

# NSTX transport study via density fluctuation measurement of FReTIP system

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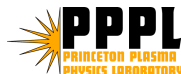
*POSTECH*

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*APS DPP meeting Nov 19, 2008*

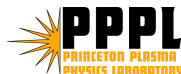


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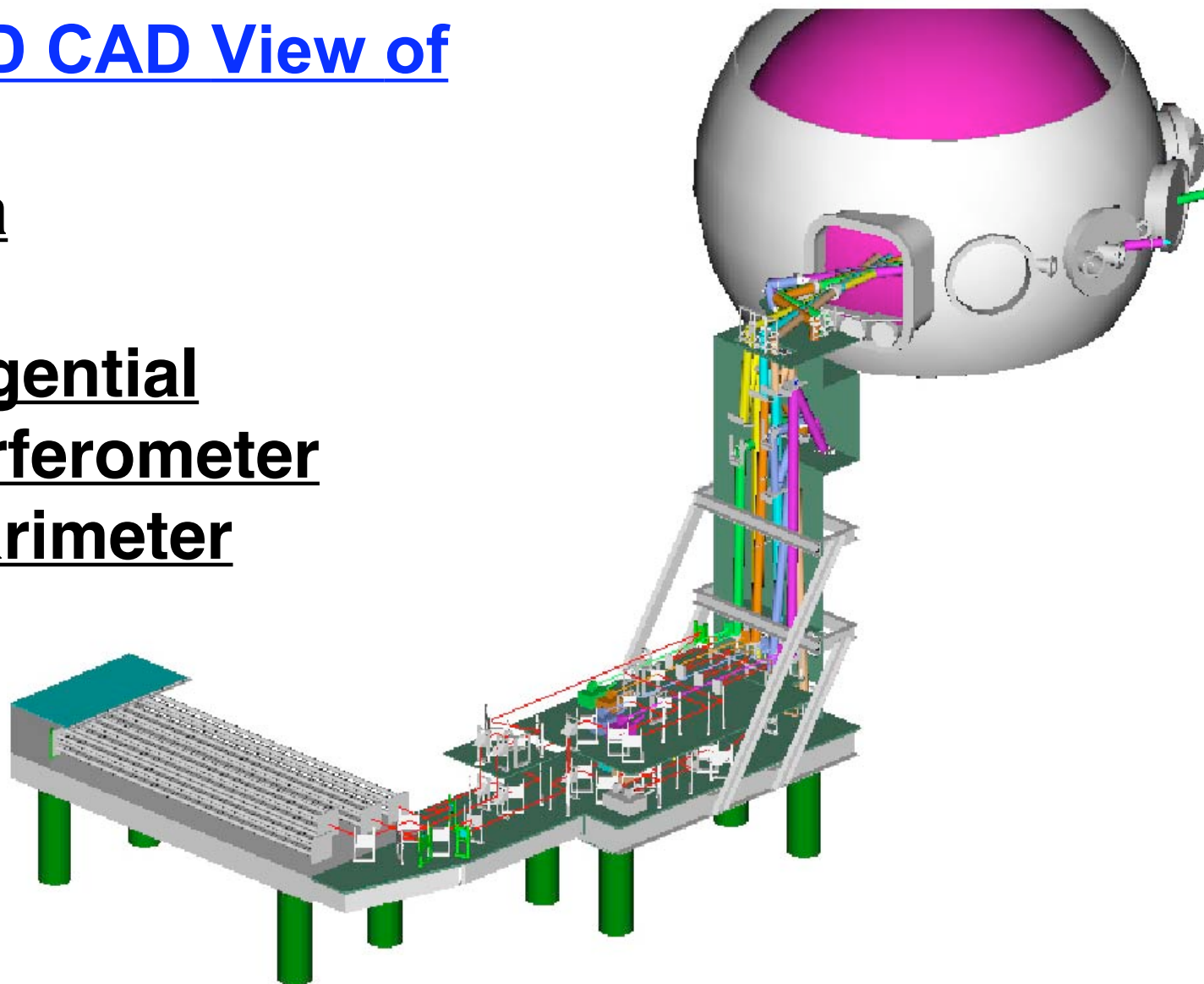
# Abstract

The density fluctuation level measured by the Far Infra Red Tangential Interferometry/Polarimetry (FIReTIP) system on National Spherical Torus Experiment (NSTX) is compared with the energy confinement for the study of turbulence transport. In the 2008 campaign, FIReTIP system was operational with 6 channels including a new channel (CH5) at the tangency radius of 132 cm. Since CH5 measures line integrated density over the turbulence dominated region from the pedestal to Scrape-Off-Layer, the density fluctuation level measured by CH5 provides correlated information with the turbulence induced transport of NSTX boundary. The density fluctuation levels are compared with the stored energy from EFIT equilibria for L-mode and H-mode cases. The possible relation to the turbulent diffusion based on the gyrocenter shift will be discussed.

\* This work is supported by U.S. Department of Energy Grant Nos. DE-FG03-99ER54518, DE-AC02-76CH03073 and DE-AC05-00OR22725.



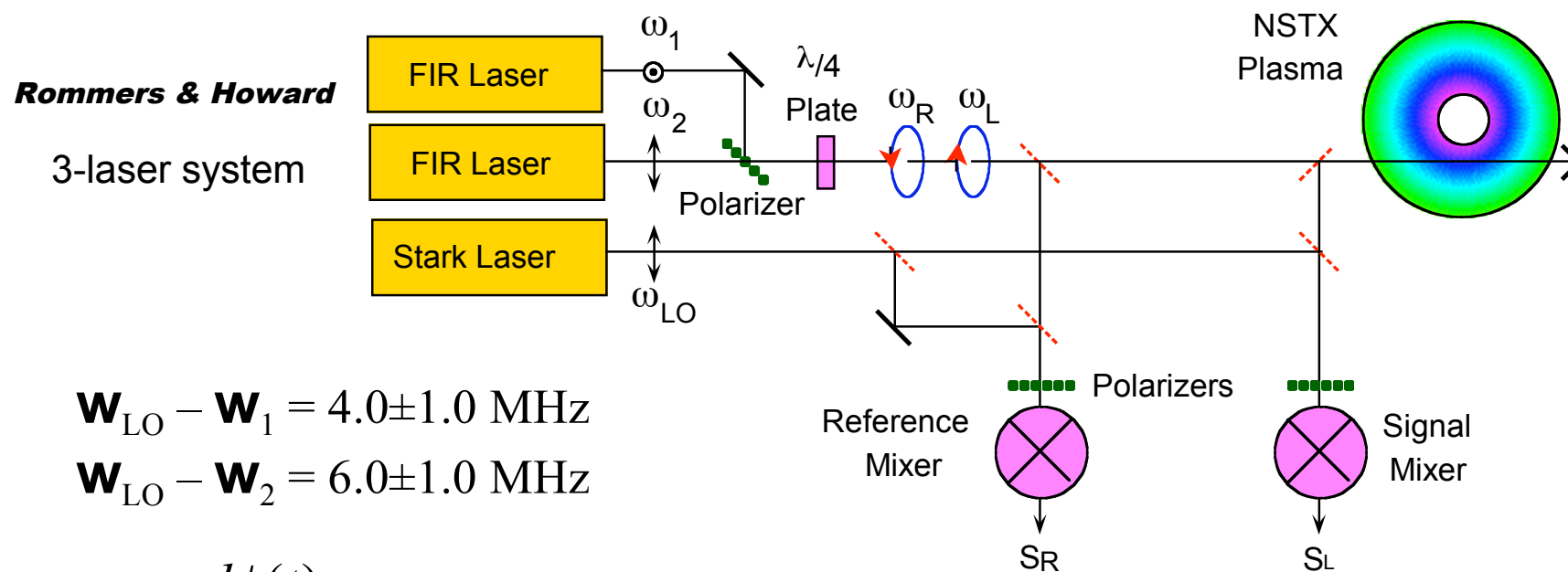
3-D CAD View of  
Far  
Infra  
Red  
Tangential  
Interferometer  
Polarimeter



# Principle of FReTIP system on NSTX

$$\phi(x) = 2.8 \times 10^{-15} \lambda \int_0^x n(x') dx'$$

$$\Psi(x) = 2.6 \times 10^{-13} \lambda^2 \int_0^x n(x') B_T(x') dx'$$



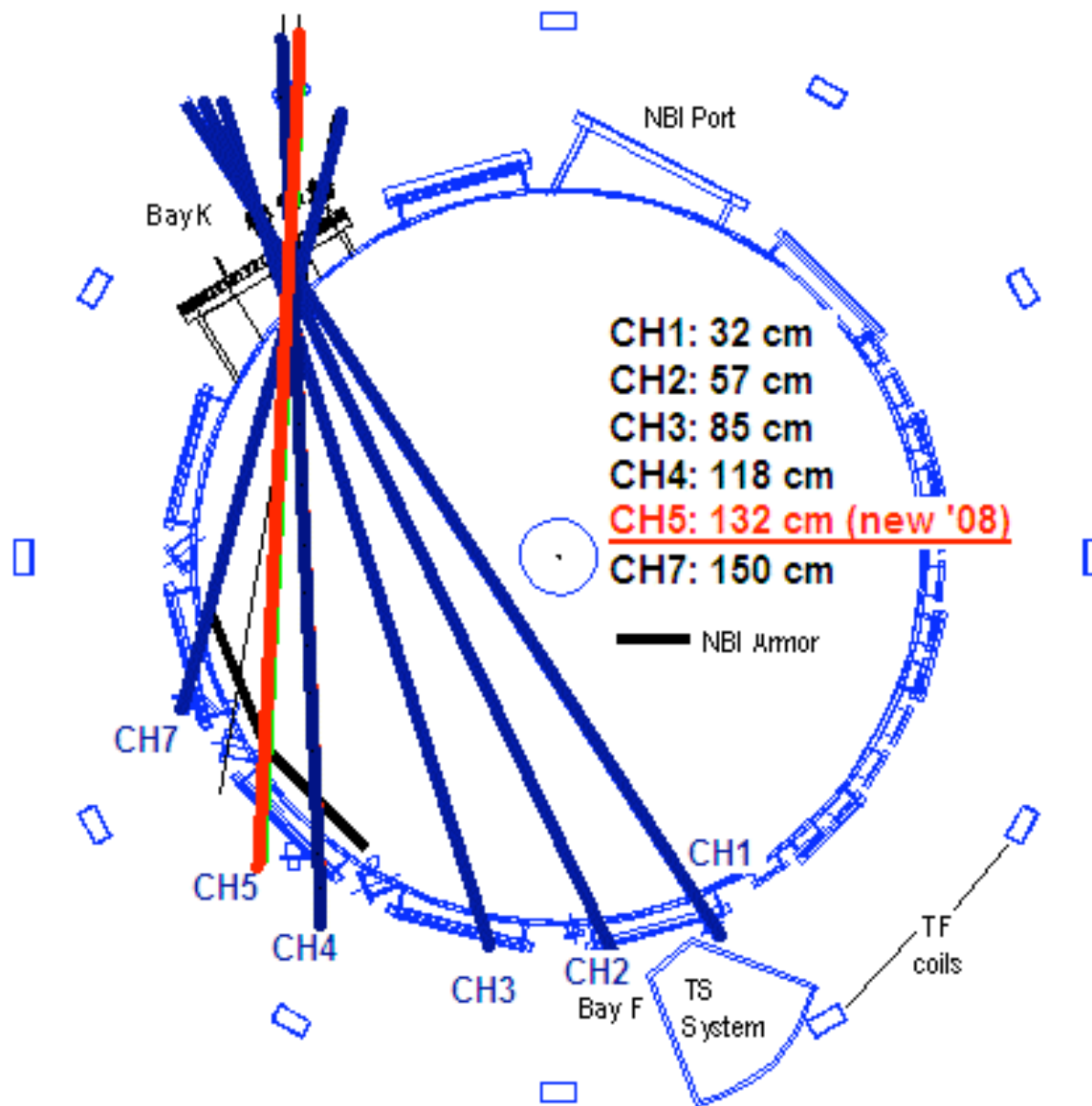
$$\mathbf{W}_{LO} - \mathbf{W}_1 = 4.0 \pm 1.0 \text{ MHz}$$

$$\mathbf{W}_{LO} - \mathbf{W}_2 = 6.0 \pm 1.0 \text{ MHz}$$

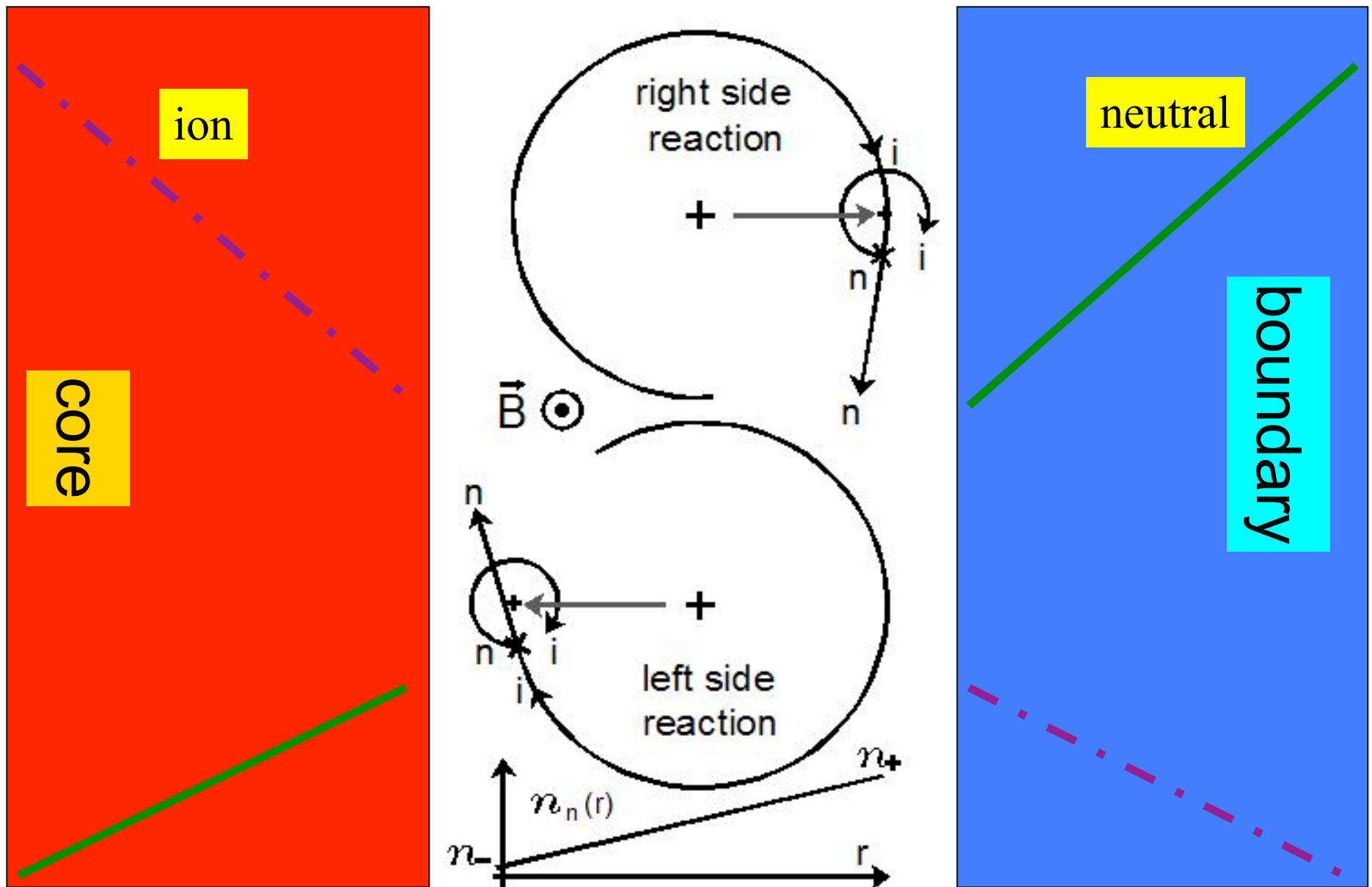
$$\frac{d\phi(t)}{dt} \ll \omega_{if}$$

[K.C. Lee *et.al.*, IEEE Trans. on Plasma **32**,1721(2004)]

# FIReTIP Operated with 6 Channels (2008)



# Gyrocenter shift due to charge exchange



# Gyrocenter shift calculation by fluid picture

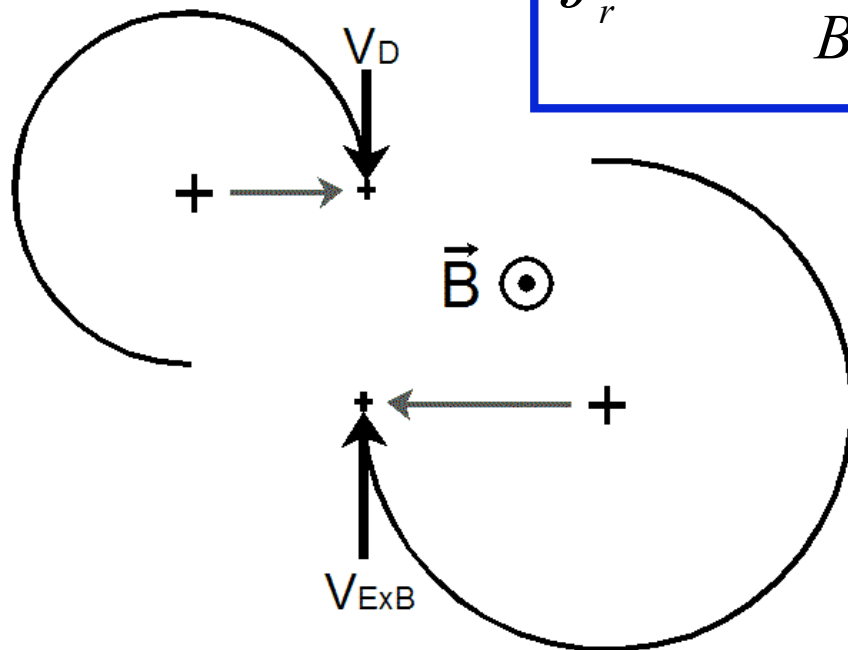
From a fluid equation of motion ;  $J \times B = n_i R_{av} S_i^m$

$$v_{av} = \frac{\oint \sigma v_i n_n(x) d\theta}{\oint \sigma v_i n_n(x) d\theta} = \frac{1}{2} r_L v_{\perp} \frac{1}{n_n} \frac{\partial n_n}{\partial r}$$

$S_i^m = m_i v_{av}$

momentum sink by charge  
exchange

$$J_r^{GCS} = \frac{m_i n_i n_n}{B^2} \langle \sigma v_i \rangle \left( E - \frac{1}{q_i n_i} \frac{\partial p_i}{\partial r} + \frac{T_i}{q_i n_n} \frac{\partial n_n}{\partial r} \right)$$



$$v_{E \times B} = \frac{E}{B}$$

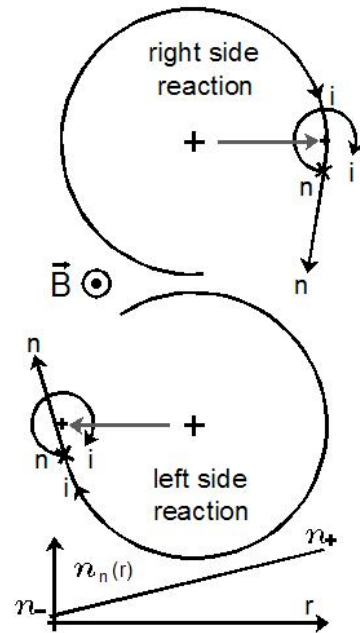
$$v_D = - \frac{1}{q_i B n_i} \frac{\partial p_i}{\partial r}$$

other contributions of  $v_{av}$

**(ExB and diamagnetic drifts)**

**ExB drift is in opposite direction  
=> return current ( $E_r$  saturation)**

# Turbulence Diffusion and H-mode Transition in Conjunction with Gyro-Center Shift



$$J_r^{GCS} = en_i \frac{r_{Li}}{\lambda_{i-n}} \left( \frac{E}{B} - \frac{1}{eB} \frac{\nabla P_i}{n_i} + \frac{kT_i}{eB} \frac{\nabla n_n}{n_n} \right)$$

Gyro-Center Shift

Turbulence Induced Diffusion

$$D = \frac{2}{\pi} \eta^2 \frac{kT_e}{eB} \quad (\eta \equiv \frac{\tilde{n}}{n})$$

Submitted PPCF 2008

E<sub>r</sub> Formation  
PoP 2006

Arc Discharge  
PRL 2007

LH Transition on NSTX  
Invited Talk APS 2006

Reynolds Number of  
Ion-Neutral Collision

$$Re = \frac{eB}{kT_i} \lambda_{i-n} \left( \frac{E}{B} - \frac{1}{eB} \frac{\nabla P_i}{n_i} + \frac{kT_i}{eB} \frac{\nabla n_n}{n_n} \right)$$

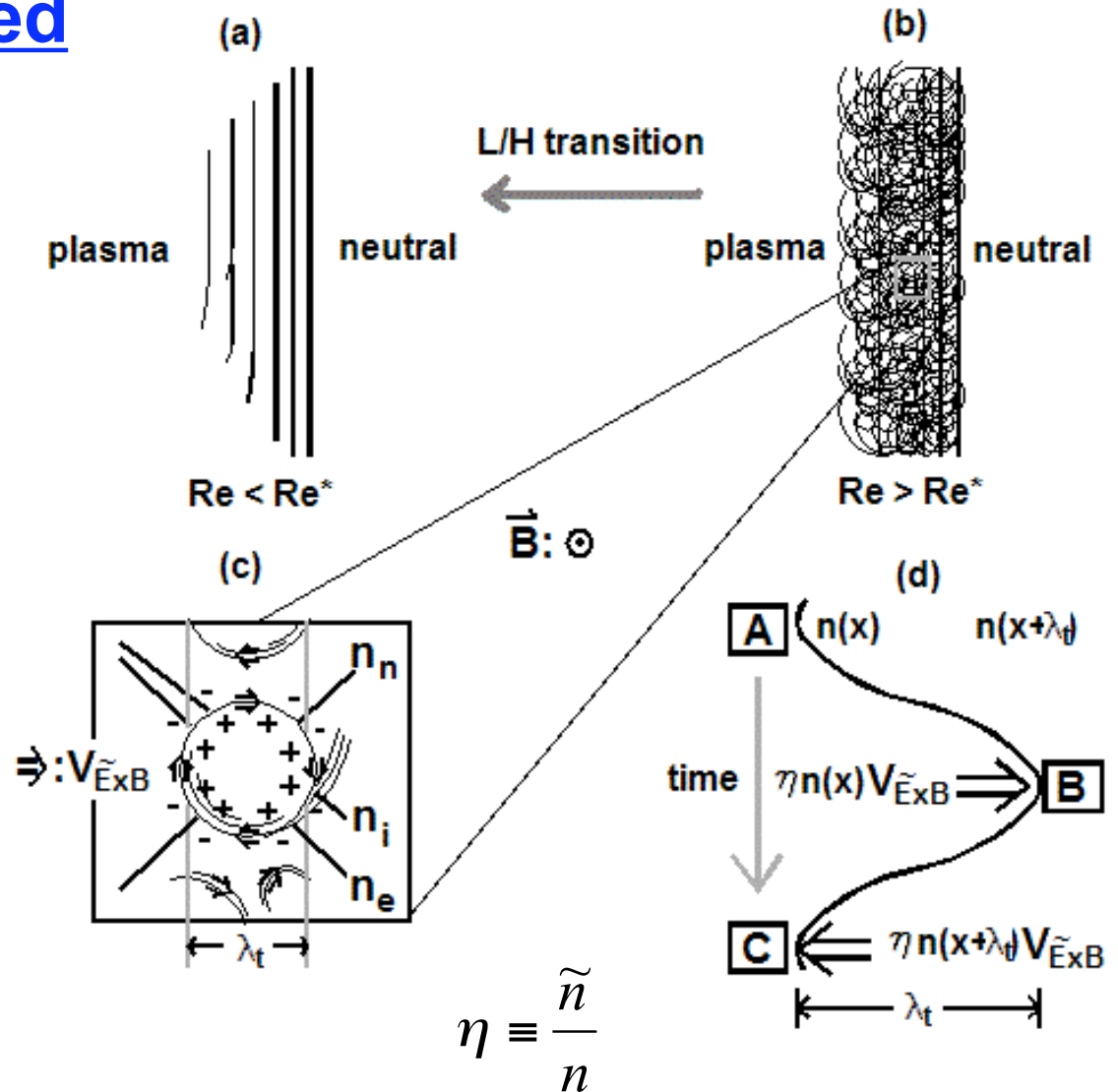
# Turbulence Induced Diffusion

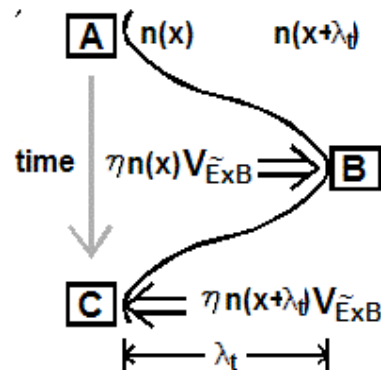
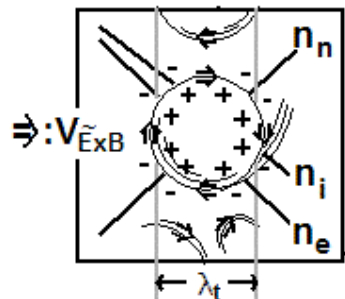
$$\Gamma \approx \partial n \cdot \tilde{v}$$

$$\eta \lambda_t \nabla n \quad V_{\tilde{E} \times B} = \frac{\tilde{E}}{B}$$

$$\frac{e \tilde{E} \lambda_t}{2} \approx \eta k T_e$$

$$D = \frac{2}{\pi} \eta^2 \frac{k T_e}{e B}$$





## Turbulence induced diffusion of particles and charge

$$\eta \equiv \frac{\tilde{n}}{n}, \quad n' \equiv \frac{\partial n}{\partial x} < 0$$

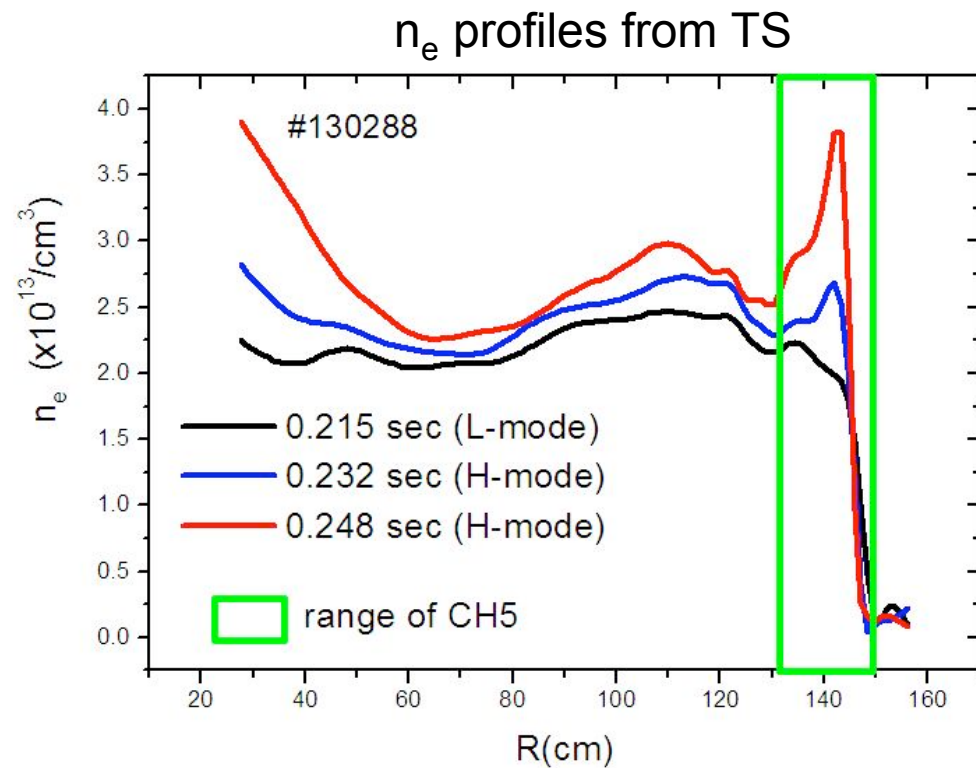
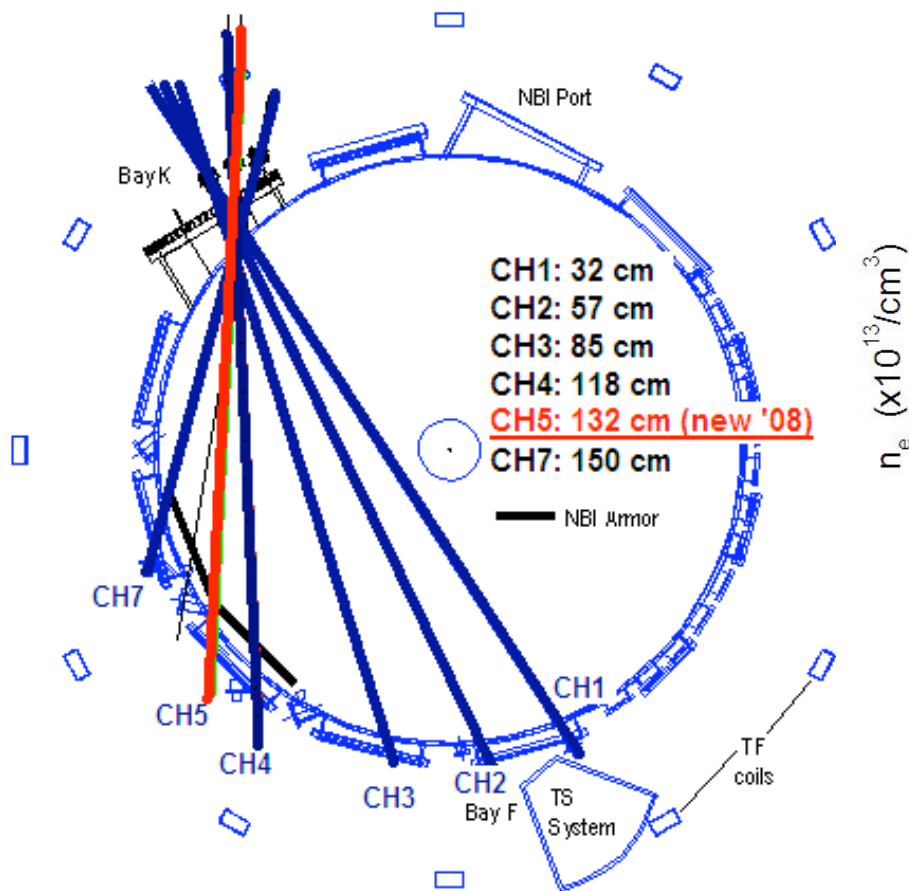
|     | $x$                                                                                                                                                                                                 | $x + \lambda_t$                                                                                                                                                                                                                                           |
|-----|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| [A] | $n_{i,e}(x) \equiv n_{i,e}$                                                                                                                                                                         | $n_{i,e}(x + \lambda_t) = n_{i,e} + \lambda_t n'_{i,e}$                                                                                                                                                                                                   |
| [B] | $n_{i,e} - \eta n_{i,e}$                                                                                                                                                                            | $n_{i,e} + \lambda_t n'_{i,e} + \eta n_{i,e}$                                                                                                                                                                                                             |
| [C] | $n_{i,e} - \cancel{\eta n_{i,e}} + \cancel{\eta n_{i,e}} + \eta \lambda_t n'_{i,e} + \cancel{\eta^2 n_{i,e}}$<br>$\approx n_{i,e} + \eta \lambda_t n'_{i,e} = n_{i,e}(x) + \eta \lambda_t n'_{i,e}$ | $n_{i,e} + \lambda_t n'_{i,e} + \cancel{\eta n_{i,e}} - \cancel{\eta n_{i,e}} - \eta \lambda_t n'_{i,e} - \cancel{\eta^2 n_{i,e}}$<br>$\approx n_{i,e} + \lambda_t n'_{i,e} - \eta \lambda_t n'_{i,e} = n_{i,e}(x + \lambda_t) - \eta \lambda_t n'_{i,e}$ |

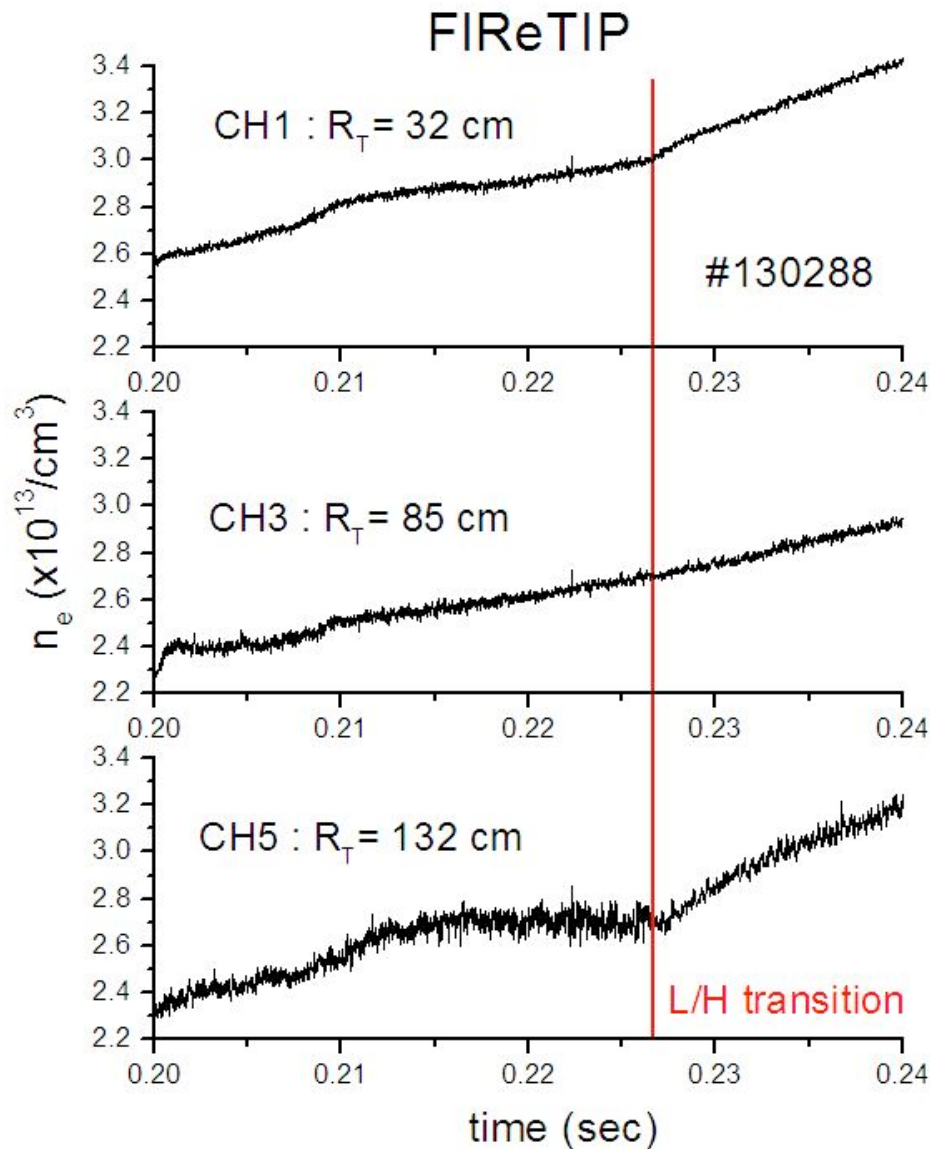
- ▶ net movement of one cycle is  $\eta \lambda_t \nabla n$  : same result from L-R-L and R-L-R cycles
- ▶ turbulence induced charge diffusion can be calculated same way as density:  $\eta \lambda_t \nabla \rho$
- ▶ diffusion takes place from high density region to low density region

▶ ion and electron move toward boundary => **diffusion**

▶ charge ( $\rho$ ) moves toward core => **return current** => **saturation condition**

# NSTX FIRETIP CH5 provides $dn_e$ data of density fluctuation dominant region





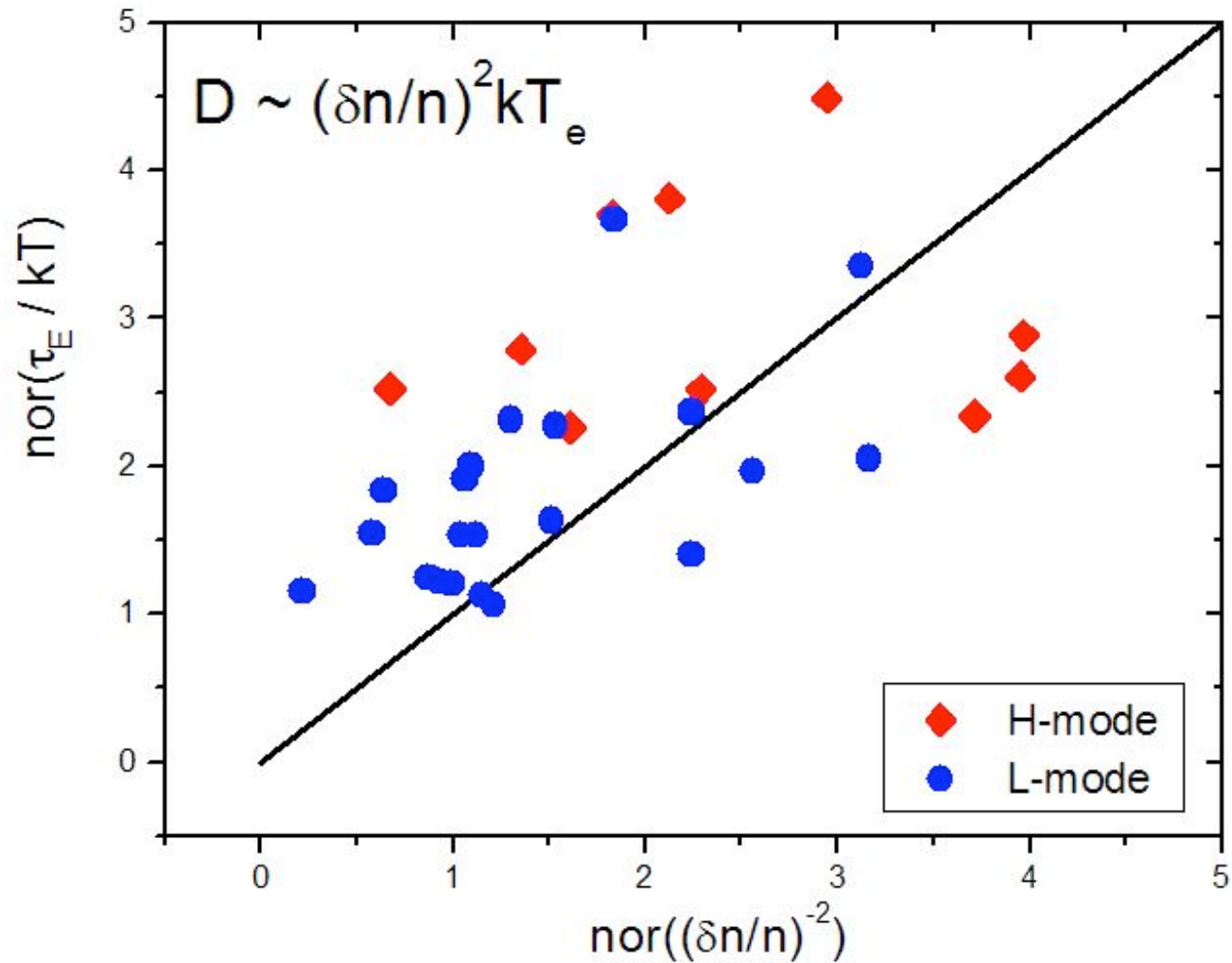
$$D = \frac{2}{\pi} \eta^2 \frac{kT_e}{eB} \quad \eta \equiv \frac{\tilde{n}}{n}$$

- ▶ FIReTIP CH5 shows high  $\eta$
- ▶ energy confinement time  $t_E$
- $t_E \sim 1/D$
- ▶  $t_E$  calculated by EFIT
- ▶  $T_e$  and  $n_e$  from Thomson Scattering

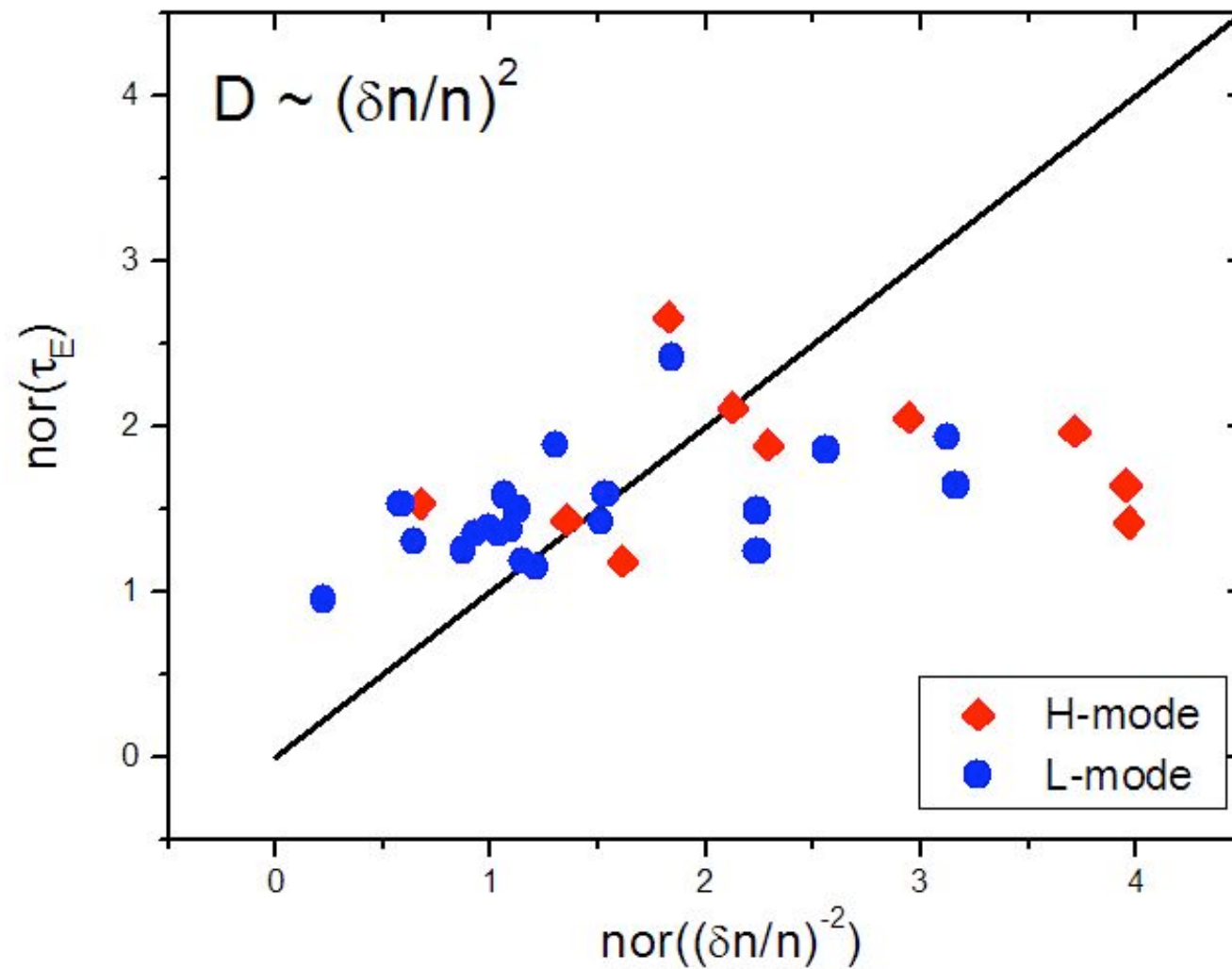
## Comparing confinement time with $dn_e$

- ▶ 16 shots are analyzed.
- ▶ ~46 points are selected within constant NB heating period.  
=> density increasing period :  $\eta$  decreasing within relatively short time. ( $T_e$  is evolving )
- ▶ first point of a shot => fiducial point : other points of same shot are normalized by the fiducial point.  
=> to remove shot to shot difference such as wall-conditioning. (no  $B_T$  effect)
- ▶ including L/H transitions, excluding MHD activities

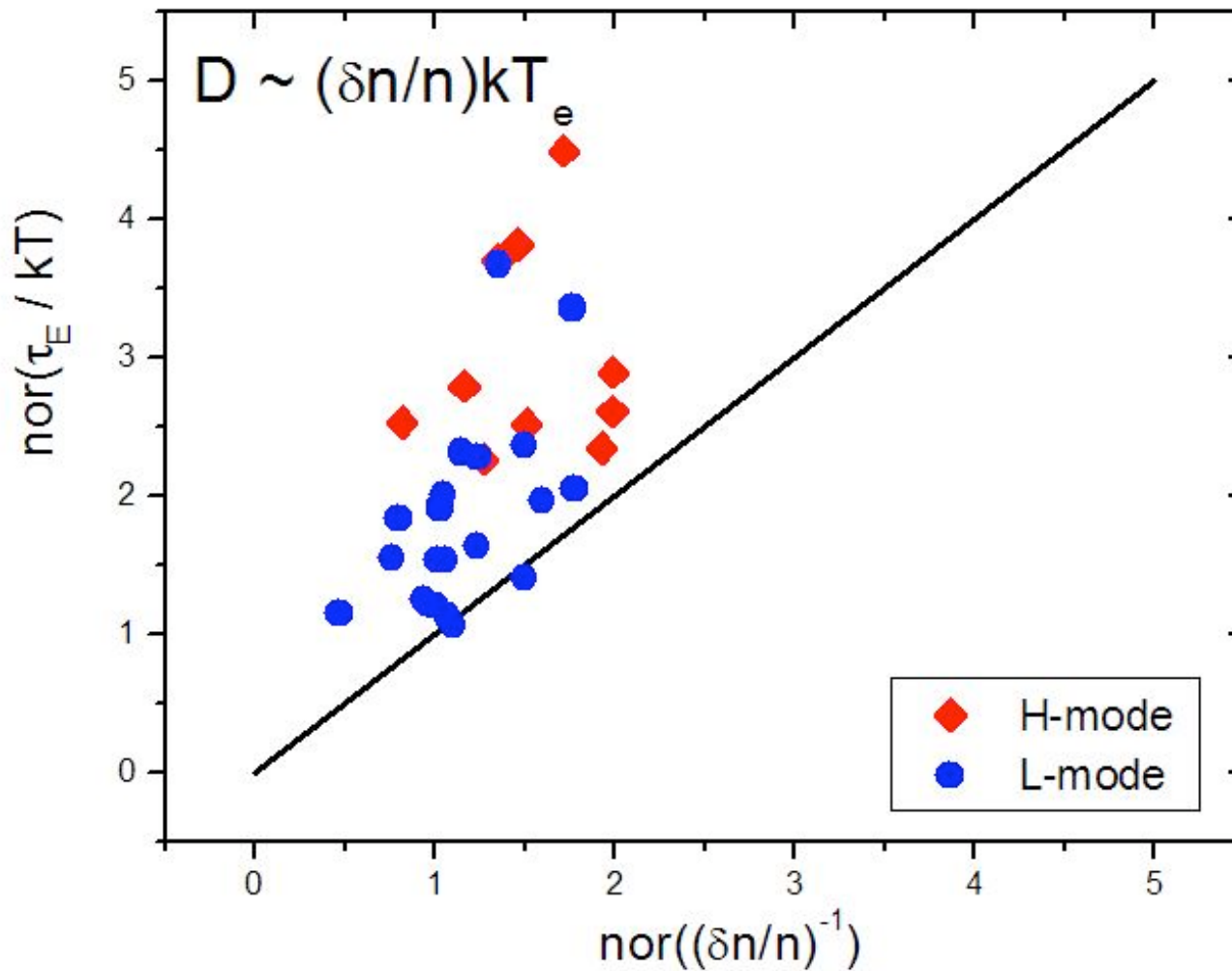
## Comparing $\tau_E$ with $\eta^2$ : including $T_e$ effect



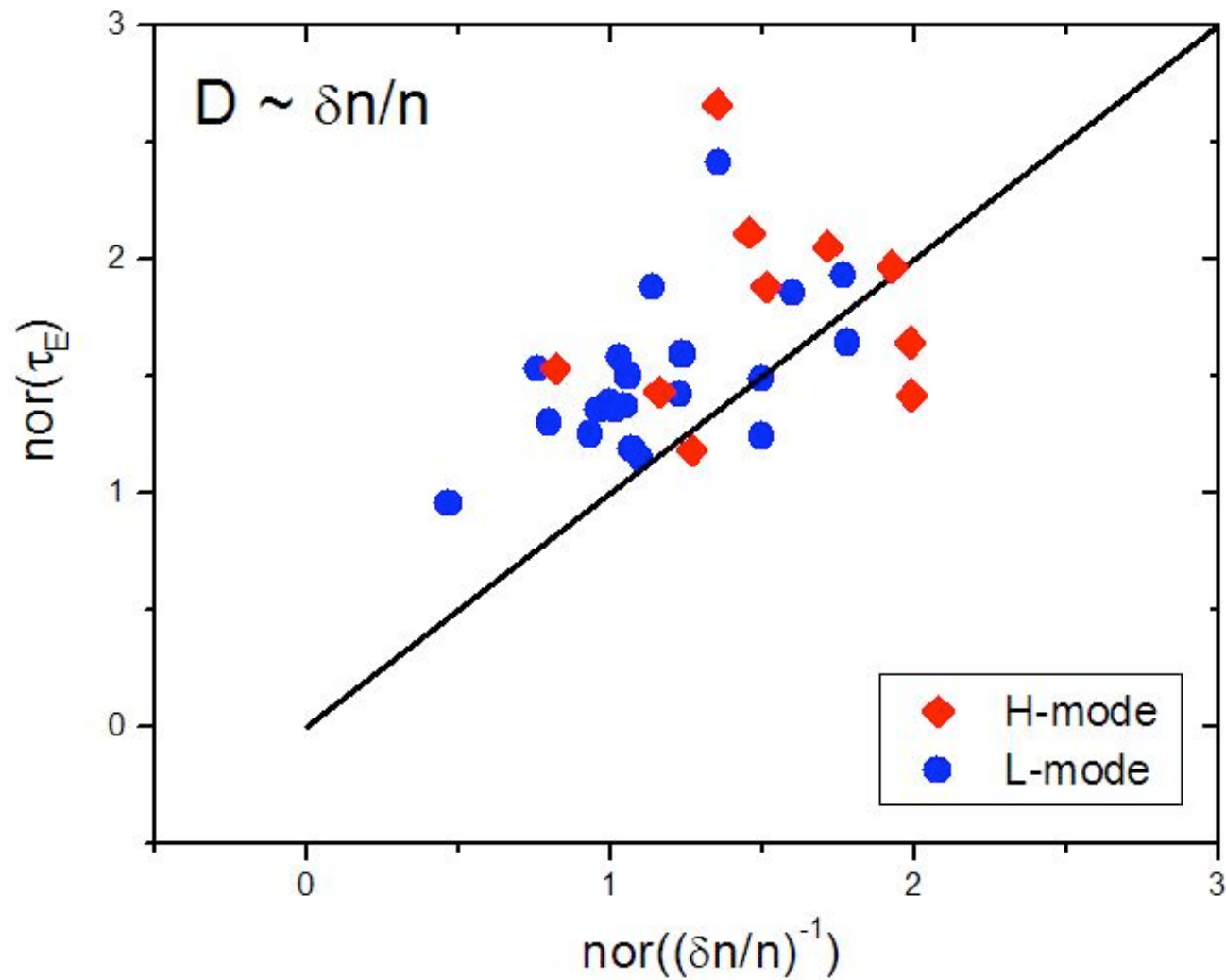
## Comparing $t_E$ with $\eta^2$ : no $T_e$ effect



## Comparing $t_E$ with $\eta$ : including $T_e$ effect



## Comparing $t_E$ with $\eta$ : no $T_e$ effect



# Summary

- FReTIP measured density fluctuations with CH5 ( $R_T=132$  cm) which is new in 2008 covering highest density fluctuation region

- gyrocenter shift theory is expanded to the diffusion coefficient;

$$D = \frac{2}{\pi} \eta^2 \frac{kT_e}{eB}$$

- comparison of confinement time (EFIT) with density fluctuation (FReTIP CH5) of NSTX showed better linearity for  $t_E \propto 1/(\eta^2 kT_e)$  than  $t_E \propto 1/(\eta^2)$  and  $t_E \propto 1/(\eta kT_e) \Rightarrow D \propto \eta^2 (kT_e/eB)$

- $t_E \propto 1/(\eta^2 kT_e)$  case indicates clearer separation of H-mode points from L-mode points than  $t_E \propto 1/\eta$

- explanation of weak correlation  $t_E \propto 1/(\eta^2)$  in former study [Nuclear Fusion, 46 848 (2006)]

- 2009 campaign will provide more data from CH5