

# ***Separation of Momentum Diffusion and Pinch Using $n=3$ Non-Resonant Braking Perturbations on NSTX***

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# Motivation



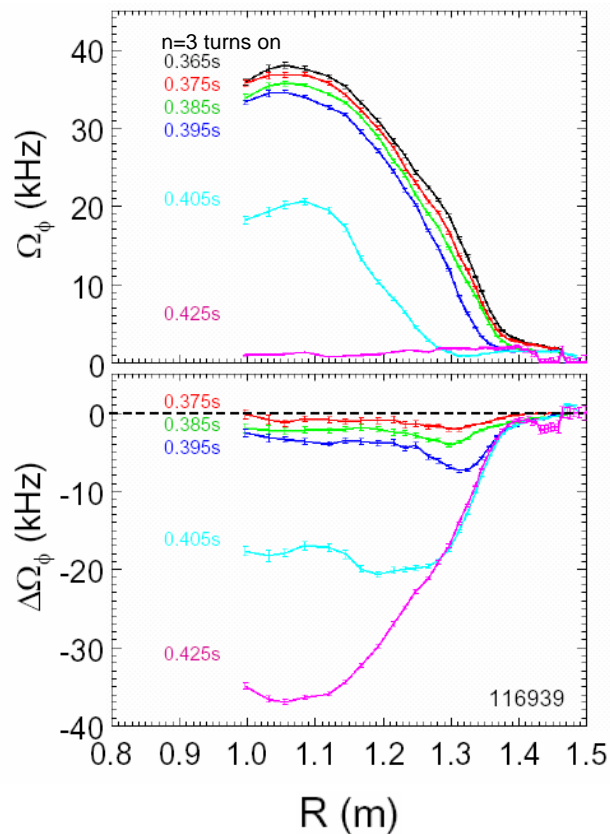
- Rotation plays an important role in fusion plasmas
  - Turbulence suppression
  - RWM and NTM stabilization
- Hence, predictive understanding of rotation and momentum transport desirable
  - Predictions for ITER and future devices
- Usually, momentum transport considered diffusive
  - Recent studies on JT-60U suggest role of convection
- Perturbative studies made on NSTX to investigate role of momentum pinch at low aspect ratio

# Momentum Transport Studied Using Non-Resonant $n=3$ Magnetic Perturbations

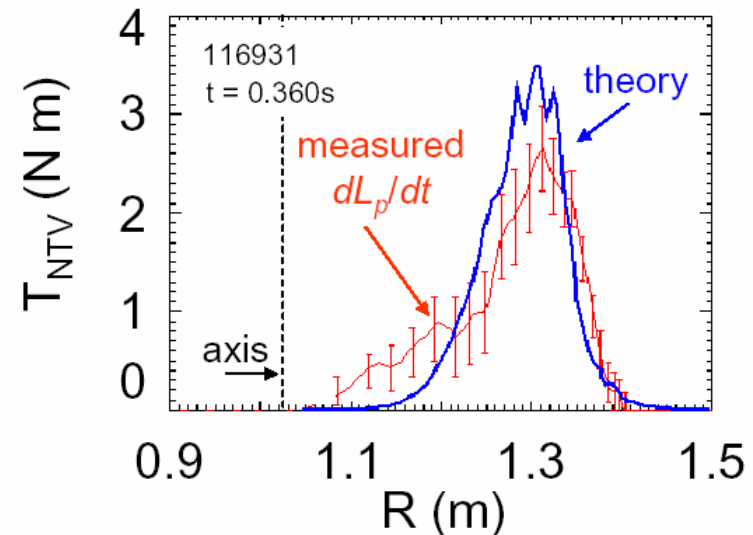


- Previously been used to slow plasma rotation for ITER-relevant RWM stabilization experiments

Zhu et al. PRL (2006)

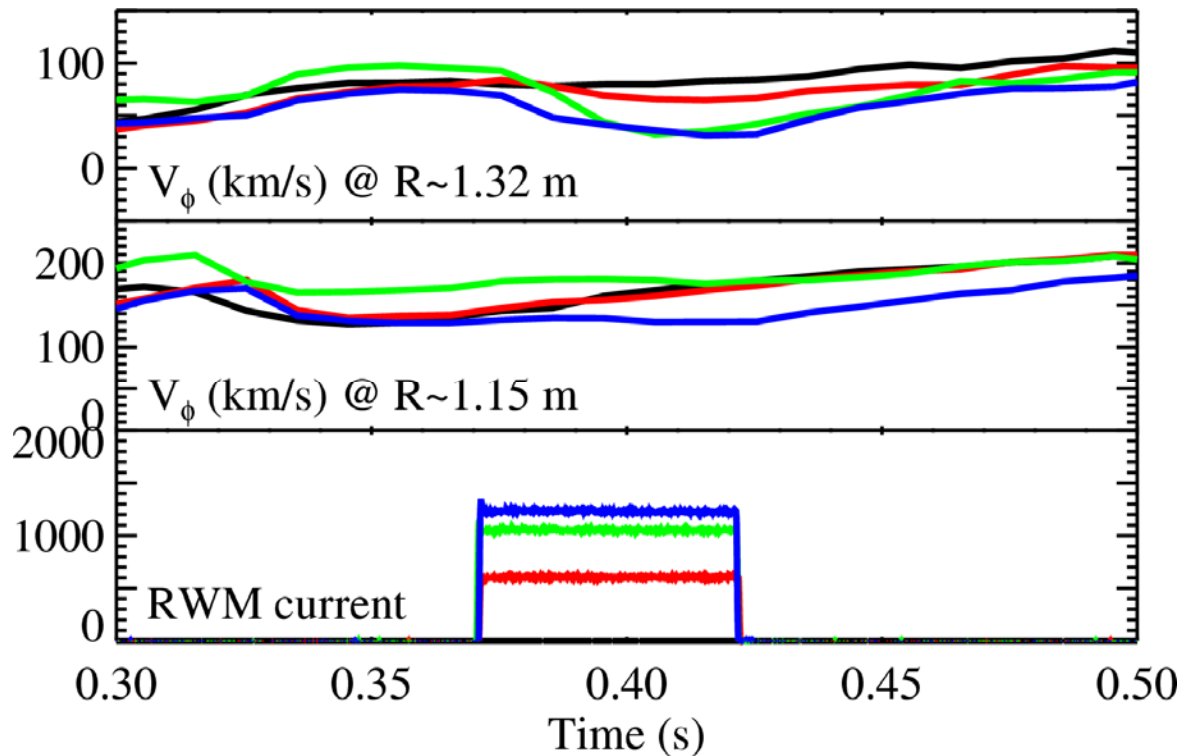


Observed rotation damping consistent with neoclassical toroidal viscosity (NTV) theory



**Steady-state & transient application**

# ***Perturbative $\tau_\phi$ , $\chi_\phi$ Can be Obtained from Transient Application of $n=3$ Braking***



- Rotation responds rapidly to nRMP braking at edge
- Effect on central rotation less pronounced

# Momentum Confinement Time Several Times Larger than Energy Confinement Time



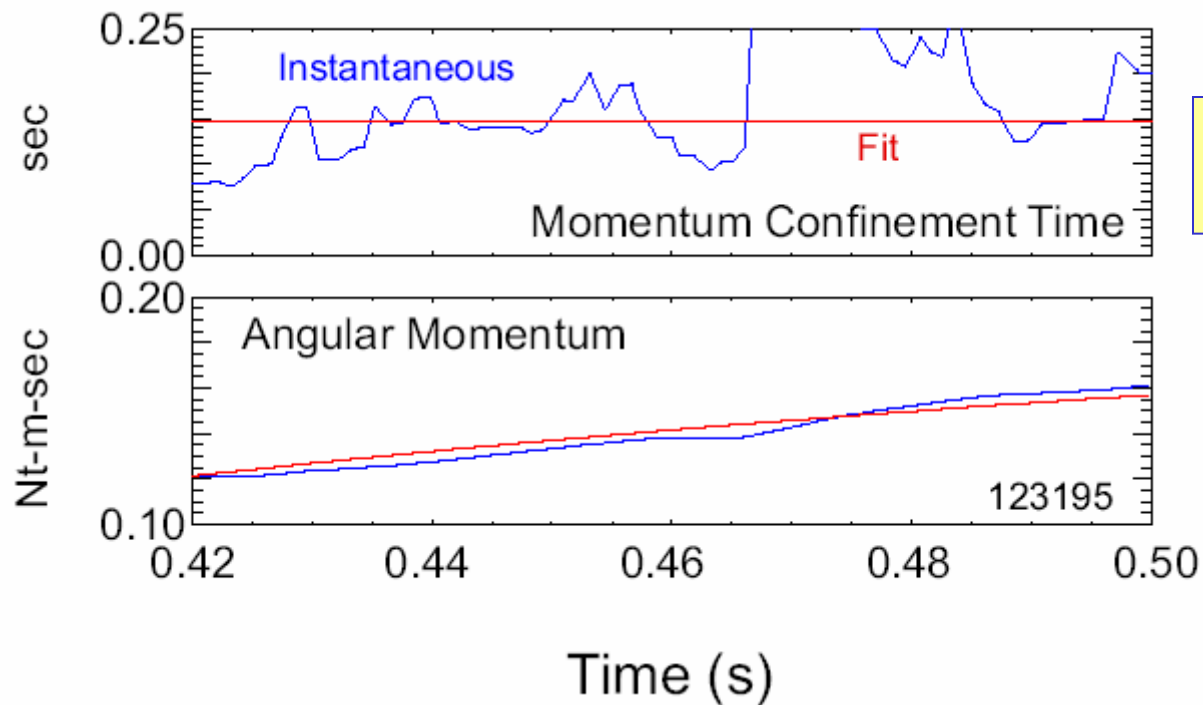
- Use  $dL/dt = T - L/\tau_\phi$  relation to determine instantaneous  $\tau_\phi$
- Model rotation recovery following perturbation to determine perturbative  $\tau_\phi$

$$L(t) = \tau_\phi * [T - (T - L_0/\tau_\phi) * \exp(-t/\tau_\phi)], \text{ where}$$

$L$  = Angular momentum

$T$  = Torque (NB torque only)

$L_0$  = Angular momentum at time of nRMP turn-off



$\tau_E \sim 30\text{-}50 \text{ ms}$   
 $< \tau_\phi$

# ***Local Momentum Transport Investigated During Spin Up After Perturbation***



- Toroidal rotation evolves according to momentum balance equation

$$mnR \frac{\partial V_{\phi}}{\partial t} = \eta + \nabla \cdot \Gamma_{\phi}$$

where

$\eta$  = Torque density,  $m$  = mass,  $n$  = density,  $V_{\phi}$  = toroidal rotation,  $\Gamma_{\phi}$  = momentum flux

- TRANSP calculation of torque coupled with CHERS rotation measurement  $\rightarrow \Gamma_{\phi}$  well determined
- Model  $\Gamma_{\phi}$  evolution to determine diffusive and convective contributions

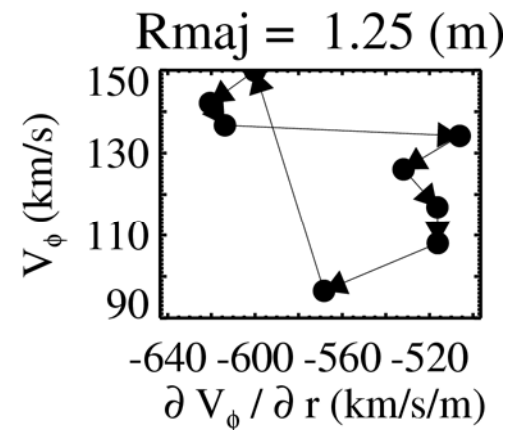
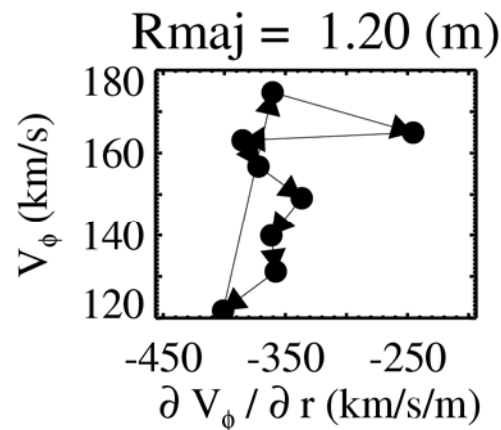
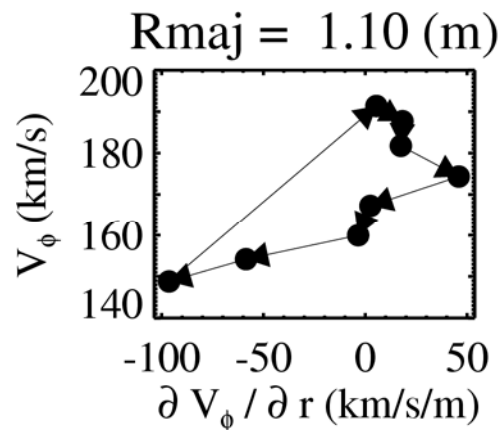
# Successful Distortion to Rotation Profile Allows Separation of $\chi_\phi$ and $V_\phi^{pinch}$



- Use simple model for momentum flux

$$\Gamma_\phi = mnR \left( \underbrace{\chi_\phi \frac{\partial V_\phi}{\partial r}}_{\text{diffusion}} - \underbrace{V_\phi V_\phi^{pinch}}_{\text{convection}} \right)$$

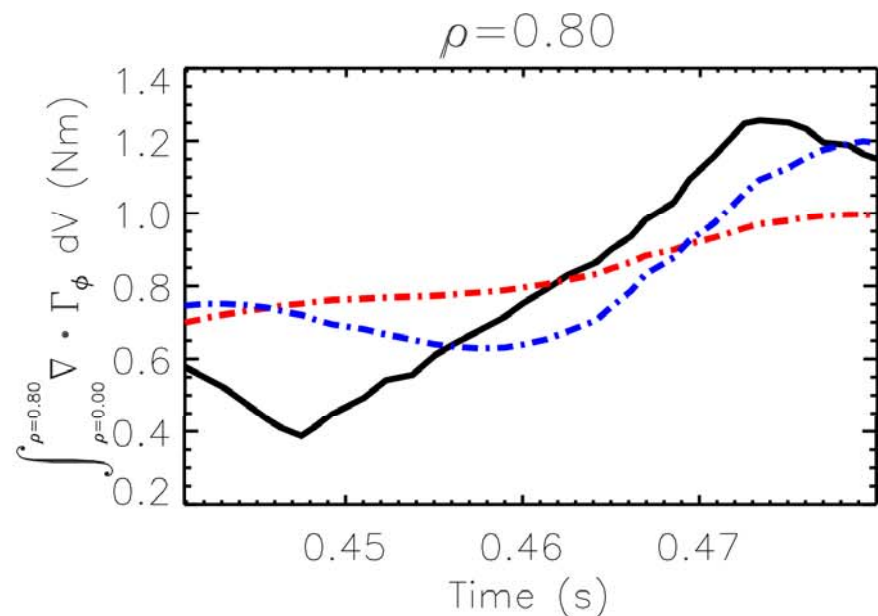
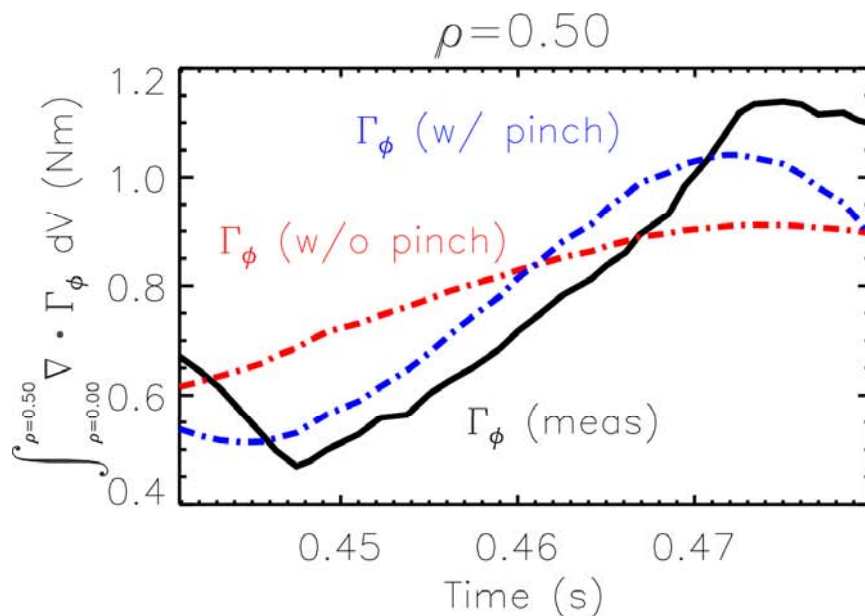
- Must change  $V_\phi$  independently of  $dV_\phi/dr$ 
  - can unravel relative contribution of  $\chi_\phi$  and  $V_\phi^{pinch}$



# Including Momentum Pinch Improves Fit to Momentum Flux



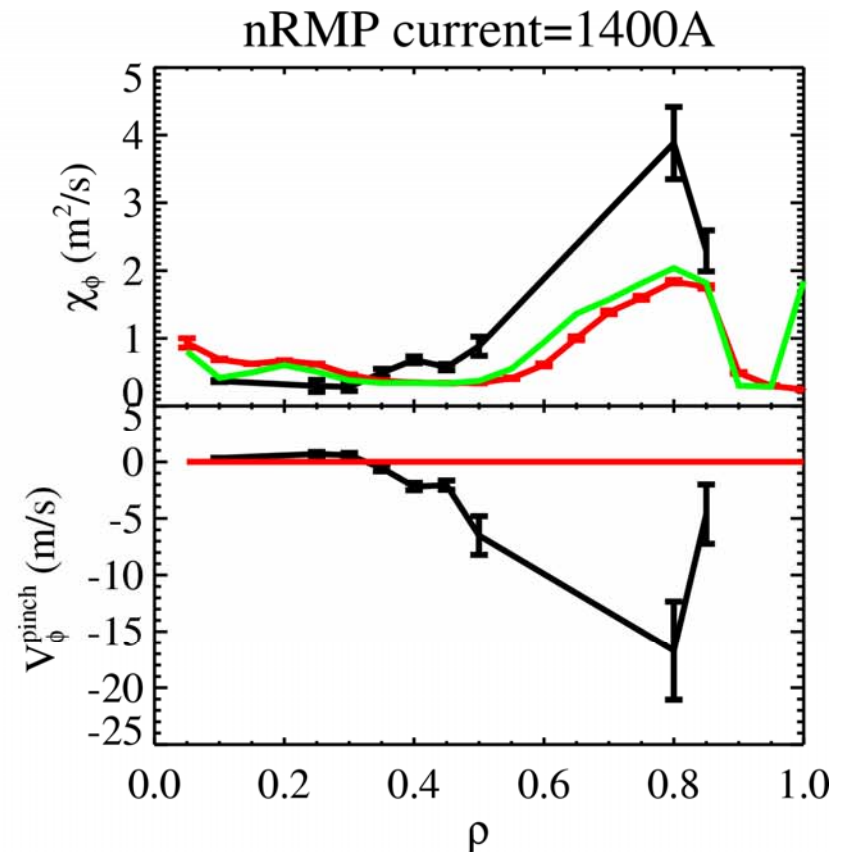
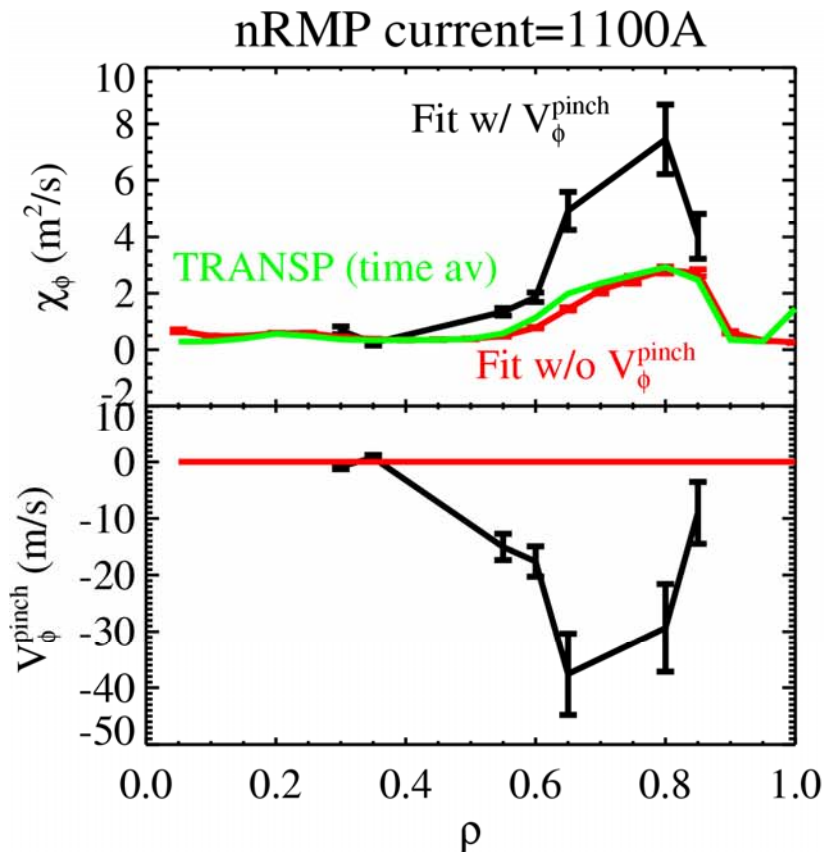
- Non linear least squares fit of  $\chi_\phi$ ,  $V_\phi^{\text{pinch}}$  profiles
  - Assumed constant in time
- Inclusion of pinch improves reconstruction of momentum flux at some radii
  - Not perfect  $\rightarrow$  Other off-diagonal terms?  $\chi_\phi$ ,  $V_\phi^{\text{pinch}}$  changing...?



# Perturbative Momentum Transport Reveal Significant Inward Pinch



- Relatively consistent result from different sized perturbation
  - Within factor of 2  
decoupling of  $V_\phi$ ,  $dV_\phi/dr$  not ideal  $\rightarrow$  trade-off between  $\chi_\phi$  and  $V_\phi^{\text{pinch}}$
  - Smallest nRMP pulse did not produce sufficient distortion to analyze



# Inferred Inward Pinch Scales with Theoretical Predictions



- Theoretical consideration of low-k turbulence drive of momentum pinch

$$V_{\text{Peeters}} = \chi_{\phi} / R \text{ } [-4 - R/L_n]$$

(Coriolis drift)

Peeters et al. PRL (2007)

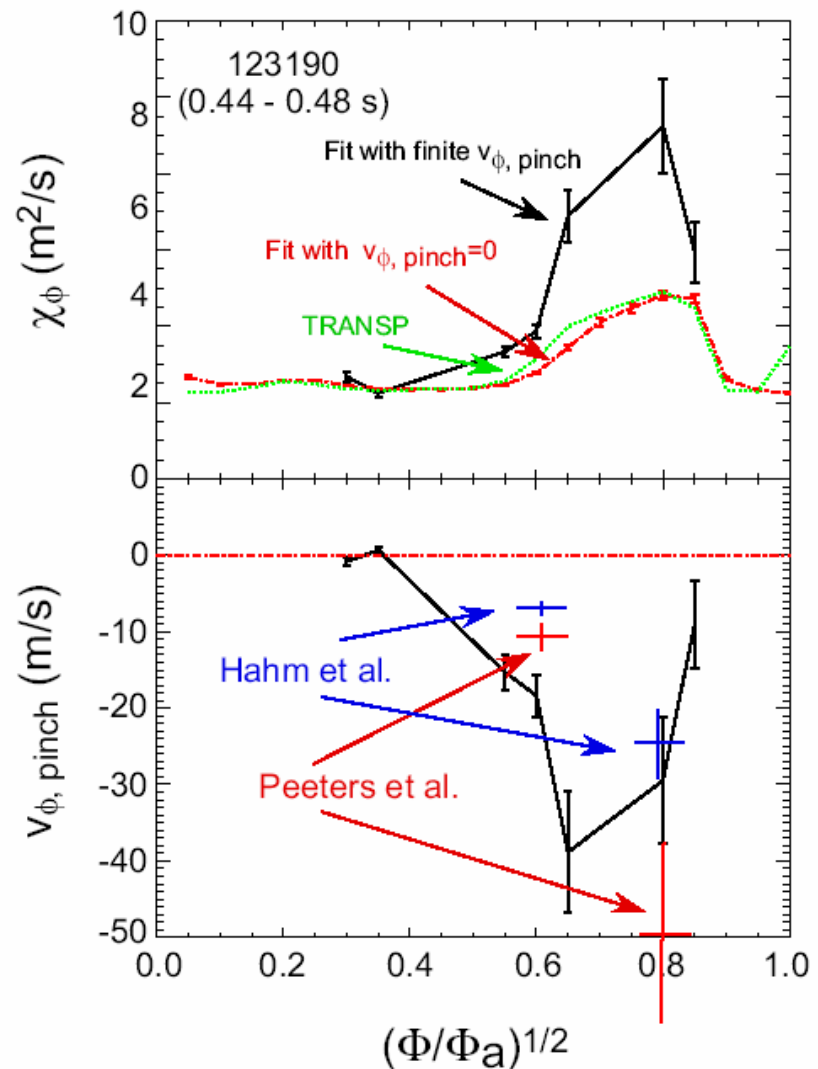
$$V_{\text{Hahm}} = \chi_{\phi} / R \text{ } [-3]$$

( $\nabla B$ , curvature drifts)

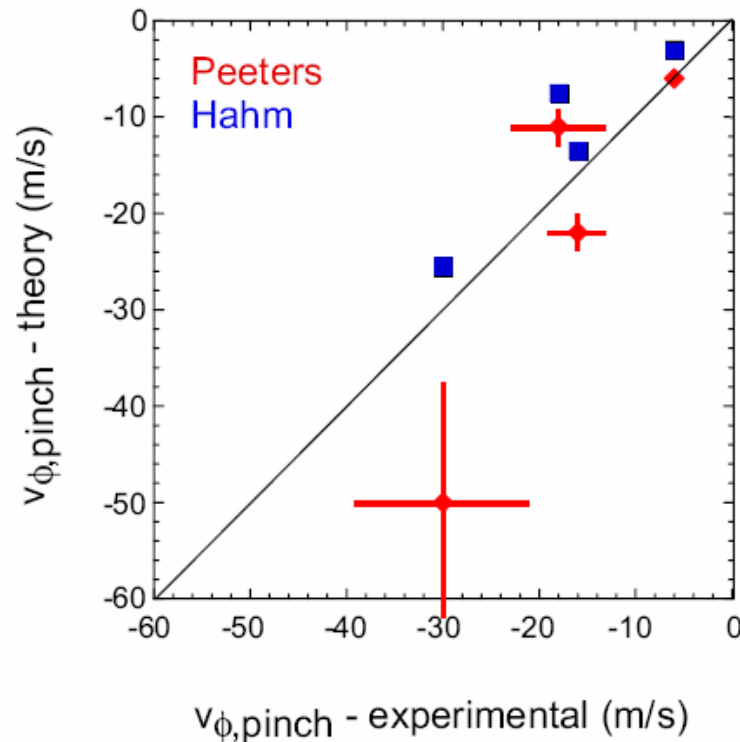
Hahm et al. PoP (2006)

- Effect of off-diagonal terms ( $\propto \nabla T_e$ ,  $\nabla n_e$ )?
- $\chi_{\phi}^{\text{ss}} < \chi_{\phi}^{\text{pert}}$  with pinch

- Important to consider when comparing  $\chi_{\phi}$  to  $\chi_i$



# Reasonably Good Agreement Between Theory and Experiment in Limited Comparison

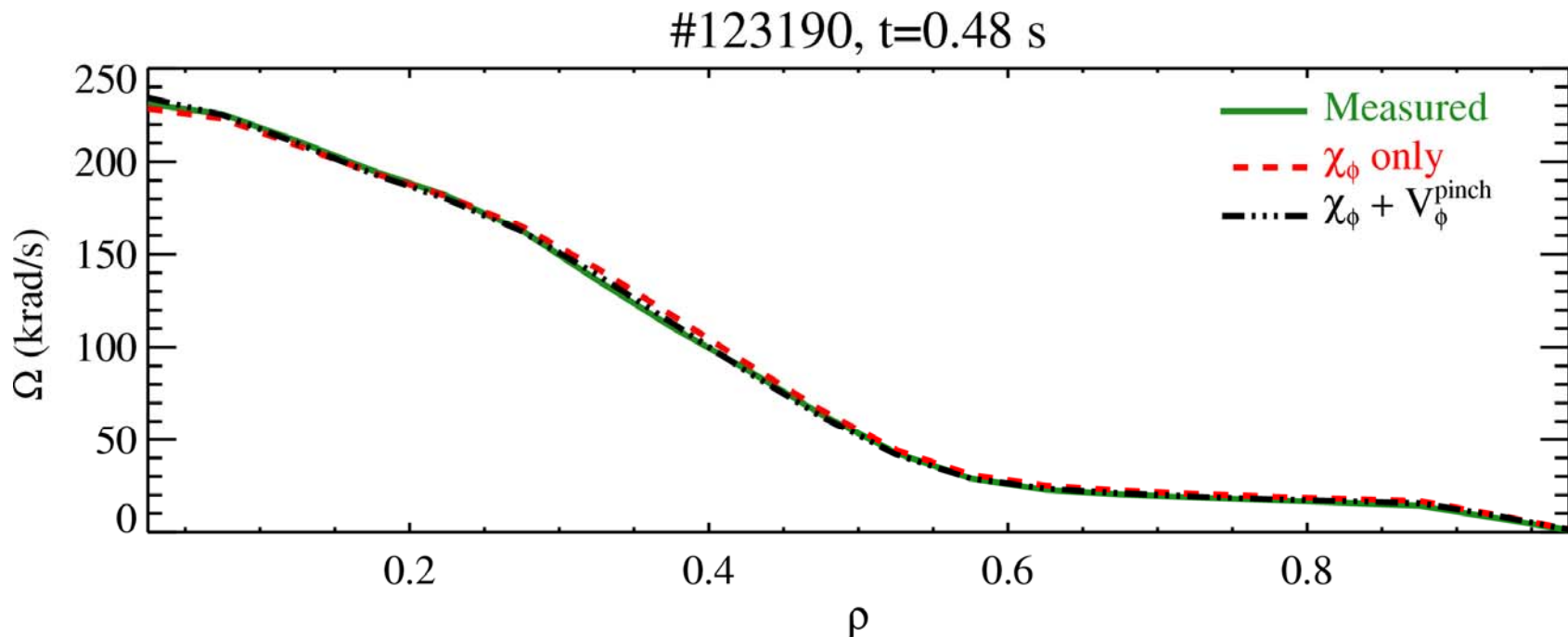


*Can comparisons with large variations in  $L_n$  be used to discriminate between theories?*

# Is a Momentum Pinch Really Needed to Describe Rotation Evolution?



- Perform predictive TRANSP run specifying momentum transport to look at expected rotation evolution
  - Compare  $\chi_\phi$  only with  $\chi_\phi + V_\phi^{\text{pinch}}$
- Over relatively short evolution time, cannot distinguish rotation profiles from measurement



# Summary



- n=3 non-resonant magnetic braking successfully used for perturbative momentum transport studies
- Perturbative momentum confinement time several times greater than energy confinement time
  - Avoids issues of intrinsic rotation
- Braking caused adequate distortion to rotation profile
  - Enabling separation of  $\chi_\phi$  and  $V_\phi^{\text{pinch}}$
- Momentum flux suggests significant inward pinch
  - Comparable to theoretical predictions
- Rotation evolution period too short to definitively illustrate need for pinch
  - Repetitive perturbations + Fourier analysis probably needed to improve this