

Energy transport analysis of NSTX plasmas with the TGLF turbulent and NEO neoclassical transport models

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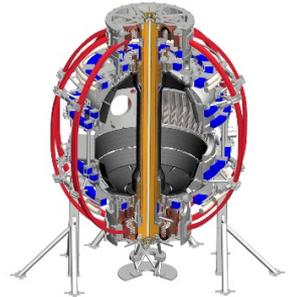
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Outline

- Motivation
- Experimental data details
- **Workflow of the data analysis**
- Profiles prediction with TGYRO (TGLF+NEO) solver
- Comparison of profiles prediction with experimental data
- **Variation of input parameters**
- Linear stability analysis
- Results

Motivation: Reduced models are more advantageous in terms of computational cost

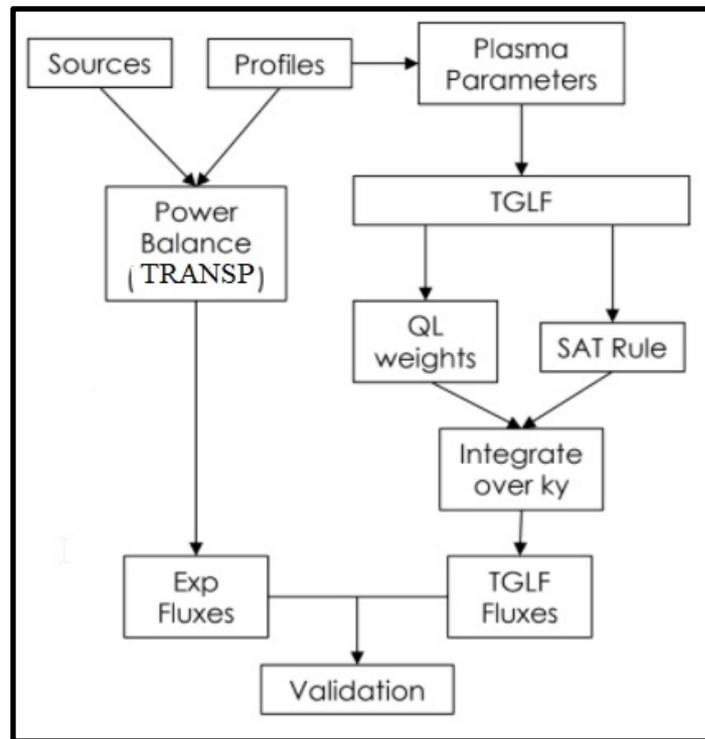
- Comprehensive numerical transport models are typically not feasible for real-scale full-device modeling



- **Fast reduced turbulent numerical models**
- Identifying the regimes of validity of such models increases the fidelity of predictive modeling
- The design of the next generation fusion machines requires **validation of transport models over a range of aspect ratio** to determine the optimal parameters

Trapped-gyro-Landau-fluid (TGLF) model is a reduced turbulent model

- TGLF¹ predicts a transport driven by drift-wave instabilities (TEMs, ITGs, ETGs)
- TGLF computes turbulent fluxes using the linear eigenmode solution and a model of the saturated intensity
- Versions of the saturation rule:
SAT0¹, **SAT1²**, SAT2³
- *NEO*⁴ is a drift kinetic neoclassical solver



1 [Staebler G.M et. al., *Physics of Plasmas* 12, (2005)]; 2 [Staebler G.M et. al., *Nuclear Fusion* 57, (2017)];
3 [Staebler G. M. et al., *Physics and Controlled Fusion* 63, (2021)]; 4 [Belli E. et. al., *Plasma Phys. and Controlled Fusion* 50, (2008)]

TGLF model validations on STs is still in its early stages

- TGLF has been **extensively utilized for transport modeling of conventional tokamaks** (ASDEX-U, JET, DIII-D)
- **Only a few studies** of validation of reduced transport models **at low aspect ratio plasmas** have been reported
 - first demonstration of TGLF on STs \Rightarrow limitations of the implementation of the collisional model and the saturation rule¹
- modeling of NSTX \Rightarrow better results with SAT1 model compared to simulations with the simplified SAT0 model²

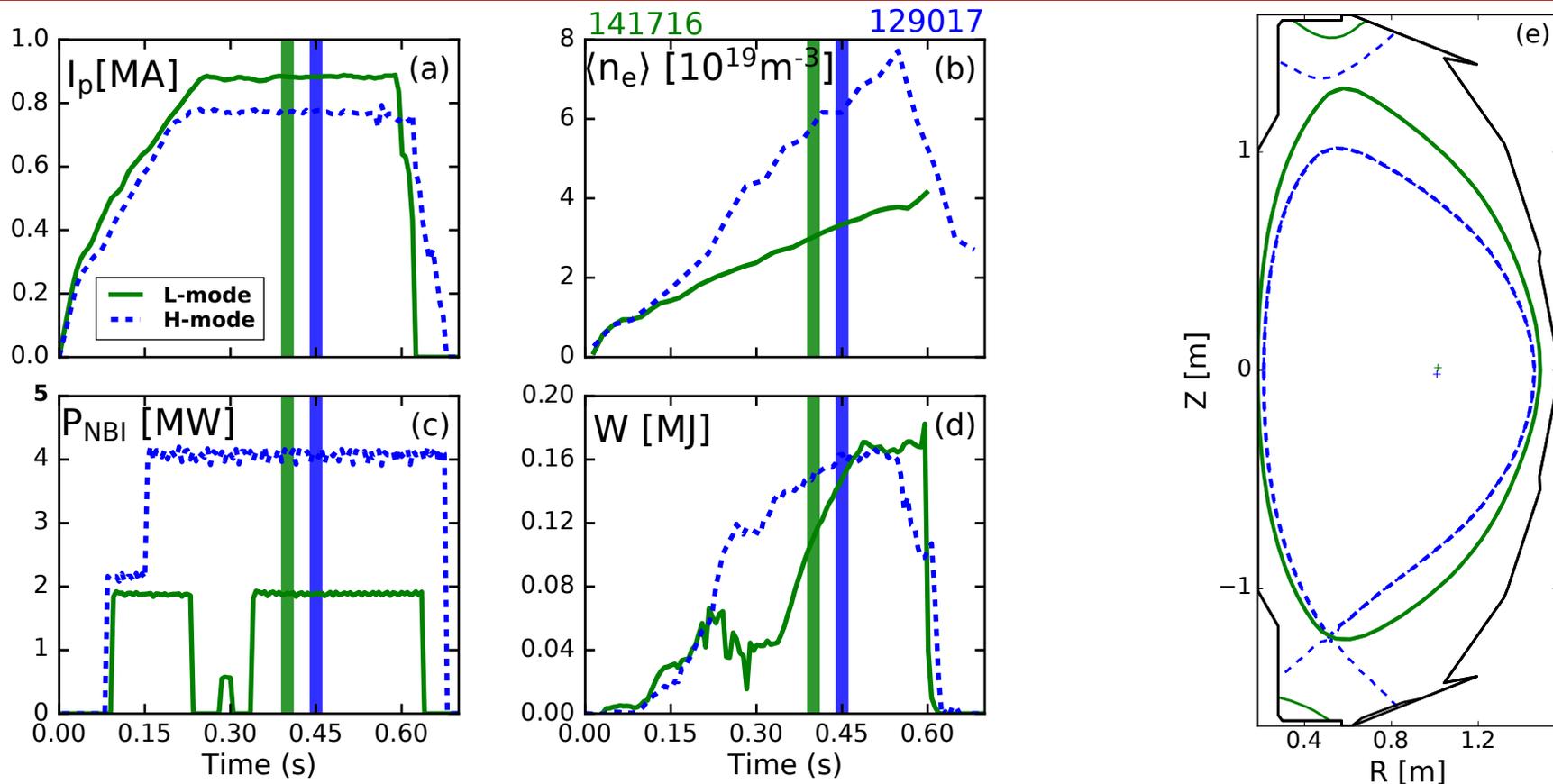
1 Staebler G.M et. al., 22nd IAEA Fusion Energy Conf., (2008)]

2 S.M. Kaye et al., Nucl. Fusion 59 (2019)

An extension of previous studies is conducted to verify TGLF and NEO models on the NSTX data

- **Two discharges** with a transport predominantly driven by the electrostatic drift-wave instabilities have been selected:
 - **L-mode** (# 141716) at low- β and density **with conditions close to the conventional tokamaks** where both low- k ($k_{\theta}\rho_s \leq 1$) ion scale and high- k ($k_{\theta}\rho_s > 1$) electron scale turbulence are present
 - **H-mode** (# 129017) which is **typical for STs**, where ion transport is neoclassical
- A **sensitivity study of predicted results** is performed by variations of input plasma profiles
- Results of a linear stability analysis are analyzed to determine if a picture of mechanisms driving the transport is captured correctly by TGLF and NEO models

Experimental data is analyzed over a time window of 40 ms



Equilibrium reconstruction is obtained through EFIT-TRANSP integrated workflow using OMFIT

Initial equilibrium

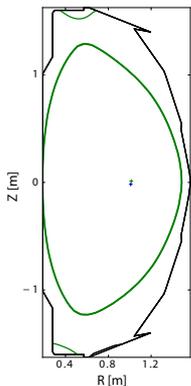


Mapping of profiles to flux coordinates

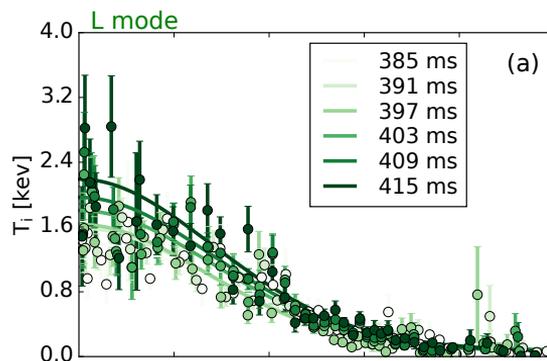


Transport code computes a current density profile and a total plasma pressure

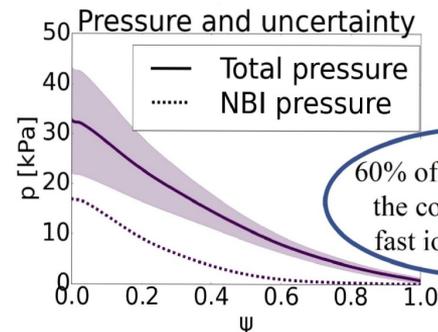
EFIT with magnetics, MSE, isothermal constraints



OMFIT profiles: fetching, mapping, slicing, fitting, averaging



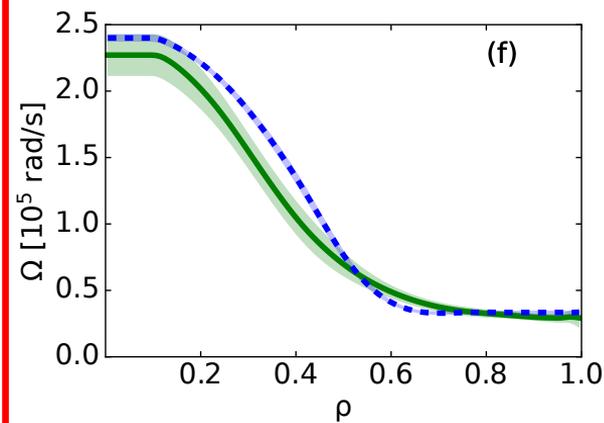
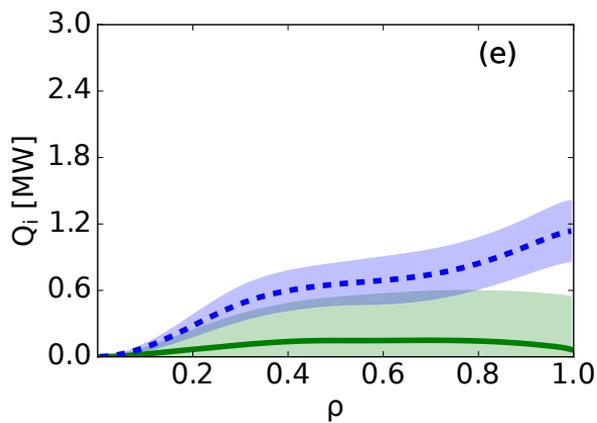
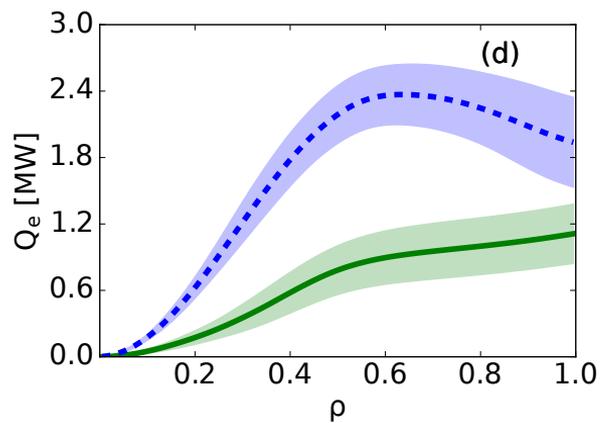
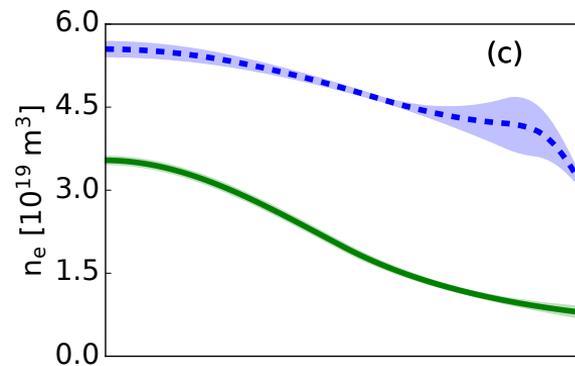
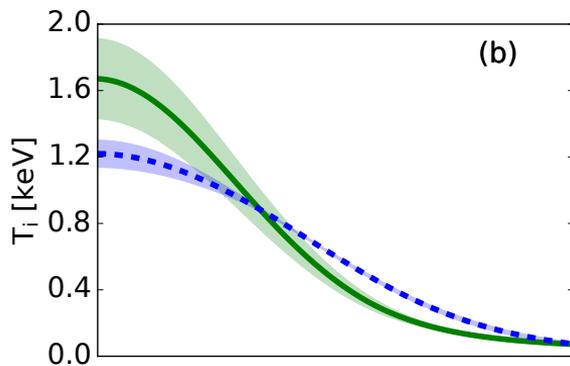
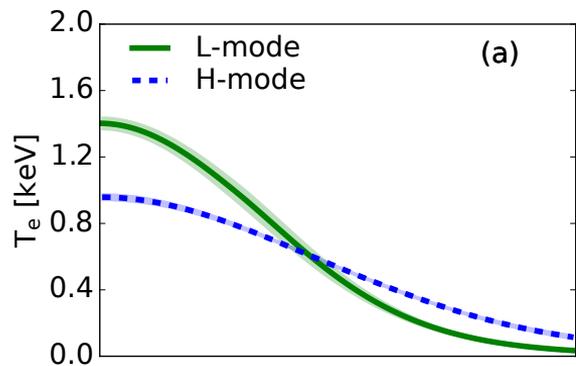
TRANSP + NUBEAM



Apply these constraints on the next iteration of the equilibrium reconstruction

The self-consistent solution is usually obtained after 3 - 4 iterations

The power deposition is determined through the power balance analysis with TRANSP+NUBEAM



TGYRO (TGLF +NEO) flux-matching solution predicts profiles based on known plasma sources

- TGYRO solver reconstructs plasma profiles based on gradients, which satisfy the steady state transport equation

$$\frac{1}{V'} \frac{\partial}{\partial r} [V'(r) Q(r)] = S$$

Q – energy flux predicted based on the plasma gradients

$$Q_{model} = Q_{turbulent}^{TGLF} + Q_{neoclassical}^{NEO}$$

S – integrated source (power/volume), obtained from the power balance analysis
auxiliary NBI heating, radiation losses, collisional e-i heat exchange minus energy gain

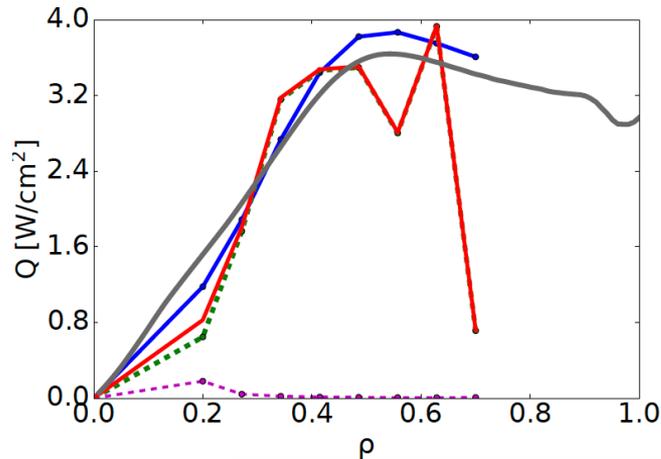
$$Q_{target} \approx S$$

TGYRO flux-matching solution predicts profiles based on known plasma sources

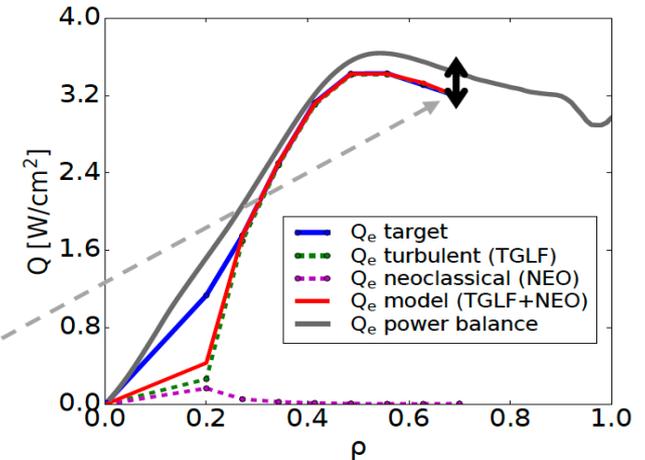
- TGYRO applies an iterative scheme varying the local gradients to minimize

$$|Q_{model} - Q_{target}|$$

Iteration 20



Iteration 60



Due to dynamic exchange term $\propto T_e/T_i$

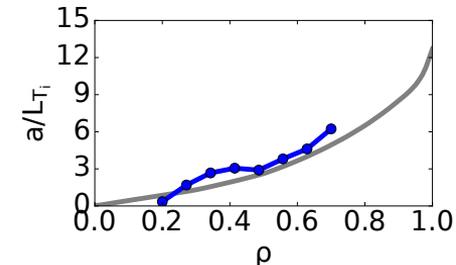
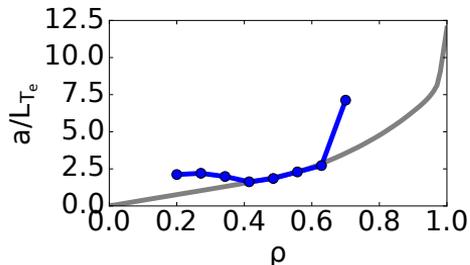
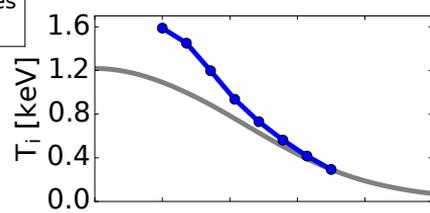
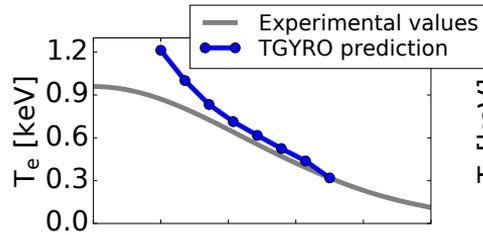
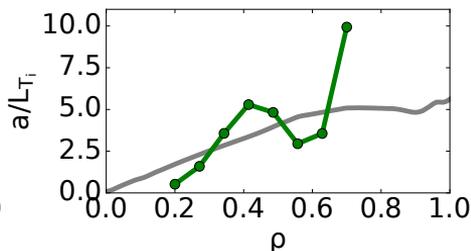
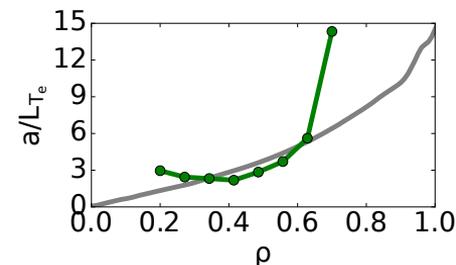
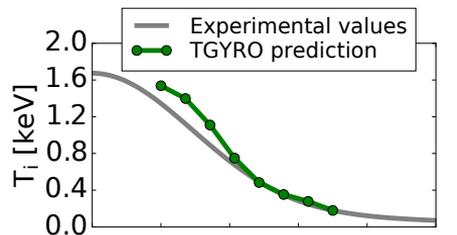
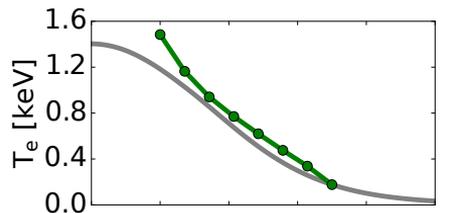
- Plasma profiles are obtained by the integral of the local gradients

$$T(r) = T^* \exp\left(-\int_r^{r^*} \frac{1}{T} \frac{\partial T}{\partial r} dr\right)$$

Predicted plasma profiles and inverse gradients are then compared with experimental data

L-mode

H-mode



Variation of input parameters

Equilibrium reconstruction is obtained through EFIT-TRANSP integrated workflow using OMFIT

Initial equilibrium



Mapping of profiles to flux coordinates



Transport code computes a current density profile and a total plasma pressure

EFIT with magnetics, MSE, isothermal d

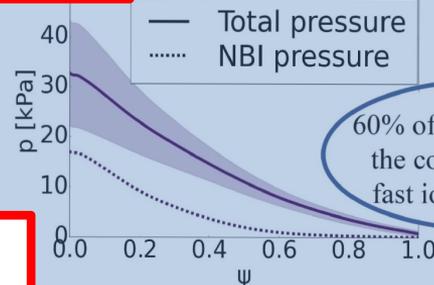
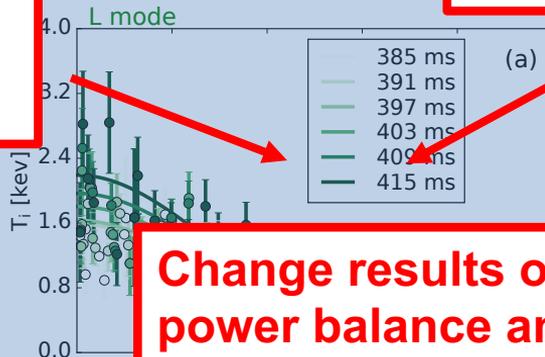
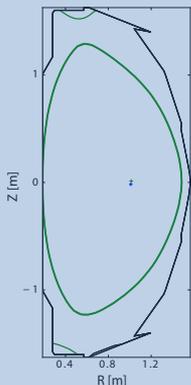
OMFIT profiles: fetching, mapping, slicing, fitting, a

TRANSP + NUBEAM

pressure and uncertainty

A) Change number of constraints

B) Change fitting method



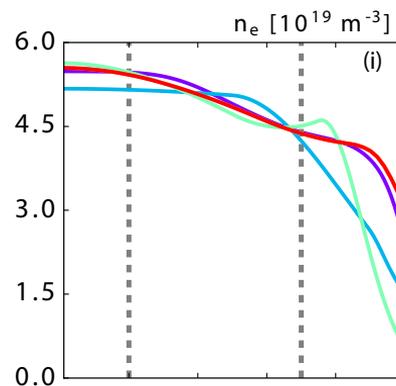
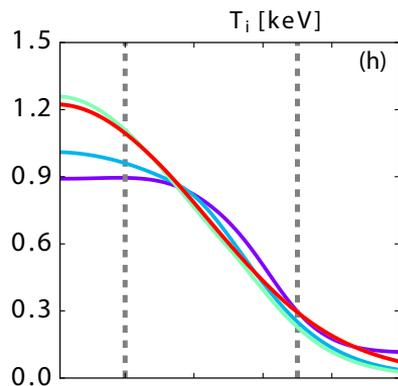
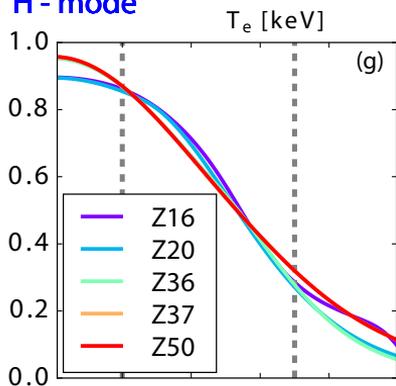
Change results of the power balance analysis

Apply these constraints on the next iteration of the equilibrium reconstruction

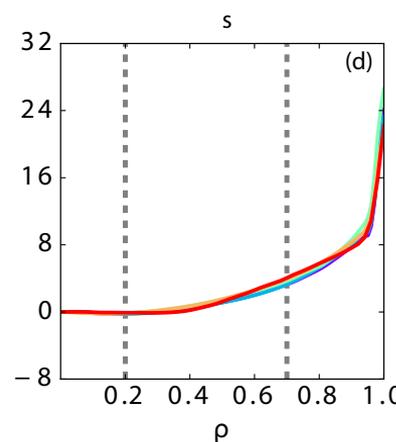
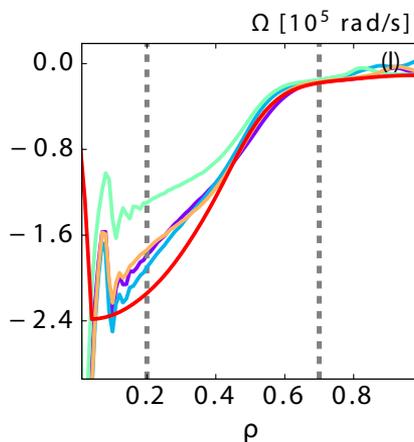
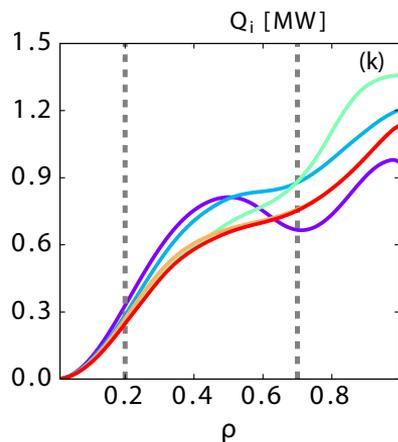
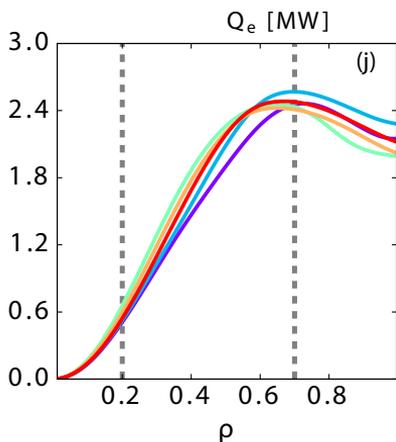
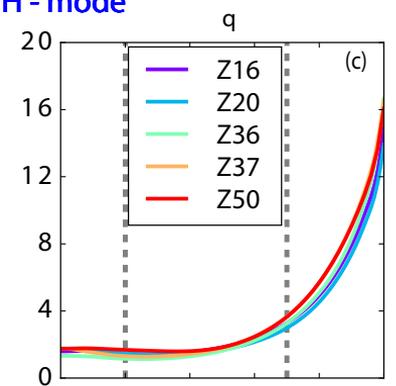
The self-consistent solution is usually obtained after 3-4 iterations

These different TRANSP runs are results of a self-consistent integrated solution

H - mode

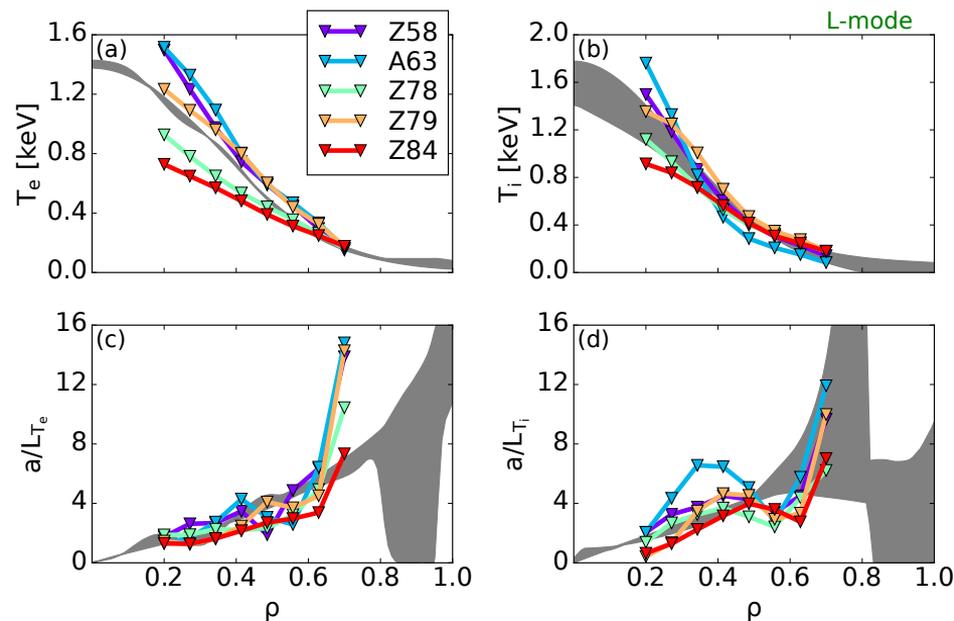


H - mode

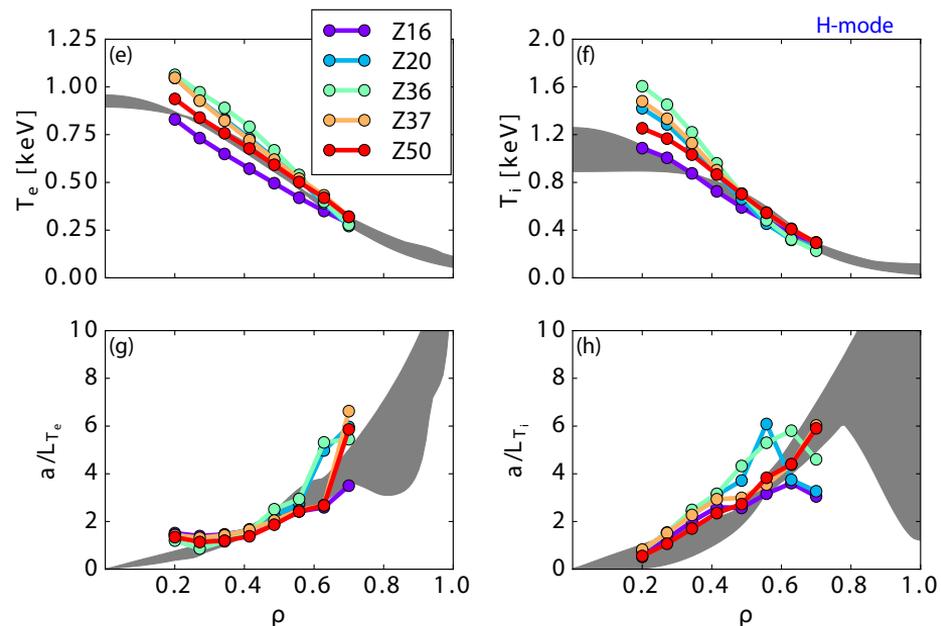


No trend of under- or over- prediction is observed

L-mode

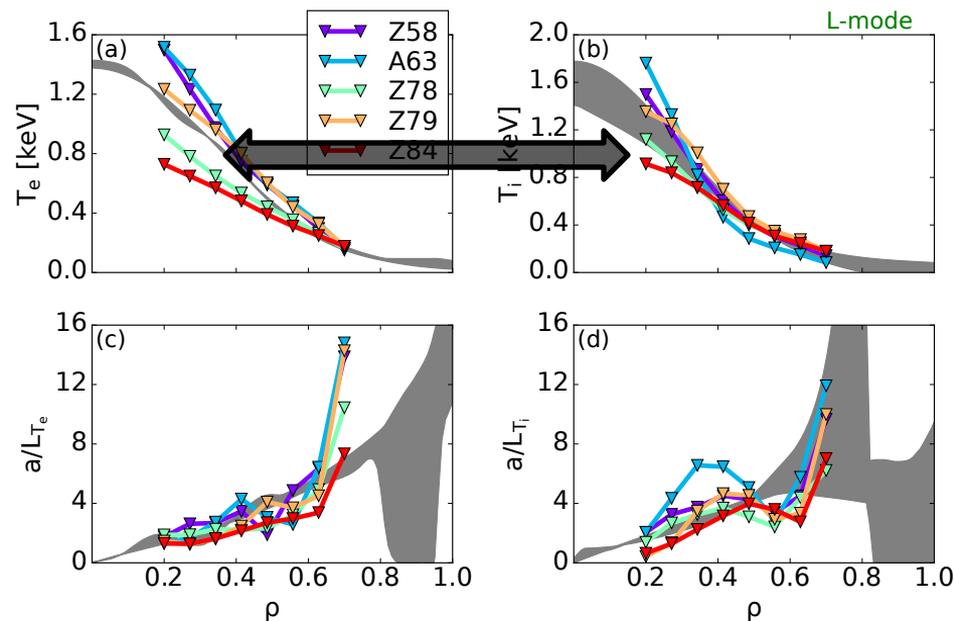


H-mode

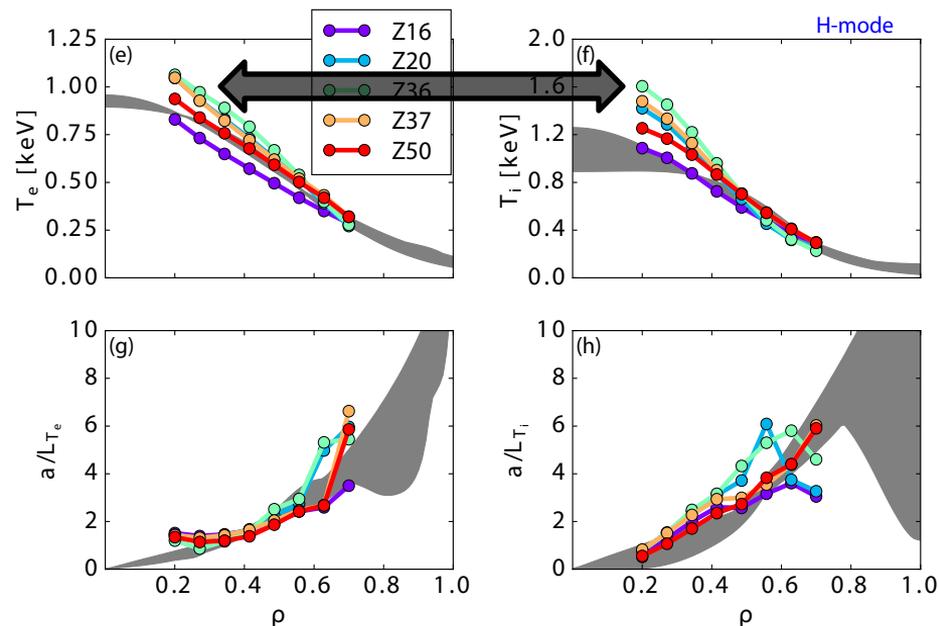


No trend of under- or over- prediction is observed

L-mode



H-mode

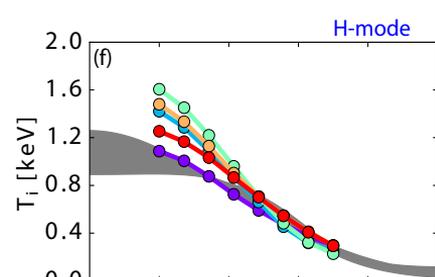
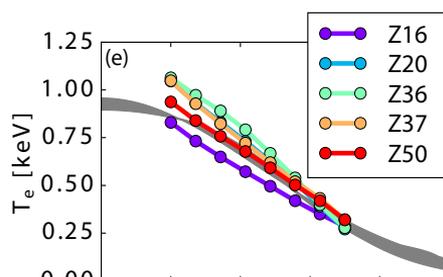
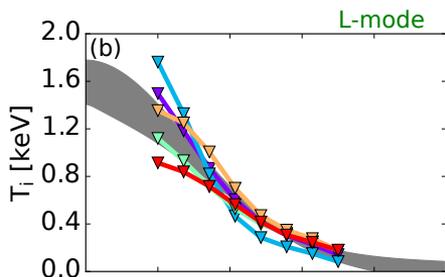
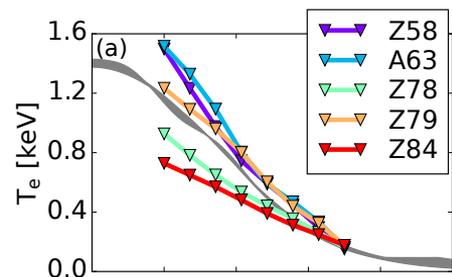


But there is a correlation in under- and over- prediction between T_e and T_i

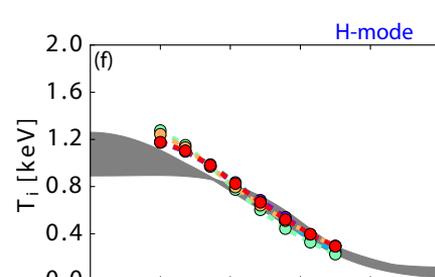
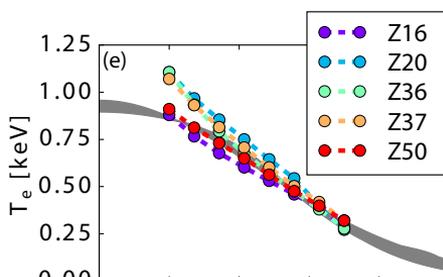
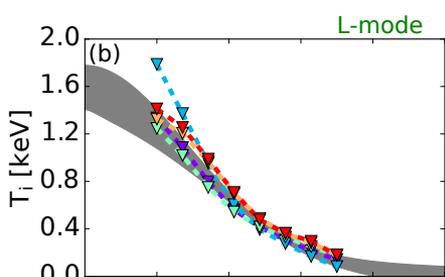
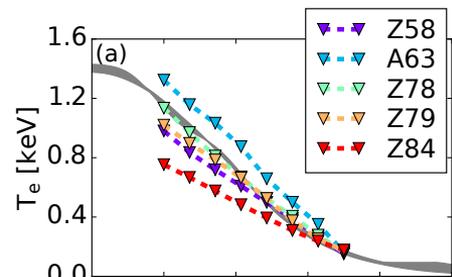
Prediction of each temperature separately gives a more uniform set of solutions

L-mode

H-mode



Prediction of each temperature separately



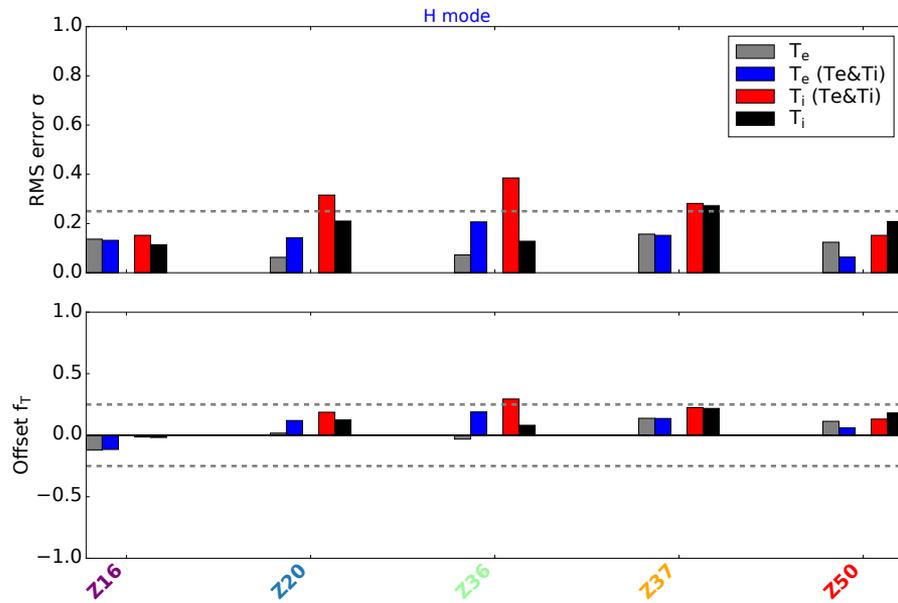
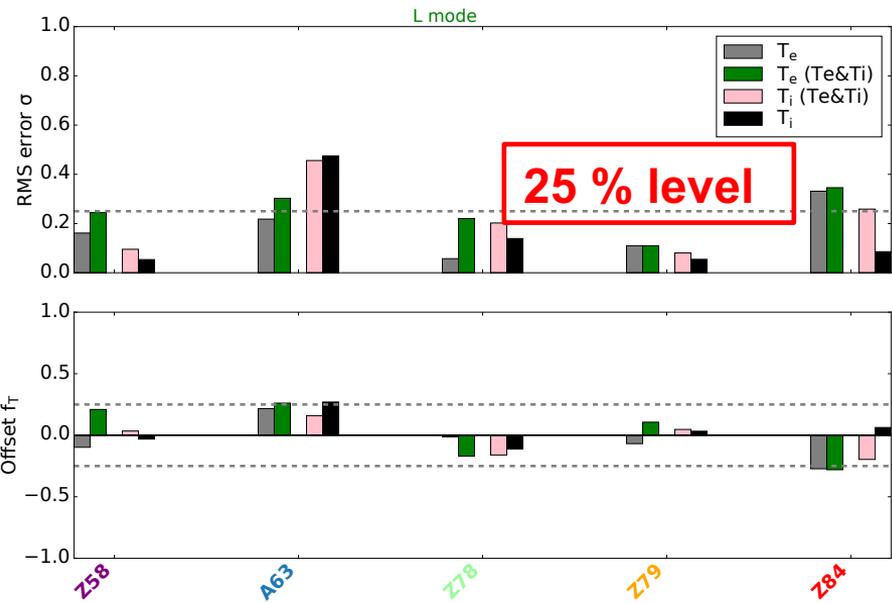
The predicted plasma profiles are consistent with experimental data on average

$$\text{RMS error } \sigma_T = \sqrt{\frac{1}{N} \sum_j \epsilon_j^2} / \sqrt{\frac{1}{N} \sum_j T_{x,j}^2}$$

$$f_T = \frac{1}{N} \sum_{j=N} \epsilon_j / \sqrt{\frac{1}{N} \sum_j T_{x,j}^2}, \quad \text{Offset}$$

L-mode

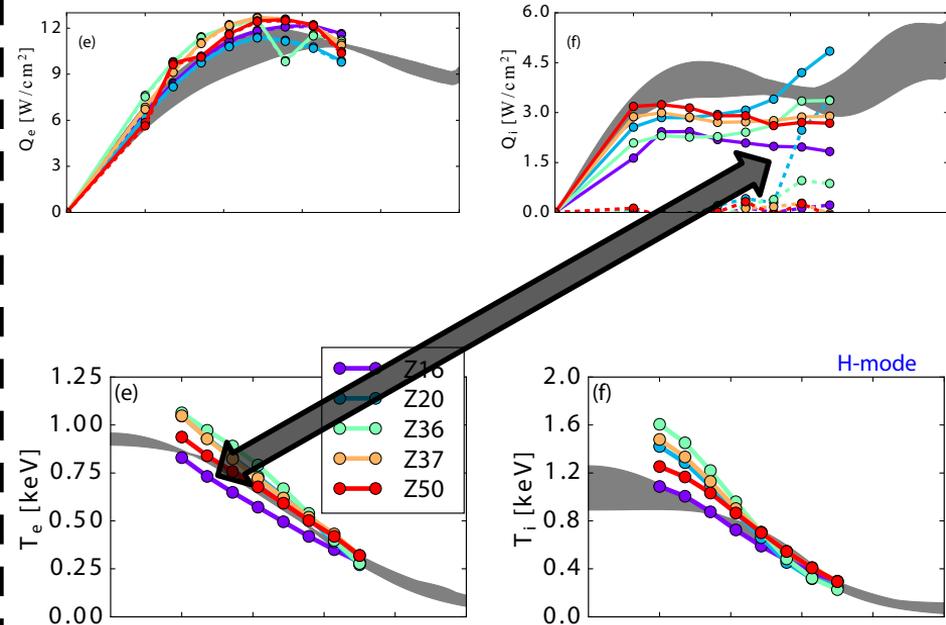
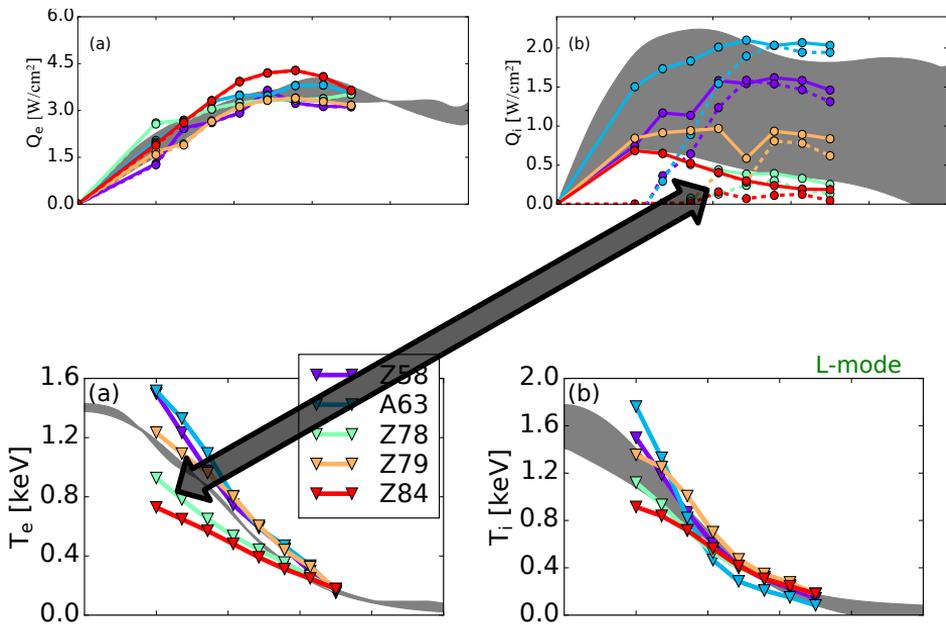
H-mode



TGYRO solution is predominantly affected by the accuracy of the sources (including Q_{ei})

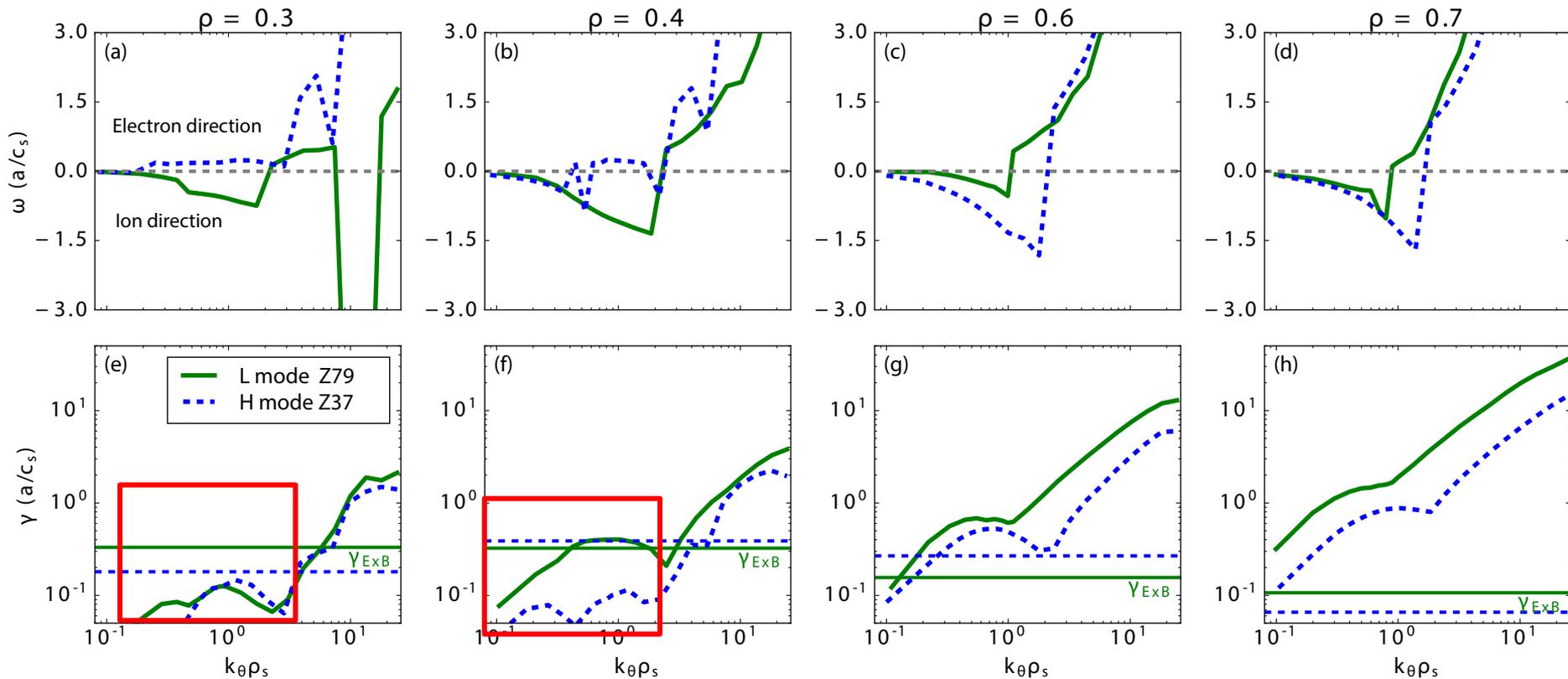
L-mode

H-mode



Linear stability analysis to identify unstable modes

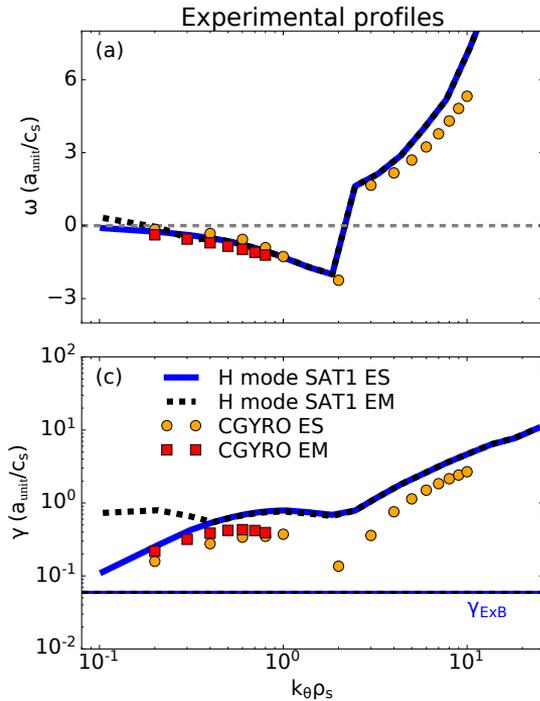
Growth rates of low- k modes ($k_\theta \rho_s < 1$) are below ExB shearing rate at deep core locations



Growth rates predicted by TGLF are higher than CGYRO simulations

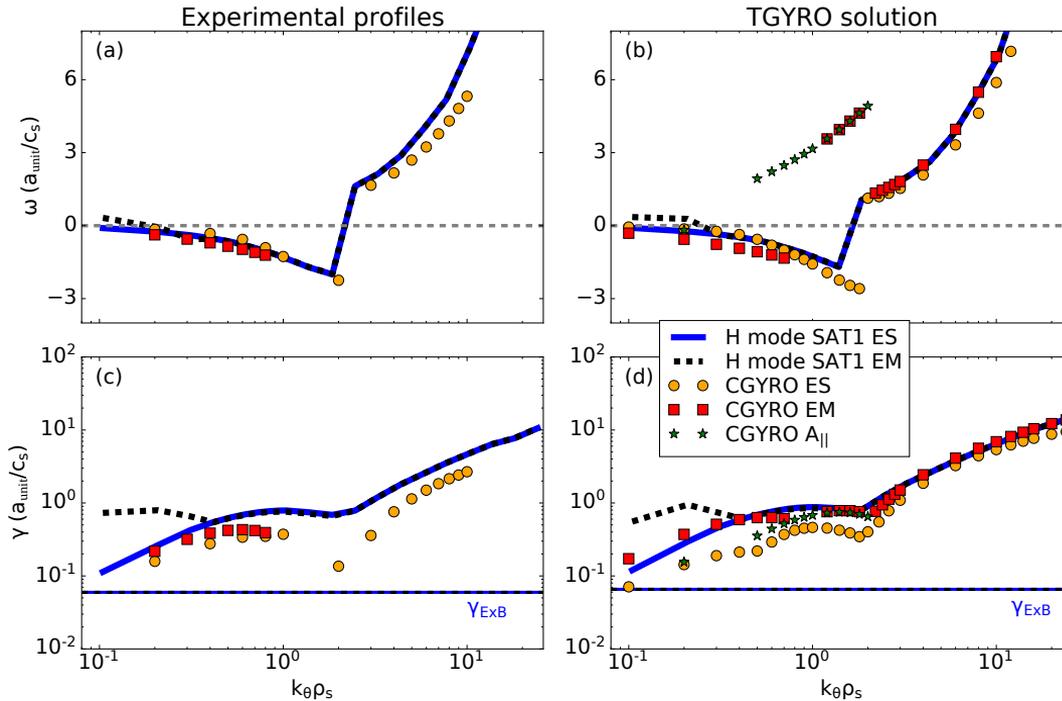
H-mode $\rho = 0.7$

- Good agreement between real frequencies
- No electromagnetic modes are unstable in simulations with experimental profiles

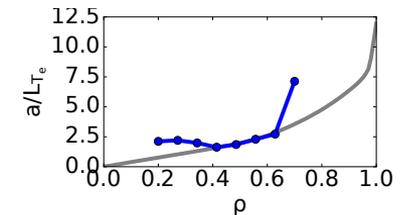


Growth rates predicted by TGLF are higher than CGYRO simulations

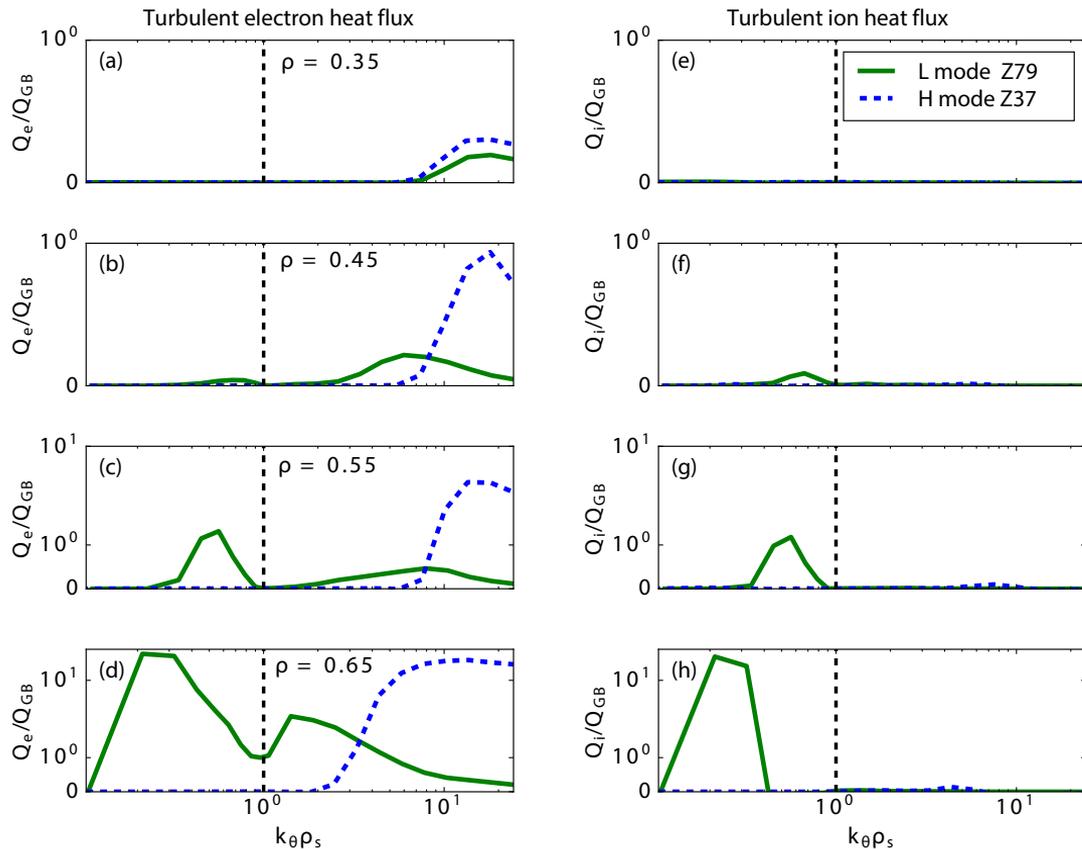
H-mode $\rho = 0.7$



- Good agreement between real frequencies
- No electromagnetic modes are unstable in simulations with experimental profiles
- TGYRO solution profiles have higher temperature gradients, which destabilize electromagnetic instabilities

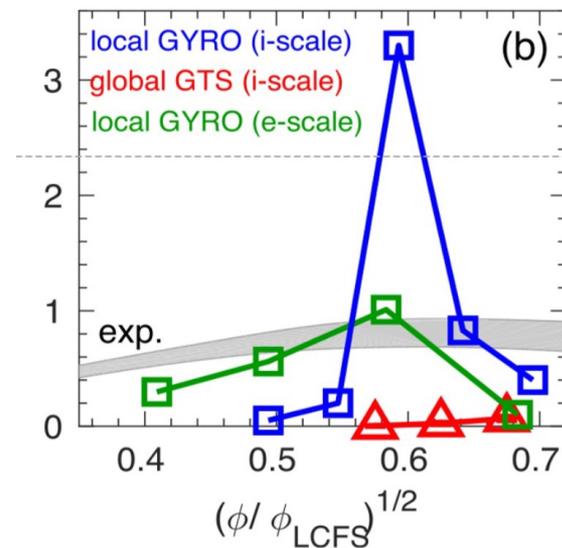


The contribution of low-k and high-k modes into the total turbulent flux is consistent with previous results



L-mode

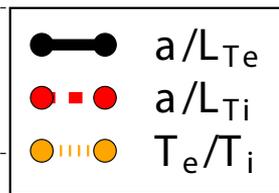
Q_e (MW)



- S.M. Kaye et al., Nucl. Fusion 59 (2019)
- Y. Ren et al., Nucl. Fusion, 53 (2013)

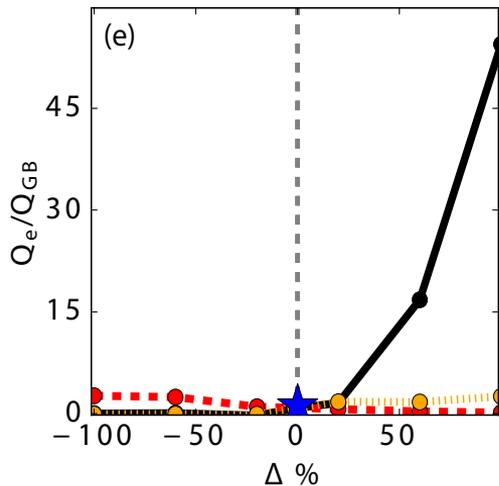
Scans of plasma parameters demonstrates how close the plasma conditions to the stability threshold

$\rho = 0.35$



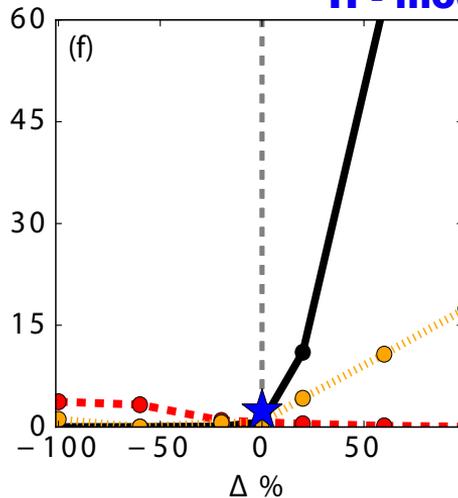
$\rho = 0.35$

H - mode



$\rho = 0.45$

H - mode

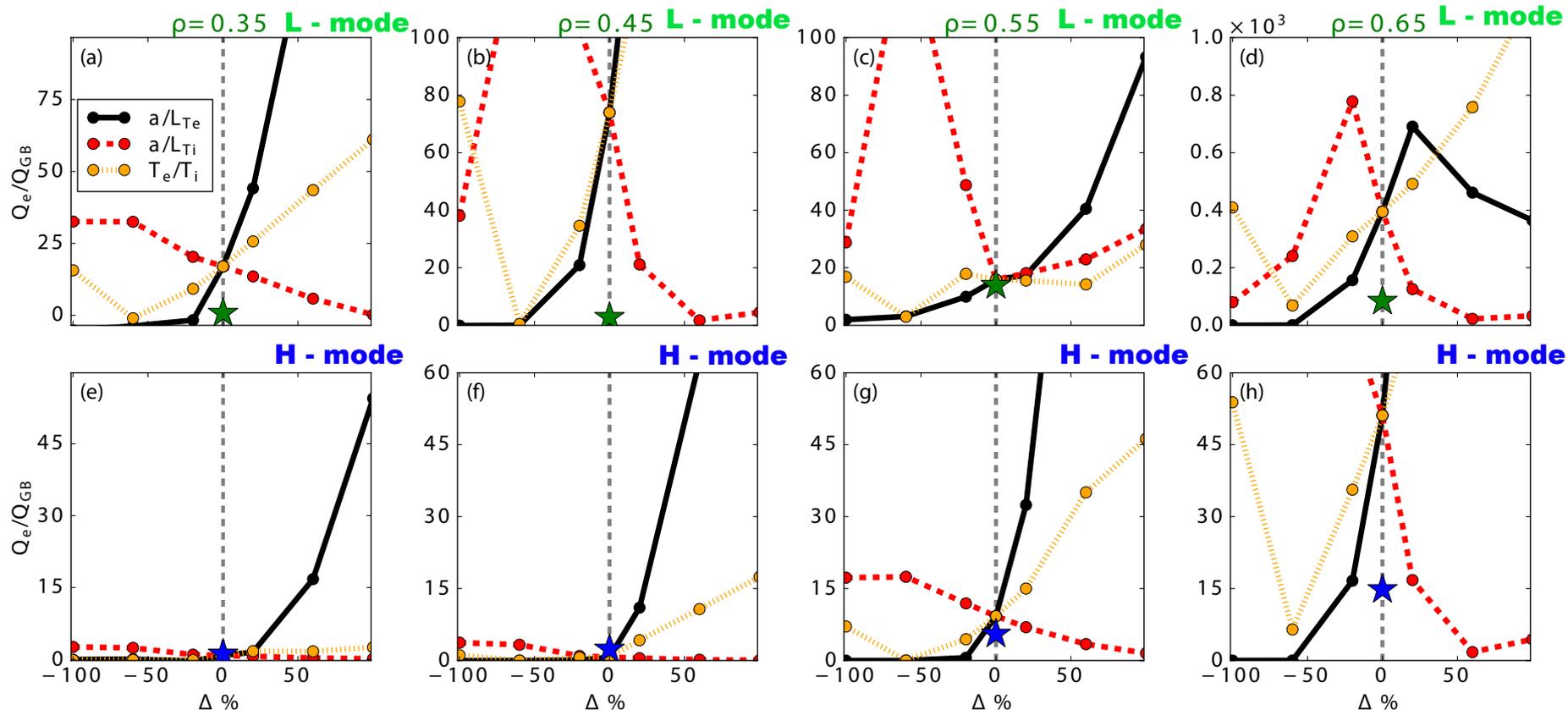


- Plasma conditions are below the critical threshold
- Instabilities driven by a/L_{Te} are destabilized only at gradients above 25% of experimental level

$\rho = 0.45$

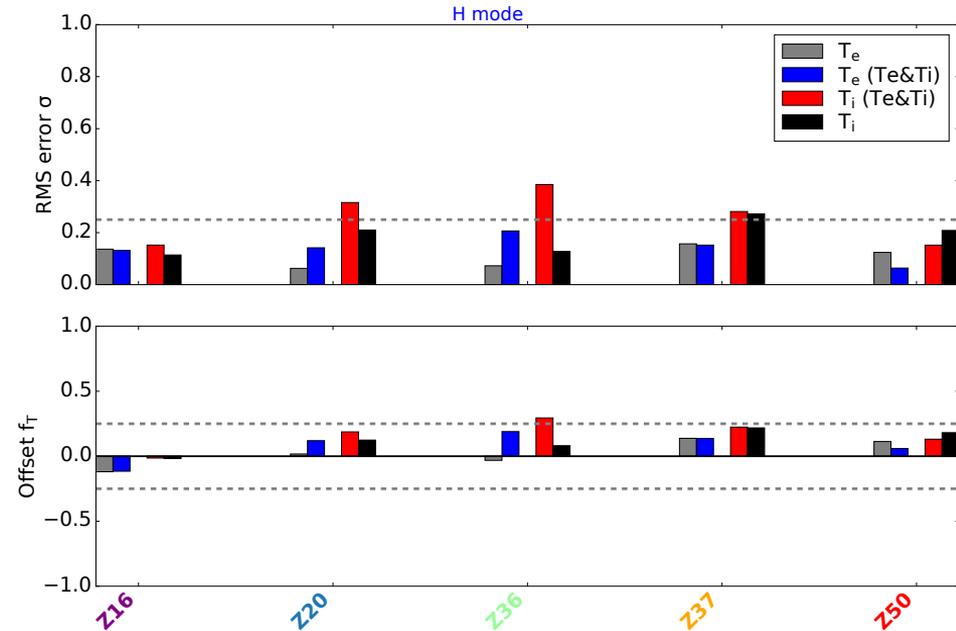
- A flux dependency from a/L_{Te} and T_e/T_i indicates unstable modes

Overall the scans demonstrate the complicated dependency of turbulent flux on the plasma parameters



Summary of results

- Overall, the predicted plasma profiles are consistent with experimental data on average
- The shortcomings of the TGYRO simulations are amplified when both temperature profiles are modeled instead of a single temperature profile
- A presence of multi-scale turbulence and ion-scale driven zonal flow mixing effects are observed



Paths toward reliable predictive modeling of STs with TGLF should include

- More accurate power balance analyses, which determines the target fluxes of the flux-matching solution
- More systematic calibrations of the saturation model on non-linear gyrokinetic simulations to verify the applicability of the saturation rule models for STs plasmas
- Models with comprehensive physics of electromagnetic instabilities would be required for a high plasma- β with increased influence of electromagnetic effects