



U.S. DEPARTMENT OF  
**ENERGY**

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Science



# Kinetic Resistive Wall Mode Stabilization Physics in Tokamaks

Jack Berkery  
Columbia University

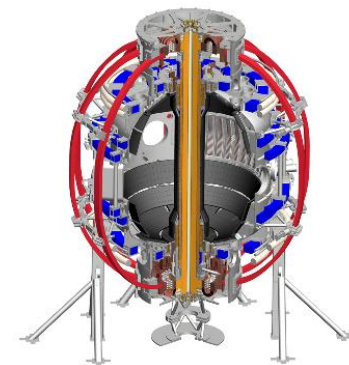
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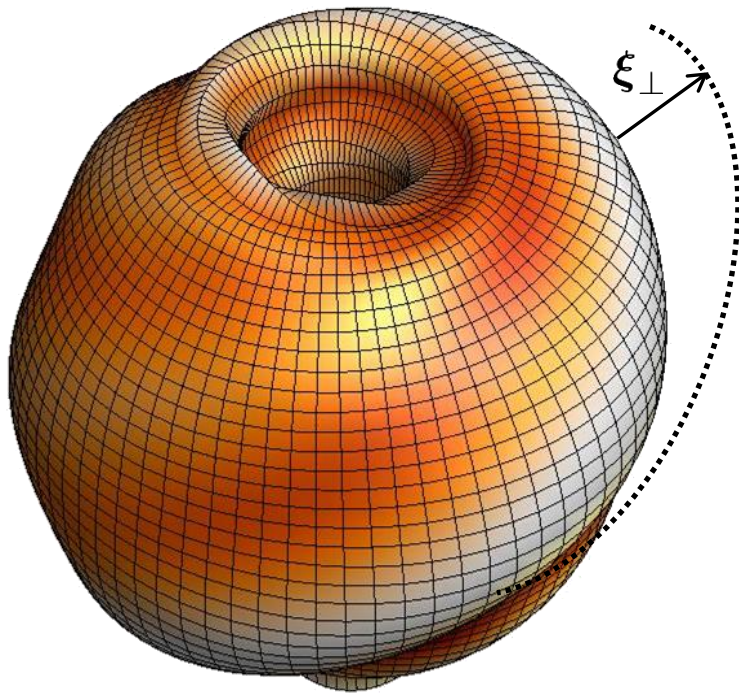


# Outline

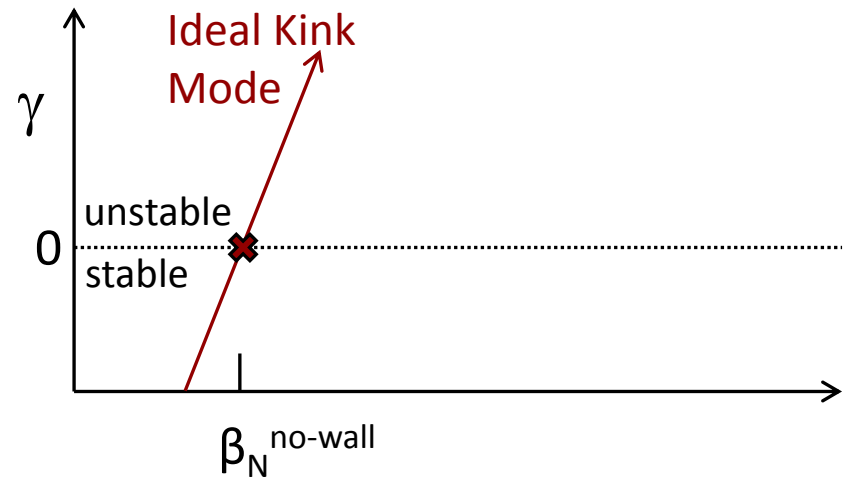
- **RWM Definition and Motivation**
- **Kinetic Stability Theory**
  - **Rotation**
  - **Collisionality**
  - **Energetic Particles**
- **Comparison of Calculations and Experimental Results**
- **Stability Estimation and Rotation Profile Control**
- **Summary**

# An unstable RWM is an exponential growth of magnetic field line kinking that can cause disruptions

- The resistive wall mode (RWM) is a kinking of magnetic field lines slowed by penetration through vessel structures



$$\xi_{\perp} \sim e^{\gamma t}$$

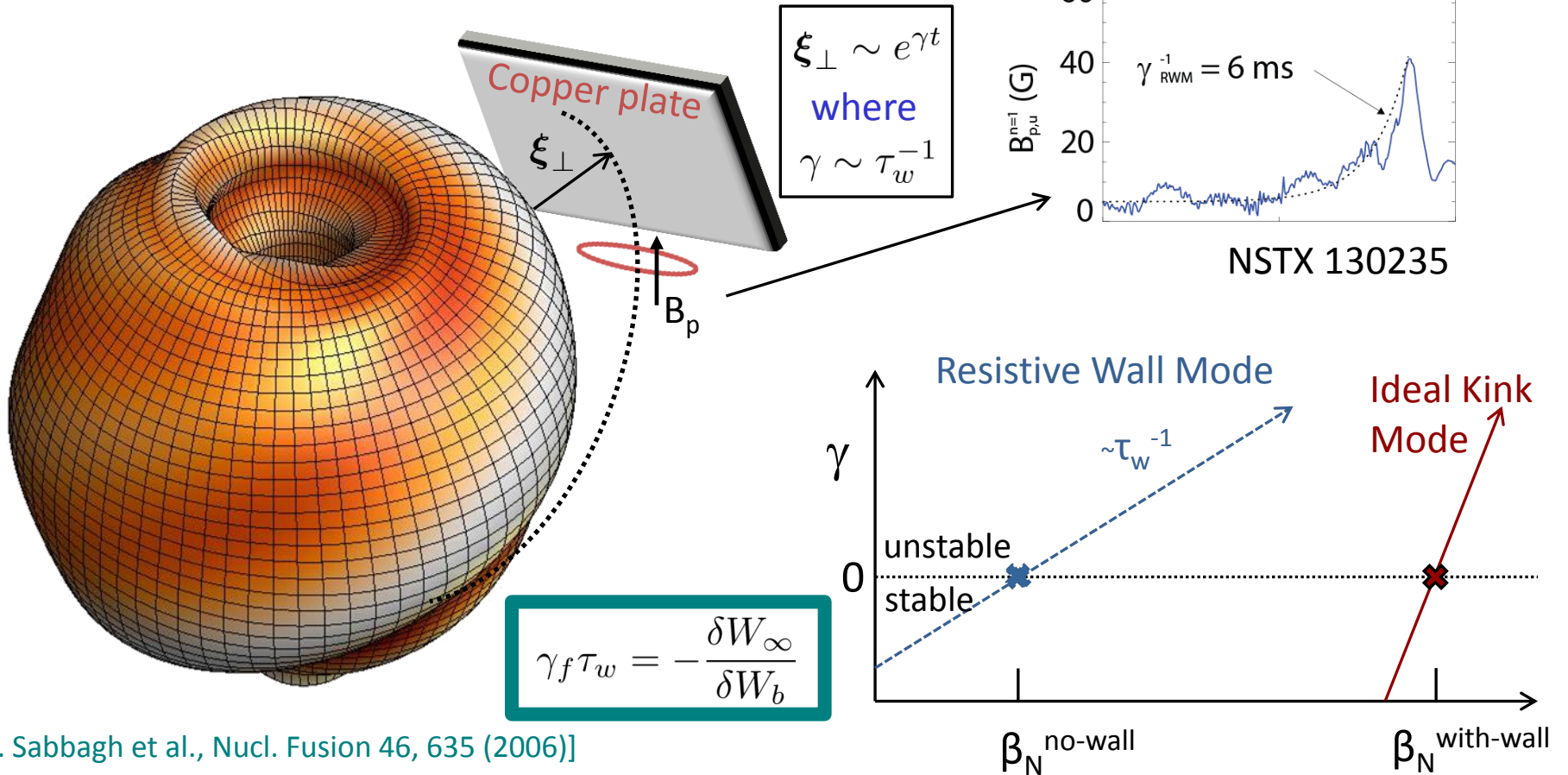


[S. Sabbagh et al., Nucl. Fusion 46, 635 (2006)]

RWMs can cause a collapse in  $\beta$ , disruption, and termination of the plasma

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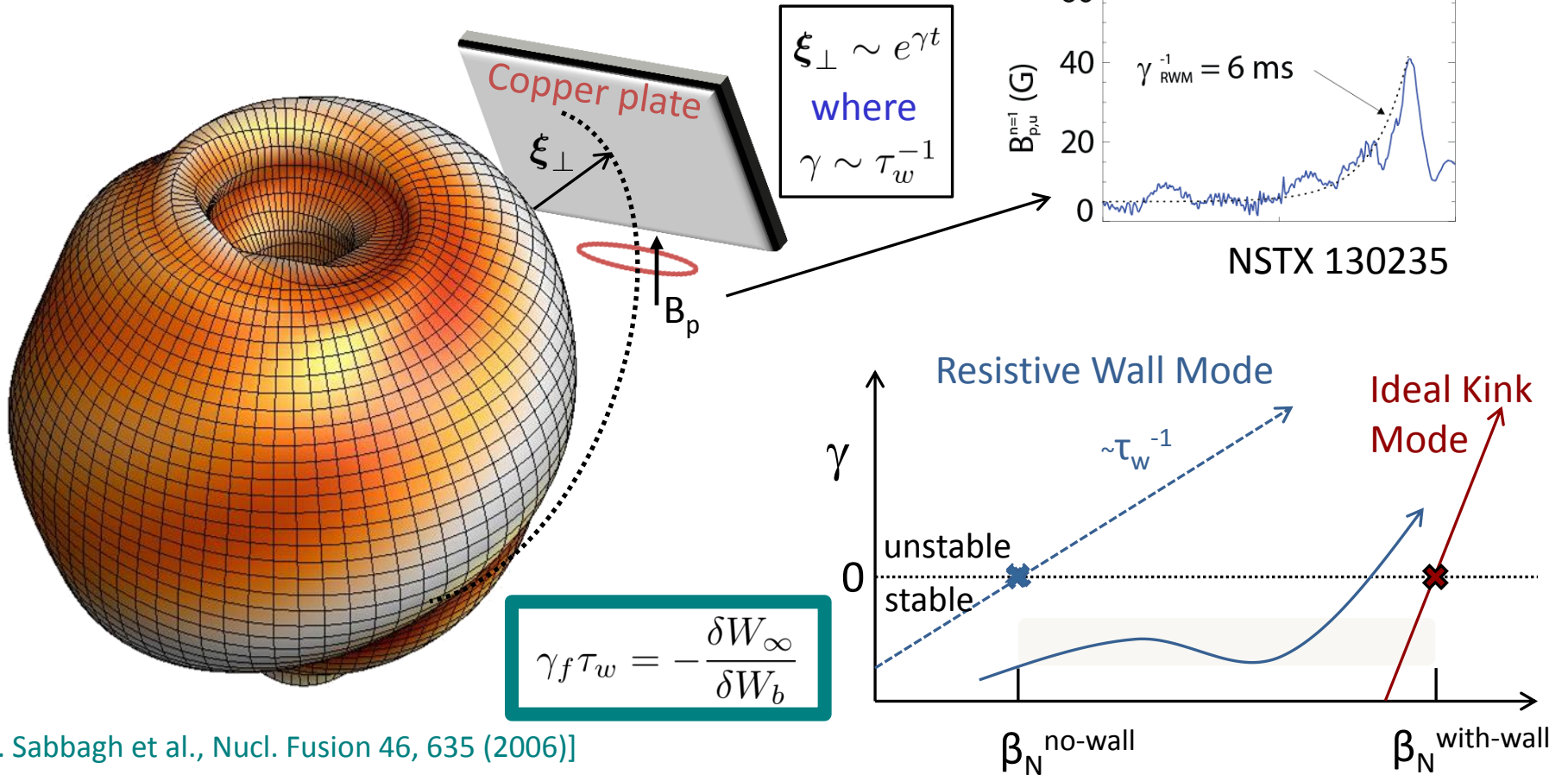


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RWMs can cause a collapse in  $\beta$ , disruption, and termination of the plasma

# A scalar critical plasma rotation model can not explain RWM stability; it depends on the $\omega_\phi$ profile

- Early stability theories:

- Collisional dissipation of mode energy
- Rotational damping

But models with scalar “critical rotation” for stability could not explain experiments

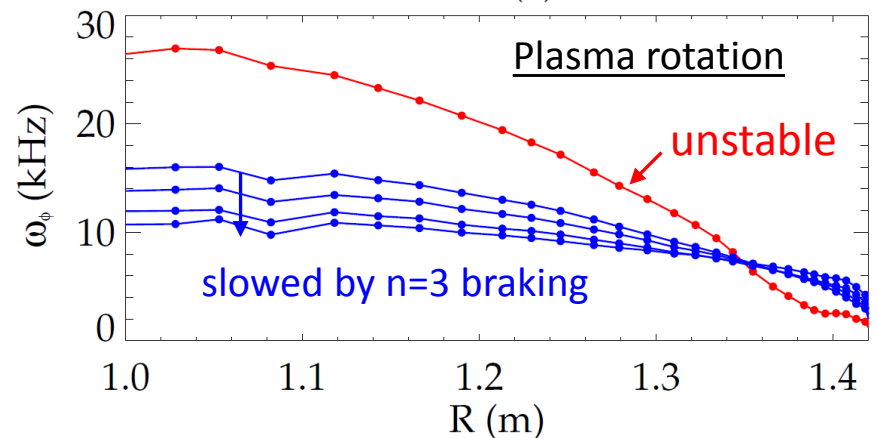
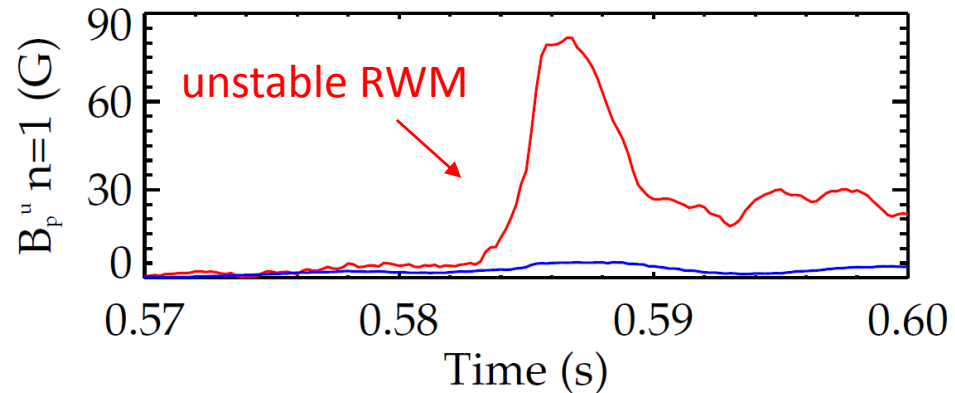
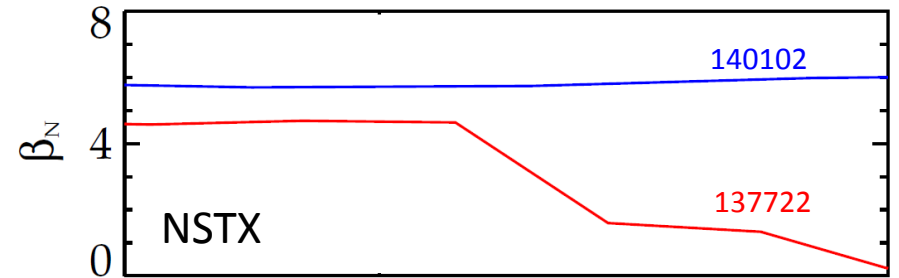
- Unexplained experiments
- New theory: consider kinetic effects

Ideal Stability

Kinetic Effects

$$(\gamma - i\omega_r) \tau_w = - \frac{\delta W_\infty + \delta W_K}{\delta W_b + \delta W_K}$$

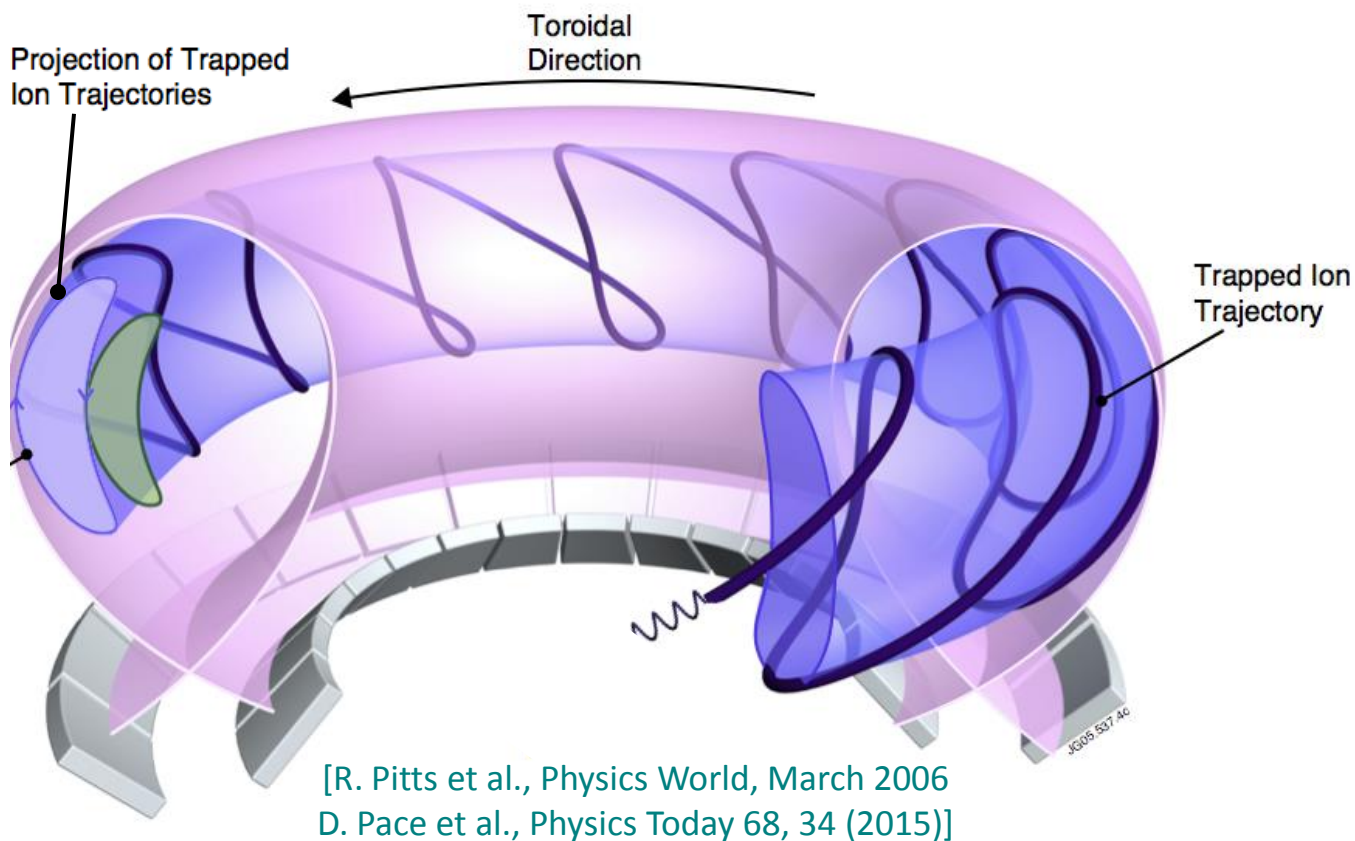
[B. Hu et al., Phys. Rev. Lett. 93, 105002 (2004)]



# Outline

- RWM Definition and Motivation
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“Kinetic effects” means taking into account complicated particle motion rather than treating the plasma as a fluid



### MISK code

- Solves for RWM growth rate
- $\delta W_K$  is solved by using  $\tilde{f}$  from the drift kinetic equation

Precession Drift

$\sim$  Plasma Rotation

**Rotational resonance effect**

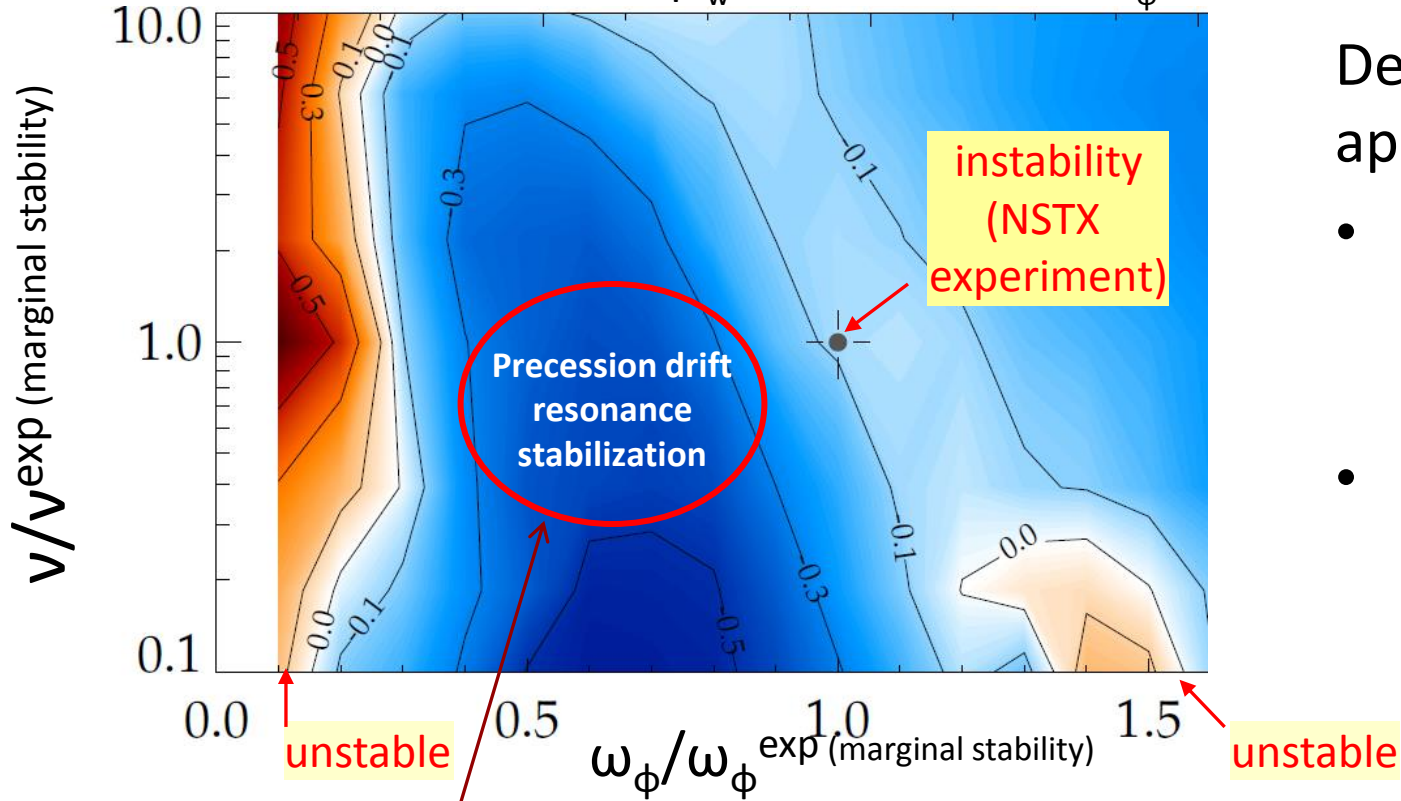
$$\delta W_K \sim \frac{1}{\langle \omega_D \rangle + \omega_E - i\nu}$$

[J. Berkery et al., Phys. Rev. Lett. 104, 035003 (2010)]



# Kinetic theory consistent with RWM destabilization at intermediate plasma rotation

MISK calculations of  $\gamma\tau_w$  contours vs.  $v$  and  $\omega_\phi$



Destabilization appears between:

- precession resonance at low  $\omega_\phi$
- bounce resonance at high  $\omega_\phi$

Precession Drift

$\sim$  Plasma Rotation

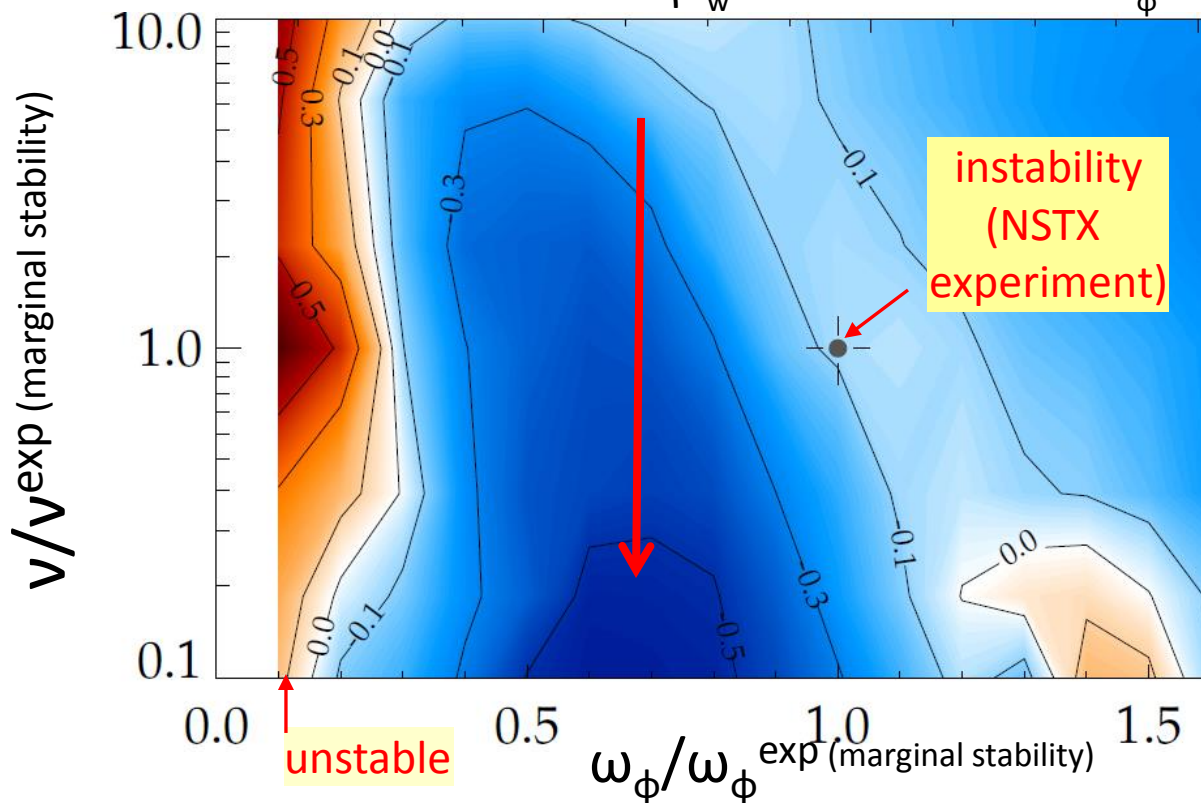
**Rotational resonance effect**

$$\delta W_K \sim \frac{1}{\langle \omega_D \rangle + \omega_E - i\nu}$$

[J. Berkery et al., Phys. Rev. Lett. 104, 035003 (2010)]

# Collisionality affects the strength of kinetic resonances

MISK calculations of  $\gamma\tau_w$  contours vs.  $\nu$  and  $\omega_\phi$



- Early theory predicted RWM stability should decrease at low  $\nu$
- Kinetic RWM stability theory:
  - Stabilizing resonant kinetic effects enhanced at low  $\nu$
- Important for ITER

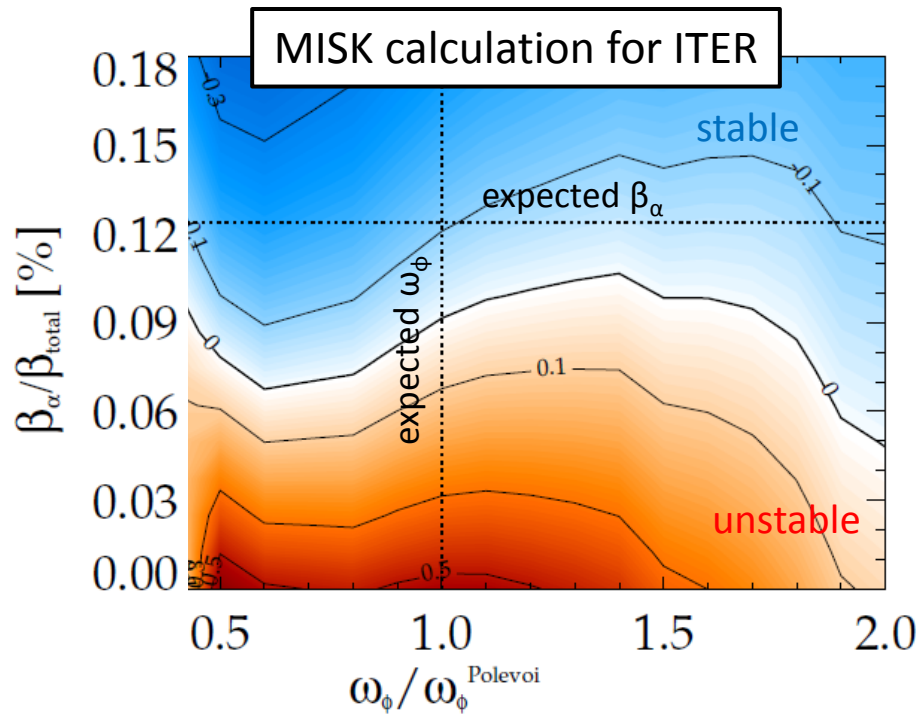
**Collisionality effect**

$$\delta W_K \sim \frac{1}{\langle \omega_D \rangle + \omega_E - i\nu}$$

Collisionality

[J. Berkery et al., Phys. Rev. Lett. 106, 075004 (2011)]

# Energetic particles provide a stabilizing force that is nearly independent of rotation and collisionality



- Energetic particles provide stabilizing effect
- Energetic particles are not in mode resonance
  - Effect is nearly independent of  $\omega_\phi$
  - Effect is not energy dissipation, but rather a restoring force

Large for EPs

Small for EPs

Precession Drift

~ Plasma Rotation Collisionality

**Energetic particle effect**

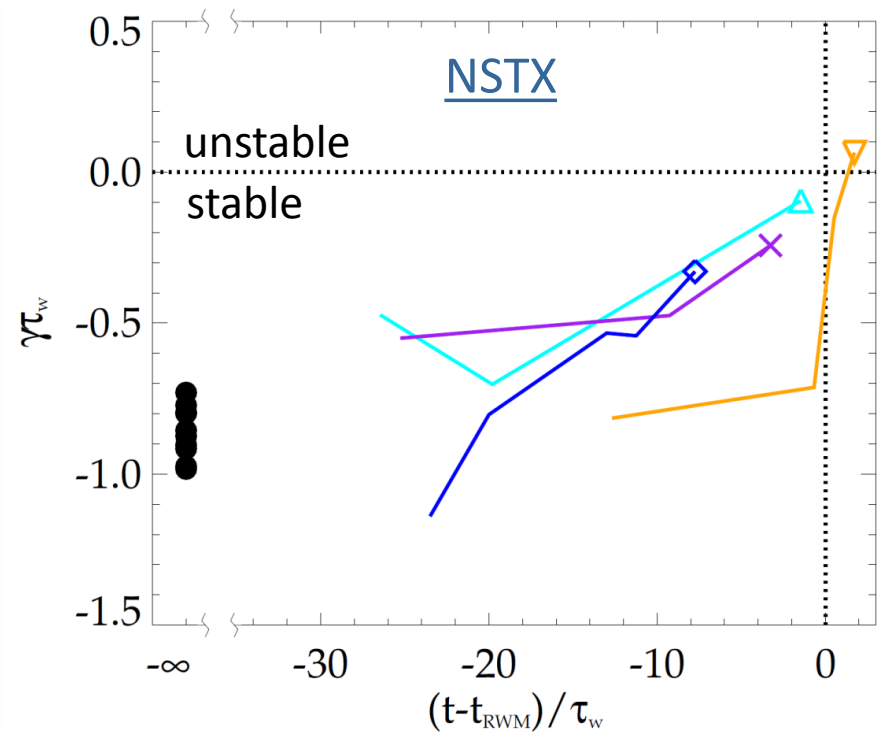
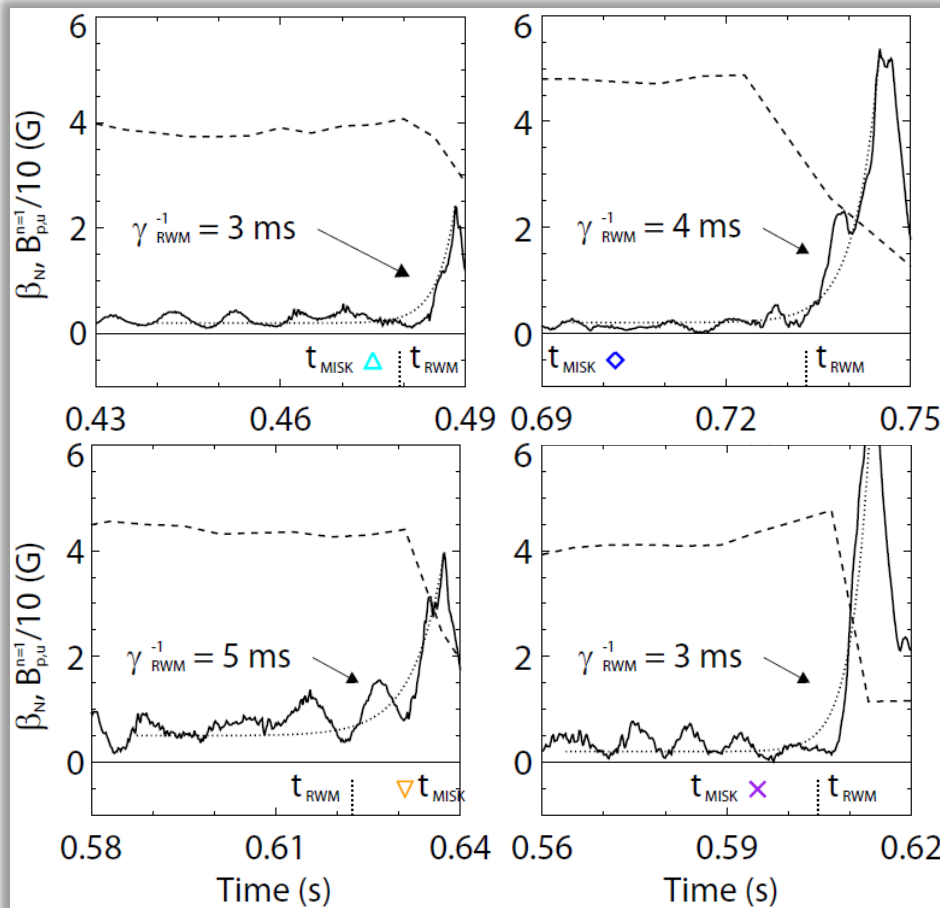
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# MISK calculations validated against unstable experimental plasmas; reproduce approach towards marginal stability



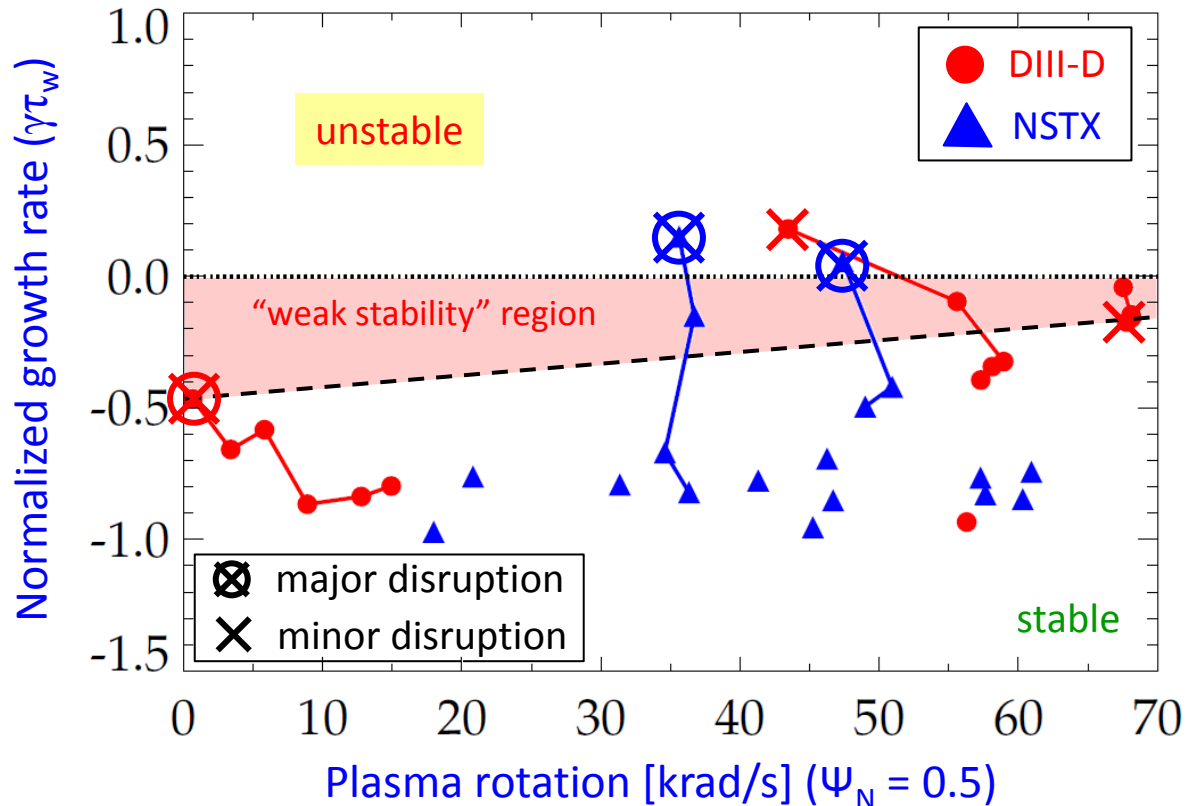
[J. Berkery et al., Nucl. Fusion 55, 123007 (2015)]

- MISK calculations including kinetic effects have been tested against many marginally stable NSTX experimental cases

# Kinetic RWM stability physics unites results from DIII-D and NSTX plasmas

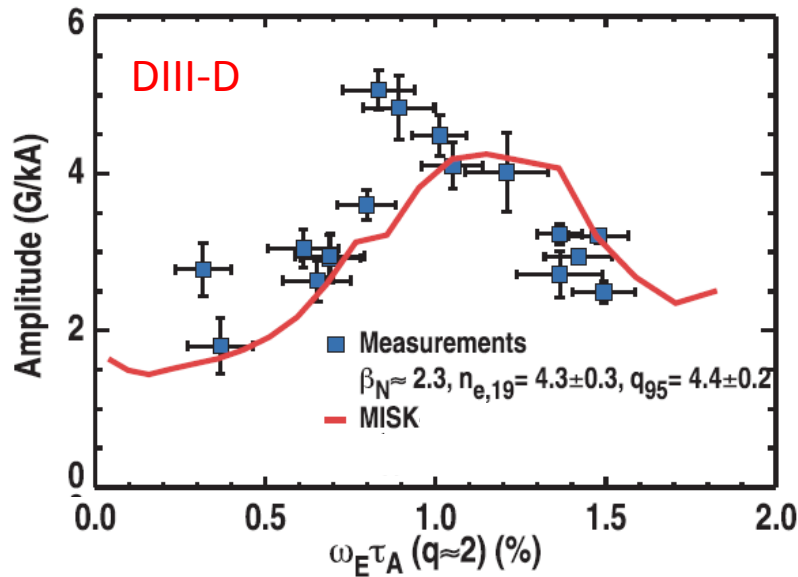
- Addition of kinetic effects yields agreement with marginal point in NSTX
- Further testing against DIII-D experiments shows good agreement
- Strong bursting MHD modes can lead to non-linear destabilization before linear stability limits are reached

Kinetic RWM stability analysis for experiments (MISK)

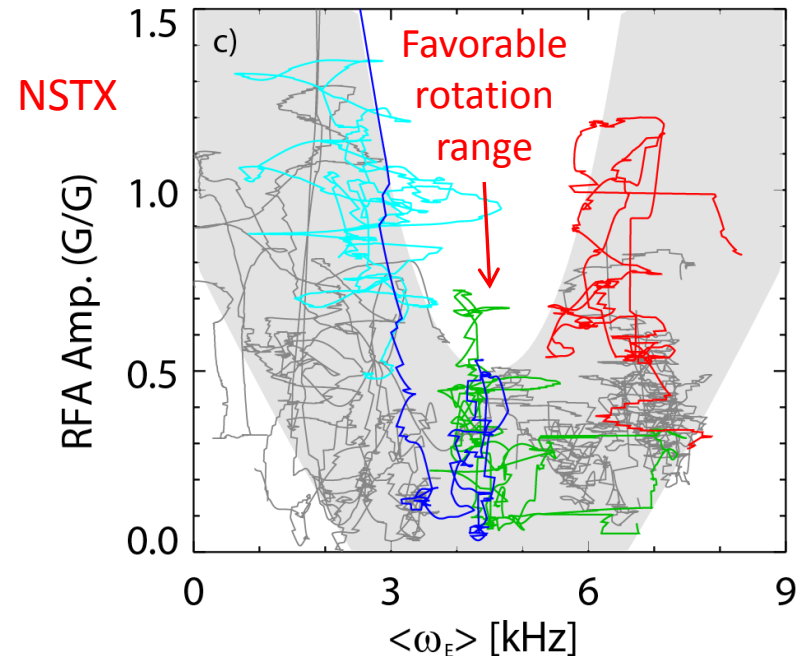


[S. Sabbagh, J. Berkery, J. Hanson, et al., APS invited 2014]

# Active MHD spectroscopy experiments show the importance of kinetic effects in stable plasmas as well



[H. Reimerdes et al., Phys. Rev. Lett. 106, 215002 (2011)]



[J. Berkery et al., Phys. Plasmas 21, 056112 (2014)]

- Resonant field amplification indicates weakening stability
  - Plasma response is enhanced where kinetic effects and RWM stability are weak

- Discharge trajectories for 20 NSTX plasmas shows favorable  $\omega$  range
  - Matches theoretical expectation for precession drift resonance



MISK calculations match experiments

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# Physics understanding from previous research used to construct a reduced kinetic model

- Goal is to forecast  $\gamma$  in real-time using parameterized reduced models for  $\delta W$  terms
- Need  $\delta W_K$  as a function of the most important, real-time measurable quantities

$$(\gamma - i\omega_r) \tau_w = - \frac{\delta W_\infty + \delta W_K}{\delta W_b + \delta W_K}$$

Fluid terms

Kinetic effects:

$$\delta W_K \sim \frac{1}{\langle \omega_D \rangle + \omega_E - i\nu}$$

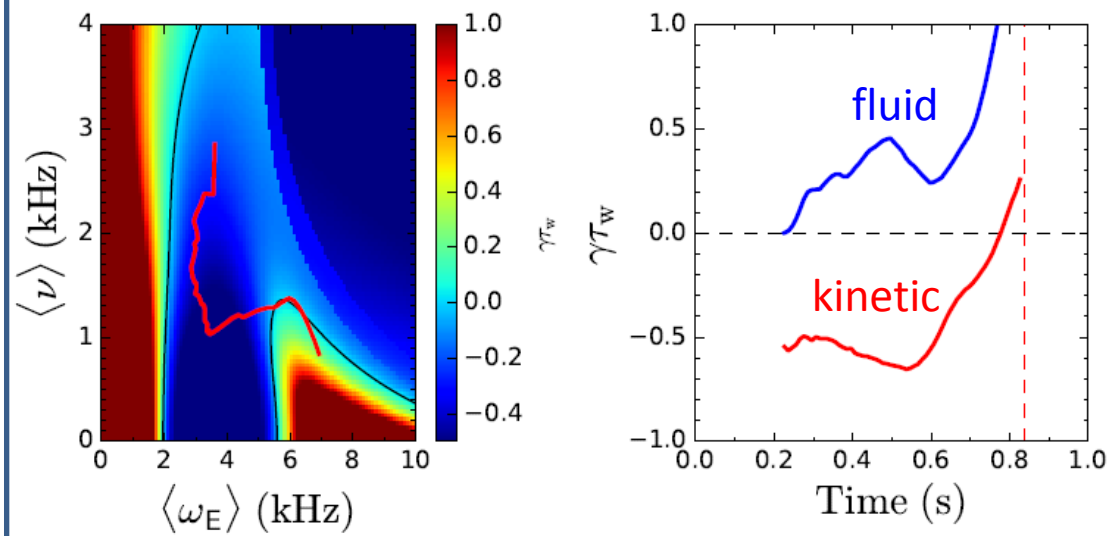
Rotation  
+ Energetic Particles

Collisionality

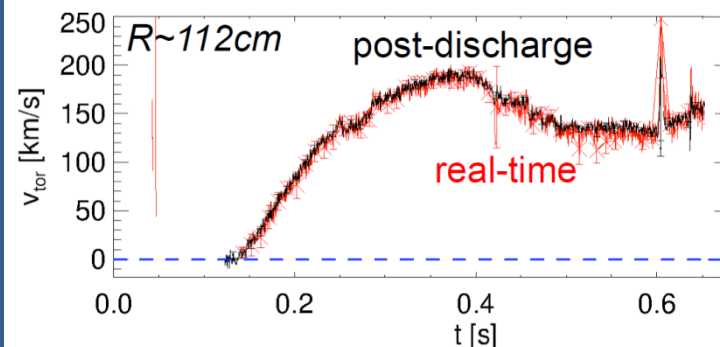
**MISK<sup>2</sup> Calculations**

Compared to experiments

## Reduced Kinetic Model



Real-time velocity data now available on NSTX-U



Rotation controller designed using NBI, NTV

# Summary

- RWM stability must be understood for future devices
- Kinetic theory modifies ideal stability, includes rotation, collisionality, and energetic particle effects
- ITER stability projections show all kinetic effects important
- MISK code calculations can explain experimental stability
- Reduced models needed for real-time disruption avoidance

Fluid terms

Kinetic effects

~ Rotation Collisionality

$$(\gamma - i\omega_r) \tau_w = - \frac{\delta W_\infty + \delta W_K}{\delta W_b + \delta W_K}$$

$$\delta W_K \sim \frac{1}{\langle \omega_D \rangle + \omega_E - i\nu}$$

Rotation resonance

Collisionality

Energetic Particles