



## Modelling of VDEs with M3D-C1

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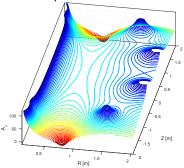


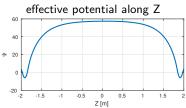




#### VDEs are inherent to diverted tokamak plasmas







- diverted plasma on a saddle due to external field (PF coils) ⇒ elongation, vertically unstable equilibrium
- conducting structures do not allow fast flux changes ⇒ passive stabilisation + feedback control
- loss of vertical control leads to deleterious contact with wall
  - transfer/induction of current from core  $\rightarrow$  halo  $\rightarrow$  wall  $\Rightarrow$  forces and stresses
  - scraping-off of  $q_{edge}$  < 2  $\Rightarrow$  3D instabilities (kink), toroidal peaking of forces
  - thermal collapse, impurities ⇒ breaking of flux surfaces, runaway electrons

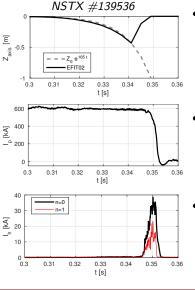
## Damaging power of VDEs calls for realistic modelling

- forces during VDEs lead to structural damages of PFCs, can result in machine shutdown
  - worst case VDE is a design drive for ITER
  - need for avoidance (preemptive measures) and mitigation (damage control)
- abundant experimental data to be analysed and interpreted
  - provide theoretical/modelling support
  - help interpret measurements and optimise diagnostics for wall/halo currents

#### Basic/fundamental questions:

- 1. What are the keys dynamics/regimes/phases of VDEs?
  - rich literature, reduced models, linear theories, Halo/Hiro debate
  - self-consistently assembling the pieces of the puzzle is not trivial (stiffness)
- 2. Can we simulate/model VDEs accurately enough to feel confident about predictions for ITER ?
  - **difficult**: 2D + prescriptions OK, 3D not (yet) with realistic parameters
  - 3D: computationally far more expensive, profoundly richer physics than 2D

### Phenomenology of VDEs serves as modelling targets



- drift phase [Pfefferlé, 2016]  $t_D \sim (L_w/R_w)(I_p/I_d)(Z_d/Z_w)^2 \sim 30$ ms
  - slow relaxation process
  - plasma mostly in force balance
  - advection (≈ rigid body), inductive coupling with wall ⇒ implicit scheme
- current quench  $t_{CQ} \gtrsim L_p^*/R_p^* \sim 3ms$  [Wesley, 2006]
  - ${\mathord{\hspace{1pt}\text{--}}}\xspace$  current transfer/induction from plasma to wall
  - $\ \, \text{flux scrape-off (advection-diffusion)} + \\ \text{time-evolving resistivity via temperature}$
- ullet normal wall currents  $\Delta t_H \sim t_{CQ}$  [Myers, 2016]
  - shared/induced currents in resistive halo
  - early  $n=1\sim n=0$  components
  - counter- $I_p$  rotation  $\Omega R \sim 3 \mathrm{km/s} = 0.1 c_s$  for max 4 turns

# VDEs progress through multiple phases/regimes associated with specific numerical difficulties

- 1. vertical drift phase (adiabatically evolving MHD equilibrium)
  - slow advection and force balance
    - fixed mesh (resolution), leading edge surface currents, spurious numerical modes
    - role of sources and sink to avoid/trigger internal instabilities (early thermal quench)
    - time-varying PF coil currents, loop voltage, pellet injection
  - plasma/wall inductive coupling and resistive decay of wall currents
    - wall shape and 3D geometry, holes and cuts (poloidal or toroidal gaps), materials with different resistivities
    - coupling with engineering code VALEN
- 2. axisymetric plasma contacting wall
- 3. 3D plasma contacting wall

# VDEs progress through multiple phases/regimes associated with specific numerical difficulties

- 1. vertical drift phase (adiabatically evolving MHD equilibrium)
- 2. axisymetric plasma contacting wall
  - multi-region problem
  - "heat" equation for flux scrape-off
    - induced (time-varying) vs shared currents (spatially non-uniform, potential build-up)
  - fast evolution of temperature  $\rightarrow$  resistivity (cold wall, hot core)
    - thermal conductivity profile
    - sharp gradients vs resolution ⇒ anisotropic mesh
- 3. 3D plasma contacting wall

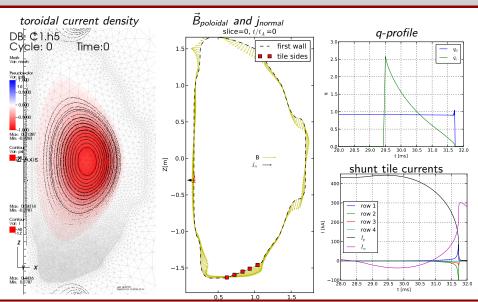
# VDEs progress through multiple phases/regimes associated with specific numerical difficulties

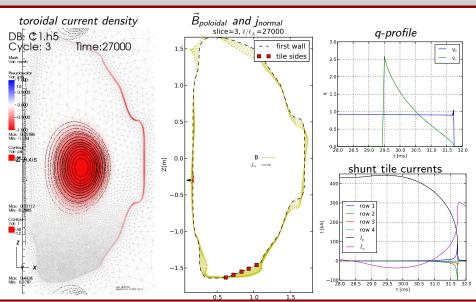
- 1. vertical drift phase (adiabatically evolving MHD equilibrium)
- 2. axisymetric plasma contacting wall
- 3. 3D plasma contacting wall
  - external kink instabilities 2/1, 3/2, 1/1 (+coupling)
  - stabilising role of halo and/or Hiro currents
    - width, breadth
    - $\blacksquare$  temperature  $\rightarrow$  resistivity
  - deformation of flux-surfaces (equilibrium) vs formation of flux tubes (growing current-carrying islands)
  - torque and rotation
    - plasma flow, rotating instability, spinning coin
    - boundary conditions

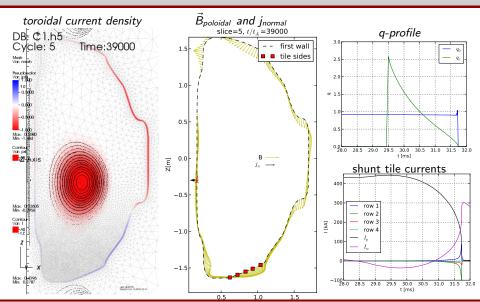
# M3D-C1 is a state-of-art FEM implicit code, suitable for modelling VDEs

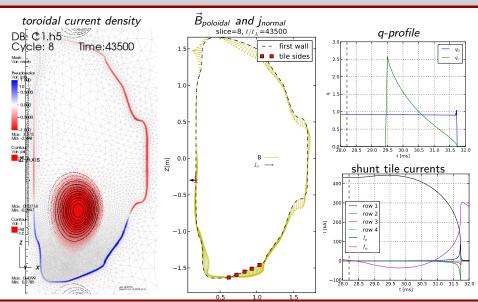
#### Typical setup, parameters and recipe:

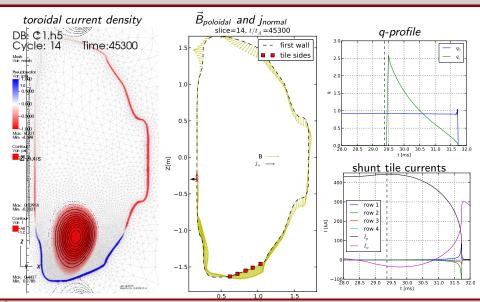
- 0.a 3 region anisotropic mesh for plasma, wall and vacuum
- 0.b Grad-Shafranov equilibrium reconstruction from experimental profiles (geqdsk) and coil currents
  - 1. 2D nonlinear implicit runs, tuned to match realistic timescales
    - Spitzer resistivity imes 30  $\Rightarrow$  Lundquist  $S \sim 10^8 10^9$
    - 2cm wall with resistivity  $\eta_w = 1.9 \times 10^{-6} \Omega m$
    - thermal conductivity  $\kappa_T=10^{-6}\kappa_0$
    - halo region:  $n_h = 10^{18} m^{-3}$ ,  $p_h = 8 \text{ Pa}$ ,  $T_h = 25 \text{eV}$ 
      - effective temperature for halo resistivity  $T_h = 9eV$
  - 2. linear analysis launched at different times during 2D drift phase
    - monitor n > 0 modes, compare instantaneous growth rates with n = 0
  - 3. 3D nonlinear **implicit** runs started when plasma almost contacts wall
    - 48 toroidal planes
    - 4608 cores for 300'000 CPU hours
    - still in progress due to NERSC queues

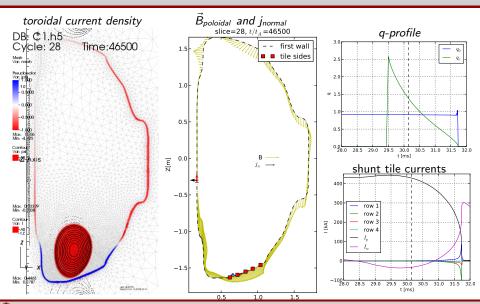


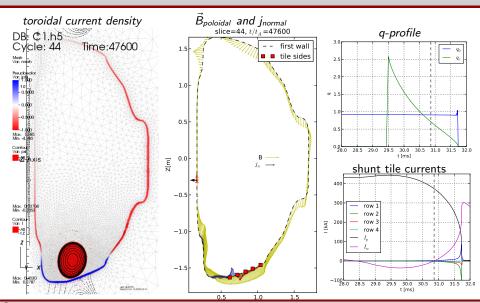


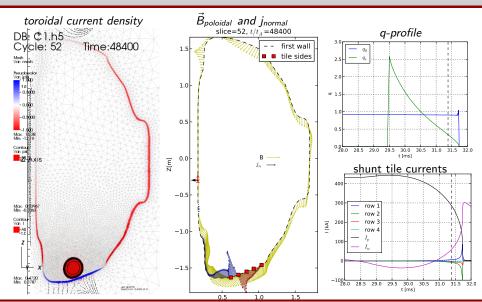


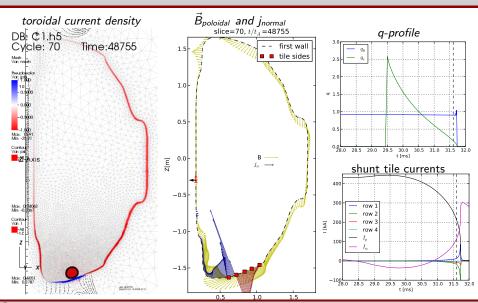


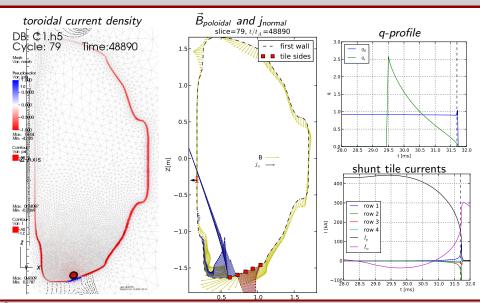


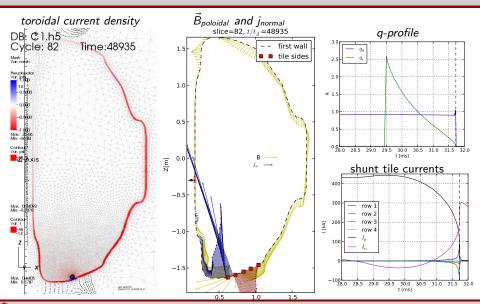


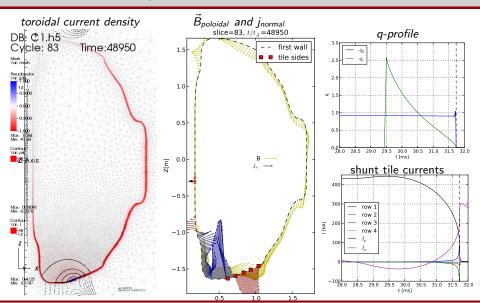


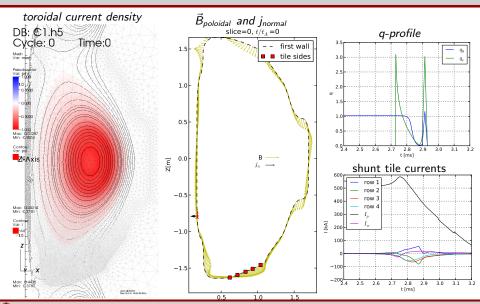


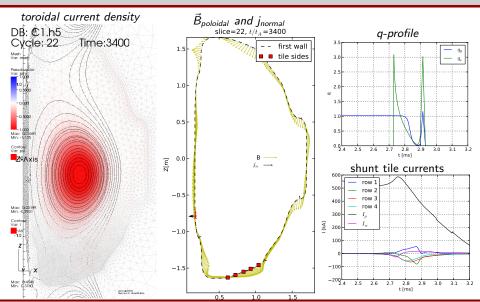


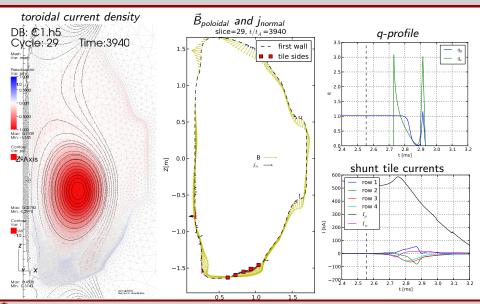


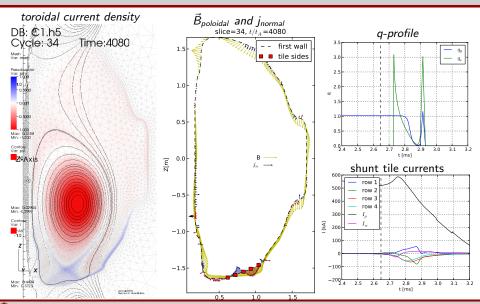


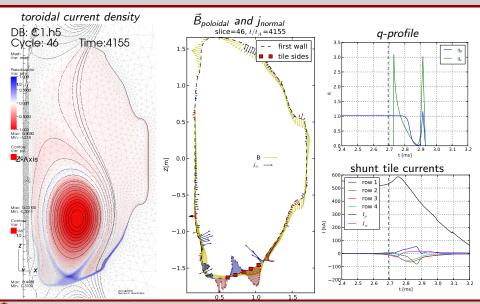


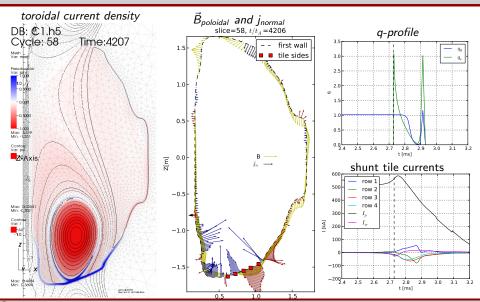


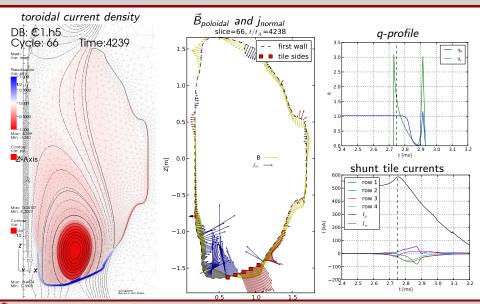


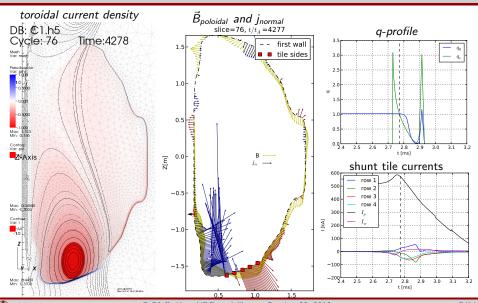


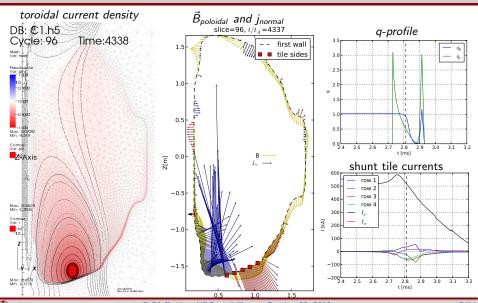


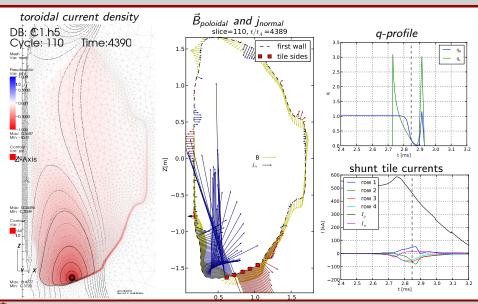


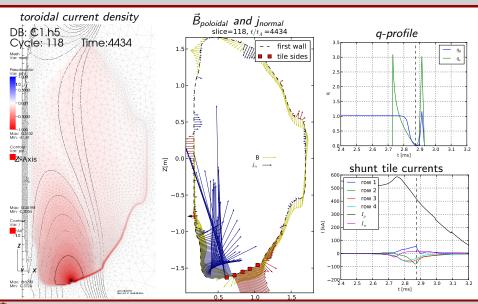


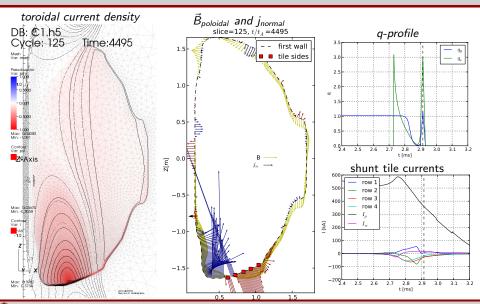


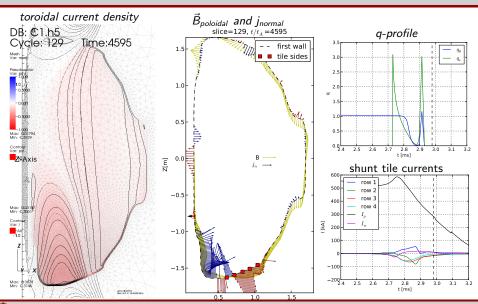


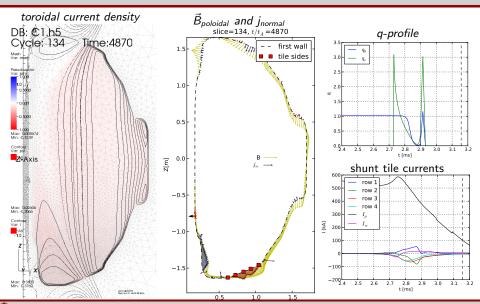








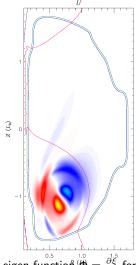




#### Comments about 2D nonlinear runs

- plasma current is slowly decaying  $(L_p/R_p)$  without loop voltage
- ullet current density naturally peaks during slow drift phase  $\Rightarrow q_0 < 1$ 
  - core stability, internal/external inductance (coupling with wall)
  - internal kink can precipitate thermal quench
- $T_h = 9 \text{eV}$  for halo resistivity reduces induced halo currents
  - no negative toroidal currents at separatrix
  - plasma current evolution  $I_p(t)$  is rounder during quench
    - contact point is narrower ⇒ slower flux release
    - later appearance and shorter duration of normal wall currents
  - growth rates decrease with halo temperature (in particular n = 0)

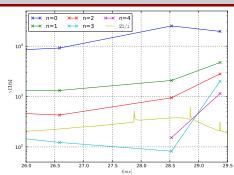
### Linear analysis informs on non-axisymmetric modes and when to initiate 3D run



eigen-function  $\Phi^{0.5} = \frac{\partial \xi}{\partial t}$  for

n = 1 at  $t = 45300 \tau_{\Delta}$ 

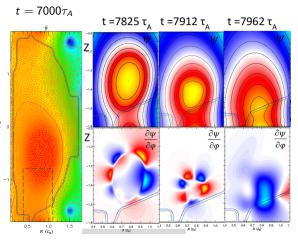
NSTX-U



- core modes during drift phase
  - current density peaks causing drop of  $q_0 < 1$
  - sawtooth instability could be used as a proxy for thermal quench
- n = 0 linear growth-rate from kinetic energy is higher than non-linear evolution of  $z_{axis}$ 
  - poloidal rotation (sliding) + contraction

#### 3D nonlinear runs launched as plasma contacts wall

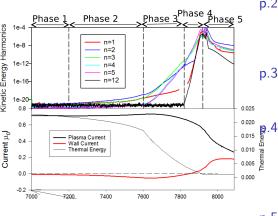
Here showing case with  $\eta_W = 5 \times 10^{-4} \Omega m$ ,  $T_h = 24 eV$ 



- computationally expensive and sensitive to run
  - 300'000 CPU hoursalleviate numerical
- alleviate numerical build-up of gradients via
  - time-step, viscosity, conductivity, resistivity
- anisotropic mesh helps
- non-axisymmetric modes confined to edge
  - halo high temperature, i.e. low resistivity
  - stabilising surface currents
  - stable core to n > 0
  - $q_e$  drops below  $q_0 \sim 1$

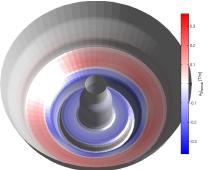
#### 3D nonlinear runs reveal stiff dynamics

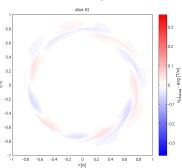
Here showing case with  $\eta_W = 5 \times 10^{-4} \Omega m$ ,  $T_h = 24 \text{eV}$ 



- p.1 drifting plasma (in 3D)
- p.2 vertical motion stalls due to induced n = 0 wall currents
  - scrapping-off of LCFS but  $q_e > 2$  stable
- p.3 edge surface currents develop as  $q_{\rm e} < 2$ 
  - stabilise external kink
  - .4 rapid growth of all modes
    - violent termination of plasma as  $q_e < 1$
    - complete loss of temperature (flux-surfaces)
- p.5 current decay in residual cold plasma

normal currents on wall (total)

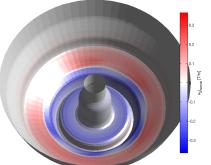


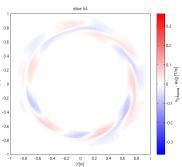


- amplitude quantitatively matches experimental shunt tile
- pattern rotation / zonal component
  - n = 3 → n = 1, stretching → shrinking of current tubes
  - globally zero momentum

<sup>&</sup>lt;sup>1</sup>C1WC: post-processing MPI parallelised FORTRAN code coupled to FIO

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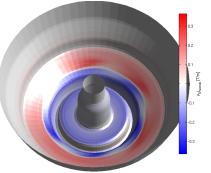


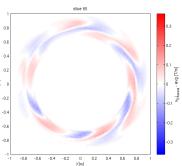


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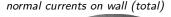
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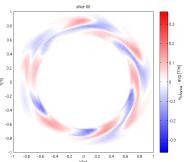


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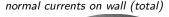




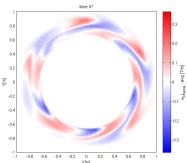


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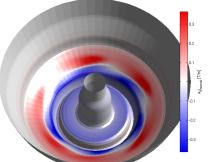


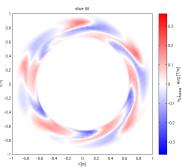


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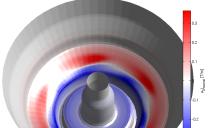


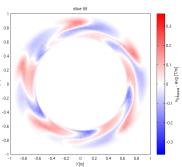


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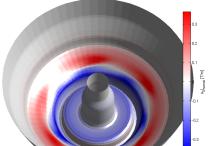




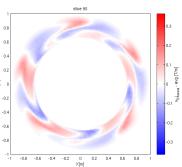
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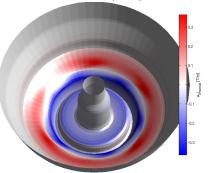


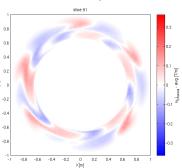
normal currents on wall (non-axisymmetric)



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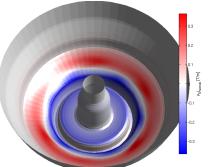




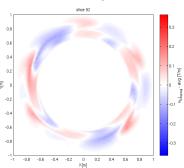
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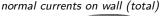
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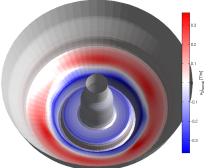


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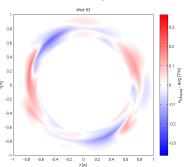


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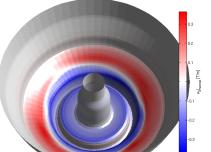


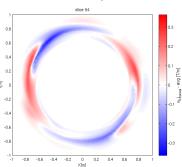
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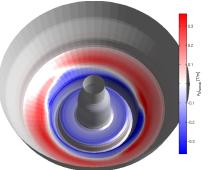


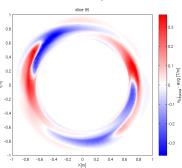


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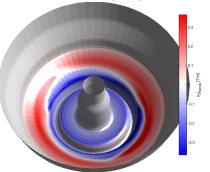




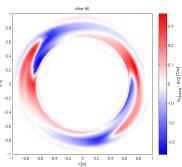
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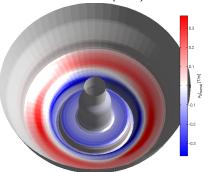


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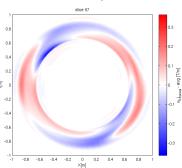


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  - globally zero momentum

normal currents on wall (total)

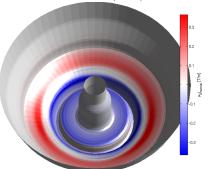


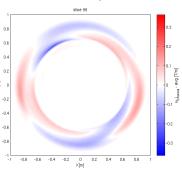
normal currents on wall (non-axisymmetric)



- · amplitude quantitatively matches experimental shunt tile
- pattern rotation / zonal component
  - $-n=3 \rightarrow n=1$ , stretching  $\rightarrow$  shrinking of current tubes
  - globally zero momentum

normal currents on wall (total)

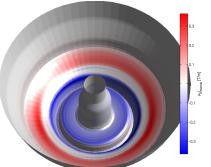




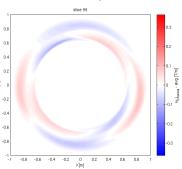
- · amplitude quantitatively matches experimental shunt tile
- pattern rotation / zonal component
  - $-n=3 \rightarrow n=1$ , stretching  $\rightarrow$  shrinking of current tubes
  - globally zero momentum

<sup>&</sup>lt;sup>1</sup>C1WC: post-processing MPI parallelised FORTRAN code coupled to FIO

normal currents on wall (total)

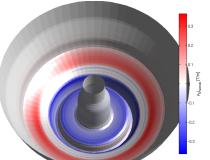


normal currents on wall (non-axisymmetric)

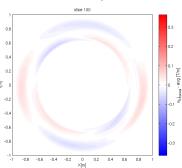


- amplitude quantitatively matches experimental shunt tile
- pattern rotation / zonal component
  - $-n=3 \rightarrow n=1$ , stretching  $\rightarrow$  shrinking of current tubes
  - globally zero momentum

normal currents on wall (total)



normal currents on wall (non-axisymmetric)



- · amplitude quantitatively matches experimental shunt tile
- pattern rotation / zonal component
  - $-n=3 \rightarrow n=1$ , stretching  $\rightarrow$  shrinking of current tubes
  - globally zero momentum

#### **Summary and conclusions**

- M3D-C1 is employed to model NSTX VDEs with realistic parameters
  - resistive wall capability with finite thickness
  - anisotropic mesh to resolve sharp gradients at plasma/wall contact point
  - implicit scheme to resolve advection-diffusion stiff problem
- faster 2D nonlinear runs are used to meet experimental timescales
- linear analysis to assess growth and structure of non-axisymmetric modes
- massive 3D nonlinear runs for evolution/saturation of non-axisymmetric wall currents
- virtual diagnostics of normal wall currents to compare with experimental data

#### Ongoing work and future plans

#### Simulations, numerics

- more 2D runs: fine-tuning of wall resistivity, halo temperature, heat conductivity, loop voltage,...
- as many 3D runs as possible: convergence with toroidal planes, timing of 2D to 3D switching, smoothing/damping of numerical instabilities,...

#### · Analysis, interpretation and comparison with experimental data

- sequence of events  $(z_{mag}, \text{ total currents}, \text{ q-profile}) + \text{linear study}$
- halo currents, wall forces, mode rotation, torque, TPF,...
- virtual diagnostics for shunt tiles + magnetic probes

#### • Extensions and additional effects

- CHI gap (enforce zero poloidal wall currents)
- non-uniform / non-axisymmetric wall resistivity
- toroidal rotation, torque, plasma/wall boundary conditions, sheath physics



#### Bibliography I

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- X. Wesley, Journal (2006).
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