

# Physics design of a cryo-pumping system for NSTX-U

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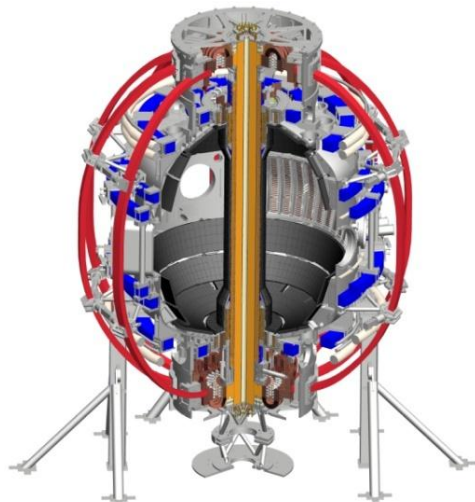
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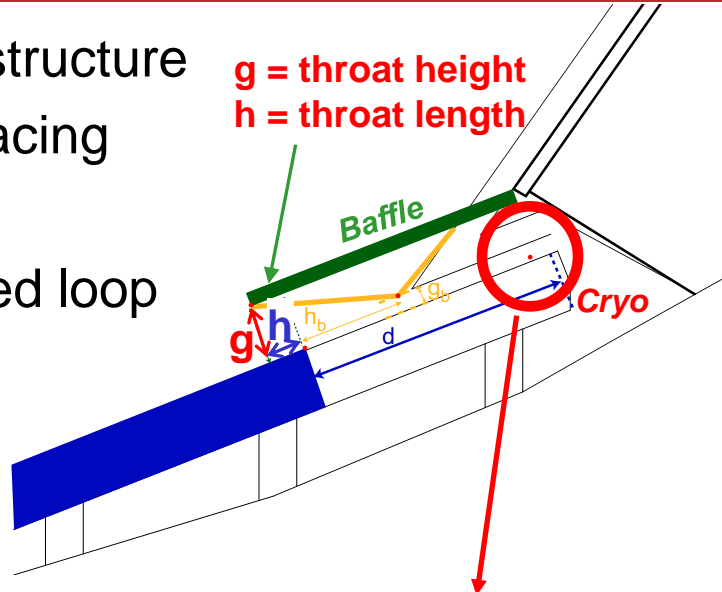
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# Motivation

- Particle control is needed to meet NSTX-U programmatic goals
  - Avoid density limit, radiative collapse during long-pulse (5s) discharge
  - Reduce collisionality to access new core physics
  - Control  $n/n_G$  for non-inductive scenarios
- Lithium coatings on PFCs sufficient for deuterium control, but ELMS are eliminated, leading to impurity accumulation
  - High  $Z_{\text{eff}}$ , prone to radiative collapse
  - Can be mitigated by ELM pace-making with 3D field pulses
- Cryo-pumping is being explored as a complement to lithium
  - Proven technique to control density in higher R/a tokamaks
  - May allow deuterium pumping without eliminating ELMS, so avoiding impurity accumulation problems

# General layout similar to DIII-D lower outer cryo-pump system is taken as starting point for design analysis

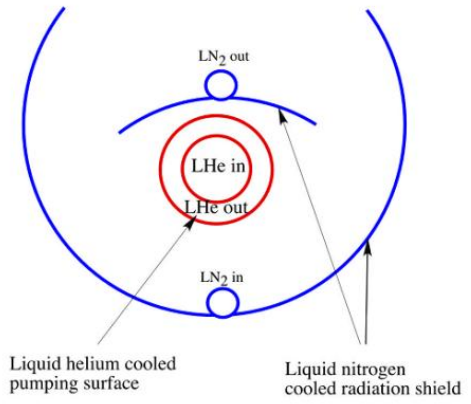
- Plenum location studied: under new baffling structure near secondary passive plates, possibly replacing some outer divertor plates and tiles
- Pumping capacity of a toroidal liquid He cooled loop (Menon, NSTX Ideas Forum 2002)
  - $S=24,000$  l/s @  $R=1.2$ m
  - Need plenum pressure of 0.83 mtorr to pump beam input (10MW~20 torr-l/s)



- Pumping rate:

$$I_{pump} = P_{pl} S = \frac{I_0}{S + C} S$$

- $P_{pl}$  = plenum pressure
- $I_0$  = neutral flux into plenum
- $C$  = throat conductance



Cross-section of the pump (10 cm outer dia.)

- To optimize, need  $C(g,h)$ ,  $I_0(g,h)$

# Semi-analytic pumping model\* used to optimize pumping chamber

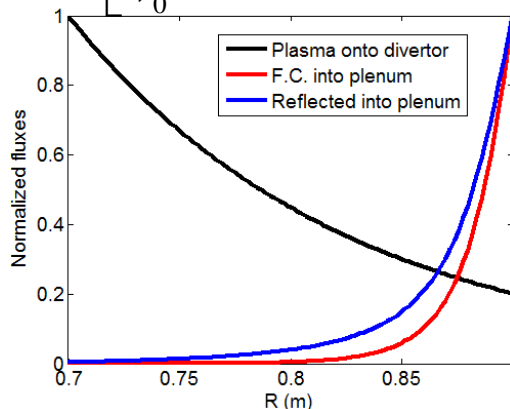
- Uses first-flight model for neutral flux into pump plenum
- Requires knowledge of divertor plasma profiles
- Validated against DIII-D experiments

$$P_{pl} = \frac{I_0}{S + C} \Rightarrow P_{pl} = \frac{I_0}{S + C} \frac{C}{C_{eff}} \quad \leftarrow \text{Plenum pressure corrected for penetration of neutrals through long duct (verified using EIRENE)}$$

$$I_0 = \int_{R_{min}}^{R_{max}} \Gamma_0(r) F(r) T(r) 2\pi R_m dr \quad \leftarrow \text{Neutral current into plenum}$$

$$F(r) = \frac{1 - \cos \Theta_{max}(r)}{2}; \Theta_{max}(r) = \tan^{-1} \left( \frac{g}{R - R_{ent}} \right) \quad \leftarrow \text{Solid angle of plenum entrance}$$

$$T(r) = \exp \left[ \frac{-1}{v_0} \int_R^{R_{max}} n_e(r) \langle \sigma v \rangle_{EH}(r) dr \right] \quad \leftarrow \text{Transmission of neutrals through plasma}$$



**Origin of neutrals making it into plenum tends to be localized to near-entrance region  
Dominantly due to solid angle factor**

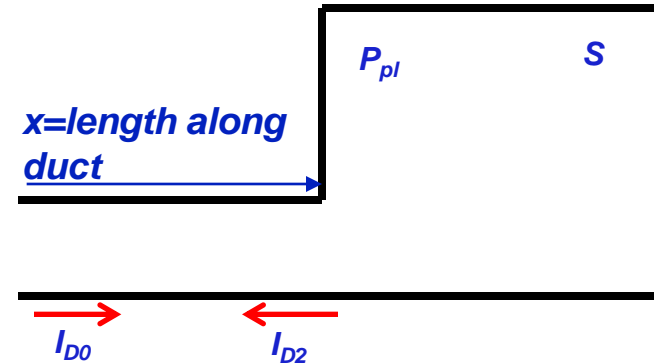
\*R. Maingi, Nucl. Fus. 39 (1999) 1187

# Model upgraded to include conductance correction in a long channel

- $I_{D0} = I_{D0}(x)$  = current of “fast” atomic deuterium entering from plasma

If fast atoms are turned into thermal molecules on collision with the wall, then:

$I_{D0}(x) = I_{D0}(0) \cdot F(x)/F(0)$ , where  $F$  is the solid angle factor evaluated along  $x$



- $I_{D2}$  = current of thermal molecules leaving
- $I_{D2}$  = volume integral of sources ( $I_{D0}$ ), sinks ( $P_{pl}S$ )

$$\Rightarrow I_{D2}(x) = I_{D0}(x) - P_{pl}S$$

- Pressure is  $\Delta P = \int_0^h I(x)\sigma(x)dx$ ,  $\sigma = \frac{3}{4\bar{v}} \frac{H}{A^2}$ ,  $\frac{1}{C} = \int_0^h \sigma(x)dx$
- So plenum pressure is

$$P_{pl} = \int_0^h I_{D2}(x)\sigma(x)dx = \int_0^h I_{D0}(x)\sigma(x)dx - \int_0^h P_{pl}S\sigma(x)dx$$

$$= I_{D0}(0) \int_0^h \frac{F(x)}{F(0)} \sigma(x)dx - \frac{P_{pl}S}{C} = \frac{I_{D0}(0)}{C_{eff}} - \frac{P_{pl}S}{C} = \frac{I_{D0}(0)}{S+C} \frac{C}{C_{eff}}$$

$$C_{eff} = \int_0^h \frac{F(x)}{F(0)} \sigma(x)dx$$

# Expressions for conductance, pressure have been checked with Monte Carlo neutral code EIRENE

- Set of ducts constructed in EIRENE, varying length and height
- Three calculations made for each:

- No pumping, gas source inside plenum

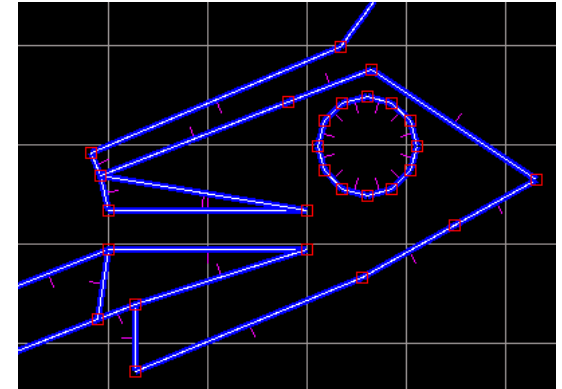
- Gives the actual conductance of duct/aperture
- $C = I_{pl}/P_{pl}$
- ( $I_{pl}$ =source in plenum,  $P_{pl}$ =plenum pressure)

- No pumping, gas source outside plenum (mimic neutrals coming from plasma)

- Gives effective conductance, accounts for how far neutrals make it down duct before hitting the walls
- $C_{eff} = I_{ent}/P_{pl}$
- ( $I_{ent}$ =current of neutrals crossing duct entrance)

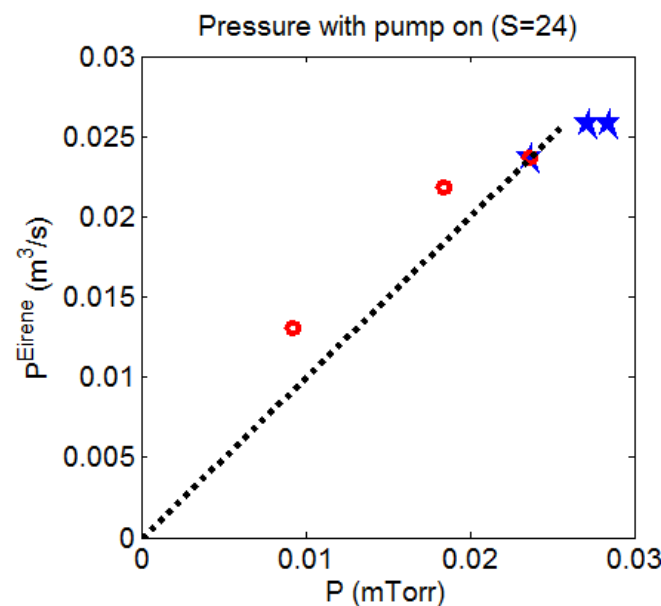
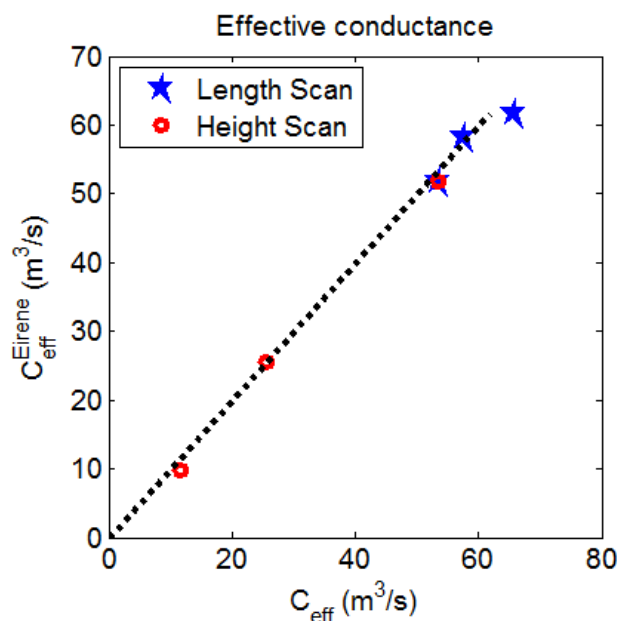
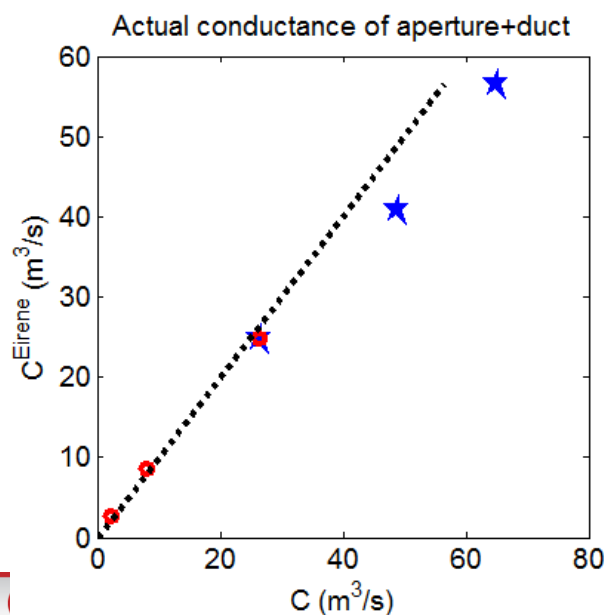
- Pumping on ( $S=24 \text{ ,m}^3/\text{s}$ ), gas source outside plenum

- Check pressure against analytic expression:
- $P = (C/C_{eff}) * I_{ent} / (S + C)$



# EIRENE confirms pressure variations with plenum entrance geometry

- X-axis: analytic expressions, Y-axis: values calculated with EIRENE
- Conductances are ok, but duct expression is somewhat off (based on length scan on left)
- Pressure variations from EIRENE largely agree with analytic expressions
  - Difference is largely due to the conductances: if the EIRENE-calculated conductances are used, pressures lie on the line
  - Just using  $P=I/(S+C)$  gives numbers higher by  $\sim x2-3$ , trends off



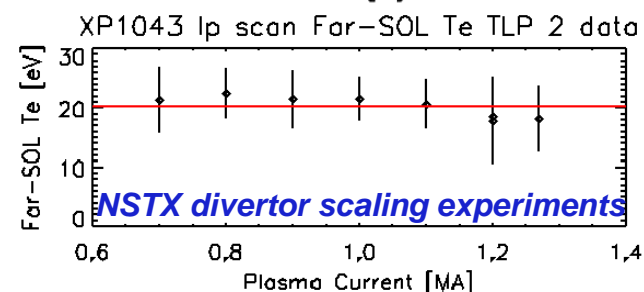
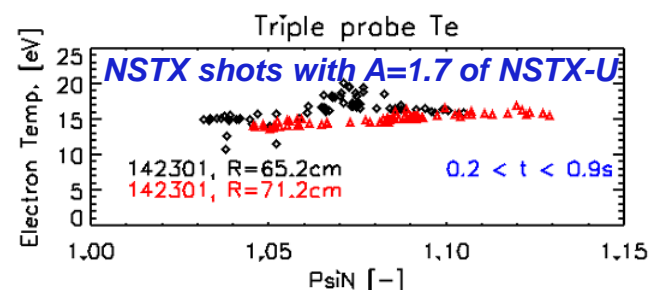
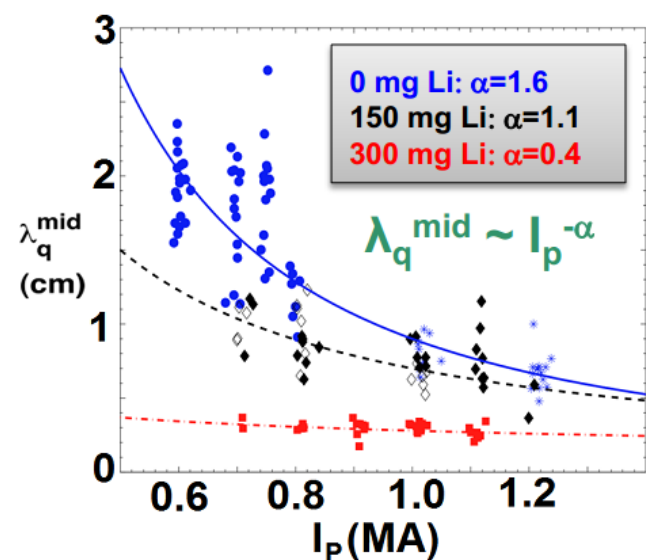
# Projected divertor parameters combined with semi-analytic pumping model are used to calculate pumping rates

- Analytic model requires divertor  $n$ ,  $T$ ,  $\Gamma$  profiles
- Heat flux, angle of B wrt PFC surface ( $\alpha$ ), and plasma temperature are sufficient to calculate  $n$ ,  $\Gamma$ :

$$\Gamma_{\perp} = q_{\perp} / 7T$$

$$n = \Gamma_{\perp} / \left( \sin \alpha \sqrt{2T/m} \right)$$

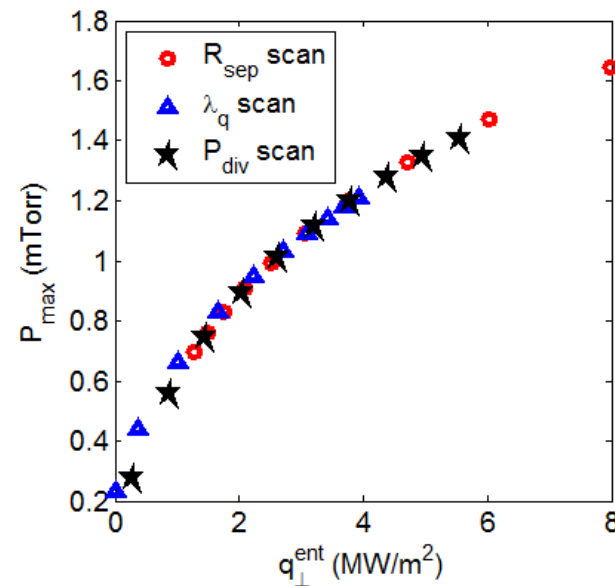
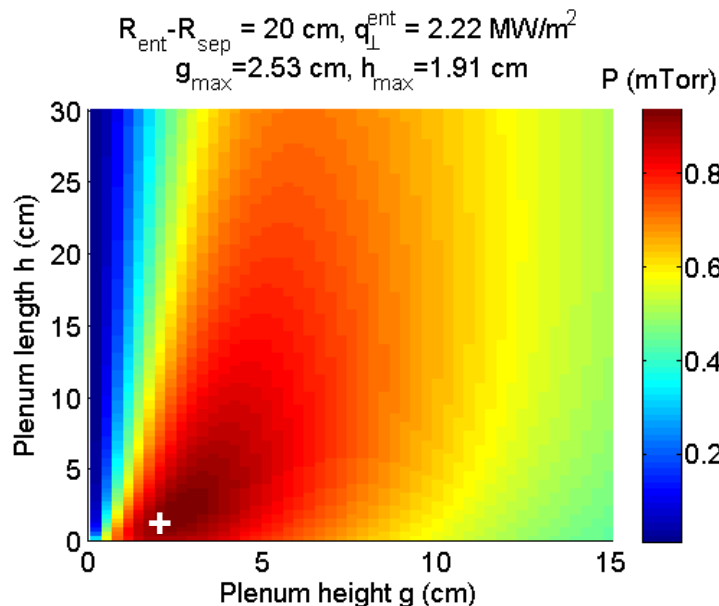
- Recent experiments yield scaling of SOL heat flux width
  - No-lithium scaling used here, but all trend towards  $\lambda_{q\sim 3\text{mm}}$  at  $I_p=2\text{MA}$
  - $P_{\text{div}} = 5 \text{ MW}$  assumed (1/2 of 10 MW input)
- Langmuir probes show  $T_e \sim 15\text{-}20 \text{ eV}$  in far SOL, with lithium radial,  $I_p$  dependence
  - $T_e \sim 15 \text{ eV}$  assumed (NSTX-U-like discharges)





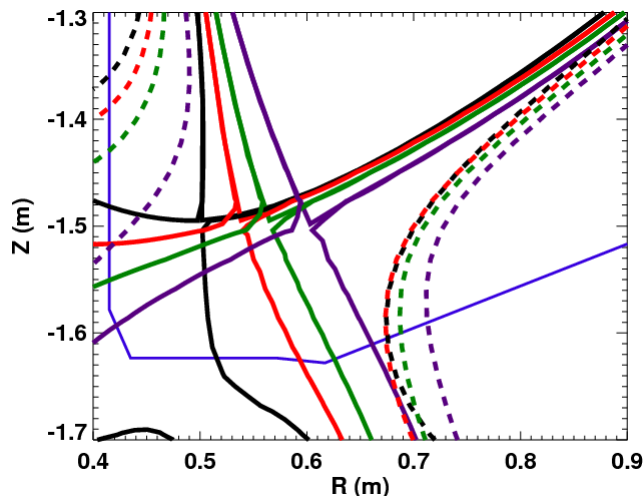
# Pressure projections are used to optimize plenum geometry parameters

- Exponentially decaying heat flux footprint imposed, with  $T_e=15$  eV
- Plenum entrance height, length are varied to maximize pressure
- Pressure in optimized plenum depends primarily on heat flux at pump entrance
  - Varied through  $R_{OSP}$ , flux expansion or  $P_{tot} \Rightarrow$  profile effects not important
  - Reaching  $P \sim 0.8$  mTorr (to pump 10 MW NBI) requires  $q_{\perp}^{ent} \sim 2$  MW/m<sup>2</sup>
- Optimal plenum entrance for  $P=0.8$  mTorr: height  $g \sim 2.5$  cm, length  $h \sim 2$  cm

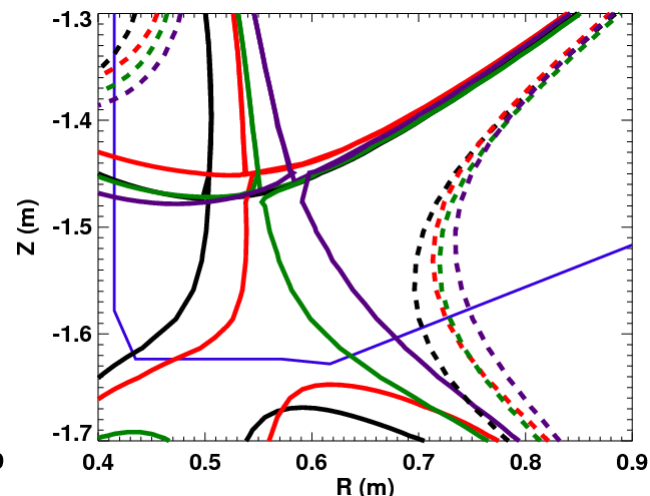


# Equilibria with variety of $R_{OSP}$ , flux expansion are used to map heat flux profiles, assess candidate pump entrance locations

- Standard and snowflake divertors considered
  - Four  $R_{OSP}$  each
  - $\psi_N=1.0, 1.03$  shown
  - Movement of  $\psi_N=1.03$  strike line is much less than that of  $R_{OSP}$

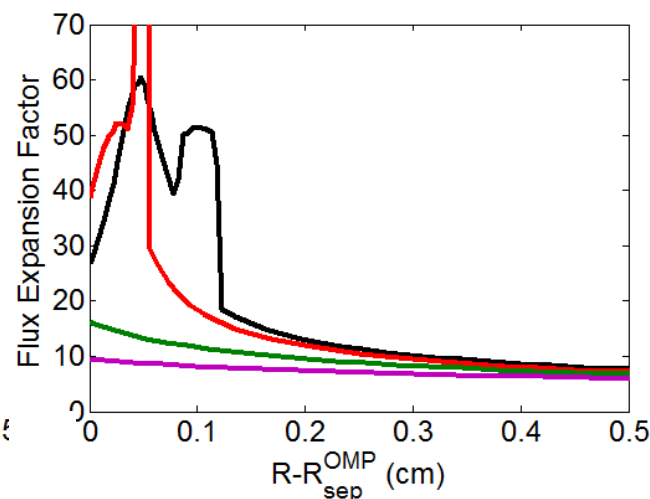
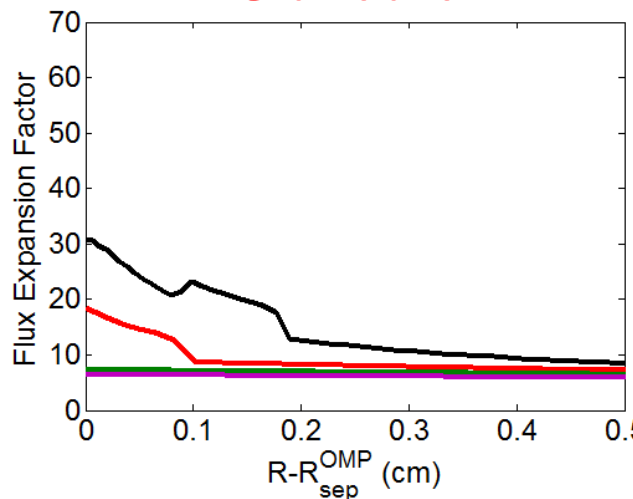


**Standard**



**Snowflake**

- Flux expansion, flux surface geometry used to convert midplane heat flux profile (from scaling) to divertor heat flux
  - As  $R_{OSP}$  is increased, flux expansion is decreased



# Realistic equilibria, heat flux scaling, and empirical $T_e^{\text{SOL}}$ are used to project plenum pressure for candidate location $R_{\text{pump}}$

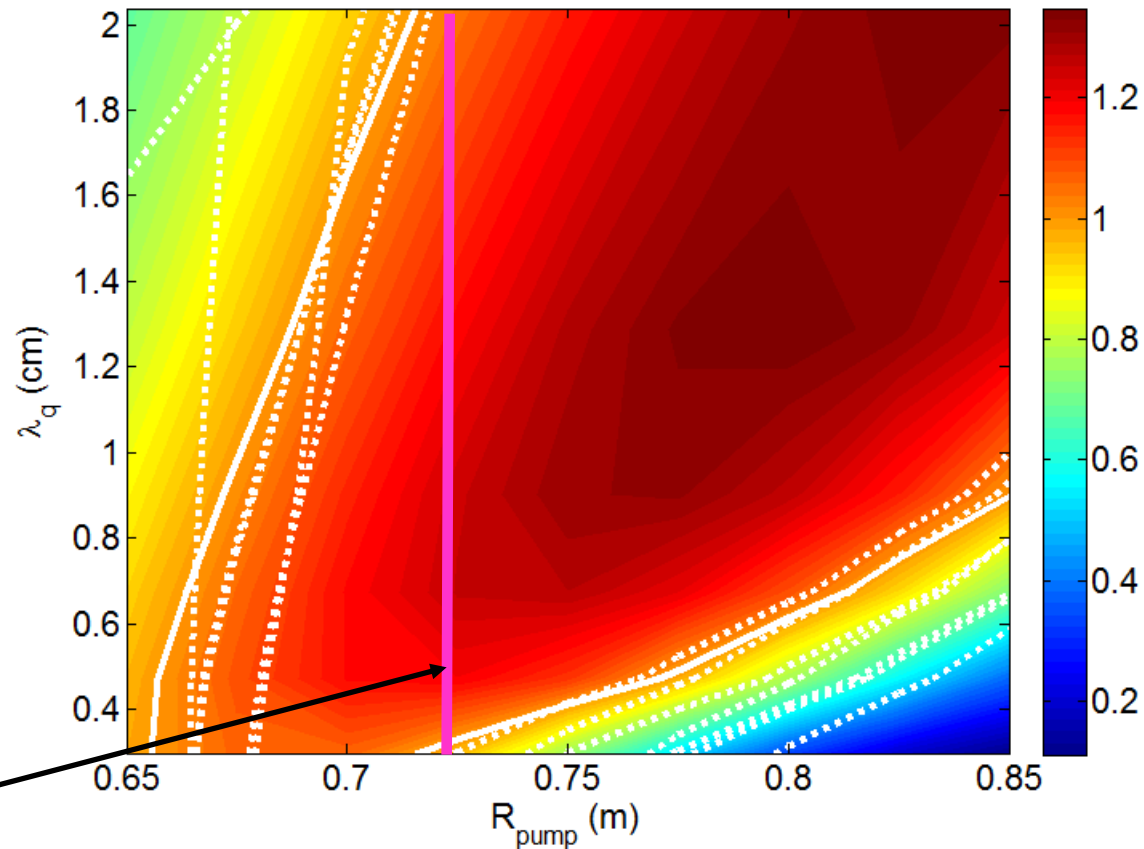
- Analytic model for plenum pressure with optimized entrance parameters
- Pressure is non-monotonic with  $R_{\text{pump}}$  due to field geometry
  - At low  $R_{\text{pump}}$ ,  $\alpha$  is lower, so  $n/\Gamma_{\perp}$  is increased  $\Rightarrow$  more neutrals ionized before reaching pump
- Optimizing position for narrowest SOL gives  $R_{\text{pump}} \sim 0.7$ 
  - Narrow SOL gives least flexibility in moving  $R_{\text{OSP}}$  to improve pumping
  - $R_{\text{pump}} = 0.72$  gives high  $P$  for wide range of SOL width

## STANDARD DIVERTOR $P_0$

P: SD,  $R_{\text{OSP}} = 0.50871$

+ 1 mTorr contours from all equilibria

mTorr



# $R_{\text{pump}}=0.72$ gives $n_e$ control for range of $I_p$ , equilibria

- Modified 2-pt model used to estimate  $n_e^{\text{sep}}$

$$T_{OMP} = \left( T_{DIV}^{7/2} + \frac{7}{4\kappa_{0e}} q_{\parallel}^{\text{sep}} L \right)^{2/7}$$

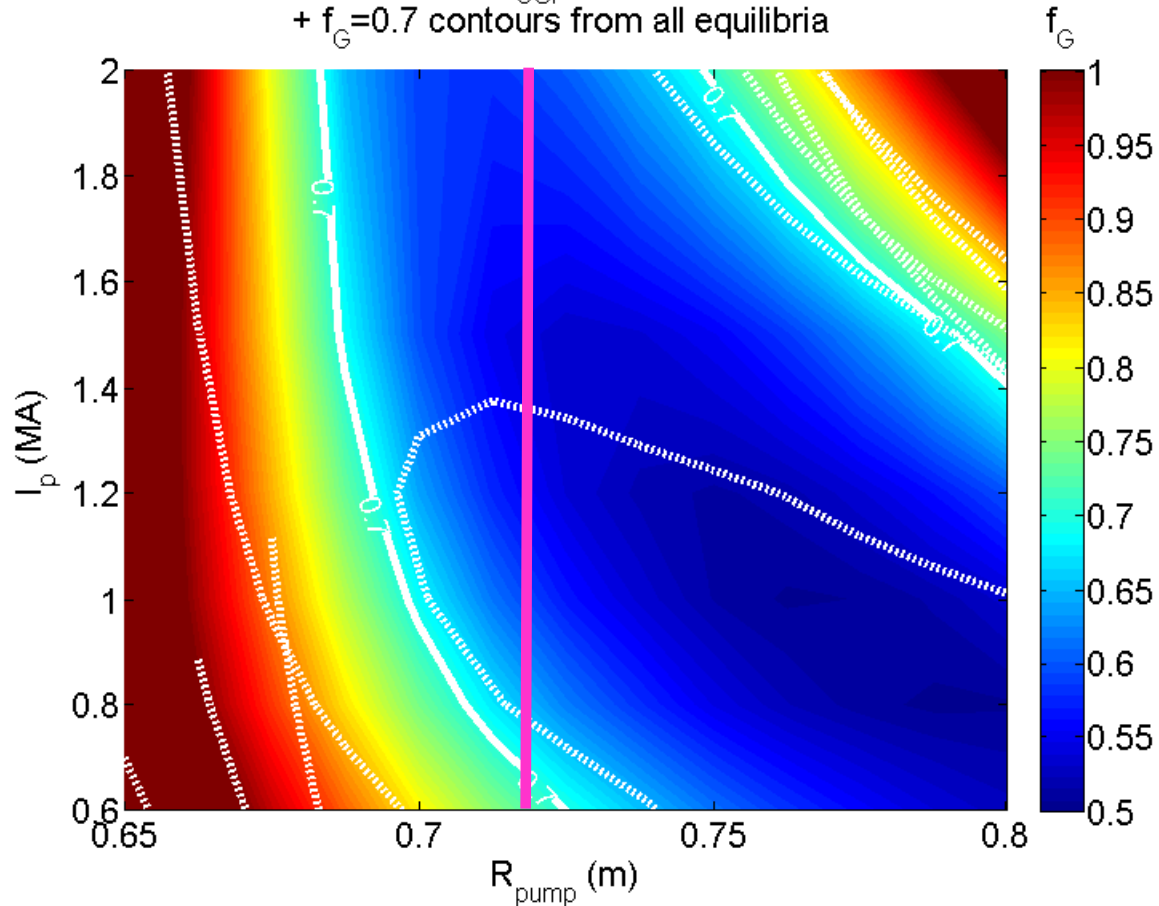
$$n_{OMP} = f_{cal} \frac{2n_{DIV} T_{DIV}}{T_{OMP}} \frac{B_{OMP}}{B_{DIV}}$$

- $q_{\parallel}^{\text{sep}}$  from  $I_p$  scaling,  $T_e^{\text{div}}$  varied
- Final  $n_e^{\text{sep}}$ : pumping=NBI input

- $\bar{n}_e/n_e^{\text{sep}} \sim 3$  used to estimate  $f_G = n/n_G$ 
  - Consistent with NSTX data

## SNOWFLAKE DIVERTOR $n/n_G$

SFD,  $R_{OSP}=0.51763$   
+  $f_G=0.7$  contours from all equilibria



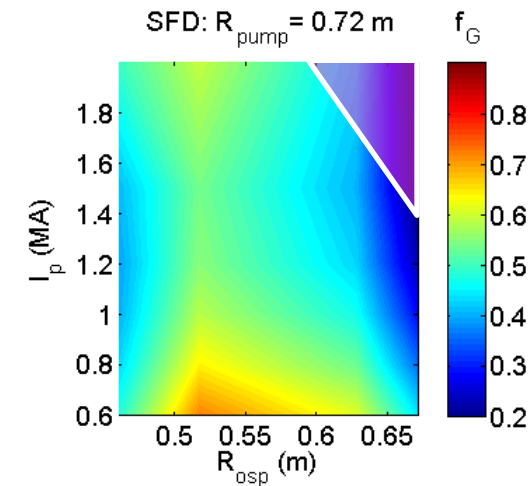
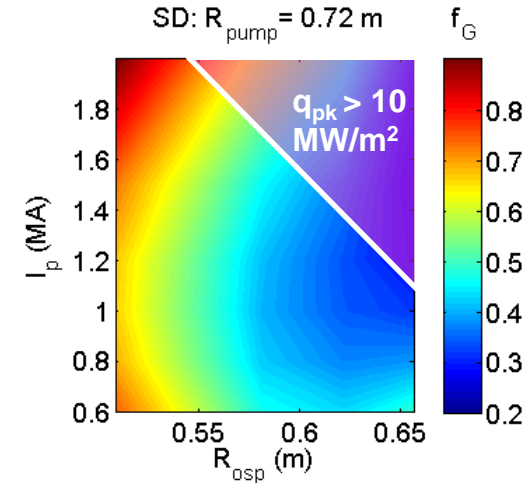
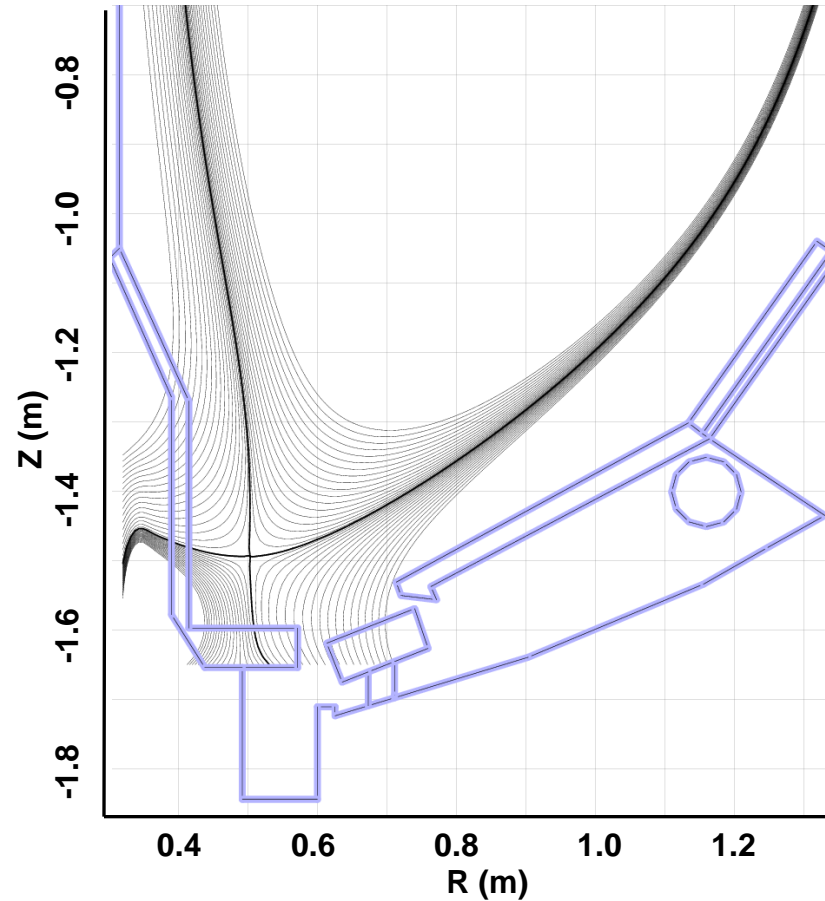
# Optimized plenum geometry capable of pumping to low density for a range of $R_{OSP}$ , $I_p$

- Equilibrium  $f_G$  down to  $< 0.5$

- Moving  $R_{OSP}$  closer to pump allows lower  $n_e$ , but limited by power handling

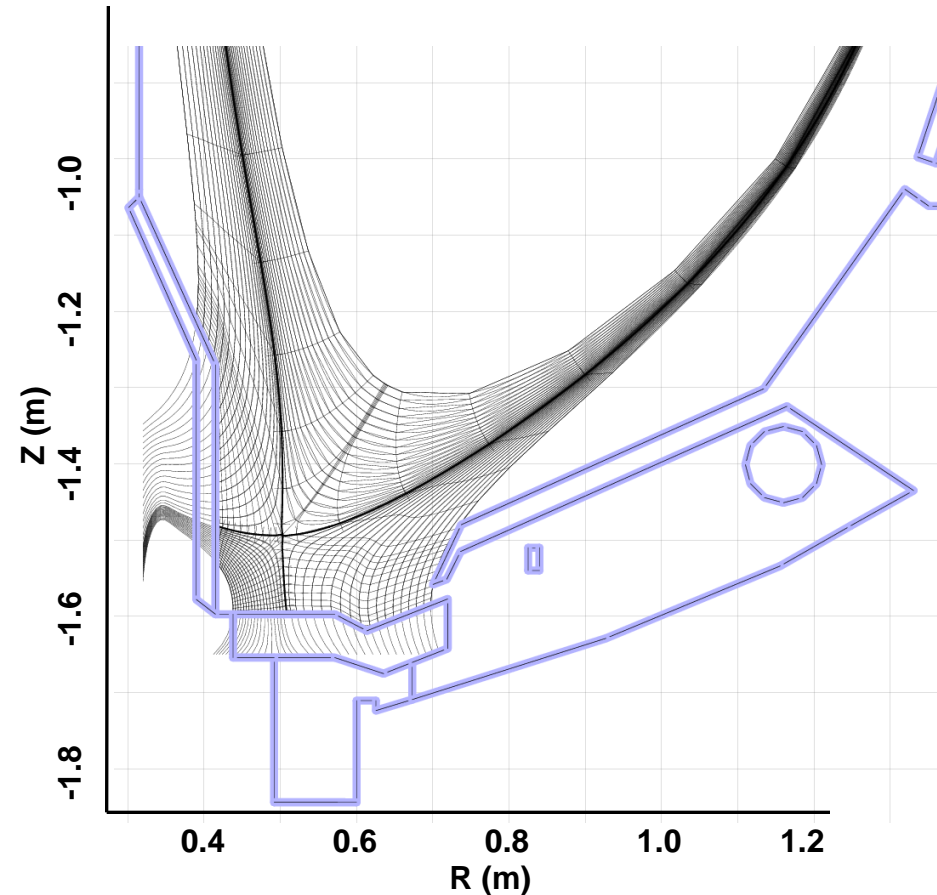
- High flux expansion in SFD gives *better* pumping with SOL-side configuration

- More plasma in far SOL near pump
- More room to increase  $R_{OSP}$  at high  $I_p$



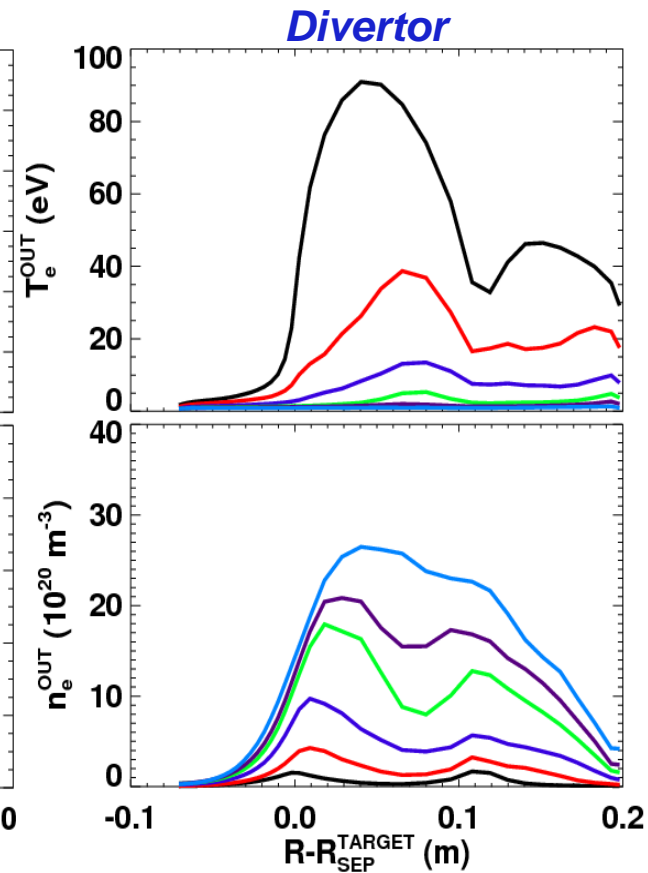
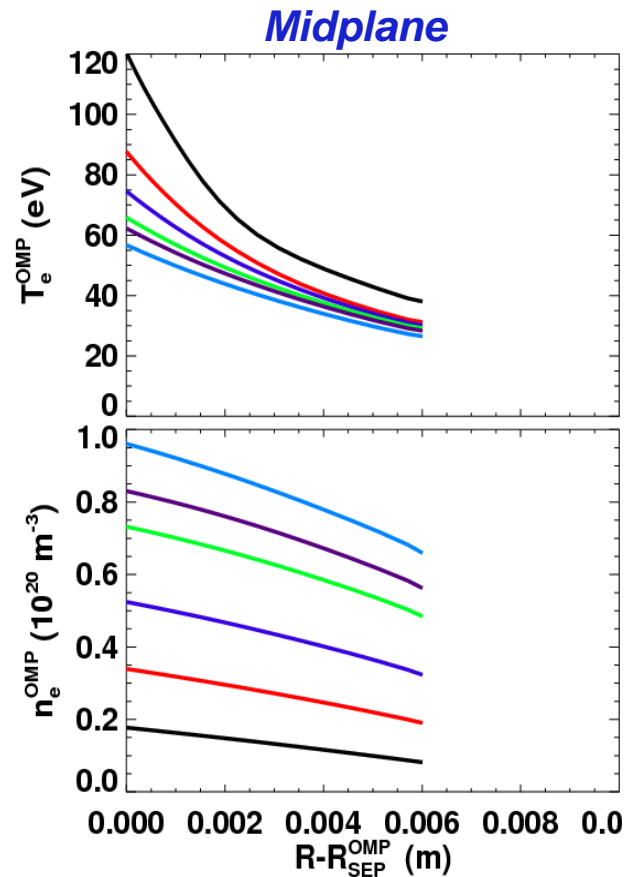
# SOLPS is used to analyze pumping including near-detached conditions

- SOLPS: 2D fluid plasma/neutral transport
  - Plasma transport classical parallel to B (+kinetic corrections), ad-hoc cross-field transport coefficients
  - Kinetic neutral transport using MC code EIRENE
    - More comprehensive treatment of neutral transport (beyond first-flight)
    - Can treat radiative/detached divertor
- Both standard and snowflake divertor with  $R_{OSP} \sim 0.5\text{m}$  studied
  - Note that grid can't extend past pump, so only small SOL region modeled
- Constant  $D=0.5$ ,  $\chi_{e,i}=2.0\text{ m}^2/\text{s}$ 
  - Gives  $\lambda_q^{\text{mid}} \sim 3\text{mm}$
  - No attempt to match expt
- Simulations both without and with carbon included have been performed



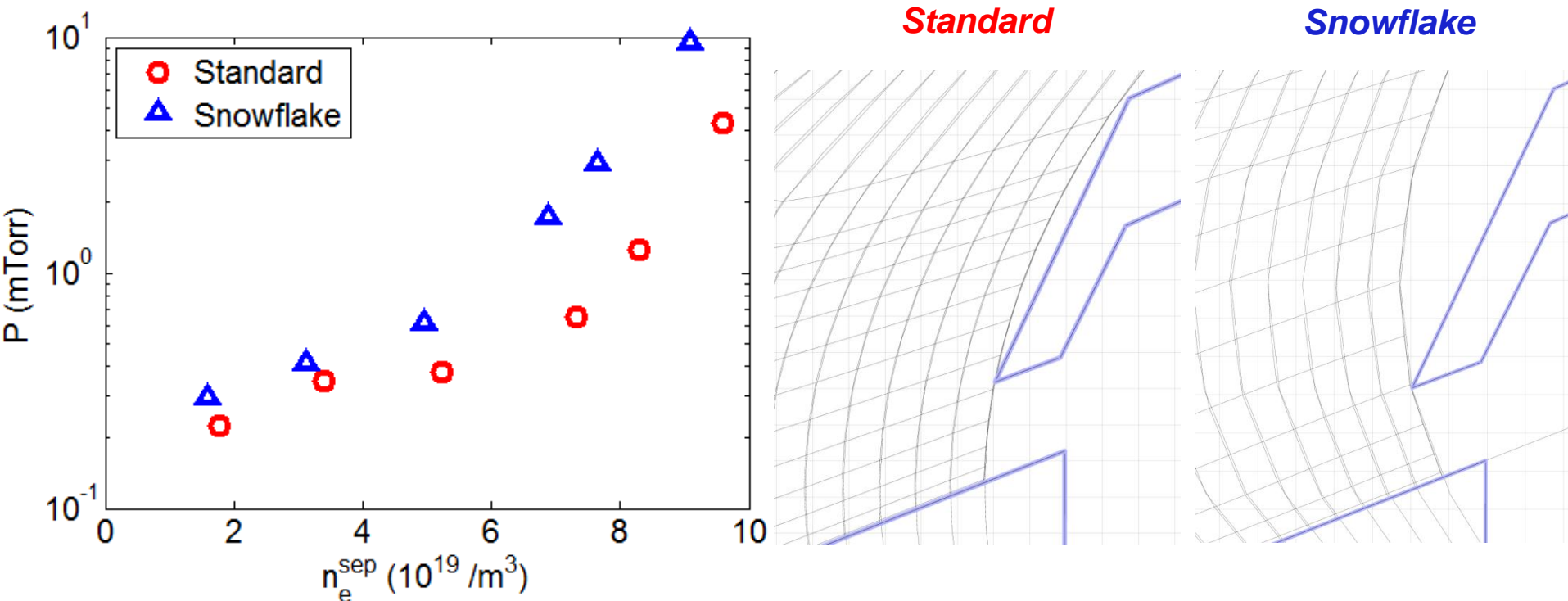
# A wide range of divertor plasma parameters have been modeled

- Input power  $P=10\text{MW}$  in all cases
- $n_e$  at core grid edge set as boundary condition
  - Scanned to vary divertor conditions
- Resulting divertor parameters vary from strongly attached to nearly detached ( $T_e \sim 1\text{eV}$ )



# Snowflake shows higher plenum pressures that standard divertor for similar conditions

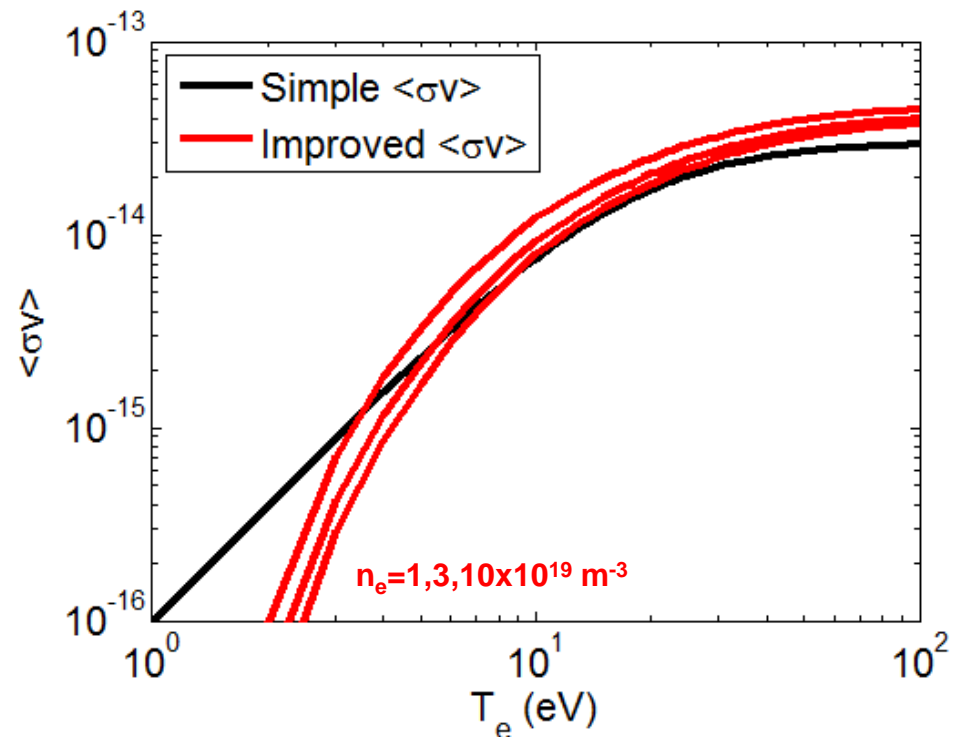
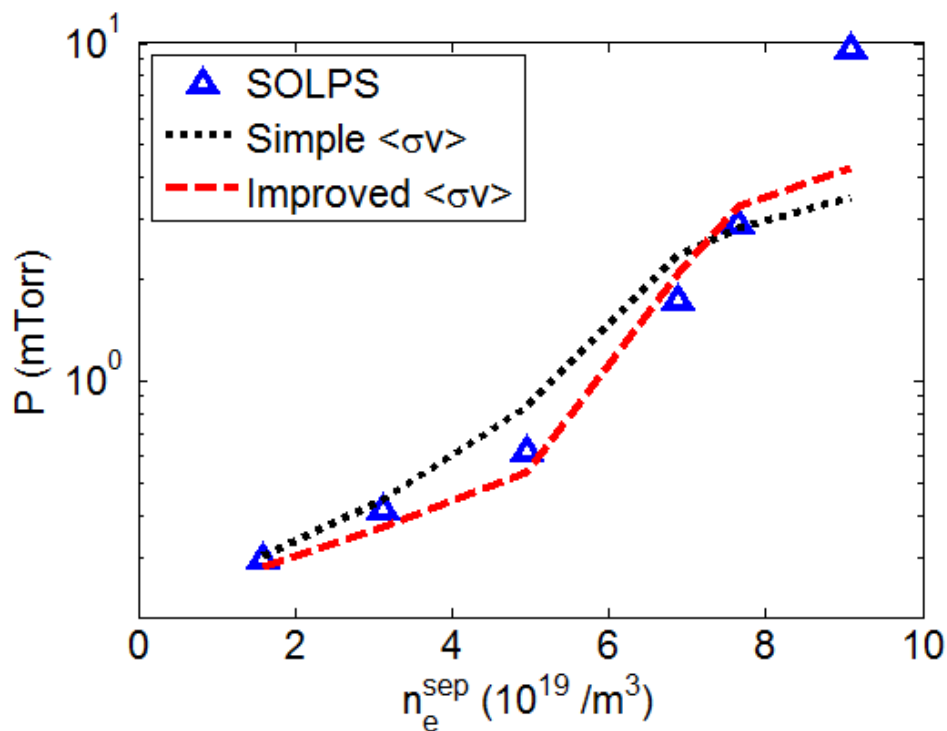
- At same separatrix density, pressure is  $\sim 2x$  higher with Snowflake divertor configuration
- Partially due to geometry of field lines at pump entrance (plasma flux reaches nearer entrance; not accounted for in earlier projections)
- Pressures above 1 mTorr can be reached at high  $n_e$  in both cases





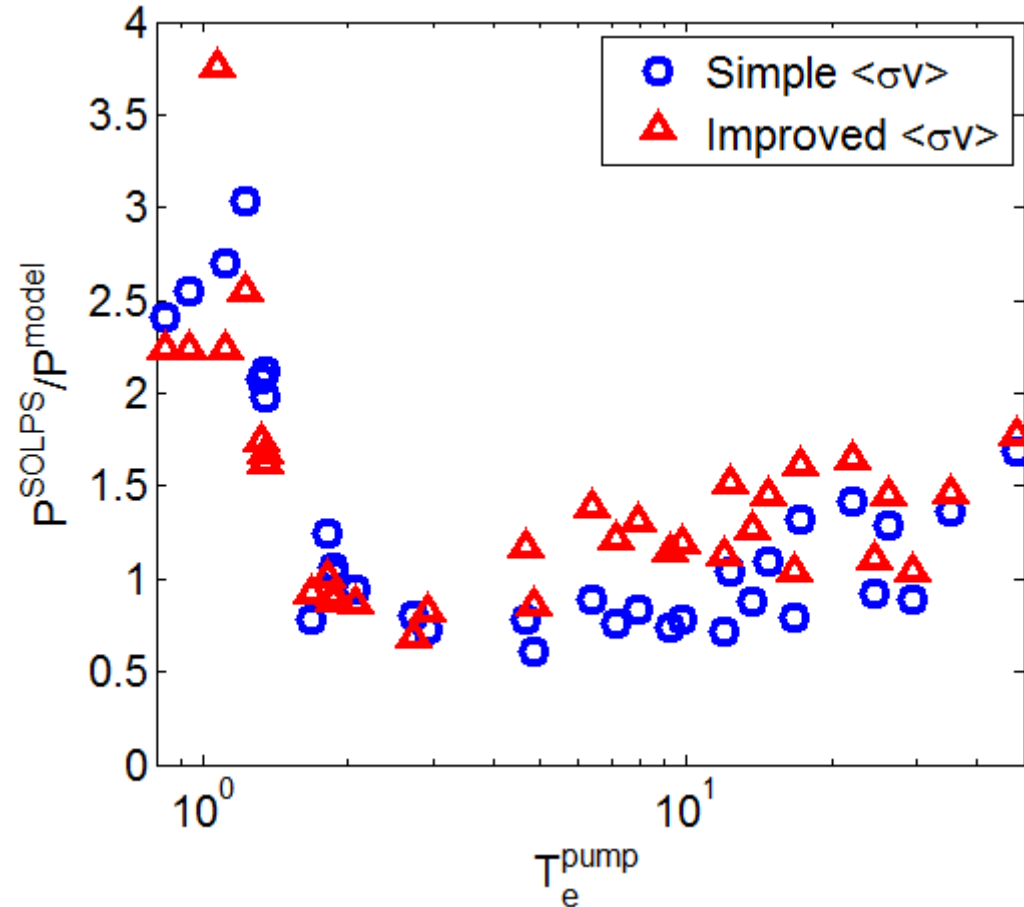
# Plenum pressure from SOLPS shows good agreement with semi-analytic expressions when divertor is attached

- Divertor  $n_e$ ,  $T_e$ ,  $\Gamma_{\perp}$  from SOLPS used in semi-analytic model
- Model reproduces pressure within factor of  $\sim 2$  (except high  $n_e$ )
- Agreement is improved using more accurate ionization rate
  - Simple rate coefficients used in original model:  $\langle\sigma v\rangle_{EII}(r) \approx \frac{3 \times 10^{-16} T_e^2(r)}{3 + 0.01 T_e^2(r)}$
  - Interpolating tables of  $\langle\sigma v\rangle(n_e, T_e)$  as in EIRENE improves comparison



# Semi-analytic model underestimates pressure under detached conditions

- Model pressure close to SOLPS calculation for  $T_e > 2$  eV
  - Often underestimates by ~50%
  - Model does not give large overestimate in any cases
- For  $T_e < 2$  eV SOLPS-calculated pressure is up to ~3x higher than model
  - First-flight neutral model expected to break down
  - Consistent with DIII-D pumping observations



⇒ **Optimization of design presented here is conservative**  
– **Pumping likely to be stronger for realistic conditions**

# Summary

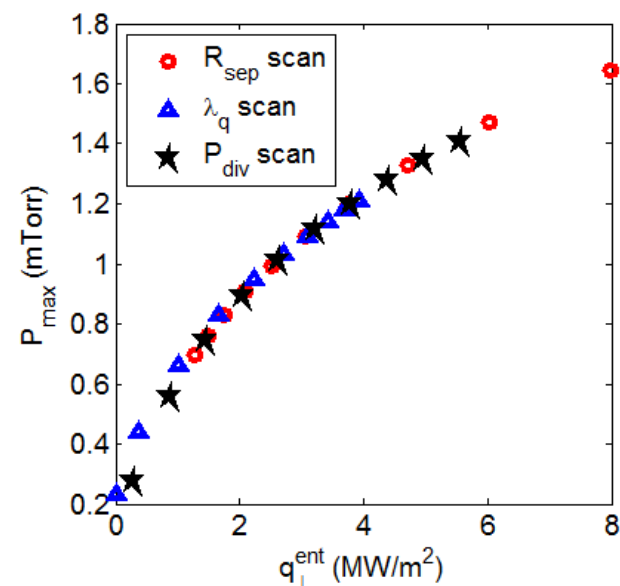
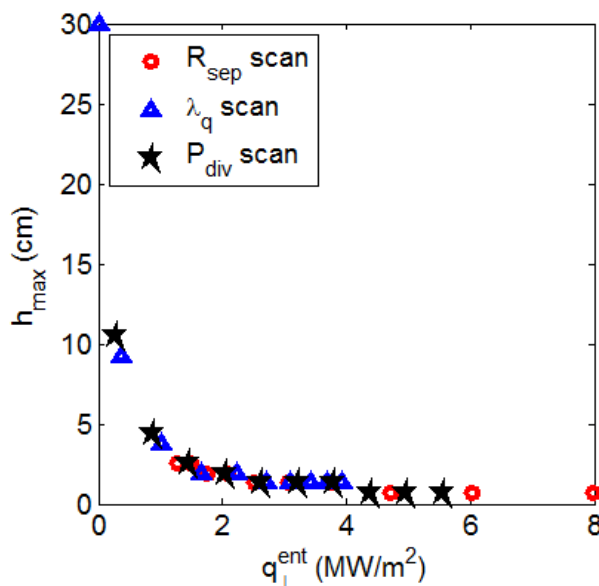
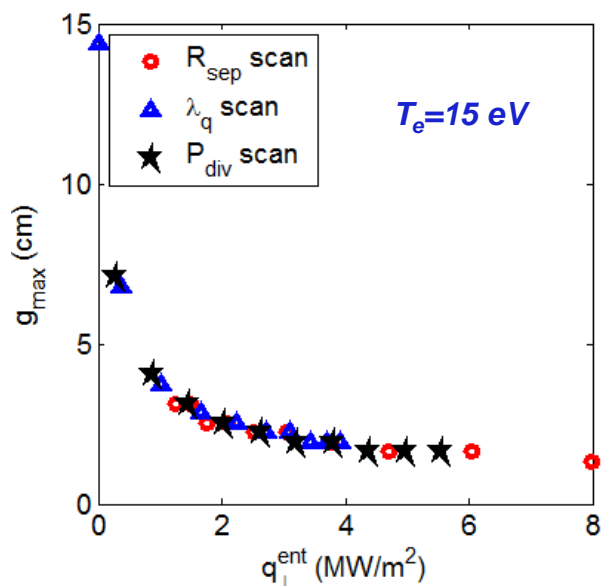
- A promising cryo-pump design point has been identified that is compatible with standard and snowflake divertors
  - Based on semi-analytic pumping model
  - Divertor profile projections based on NSTX data
  - Snowflake shows better pumping than standard divertor
- SOLPS calculations confirm approach taken in design optimization
  - Pumping model adequate under attached conditions
  - Pressure significantly larger than model for  $T_e < 2\text{eV}$
- Next steps in pump design
  - Investigate details of plenum design, compatibility with engineering
    - Begin engineering design
  - Explore interaction between cryo and lithium coatings
    - Coating of pumping surface?
    - Pumping of lithium-modified SOL?

# BACKUP

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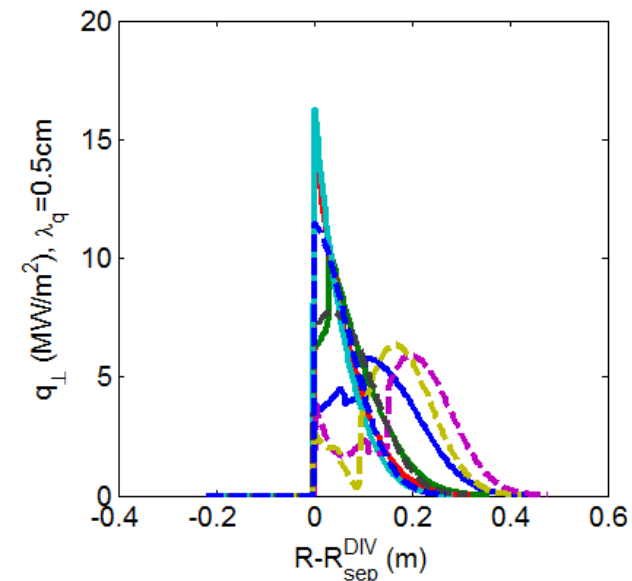
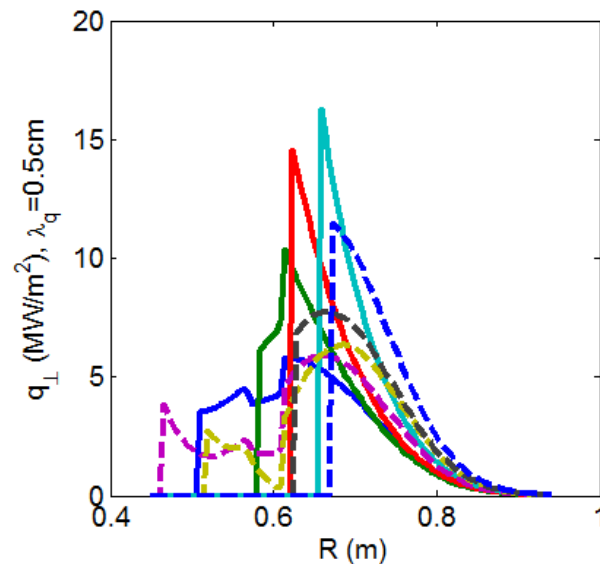
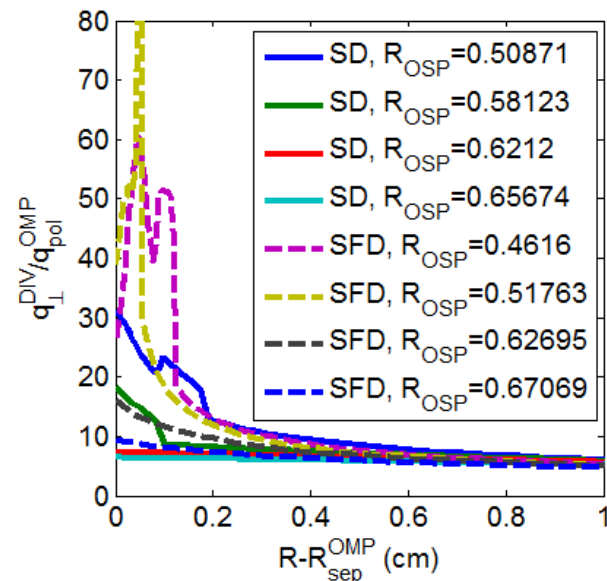
# For given pump entrance position, heat flux at pump entrance orders the “optimal” geometry parameters

- Optimal throat height/length depend mainly on heat flux near entrance
  - Doesn't matter if it's varied by moving the OSP, changing flux expansion, or changing total power
  - $T_e$  affects maximum pressure achievable, but only weakly affects  $g/h$
- Optimizing for  $P=0.8\text{mTorr}$  at  $T_e=15.0\text{ eV}$  gives  $g\sim 2.5\text{ cm}$ ,  $h\sim 2\text{ cm}$  at  $q\sim 2\text{MW/m}^2$

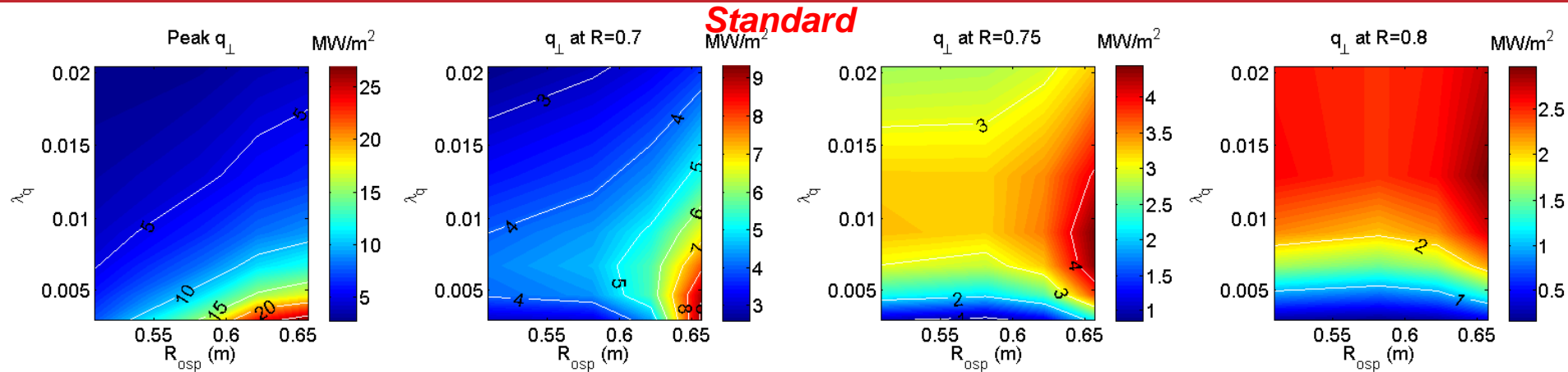


# Projecting heat flux profiles

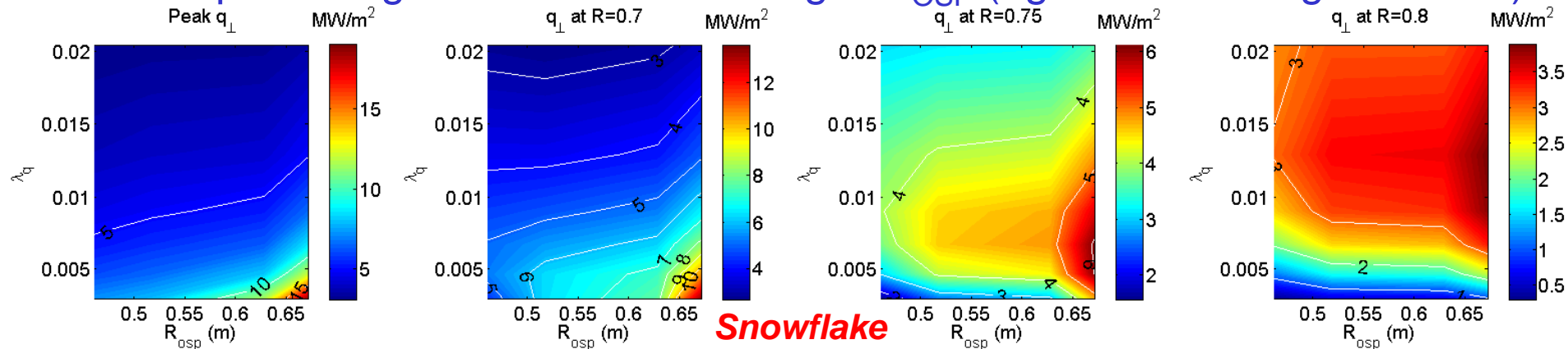
- Exponential poloidal heat flux profile imposed at midplane
  - $P=5$  MW (e.g., 1/2 of 10 MW goes to outer divertor)
  - $\lambda_q^{\text{OMP}} \sim 0.3\text{-}2.0$  cm
- Mapped along field lines to divertor
  - Total geometric heat flux reduction factor shown on left
  - Example heat flux profiles showing for  $\lambda_q^{\text{OMP}}=5\text{mm}$ 
    - Heat flux high at  $R=0.7$ , significantly lower at 0.8



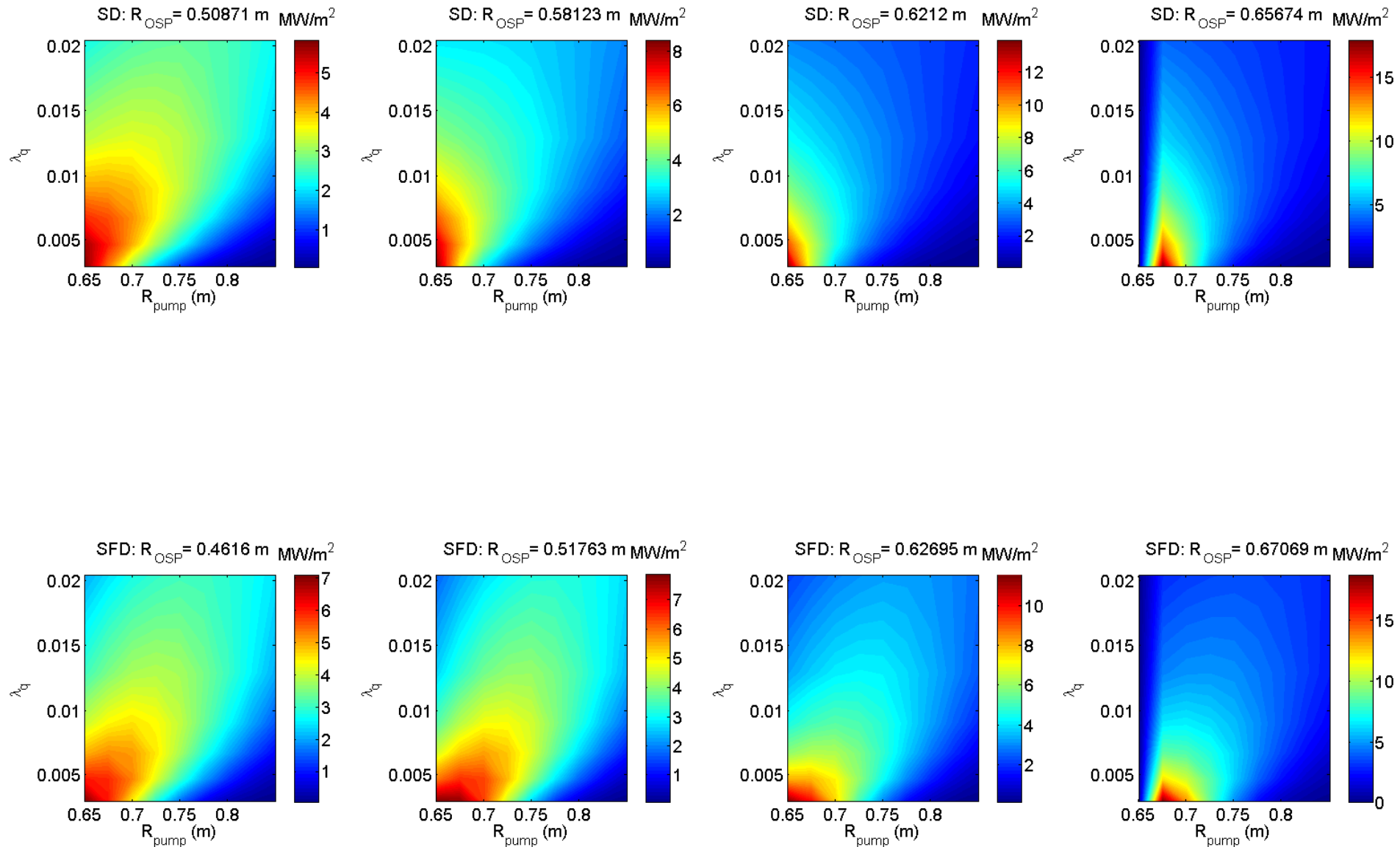
# Heat flux projections show plenum entrance at $R \sim 0.7-0.75$ m likely to provide sufficient pumping



- Power handling: peak heat flux  $< 10 \text{ MW/m}^2$ 
  - Restricts  $R_{\text{OSP}}$  for narrow SOL (wider range for SFD)
- Pumping:  $q_{\perp \text{ entrance}} > \sim 2 \text{ MW/m}^2$ 
  - Requires larger SOL widths for larger  $R_{\text{OSP}}$  (again wider range for SFD)

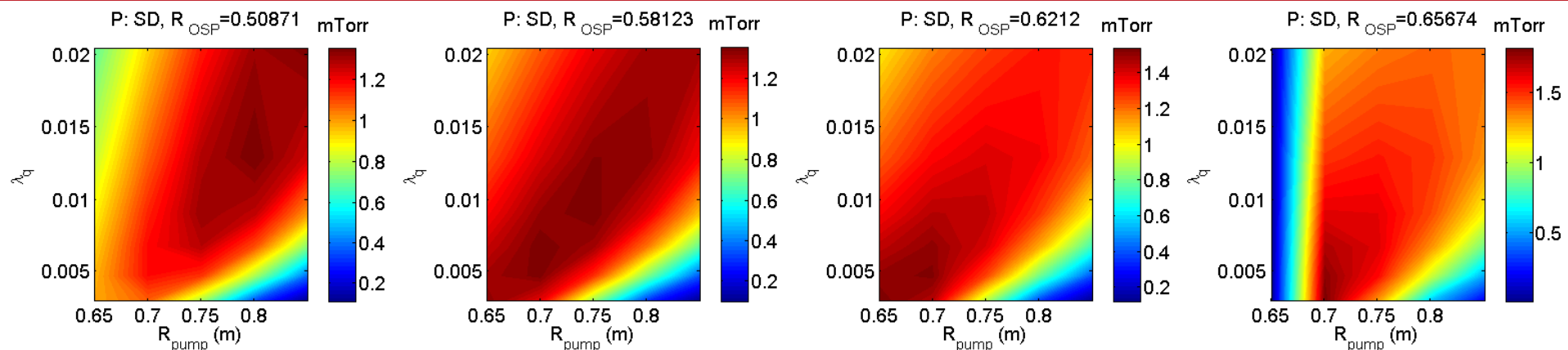


# Heat flux at potential plenum entrances for 8 equilibria

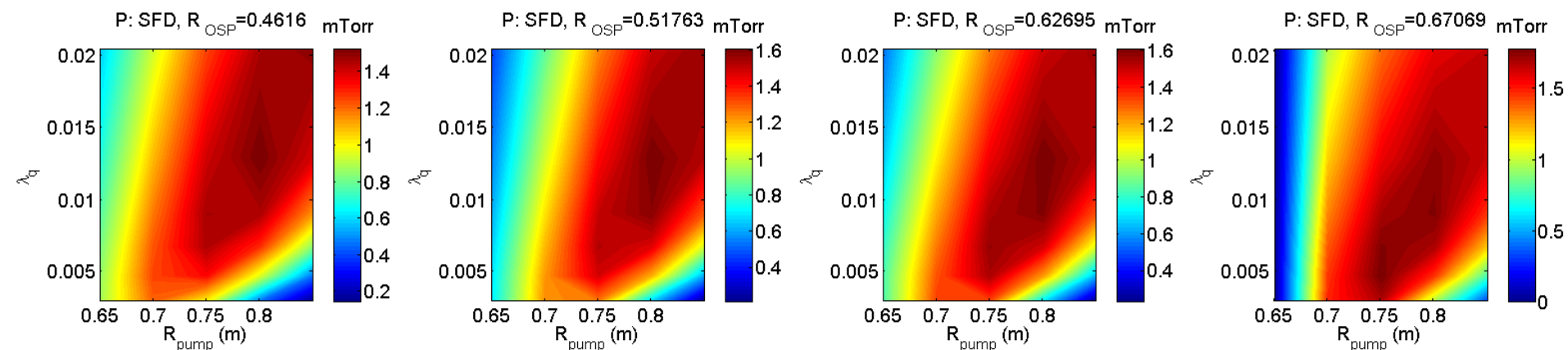




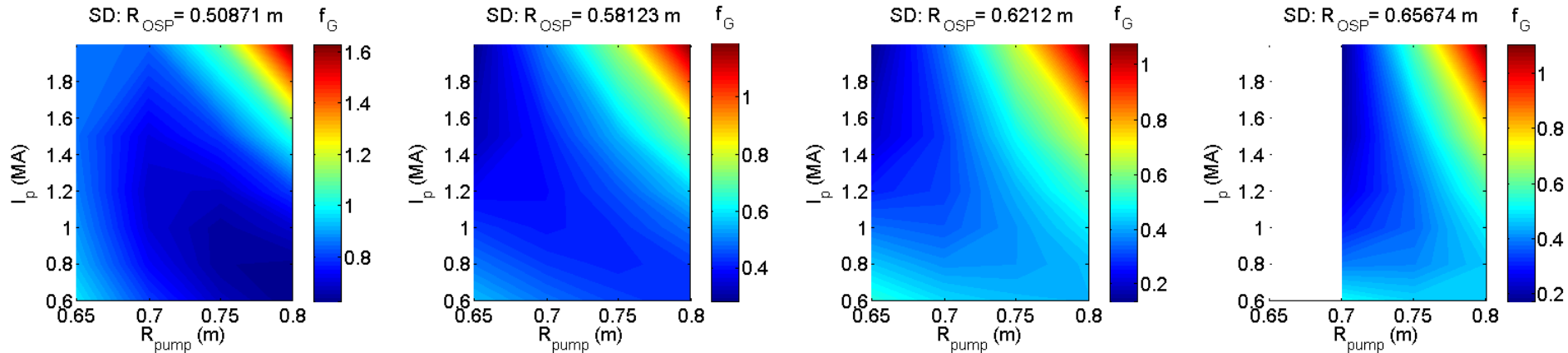
# Projections show plenum entrance at $R=0.72$ can give $>1$ mTorr for wide range of SOL width, equilibria



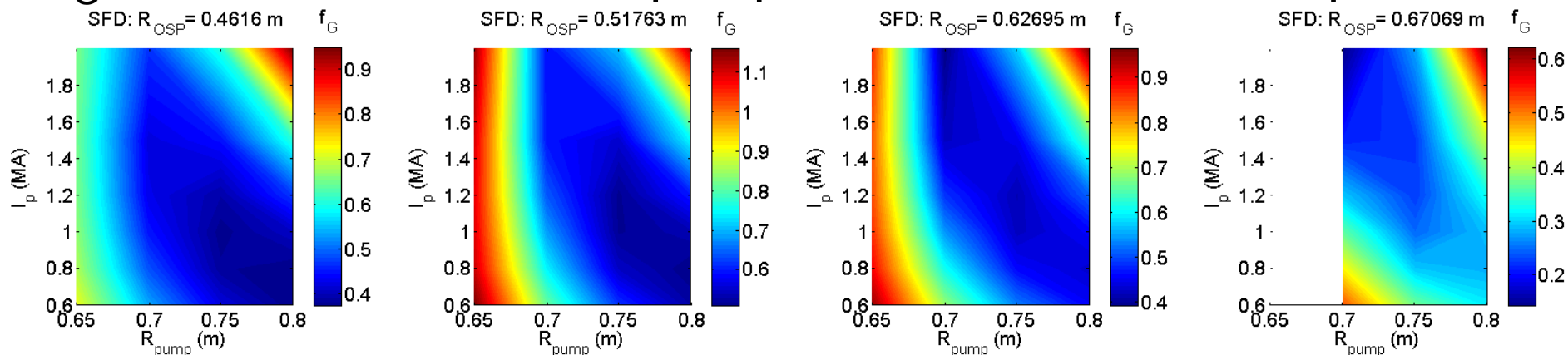
- Heat flux profiles,  $T_e^{\text{div}}$ , and optimized entrance parameters used in analytic model for plenum pressure
- Optimizing position for narrowest SOL gives  $R_{\text{pump}} \sim 0.72$ 
  - Narrow SOL gives least flexibility in moving  $R_{\text{OSP}}$  to improve pumping



# $R_{\text{pump}}=0.72$ supports low Greenwald fraction for range of $I_p$ , equilibria

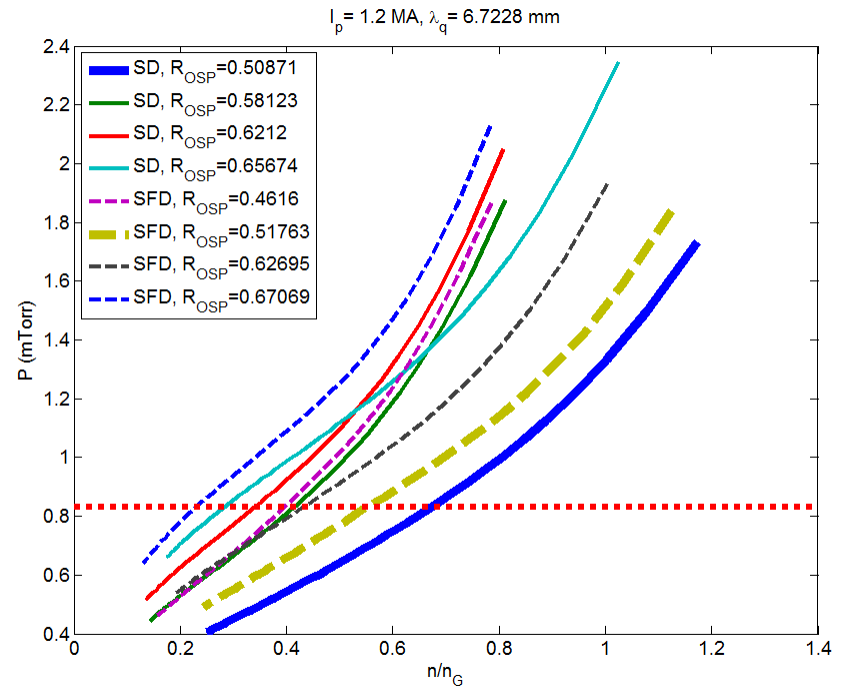
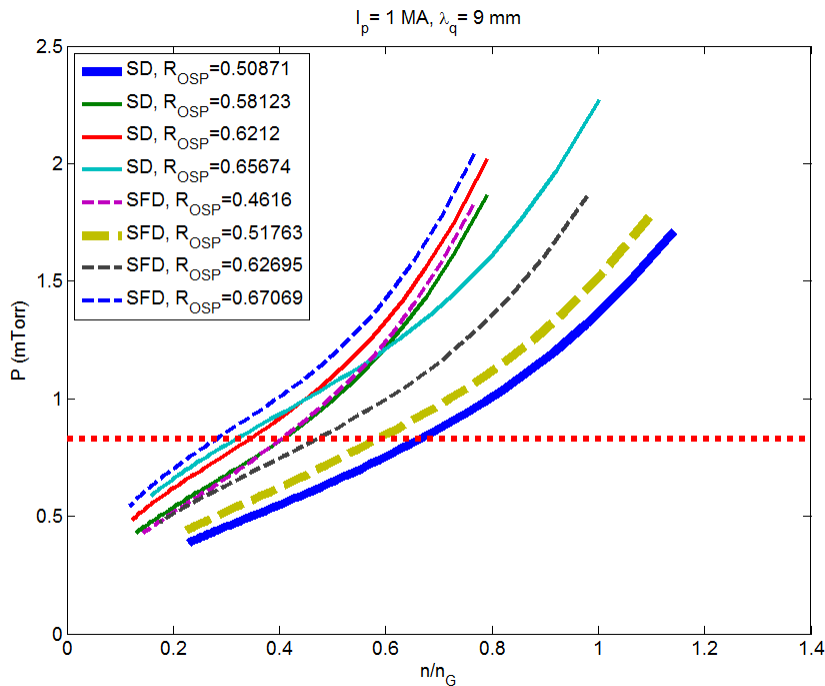


- $q_{\parallel \text{sep}}, T_e^{\text{div}}$  used in modified 2-pt model used to estimate  $n_e^{\text{sep}}$ 
  - $q_{\parallel \text{sep}}$  from  $I_p$  scaling,  $T_e^{\text{div}}$  varied
- $n_e/n_e^{\text{sep}} \sim 3$  assumed to estimate  $f_G$
- $f_G$  shown is that at which pumped flux balances NBI input



# Estimating achievable $n/n_G$

- $n/n_G$  varied by scanning  $T_e^{\text{div}}$
- To pump beams, need  $P \sim 0.8$  mTorr
- $f_G$  shown is where the pumping balances beam input
  - Minimum achievable  $n_e$  -> could puff to increase



# The Basic Two-Point Model

- Begins from the fluid equations and simplifies...
- Provides simple relations for upstream and target (PFC) plasma parameters
- Varying levels of complexity can be implemented
  - Fluid reconstruction via generalized 2-point (e.g. OSM/OEDGE code)
  - Coupling with Monte Carlo neutrals and impurities (e.g. DEGAS 2/EIRENE/DIVIMP)
- **Start with the basics**

**Assume:**

$$T_e = T_i \quad \& \quad p = p_e + p_i$$

$$\frac{d}{dx} \left[ \left( \frac{1}{2} m_i v^2 + 5kT \right) n v - \kappa_{0e} T_e^{5/2} \frac{dT_e}{dx} \right] = Q_R + Q_E$$

**Assume:**

**Conduction Dominates  
Neglect Sources**

$$\frac{d}{dx} \left[ -\kappa_{0e} T_e^{5/2} \frac{dT_e}{dx} \right] = 0$$



$$T_u = \left[ T_t^{7/2} + \frac{7}{4\kappa_{0e}} q_t L \right]^{2/7}$$

# Simple Extensions Attempt to Capture More Physics

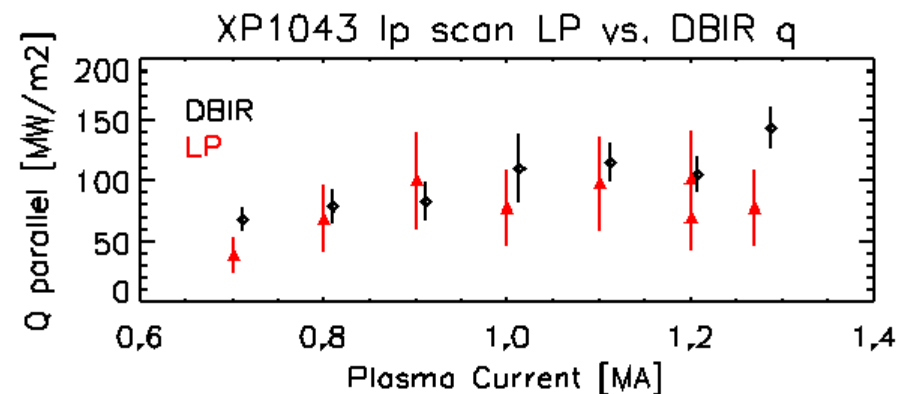
- Volumetric loss terms can be included via  $f_{power}$  term
- Term can be estimated with interpretative modeling in lieu of better div. Bolom. Coverage
- Comparison of nominal LP and DBIR results are encouraging
- Two values of  $f_{power}$  used following: 0 and 0.5

## Radiation and charge-exchange

$$q_{rad} + q_{cx} = f_{power} q_0$$

$$(1 - f_{power}) q_0 = q_t = \gamma n_t c_{st} k T_t$$

$$\frac{T_t}{T_u} \propto (1 - f_{power})^2$$



# Updated Upstream Density

- Force balance in the ST requires modification to 2-PM
  - Typical formulation assumes “straight” flux tubes
  - 1.5m OMP vs. 0.5m target results in significant variation
- Flux-tube definition allows conversion of magnetic field to area
- Not yet consistently applied everywhere in calculations

$$F_u = F_t$$

$$P_u A_u = P_t A_t$$

$$N_u T_u = N_t T_t (1 + M^2) \frac{A_t}{A_u}$$

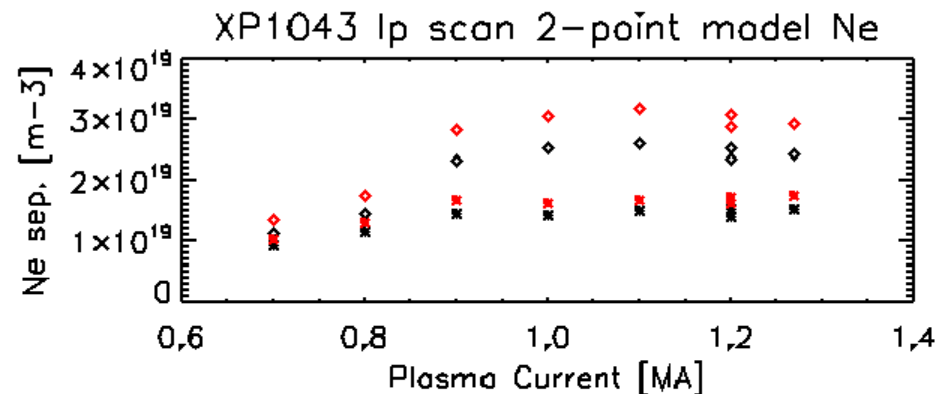
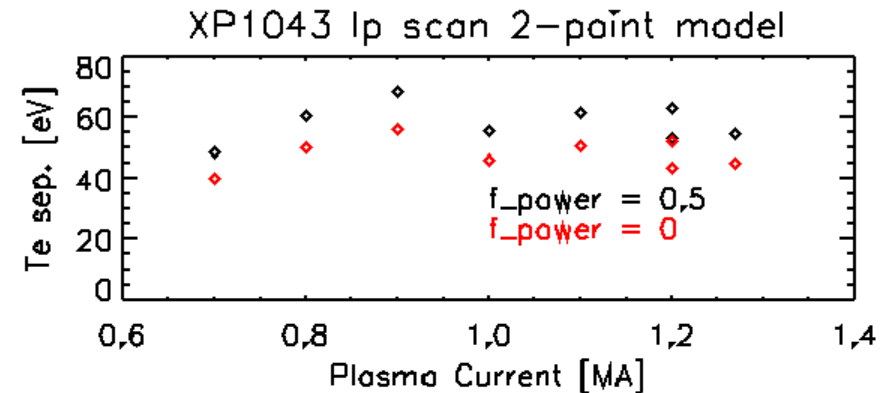
$$M = v/c_s \geq 1 \quad \text{Mach No. at sheath}$$

$$B A = \Psi_0 = \text{const.} \rightarrow \frac{A_t}{A_u} = \frac{B_u}{B_t}$$

$$N_u = \frac{N_t T_t (1 + M^2)}{T_u} \frac{B_u}{B_t}$$

# Upstream Quantities Determined via 2-Point Model

- Parallel connection length calculated from EFIT02
  - $q_{\text{peak}}$  used to locate nominal  $\Psi_N$  value for integration
  - Solution not sensitive to variance in length (robust model from target)
- Interpolated MPTS density at the upstream temperature shown for comparison
- Uncertainty not yet propagated in calculations to determine significance in discrepancy



# Wall fuel uptake is ~zero during long-pulse H-modes in pumped machines

- FY09 Joule Milestone Report
- Close balance is observed between particle input (beams+puff) and pumping
  - True for both DIII-D and C-Mod
  - Motivates pumping the beam input as figure of merit

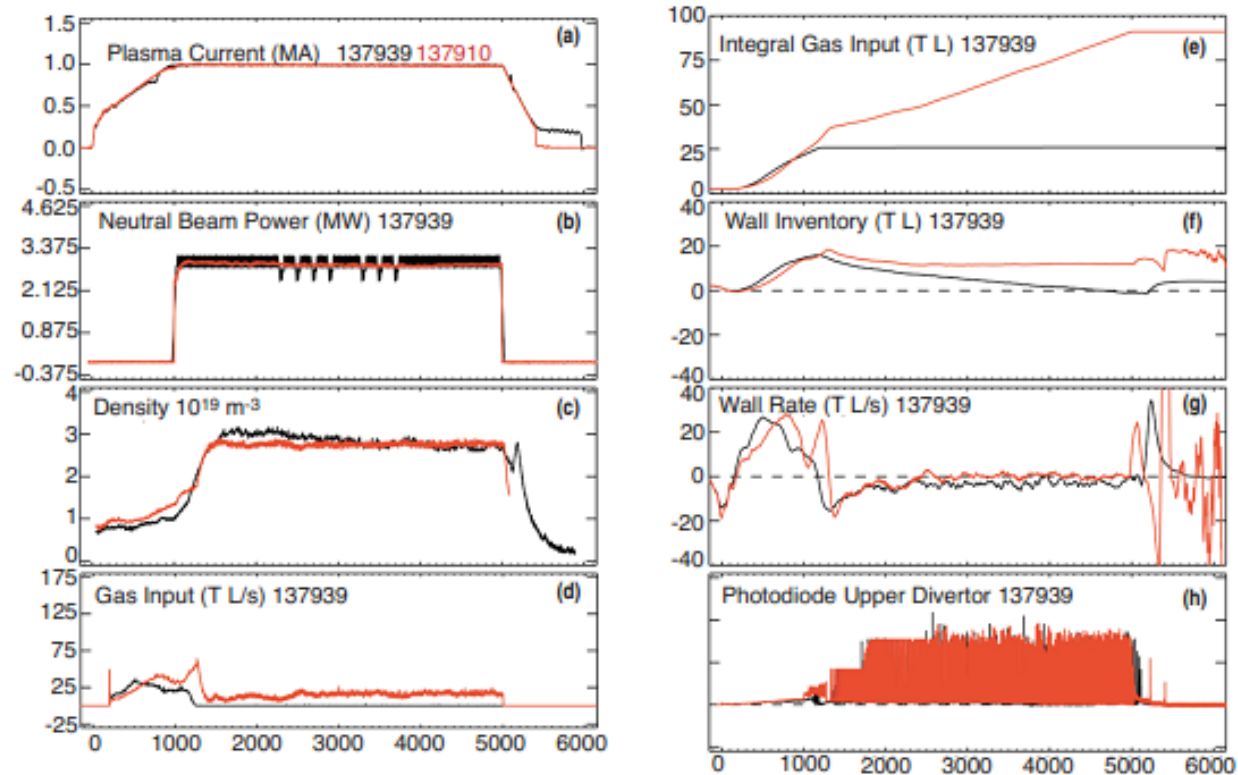


Fig. 2. ECH heated (red) H-mode plasma is compared with a NBI (black) discharge. The plasma current, neutral beam or ECH power, electron density, gas input, integral of the gas input; wall inventory and wall rate from the dynamic particle balance; along with the photodiode signal are compared with a neutral beam heated H-mode DIII-D shot. Note that in both cases, the wall flux is quite large in the L-mode period, but during the ELMing H-mode, the wall flux is very close to zero.