

Kinetic Theory of Alfven Cascades

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Introduction

- This work considers kinetic effects of thermal ions and energetic particles on Alfvén Cascades.
- MHD dispersion relation for Alfvén cascades:

$$\omega^2 = k_{\parallel}^2 v_A^2 + \omega_{GAM}^2 + \Delta_{MHD}$$

$$\omega_{GAM}^2 = \frac{2\gamma P}{\rho R^2}$$

- What is γ ?

Kinetic Dispersion Relation

- MHD $\omega_{GAM}^2 = \frac{2\gamma P}{\rho R^2}$
- Kinetic $\omega_{KGAM}^2 = \frac{2(\gamma_e P_e + \gamma_i P_i + \gamma_h P_h)}{\rho R^2}$

$$\gamma_e = \frac{(1 - \omega_{*pi}/\omega)^2}{1 + \frac{T_e}{T_i} \omega_{*ni}/\omega}$$

for $q \gg 1$

$$\gamma_i = \frac{7}{4} \left(1 - \frac{\omega_{*pi}}{\omega} - \frac{\omega_{*Ti}}{\omega} \right)$$

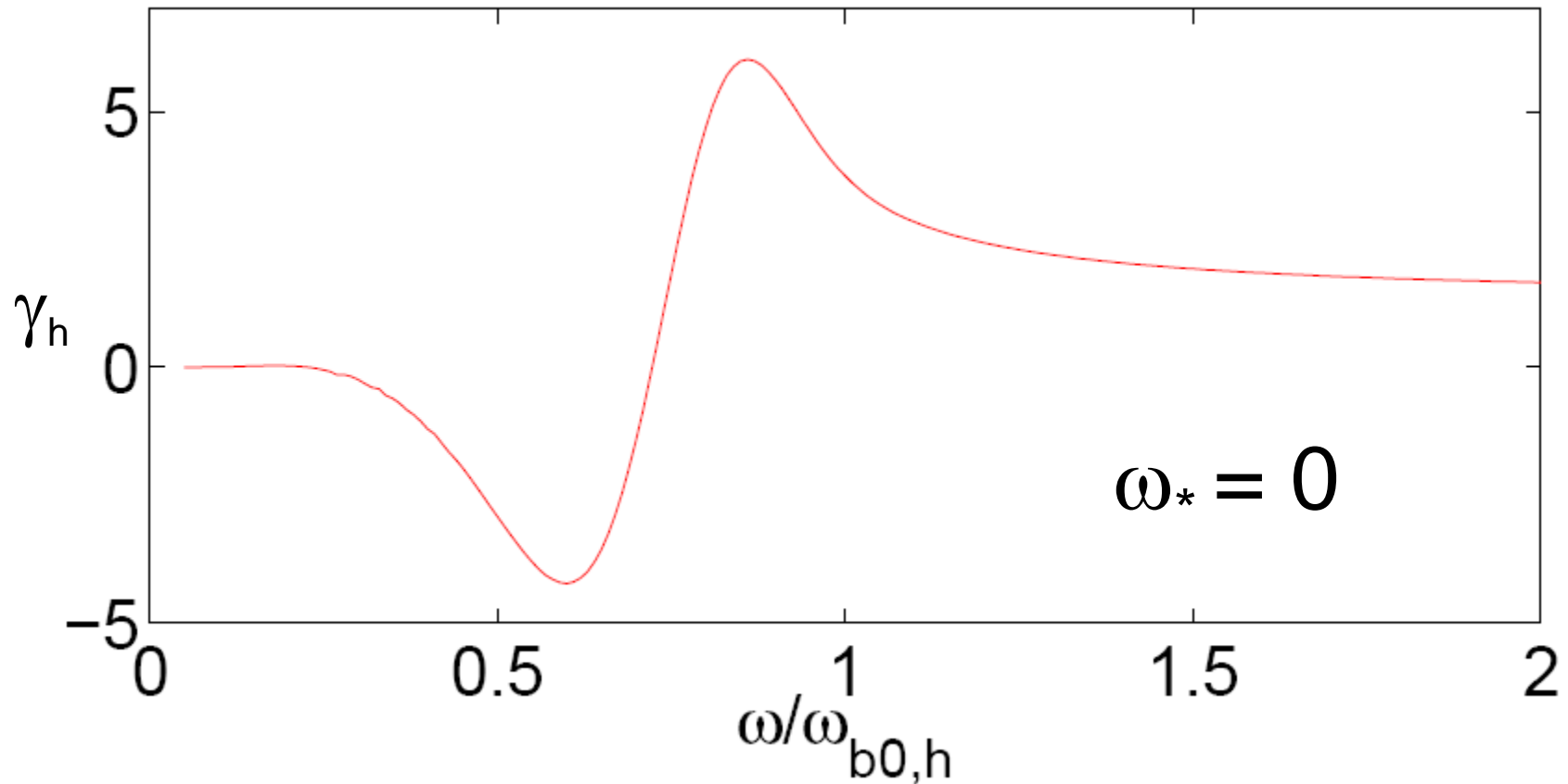
Energetic Particle Contribution

$$\gamma_h = - \frac{2 \int \frac{\partial f}{\partial E} E^3 dE d\Lambda \tau_b H_1^2 (1 - \omega_{*h}/\omega) \omega^2 / (\omega^2 - \omega_b^2)}{\int f E^2 dE d\Lambda \tau_b < 2 - \Lambda B >}$$

$$H_1 = \frac{1}{\tau_b} \int dt' (2 - \Lambda B) G(r', \theta') \sin(\omega_b t')$$

$$G(r, \theta) = - \frac{B_\phi R}{J B^3} \frac{\partial B}{\partial \theta}$$

Energetic Particle Contribution: frequency dependence



Summary

- We have derived a kinetic dispersion relation for Alfvén cascade modes including kinetic effects of thermal ions and energetic particles;
- Thermal ion temperature gradient can drive high- n Alfvén cascade modes;
- Kinetic theory should be used for evaluation of Alfvén Cascade frequency;
- In principal, energetic particle effects can reduce Cascade mode frequency.