), which describes the increase in the plasma response when plasma approaches a marginal stability,  $\beta_N \rightarrow \beta_{N,marginal}$ . Note again that our experiments are designed not to hit the actual marginal limit, since then RWM can play an important role.

Results imply that plasma response becomes stronger for higher  $\beta_N$ , and thus the lower external field is required to produce the same electromagnetic torque. On the other hand, the compensating mechanism against the electromagnetic torque arises through the viscous torque, which is tightly associated with the rotation but empirically seems to appear as the positive density correlation. So empirically, the higher external threshold is expected for the higher plasma density, which is typically accompanied with higher  $\beta_N$ plasmas. However, this prediction fails due to plasma response effects. Figure 5 shows the external current threshold versus



**Figure 5.** Summary of locking threshold measurements in external currents versus density for NBI-heated high  $\beta$  cases (red circles) as well as ohmic plasma cases (black diamonds). The linear density correlation in ohmic plasmas is no longer valid for high  $\beta$  plasmas when the external measures are used.

the line-averaged plasma density, combining previous ohmic experiments (black diamonds) and present high  $\beta$  experiments (red circles). One can see the almost linear correlation for ohmic experiments, but the correlation is no longer valid for high  $\beta$  cases. In fact, one can see the opposite correlation for high  $\beta$  cases roughly as well as the large discrepancy between ohmic cases [8] and high  $\beta$  cases. It is found that the linear correlation can be restored if the total resonant field including plasma response is used for threshold instead of external current or external resonant field, as will be discussed in detail later.

It is also worth mentioning that there are some effects of intrinsic error field in our experiments. In most of the shots, the toroidal phase of EFC currents is designed to be approximately aligned with the intrinsic error field, to reduce the currents we need to apply. In order to ensure this, several shots used the opposite toroidal phase of EFC currents, as shown in figure 6. One can see the blue traces caused locking later with larger threshold, which implies in this case that the applied field is compensating intrinsic error field. The difference in FEC currents is about  $\sim 200 \text{ A}$ , and thus the effects of intrinsic error field in our experiments are 10-20%.

Another set of experiments was designed to study the role of plasma rotation, which can be directly measured by CHERS in NBI-heated plasmas, unlike ohmic plasmas. We used magnetic braking to change rotation, as the n = 3components of 3D fields can be produced independently of the n = 1 components. Plasmas with a braking may not be identical to plasmas without a braking even if the same rotation profile is achieved, but our experiments ignored such possible differences. A typical example is shown in figure 7. Three different shots represent a reference (black), a shot with only the n = 1 (red) and a shot with the n = 1 and n = 3 fields (blue). Almost identical conditions, as shown in (a) plasma currents and (b) densities, are produced except (c) rotations, by utilizing different 3D fields with (e) the n = 1 and (f) the n = 3 to find different thresholds in (d). In the shot with the n = 3 braking (blue), one can see the lower level of rotation

was maintained. As a result, the locking threshold measured by the n = 1 currents becomes lower, by a factor of 2 in this case.

The positive correlation between the threshold and the rotation, illustrated in figure 7, can be easily predicted by theory as the rotation would increase viscous torque compensating against electromagnetic torque. However, it has been rather implicit in the traditional locking scaling due to difficulties in measuring the rotation profile evolutions in ohmic plasmas, during a short period of time during the locking process. Instead, the correlation with the density has been used since it appears to be very strong and robust. This density correlation is not yet fully resolved in the theory. Only a theory by Cole showed a possible role of neoclassical toroidal viscosity (NTV) [23] since then the linear density scaling could be obtained. The validation of this theory remains as future work. The primary focus of this paper is on the role of plasma response to explain ohmic and high  $\beta$  results consistently, with a conventional scaling such as the density scaling, but the effect of rotation on error field threshold is obvious, as seen in figure 7, and cannot be ignored.

#### 3. Theory: amplification through plasma coupling

Error fields produce plasma response along with perturbed plasma currents, which often largely distort field penetration. Therefore, plasma response should be considered to determine actual resonant field driving islands and locking. Plasma response is important even in ohmic plasmas as found in NSTX and DIII-D [9, 13, 14], but perhaps plays a more important role in high  $\beta$  plasmas due to larger amplification of the field. Figure 4 already implies the importance of plasma response and amplification, as it can be understood that the threshold decreases because plasma approaches the marginal  $\beta_N$  limit and thus plasma response increases.

When one studies the error field threshold including plasma response effects, one needs to define a field component that can relevantly describe or dominate locking dynamics. It has been traditional to define this as the 2/1 resonant component,  $\delta B_{21}$ , since locking mostly appears to be directly related to magnetic island activities at the q = 2/1 surface, as discussed in the introduction, and  $\delta B_{21}$  determines the size of magnetic islands. One can calculate this in terms of external (vacuum) field,  $\delta B_{21}^x$  by ignoring plasma response and assuming a full penetration, or one can calculate this by including perturbed plasma current effects,  $\delta B_{21} = \delta B_{21}^x + \delta B_{21}^p$ . As shown in previous work [9, 14], the external resonant field  $\delta B_{21}$  often fails, and the total resonant field  $\delta B_{21}$  with ideal plasma response better addresses locking physics and experimental observations.

Figure 8 is a revision of figure 5, using the total resonant fields calculated by the Ideal Perturbed Equilibrium Code (IPEC) [25], instead of external currents or external fields. Compared with figure 5, the difficulty of observing any correlation in terms of external currents can be resolved, as the linear correlation appears again consistently for both ohmic and NBI-heated plasmas. This resolution comes from plasma amplifications by a factor of 2–3 in high density and high  $\beta$  plasmas, as briefly reported in a recent NSTX overview paper [24]. Note that these calculations of total resonant fields included the contributions from the intrinsic error field



**Figure 6.** Time trace of locking experiments indicating the intrinsic error field, including each (*a*) plasma current, (*b*)  $\beta_N$ , (*c*) electron density, (*d*) n = 1 signal and (*e*) applied currents for n = 1 field. The field in the blue traces is identical but different by 180° toroidal phase, compared with the red traces. The large threshold in the blue traces implies that the intrinsic error field exists and is compensated by the applied field.



**Figure 7.** Time trace of locking experiments with the n = 3 rotation braking, including each (*a*) plasma current, (*b*)  $\beta_N$ , (*c*) electron density, (*d*) n = 1 signal, (*e*) applied currents for n = 1 field and (*f*) applied currents for n = 3 field. The black traces are for the reference discharge, and the red and blue traces are for the high  $\beta$  discharges but only the blue traces have the n = 3 braking and thus different rotation. One can see the increased sensitivity when rotation is low.

by the centre-stack distortion and PF5 non-circularity. These contributions are not significant, but are also not ignorable, as demonstrated in figure 6.

The actual scaling of error field threshold should include other parameters as well as the density. Previous work has shown the strong correlation with plasma density  $n_e$ , toroidal field  $B_{T0}$ , and major radius  $R_0$  [3–6, 8]. Many global parameters were investigated, and this study also found  $n_e$  and  $B_{T0}$  are the most important variables. The major radius is not relevant here since experiments are limited in NSTX configuration, but it is still important to ensure that our scaling is dimensionless and independent of size. Based on the Connor–Taylor invariance [26],  $n_e R_0^2$  and  $B_{T0} R_0^{5/4}$  are used for scaling instead of merely  $n_e$  and  $B_{T0}$ .



**Figure 8.** Revision of figure 5, using total resonant fields at the q = 2/1 surface instead of external currents. The Ideal Perturbed Equilibrium Code (IPEC) is used for these calculations. One can see that the density correlation is now restored consistently for both ohmic and NBI-heated plasmas. This is due to large plasma amplifications in high  $\beta$  plasmas as briefly reported by figure 3, in a recent NSTX overview paper [24].

In NSTX, there exists an additional parameter showing significant correlation. It is the shear in *q*-profiles, and this scaling has already been found in a previous study for NSTX ohmic plasmas [8]. This *q*-shear is in fact very natural if one notes the size of magnetic islands is inversely proportional to  $dq/d\psi$ . Since higher fields are required to open the same size of islands when the  $dq/d\psi$  is higher, so the positive correlation in the threshold is naturally expected, as found in the previous study. The *q*-shear scaling has not been clearly shown in other studies and devices, but it is possibly due to the limited range of the *q*-profiles in experiments. In fact, DIII-D has reported the different scaling for different  $q_{95}$ 's, although sometimes the effects of *q*-profiles were not clearly separable from  $B_{T0}$  [9].

Resulting scaling is presented in figure 9. One can see that ohmic (black diamonds) and high  $\beta$  (red circles) results are well combined by one scaling with reasonably small deviations, which are not found when the external resonant fields are used. Including proportional factors, error field threshold in NSTX is given by

$$\left(\frac{\delta B_{21}}{B_{\rm T0}}\right) \cong 2.2 \times 10^{-4} n_{\rm e}^{0.60} B_{\rm T0}^{0.45} s^{0.76} R_0^{1.74},\tag{1}$$

where the shear is defined as  $s \equiv dq/d\rho$  at q = 2/1, with the  $\rho \equiv \sqrt{\psi_{\rm N}}$ . The density correlation is weaker quite significantly than the linear correlation when including high  $\beta$  cases, and this aspect will be discussed in the next section. One can also compare this with the previous ohmic results,  $\delta B_{21}/B_{\rm T0} \propto n_{\rm e}^{0.88} B_{\rm T0}^{0.23} s^{0.79}$  in [8], where the density correlation is closer to the linear correlation. The major radius scaling appears to be strong, but here this is just the result of a Connor–Taylor constraint and should not be taken as a robust parameter.



**Figure 9.** Error field threshold scaling by the total resonant fields including ohmic (black diamonds) and high  $\beta$  (red circles) cases. One can see that the correlation is improved from figure 8 by including additional parameters such as  $B_{T0}$  and the shear at the q = 2/1 surface, *s*. Note that the density correlation becomes weaker than ohmic plasmas.

### 4. Discussion: effects of plasma rotation

The weaker density correlation can be understood as a result of the additional drive of the torque in high  $\beta$  cases due to NBI heating. In fact, one may argue that it would result in the threshold increase rather than the decrease in the same density, since the additional torque drive should be compensating to error field. However, the decrease for the density power index may imply that our NBI heating is slightly more effective at increasing the density rather than the torque or the rotation. The density increases by up to a factor of ~10 compared with ohmic plasmas, and indeed the rotation increase by a factor of ~10 from ohmic to high  $\beta$  plasmas is unlikely.

The rotation is a more attractive parameter than the density for scaling, by its direct implication on the viscous torque. However, the experimental information for the rotation is available only for NBI-heated cases. Also, effects of the rotation and density are not clearly separable, and the interlink between the two parameters are not that simple since their contributions to the electromagnetic torque or the viscous torque are coupled [12]. It is found when both the rotation and density are included simultaneously, their effects are largely duplicated and the regression analysis is performed with illconditions. Therefore, our approach is to hold the scaling in figure 9, but to consider effects of rotation as a correction. For a dimensionless variable, the ratio of the toroidal rotation to the diamagnetic rotation at the q = 2/1 is chosen.

Figure 10 shows the resulting scaling in high  $\beta$  cases, with the rotation as a correction. Although the standard deviations are increased, it represents well high  $\beta$  experiments with and without magnetic braking. With the proportional factors, the error field threshold in NSTX high  $\beta$  cases is given by

$$\left(\frac{\delta B_{21}}{B_{\rm T0}}\right)_{\omega} \cong \left(\frac{\delta B_{21}}{B_{\rm T0}}\right) \times \left(0.22\frac{\omega_{\phi}}{\omega_{\rm D}}\right)^{1.46}.$$
 (2)



**Figure 10.** Error field threshold scaling with the rotation, including high  $\beta$  cases with (blue squares) and without (red circles) magnetic braking. The correlation between the field threshold and the rotation is strong as expected.

The correlation with the rotation is strong as expected, and indicates that the error field sensitivity would increase faster than the linear when the rotation decreases. The proportional factor 0.22 is interesting, since this implies that the scaling without magnetic braking in figure 9 can be restored if  $\omega_{\phi} \sim 4.5 \times \omega_{\rm D}$ . That is, equations (1) and (2) can be consistent when the actual rotation is higher than  $\omega_{\rm D}$  by a factor of 4–5.

# 5. Summary

This paper presented various n = 1 locking experiments in NSTX high  $\beta$  plasmas, with and without n = 3 magnetic braking. It is shown that plasmas have the greater sensitivity in higher  $\beta$  plasmas due to plasma amplification. Error field threshold becomes lower, which is seemingly inconsistent with ohmic threshold scaling, which predicts the higher threshold in high density and high  $\beta$ . This can be resolved by considering the total resonant field including plasma response and amplification, and the resulting scaling becomes consistent for both ohmic and high  $\beta$  plasmas. The sensitivity can be greater if the rotation is decreased by reducing input torques by magnetic braking. The strong correlation is indeed found between the error field threshold and the rotation as predicted. Resulting scaling may be helpful for ITER, but the actual extrapolation to ITER is not discussed here since the extrapolation will be more relevant when these data are combined with other tokamaks, as planned for future work. Nevertheless, this scaling will be useful specifically for Spherical Torus (ST) including future devices such as NSTX-Upgrade.

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#### References

- [1] Hender T.C. et al 1992 Nucl. Fusion 32 2091
- [2] La Haye R.J., Fitzpatrick R., Hender T.C., Morris A.W.,
- Scoville J.T. and Todd T.N. 1992 *Phys. Fluids* B 4 2098
  [3] Buttery R.J. *et al*, the JET Team, the COMPASS-D Research Team and the DIII-D Team 1999 *Nucl. Fusion* 39 1827
- [4] Buttery R.J., Benedetti M.D., Hender T.C. and Tubbing B.J.D. 2000 Nucl. Fusion 40 807
- [5] Scoville J.T. and LaHaye R.J. 2003 Nucl. Fusion 43 250
- [6] Wolfe S.M. et al 2005 Phys. Plasmas 12 056110
- [7] Howell D.F., Hender T.C. and Cunningham G. 2007 Nucl. Fusion 47 1336
- [8] Menard J.E. et al and the NSTX Research Team 2010 Nucl. Fusion 50 045008
- [9] Park J.-K., Schaffer M.J., La Haye R.J., Scoville T.J. and Menard J.E. 2011 Nucl. Fusion 51 023003
- [10] Fitzpatrick R. and Hender T.C. 1991 Phys. Fluids B 3 644
- [11] Fitzpatrick R. 1993 Nucl. Fusion 33 1049
- [12] Cole A.J. and Fitzpatrick R. 2006 Phys. Plasmas 13 032503
- [13] Park J.-K., Schaffer M.J., Menard J.E. and Boozer A.H. 2007 Phys. Rev. Lett. 99 195003
- [14] Park J.-K., Boozer A.H., Menard J.E., Garofalo A.M., Schaffer M.J., Hawryluk R.J., Kaye S.M., Gerhardt S.P., Sabbagh S.A. and the NSTX team 2009 *Phys. Plasmas* 16 056115
- [15] Reimerdes H. et al 2009 Nucl. Fusion 49 115001
- [16] Lanctot M.J. et al 2010 Phys. Plasmas 17 030701
- [17] Boozer A.H. 2001 Phys. Rev. Lett. 86 5059
- [18] Sontag A.C. et al 2005 Phys. Plasmas 12 056112
- [19] Sabbagh S.A. 2006 Nucl. Fusion 46 635
- [20] Sontag A. 2007 Nucl. Fusion 47 1005
- [21] Bell M.G. et al and the NSTX team 2006 Nucl. Fusion 46 \$565
- [22] Menard J.E. et al 2006 Phys. Rev. Lett. 97 095002
- [23] Cole A.J., Hegna C.C. and Callen J.D. 2007 Phys. Rev. Lett. 99 065001
- [24] Raman R. et al 2011 Nucl. Fusion 51 094011
- [25] Park J.-K., Boozer A.H. and Glasser A.H. 2007 Phys. Plasmas 14 052110
- [26] Connor J.W. and Hastie R.J. 1973 Nucl. Fusion 13 221