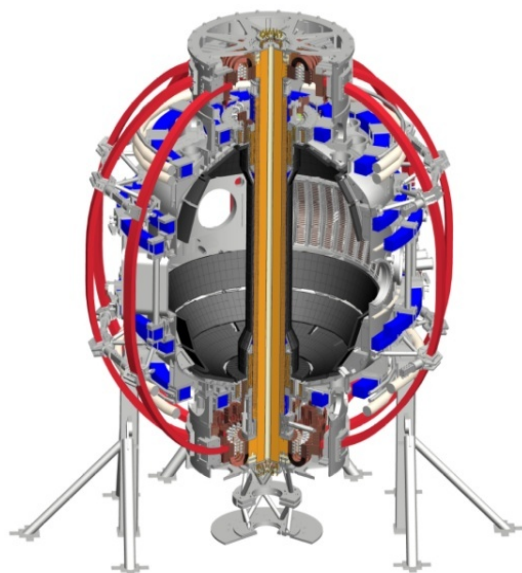


Effects of MHD instabilities on Neutral Beam current drive

M. Podestà, M. Gorelenkova, D. S. Darrow,
E. D. Fredrickson, S. P. Gerhardt,
W. W. Heidbrink, R. B. White
and the NSTX-U Research Team

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Reliable, quantitative predictions of Energetic Particle (EP) dynamics are crucial for burning plasmas

- EPs from Neutral Beam (NB) injection, alphas, RF tails drive instabilities,
 - e.g. Alfvénic modes – AEs
 - With instabilities, ‘classical’ EP predictions (e.g. for NB heating, current drive) can fail
- > Predictive tools are being developed, validated for integrated modeling of these effects in present and future devices (ITER, Fusion Nuclear Science Facility – FNSF)*

Outline

- NSTX discharges with strong MHD are used to test and validate EP transport models
- Modeling methods beyond ‘classical’ EP physics are developed to account for MHD effects
- New model captures MHD modifications of EP phase space leading to Neutral Beam current redistribution

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Alfvénic modes (AEs) and kink-like modes degrade fast ion confinement, plasma performance

NSTX

Major radius 0.85 m

Aspect ratio 1.3

Plasma current ~ 1 MA

Toroidal field < 0.55 T

Pulse length < 2 s

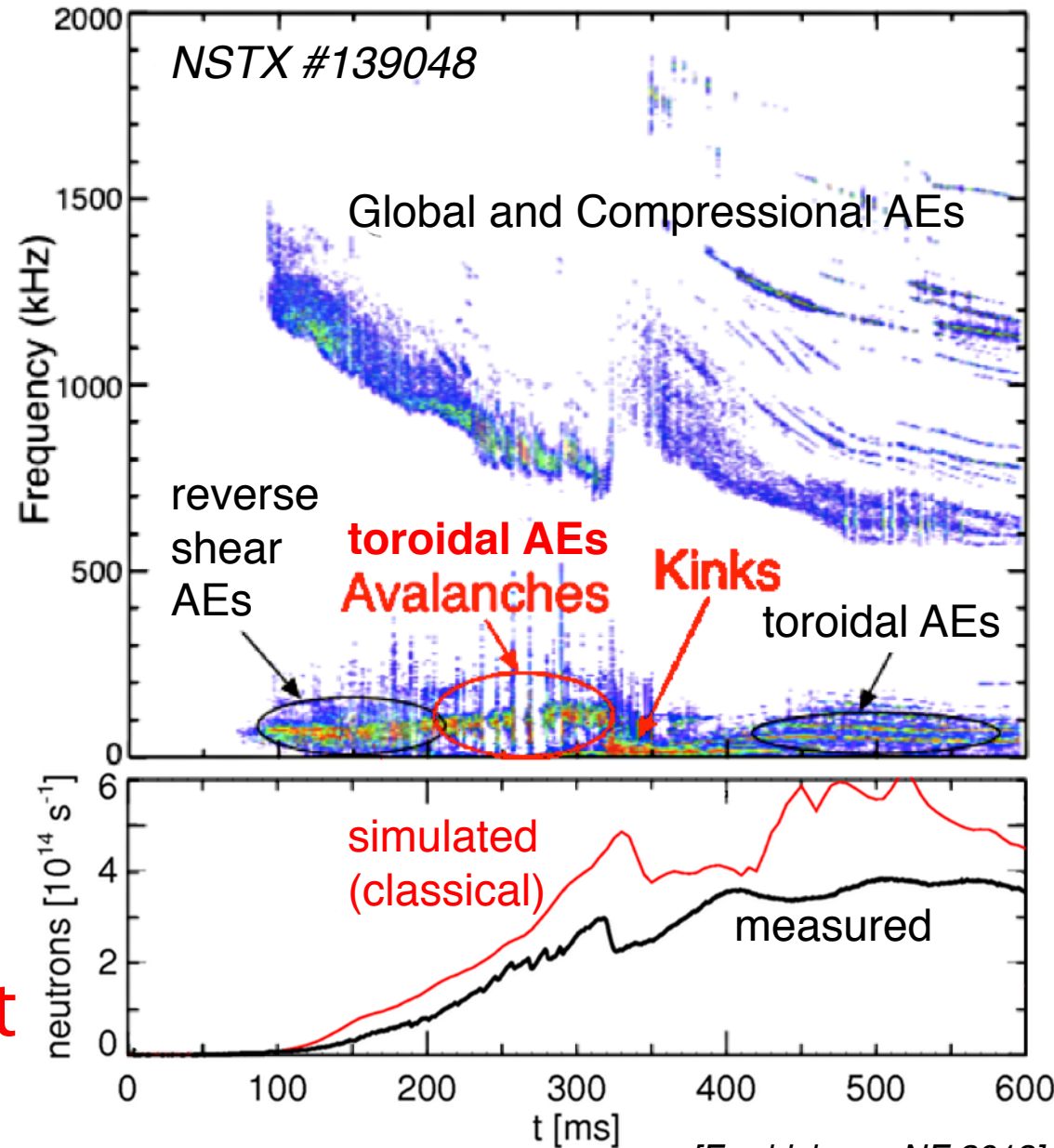
Neutral Beam sources:

$P_{\text{NBI}} \leq 6$ MW

$E_{\text{injection}} \leq 95$ keV

$1 < v_{\text{fast}}/v_{\text{Alfvén}} < 5$

Super-alfvénic ions,
high β_{fi} : plethora of fast
ion driven instabilities



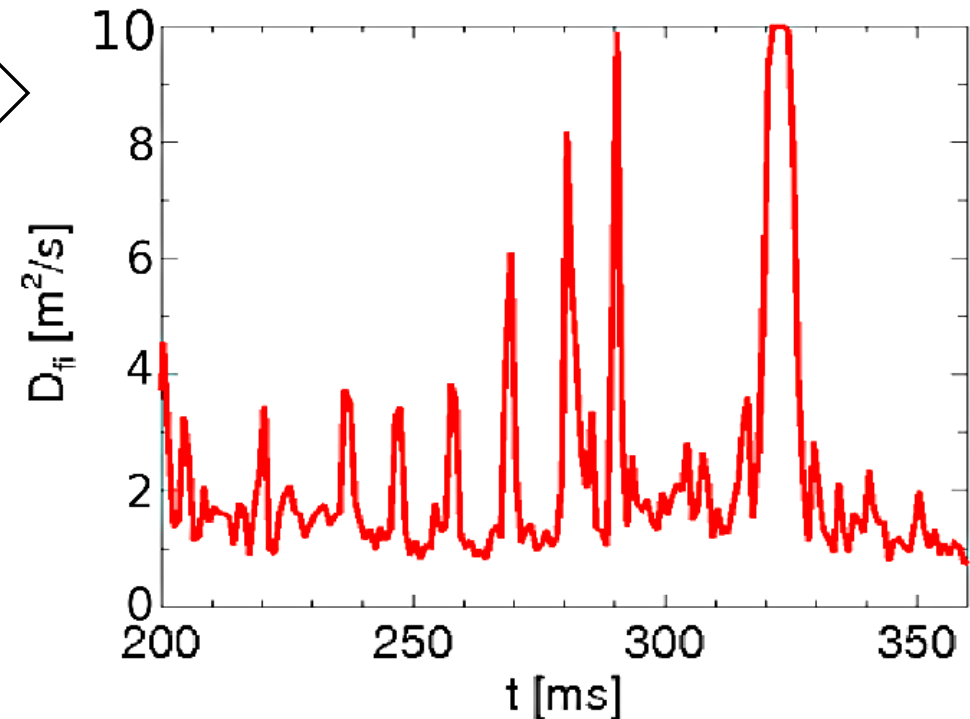
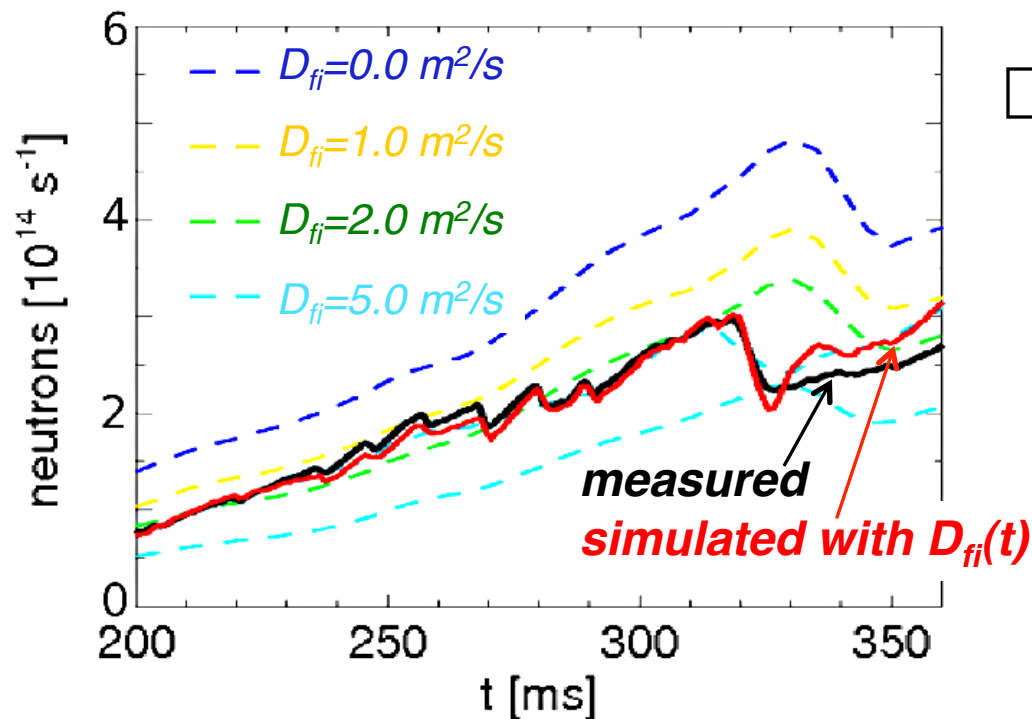
[Fredrickson, NF 2013]

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Transport code TRANSP includes NUBEAM module for classical fast ion physics

- Additionally, *ad-hoc* diffusivity D_{fi} is used to mimic enhanced fast ion transport
 - Assumed uniform in radius, pitch, energy in this work
- Metric to set D_{fi} : match neutron rate, W_{mhd}



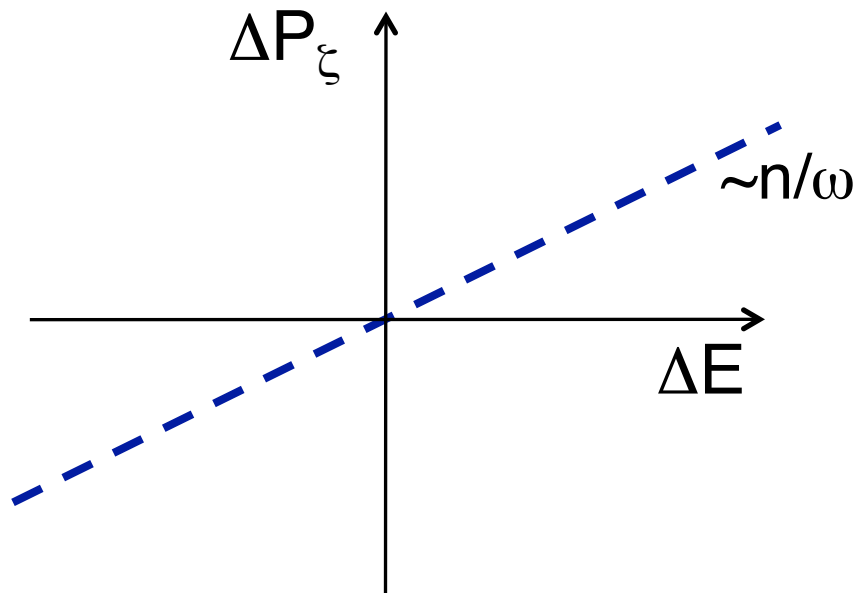
However: instabilities introduce fundamental constraints on particle dynamics

From Hamiltonian formulation - single resonance:

$$\omega P_{\zeta} - nE = \text{const.} \implies \Delta P_{\zeta} / \Delta E = n / \omega$$

$\omega = 2\pi f$, mode frequency

n , toroidal mode number



E , energy

$P_{\zeta} \sim mRv_{\text{par}} - \Psi$, canonical angular momentum

$\mu \sim v_{\text{perp}}^2 / (2B)$, magnetic moment

where Ψ : poloidal flux

R : major radius

m : mass

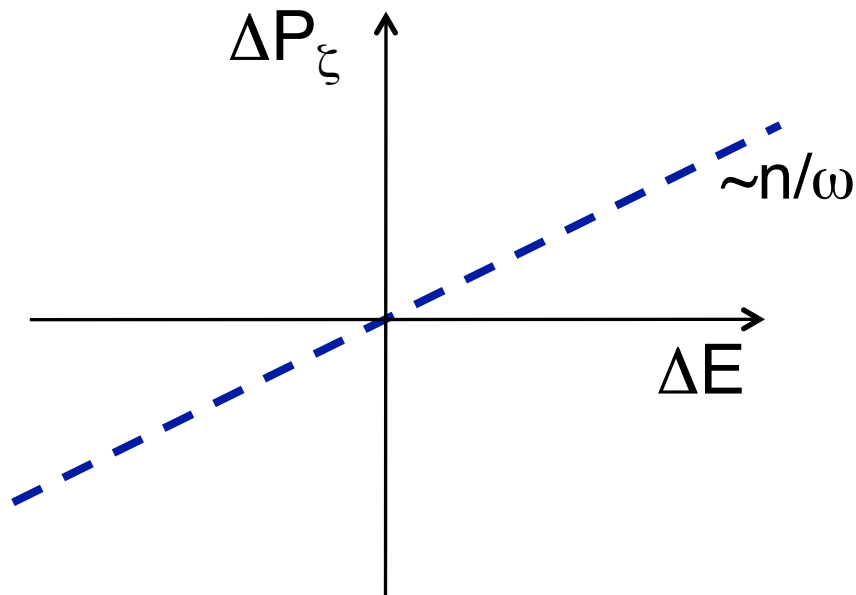
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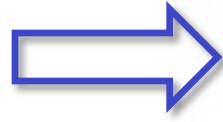
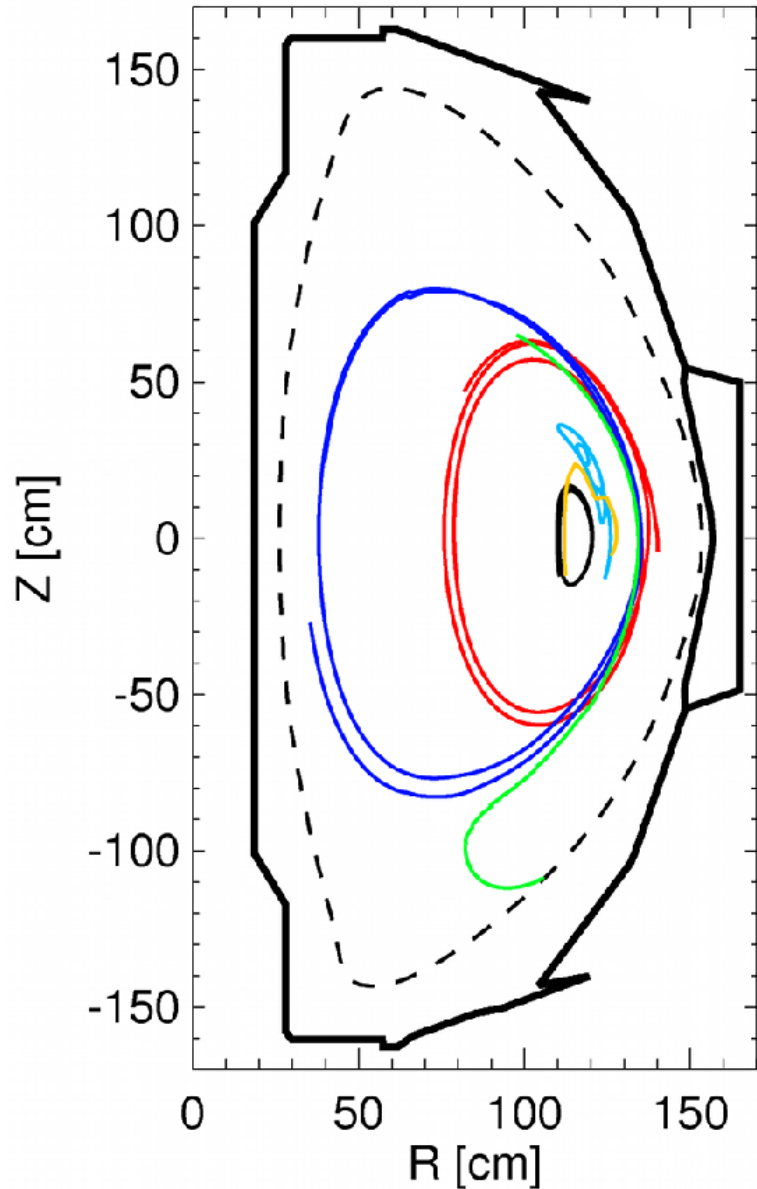
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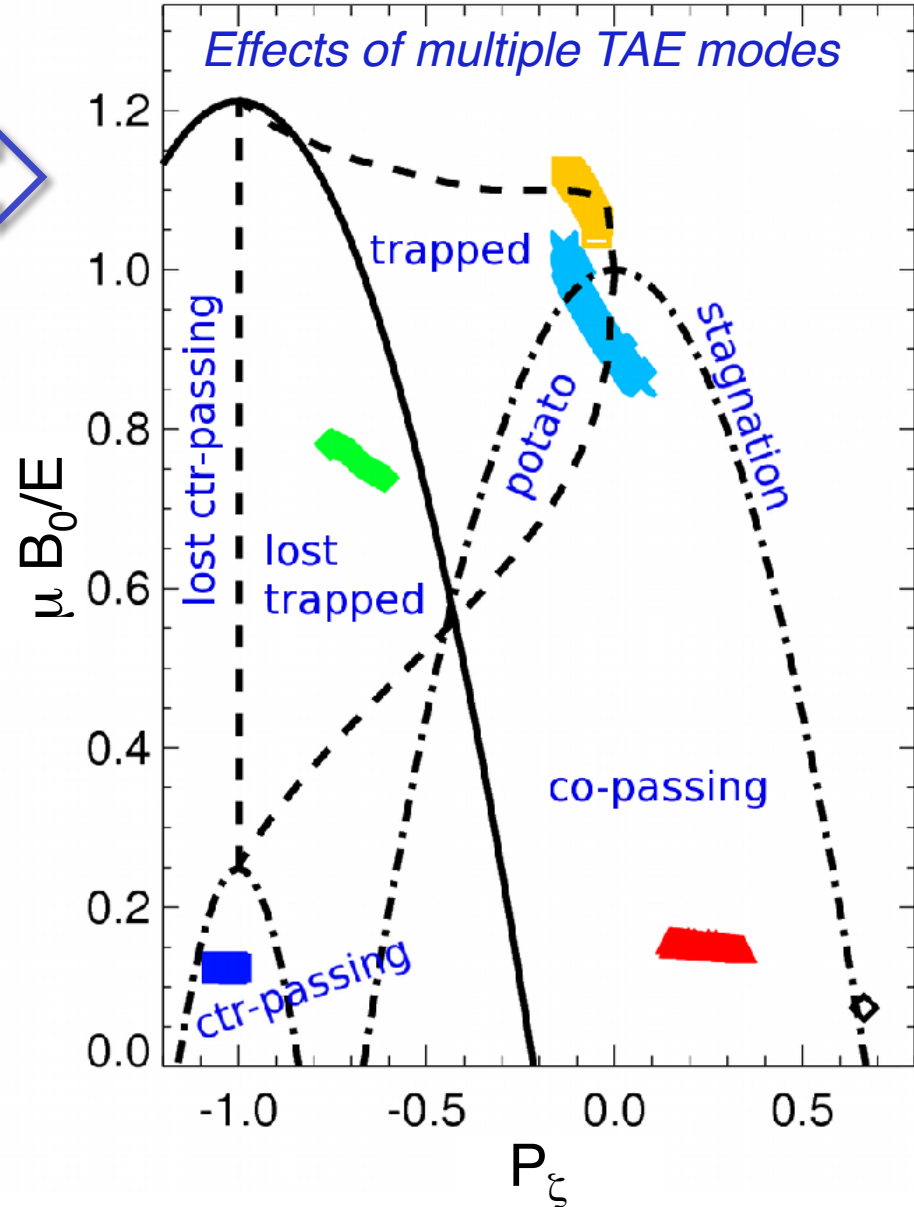
*These effects are not accounted for by ad-hoc D_{fi} .
A new method is needed to include them in integrated modeling.*

Constants of motion (E, P_ξ, μ) are the natural variables to describe wave-particle interaction

NSTX poloidal section



Phase space, $E_0=80.0\text{keV}$



R. B. White, *Theory of toroidally confined plasmas*,
Imperial College Press (2014)

Particle-following codes are used to extract distribution of 'kicks' ΔE , ΔP_ξ for each *bin* (E, P_ξ, μ)

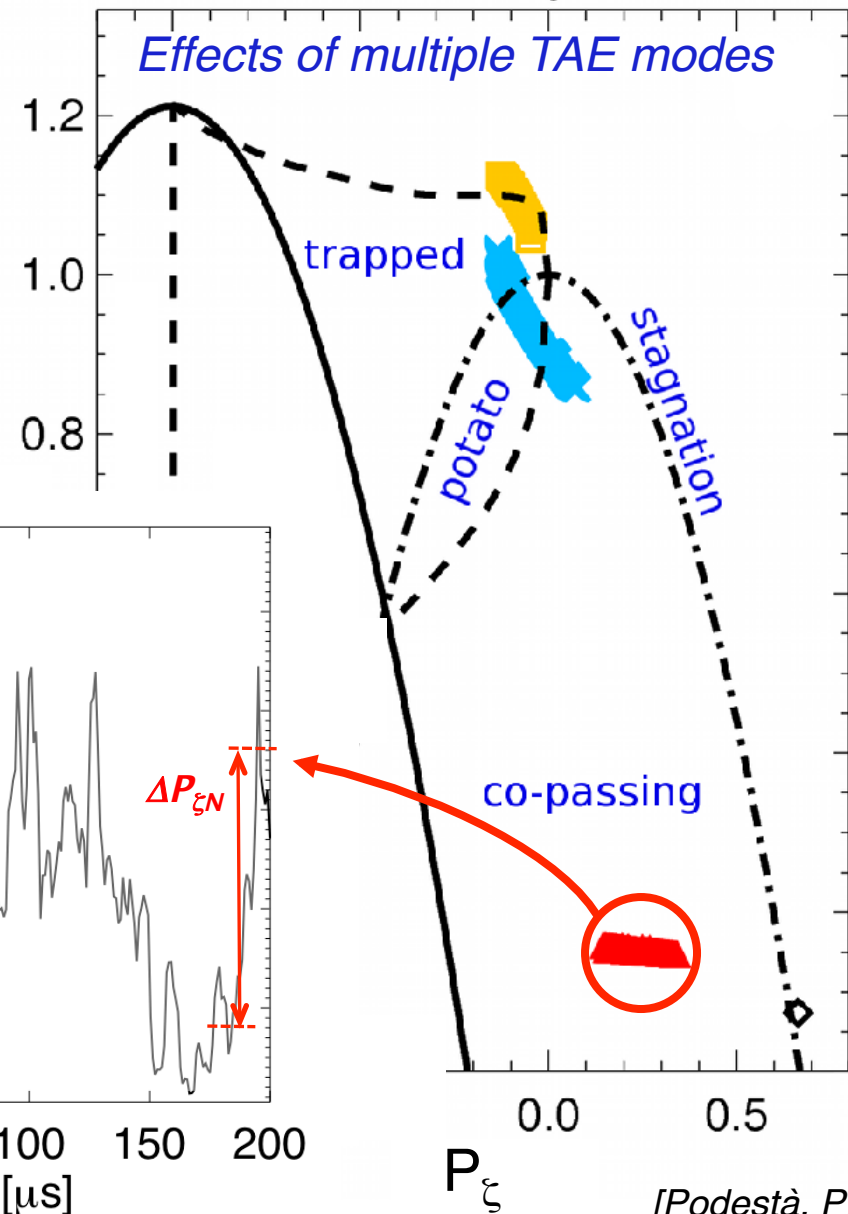
- ORBIT code: record E, P_ξ, μ vs. time for each particle
- Compute average kicks over multiple wave periods:

$$\underbrace{1/f_{\text{wave}}}_{\text{neglected}} < \underbrace{\tau_{\text{resonance}}}_{\text{relevant time scale}} < \underbrace{\tau_{\text{collisions}}}_{\text{classical}}$$

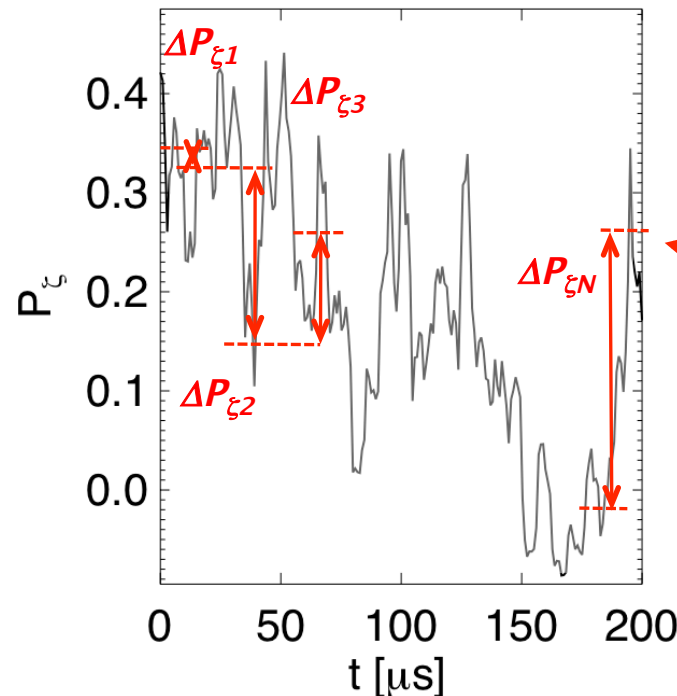
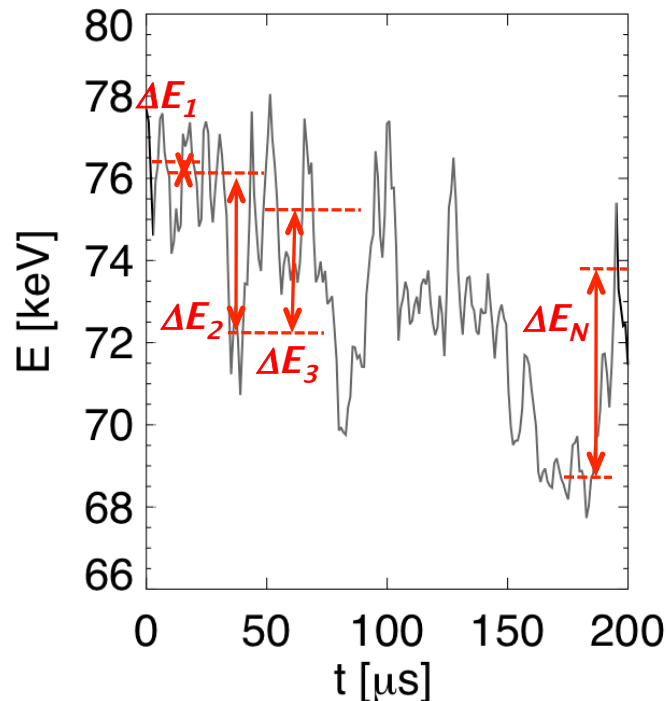
- Re-bin for each (E, P_ξ, μ) region

Phase space, $E_0=80.0\text{keV}$

Effects of multiple TAE modes



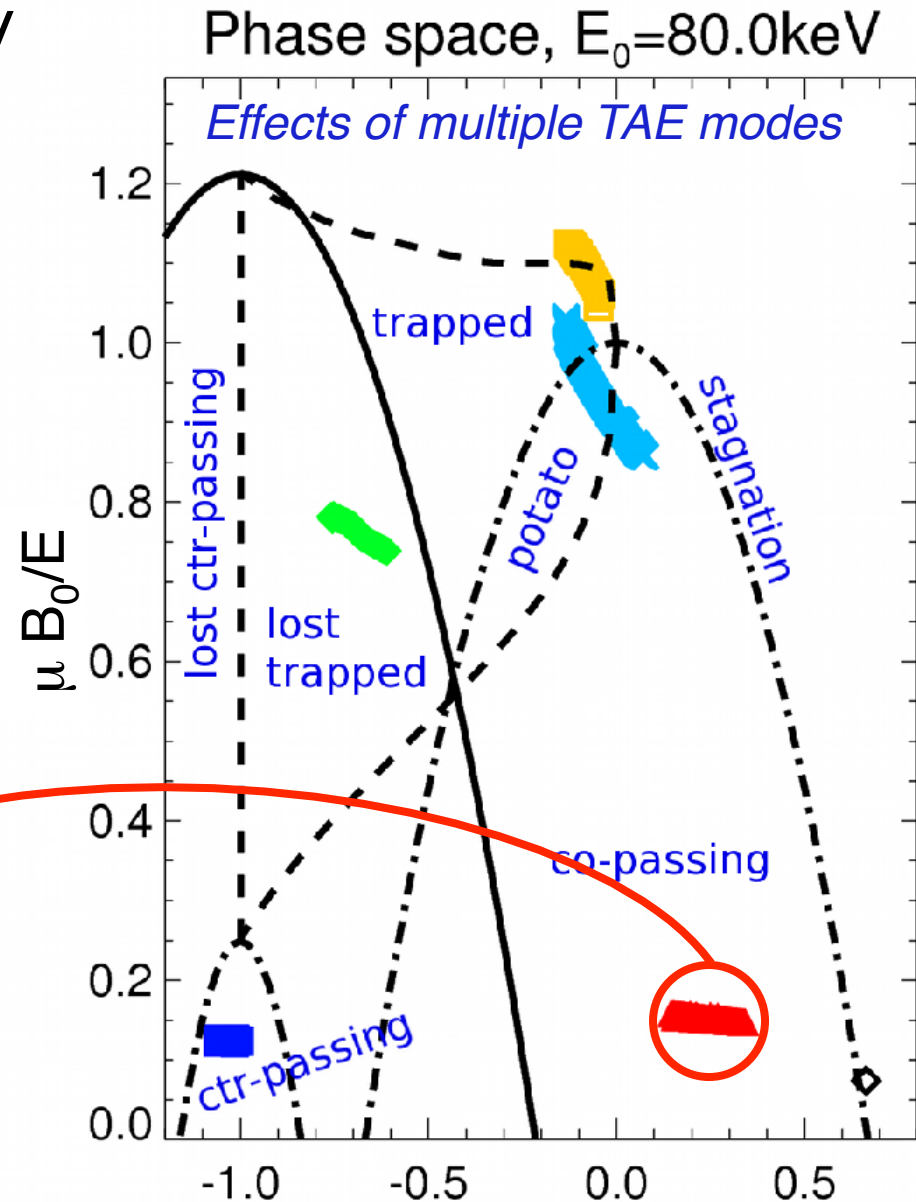
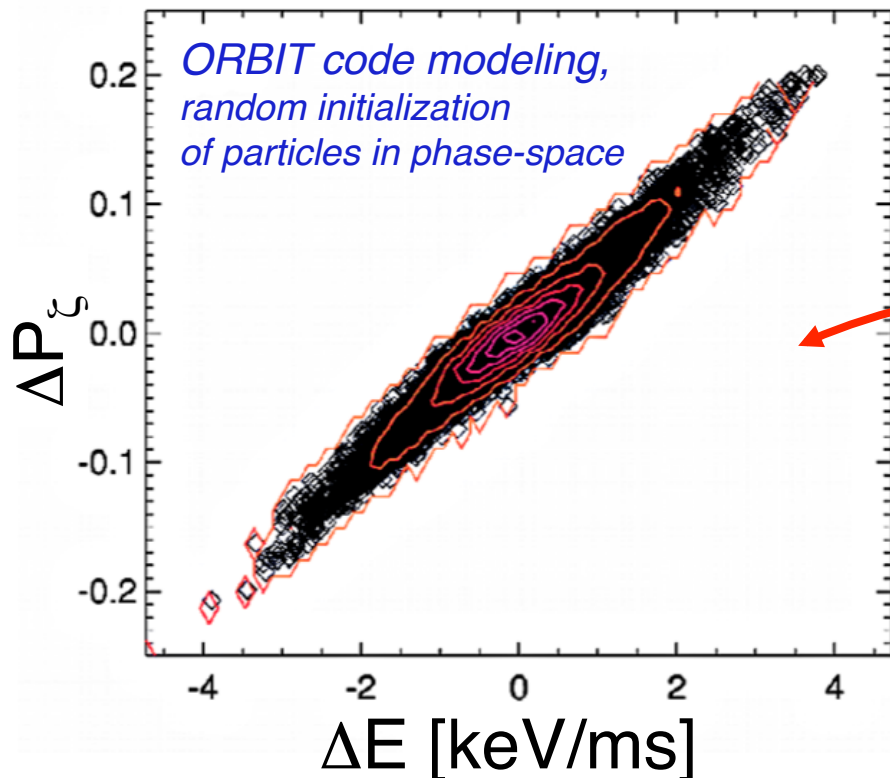
[Podestà, PPCF 2014]



New 'kick model' uses a *probability distribution function* for particle transport in (E, P_ζ, μ) space

Kicks $\Delta E, \Delta P_\zeta$ are described by $p(\Delta E, \Delta P_\zeta | P_\zeta, E, \mu, A)$ which includes the effects of multiple modes, resonances.

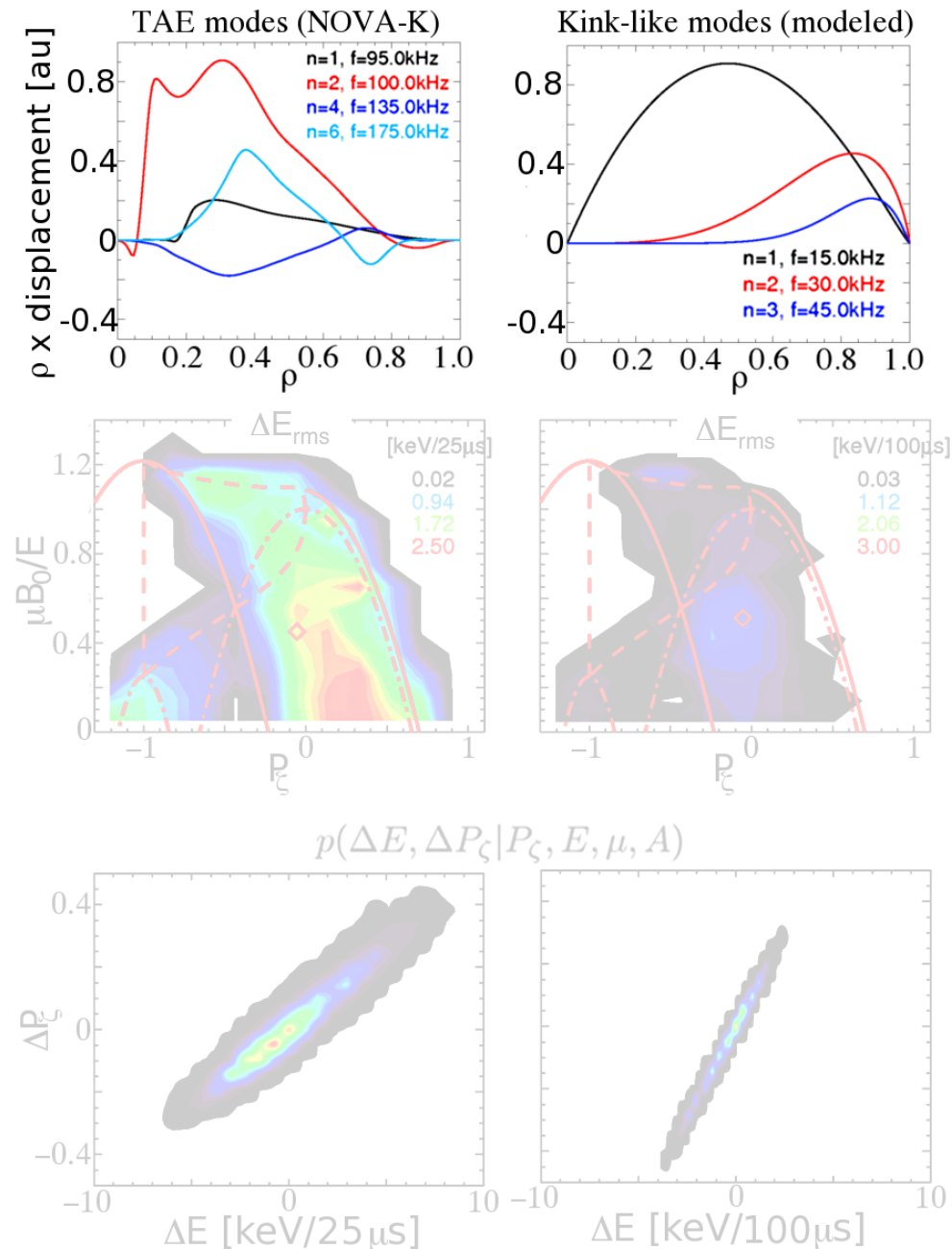
→ *correlated random walk in E, P_ζ*



[Podestà, PPCF 2014]

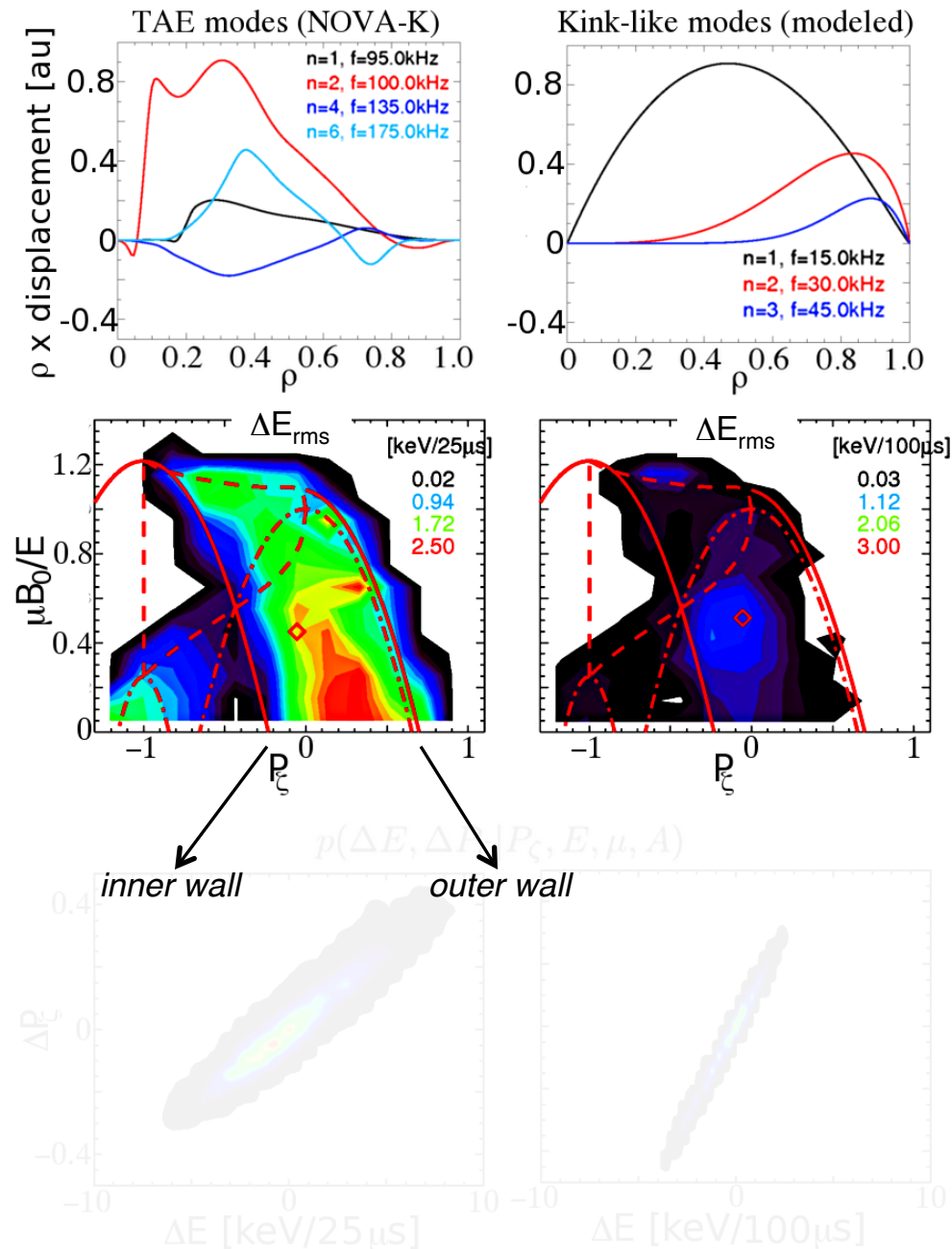
$p(\Delta E, \Delta P_\zeta | P_\zeta, E, \mu)$ and a time-dependent 'mode amplitude scaling factor' enable multi-mode simulations

- Example: toroidal AEs (TAEs) and low-frequency kink
- $p(\Delta E, \Delta P_\zeta | P_\zeta, E, \mu)$ from particle-following code ORBIT
- Each type of mode has separate $p(\Delta E, \Delta P_\zeta)$, $A_{\text{mode}}(t)$
- TAEs and kinks act on different portions of phase space
- Amplitude vs. time can differ, too
- Effects on EPs differ
 - > TAEs: large ΔE , ΔP_ζ
 - > kinks: small ΔE , large ΔP_ζ



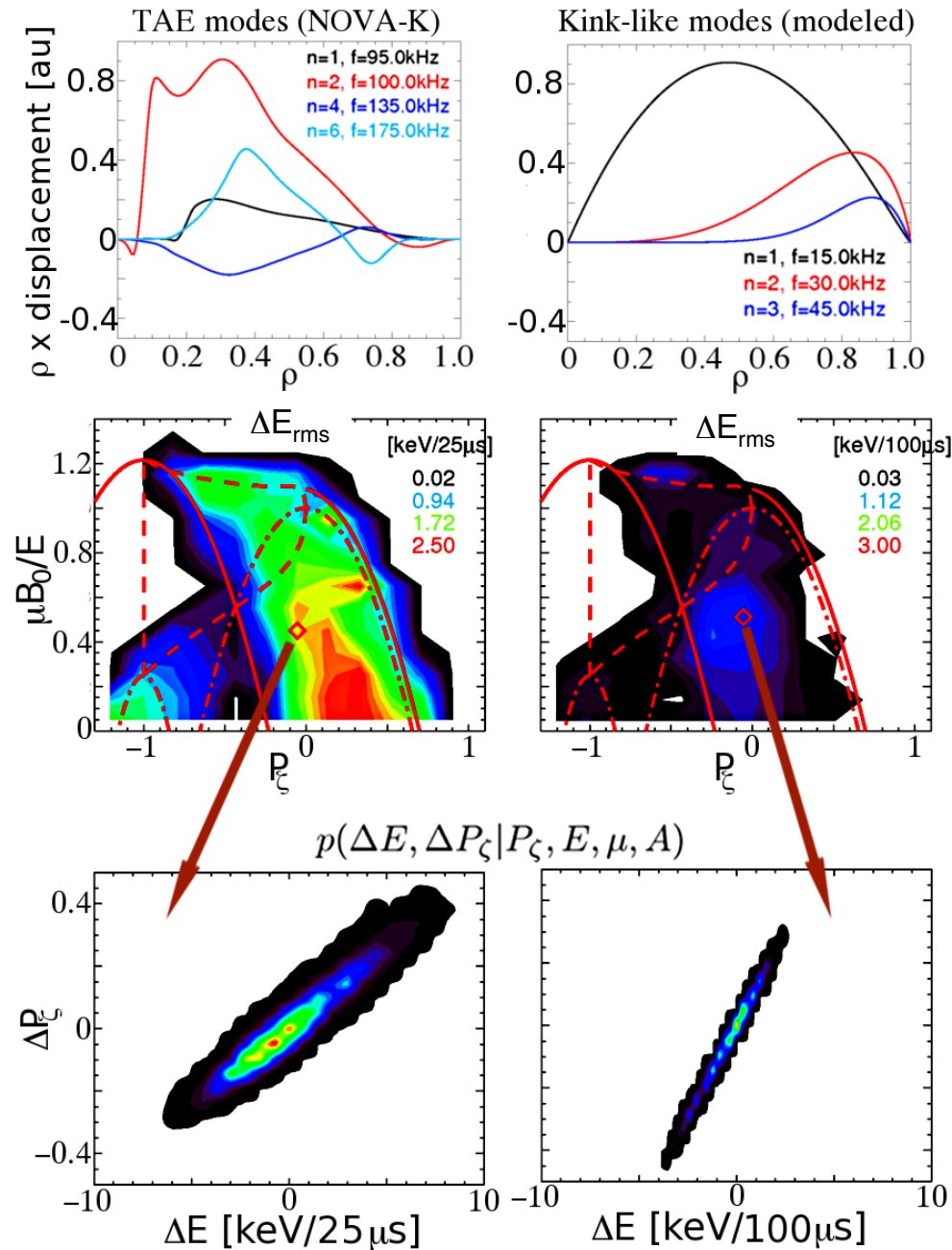
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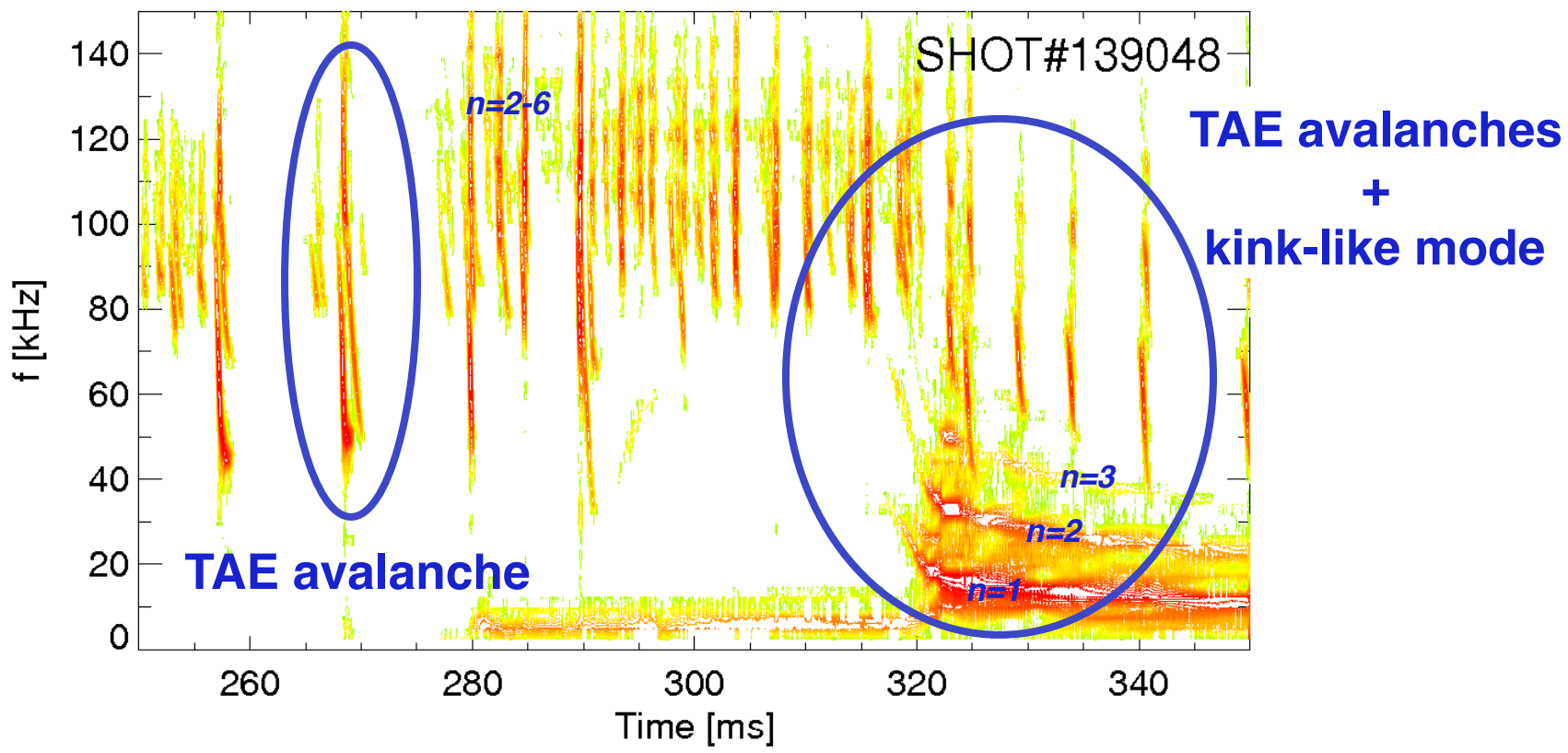
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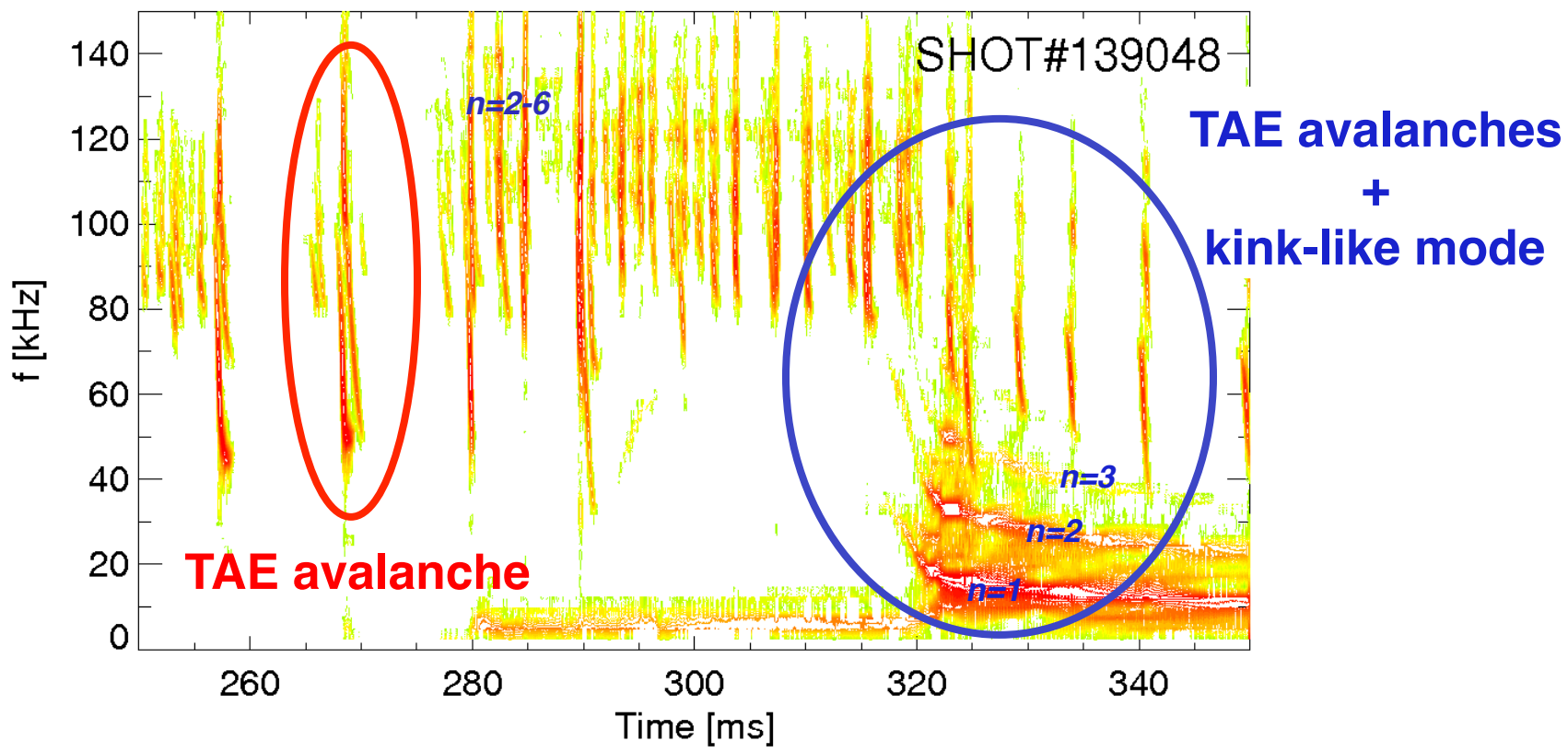
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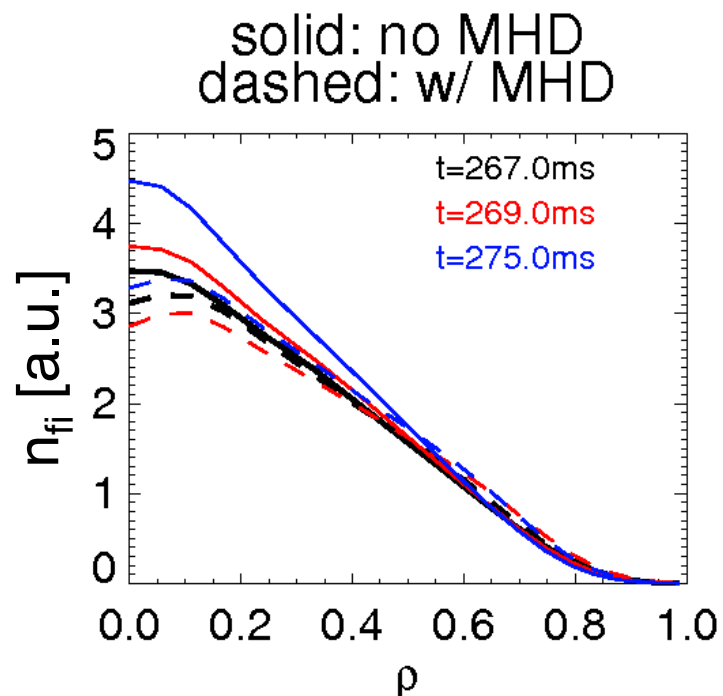
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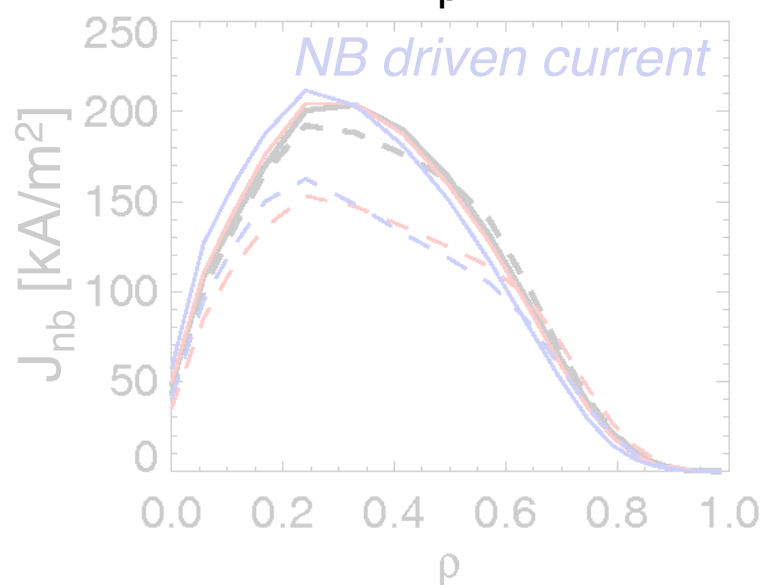


TAE avalanches cause an abrupt drop in fast ions and up to ~40% reduction in local NB-driven current density



- Results from ‘kick model’
- Fast ions redistributed outward, lose energy
 - Consistent with constraints from resonant interaction:

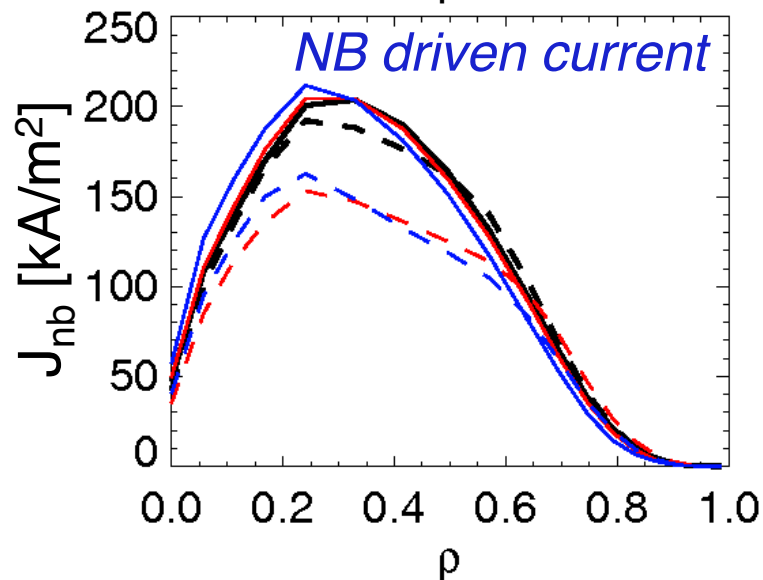
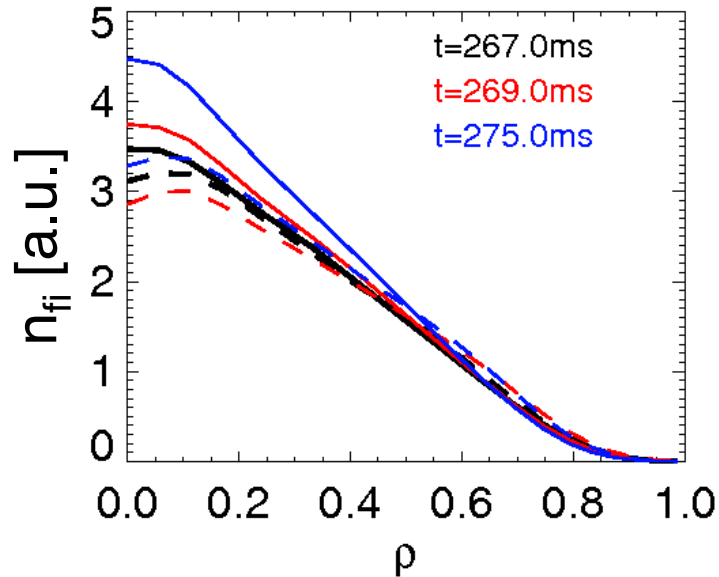
$$\Delta P_{\zeta} / \Delta E = n / \omega$$



- NB-driven current J_{nb} is also redistributed out
- $J_{nb}(r)$ modification largely unpredicted by *ad-hoc* D_{fi} in this case

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solid: no MHD
dashed: w/ MHD

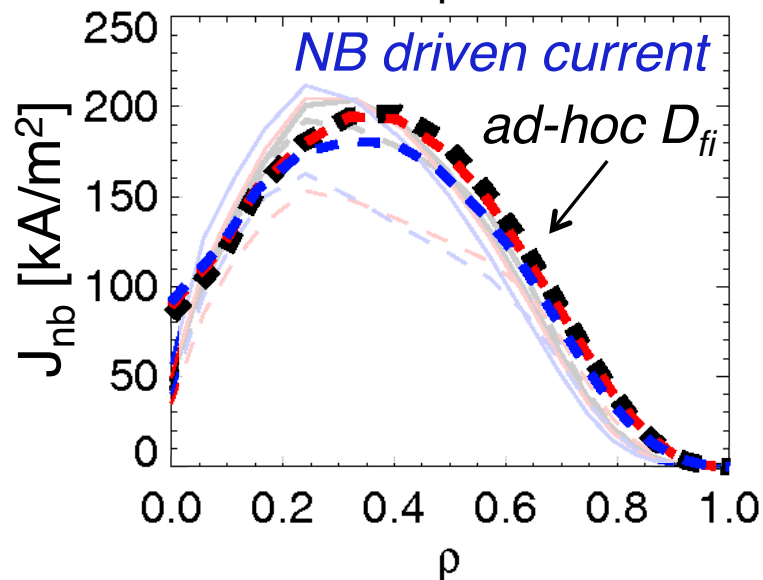
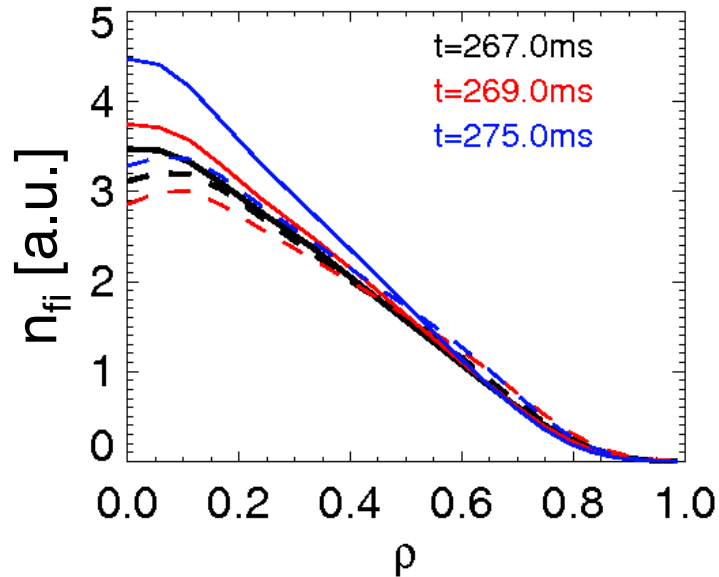


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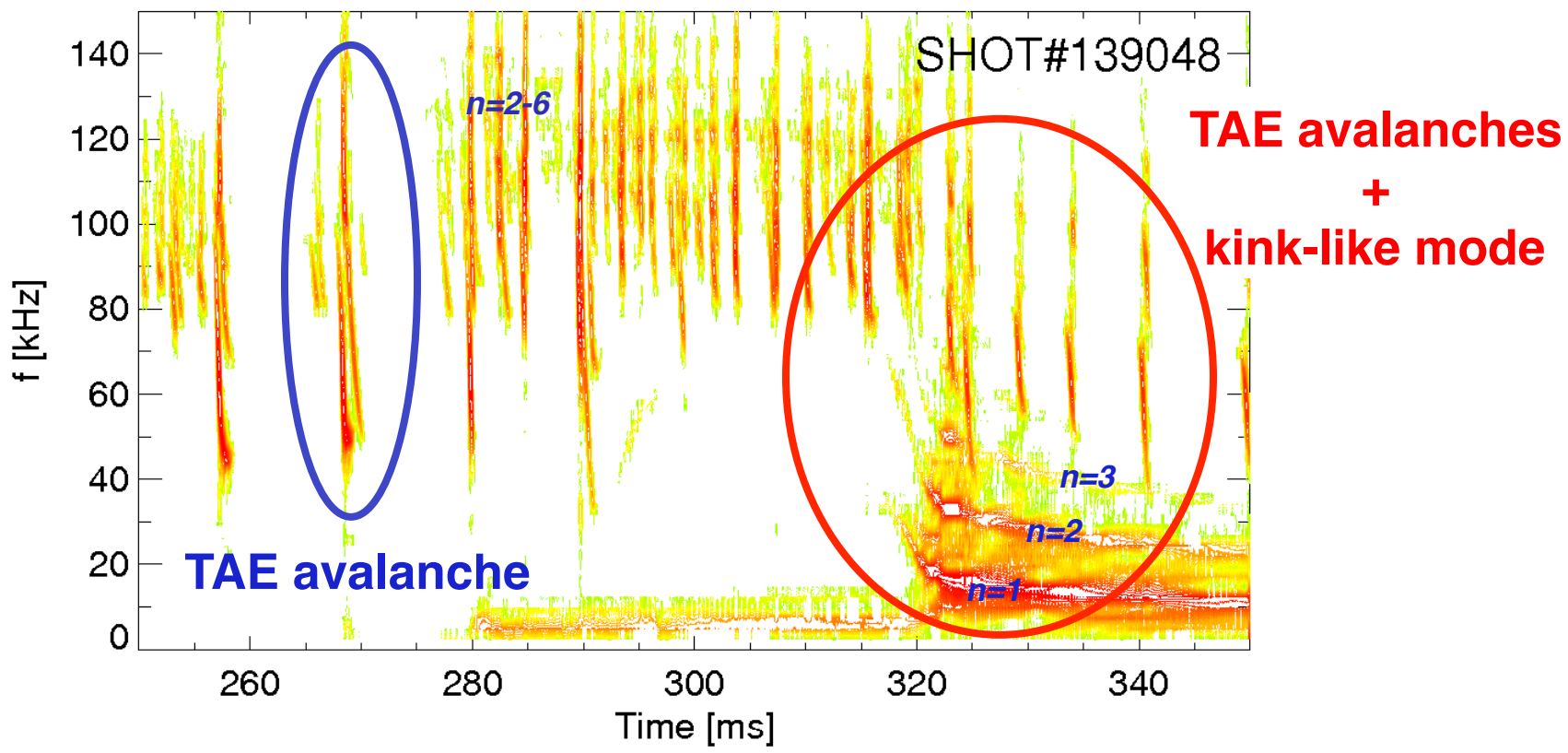
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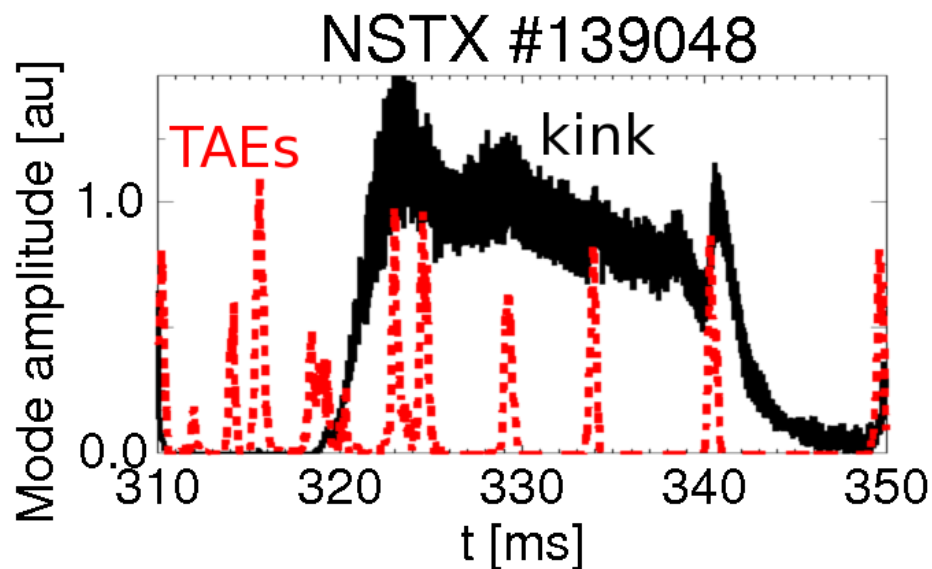
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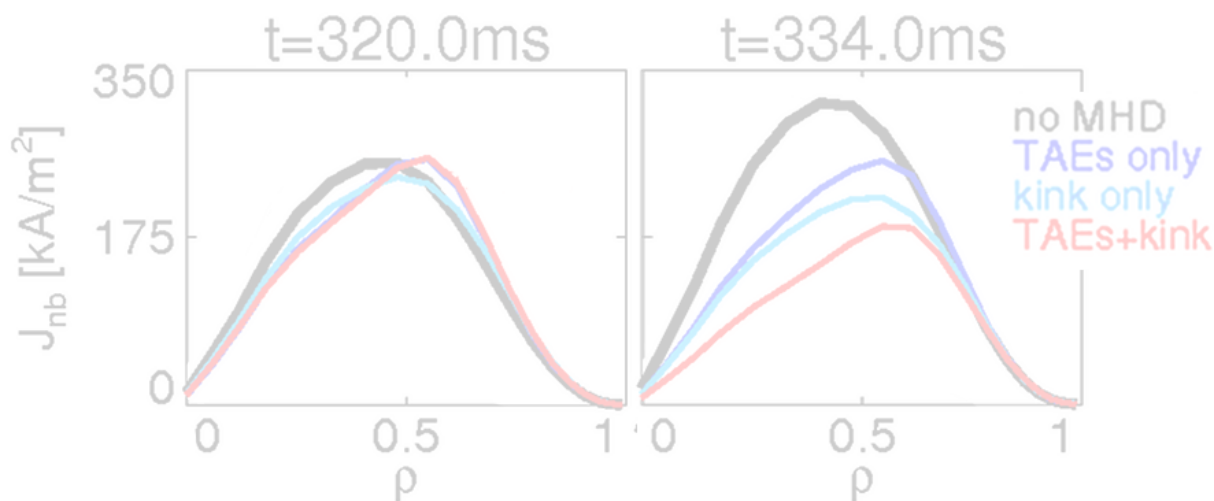
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Synergy between different classes of instabilities modifies MHD effects on $J_{nb}(r)$ – not captured by *ad-hoc* D_{fi}

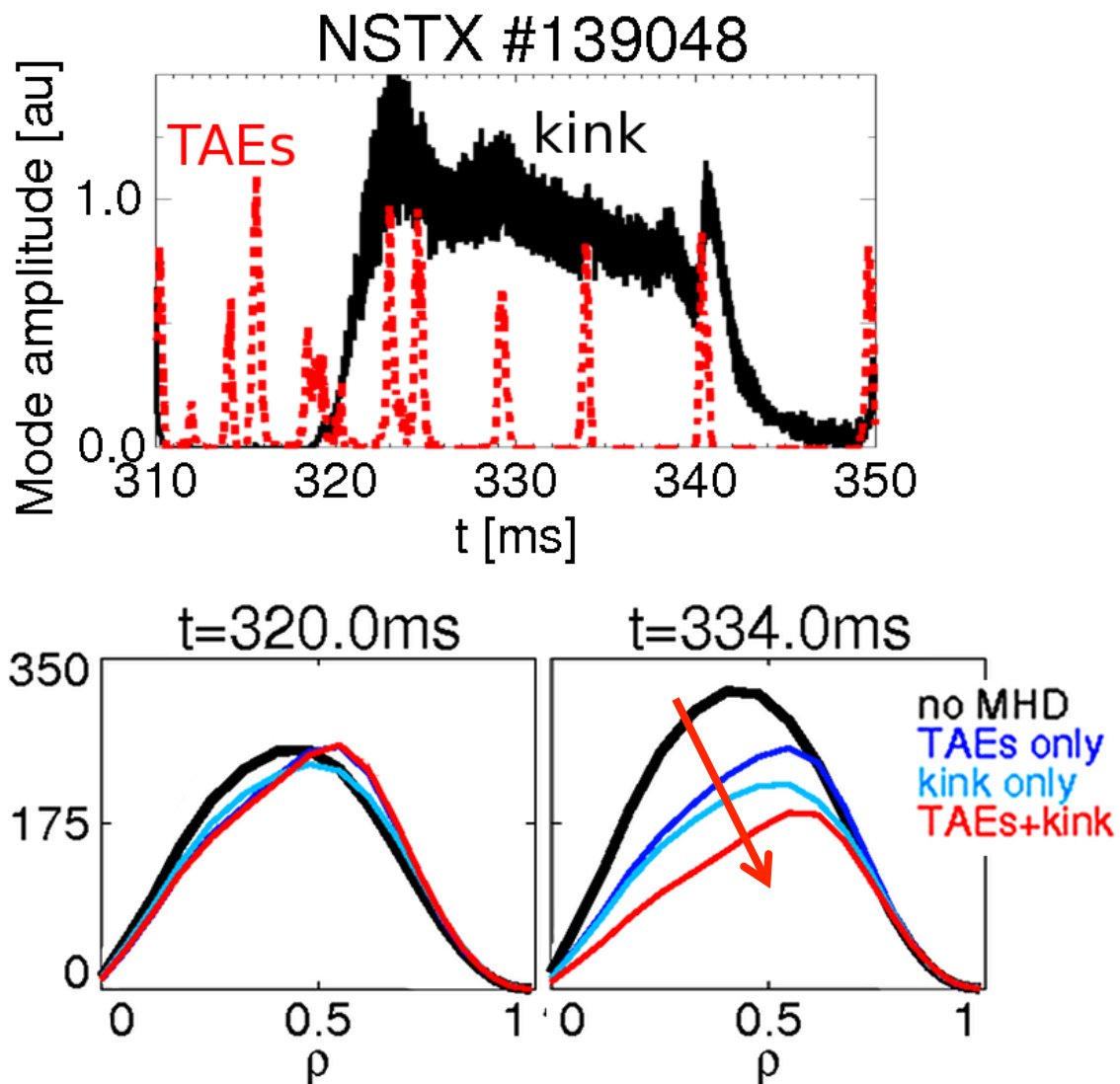


- Kinks have broad radial structure, connect core to boundary



> Synergy arises from mode overlap in phase space

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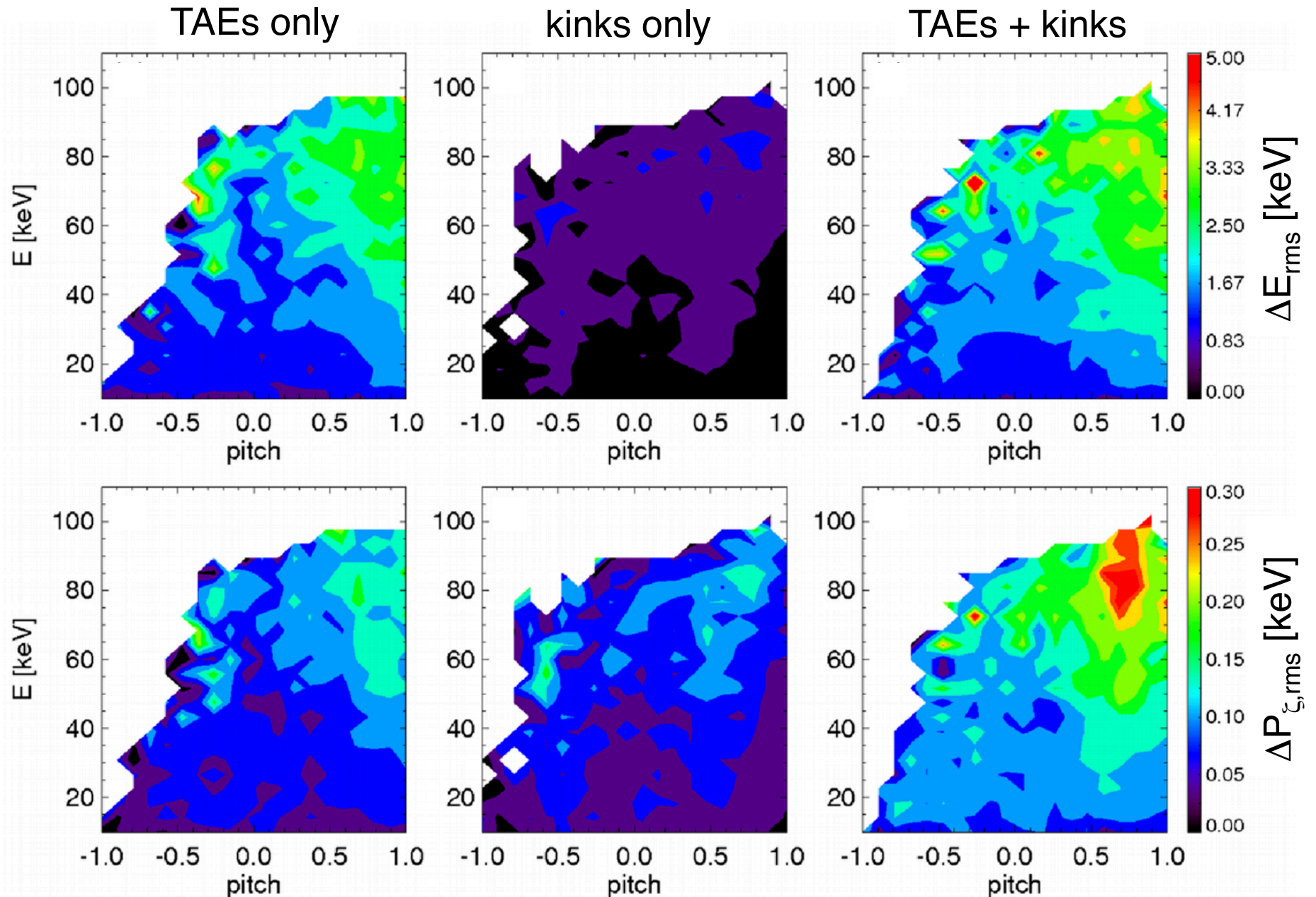


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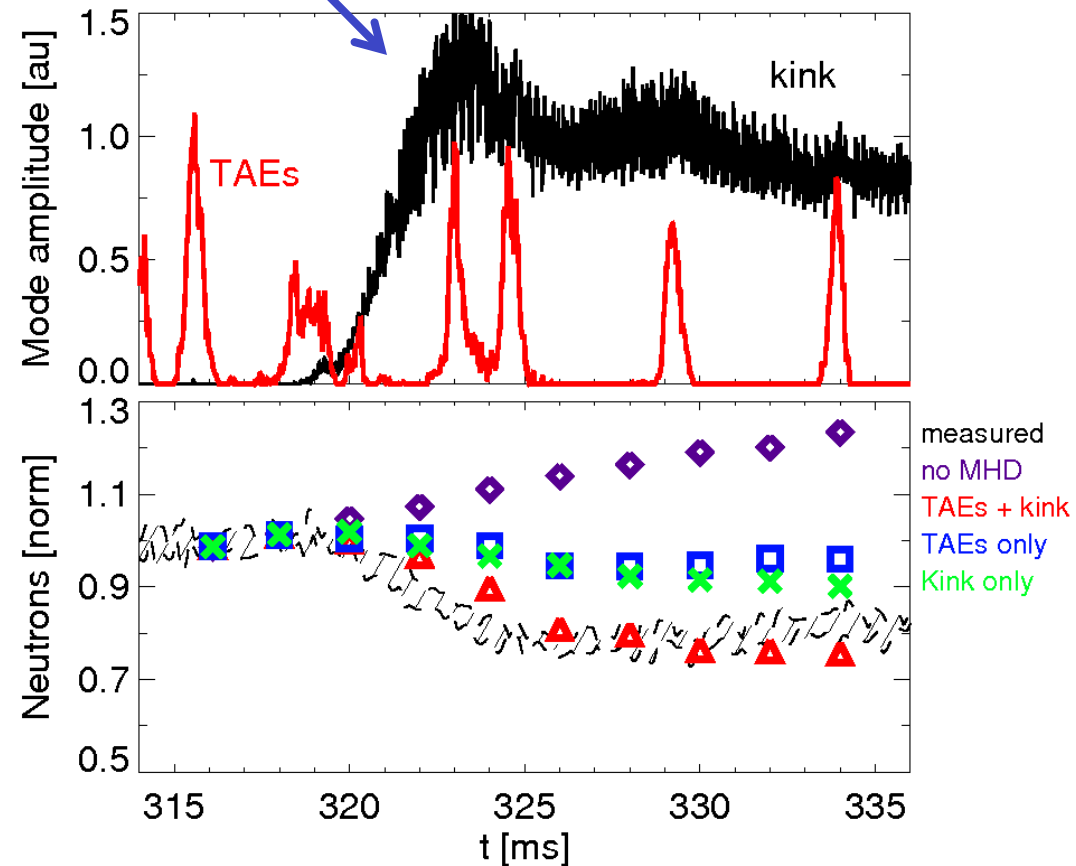
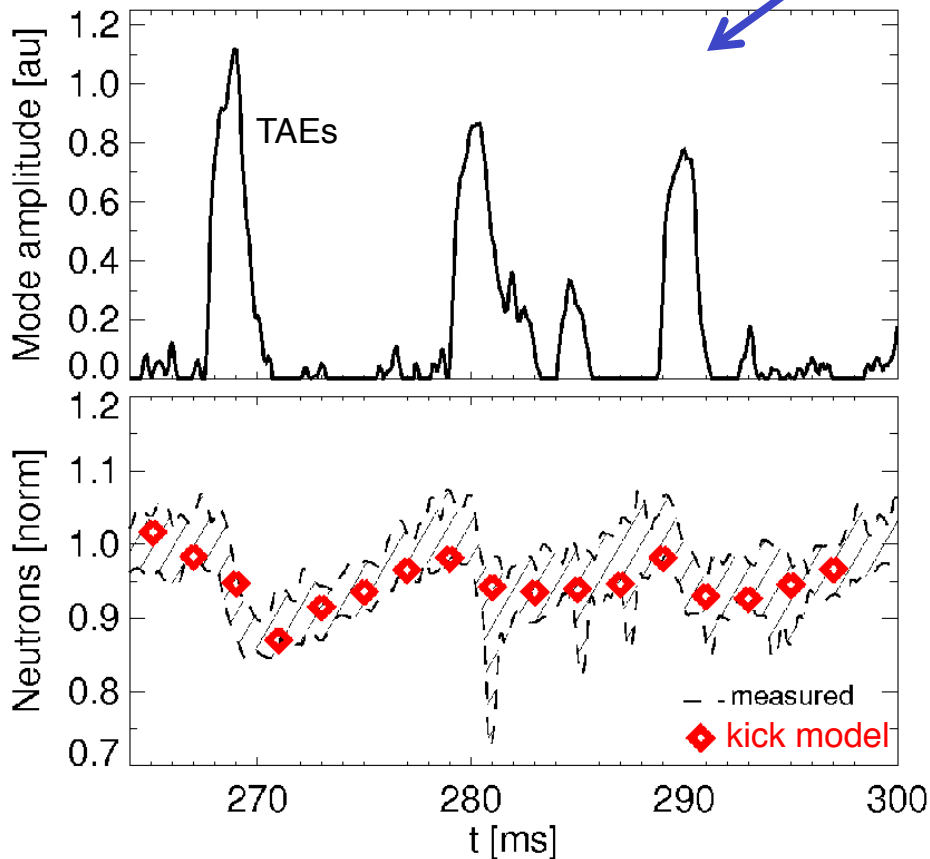
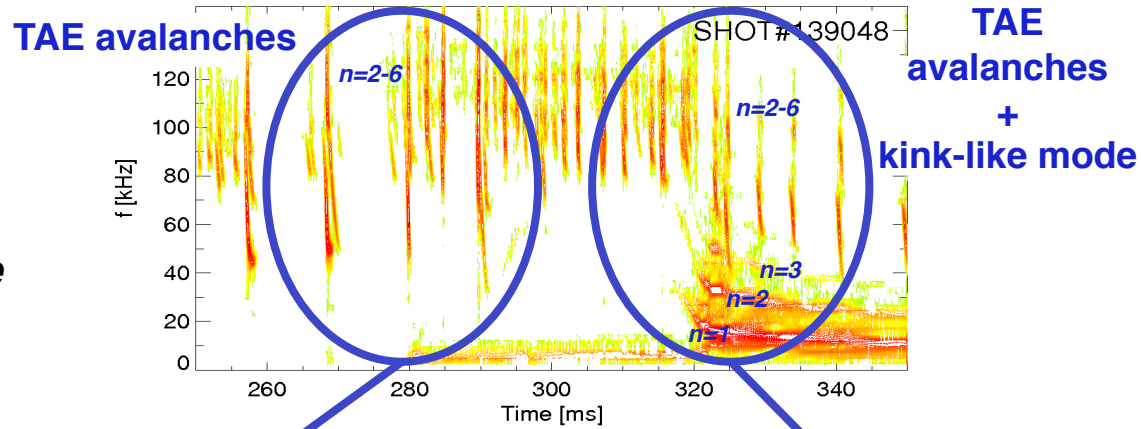
Phase-space is *selectively* modified by instabilities:

TAEs $\rightarrow \Delta P_{\zeta} / \Delta E = n / \omega$, kinks \rightarrow mostly ΔP_{ζ}



Simulated neutron rate agrees with experiments for both TAE avalanches & multi-mode cases

Use 'kick model' coupled to stand-alone NUBEAM



Summary

- NB-driven current profile can be strongly affected by MHD instabilities
 - Not all effects properly captured by classical EP physics
- A new model is implemented in TRANSP for EP simulations including phase-space details
 - Validation within TRANSP framework is in progress
- New tools will improve scenario development on NSTX Upgrade & future devices
 - NB current drive optimization
 - NB-driven current profile control for high- q_{\min} steady state operations