

To validate TGLF against GYRO, need to ensure identical model assumptions and inputs

- For comprehensive gyrokinetic analysis, we usually run GYRO with:
 - Profiles from TRANSP Plasma State files, three species (D,C,e), electron collisions (pitch angle scattering), general numerical equilibrium (from EFIT), fully EM ($A_{||}$, $B_{||}$), no MHD approximation (finite ∇P_{eq} , $\nabla B/B \neq \kappa$)
 - Typically ignore toroidal flow for linear runs ($Ma=\gamma_p=\gamma_E=0$) unless investigating quasi-linear momentum transport
- The TGLF default is slightly different:
 - Miller geometry, EM with $A_{||}$ only, MHD approximation (finite ∇P_{eq} but $\nabla B/B=\kappa$)
- To ensure identical model assumptions we have used TGLF default model for GYRO as well
 - Also need to ensure same ∇P_{eq} is used in both (typically sum of thermal species only, but can also include contribution from fast ion/beam species)
- Have double checked out.gyro.run and out.tglf.localdump to verify identical input parameters

NSTX test cases

- In NSTX H-mode discharges, any and all of the following micro-instabilities can be unstable at different regions, simultaneously: ITG, TEM, ETG, KBM, microtearing
→ challenges any reduced model
- To start, focus on cases expected to be dominated mostly by one instability
 - [Ref. 1] L-mode discharge (ITG) – NSTX 141761
 $I_p=0.9$ MA, $B_T=0.55$ T, $P_{\text{NBI}}=2$ MW
 - [Ref. 2] “Low” beta H-mode discharge (ETG) – NSTX 141031/141040
 $I_p=$, $B_T=$, $P_{\text{NBI}}=3$ MW
 - [Ref. 3] “High” beta H-mode discharge (microtearing) – NSTX 120968/138564
 $I_p=0.7$ MA, $B_T=0.35$ T, $P_{\text{NBI}}=4$ MW
 - [Ref. 4] NSTX-U scenario – 142301 (?)
 $I_p=$, $B_T=$, $P_{\text{NBI}}=6$ MW

[1] Y. Ren et al., IAEA (2012), Nucl. Fusion (2013)

[2] Y. Ren et al., Phys. Plasmas (2012)

[3] W. Guttenfelder et al., Phys. Rev. Lett. (2011)

[4] S.P. Gerhardt et al., Nucl. Fusion (2012)

NSTX L-mode at relatively low beta

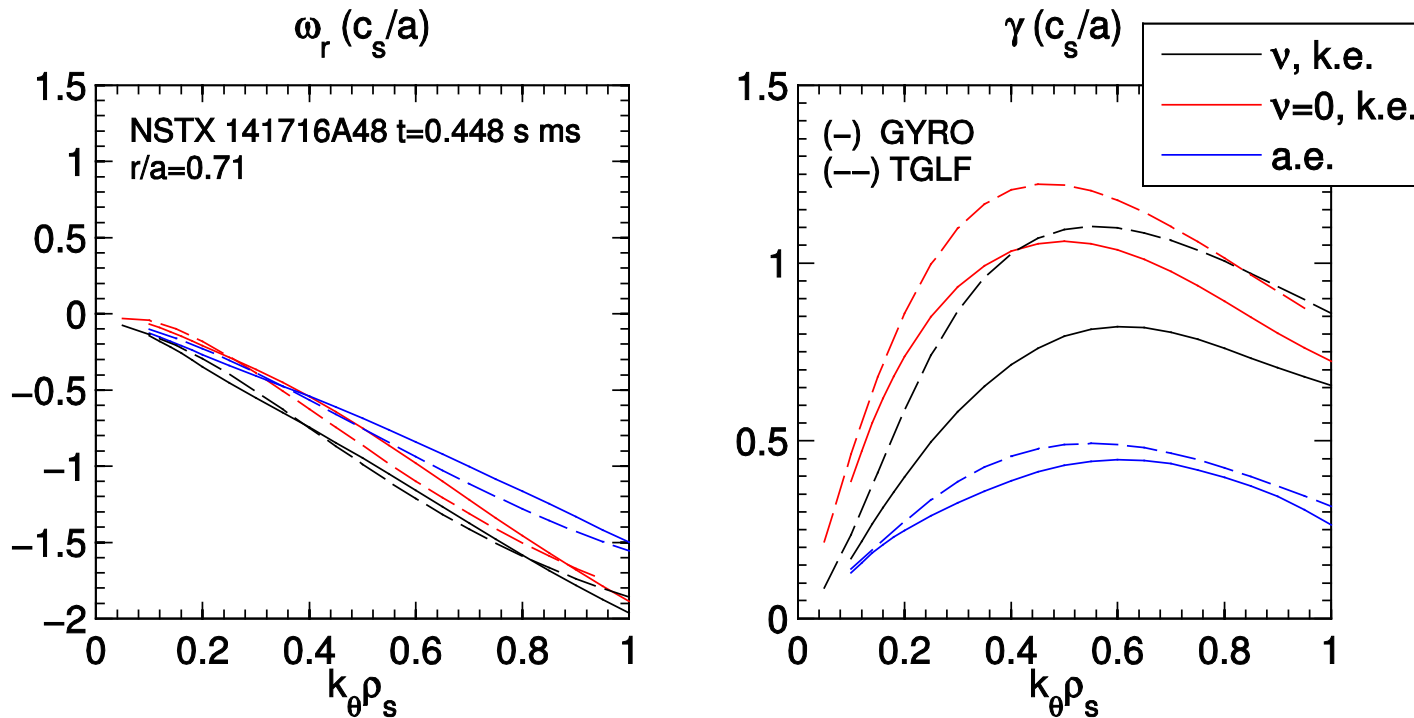
- Shaping not very extreme (local surface shape $\kappa=1.5$, $\delta=0.1$)
- Biggest difference to DIII-D is aspect ratio ($R/a < 1.5$) and higher $v_{ei} \cdot a/c_s \sim 0.4-2.9$

r/a	q	s	T_e/T_i	a/L_{Ti}	a/L_{Te}	a/L_{ne}	Z_{eff}	v_{ei}	β_e (%)	γ_E	γ_p	Ma	α_{MHD}
0.6	1.39	0.89	0.89	4.68	5.17	3.47	1.19	0.39	0.586	0.77	2.57	0.47	0.46
0.66	1.55	1.45	0.90	6.82	5.98	3.03	1.19	0.61	0.312	0.59	2.00	0.40	0.31
0.71	1.77	2.30	0.94	6.83	6.35	1.60	1.15	0.99	0.184	0.35	1.22	0.37	0.20
0.76	2.15	3.49	0.95	7.00	6.94	1.63	1.15	1.75	0.104	0.24	0.95	0.38	0.16
0.8	2.64	4.65	0.96	8.46	7.94	2.55	1.15	2.86	0.060	0.25	1.16	0.39	0.15

r/a	R/a	Z/a	κ	δ	ζ	dR/dr	dZ/dr	s_κ	s_δ	s_ζ
0.6	1.449	0.008	1.542	0.090	-0.013	-0.267	-0.001	-0.023	0.036	-0.027
0.66	1.432	0.008	1.540	0.094	-0.015	-0.286	-0.001	0.002	0.049	-0.029
0.71	1.417	0.008	1.542	0.099	-0.017	-0.312	-0.002	0.029	0.078	-0.025
0.76	1.401	0.008	1.547	0.106	-0.019	-0.351	-0.002	0.073	0.140	-0.017
0.8	1.386	0.008	1.555	0.115	-0.019	-0.392	-0.003	0.129	0.229	-0.002

Using identical models with collisions ($v_{ei}=0.99 c_s/a$) TGLF predicts growth rates ~35% larger than GYRO

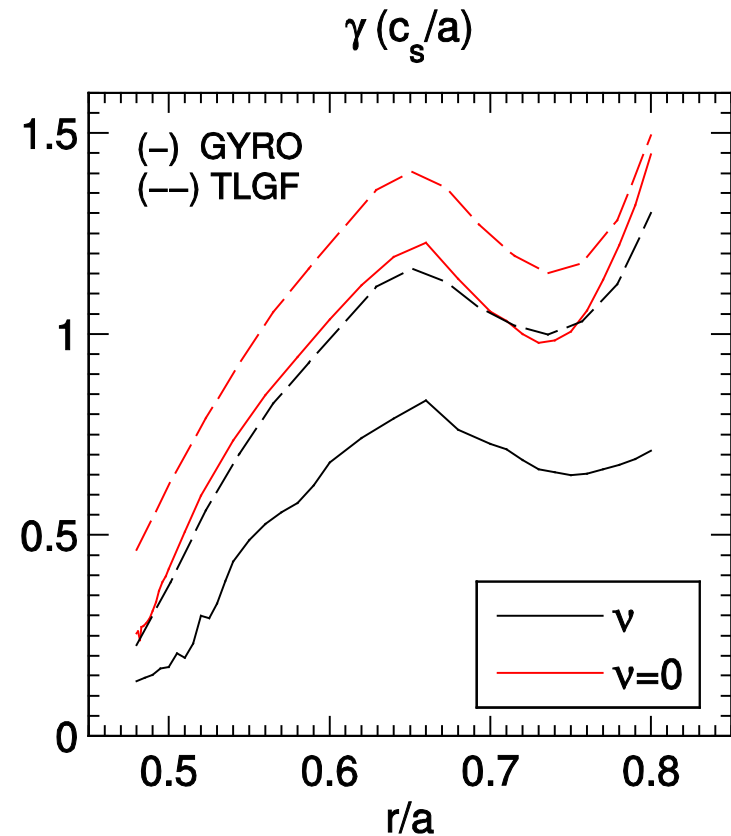
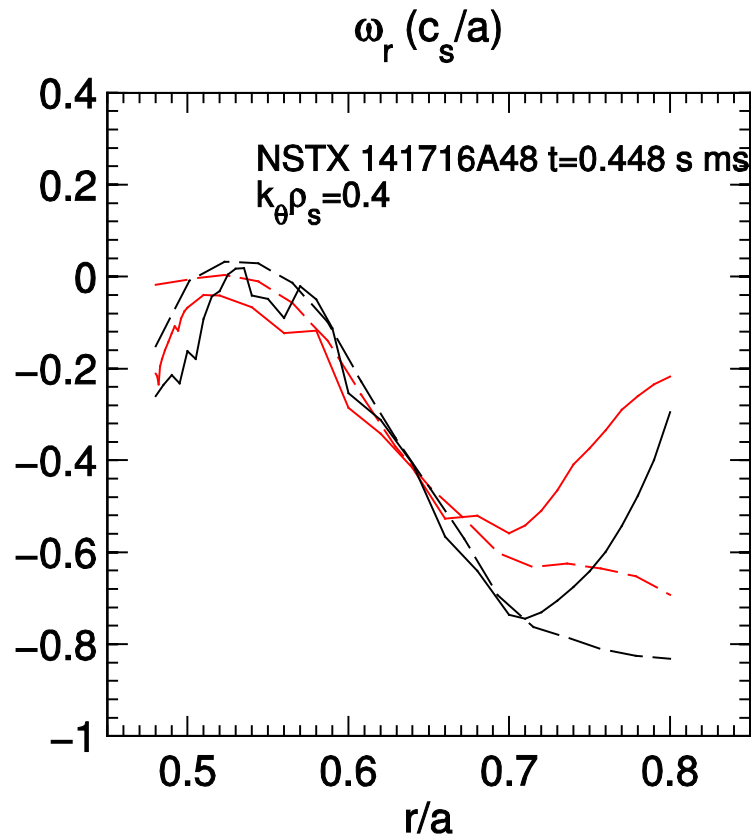
- Miller, ES (EM effects negligible in this case), MHD approx. ($\nabla B/B=\kappa$)
- Real frequencies very close
- Discrepancy is reduced to ~15% in the collisionless limit, or with adiabatic electrons



- Using GYRO eigenvalue solver [Belli]
- Have verified numerical convergence for GYRO with energy grid (8→12), radial grid (4→8), parallel grid (14→22), radial basis function order (3→5)

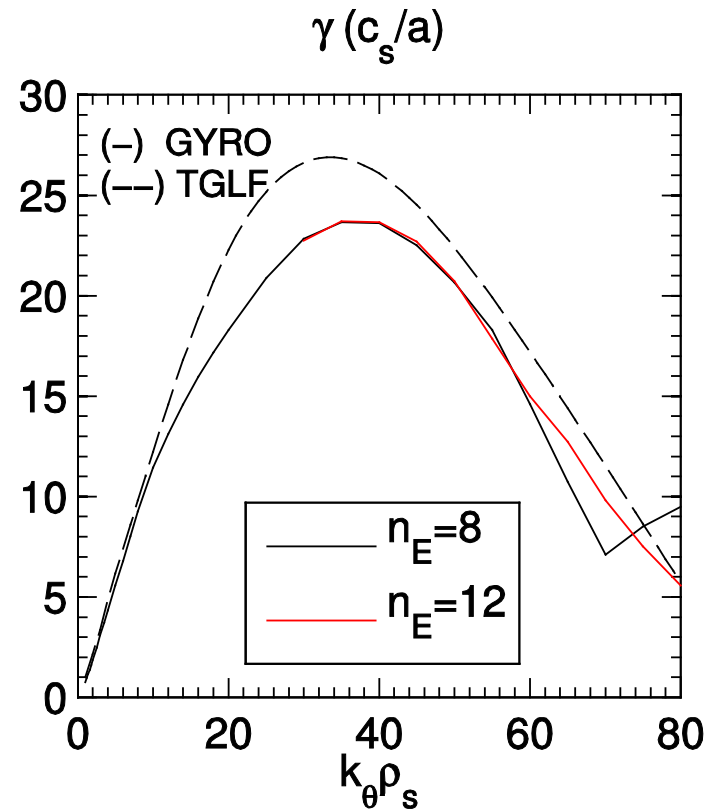
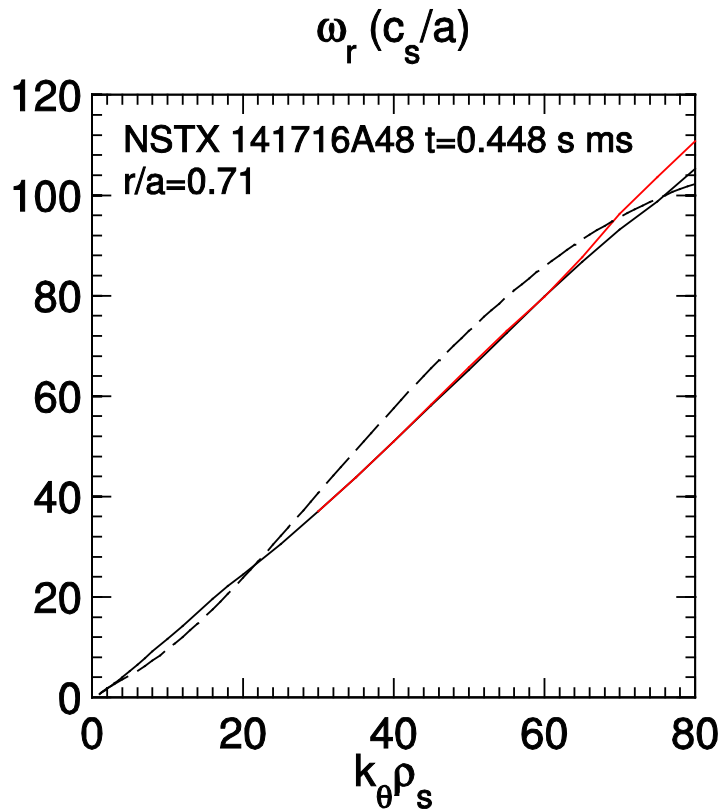
Similar agreement/discrepancy found across $r/a=0.5-0.8$

- Testing both with and **without** collisions ($k_\theta \rho_s = 0.4$)



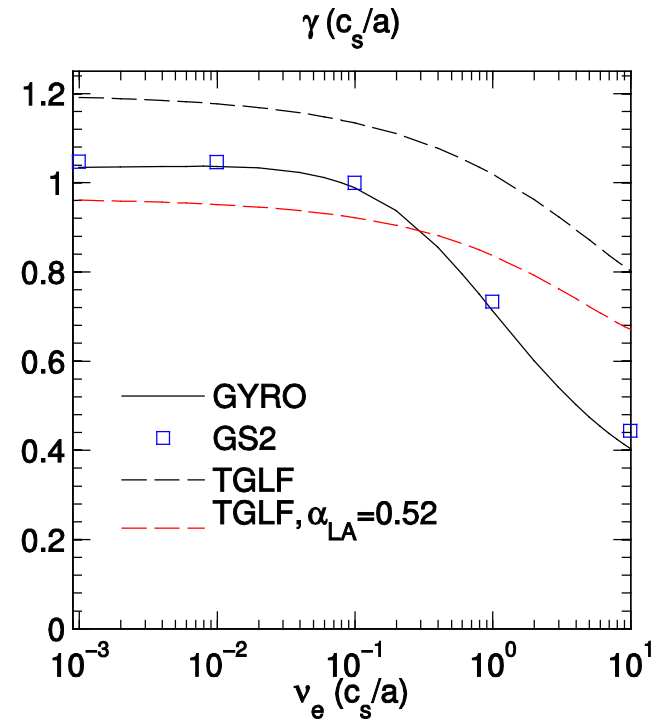
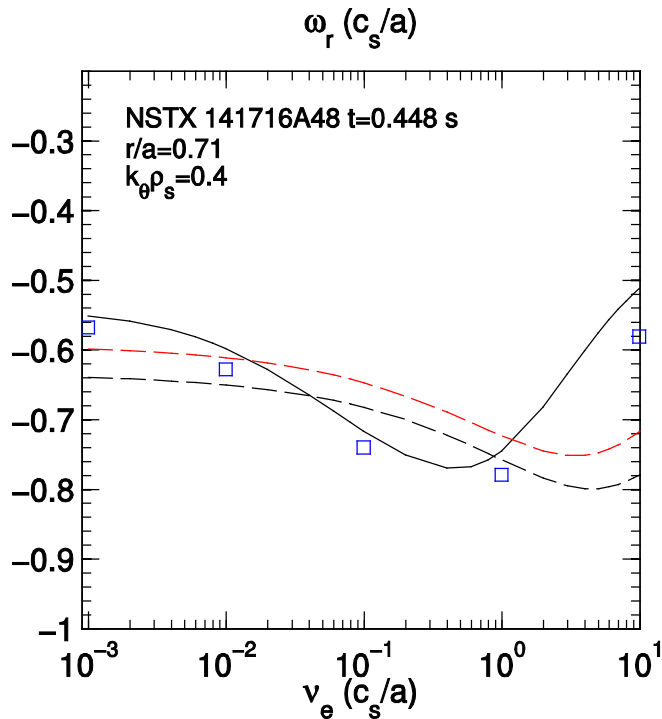
Comparable agreement for ETG growth rates

- This is collisionless, collisions make little difference
- High $k_{\theta}\rho_s$ GYRO simulations require more energy grid points (8→12)



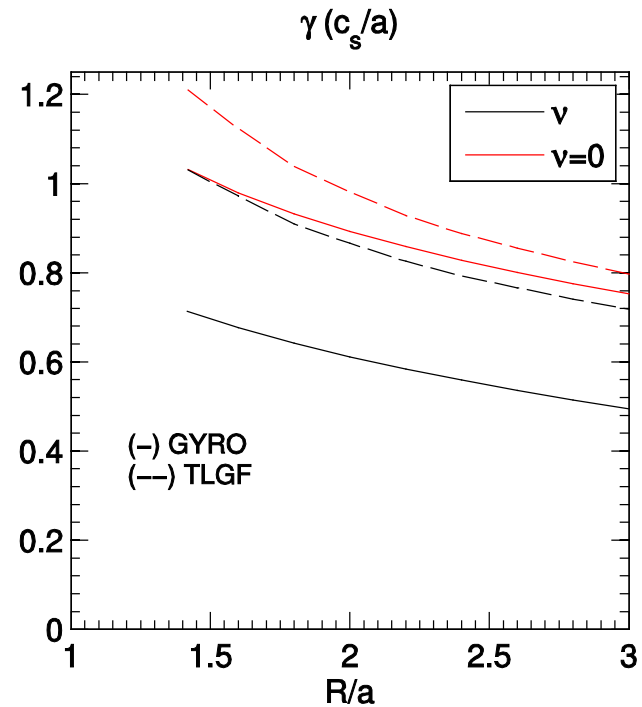
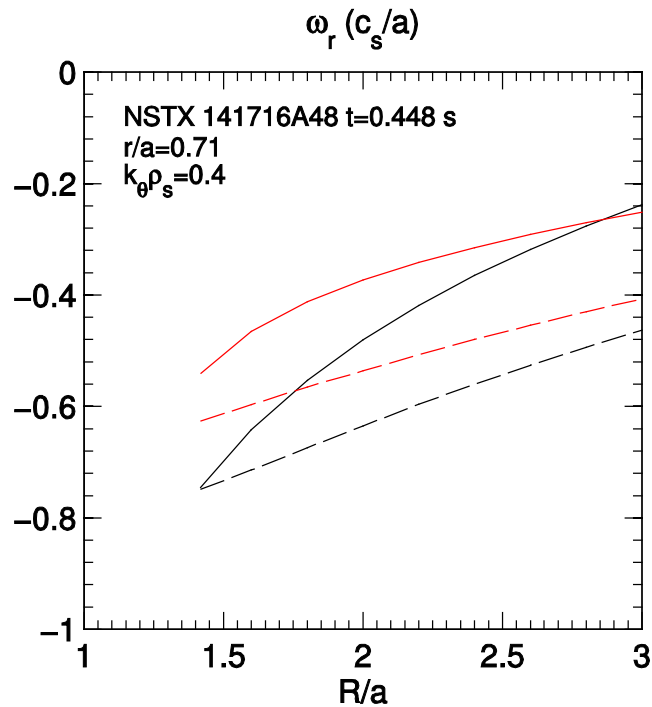
Testing sensitivity to collisionality

- GS2 agrees pretty well with GYRO (GS2 not using $\nabla B/B=\kappa$, but \sim negligible effect here)
- Reducing THETA_TRAPPED (α_{LA} in the paper) from 0.7 \rightarrow **0.52** improves agreement
- TGLF predicts a weaker tearing parity (ES) mode present over entire range



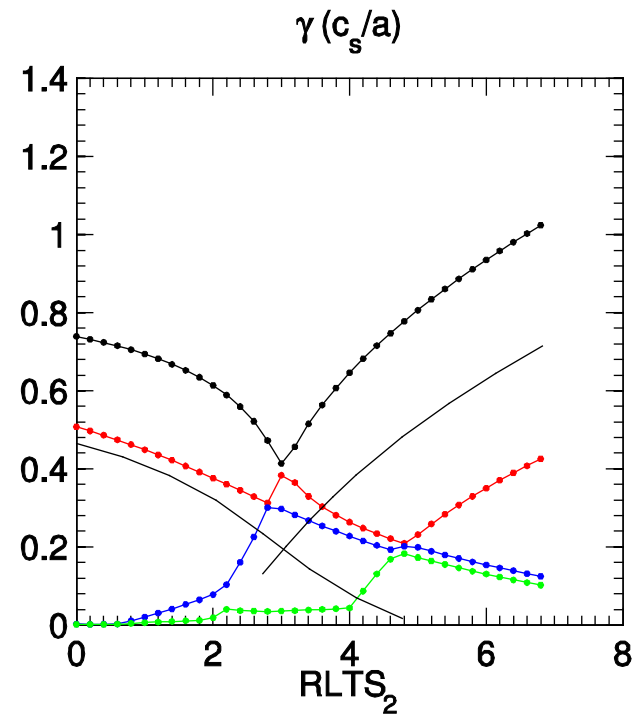
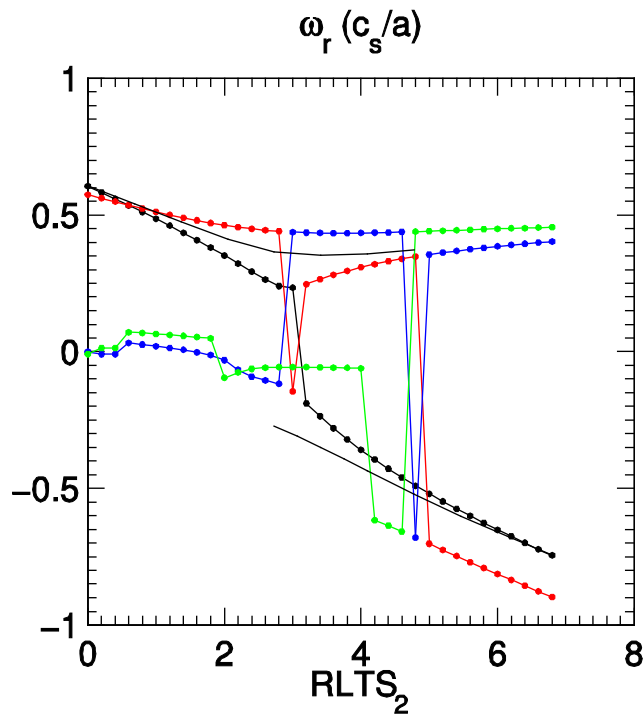
Aspect ratio doesn't matter too much

- Using Miller



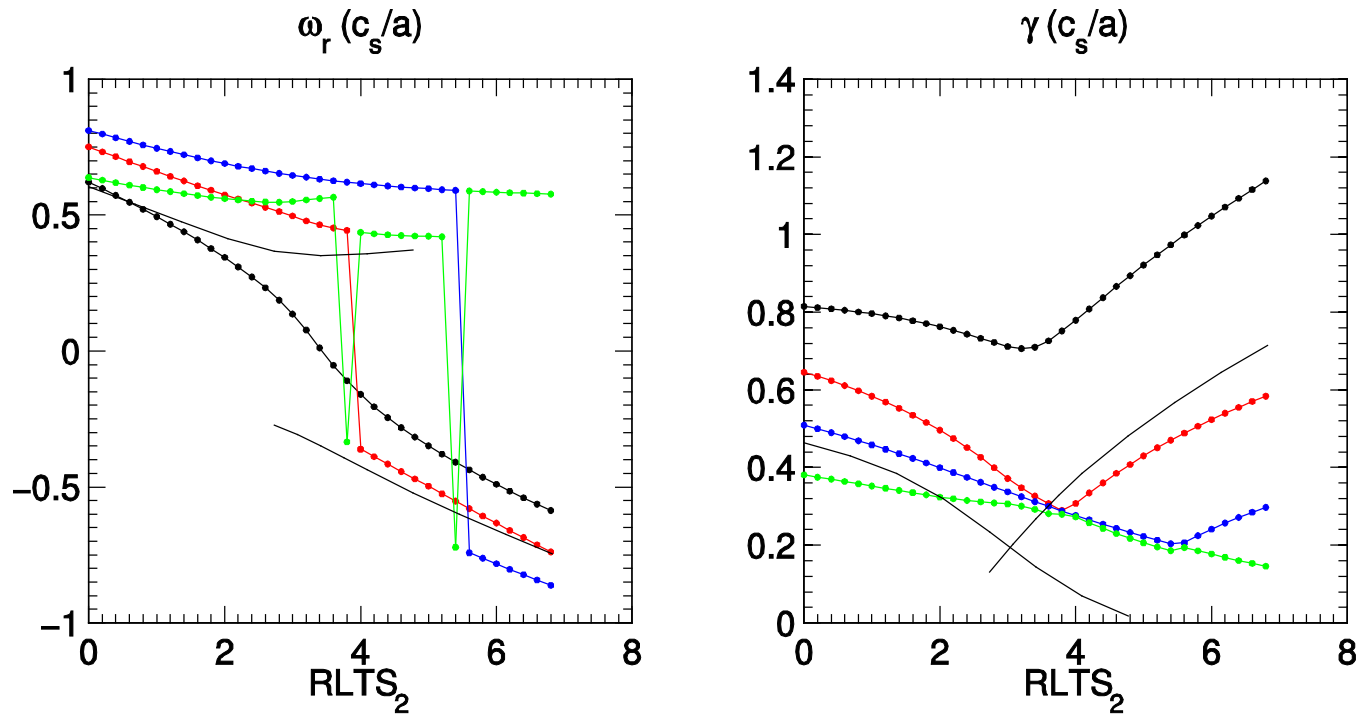
Ion temperature gradient scan ($R/L_{Td}=R/L_{Tc}$)

- Threshold for strongest mode appears to be similar
- GYRO finds second root from $a/L_{Ti} \geq 0$
- Two weaker TGLF roots are ES-tearing



Ion temperature gradient scan – nbasis = 16

- Growth rates are larger with more basis functions
- Instead of two distinct roots, fastest growing modes at low/high a/L_{Ti} look like one smoothly varying root

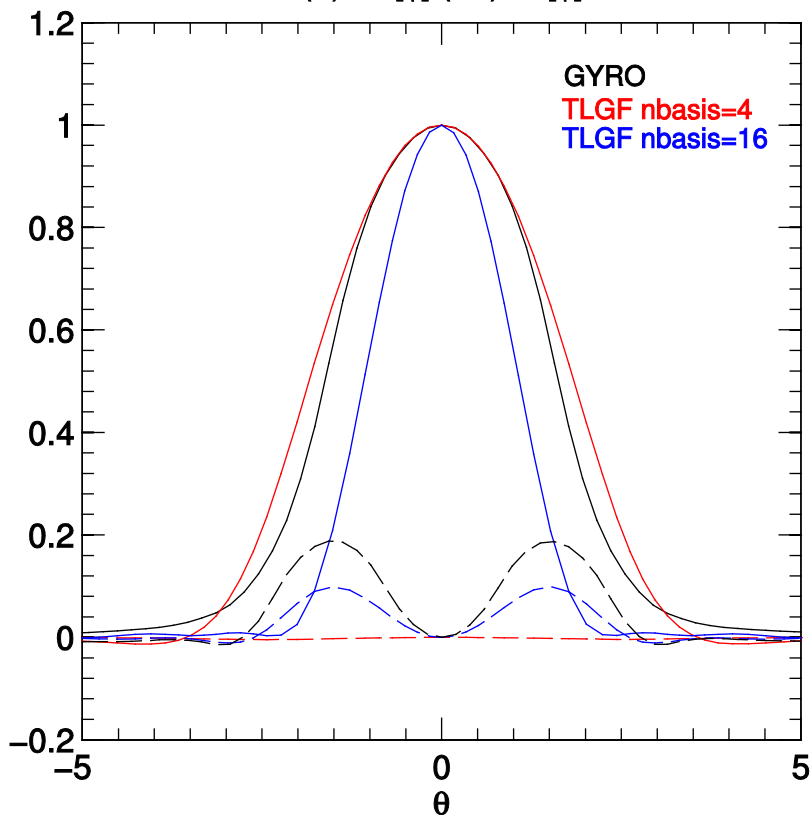


TGLF eigenfunction width is pretty close using nbasis=4

- Using nbasis=16, TGLF eigenfunctions are narrower
- Collisions make very little difference in eigenfunctions

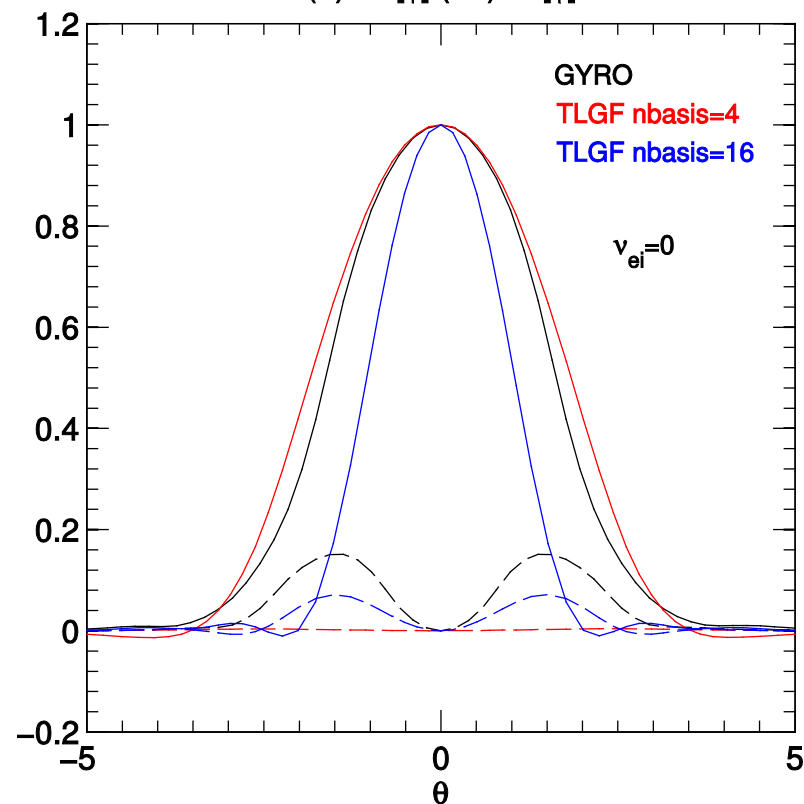
with collisions

(-) Re[ϕ] (---) Im[ϕ]



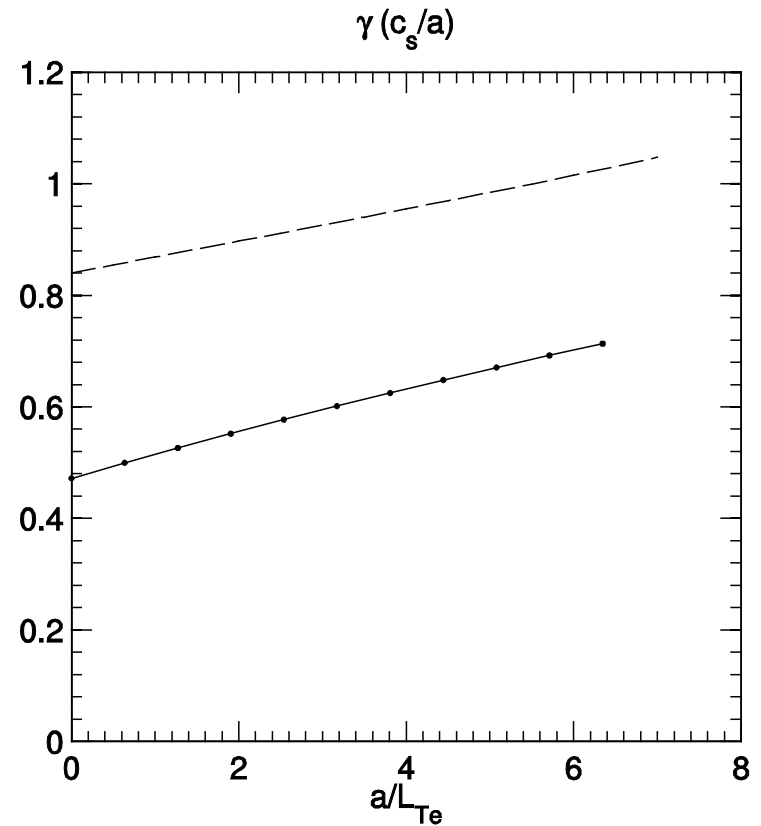
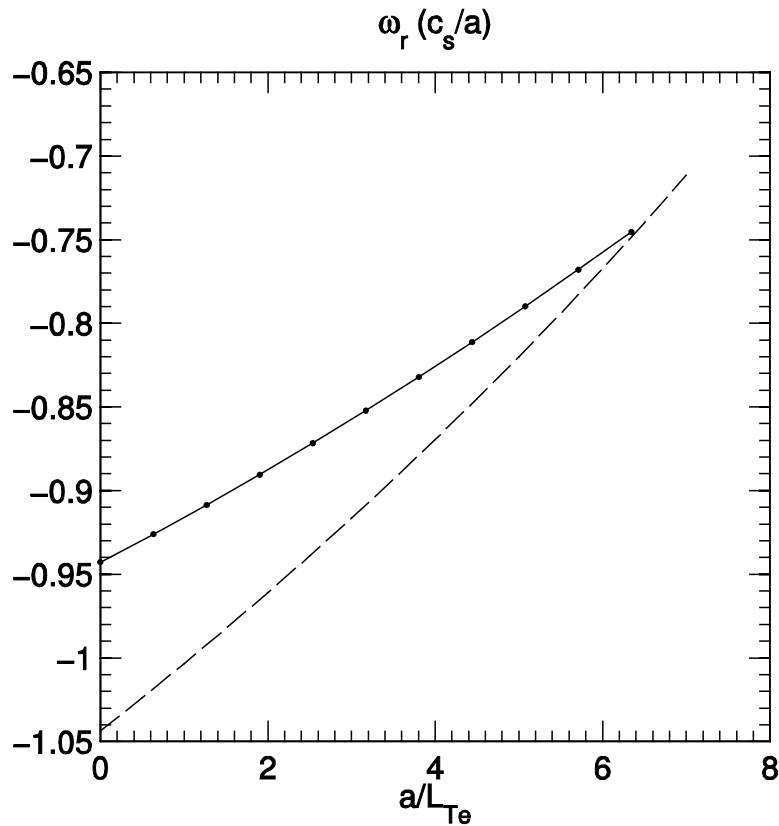
without collisions

(-) Re[ϕ] (---) Im[ϕ]



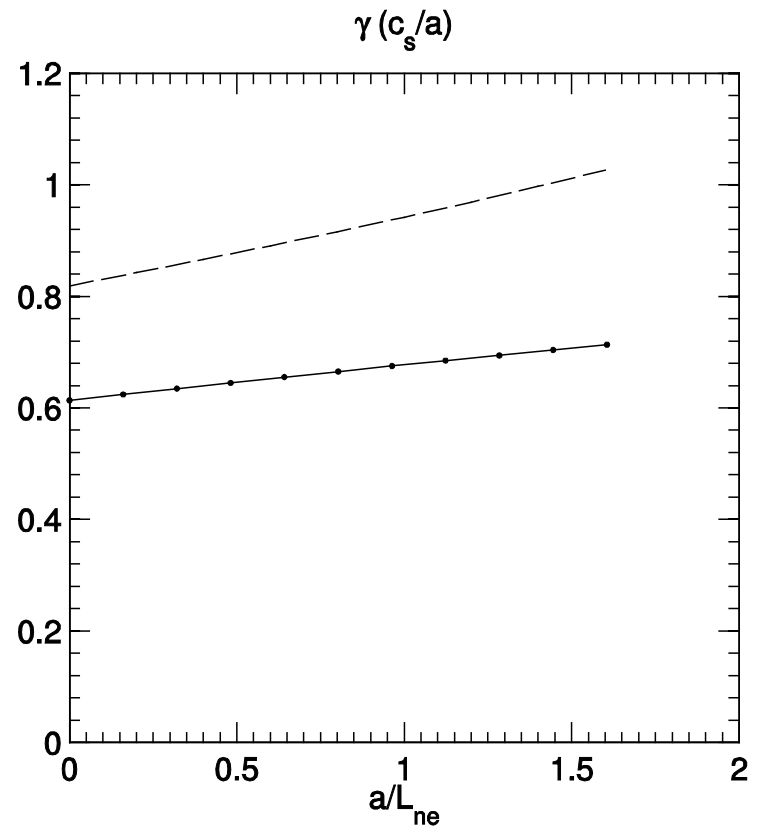
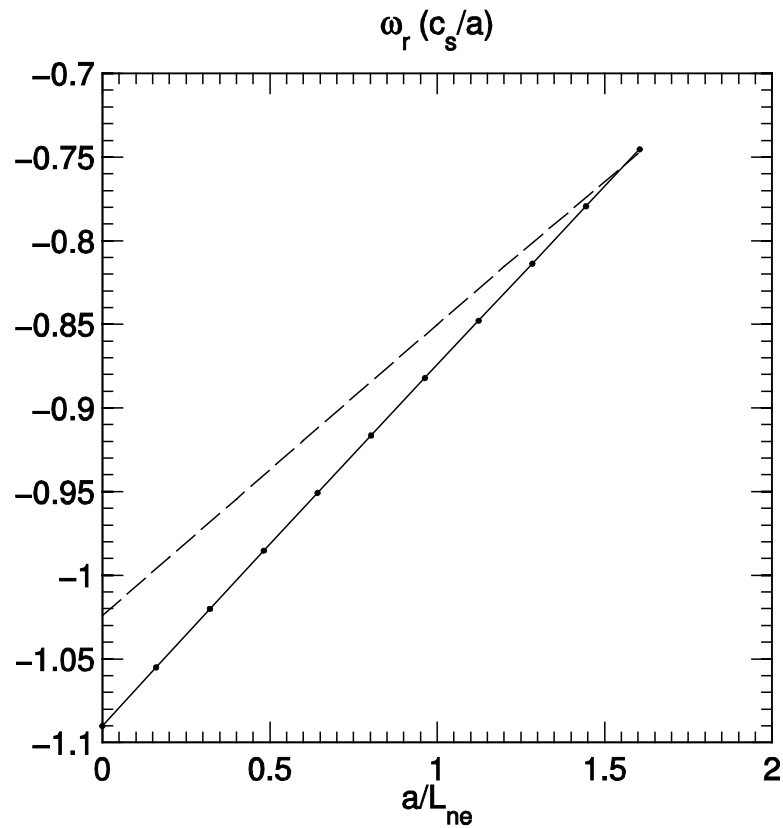
Electron temperature gradient scan

- No threshold in a/L_{Te}



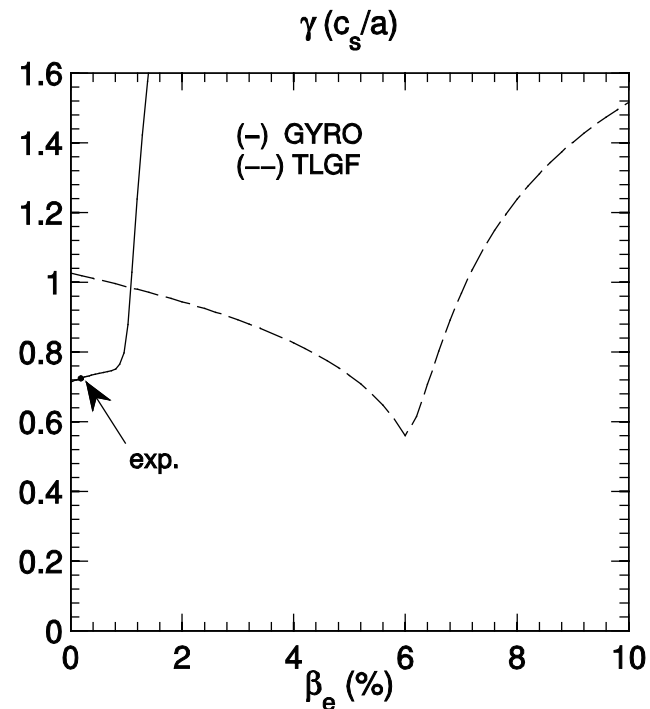
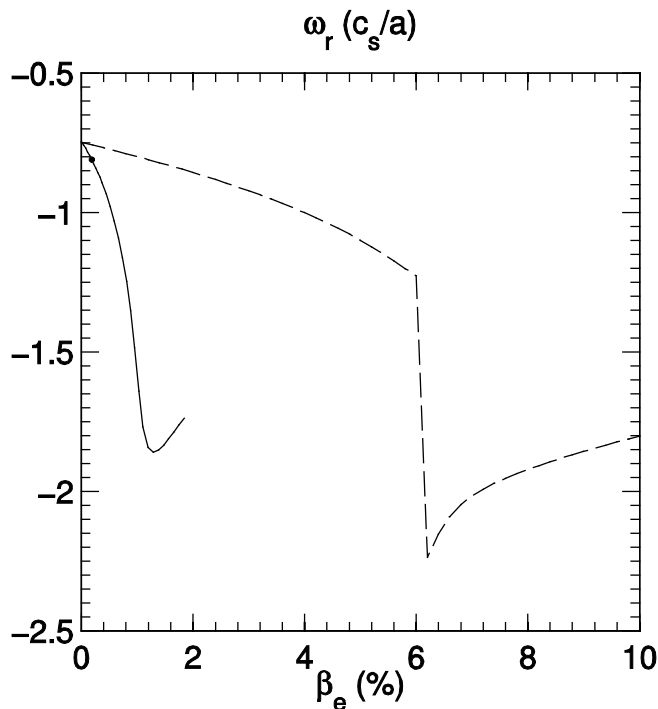
Density gradient scan

- Weak dependence ($a/L_{ne}=a/L_{nd}=a/L_{nc}$ for TGLF)



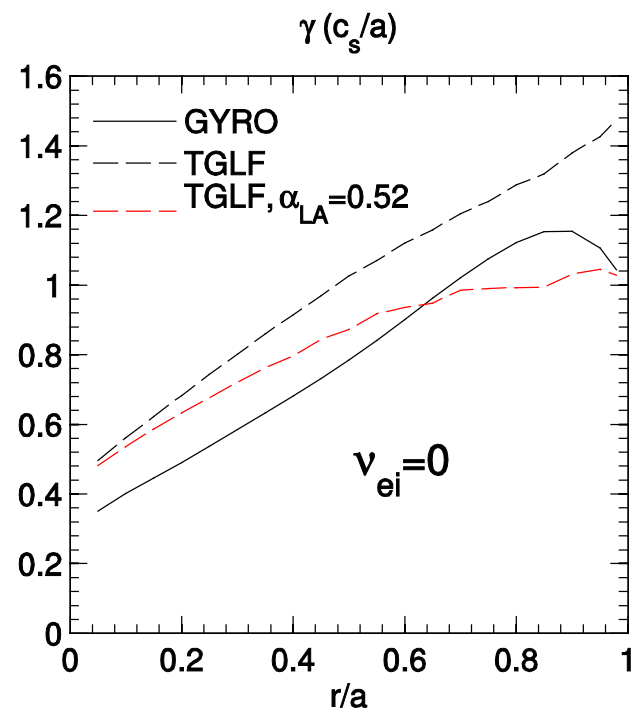
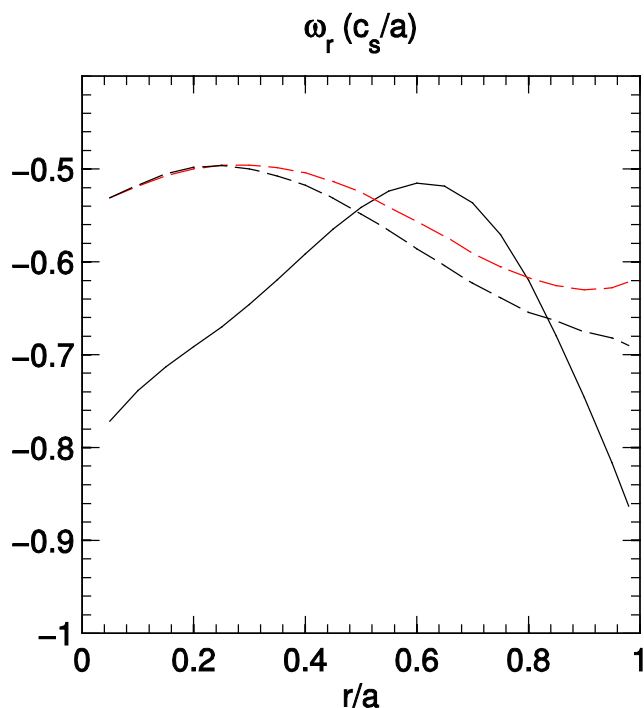
Beta scan shows negligible dependence around experimental value

- At higher β_e approaching H-mode values, GYRO shows “hybrid-KBM” behavior [Belli, PoP (2010); Guttenfelder, IAEA (2012)]
 - ITG growth rate *increases* with β_e , slowly transitions into KBM mode (not two distinct roots), phasing of $\text{Re}[A_{\parallel}]/\text{Im}[A_{\parallel}]$ transitions at the same point
- TGLF shows two distinct roots, KBM threshold much higher – this seems weird
 - The GYRO transition point is around $\alpha_{\text{MHD,unit}}=0.8$, typical of what I’ve seen in other NSTX cases
- I think both cases are using the same fixed pressure gradient in equilibrium



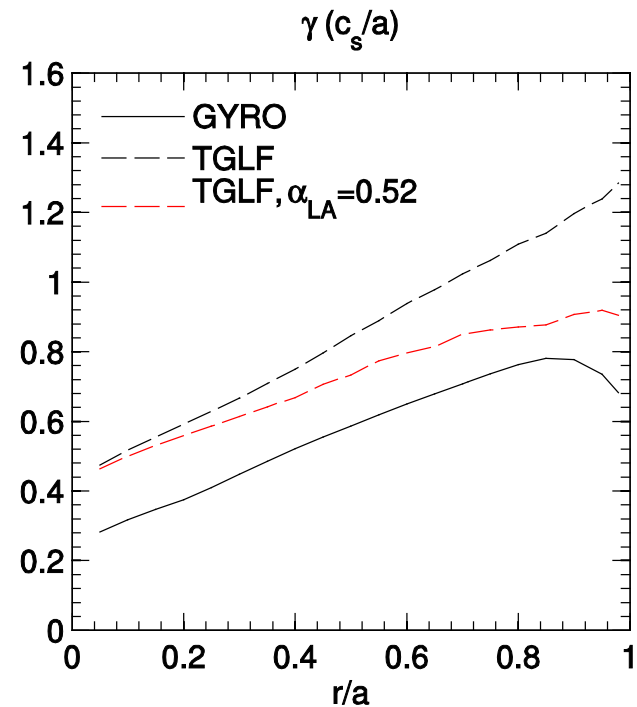
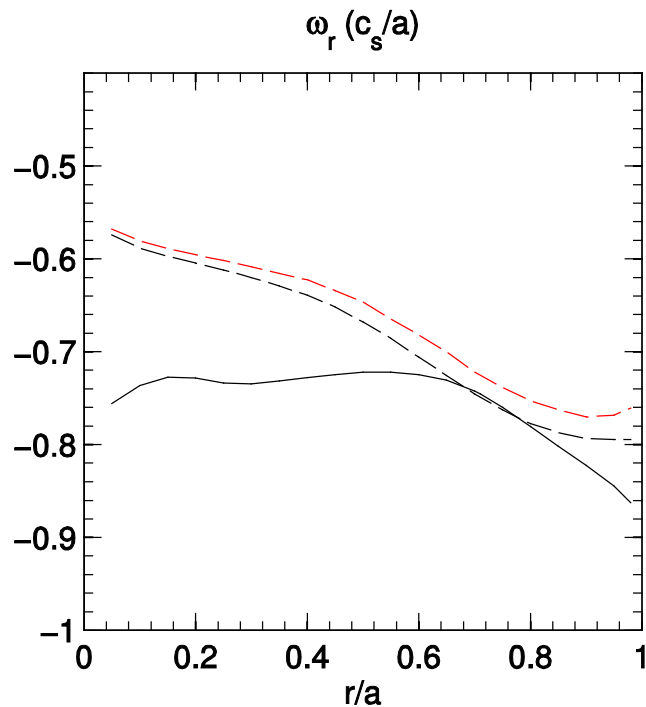
r/a scan using Miller inputs (all other parameters constant) collisionless ($v_{ei}=0$)

- Reducing THETA_TRAPPED (α_{LA} in the paper) from 0.7 \rightarrow **0.52** improves agreement for larger trapped particle fraction (r/a)



r/a scan using Miller inputs (all other parameters constant) with collisions ($v_{ei}=0.99 c_s/a$)

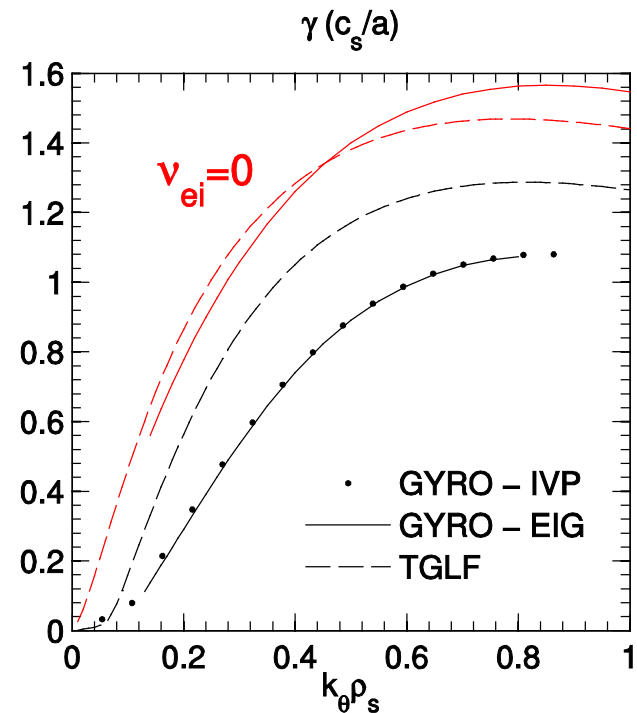
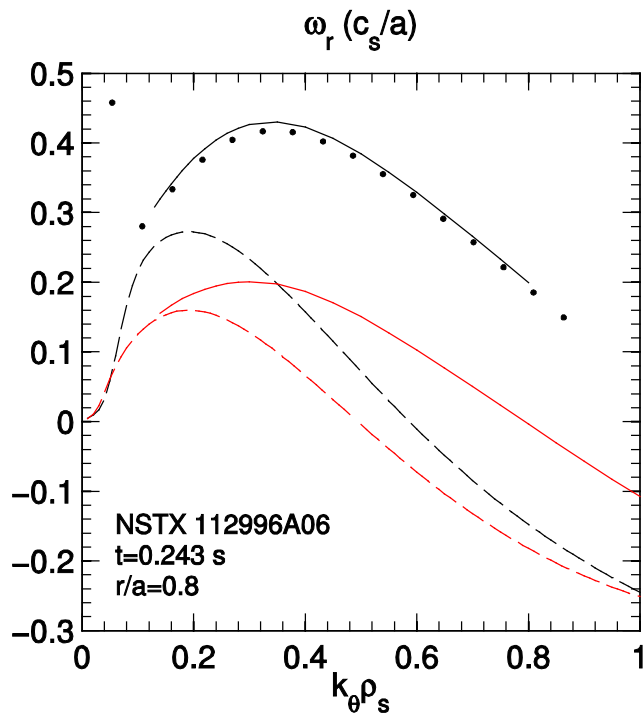
- Reducing THETA_TRAPPED (α_{LA} in the paper) from 0.7 \rightarrow **0.52** improves agreement for larger trapped particle fraction (r/a)



112996A06, t=0.243 s

$k_{\theta}\rho_s$ scan (r/a=0.8)

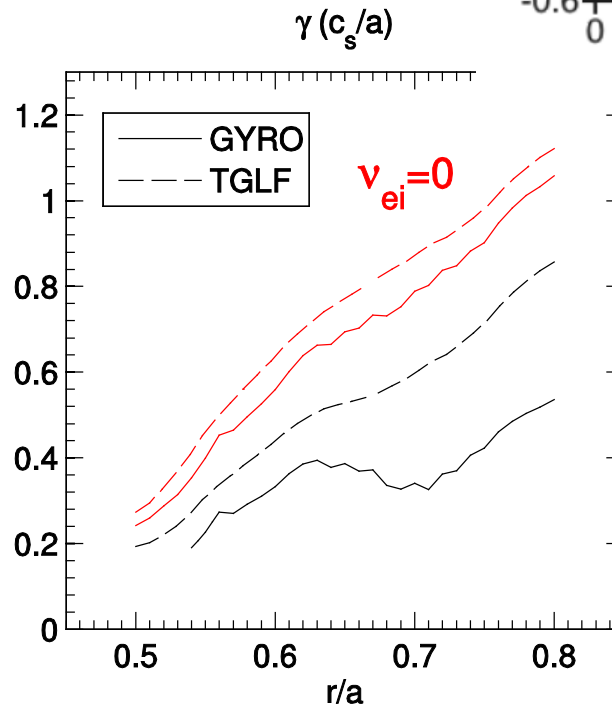
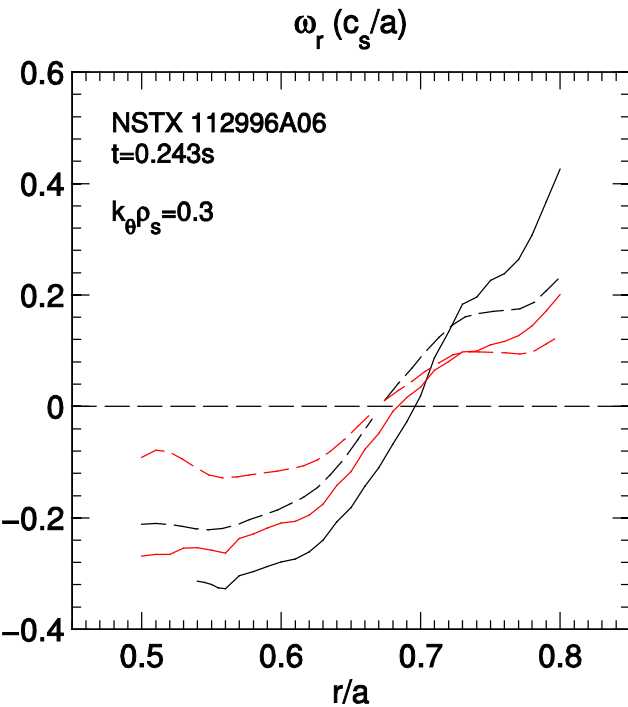
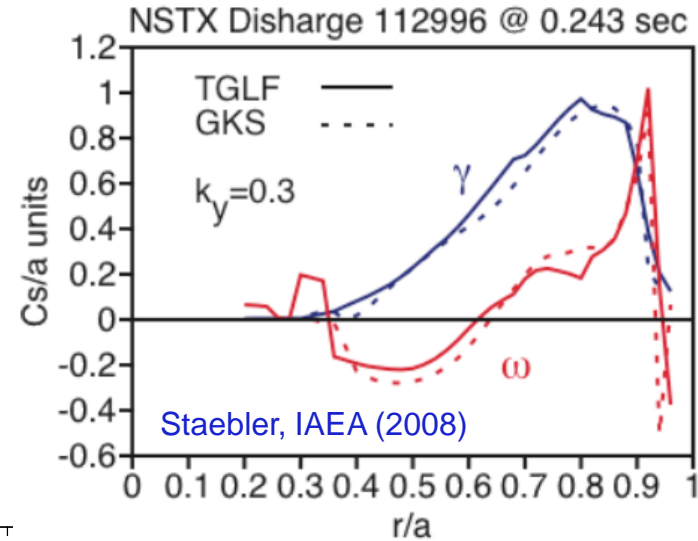
- L-mode case from Stutman, PoP (2006) & Staebler, IAEA (2008)
- Both GYRO and TGLF using Miller ($\nabla B=\kappa$), EM (ϕ, A_{\parallel})
- With collisions, comparable discrepancy as previous case
- **Good agreement in growth rate without collisions**
- (lowest $k_{\theta}\rho_s$ dot in GYRO-IVP run is microtearing)



112996A06, $t=0.243$ s

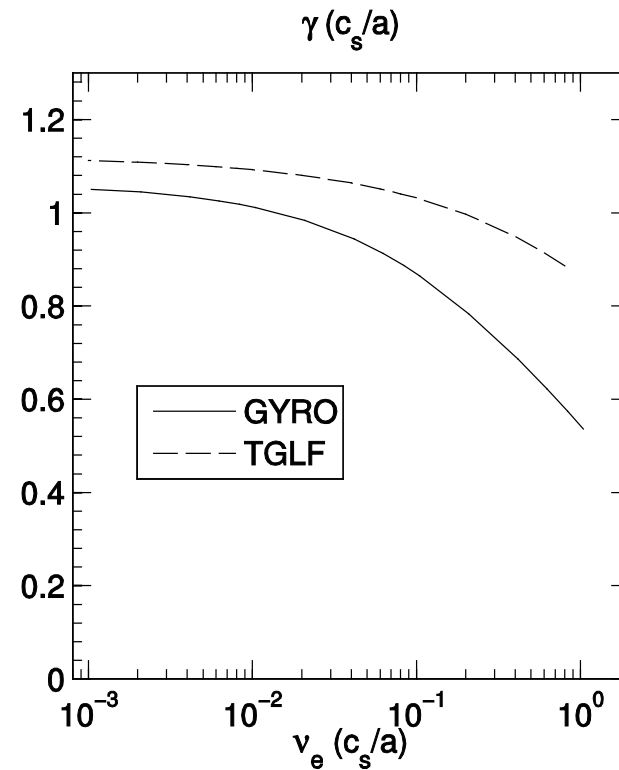
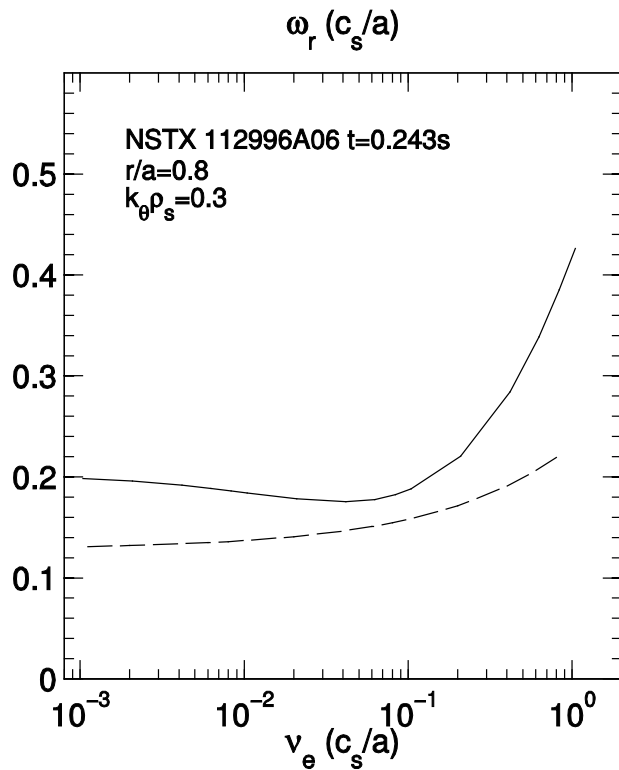
r/a scan ($k_\theta \rho_s = 0.3$)

- With collisions, agreement not as good as Staebler, IAEA (2008)
- With collisions, growth rates in much better agreement
- GS2 at $r/a=0.7$, $k_y=0.3$



112996A06, $t=0.243$ s

v_e scan ($r/a=0.8$, $k_\theta \rho_s=0.3$)



Profiles of relevant parameters for both L-mode shots (141716, 112996)

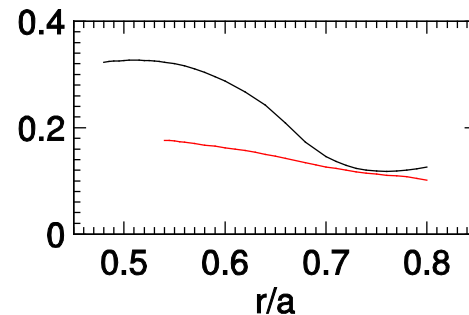
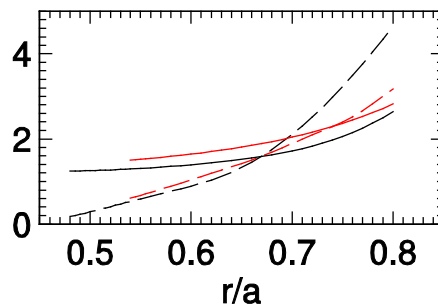
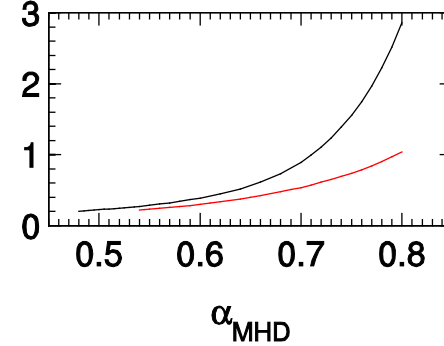
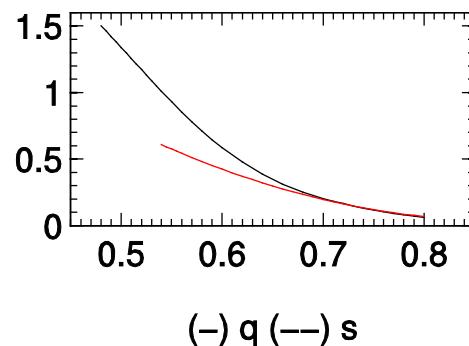
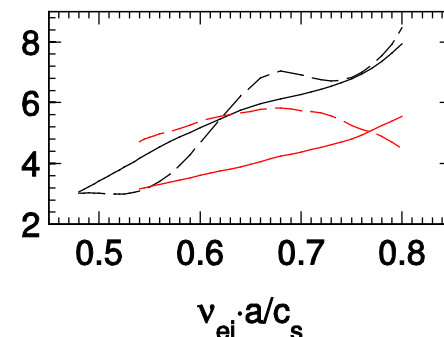
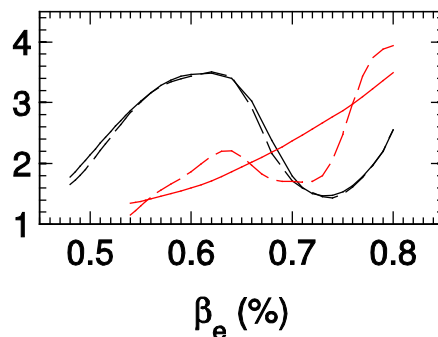
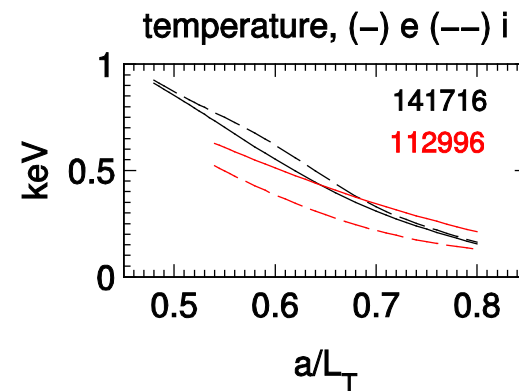
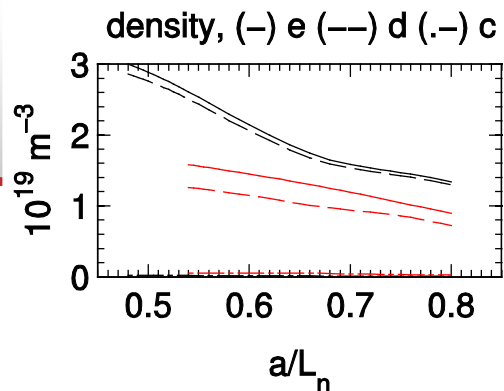
- For 112996:

n_e , v_e , β_e a little lower

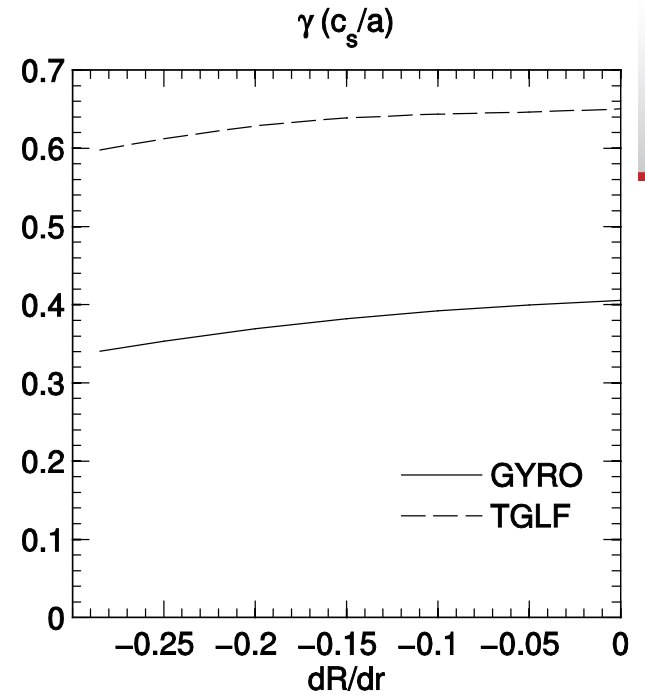
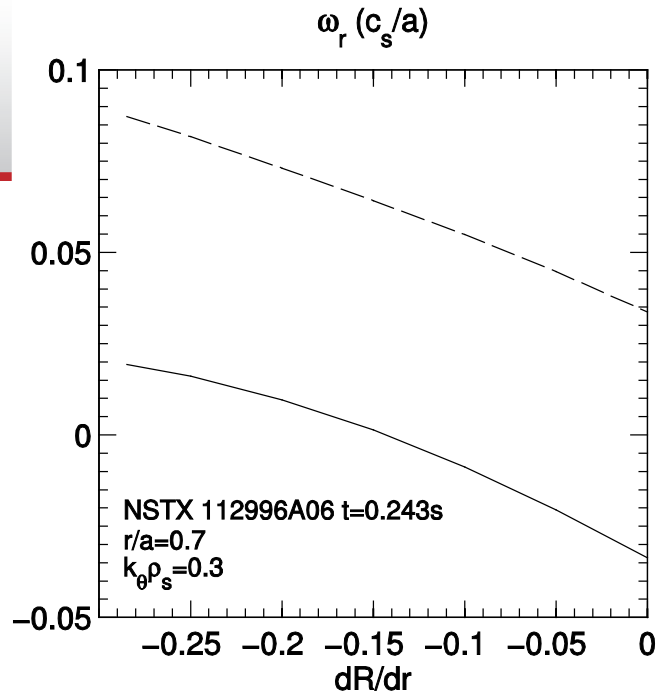
$T_e/T_i \sim 1.5$

weaker a/L_{Te}

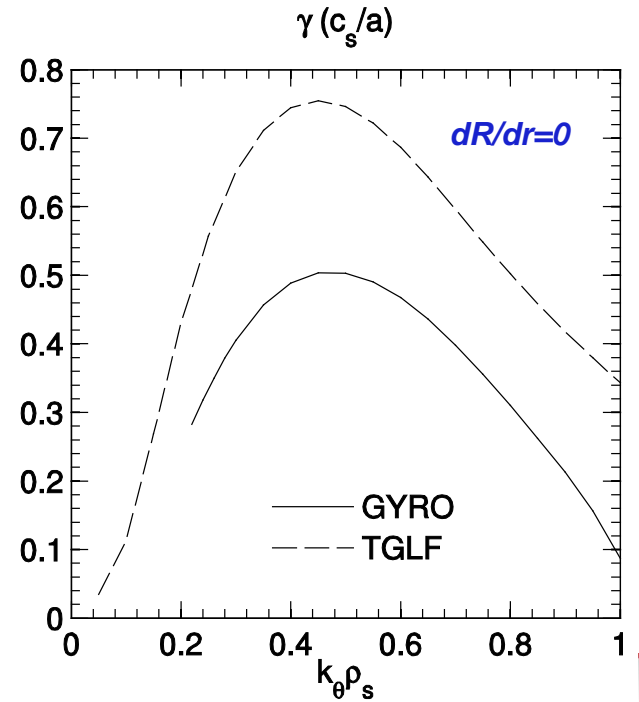
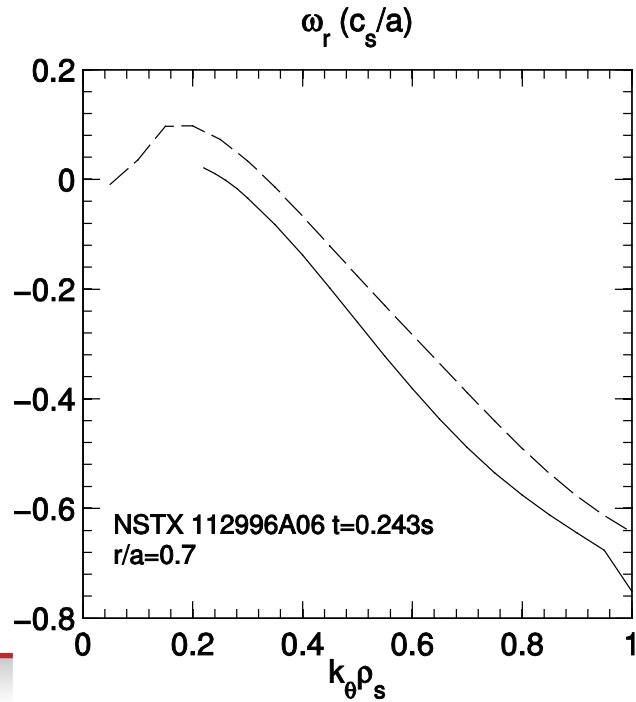
slightly higher q



dR/dr scan

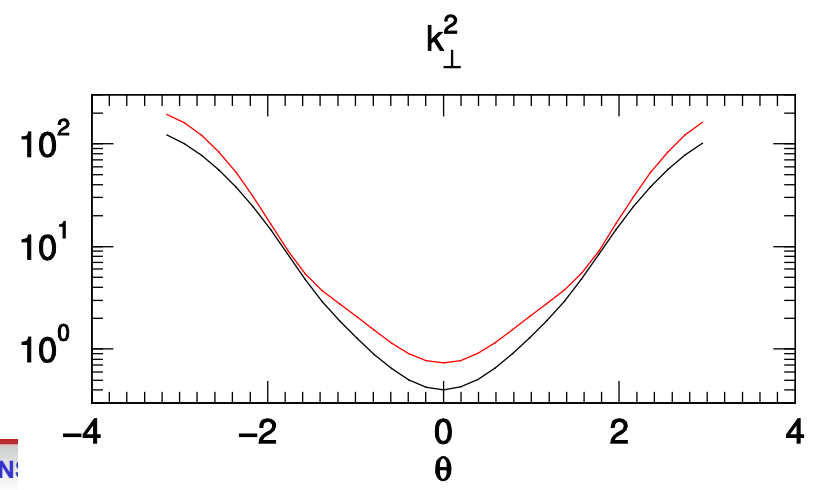
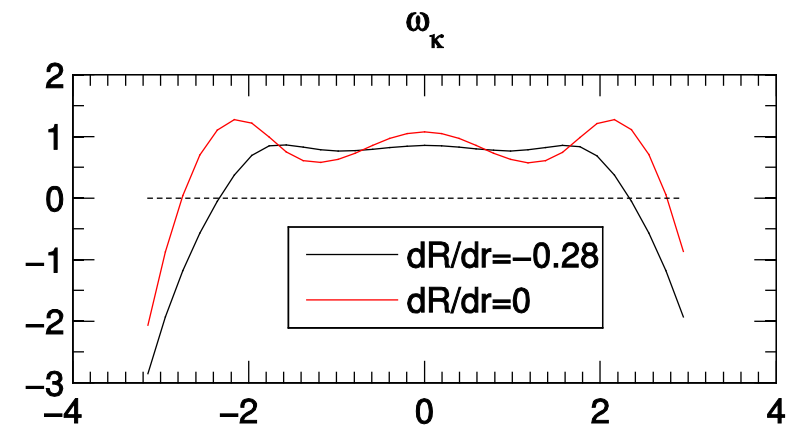
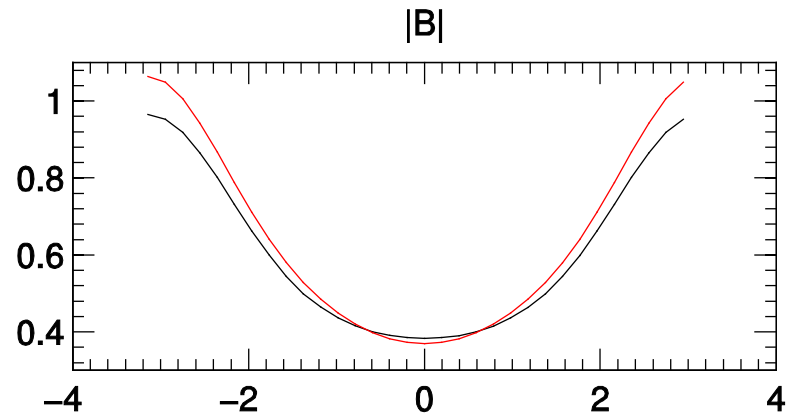


- $k_\theta \rho_s$ spectra for $dR/dr=0$



Comparing geometry metrics for $dR/dr=-0.28$ & 0

- Normalizing B_{unit} is different for each case
- Curvature drift coefficient is normalized in same way as GS2
 - Broader region of bad curvature with $dR/dr=0$
- Only showing k_{\perp}^2 (and ω_{κ} above) terms that are independent of θ_0



Overview

- Motivation
- TGLF standalone linear tests
- TGLF standalone transport tests
- TGYRO/TGLF/NEO profile predictions

Motivation

- Desire predictive capability for spherical tokamaks (STs) to help develop fully non-inductive discharges for NSTX-Upgrade and next-generation devices: CTF, FNSF, Pilot Plant, etc...
- Non-linear gyrokinetic simulations are expensive → develop reduced transport models that are much faster to evaluate in integrated simulations
- TGLF is one such physics-based model which is capable of including most effects expected to be important: general geometry, collisions, electromagnetic effects, flow and flow shear, multi-species
 - Does not include non-local effects at large $\rho_* = \rho_s/a$

⇒ Limited tests of TGLF for realistic ST parameters

TGYRO, TGLF, NEO used for modeling

TGYRO [1]

- Transport solver that takes as input TRANSP-calculated sources (P_{NBI} , dW/dt , S_{particle} , ...) and equilibrium \rightarrow predicts profiles (T_i , T_e , n_e , ...) using choice of transport models (TGLF+NEO, TGLF+Chang-Hinton, GYRO+NEO, ...)

TGLF [2]

- Fluid moments of *linear* gyrokinetic equation with closures chosen to best match a database of ~ 1800 linear gyrokinetic simulations
- Predicts transport using a quasi-linear + mixing length model, with coefficients tuned to best match ~ 100 non-linear gyrokinetic simulations (no empirical tuning, only theory based)
- Gyrokinetic simulations for validation are based on conventional aspect ratio parameters
– Limited testing using realistic ST parameters⁴

NEO [3]

- Drift kinetic solution (...) of neoclassical transport, allowing for multiple species, toroidal flow (poloidal asymmetry), and various collision operator models
- For cases shown here, Chang-Hinton used – very close to DKE solution

¹ J. Candy et al., Phys. Plasmas **16**, 060704 (2009).

² G.M. Staebler et al., Phys. Plasmas **14**, 055909 (2007); Phys. Plasmas **17**, 122309 (2010).

³ E.A. Belli & J. Candy, Plasma Phys. Control. Fusion **50**, 095010 (2008).

⁴G.M. Staebler et al., IAEA (2008).

NSTX L-mode is unstable to ~electrostatic ITG [This is older, not identical models, but basically same as new stuff]

- Linear calculations at five different radii ($r/a=0.6-0.8$)
- GYRO growth rates are larger than $E \times B$ shearing rates (γ_E) except for $r/a=0.6$
- TGLF growth rates always much larger (up to $2\times$)

