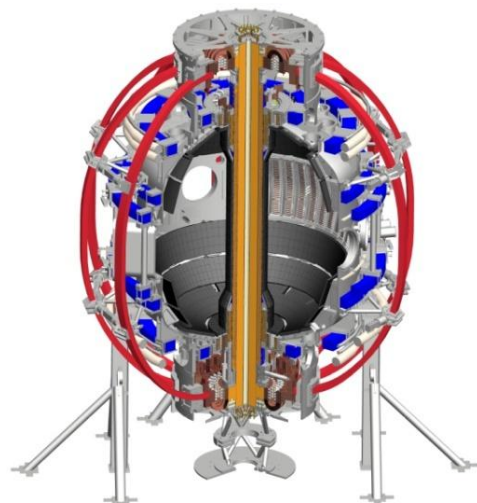


# Survey of microinstability and simulated turbulent transport in NSTX

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# Motivation: Understand mechanism(s) responsible for thermal, momentum, particle transport over broad range of parameters

- Wide range of parameters accessible by spherical tokamaks (ST)
- H-mode ion thermal transport often near neoclassical in STs
- **Observed confinement scaling**  $\Omega\tau_E \sim v_*^{-0.8}$  [Kaye, IAEA 2012 EX/7-1]  
⇒ does it extrapolate to future devices at lower  $v_*$  (NSTX-U, ST-FNSF, ...)?
  
- Considering core thermal gradient micro-instabilities ( $r/a \sim 0.4-0.8$ )
  - Local GYRO simulations based on experimental profiles & equilibrium reconstructions
  
- Although important, not addressing:
  - Pedestal [IAEA 2012: Canik (EX/P7-16), Diallo (EX/P4-04), Kubota (EX/P7-21), Maingi (EX/11-2), Smith (EX/P7-18)]
  - Energetic particle driven instabilities [IAEA 2012: Belova, TH/P6-16; Crocker, EX/P6-2]

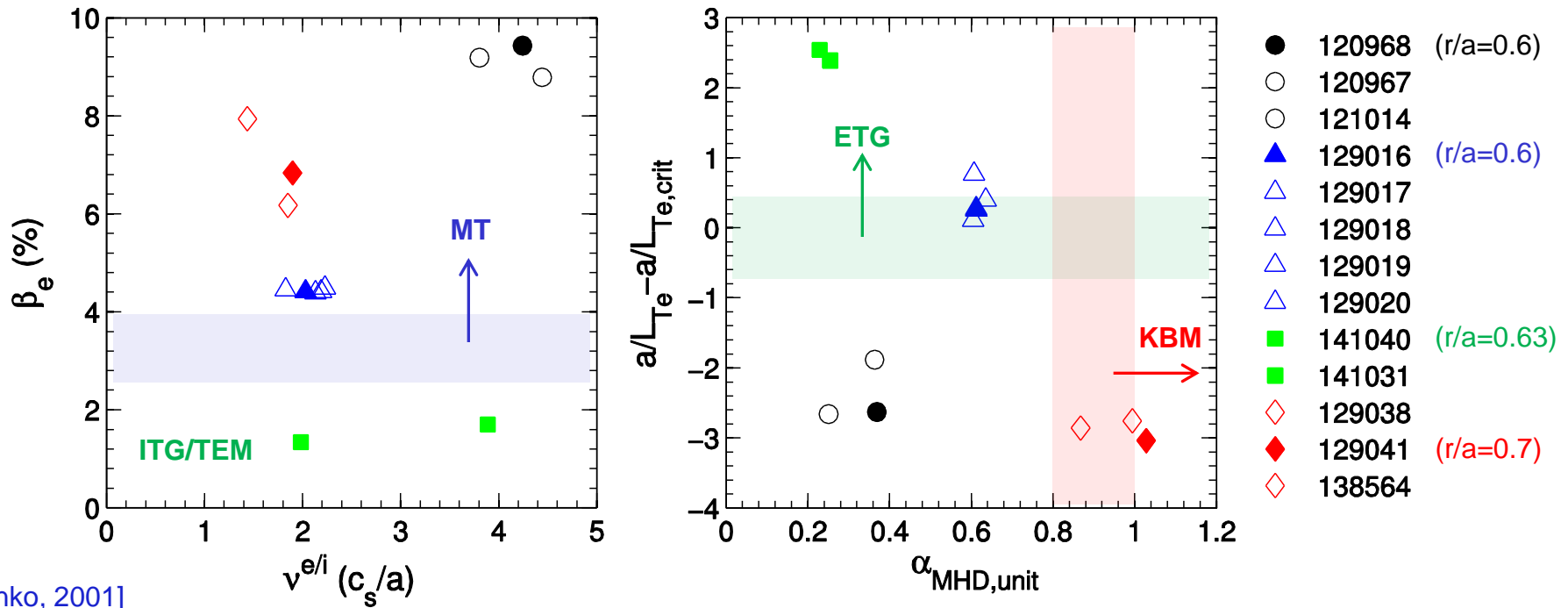
# Attempting to validate gyrokinetic simulations using NSTX experimental data

- Comparing to experimental transport and sensitivity to parametric variations
- Following simulations based on many NSTX discharges:
  - H-mode  $v_*$  scaling experiments, without Lithium wall conditioning [Kaye NF 2007; IAEA 2012]
  - H-mode scan of Li-deposition for wall conditioning (will be referring to “pre-Li” and “post-Li”) [Maingi PRL 2011, IAEA 2012]
  - “Low beta” H-mode  $v_*$  scaling [Ren PoP 2012]
- Using Eulerian gyrokinetic code GYRO [1-3], almost all cases use:
  - Numerical equilibrium
  - Two ion species (D,C)
  - Fully electromagnetic perturbations ( $\phi$ ,  $A_{||}$ ,  $B_{||}$ )
  - Cases usually run without and with toroidal flow/flow shear ( $Ma \sim v_{Tor}$ ,  $\gamma_P \sim dv_{||}/dr$ ,  $\gamma_E \sim d(E_r)/dr$ )
- All simulations are *local*  $\rightarrow$  **non-local/global effects** ( $\rho_* = \rho_s/a \sim 1/120$ ,  $\rho_s/L \sim 1/50$ ) **almost certainly will change results quantitatively**

[1] J. Candy, R.E. Waltz, J. Comput. Phys. **186**, 545 (2003); [2] J. Candy, E.A. Belli, General Atomics Report **GA-A26818** (2010).  
[3] E.A. Belli, J. Candy, Phys. Plasmas **17**, 112314 (2010).

# Broad range of parameters requires consideration of many micro-instabilities

- “Electrostatic” **ITG/TEM** can be found at lower beta, often with  $\gamma_E \sim \gamma_{lin}$
- **ETG** found for  $a/L_{Te} > a/L_{Te,crit}$  (high and low  $\beta_e$ )
- Microtearing tearing (**MT**) found at sufficiently high  $\beta_e$  and  $v_{ei}$
- **KBM** unstable at high  $\alpha_{mhd} \sim \nabla\beta$



[Jenko, 2001]

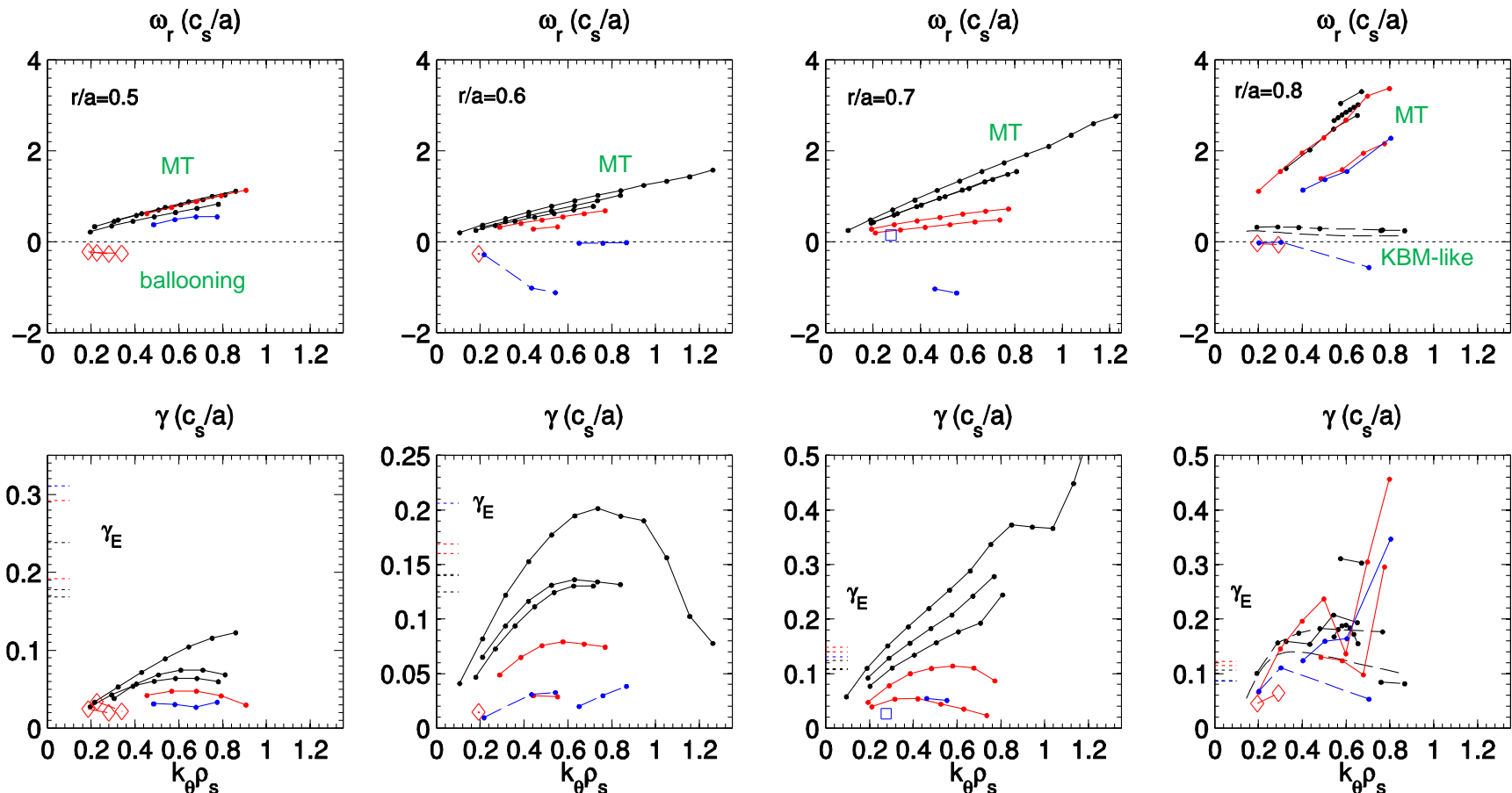
$$\left(\frac{R}{L_{Te}}\right)_{crit}^{etg} = \max \left\{ \frac{(1 + Z_{eff} T_e / T_i) \cdot (1.3 + 1.9s/q) \cdot (\dots)}{0.8R/L_{ne}} \right\}$$

$$\alpha_{mhd,unit} = -q^2 R \nabla\beta$$

$$\nabla\beta = \sum_s \nabla(n_s T_s) \cdot 2\mu_0 / B_{unit}^2$$

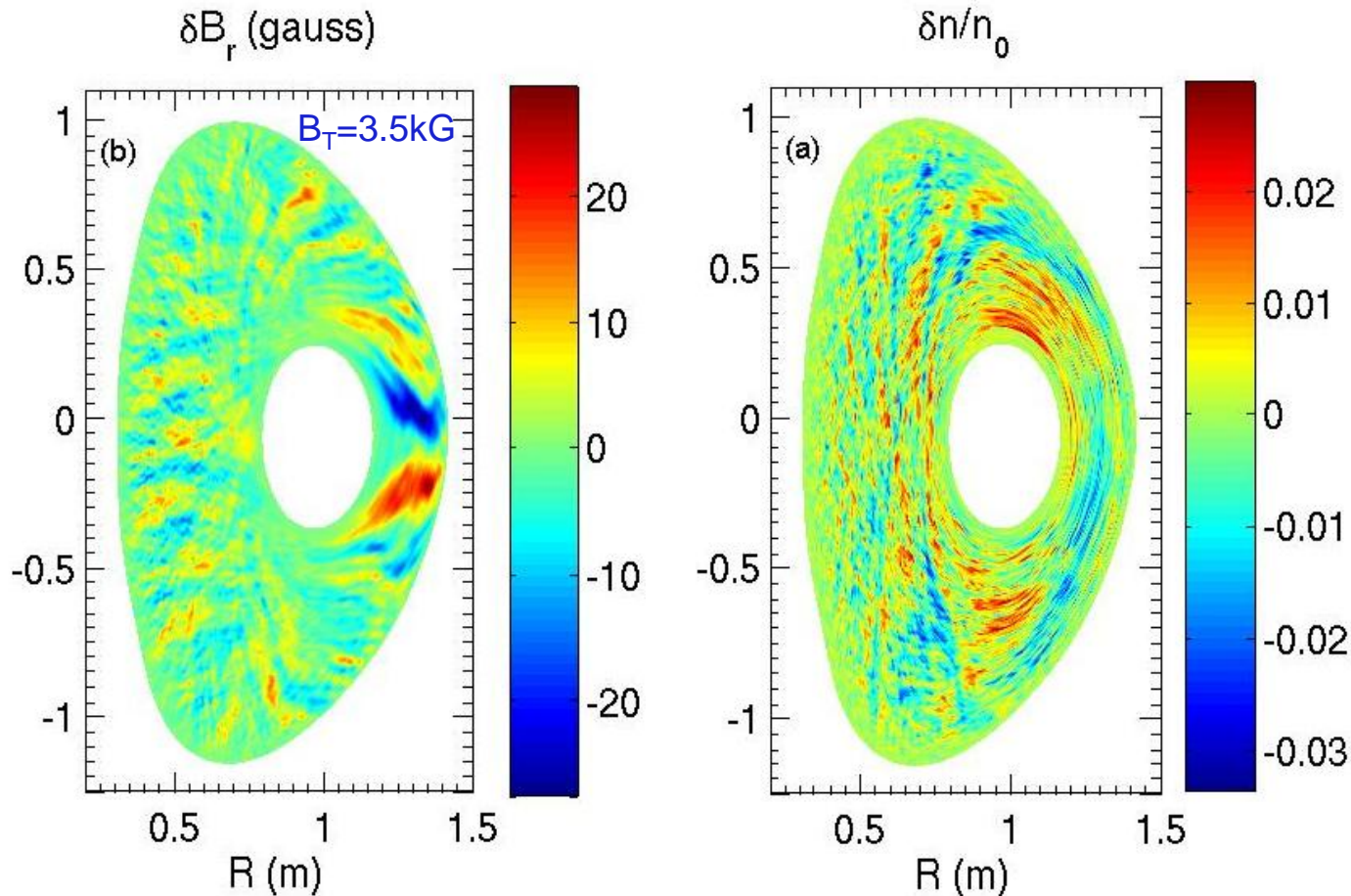
# Microtearing prevalent in older $v_*$ discharges (2006 data, without Li wall conditioning)

- Color coding in plots: 3 high  $v_*$ , 2 med  $v_*$ , 2 low  $v_*$  [Kaye NF 2007]
- Microtearing dominates  $r/a=0.5-0.8$ ; ETG almost entirely stable throughout (not shown)
- At  $r/a=0.8$  other ballooning modes (KBM) compete with MT (more later)
- $\gamma_{\text{lin,max}}/\gamma_E$  increases with  $r/a$



# Nonlinear microtearing (MT) simulations for high $v_*$ discharge predict large $\delta B_r$ and dominant magnetic flutter transport

- $\chi_{e,em} \approx 6 \text{ m}^2/\text{s}$  from  $\delta B_r/B \sim 0.15\%$  (rms)
  - Measurable phase fluctuation predicted for proposed polarimetry diagnostic [J. Zhang, 2012]
- Narrow density perturbations distinct from traditional ITG/TEM



$L_x, L_y = 80, 100 \rho_s$   
 $n_x, n_y = 540, 16$   
 D only;  $\phi, A_{||}$   
 $\gamma_E = 0$

Resolution  
 constrained by  
 $\Delta r_{\text{rat}} = 1/k_{\theta} s$   
 $\Delta x \leq 0.2 \rho_s$

Toroidal mode  
 numbers:  
 $n \approx 5-40$

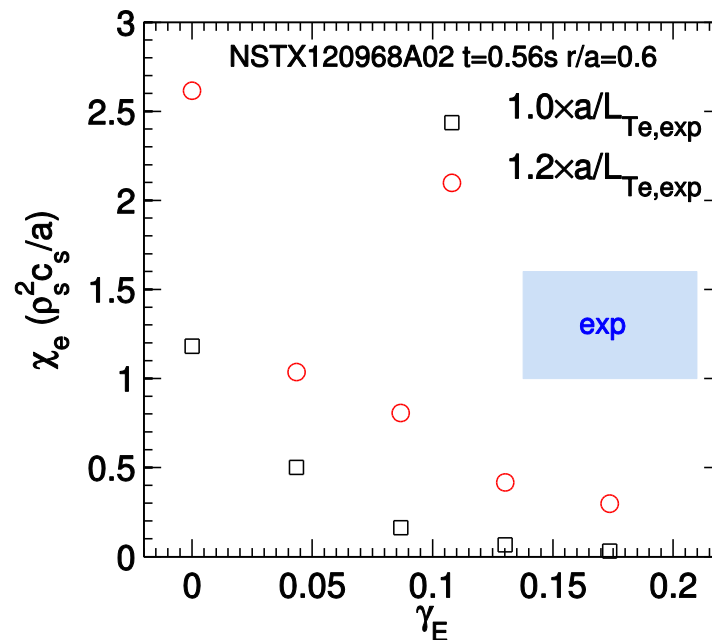
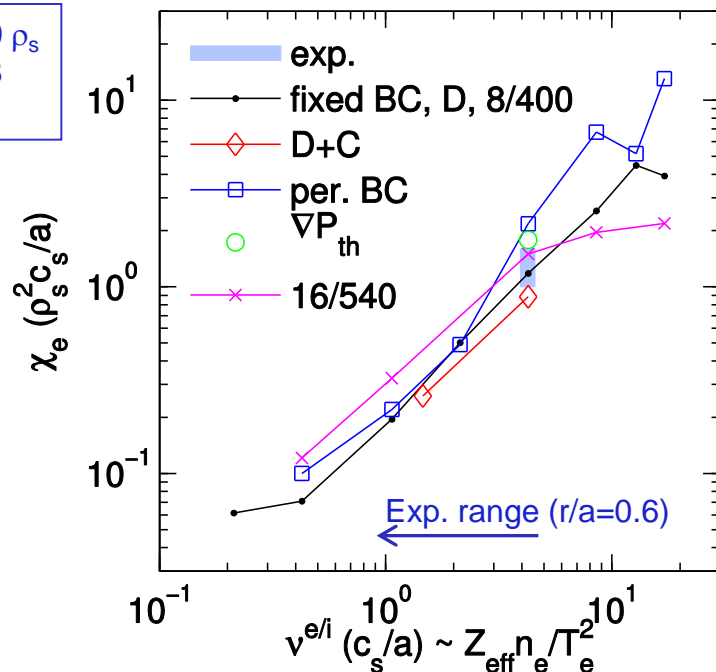
W. Guttenfelder et al., Phys. Rev. Lett. (2011); Phys. Plasmas (2012).



# MT transport increases with collisionality consistent with confinement scaling

- Possible component of confinement scaling in NSTX ( $\Omega\tau_E \sim v^{*-0.8}$ )
- However, also suppressed by  $E \times B$  shear ( $\gamma_{E,exp} \approx \gamma_{lin,MT}$ )

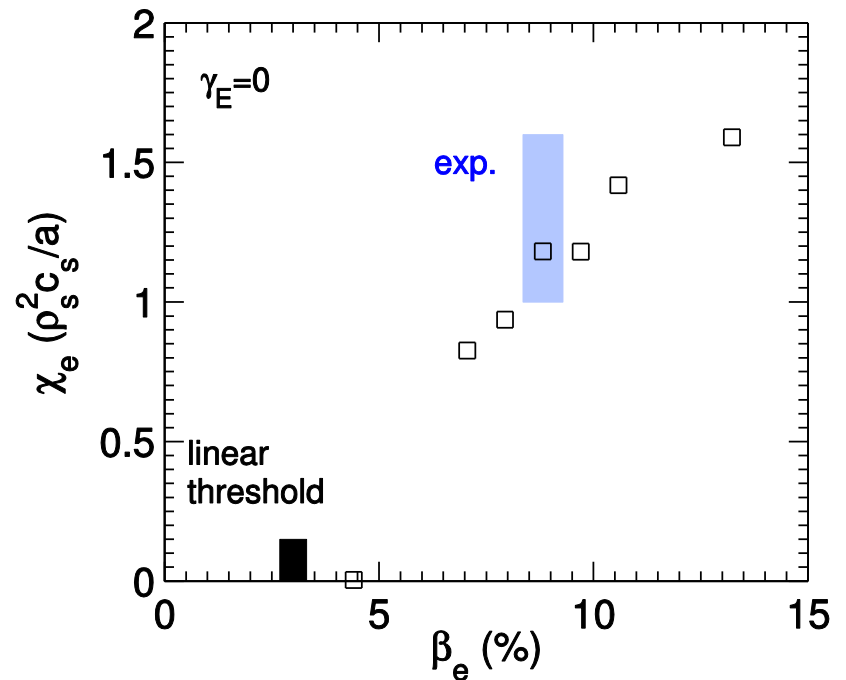
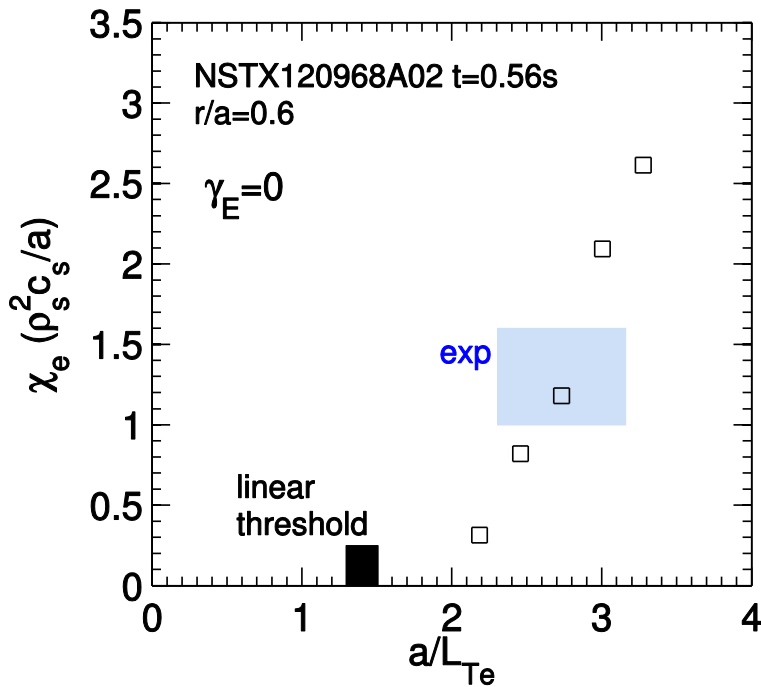
$L_x, L_y = 80, 60 \rho_s$   
 $n_x, n_y = 400, 8$   
 D only;  $\varphi, A_{||}$



- Scaling of MT transport with  $v_e$  confirmed for different physical and numerical assumptions: **addition of impurity species (C)**, **periodic boundary condition**, **equilibrium pressure gradient**, **perpendicular resolution** (all without  $E \times B$  shear)

# Microtearing transport also stiff with $\nabla T_e$ and $\beta_e$

- Beta scaling not consistent with weak confinement scaling,  $\Omega\tau_E \sim \beta^{-0.1}$  [Kaye, 2007]
- Useful to characterize threshold scaling for experimental interpretation and relating to MT as found conventional tokamaks [Doerk, PRL (2011), PoP (2012)]

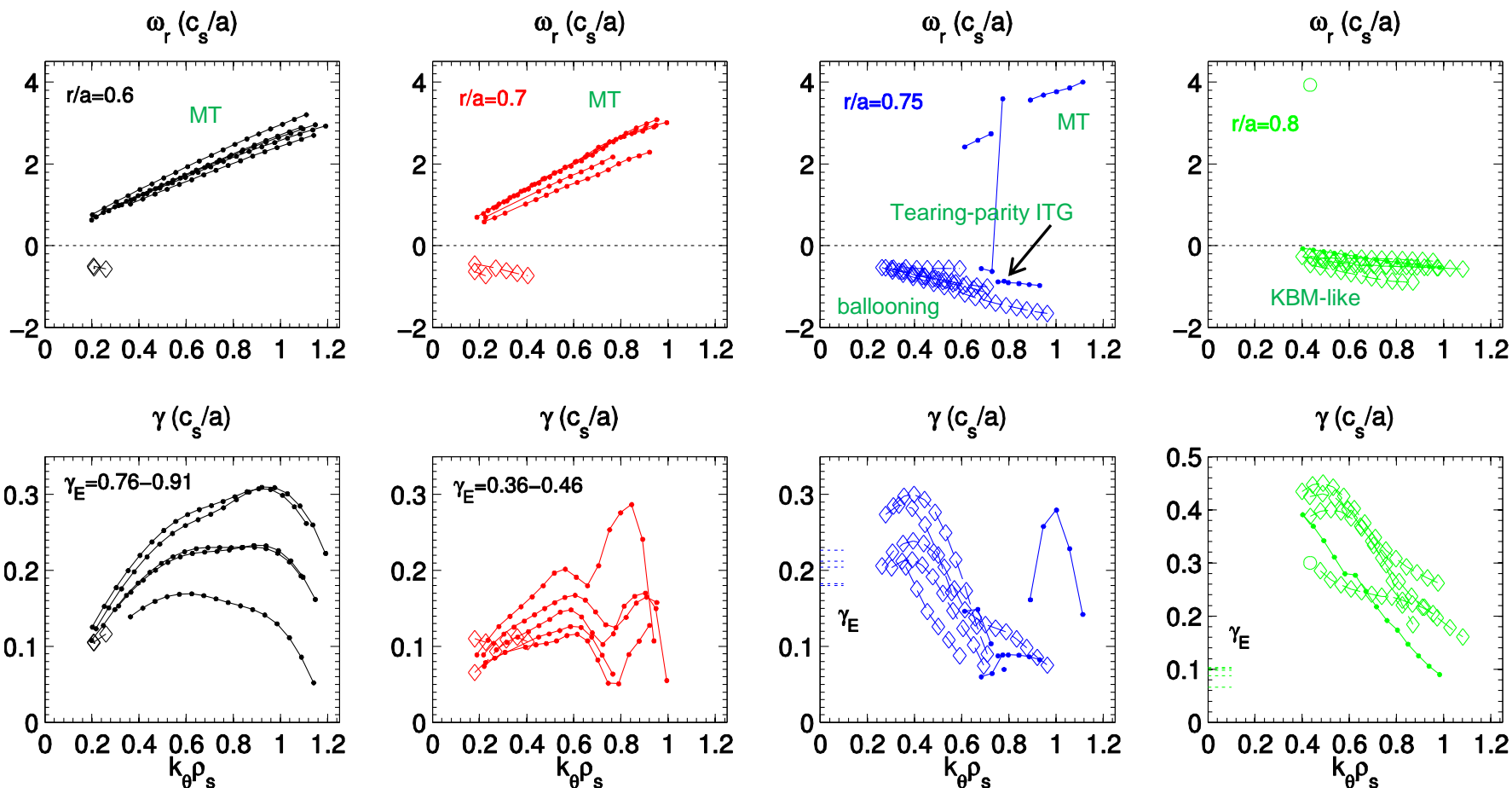


⇒ Confinement scaling unlikely described by any individual theory parameter (e.g.  $v_e$ ,  $\beta$ , ...), requires transport modeling

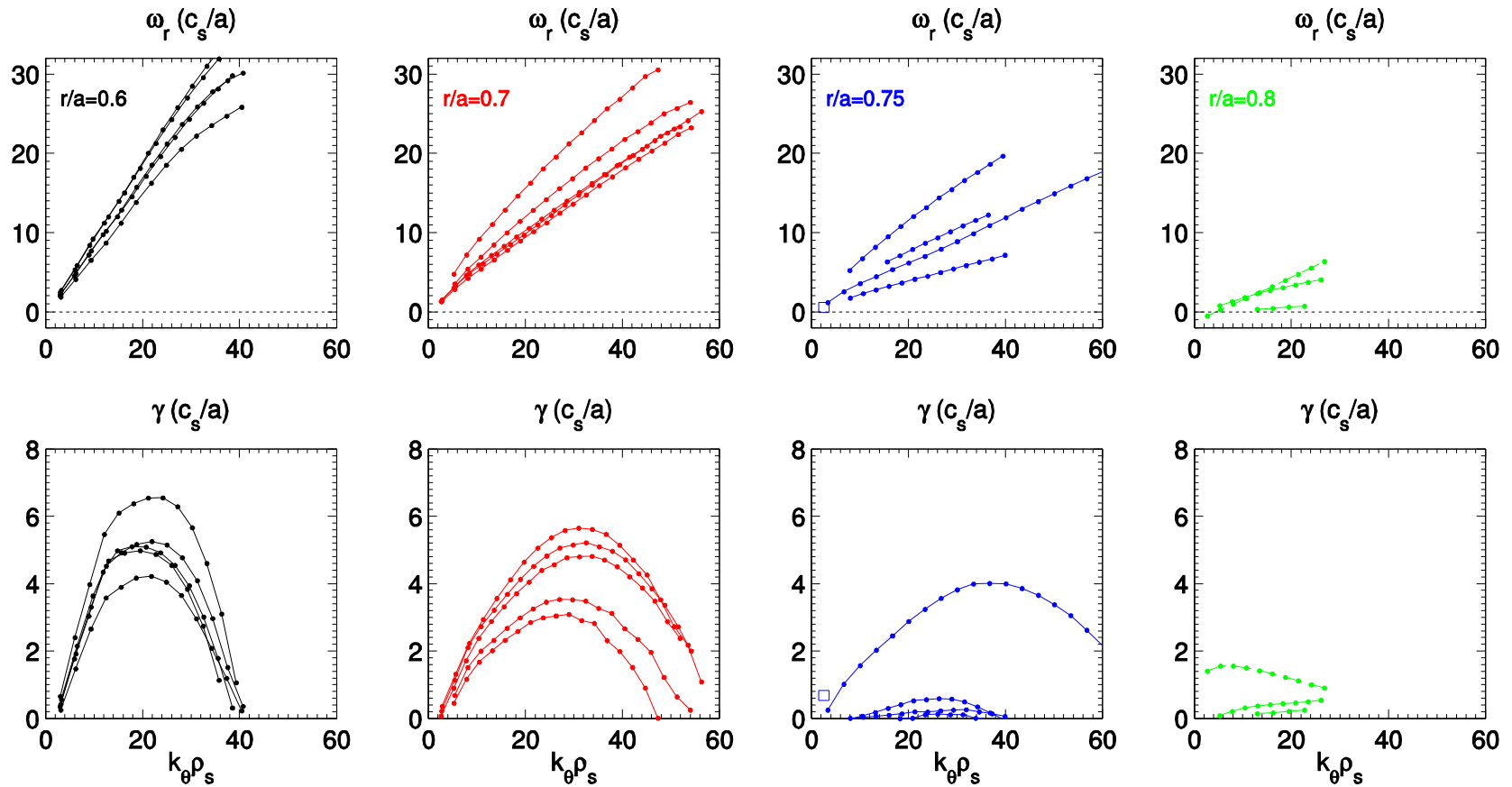


# Microtearing also unstable in “pre-Lithiated” shots from Li deposition scan (2008 data, Maingi PRL 2011, IAEA 2012)

- Five similar discharges (129016-129020), MT strongest at  $r/a=0.6-0.7$
- Ballooning modes dominate at  $r/a=0.75-0.8$  (different from 2006 data)
- Very strong  $E \times B$  shear at  $r/a=0.6-0.7$ ...

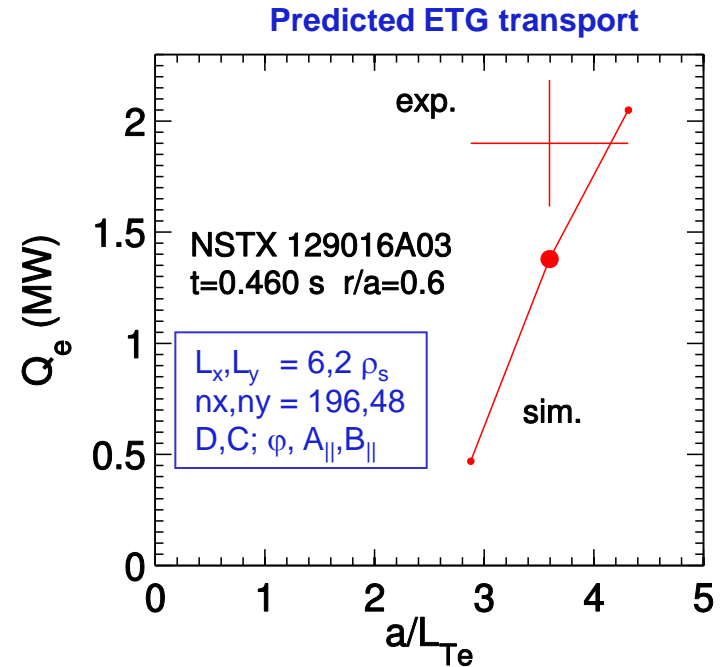
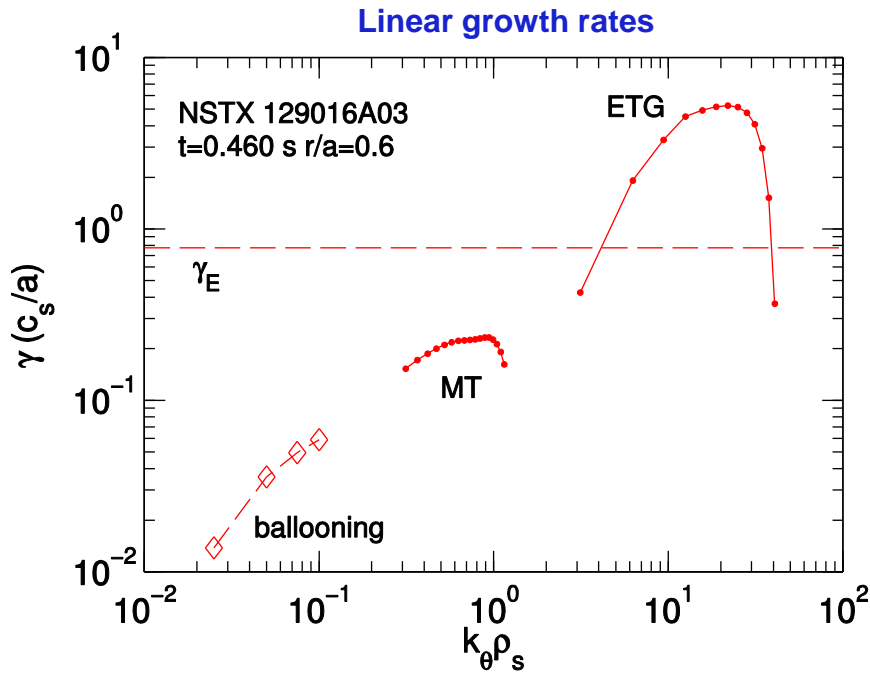


# ETG strongly unstable at $r/a=0.6-0.7$ in “pre-Li” discharges



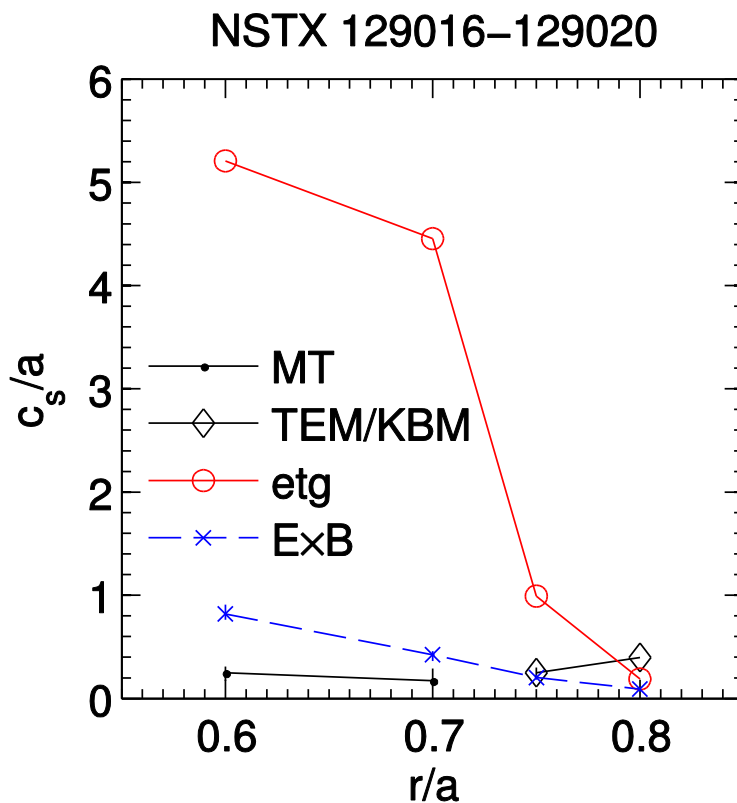
# Nonlinear ETG transport significant in core of “pre-Li” discharges

- Microtearing (and ballooning) instabilities at ion scales, but  $\gamma_E \gg \gamma_{\text{lin,ion}}$
- ETG nonlinear transport,  $Q_e \sim 1\text{-}2 \text{ MW}$  ( $\chi_e \sim 10 \rho_e^2 v_{Te}/L_{Te}$ )
- Relatively stiff ( $a/L_{Te,\text{crit}} \sim 2.2$ )



# Multiple instabilities & profile variations (non-local effects at $\rho_i$ scales) important to theoretically describe entire discharge

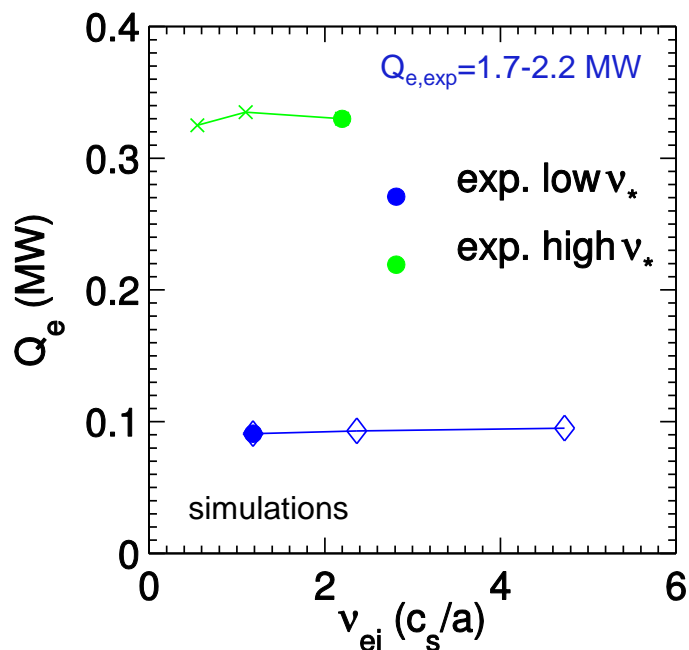
- Even over limited range of  $r/a=0.6-0.8$ , stability changes from ETG dominant (at  $\rho_e$  scales) to ballooning dominant (at  $\rho_i$  scales)
- Profile effects will matter for ion scales,  $\rho_i/L \sim 1/50$
- Ideally would use multi-scale, global simulations – too expensive computationally



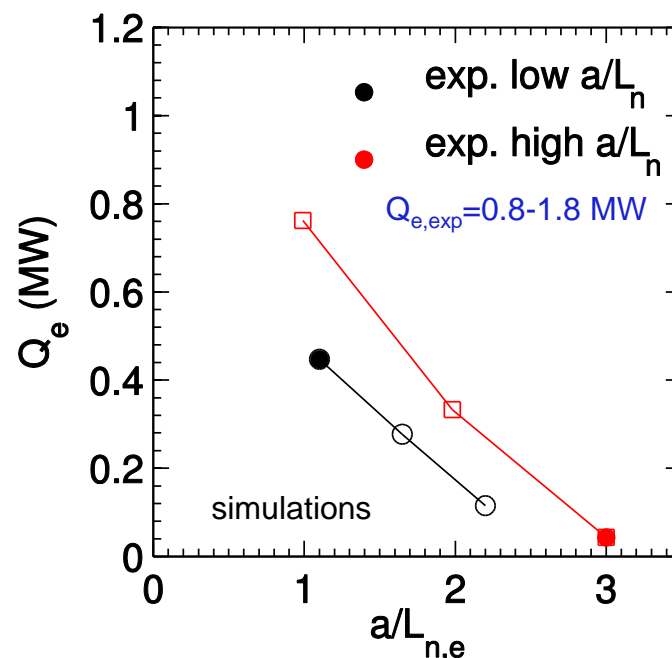
Maximum linear growth rates (ion and electron scale) and  $E \times B$  shearing rates (averaged over 5 discharges)

# Nonlinear ETG transport independent of $v_e$ , suppressed by $\nabla n$

$v_*$  scaling experiment  
lower  $n_e$  &  $P_{\text{NBI}} \rightarrow$  lower beta



Change in core ( $r/a \approx 0.6$ ) density gradient before/after large ELM



- Weak dependence follows linear stability ( $v_e \ll \omega$ )
- Not consistent with confinement scaling,  $\Omega\tau_E \sim v_*^{-0.8}$

- Partially described by linear ETG threshold
- $\nabla n$  stabilization observed in reduction of high-k scattering intensity
- Higher density gradient causes electrostatic TEM to be unstable

Y. Ren et al., Phys. Plasmas (2012); Phys. Rev. Lett. (2011).

# Stiffness of ETG transport depends on $\nabla n$

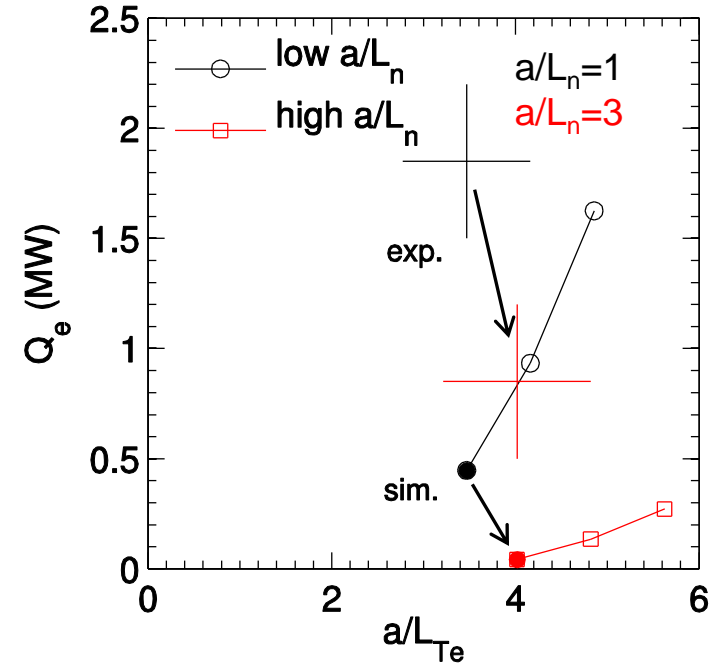
- Consider critical gradient model for ETG:

$$\chi_e = \frac{\rho_s^2 c_s}{a} \cdot \left[ \left( \frac{R}{L_{Te}} \right) - \left( \frac{R}{L_{Te}} \right)_{\text{crit}} \right] \cdot \underline{F(s, q, \dots)}$$

Little variation in  $\rho_s^2 c_s / a \approx 1.4 \text{ m}^2/\text{s}$

~25% increase in effective threshold  $\rightarrow$

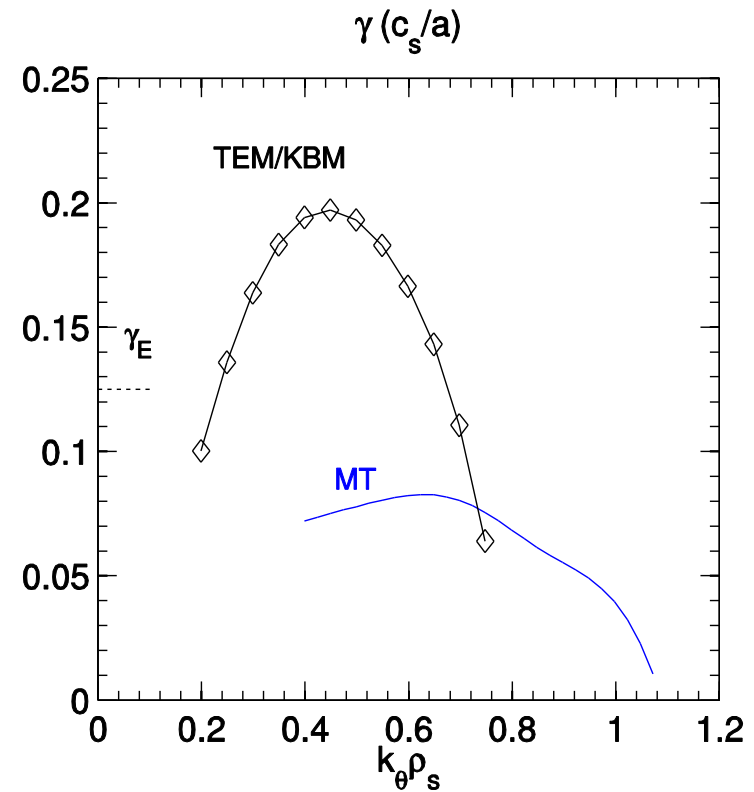
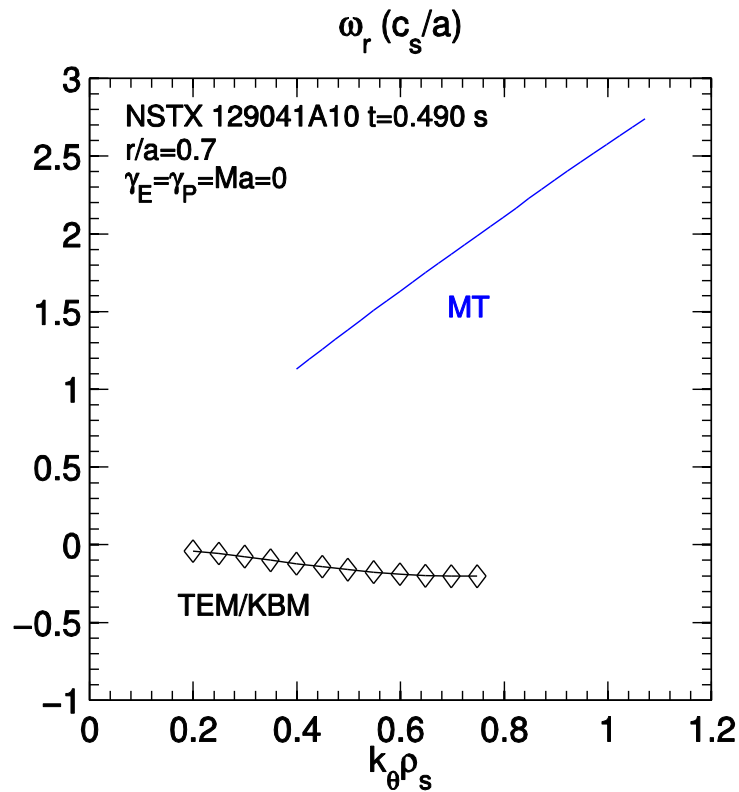
- $\Rightarrow$  **Large  $a/L_n$  decreases ETG stiffness (F) regardless of threshold**



- Strong correlation between  $Q_{e,ETG}$  and  $a/L_n$  also found in low- $\beta$   $v_*$ -scan discharges with **apparent nonlinear threshold  $\eta_e = L_n/L_{Te} \sim 1.5-2.0$**

# Different ion scale instabilities often overlap simultaneously

- Low  $v_*$  discharge with Lithium (129041 [Kaye, Maingi]) shows microtearing unstable but subdominant to ballooning mode ( $r/a=0.7$ )
- **Ballooning mode disappears in absence of compressional perturbations ( $B_{||}$ )**

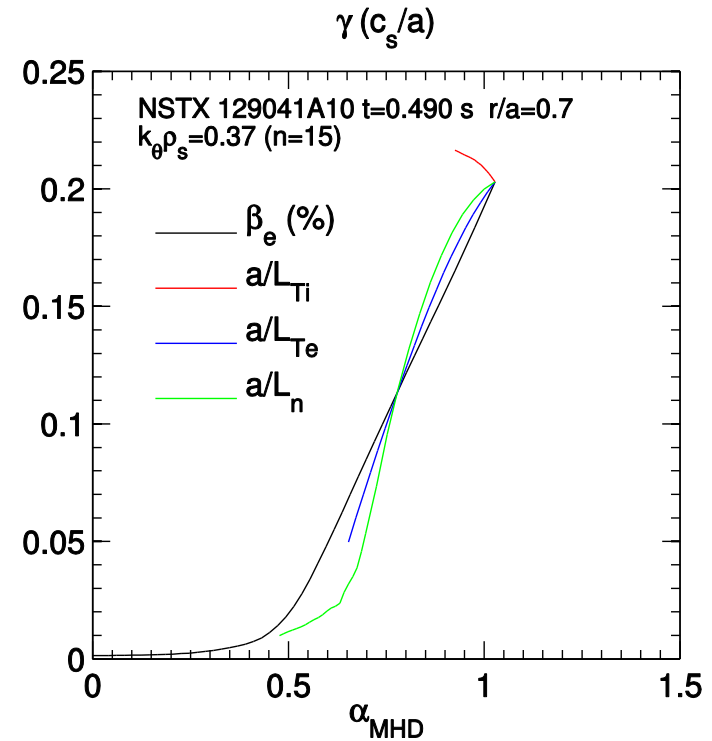
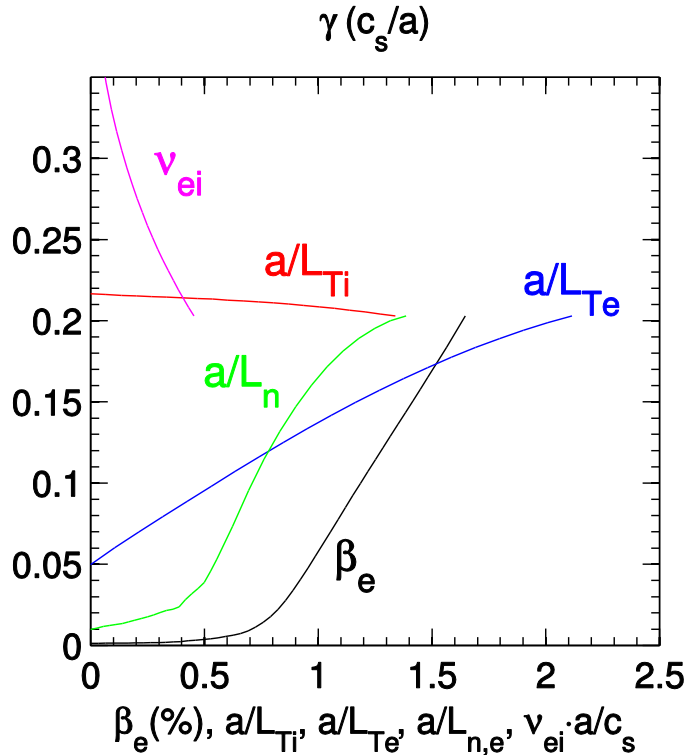


- What is the nature of these ion scale ballooning modes?



# Ballooning mode scales like TEM, but very sensitive to beta like KBM

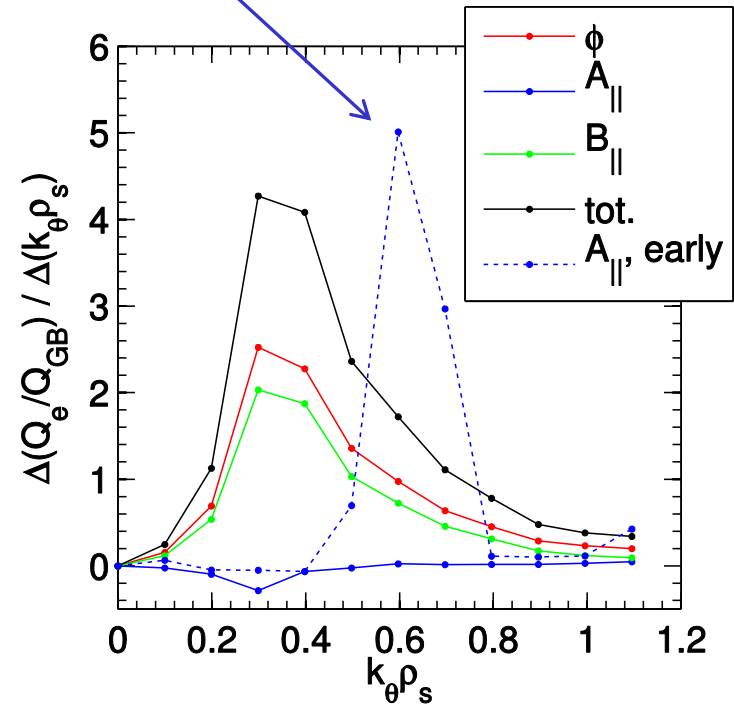
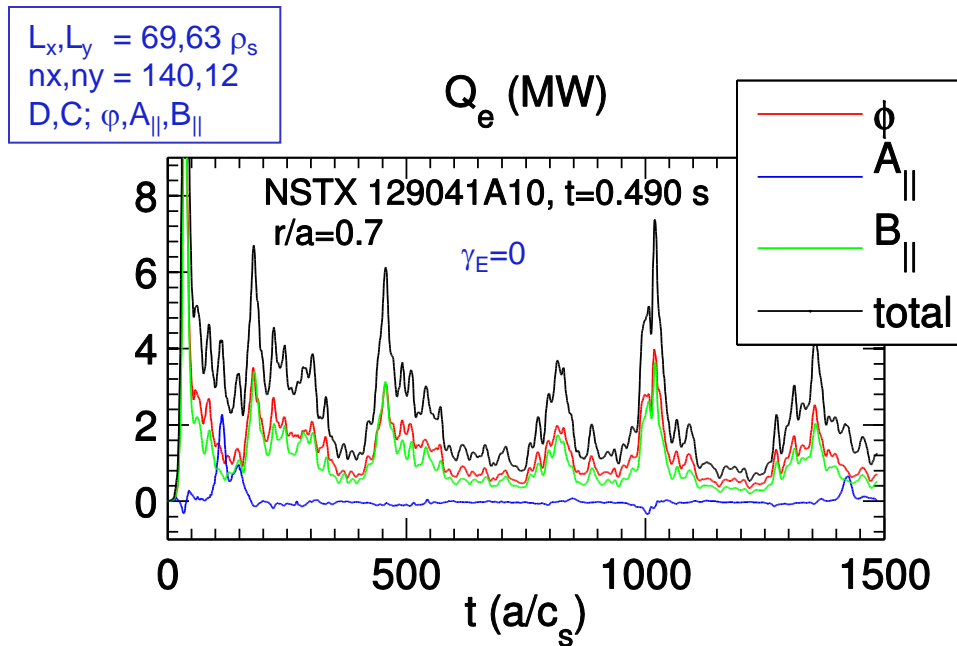
- Destabilized by  $a/L_{Te}$ ,  $a/L_n$ , weakly dependent on  $a/L_{Ti}$ , stabilized by  $v_e$  (like TEM)
  - $\gamma \sim 1/v_e$  scaling opposite to MT and confinement scaling
- Growth rate scaling largely unified by  $\alpha_{mhd} = -q^2 R \nabla \beta$ ,  $\nabla \beta \sim \beta_e \sum_s \frac{n_s}{n_e} \frac{T_s}{T_e} \left( \frac{a}{L_{n,s}} + \frac{a}{L_{T,s}} \right)$ 
  - expected for ideal/kinetic ballooning mode (KBM)



- Similar behavior predicted in linear pedestal simulations [Canik, EX/P7-16]

# Nonlinear TEM/KBM simulations predict significant transport, from both $\phi$ and $B_{\parallel}$ perturbations

- Significant transport in all channels (heat, particles), nearly half from  $\delta B_{\parallel}/B \sim 0.08\%$
- Spectra peak around  $k_{\theta}\rho_s \sim 0.3$ , MT apparent early in  $A_{\parallel}$  but does not survive



- Including finite  $dV_{\parallel}/dr$  &  $V_{\text{Tor}}$   $\rightarrow$  momentum transport ( $\Pi_{i,\text{sim}} \sim 0.3 \text{ N}\cdot\text{m}$ ;  $\Pi_{i,\text{exp}} \sim 1-1.5 \text{ N}\cdot\text{m}$ )
  - May reconcile scenarios with anomalous  $\chi_e, \chi_{\phi}$ , near neoclassical  $\chi_i$  [Kaye, NF (2009)]
  - However, significantly suppressed when also including  $E \times B$  shear

# Summary: Many turbulence mechanisms predicted over broad range of parameter space (especially $\beta$ )

- (1) Nonlinear microtearing (MT) simulations predict significant electron transport from magnetic flutter ( $\sim B_r$ )
  - $\gamma, \chi_e \sim \nu_e^{+1}$
  - Stiff with  $\beta_e$  and  $a/L_{Te}$  (suppressible by  $E \times B$  shear)
- (2) ETG predicts significant electron transport, in some scenarios
  - $\gamma, \chi_e \sim \nu_e^0$
  - Stiffness depends on  $\nabla n_e$
- (3) TEM/KBM simulations predict large transport in all channels from  $\varphi$  and  $B_{||}$ 
  - $\gamma \sim \nu_e^{-1}$
  - Stiff with  $\alpha_{MHD} \sim \nabla \beta$  (suppressible by  $E \times B$  shear)

Unlikely that one mechanism or parameter can theoretically describe transport scaling  $\rightarrow$  predictive modeling