

Investigations of pedestal turbulence and ELM bursts in NSTX H-mode plasmas

David R. Smith¹

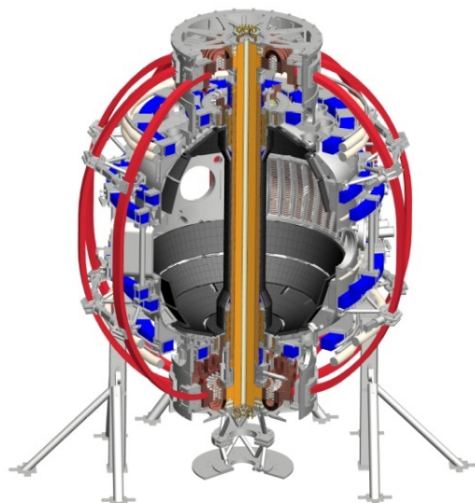
W. Wan², R. Fonck¹, G. McKee¹, S. Parker², A. Diallo³, S. Kaye³,
W. Guttenfelder³, and the NSTX Research Team

¹ University of Wisconsin-Madison

² University of Colorado-Boulder

³ Princeton Plasma Physics Lab

**55th APS-DPP Meeting
Denver, CO
November 11-15, 2013**

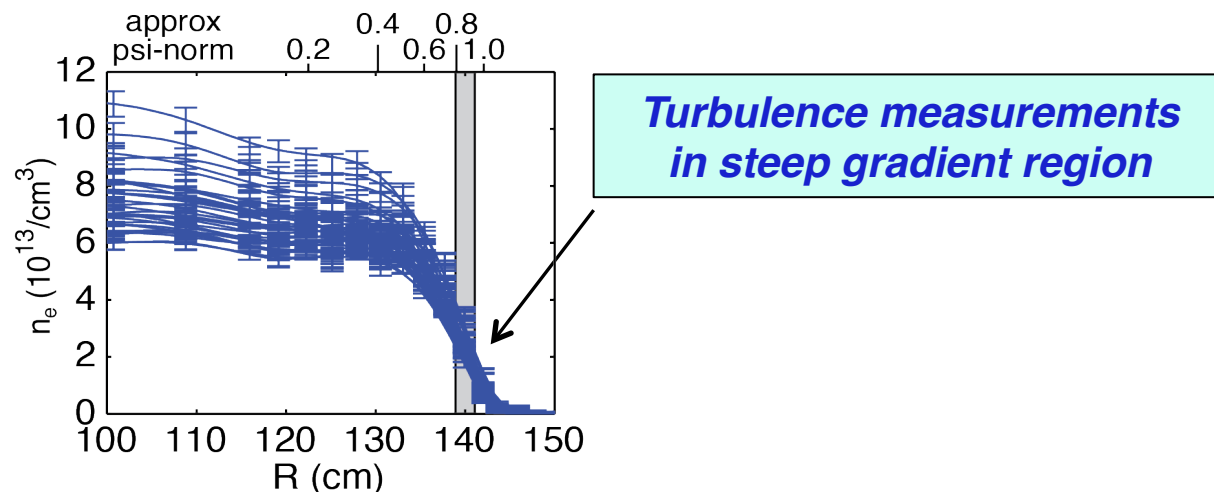


Coll of Wm & Mary
 Columbia U
 CompX
 General Atomics
 FIU
 INL
 Johns Hopkins U
 LANL
 LLNL
 Lodestar
 MIT
 Lehigh U
 Nova Photonics
 ORNL
 PPPL
 Princeton U
 Purdue U
 SNL
 Think Tank, Inc.
 UC Davis
 UC Irvine
 UCLA
 UCSD
 U Colorado
 U Illinois
 U Maryland
 U Rochester
 U Tennessee
 U Tulsa
 U Washington
 U Wisconsin
 X Science LLC

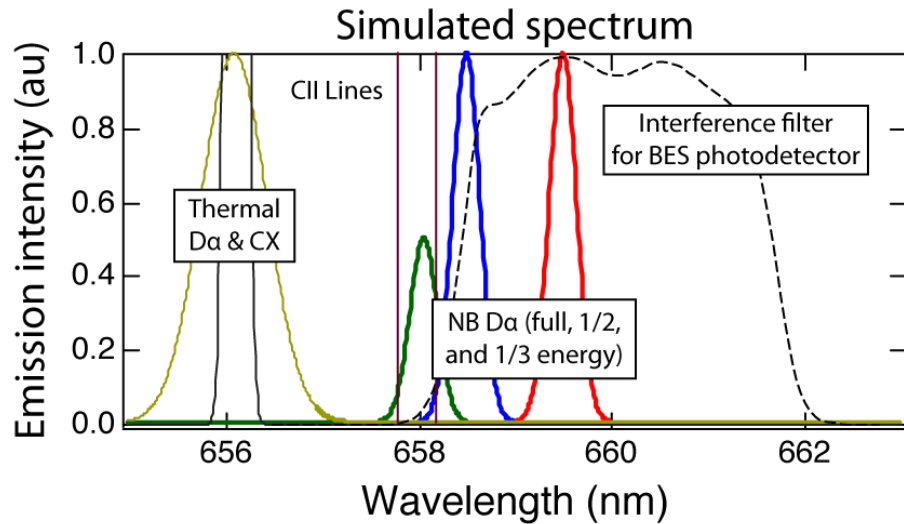
Culham Sci Ctr
 York U
 Chubu U
 Fukui U
 Hiroshima U
 Hyogo U
 Kyoto U
 Kyushu U
 Kyushu Tokai U
 NIFS
 Niigata U
 U Tokyo
 JAEA
 Inst for Nucl Res, Kiev
 Ioffe Inst
 TRINITI
 Chonbuk Natl U
 NFRI
 KAIST
 POSTECH
 Seoul Natl U
 ASIPP
 CIEMAT
 FOM Inst DIFFER
 ENEA, Frascati
 CEA, Cadarache
 IPP, Jülich
 IPP, Garching
 ASCR, Czech Rep

The pedestal sets boundary conditions for the core and ejects structures that damage plasma-facing components

- Projections for ITER depend on accurate pedestal models
 - **ST parameter regime** (large ρ^* , high β , shaping, beam-driven flow) is a challenging environment for pedestal simulations
- **Pedestal turbulence measurements** in NSTX H-mode plasmas during ELM-free, MHD quiescent periods
 - Identify **parametric dependencies** between turbulence quantities and transport-relevant plasma parameters
 - Compare to turbulence models → scalings point to TEM turbulence
 - Compare to pedestal turbulence **simulations**



Beam emission spectroscopy (BES) measures Doppler-shifted D_α emission from neutral beam particles

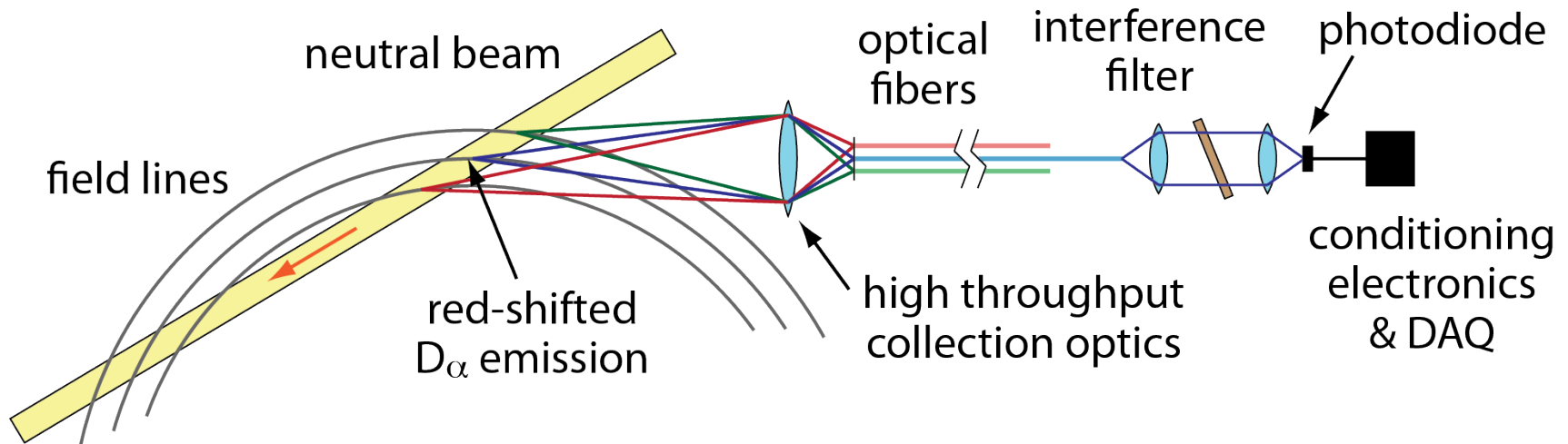


$$\frac{\delta I_{D\alpha}}{I_{D\alpha}} = \frac{\delta n}{n} \times C(E_{NB}, n, T_e, Z_{eff})$$

neutral beam D_α emission

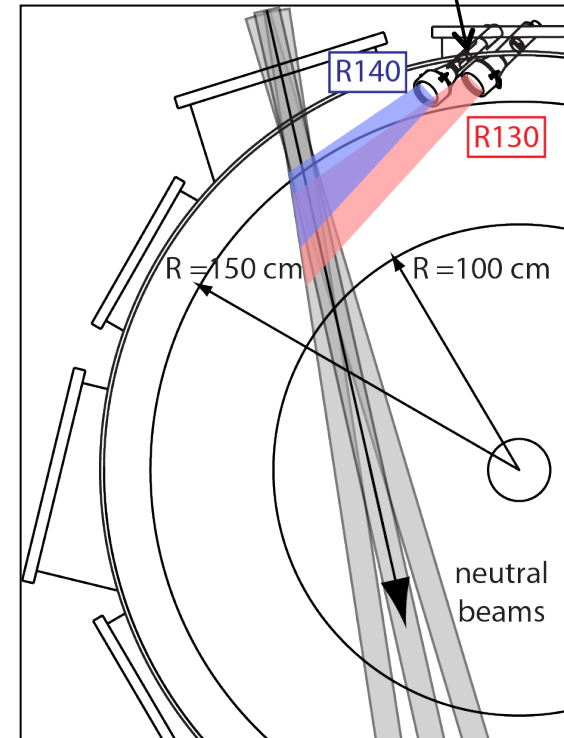
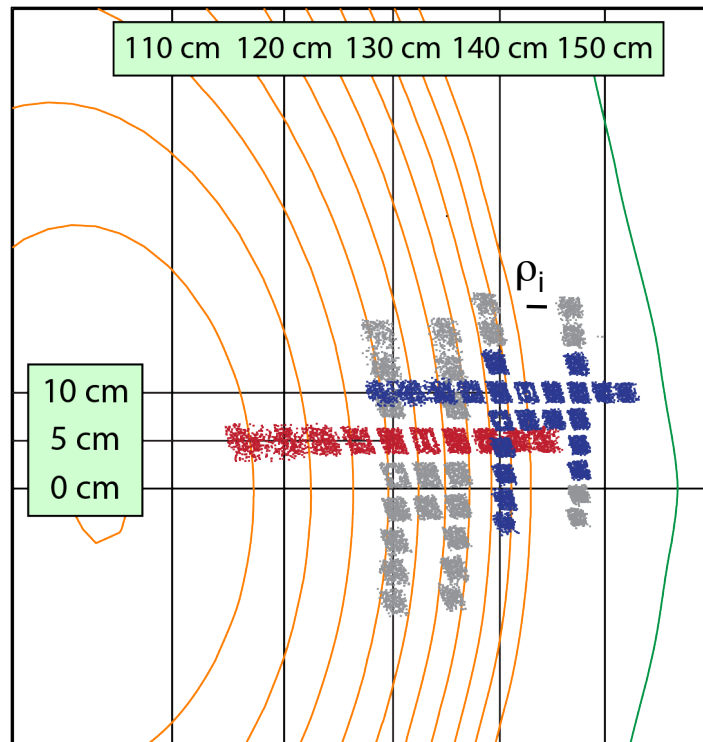
density fluctuation

$C \approx 1/2$



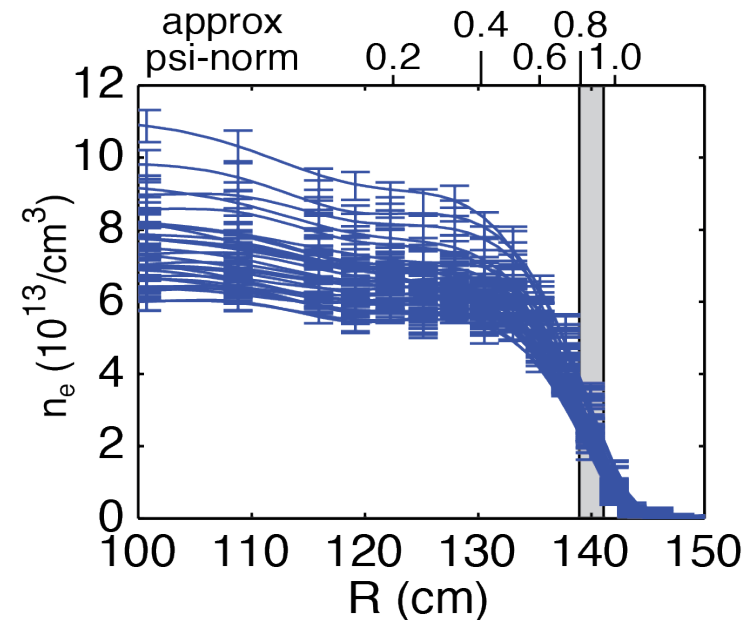
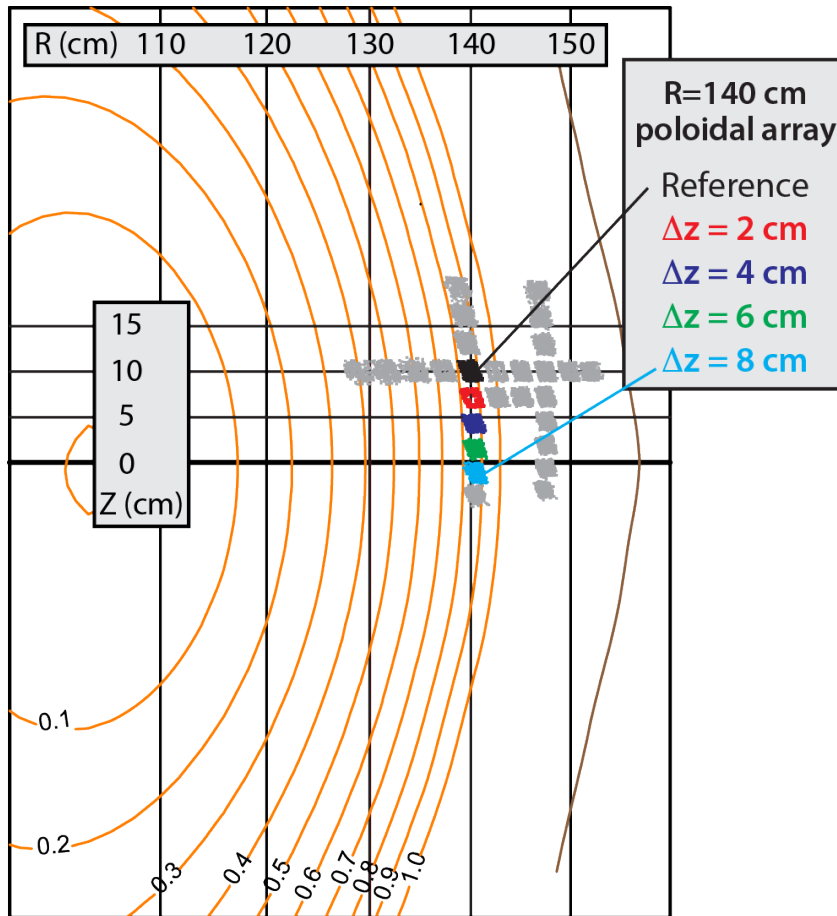
The beam emission spectroscopy (BES) system on NSTX measures fluctuations on the ion gyroscale with $k_{\perp}\rho_i \leq 1.5$

- Radial and poloidal arrays spanning core to SOL
- 32 detection channels
- **2-3 cm spot size and $k_{\perp}\rho_i \leq 1.5$**



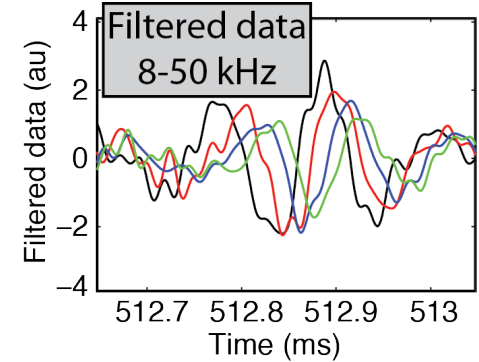
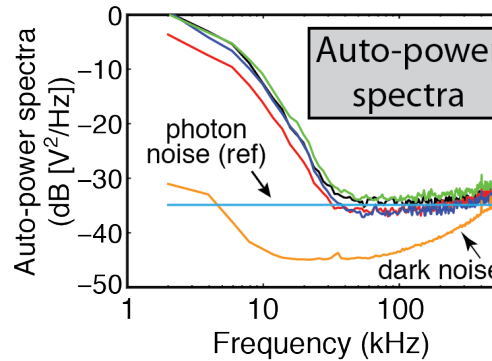
Pedestal turbulence measurements

- ELM-free, MHD quiescent H-mode with Li conditioning
- $\Psi_N \approx 0.8 - 0.95$ in steep gradient region



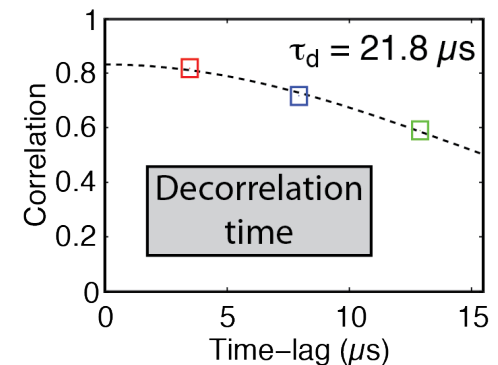
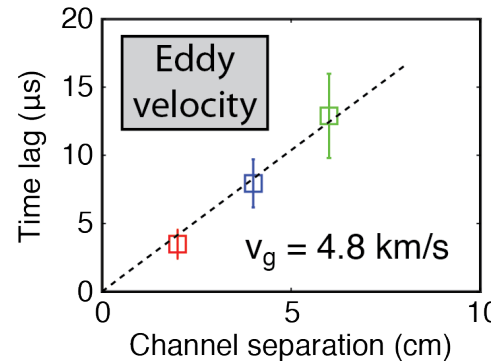
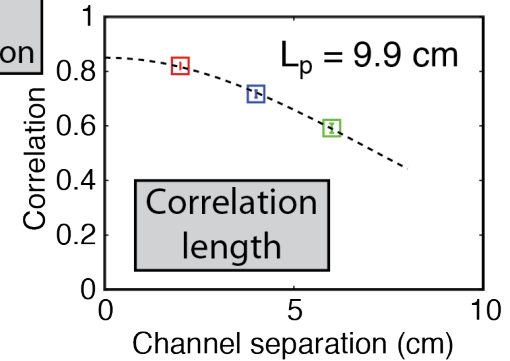
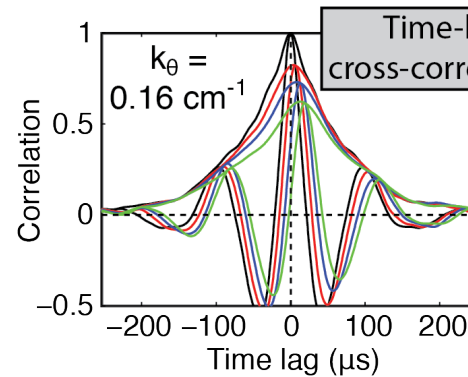
BES can measure poloidal correlation lengths (L_c), poloidal wavenumbers (k_θ), decorrelation times (τ_d), and amplitude ($\tilde{n}/n$)

- Auto-power spectra show plasma turbulence signals above detector noise levels
- Filtered data (8-50 kHz) show eddies moving down BES array

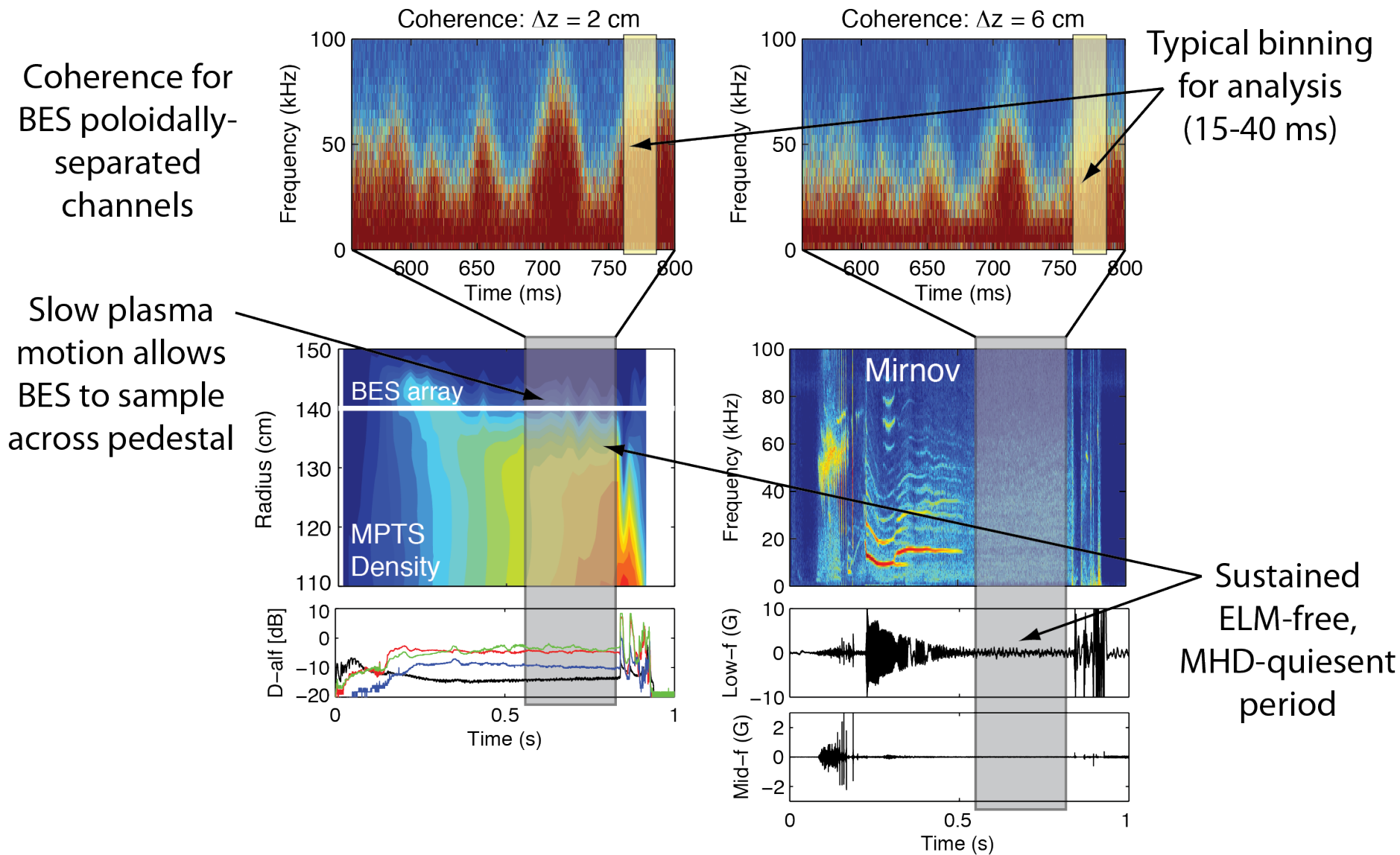


Time-lag cross-correlation gives:

- Correlation length $C(x, \tau=0)$
- Decorrelation time $C_{\max}(\tau)$
- Eddy velocity $\Delta z / \Delta \tau_{\text{lag}}$
- Dominant wavenumber
 - Inferred from auto-correlation and eddy velocity



ELM-free, MHD quiescent periods > 150 ms were identified and partitioned into 15-40 ms bins for turbulence analysis



Populated database with pedestal turbulence measurements and transport-relevant plasma parameters

- Database with 129 observations from 29 discharges

$$B_{T0} = 4.5 \text{ kG}$$

$$I_p = 700\text{-}900 \text{ kA}$$

15-45 ms averaging

- Turbulence quantities are consistent with **drift wave turbulence**

$$L_c/\rho_i \approx 8 - 18$$

$$k_\theta \rho_i \approx 0.07 - 0.31$$

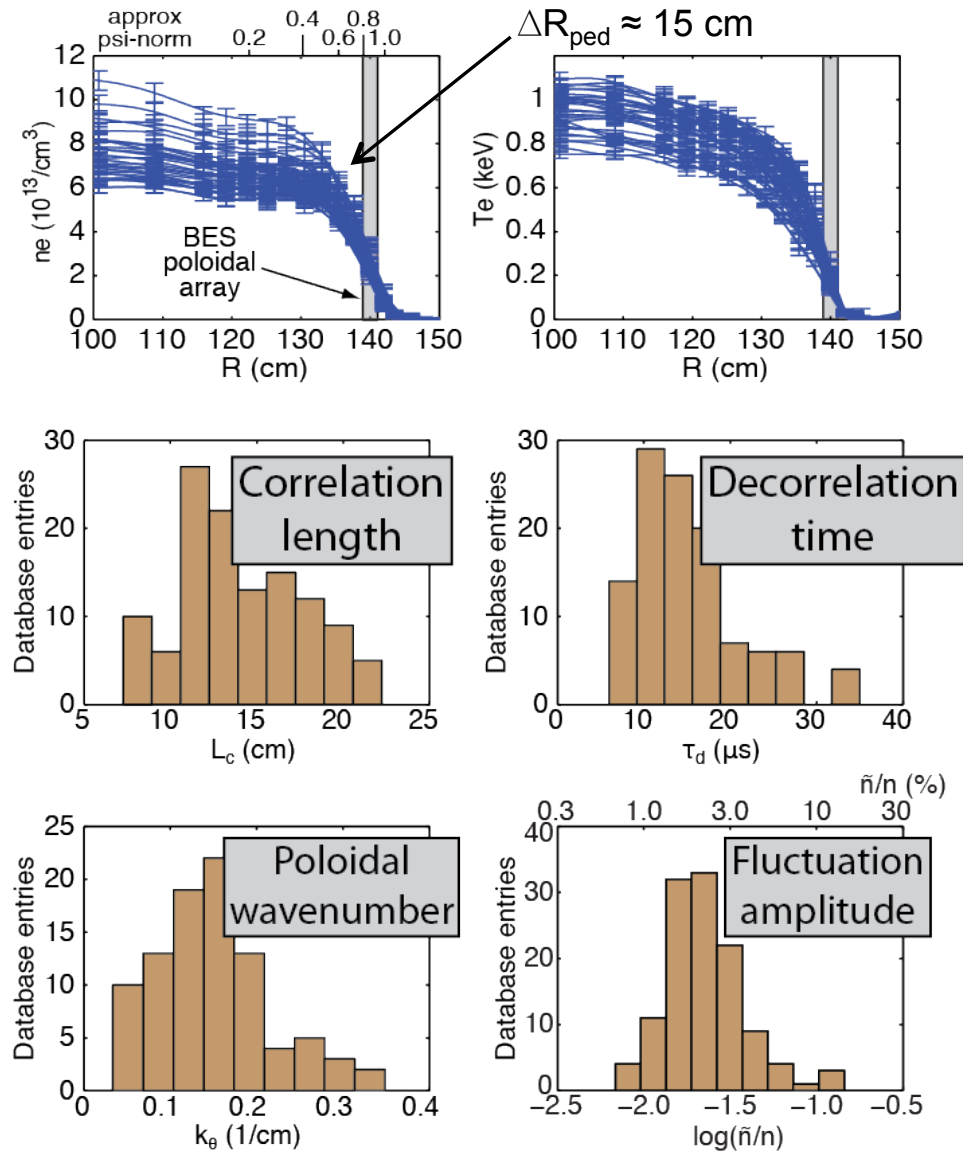
$$\tau_d/(a/c_s) \approx 2.6 - 6.5$$

$$\tau_d \omega_{pi}^* \approx 0.04 - 0.28$$

$$\tilde{n}/n \approx 1\%\text{-}4\%$$

- Transport-relevant parameters

- $n_e, \nabla n_e, 1/L_{ne}, T_e, \nabla T_e, 1/L_{Te}, T_i, \nabla T_i, 1/L_{Ti}, v_t, \nabla v_t, q, \hat{s}, v_e, v_i, \beta, \beta_e, n_{ped}, \Delta R_{ped}, \delta_r^{sep}$
- generally 50%-300% variation



A search algorithm identified many linear regression models among turbulence quantities and plasma parameters

$$\frac{\hat{y} - \bar{y}}{\sigma_y} = \sum \alpha_k \frac{x_k - \bar{x}_k}{\sigma_{xk}}$$

↑ turbulence quantities
 ↑ scaling coefficient
 ↑ plasma parameters

- **Many models exist** in high dimensional x_k space
 - Models are error local minima
- Screen models for good statistics
 - **High statistical significance**
t-statistics $\rightarrow P(H_0: \alpha_k=0) < 5\%$
 - **Low multicollinearity**
Pair-wise corr. $\rightarrow \max(|C_{jk}|) < 0.6$
Var. inflation factor $\rightarrow \max(VIF_k) < 5$
 - **Normally distributed residuals**
 $P(\varepsilon) \rightarrow$ Skew and Ex. Kurt. within 2σ
Studentized residuals $\rightarrow$ no outliers

6 representative models for L_c/ρ_s

Model	α_k coefficients						
R^2	∇n_e	T_e	T_i	$1/L_{Ti}$	∇V_t	ν_e	n_{ped}
0.63	0.28	–	-0.20	-0.29	–	0.31	–
0.63	0.34	–	–	–	-0.37	0.30	–
0.61	0.46	-0.21	–	–	-0.38	–	–
0.60	–	–	–	–	-0.47	0.38	0.24
0.60	–	–	-0.22	-0.35	–	0.40	0.15
0.55	–	-0.24	–	–	-0.55	–	0.36

Should we try to identify a single “best” model?

Not a good idea because...

- Highly subjective
- Each model contains only a few (3-4) plasma parameters

Is there a better method?

Model aggregation is helpful when assessing many potential predictor variables with complex interdependencies

Scalings are **robust** across models, regardless of number or combination of parameters in models

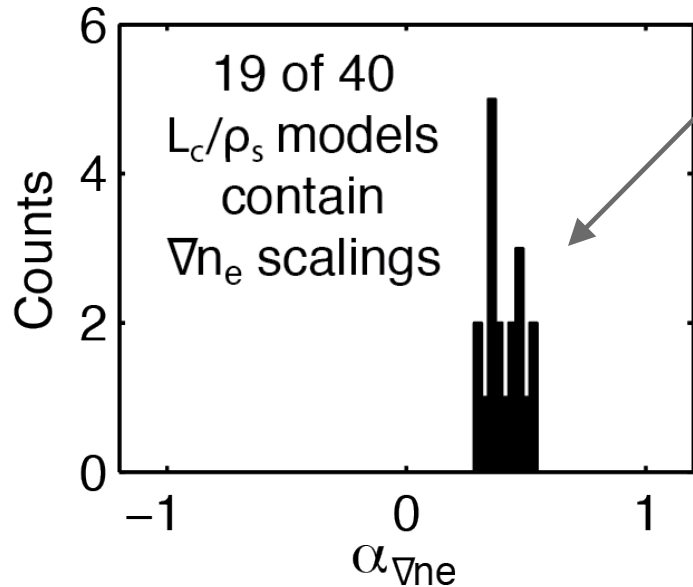


TABLE II: α_k coefficients for a subset of L_c/ρ_s models

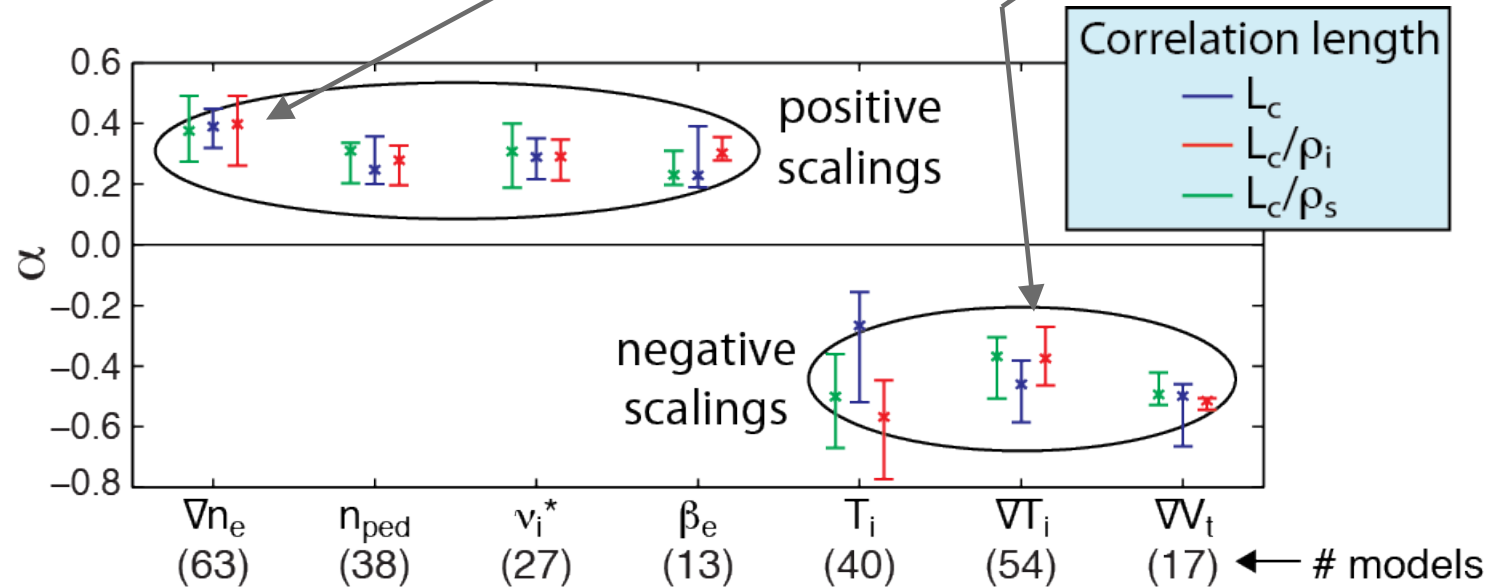
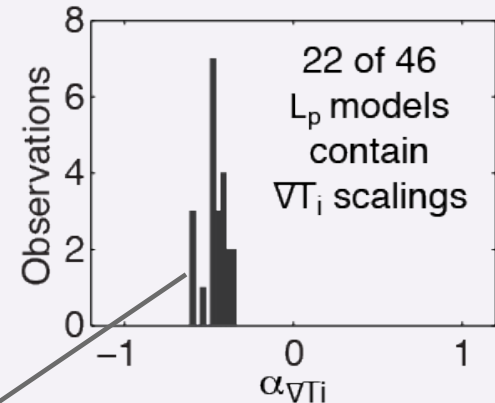
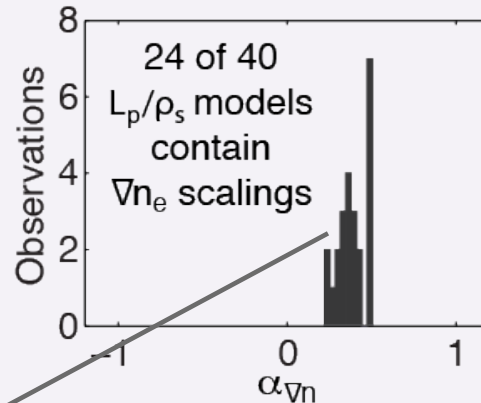
Model R^2	α_k coefficients						n_{ped}
	∇n_e	T_e	T_i	$1/L_{Ti}$	∇V_t	ν_e	
0.63	0.28	—	-0.20	-0.29	—	0.31	—
0.63	0.34	—	—	—	-0.37	0.30	—
0.61	0.46	-0.21	—	—	-0.38	—	—
0.60	—	—	—	—	-0.47	0.38	0.24
0.60	—	—	-0.22	-0.35	—	0.40	0.15
0.55	—	-0.24	—	—	-0.55	—	0.36

Model aggregation **advantages**:

- Identify more parameter scalings than single model
- Scalings are robust across different models

Model aggregation for L_c increases ($\alpha > 0$) with ∇n_e , v_i , β_e , and n_{ped} ; L_c decreases ($\alpha < 0$) with T_i , ∇T_i , and ∇V_t

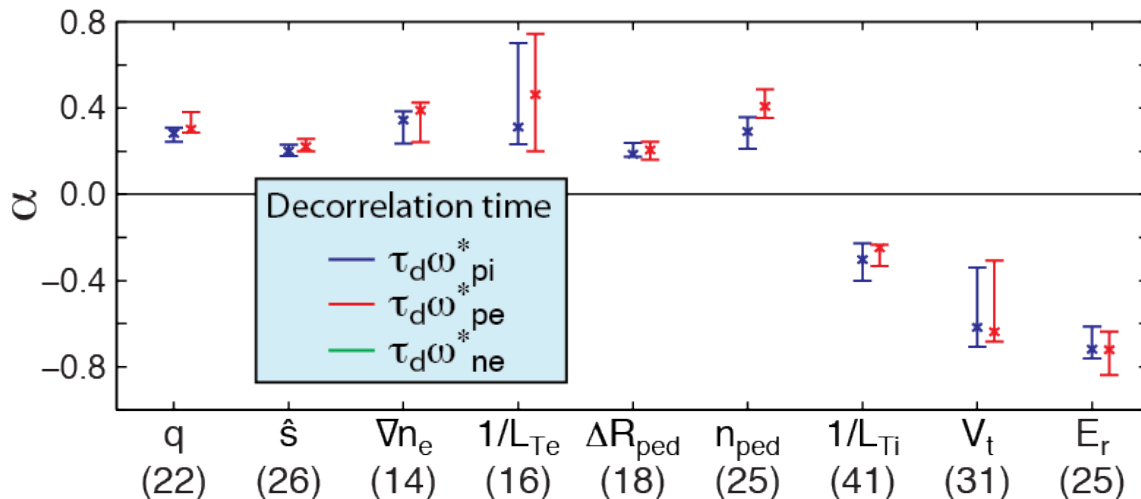
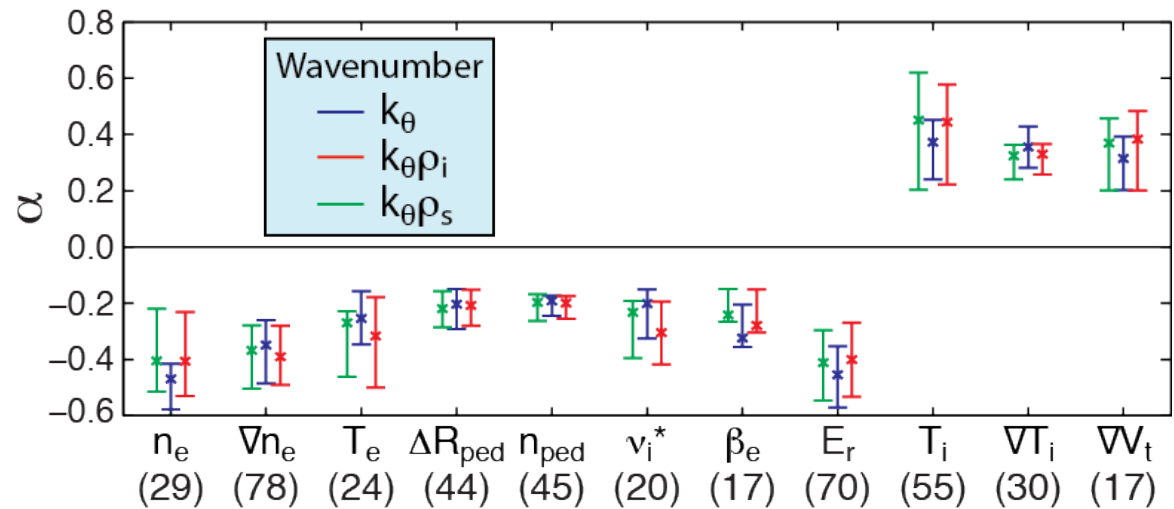
Scalings are robust
across models with
different parameter
combinations



D. Smith et al, PoP 20, 055903 (2013)

Observed scalings can help identify turbulent modes

k_θ scalings are opposite to L_c scalings as expected ($k_\theta \sim 1/L_c$ for broadband turbulence)

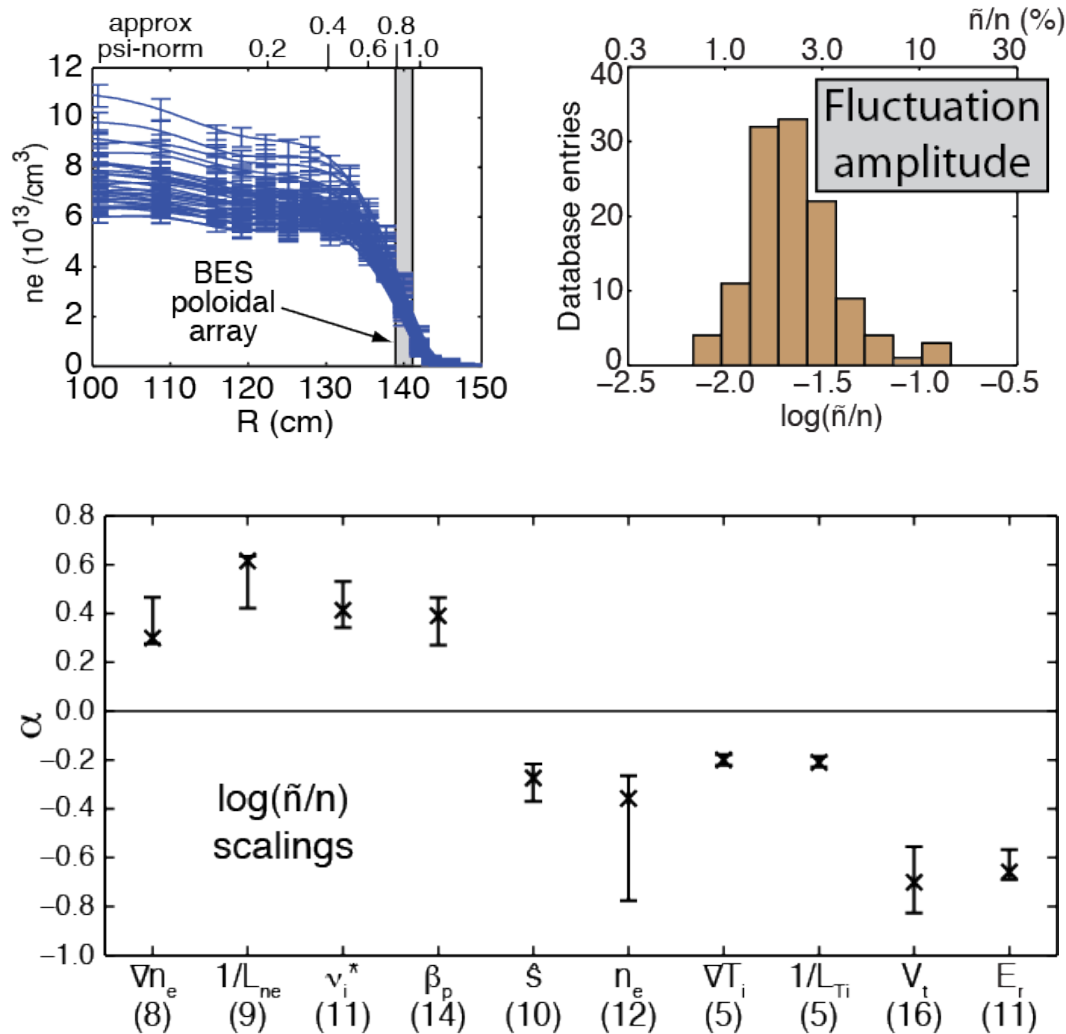


That's a lot of scalings, but what does it all mean?

Turbulence reduction by equilibrium and zonal $E \times B$ flows can be inferred from observed scalings

- ∇v_t scalings for L_c and k_θ consistent with turbulence suppression by **equilibrium $E \times B$ flow shear**
 - L_c decreases and k_θ increases at higher ∇v_t
- E_r scalings for τ_d are **consistent** with turbulence decorrelation by $E \times B$ flow shear
- Collisionality scalings **consistent** with collisionally-damped **zonal flows**
 - L_c increases at higher ν
- n_{ped} and ΔR_{ped} scalings **consistent** with empirical relationship between wider pedestals and larger turbulent structures (Z. Yan et al., PoP 18, 056117 (2011))

Recent $\tilde{n}/n$ scalings bolster previous results



- Most consistent with **TEM**, **KBM**, and **MT** instabilities
- Least consistent with **ITG**
- Positive scalings with
 - ∇n_e and $1/L_{ne}$
 - v_i^* (and other v quantities)
 - β_p
- Negative scalings with
 - ∇T_i and $1/L_{Ti}$
 - $\hat{s}$
 - E_r and V_t
- Scalings consistent with equilibrium and zonal ExB turbulence suppression.
- Scalings consistent with larger $\tilde{n}/n$ at edge.

Observed scalings point to TEM, KBM, or microtearing instabilities

Transport models (crude, but useful)

Random walk

$$D, \chi \approx \frac{L_r^2}{\tau_d} \approx \frac{L_p^2}{\tau_d}$$

Quasi-linear

$$D, \chi \approx \left(\frac{\gamma_l}{k_\theta^2} \right)_{\max \gamma}$$

Nonlinear mixing

$$D, \chi \approx \sum k_\theta |\Phi(k_\theta)|^2$$

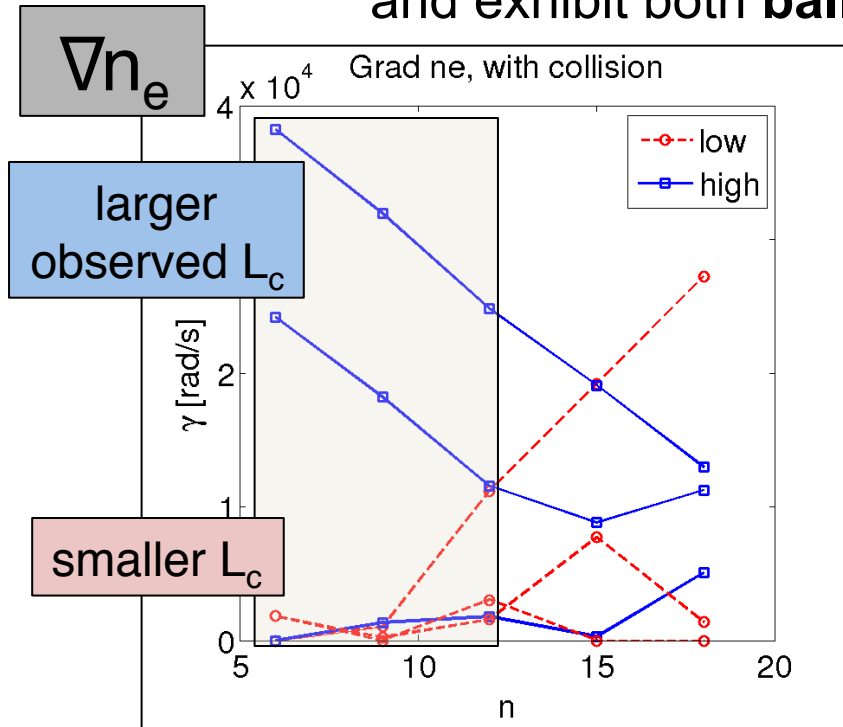
with $|\Phi(k_\theta)|^2 \propto k_\theta^{-\alpha}$ and $\alpha \approx 2 - 4$

- Microturbulence instabilities

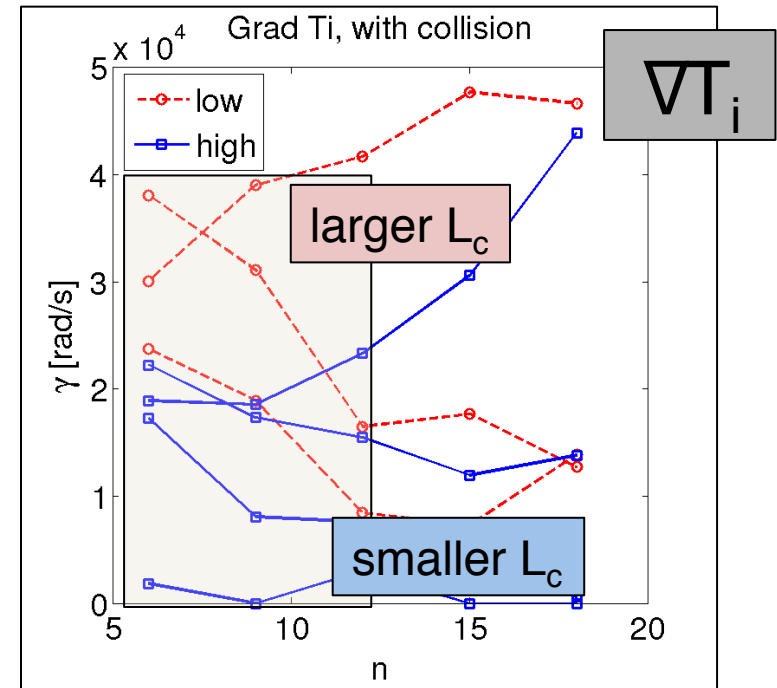
- ∇T_i , ∇n_e , and v_i^* scalings are **inconsistent** with **ITG**-driven transport
- ∇n_e , T_e , and T_i scalings are **consistent** with **TEM**-driven transport
- β_e scalings are **consistent** with **KBM**-driven transport
- ∇T_i , $1/L_{Te}$, and ∇n_e scalings show **mixed agreement** with **KBM**
- β_e and v scalings are **consistent** with **microtearing**-driven transport
- $1/L_{Te}$ scalings τ_d are **inconsistent** with **microtearing**-driven transport

Linear growth rates from GEM gyrokinetic simulations show scalings consistent with measured L_c scalings

GEM* global (pedestal) simulations with $6 \leq n \leq 15$ and $k_\theta \rho_s \sim 0.2$ indicate instabilities are **electromagnetic**, destabilized by **collisions**, and exhibit both **ballooning** and **tearing parity**



5 of 6 ∇n_e scenarios indicate low- n growth rates increase at higher ∇n_e



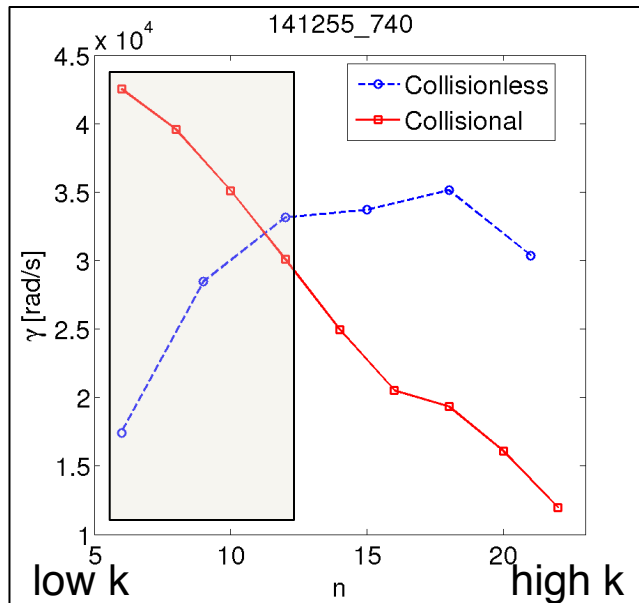
7 of 7 ∇T_i scenarios indicate low- n growth rates decrease at higher ∇T_i

GEM γ dependencies on ∇n_e and ∇T_i are consistent with observed L_c scalings

* Y. Chen and S. Parker, J. Comp. Phys. 220, 839 (2007)

Linear GEM simulations point to mixed-parity modes and highlight the importance of collisions

Collisions increase γ at low- n
(decrease γ at high- n)



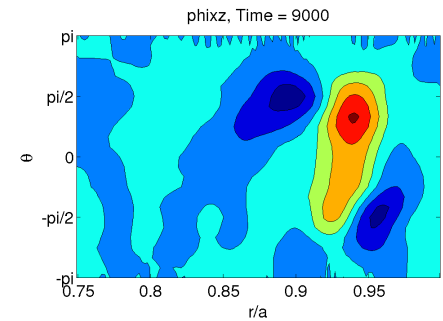
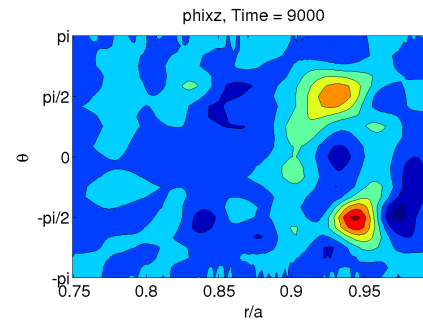
Low- n modes consistent
with observed scalings that
show lower k_θ at higher ν

GEM ϕ contours in plane $\perp B$ ($n=6$)

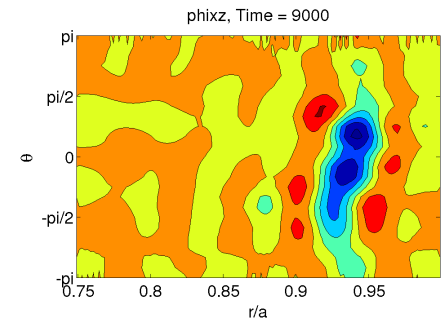
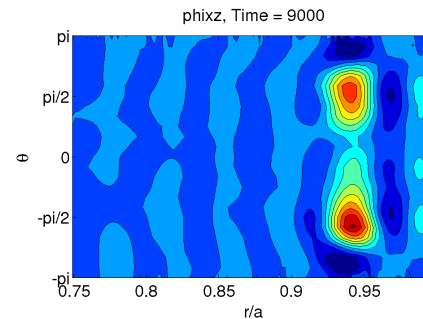
Collisionless

Collisional

$n=6$



$n=24$



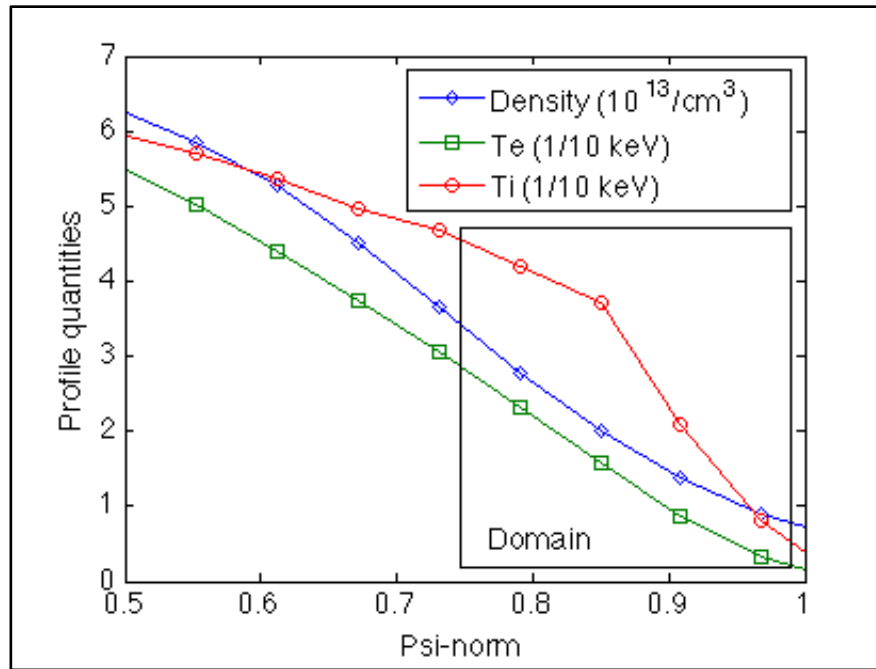
even parity

mixed parity

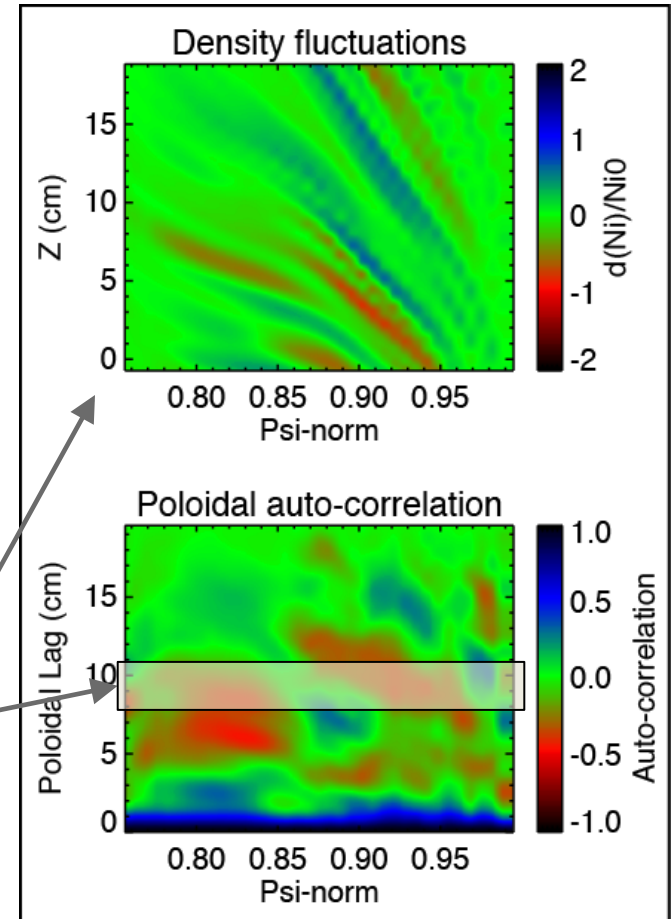
D. Smith et al, NF 53, 113029 (2013)

L_c and k_θ from BOUT++ pedestal simulations compare favorably with measurements

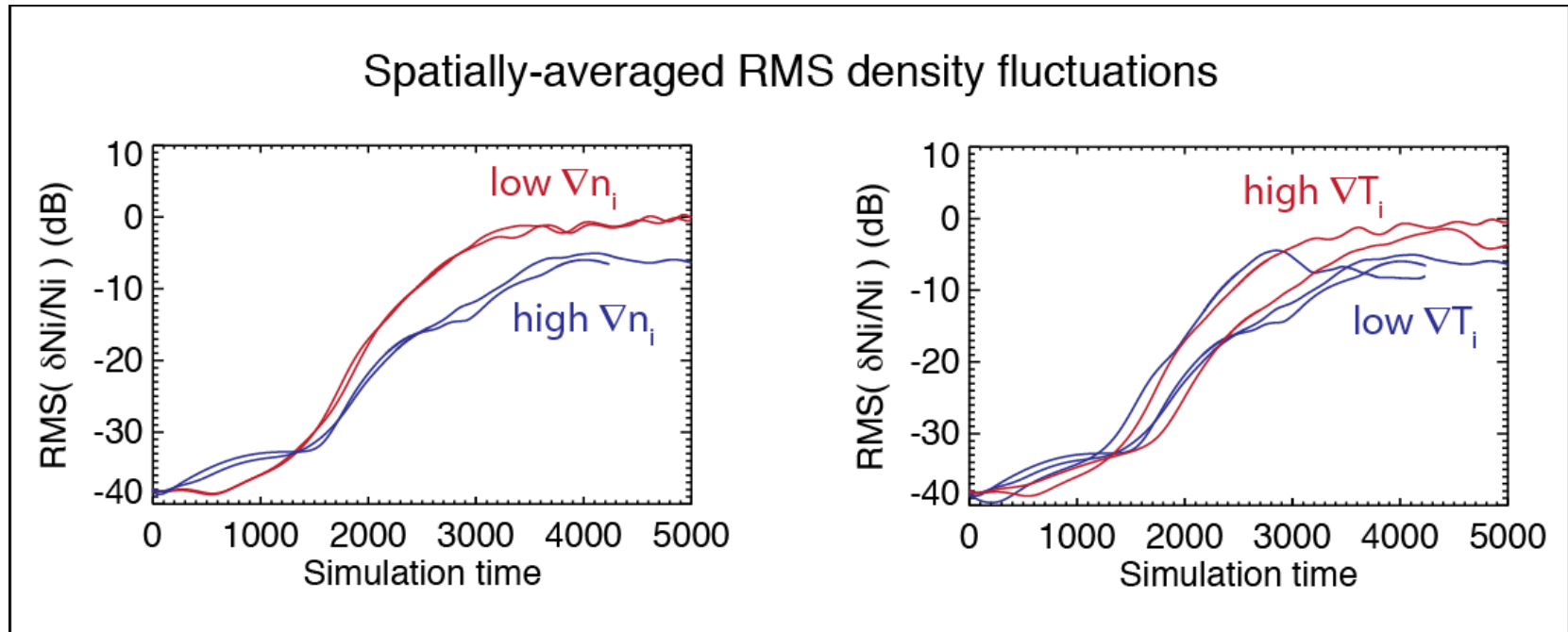
Initial value 3D Braginskii fluid simulations evolve n_i , ω , $j_{||}$, $A_{||}$, T_i , and T_e with collisionality, $E \times B$ advection, field line curvature, and drive terms for $j_{||}$ and ∇P . Simulations do not include toroidal rotation and parallel advection.



$L_c/\rho_i \sim 8$ is in line with measurements, but $k_\theta \rho_i \sim 0.7-1.4$ is higher than measurements



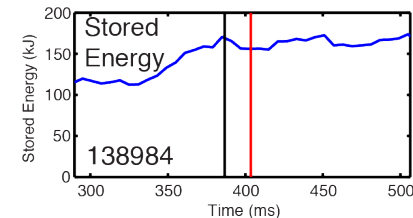
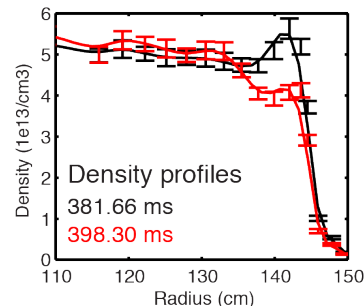
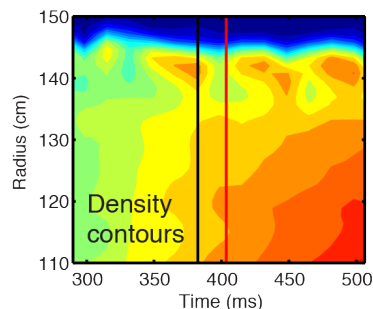
BOUT++ parameter scans point to larger fluctuation amplitudes at lower ∇n_i and higher ∇T_i



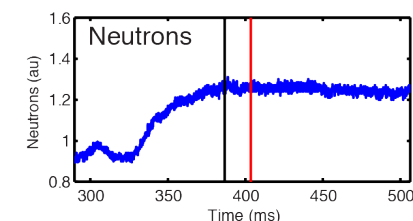
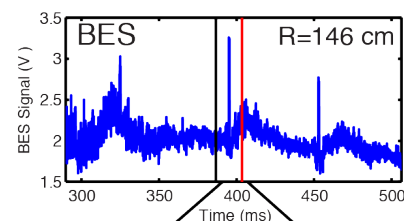
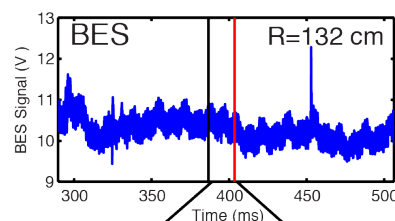
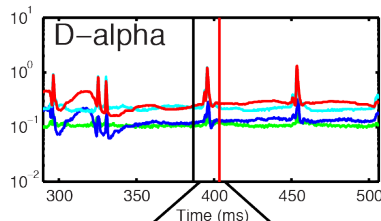
- ∇n_i and ∇T_i trends from Braginskii model do not reproduce observed scalings
 - Highlights the importance of **electron dynamics** for TEM and MT physics
 - Demonstrates that simple, order-of-magnitude comparisons (e.g. correlation length) can lead to erroneous inferences
 - Will benefit from BOUT++ **gyrofluid** model → X. Xu et al, in press, PoP (2013)

BES measurements with high time resolution show evolution and radial profile of ELM bursts

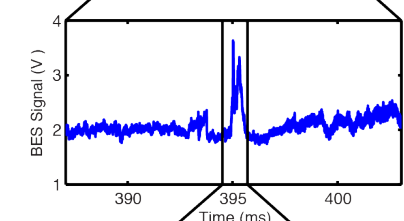
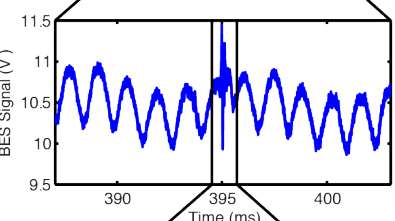
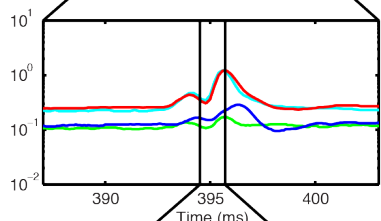
- Survey of 57 ELM bursts from 26 discharges
- Stored energy drops 1-16%
- Burst length 0.1-1.0 ms



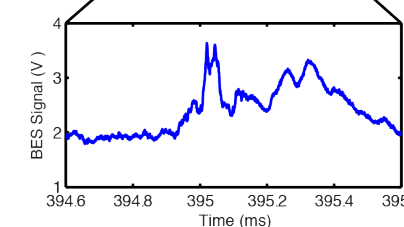
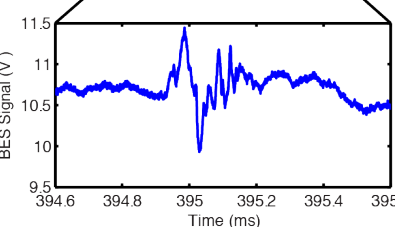
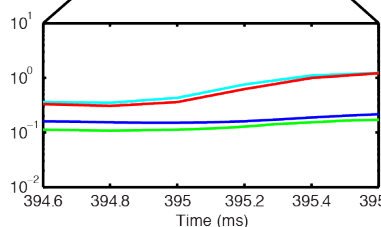
215 ms
window



16 ms
window



1 ms
window



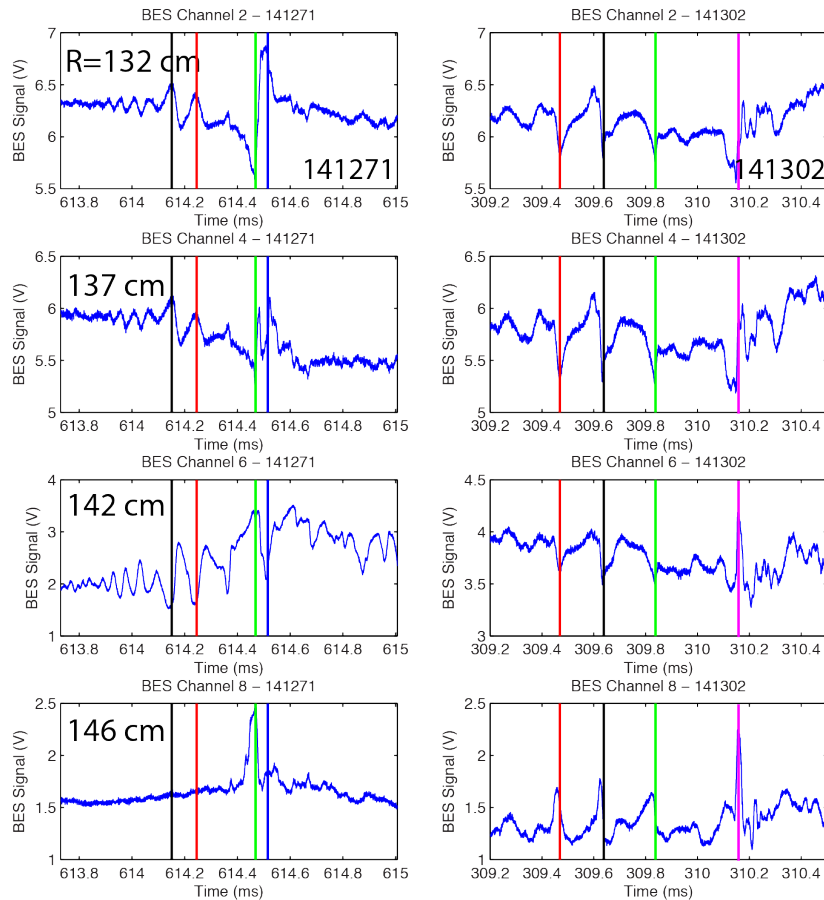
ELM bursts can show radial structure

Strong radial variation

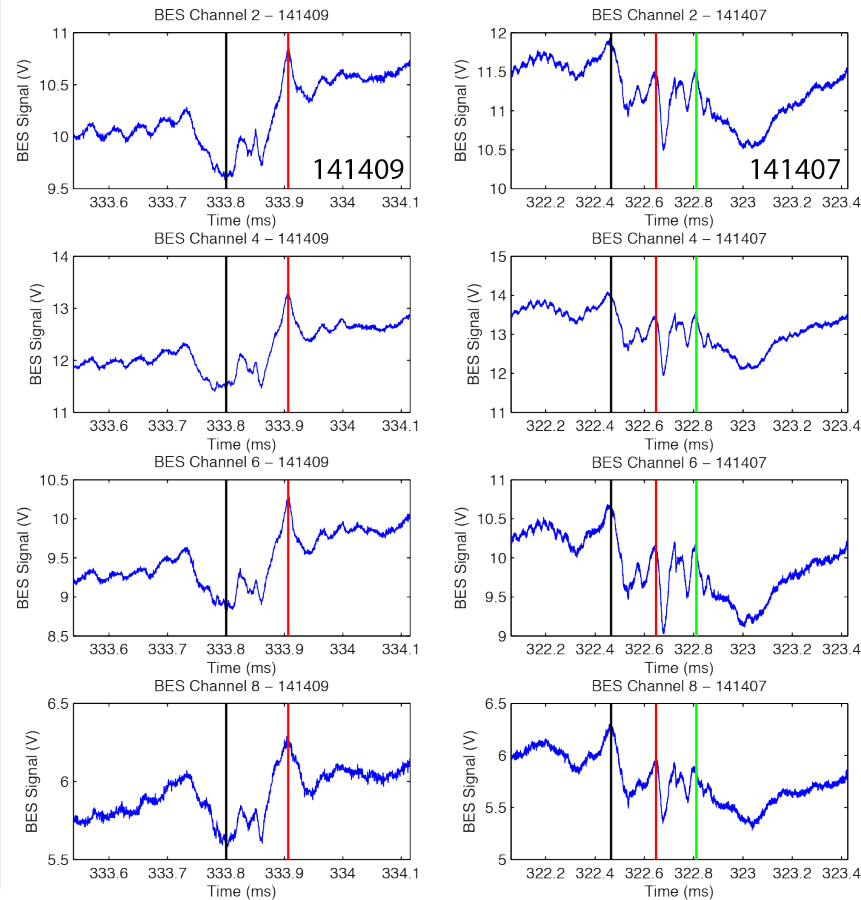
Pedestal
Top



SOL

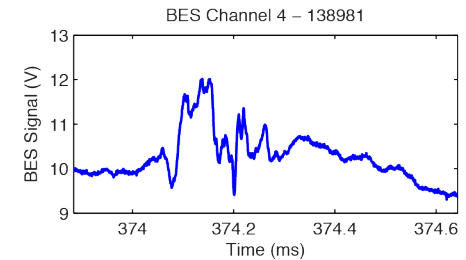
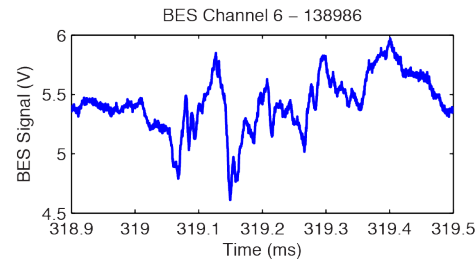
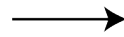


Radially uniform evolution

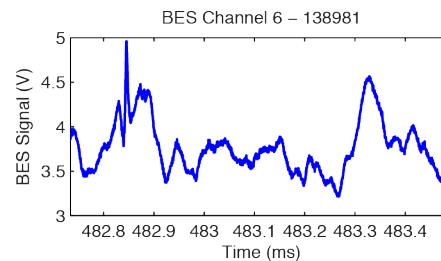
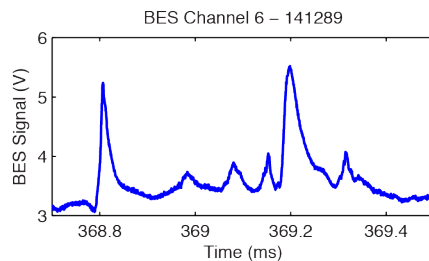
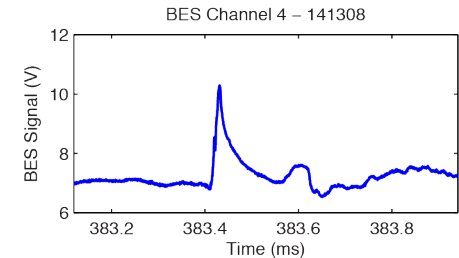
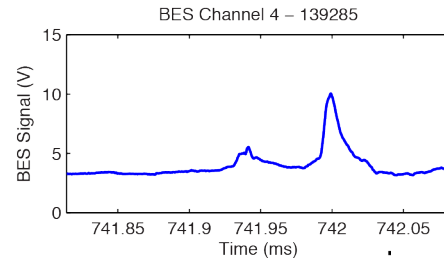
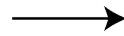


ELM bursts can also exhibit oscillations or multiple peaks

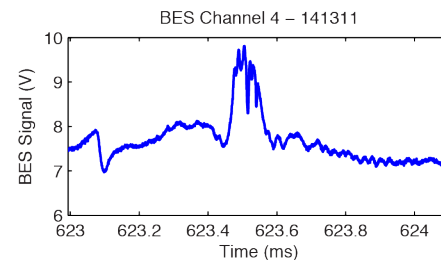
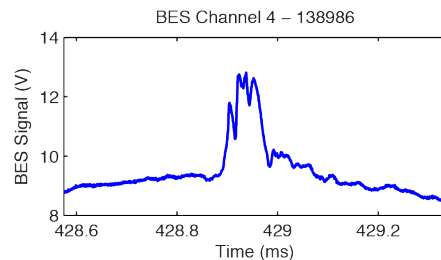
Oscillatory bursts



Non-oscillatory bursts



← Multiple peaks



← Single peak

Summary (ELM burst survey)

- **Strong radial variation** is generally observed with **small ΔW**
 - $\Delta W < 7$ kJ and $\Delta W/W < 5\%$
- Non-oscillatory bursts are generally short duration ($< 300 \mu\text{s}$) with **modest to large ΔW**
 - $\Delta W > 8$ kJ and $\Delta W/W > 5\%$
- Single, isolated bursts are generally short duration ($< 300 \mu\text{s}$)
- Multi-peak bursts show **modest to large ΔW**
 - $\Delta W > 7$ kJ and $\Delta W/W > 4\%$

Summary (Pedestal Turbulence)

- ST parameter regime can extend the parameter space and confidence in pedestal models
- We measured pedestal turbulence parameters in NSTX H-mode plasmas during ELM-free, MHD quiescent periods (with Li conditioning)

$$- L_c/\rho_i \sim 12k_\theta\rho_i \sim 0.2 \quad \tau_d/(a/c_s) \sim 5 \quad \tilde{n}/n \sim 1\%-4\%$$

- Parametric dependencies for pedestal turbulence measurements are most consistent with **TEM turbulence** and partially consistent with **KBM** and **μ -tearing turbulence**
 - **GEM** gyrokinetic simulations show linear γ scalings **consistent** with measured L_c scalings for ∇n_e and ∇T_i