

# Comparison of Measurements and Modeling of Beam Ion Loss During TAE Avalanches in NSTX

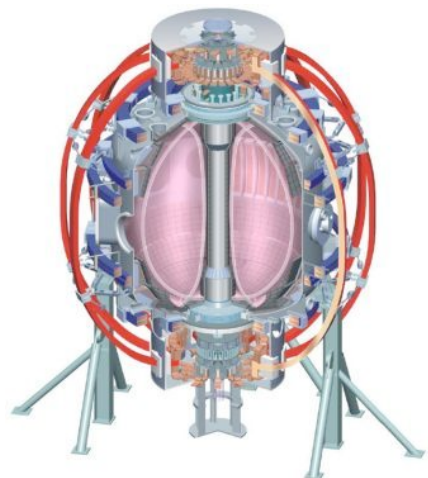
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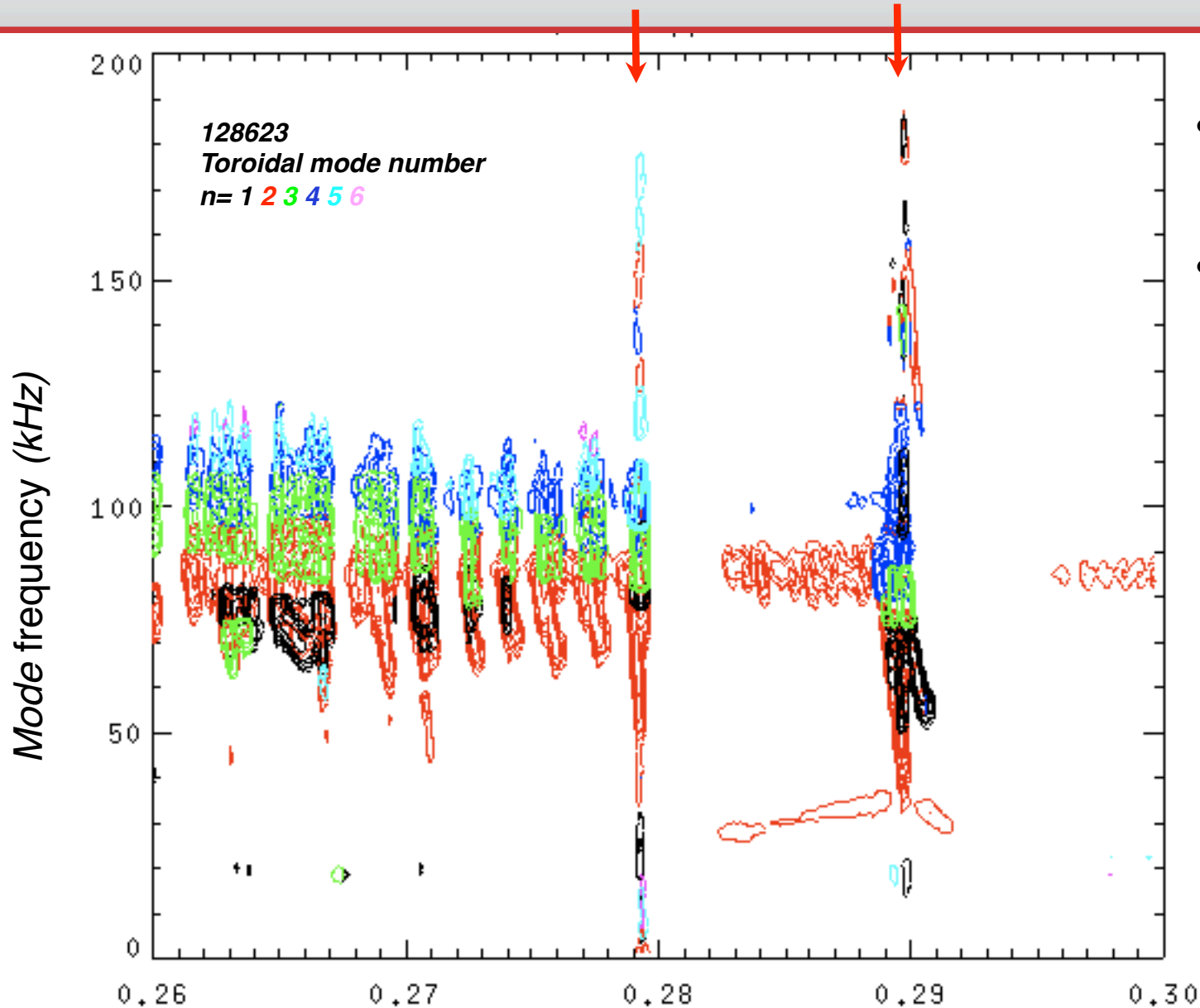


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## TAEs and avalanches

- Toroidal Alfvén eigenmodes (TAEs) are weakly damped Alfvén waves in a toroidal plasma, often driven by ions whose velocity approaches the Alfvén velocity (or a fraction thereof)
- A TAE is characterized by a toroidal mode number,  $n$ , and may occur steadily or intermittently
- A burst in which several TAEs of differing  $n$  occur is termed an avalanche
- Avalanches produce **drops in the neutron rate** and losses of beam ions are sometimes observed concurrent with an avalanche

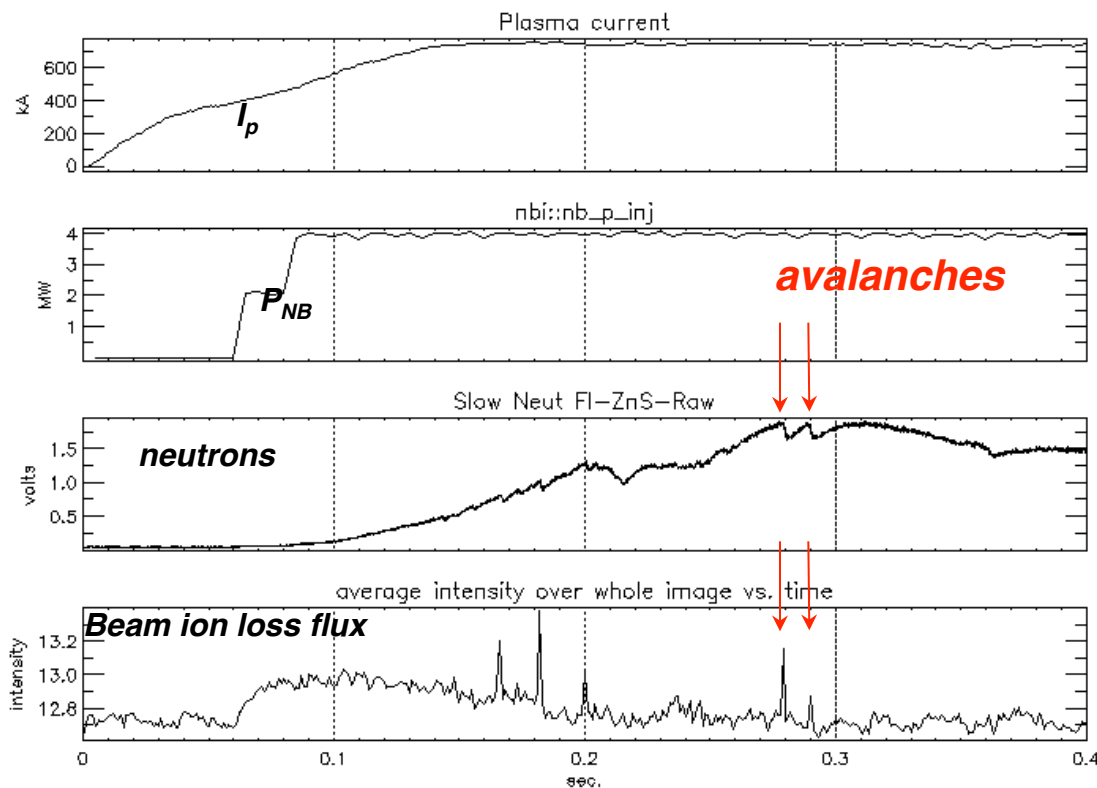
# Typical avalanche in NSTX shows multiple n on Mirnovs



- TAEs appear as burst
- Beam ion redistribution stabilizes modes for a time

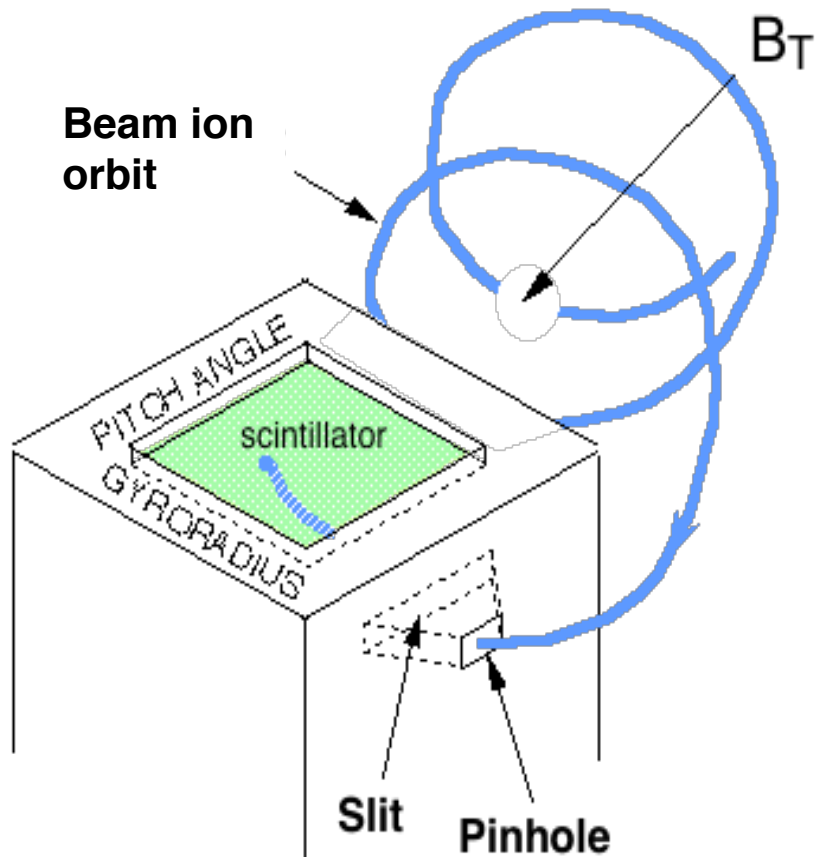
# Avalanches can cause drop in neutron rate and sometimes burst of loss

Shots:  
128623



- But, loss is not observed with every avalanche
- Pitch angle distributions of loss during avalanches sometimes differ

# Any avalanche induced beam ion loss is measured with scintillator probe



Scintillator probe:

Combination of aperture geometry &  $\mathbf{B}$  acts as magnetic spectrometer

Fast video camera captures luminosity pattern on scintillator as function of time

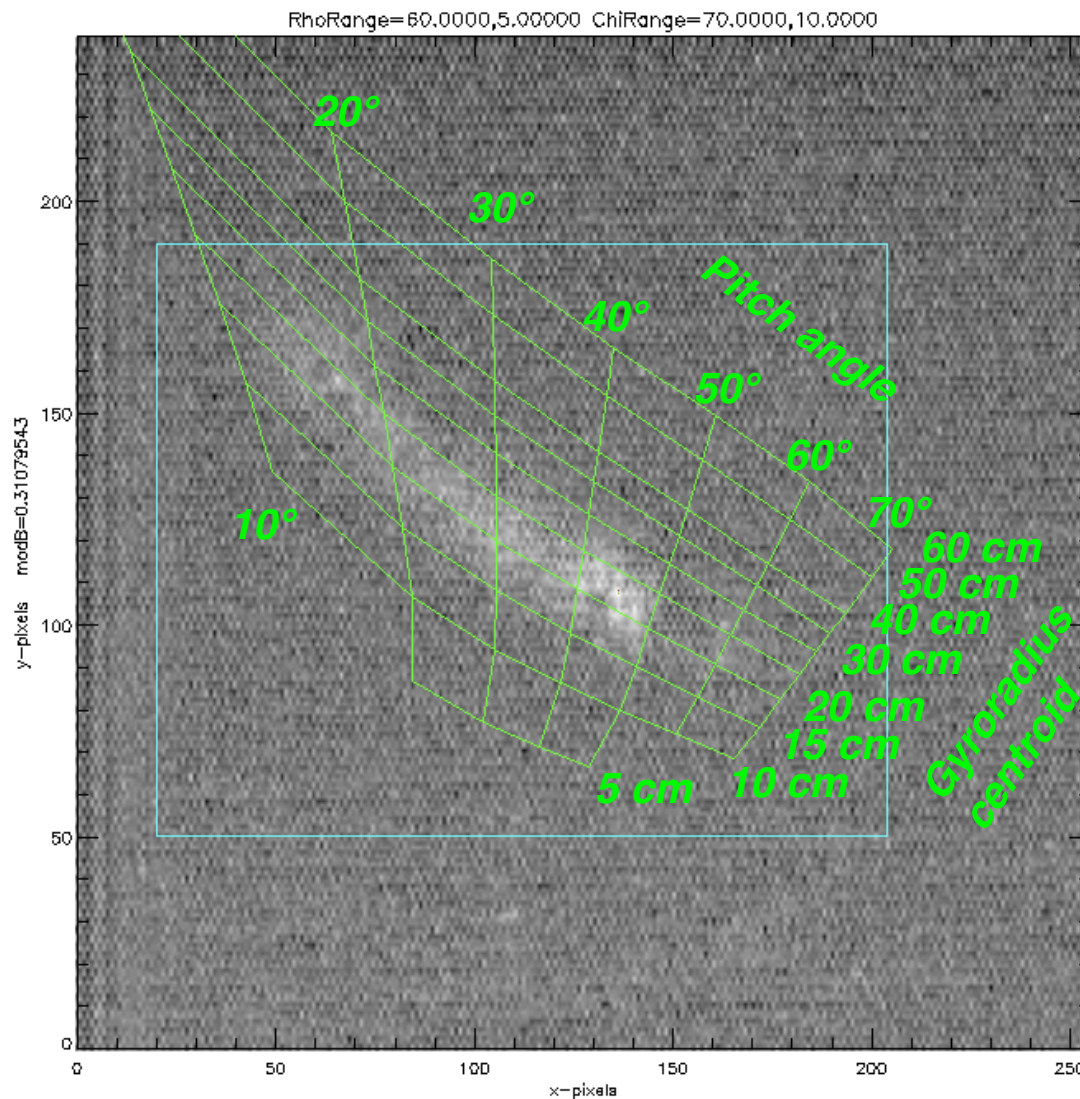
$$\Gamma_{\text{loss}}(\rho, \chi, t)$$

NSTX probe:

$$5 \text{ cm} \leq \rho \leq 60 \text{ cm}$$

$$15^\circ \leq \chi \leq 80^\circ$$

# Avalanche induced loss often occurs over a wide range of pitch angles



128623, 290 ms

- Interpreted as beam ion phase space being stochastized by multiple modes

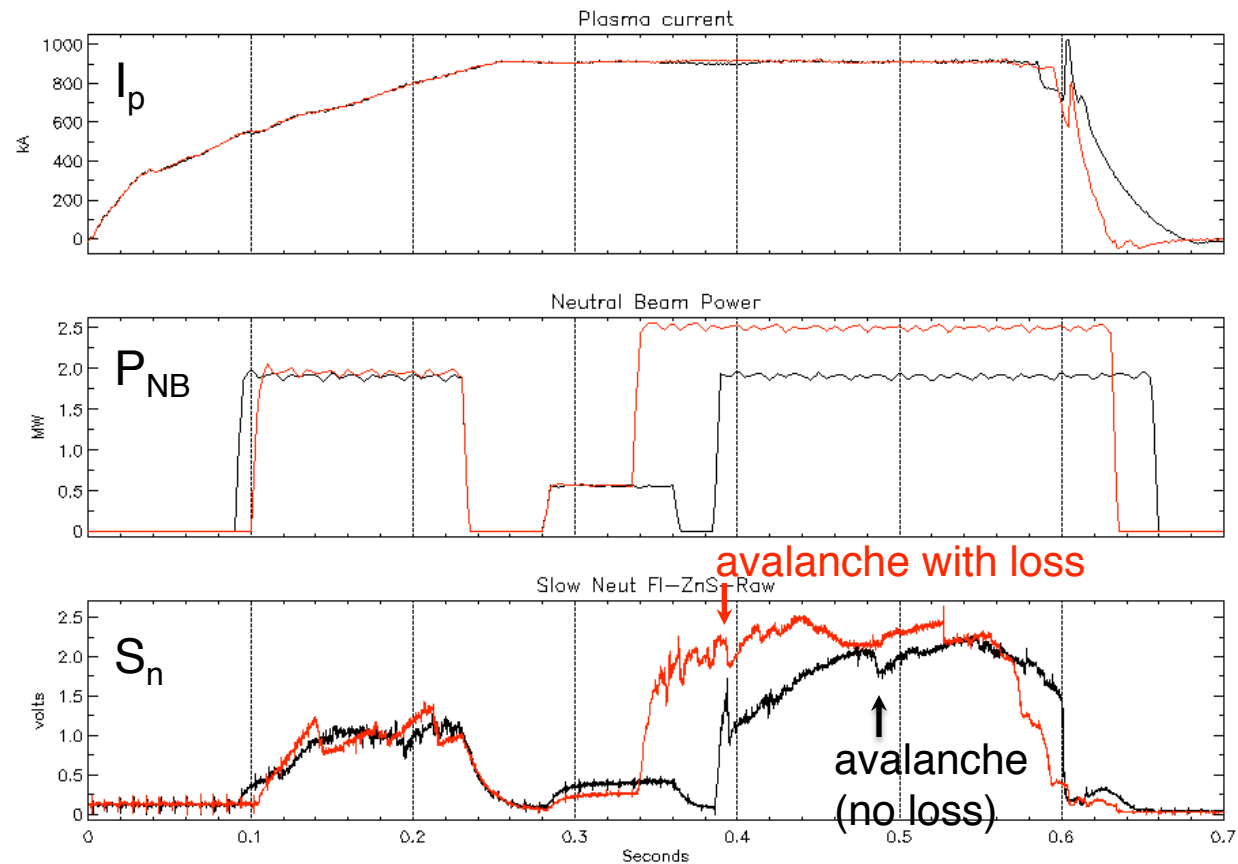


## Goal: compare measured and modeled lost ion pitch angle distributions

- Measured distribution recorded by scintillator probe
- Loss distribution modeled by guiding center orbit code that incorporates:
  - Measured TAE n numbers, frequencies (Mirnov coils)
  - Radial mode structures and amplitudes (multichannel microwave reflectometer data coupled to NOVA-K calculations of eigenmodes)
  - Deposited beam ion distribution function from TRANSP
  - Focus on recently deposited beam ions since losses appear at or very close to injection energy of 90 keV

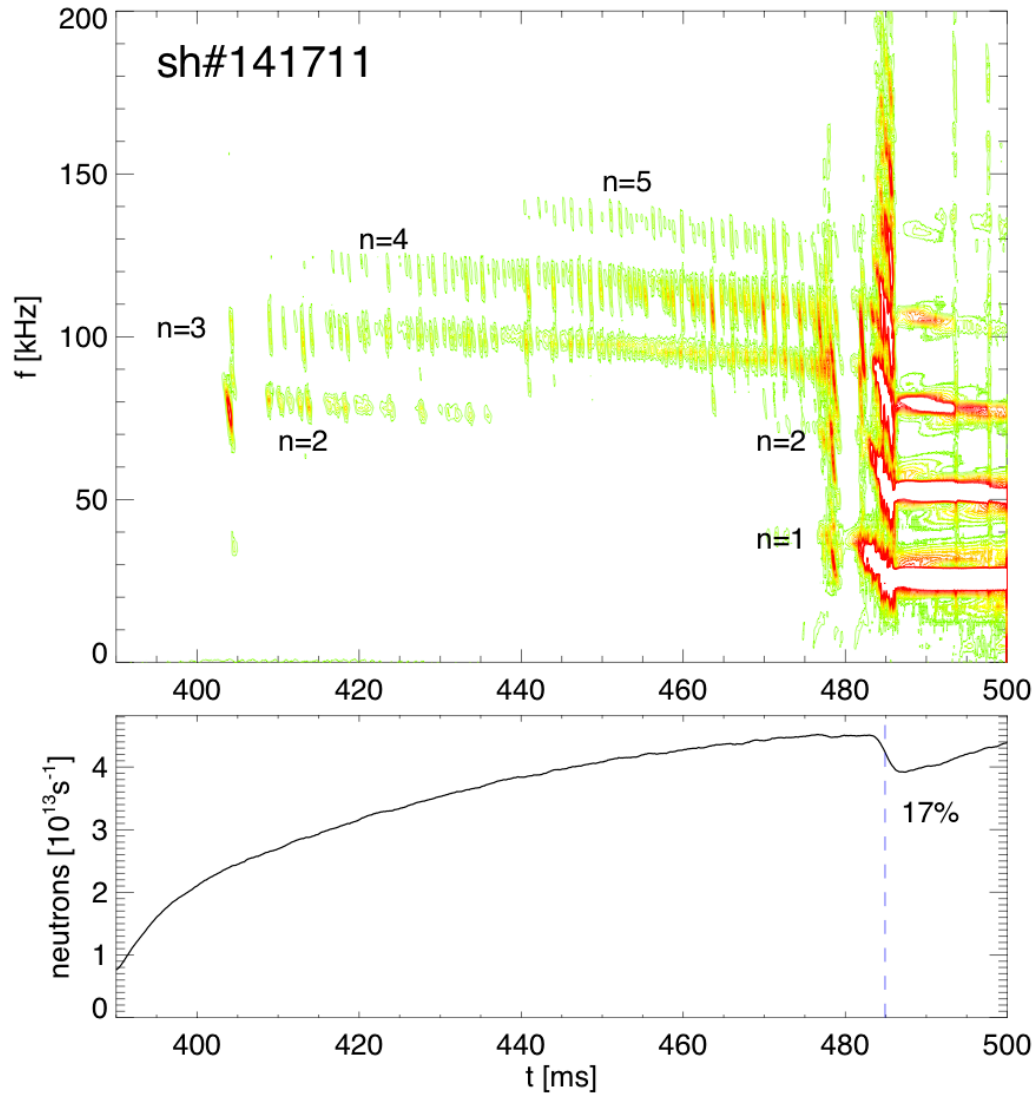
# Compare cases with and without losses to draw inferences about conditions when fast ions may be lost

Shots:  
141711  
141719



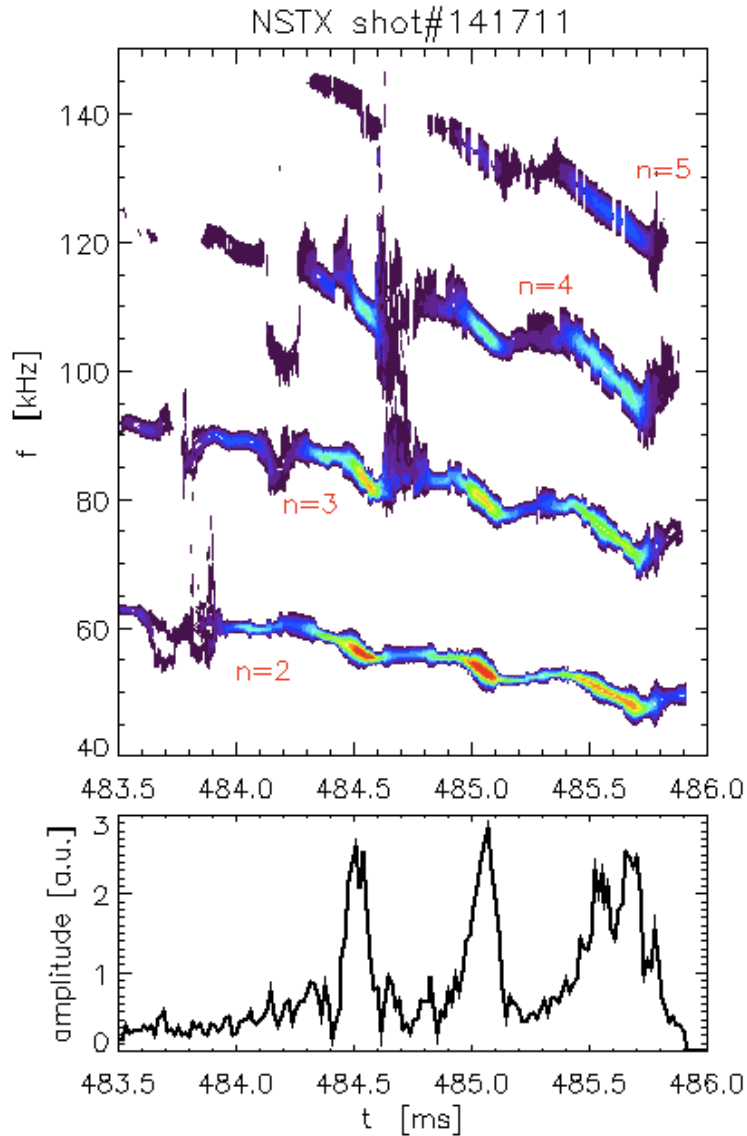


## Example avalanche with no loss observed



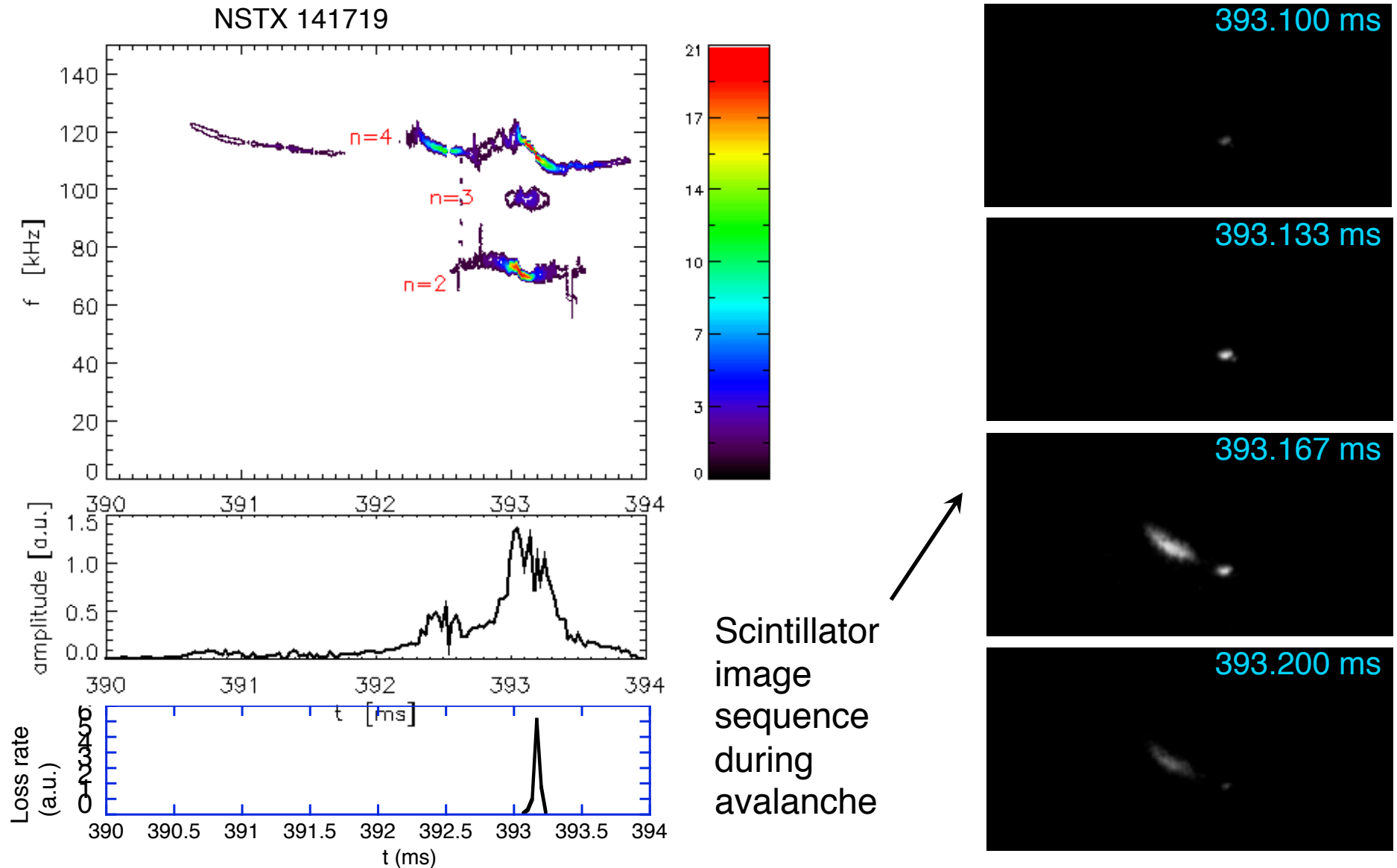
- $n=2-5$  present, but no loss evident on scintillator probe
- Neutron rate drops 17%
- Single beam injecting at 90 kV

## Case of no observed losses

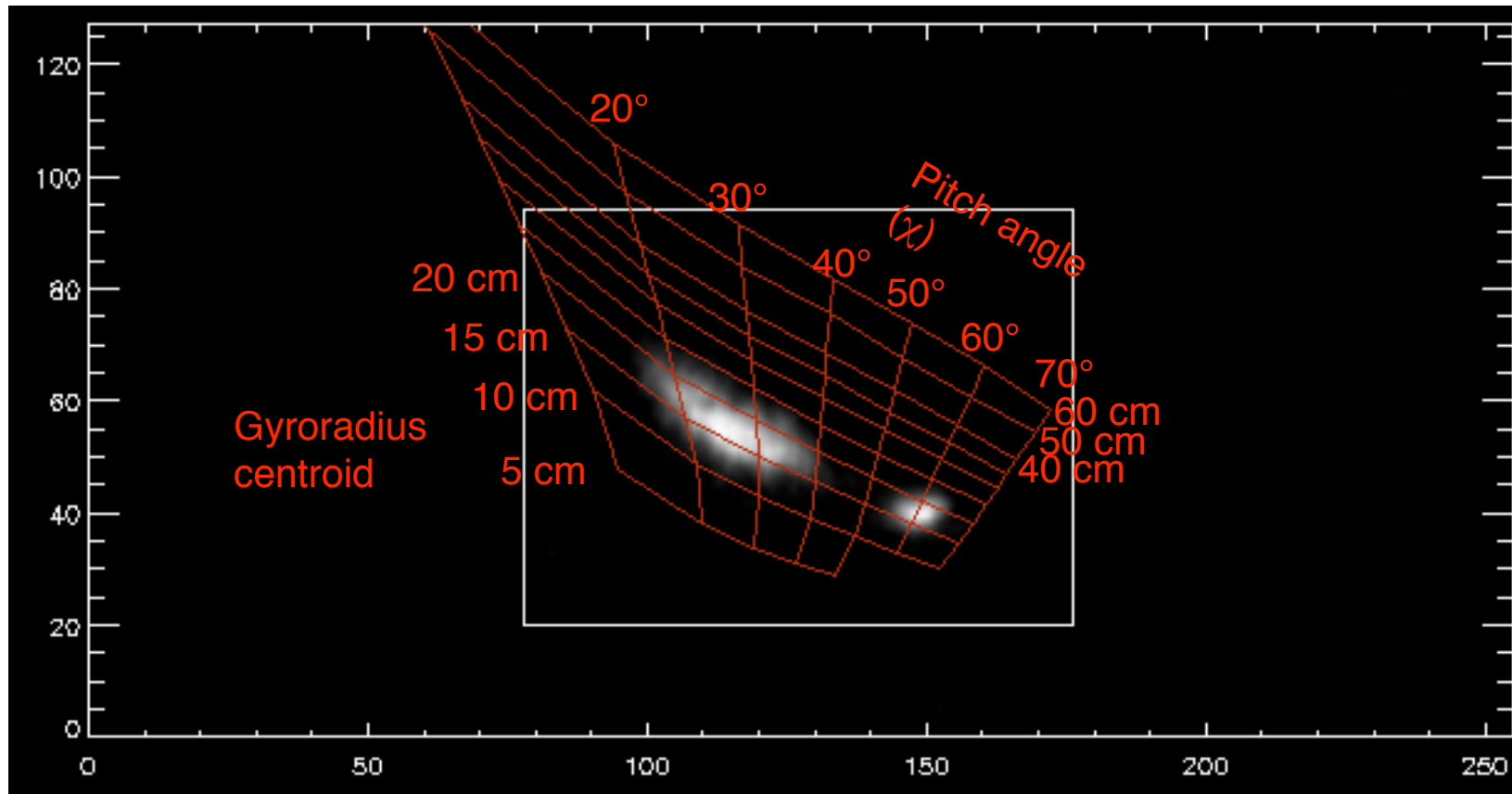


- $n=2-5$  concurrently present in 3 rapid bursts
- Neutron rate drops by 17%, yet no lost beam ions seen by detector
- Could there be loss, but not to detector position?
  - Possible, but see below
- Internal redistribution only?
  - Might occur if modes are more core-localized with small edge amplitudes, but  $\rho_{NB}$  large in NSTX
  - Orbit simulations suggest redistribution does occur

# Avalanche with loss also has multiple $n$ , and loss evolves rapidly during event



## 60° pitch angle loss appears first, then range of lower pitch angles

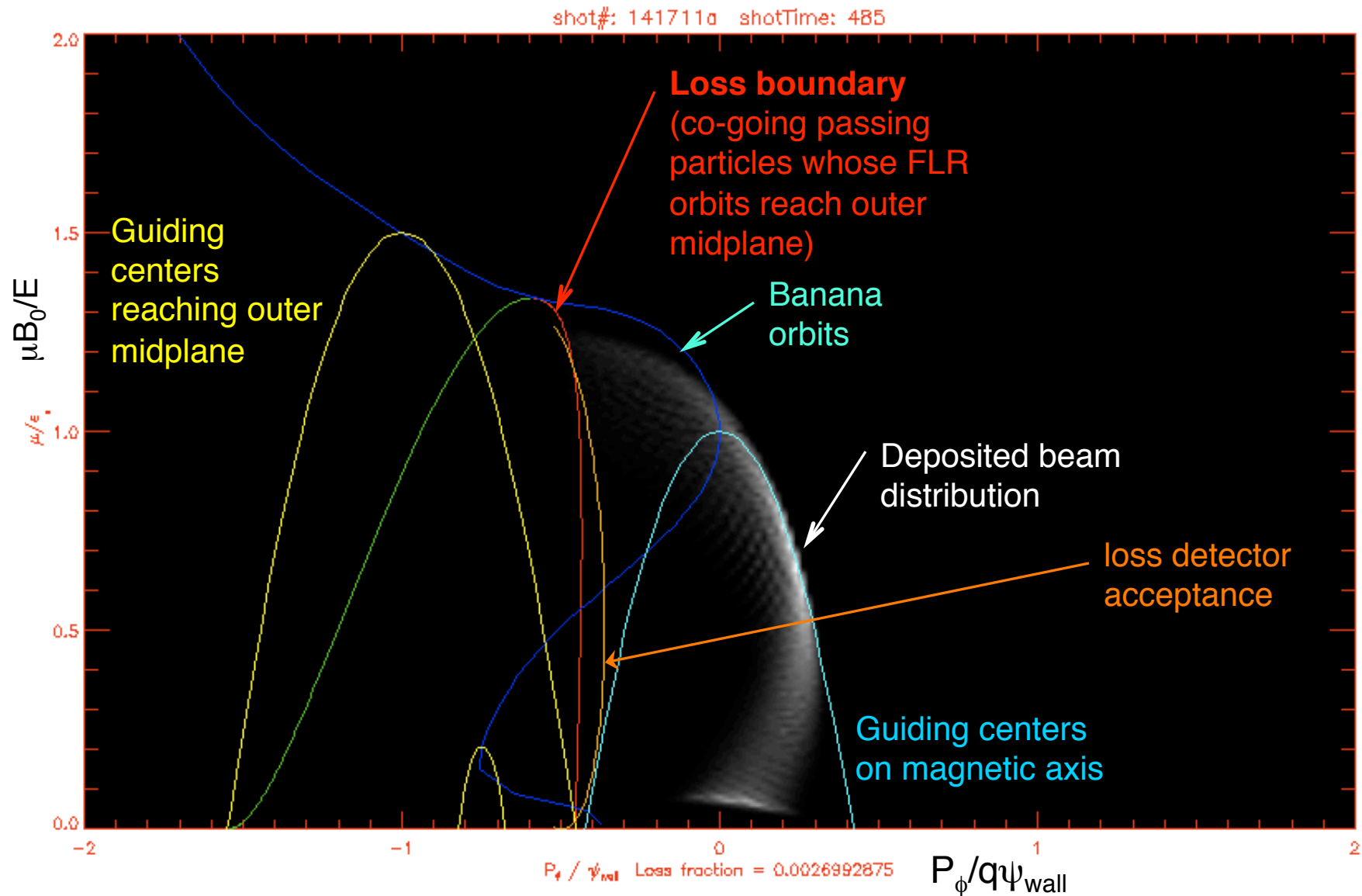


- Rapid appearance of wide pitch angle spot (18°–40°) in 33  $\mu\text{s}$  ( $\leq 10$  toroidal transits) indicates transport of fast ions is very strong during avalanche

## Beam ion orbits can be completely characterized by 3 constants of the motion

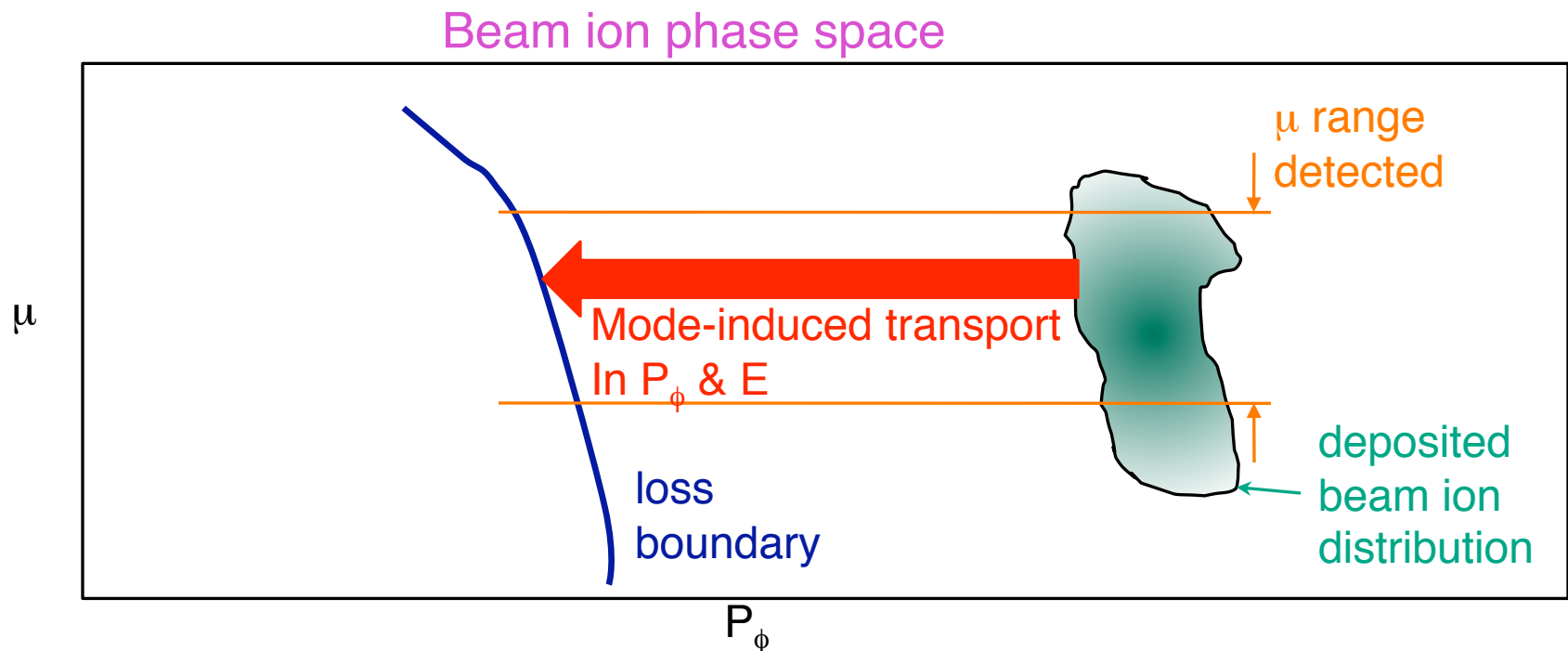
- $E = \frac{1}{2} mv^2$  (kinetic energy)
  - Conserved on time scales short compared to collisional slowing down time; also roughly conserved in avalanche losses as these ions lost at injection energy
- $\mu = \frac{1}{2} mv_{\text{perp}}^2/B$  (magnetic moment)
  - Conserved in the absence of fields varying near the particle's cyclotron frequency or field gradients shorter than length  $\rho_i$
- $P_\phi = mv_\phi R + q\psi_{\text{pol}}$  (canonical angular momentum) (a.k.a.  $P_\xi$ )
  - Conserved in axisymmetry (i.e. in absence of nonaxisymmetric MHD or error field correction coil fields)
- Conservation conditions usually satisfied in NSTX
- Knowledge of these 3 parameters **fully determines orbit** (except toroidal position,  $\phi$ , and gyromotion, which are not used in this work)
- This approach equivalent to guiding center orbit following

# Deposited full energy beam distribution can be represented in $(\mu, P_\phi)$ space, along with certain phase space boundaries



## Phase space model also helps understand MHD loss

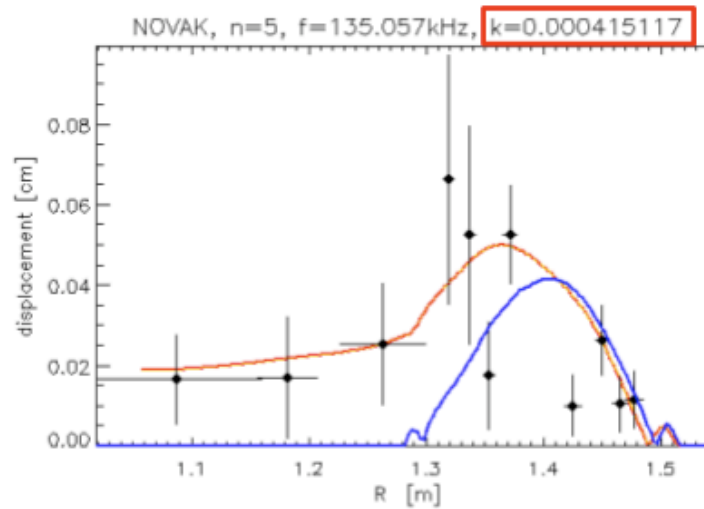
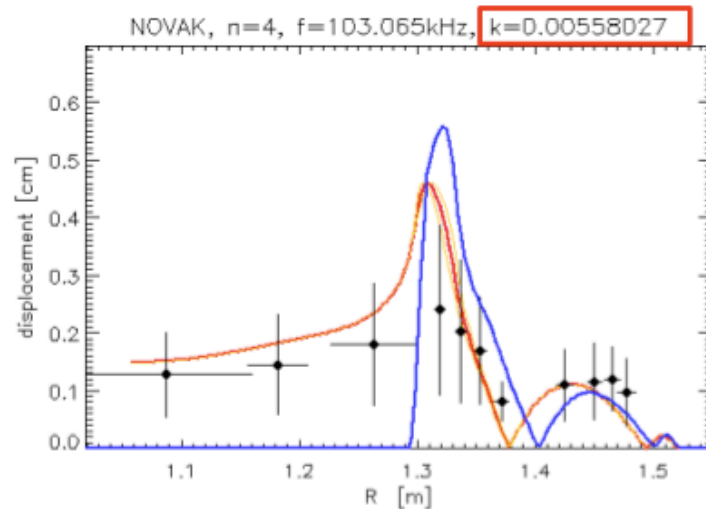
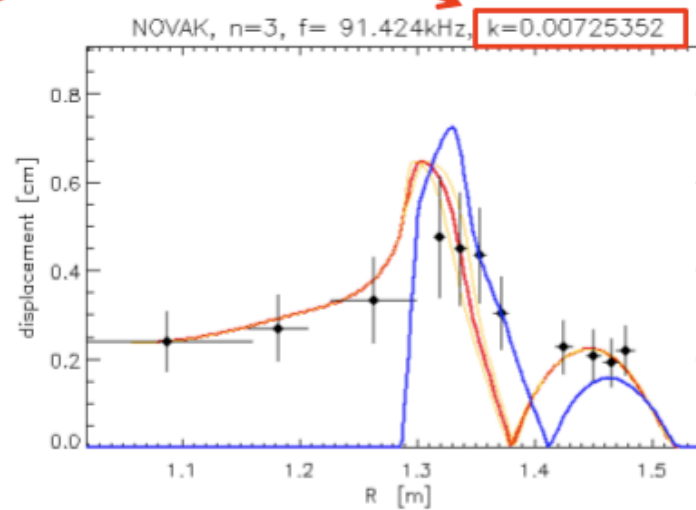
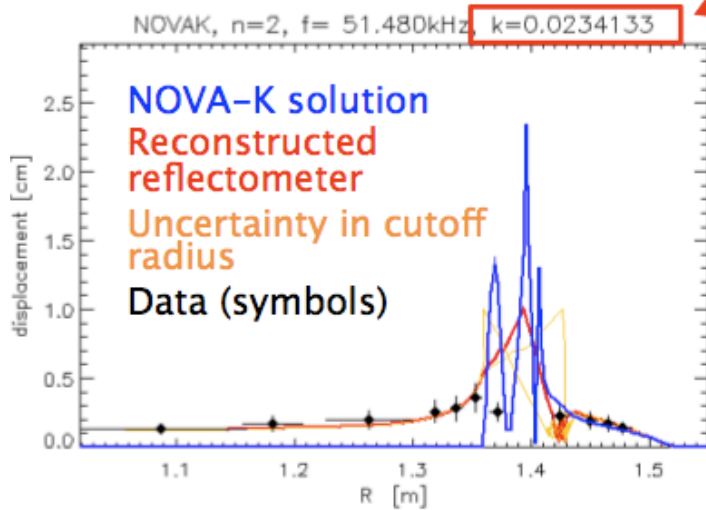
- Observed MHD frequencies  $\ll \Omega_{ci}$ , so  $\mu$  will be conserved
- Mode destroys toroidal symmetry, so  $P_\phi$  no longer constant
- A single  $n$  mode moves particles along a line  $nE - \omega P_\phi = \text{const}$  in diffusive fashion, at fixed  $\mu$
- Multiple  $n$  in avalanche can cause broader transport





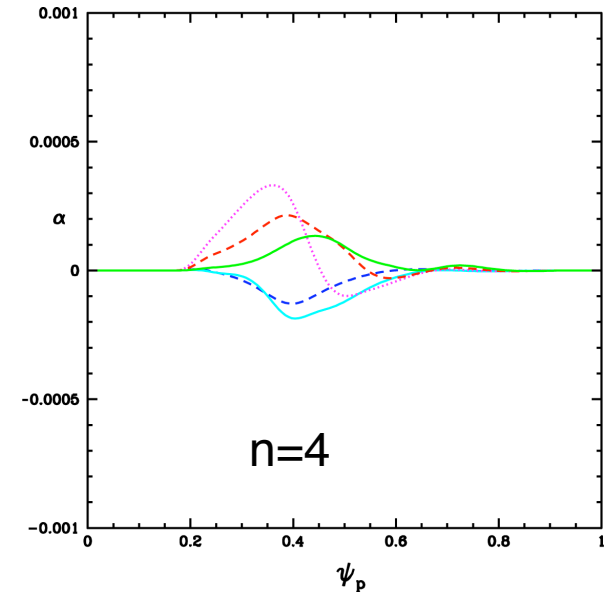
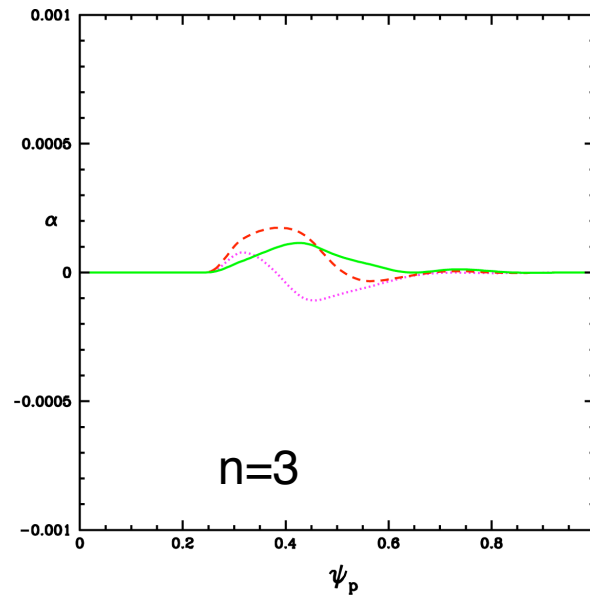
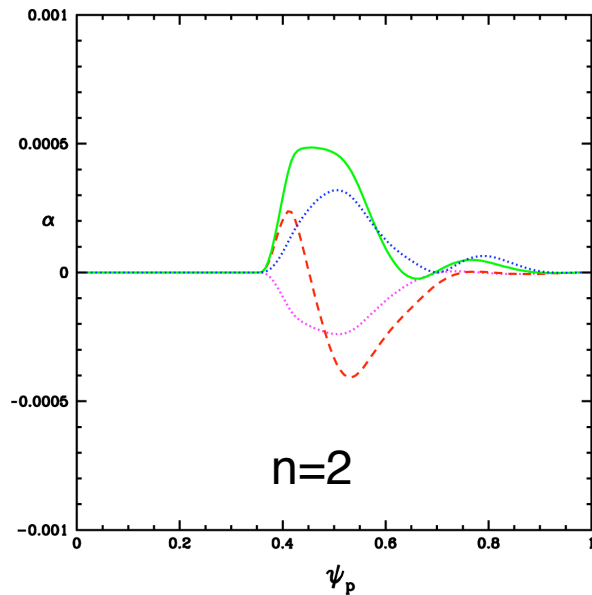
# NOVA-K TAE radial eigenfunctions can be fit to reflectometer fluctuation profiles of principal modes

scaling factor



- Displacement can be matched, giving absolute amplitudes of various  $n$  modes for input into orbit following code

## In this avalanche, n=2 has largest amplitude

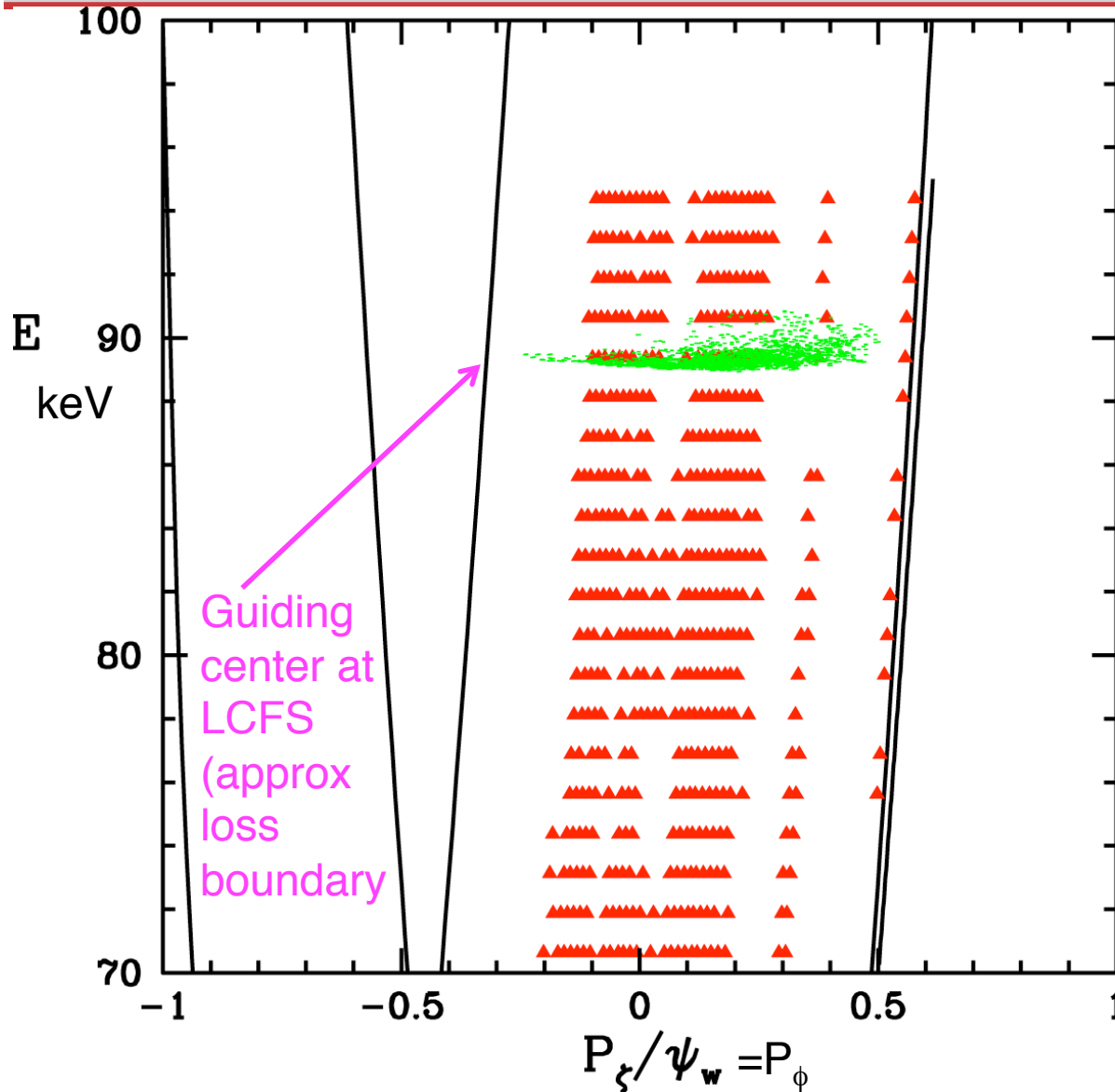


- $n=2$  also has the largest amplitude near edge, likely contributing to NBI loss

## Mode structures and amplitudes can be used to determine regions of phase space subject to stochasticity

- Use guiding center code ORBIT to follow nearby pairs of ions for a number of toroidal transits
- If vector between particles in action/angle space rotates by more than  $\pi$ , then that region of phase space is stochastic
- Repeat process for many particle pairs, spanning phase space, and shade volumes of phase space in plot to designate stochastic domains
- Since losses are near injection energy, overlay full energy beam particle deposition on stochastic region map to ascertain which particles may be lost via this channel

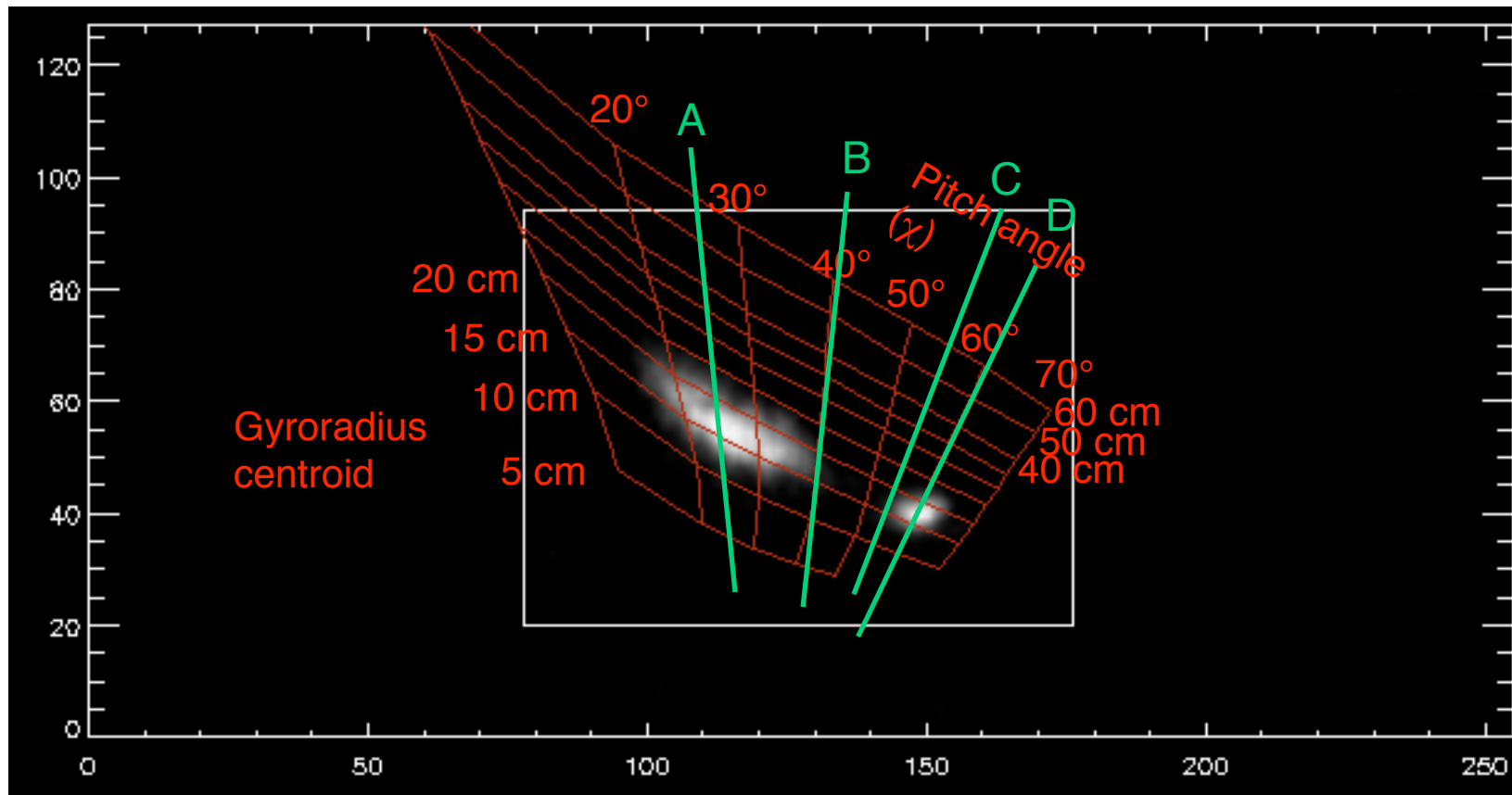
## Example plot of stochastic domains at fixed $\mu$



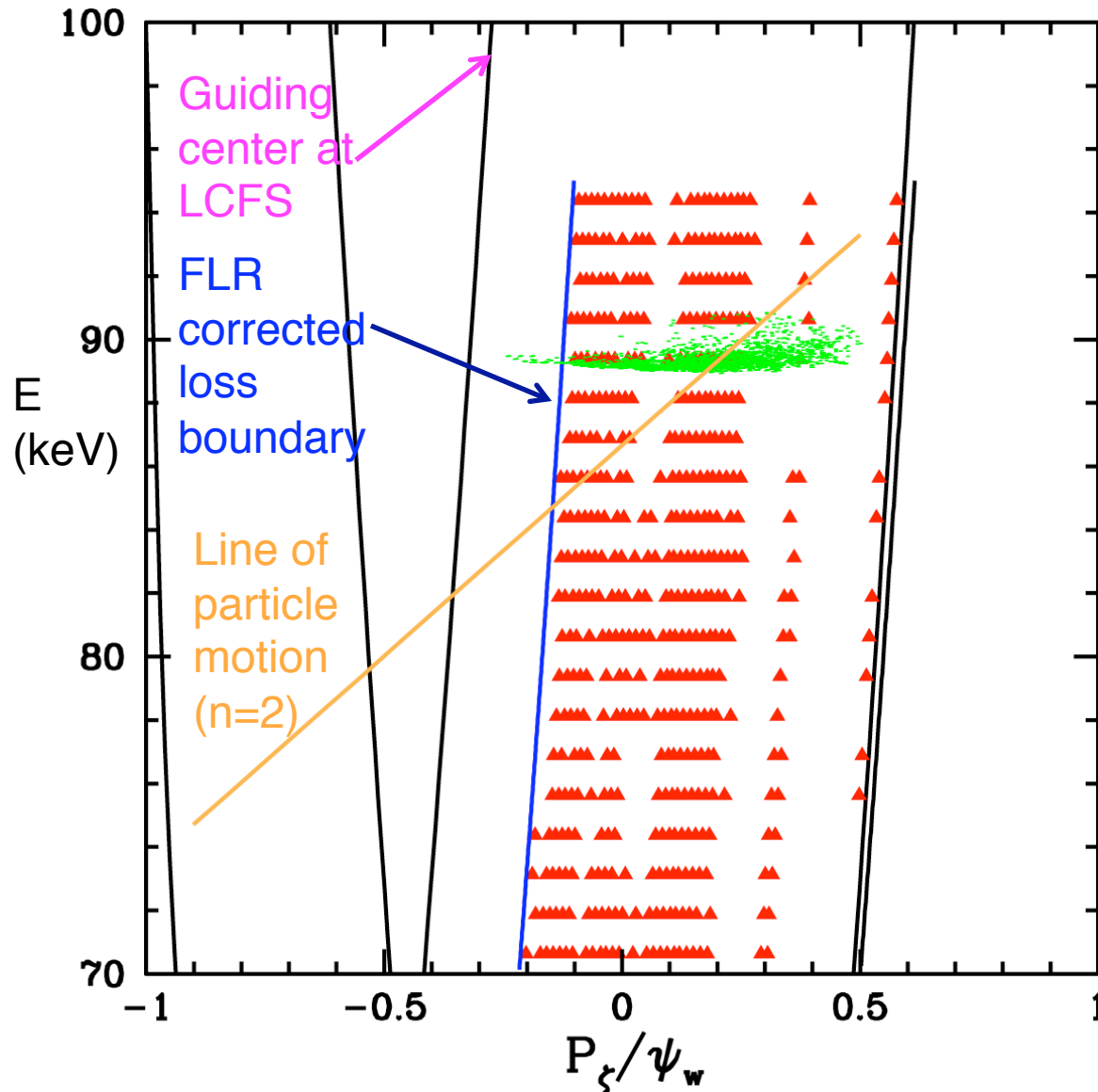
- Evaluate stochastic condition on grid in  $(E, P_\phi)$  plane
- Red triangles mark stochastic locations
- White space extending in  $P_\phi$  direction indicates good surfaces in phase space with no stochasticity
- Green points: TRANSP deposited beam ions

## Test whether code-modeled stochastic domain presence coincides with lost pitch angle ranges

- Stochastic maps shown on following slides for 4 pitch angles marked (4  $\mu$  values)

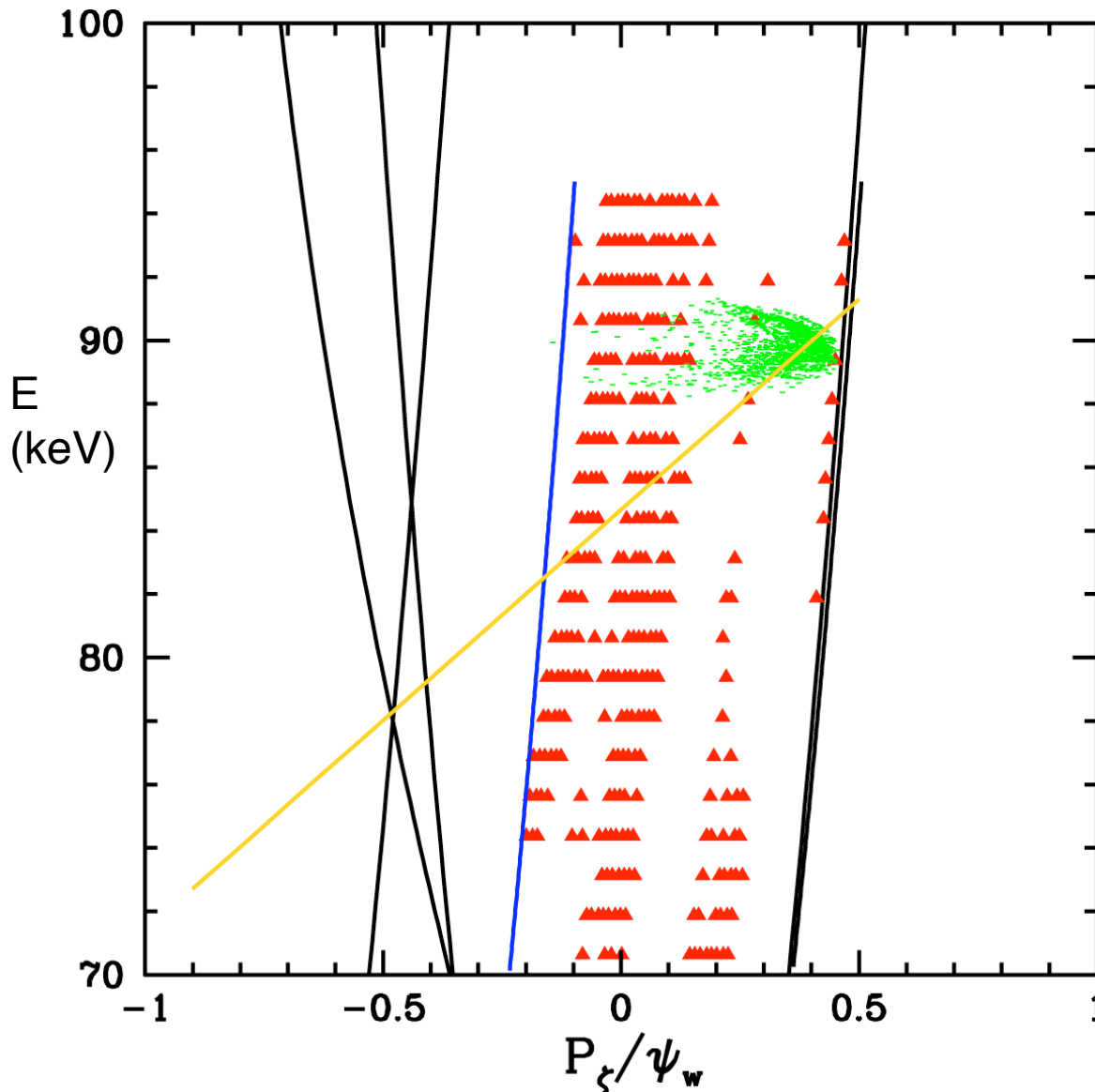


## Case A (25°) is center of a detected loss spot & model predicts loss



- Beam ions deposited in stochastic region
- Particles move along orange line (or parallel lines) under influence of  $n=2$  mode
- Particles clearly deposited in stochastic region and that region extends to loss boundary

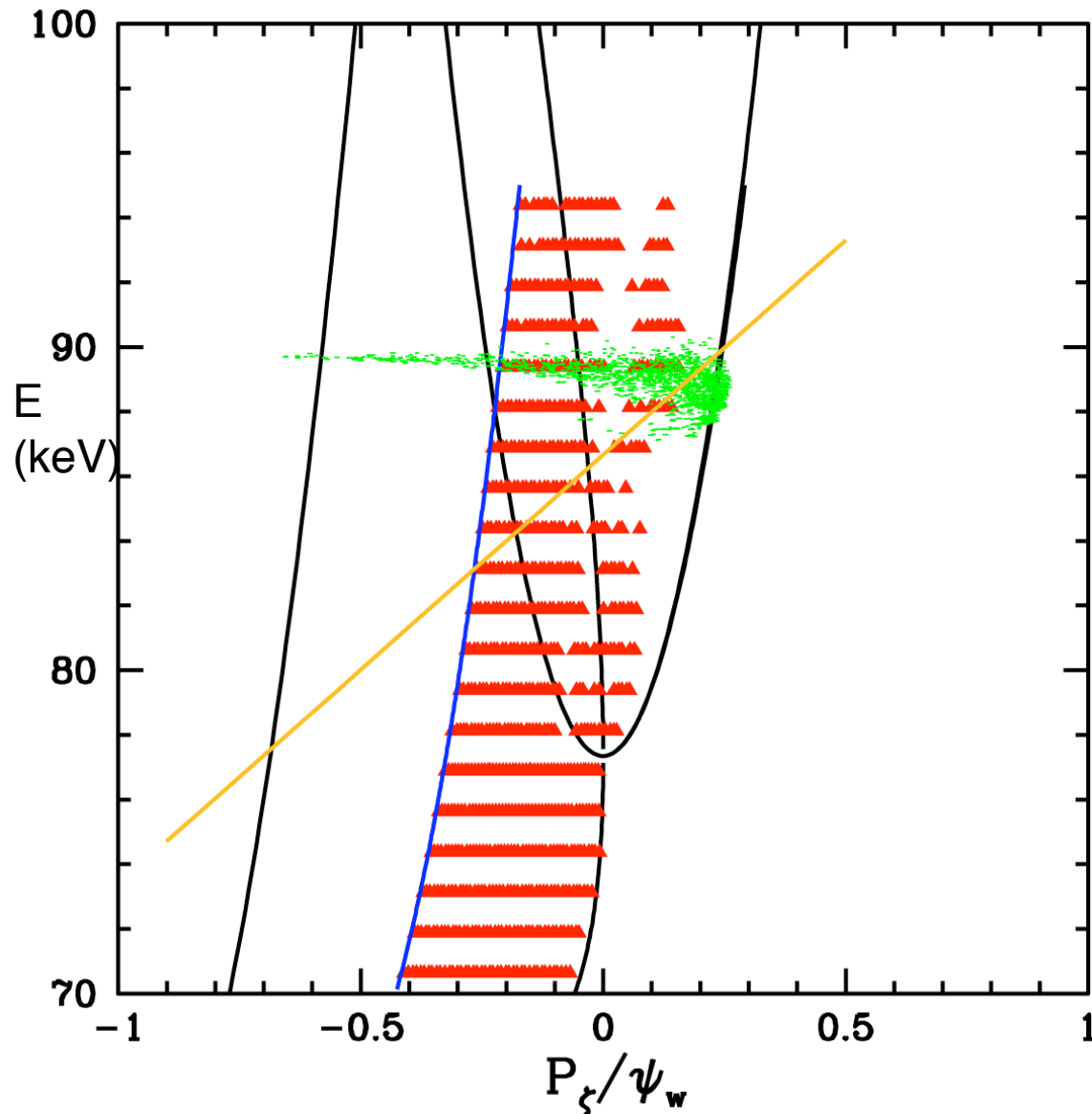
## Case B (40°) is at boundary of no-loss region & model shows deposition only on good surfaces



- Deposition in a region of good surfaces in phase space means beam ions have no chance to be transported to loss boundary, even though stochasticity exists at other locations
- Agrees with transition to no-loss pitch angle range

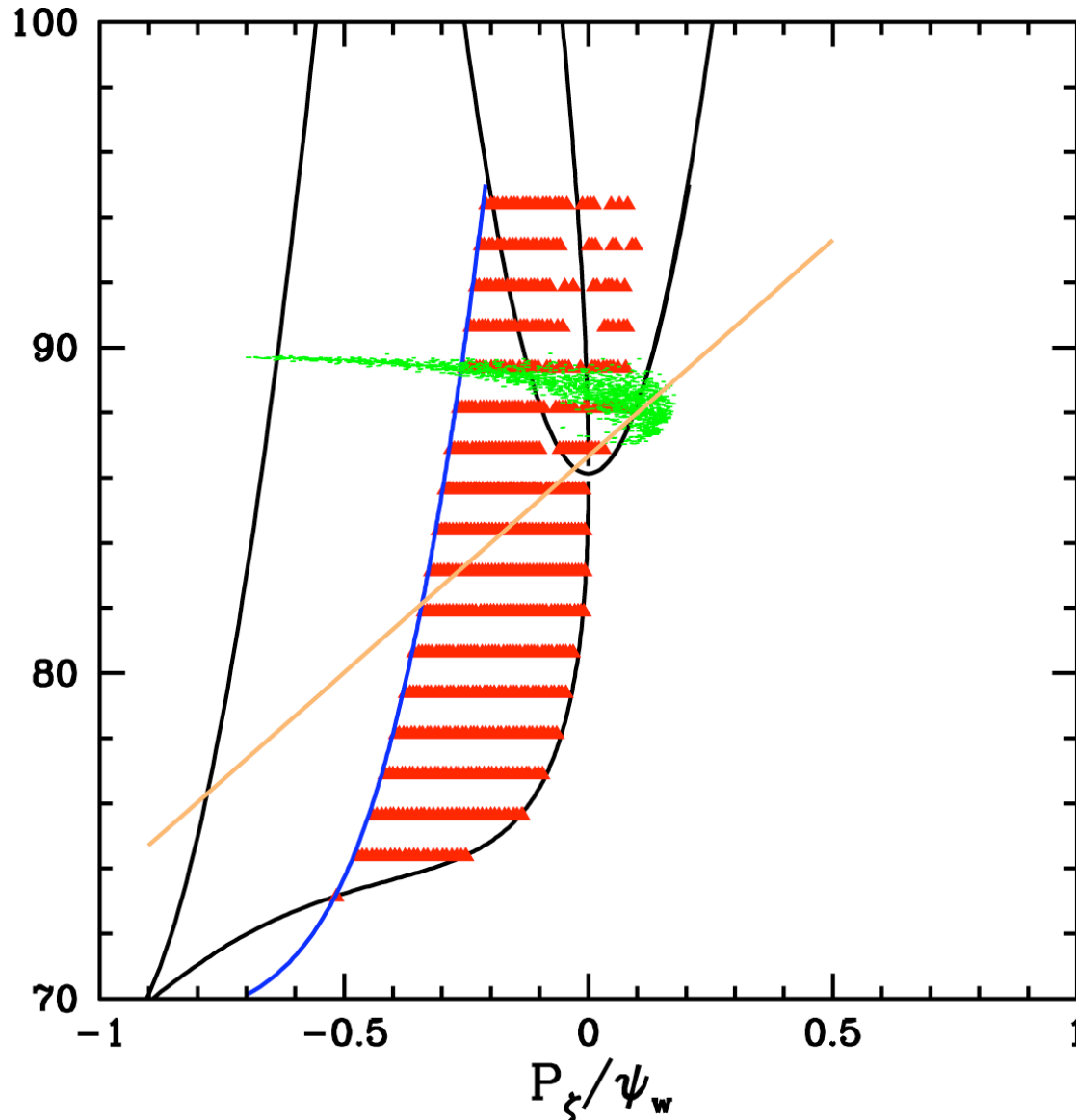


## Case C (55°) is at boundary of a loss spot; deposition starts to appear in stochastic region again



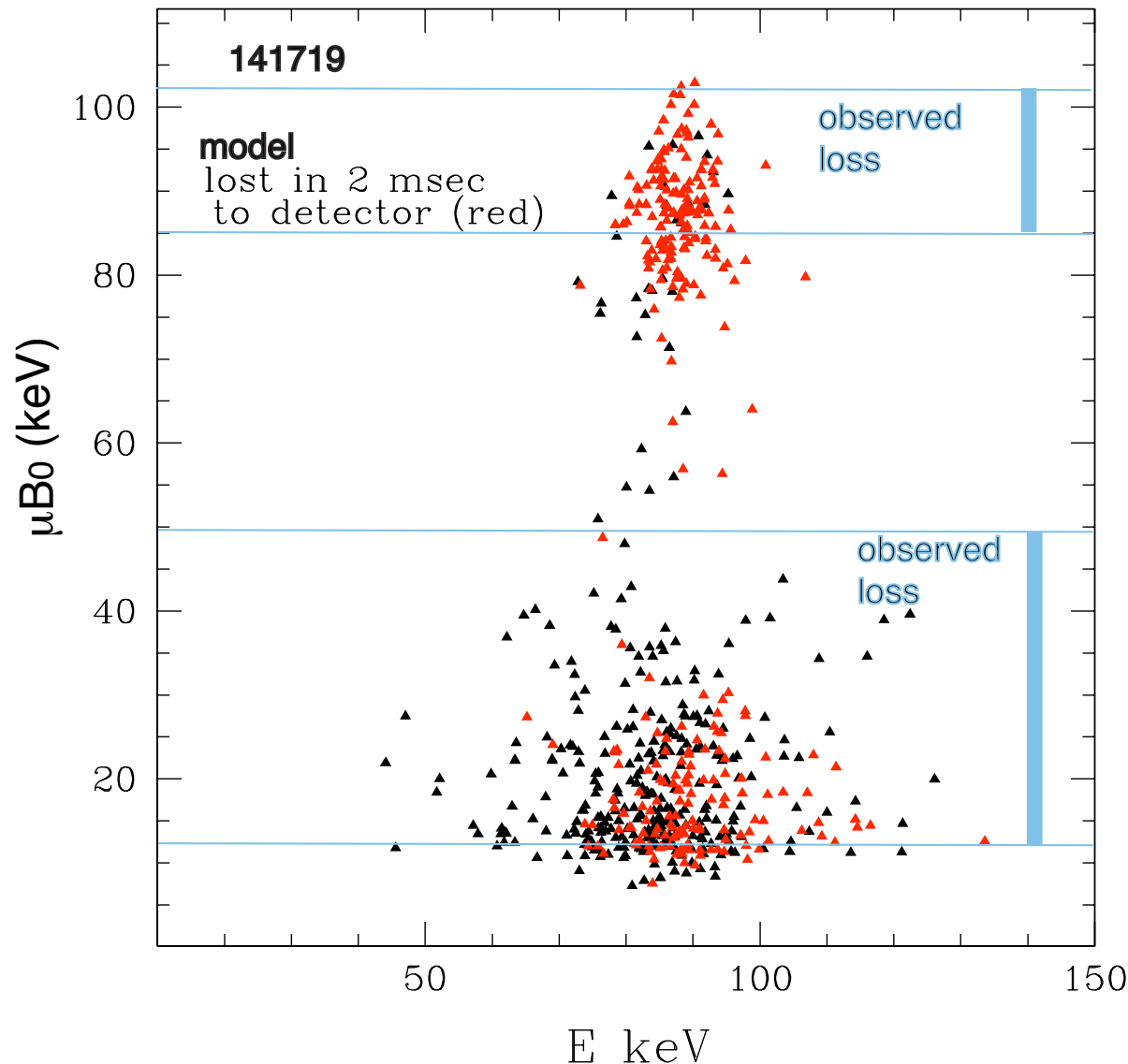
- Apparent good surfaces around  $P_\xi=0$  &  $E > 85$  keV may prevent some of deposited population from reaching loss boundary

## Case D (60°) is in middle of loss spot; deposition squarely in stochastic region again



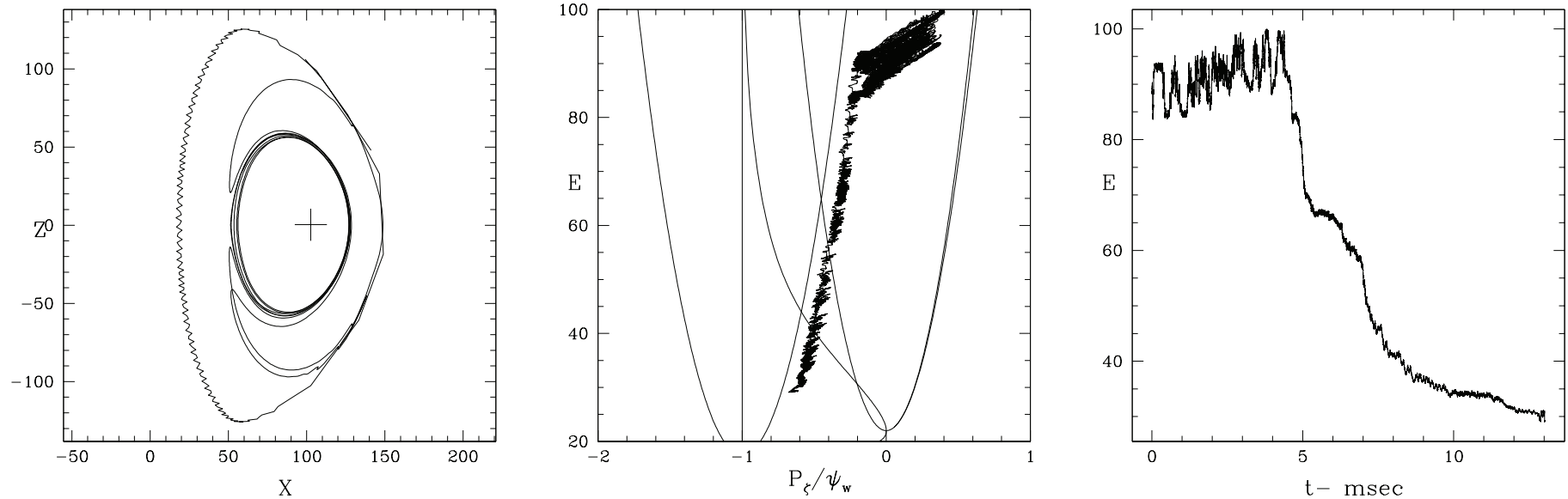
- Note that deposition is in stochastic region and that stochasticity exists along entire line of transport up to loss boundary
- Both conditions required for loss

## Orbit following including mode structure shows bimodal loss distribution in pitch angle, as observed



- Modeled pitch angle boundaries roughly agree with measurement
- Same simulation for no loss case shows no particles reach detector!
- Note also that detector loss (red points) is representative of all losses (black points)

# Modeling reveals some beam ions that remain barely confined while their energy is greatly diminished by modes



- Example is for particle in no loss shot (141711)
- Particle above starts passing, later becomes banana orbit
- Trajectory in  $(E, P_\phi)$  plane skirts loss boundary, but stays confined
- Energy drops from 90 keV to 30 keV before loss
- Neutron reactivity drops rapidly as energy falls below 90 keV
- What features of modes cause this?

## Summary

- TAE avalanches in similar NSTX plasmas sometimes produce observable fast ion loss at wall and sometimes do not
- To pursue differences between loss seen vs unseen, measured TAE amplitudes and structures were put into ORBIT code to compute stochastic orbit domains
- Loss appears at a given pitch angle only if:
  - Beam deposited in stochastic region
  - Stochasticity extends all the way to the loss boundary along the line of transport, with no intervening good surfaces
- Loss distribution at detector in ORBIT model shows 2 groups of lost particles, in agreement with measurement
- Modeling reveals some beam orbits rapidly lose energy in avalanche but remain confined—may explain cases when no loss observed