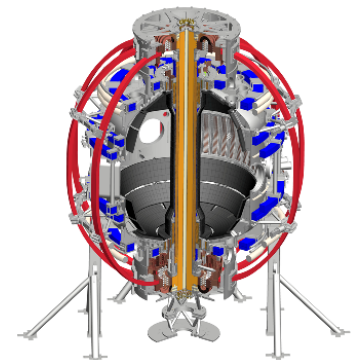


# Comparison of neutral density profiles measured using $D_\alpha$ and $C^{5+}$ in NSTXU

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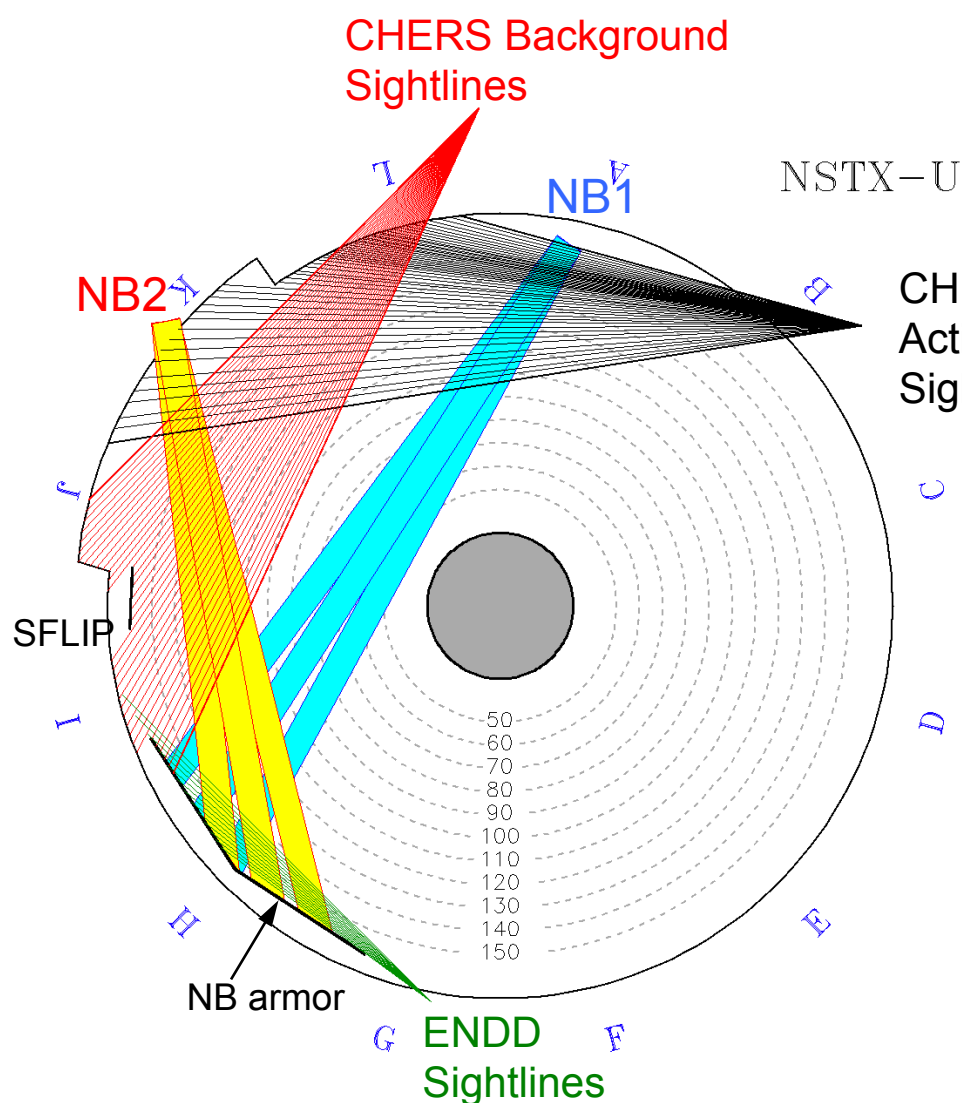
59<sup>th</sup> Annual Meeting of the APS Division of Plasma Physics  
Milwaukee, Wisconsin  
October 23-27, 2017



# Abstract

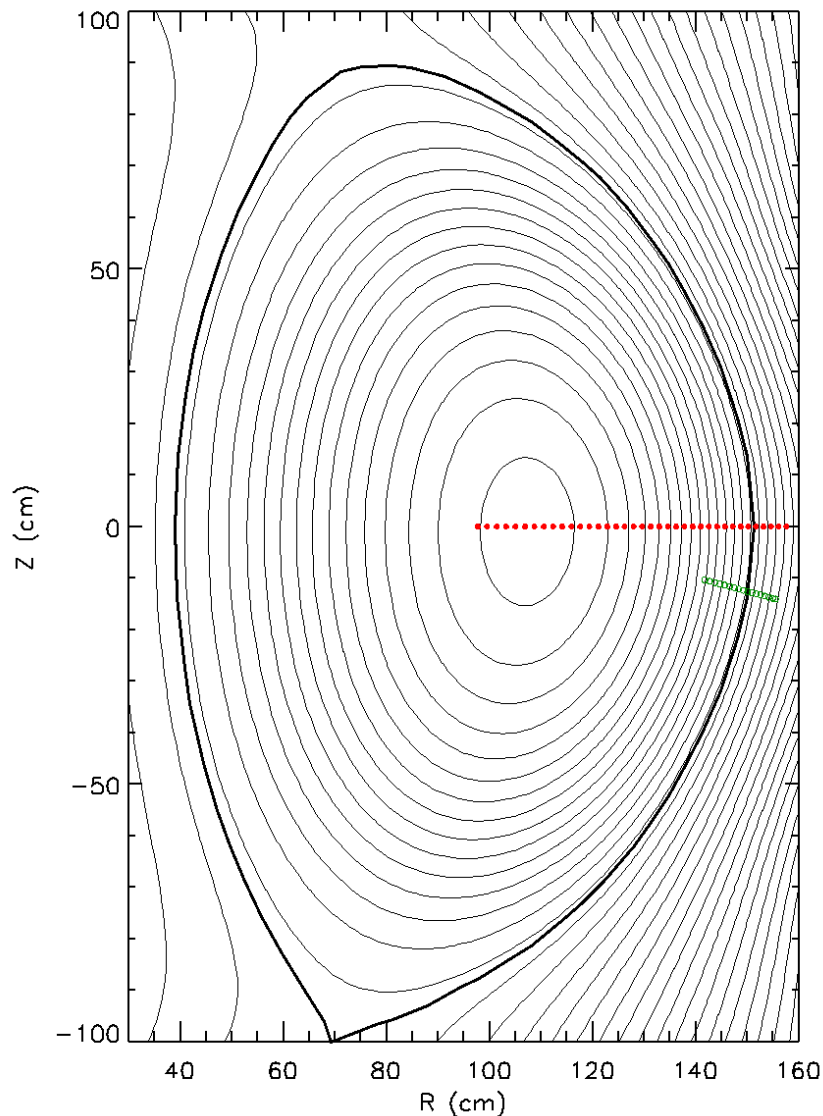
Edge neutral density profiles determined from two different measurements are compared on NSTXU plasmas. Neutral density measurements were not typical on NSTX plasmas. An array of fibers dedicated to the measurement of passive emission of  $C^{5+}$ , used to subtract background emission for charge exchange recombination spectroscopy (CHERS), can be used to infer deuterium neutral density near the plasma edge. The line emission from  $C^{5+}$  is dominated by charge exchange with neutral deuterium near the plasma edge. An edge neutral density diagnostic (ENDD) consisting of a camera with a  $D_\alpha$  filter was installed on NSTXU. The line-integrated measurements from both diagnostics are inverted to obtain local emissivity profiles. Neutral density is then inferred using atomics rates from ADAS and profile measurements from Thomson scattering and CHERS. Comparing neutral density profiles from the two diagnostic measurements helps determine the utility of using the more routinely available  $C^{5+}$  measurements for neutral density profiles. Initial comparisons show good agreement between the two measurements inside the separatrix.

# NSTXU Viewing Geometry



- **CHERS Active views**
  - Charge exchange recombination spectroscopy measuring  $T_i$ ,  $N_C$ ,  $V_\phi$
  - Optimized views across NB1
  - Views CX emission and background emission for  $C^{5+}$
- **CHERS Background views**
  - View parallel to NB1
  - View *only*  $C^{5+}$  background emission
  - Background measurement *simultaneous* with active measurement
- **ENDD**
  - Edge Neutral Density Diagnostic sightlines below midplane viewing upward
- **Second neutral beam (NB2) compromises CHERS Background views**
  - Bright CX emission contaminates background views

# NSTXU Viewing Geometry

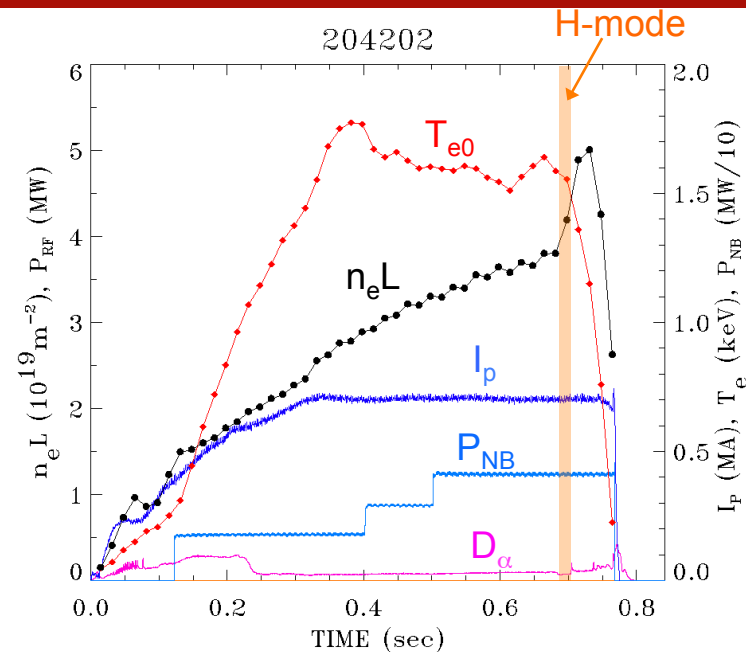


CHERS  
Background  
Sightlines

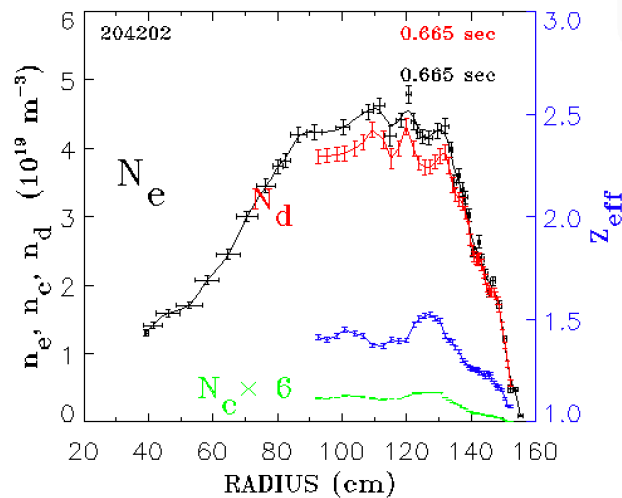
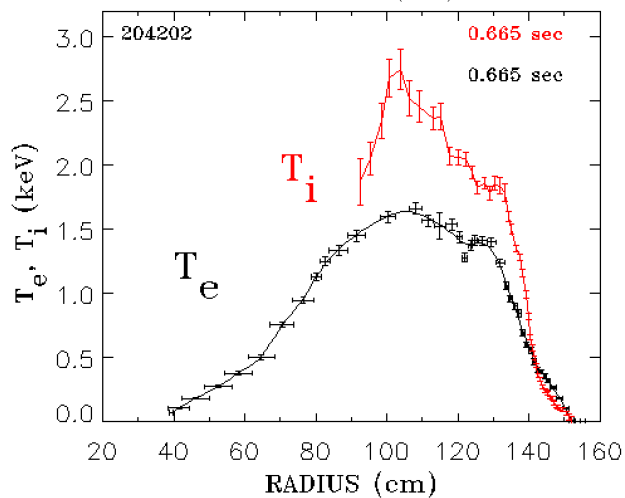
ENDD  
Sightlines

- **CHERS Background views**
  - On midplane
  - CHERS exposure 10 ms
  - 37 fibers in background view
- **ENDD**
  - Edge Neutral Density Diagnostic sightlines below midplane viewing upward
  - ENDD exposure 3.7 ms
  - Camera with  $D_{\alpha}$  filter
  - Subset of 127 x 128 pixels used

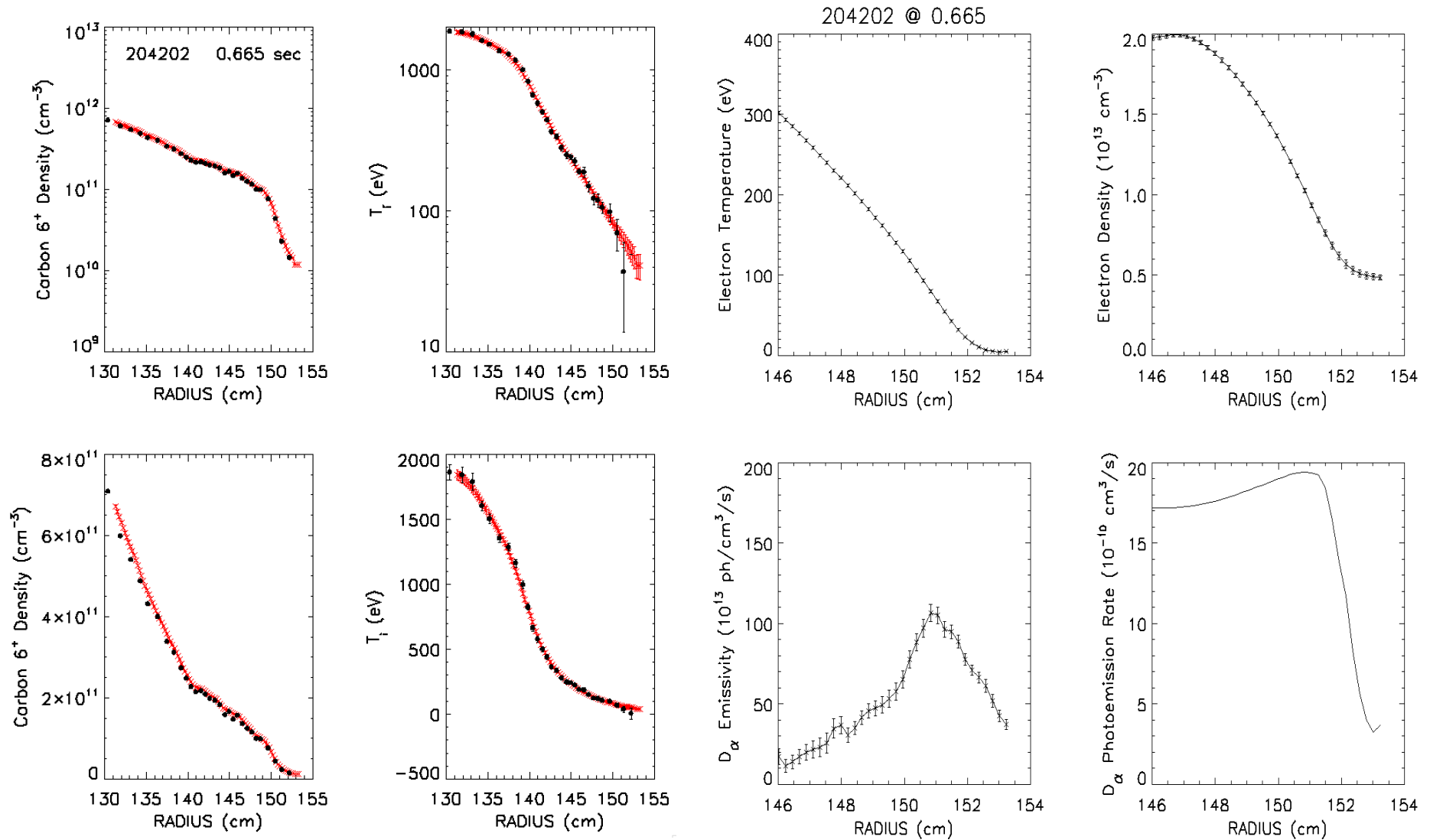
# NSTX-U L-mode plasma



- L-mode plasma
- Brief H-mode 690-700 ms
- $I_p = 700 \text{ kA}$



# Measured profiles of temperature and density are interpolated or extrapolated onto common fine grid



# Three Processes Contribute to $C^{5+}$ passive emission

$$E_{C^{5+}} = Q_{ex} n_e n_{C^{5+}} + Q_{rec} n_e n_{C^{6+}} + Q_{cx} n_0 n_{C^{6+}}$$

  
*Excitation*

  
*Recombination*

  
*Thermal Charge Exchange*

## **UNKNOWN:**

$n_{C^{5+}}$  Density of  $C^{5+}$

$n_0$  Density of thermal deuterium neutrals

## **MEASURED:**

$E$  Emissivity of passive emission from  $C^{5+}$   $n = 87$

$n_e$  Electron density

$n_{C^{6+}}$  Density of  $C^{6+}$

## **COMPUTED:**

$Q_{ex}$  Photoemission rate for electron impact excitation,  $[T_e, n_e]$

$Q_{rec}$  Photoemission rate for recombination from  $C^{6+}$  to  $C^{5+}$ ,  $[T_e, n_e]$

$Q_{cx}$  Photoemission rate for thermalthermal charge exchange  $[T_e, n_e, Z_{eff}]$

## Cannot independently determine both $C^{5+}$ density and thermal neutral density

- Determination of density of  $C^{5+}$  requires thermal neutral deuterium ( $n_0$ ) profile

$$n_{C^{5+}} = \frac{E}{Q_{ex} n_e} - \left( \frac{Q_{rec}}{Q_{ex}} + \frac{Q_{cx}}{Q_{ex}} \frac{n_0}{n_e} \right) n_{C^{6+}}$$

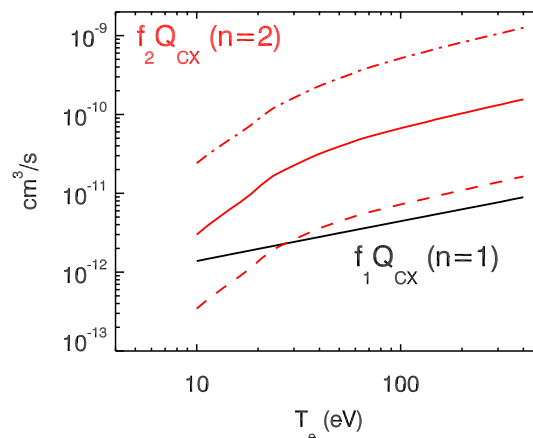
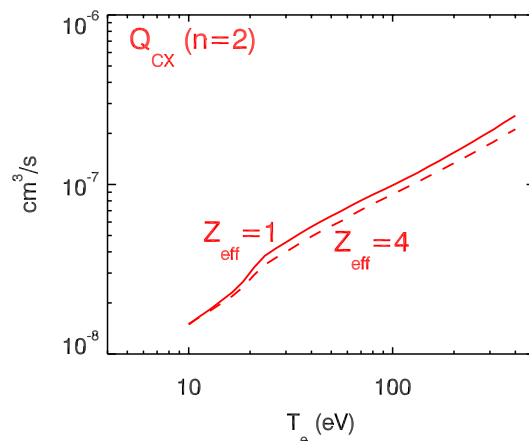
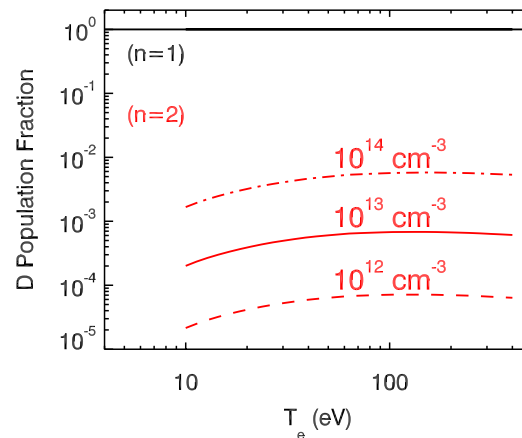
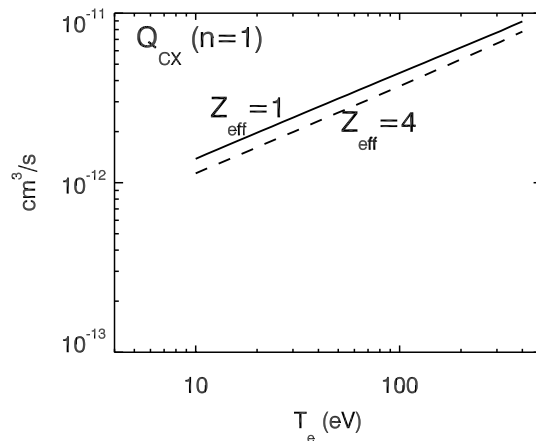
- Conversely, the thermal neutral density depends on the  $C^{5+}$  density or on the *ratio* of densities of  $C^{5+}$  to  $C^{6+}$

$$n_0 = \frac{E}{Q_{cx} n_{C^{6+}}} - n_e \left( \frac{Q_{ex}}{Q_{cx}} \frac{n_{C^{5+}}}{n_{C^{6+}}} + \frac{Q_{rec}}{Q_{cx}} \right)$$



# Effective thermal-thermal charge-exchange rate is dominated by n=2 excited population fraction

Effective CX rate:  $Q_{cx}^{eff} \cong f_1 Q_{cx}^{n=1} + f_2 Q_{cx}^{n=2}$   $n_0 = \sum f_i n_{0,n=i}$   $\sum f_i = 1$



- Thermalthermal charge exchange rates for C<sup>6+</sup> and D computed using ADAS 308 data.
- Population fraction derived from ADAS photoemission coefficients,

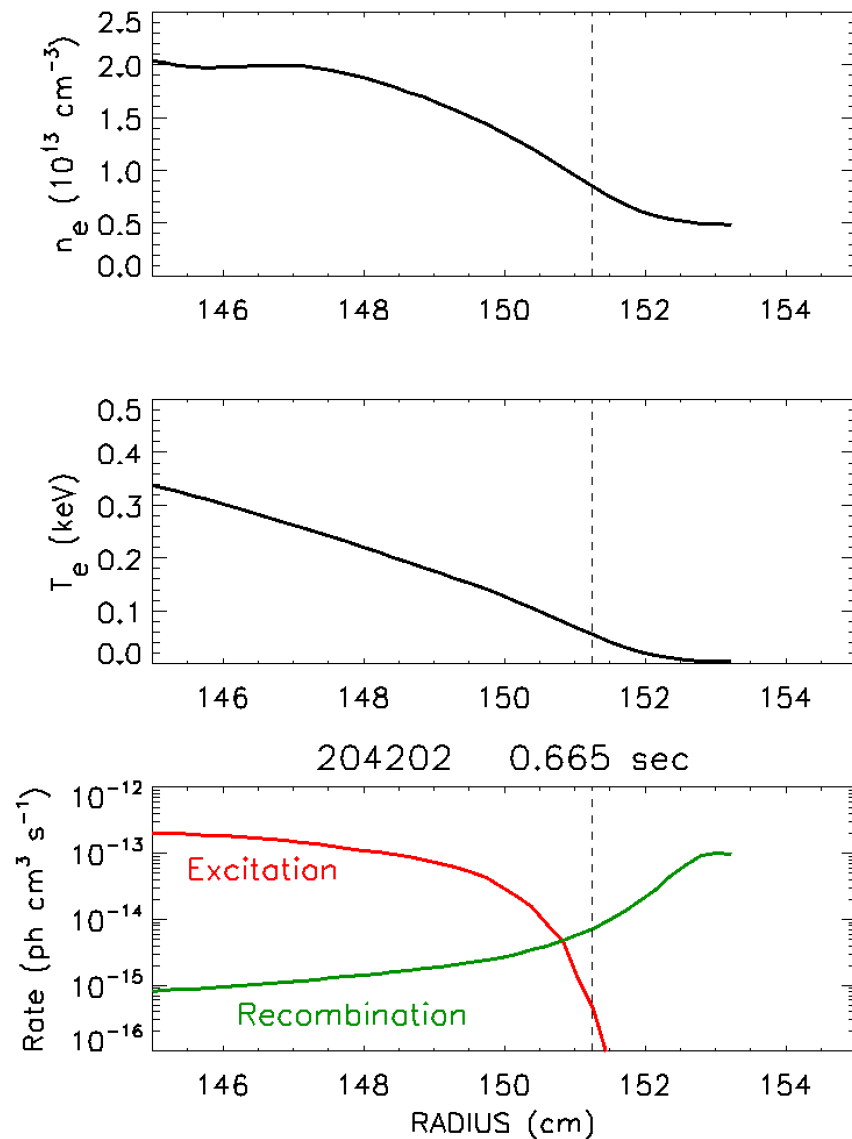
$$f_2 = \frac{n_D(n=2)}{n_D(n=1)} = \frac{PEC_{21}^{exc}}{A_{21}} n_e$$

or a from CollisionalRadiative model from DEGAS 2\*

- n=2 neutral fraction varies with electron density
- n=2 population is less than a percent of the thermal neutral density
- Contribution from n=1 ground state neutrals are only important at lower densities or low temperature

\*<http://w3.pppl.gov/degas2/ehr3.dat>

# At lower temperature (plasma edge), electron impact excitation can be neglected for carbon



- For  $T_e < 50$  eV, the contributions to  $C^{5+}$  emission from electron impact excitation are negligible

- Neglecting electron impact excitation:

$$E \approx n_0 n_{C^{6+}} Q_{cx} + n_e n_{C^{6+}} Q_{rec}$$

$$n_0 \approx \frac{E}{n_{C^{6+}} Q_{cx}} - n_e \frac{Q_{rec}}{Q_{cx}}$$

- Most of the emission is from thermal charge exchange (second term above is small)
- This sets upper limit on thermal neutral density
- Without electron impact excitation, knowledge of  $C^{5+}$  density is not needed to determine neutral density

# Neutral density is determined from $D_\alpha$ emission

$$E_{D_\alpha} = Q_{ex}^{D_\alpha} n_e n_0$$

  
*Excitation rate*

$$n_0 = \frac{E_{D_\alpha}}{Q_{ex}^{D_\alpha} n_e}$$

## **UNKNOWN:**

$n_0$  Density of thermal deuterium neutrals

## **MEASURED:**

$E$  Emissivity of passive emission from  $D_\alpha$  ( $n = 3-2$ )

$n_e$  Electron density

## **COMPUTED:**

$Q_{ex}$  Photoemission rate for electron impact excitation,  $[T_e, n_e]$

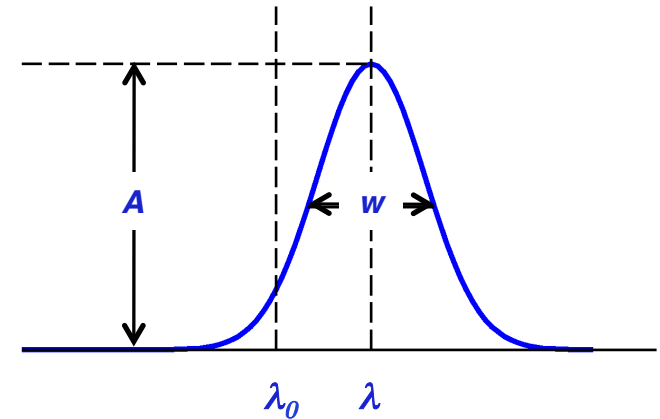
# Local carbon values are extracted from line-integrated measurements with a matrix inversion approach

## Line integrated measurements

- Spectral Brightness,  $B^\lambda$
- Total Brightness,  $B = \int B^\lambda d\lambda$

## Fitted Parameters

- Amplitude,  $A$
- Line width,  $w$
- Line shift,  $(\delta\lambda)$



$$B^\lambda = \frac{B}{w} \sqrt{\frac{4 \ln 2}{\pi}} \exp\left(-\frac{4 \ln 2 (\lambda - \lambda_0 - \delta\lambda)^2}{w^2}\right)$$

(Form for a Gaussian line shape)

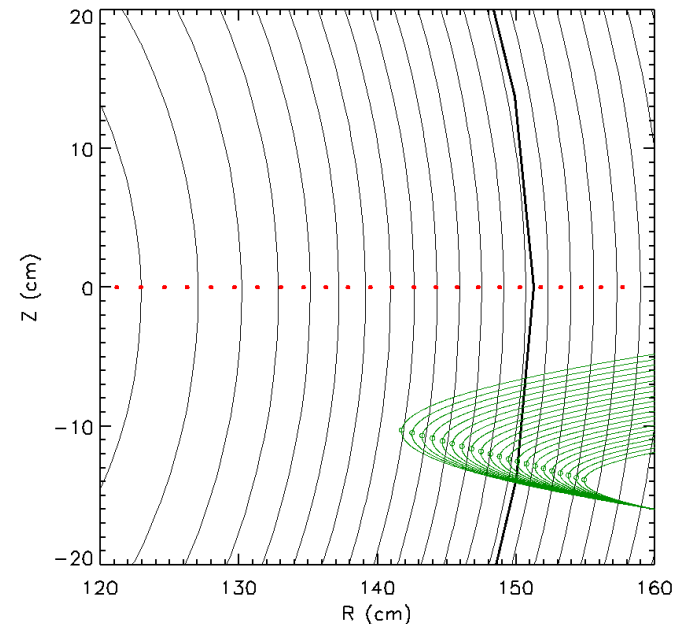
## Emissivity from Brightness

- Subscript  $i$  refers to a particular sightline (*line-integrated* measurement)
- Subscript  $j$  refers to a particular zone in the plasma (*local* value)
- $L_{ij}$  is a matrix of path lengths
- Line-integrated brightness ( $ph/s/cm^2/st$ ) can be related to local emissivity ( $ph/s/cm^3$ ) by length matrix
- Local emissivity is obtained using inverted length matrix

$$4\pi B_i = \sum_j L_{ij} E_j$$
$$E_j = 4\pi \sum_i L_{ij}^{-1} B_i$$

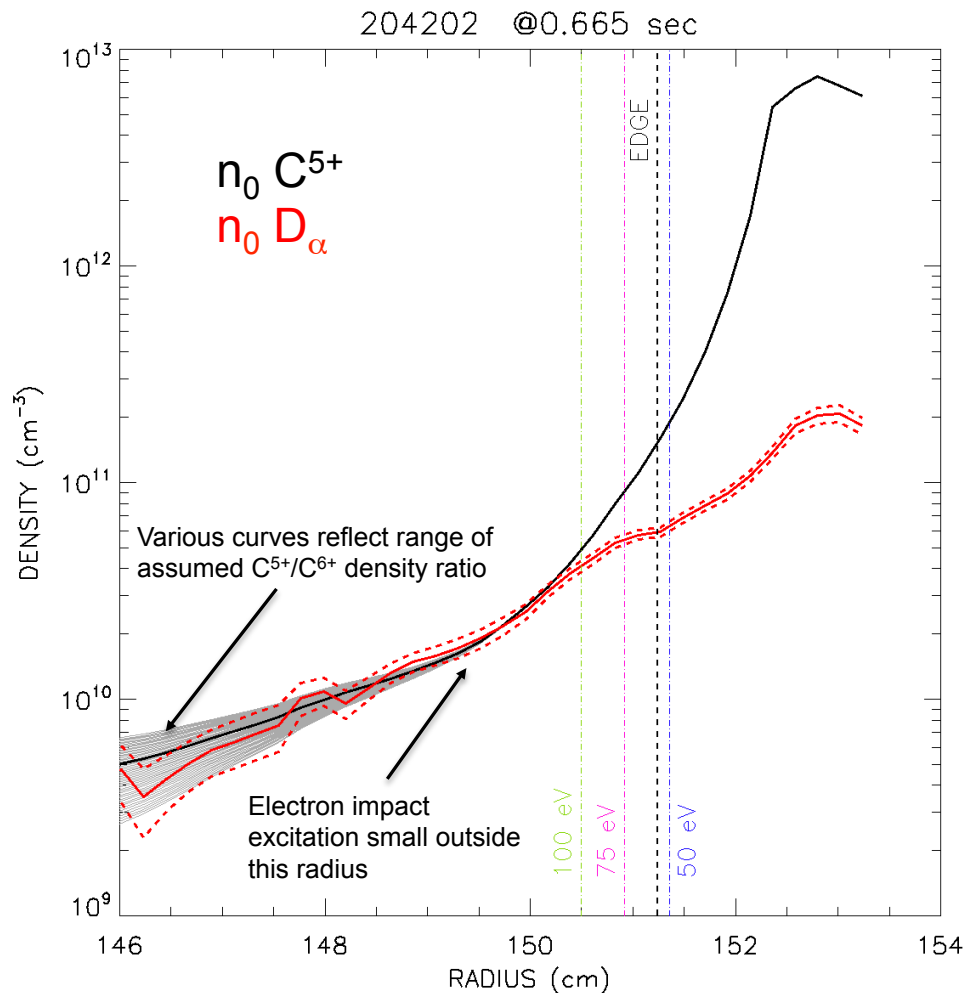
# Local $D_\alpha$ emissivity from line-integrated measurements with a matrix inversion approach

- Line-integrated measurements
  - Camera with 127 x 128 pixels
  - $D_\alpha$  filter
  - Absolutely calibrated
- Local tangency of sightline each pixel computed using EFIT equilibrium code
- Tangency mapped to R at Z=0
- Pixels binned to improve S/N
- Emissivity from Brightness using matrix inversion with length matrix calculated for 3D geometry



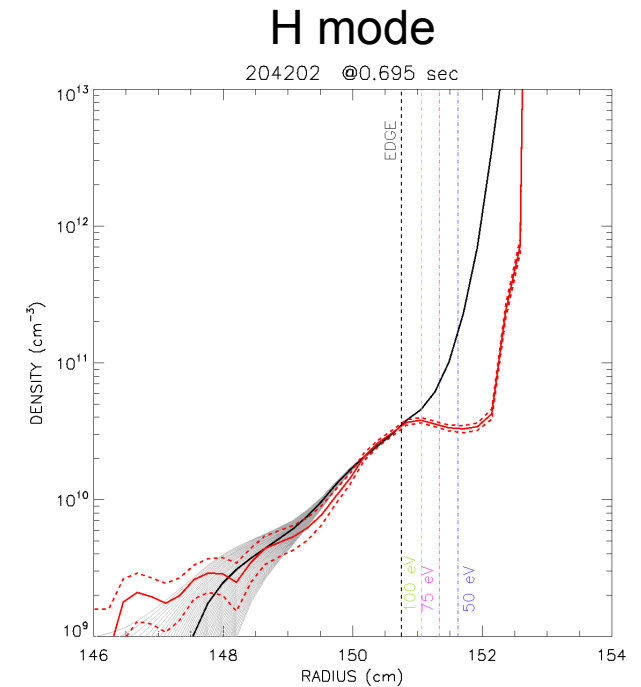
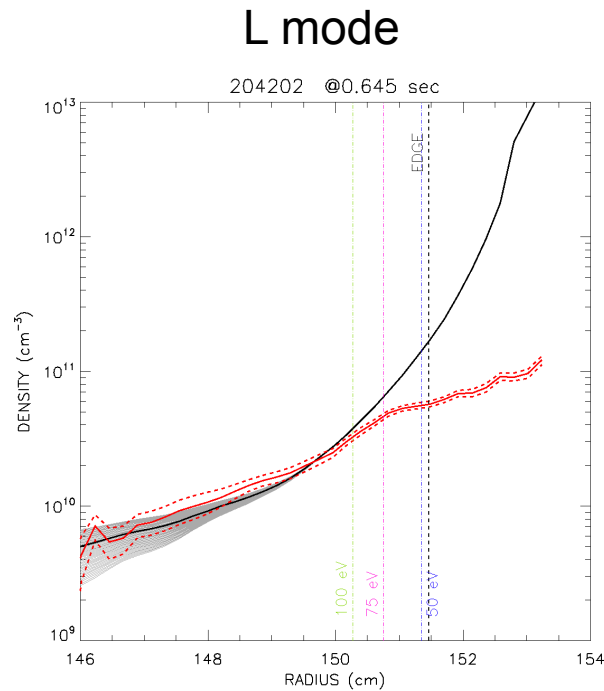
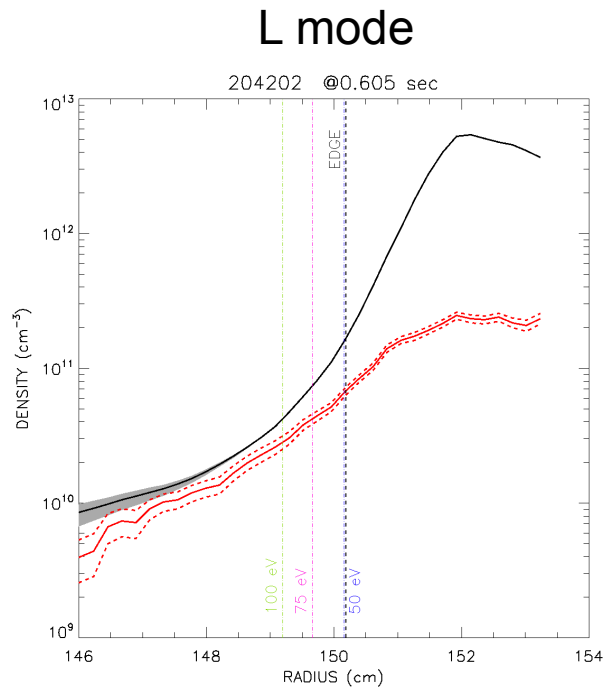
$$4\pi B_i = \sum_j L_{ij} E_j$$
$$E_j = 4\pi \sum_i L_{ij}^{-1} B_i$$

# Neutral density profiles from $C^{5+}$ and $D_\alpha$ are comparable inside plasma edge

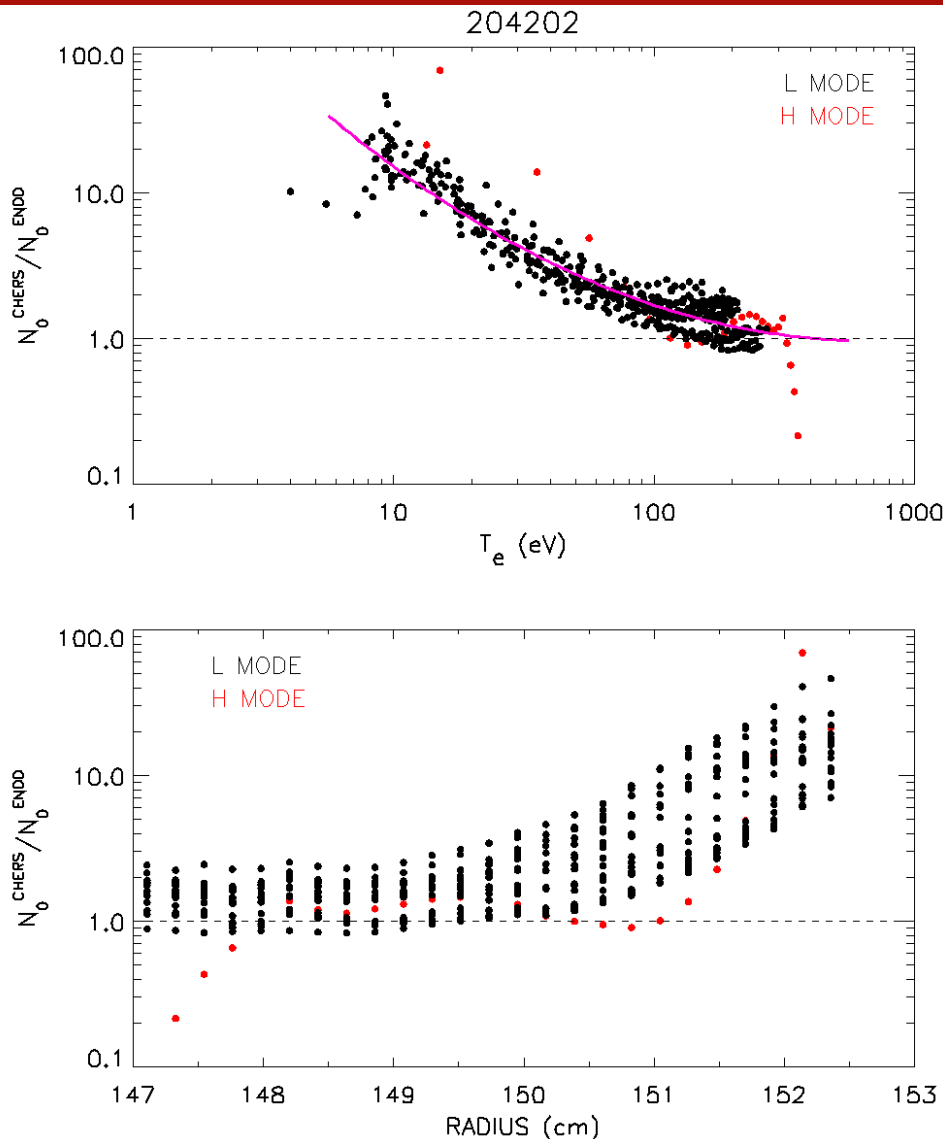


- L mode plasma edge
- Similar neutral density profiles over 45 cm inside LCFS
- Neutral densities strongly diverge outside LCFS
- $n_0$  from  $C^{5+}$  exceeds  $n_0$  from  $D_\alpha$  by an order of magnitude just a few cm away from edge

# Some variation is observed in neutral density profiles inferred from $C^{5+}$ and $D_\alpha$



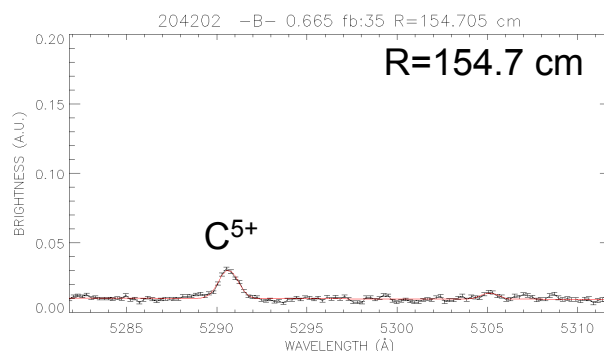
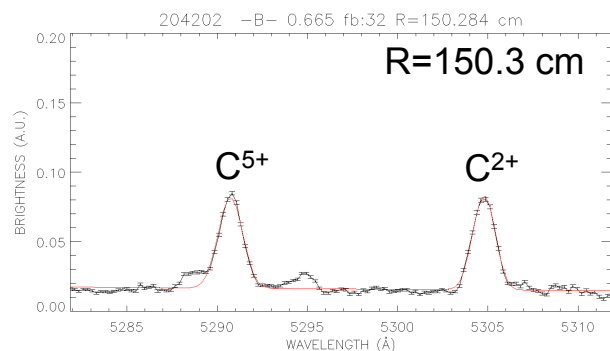
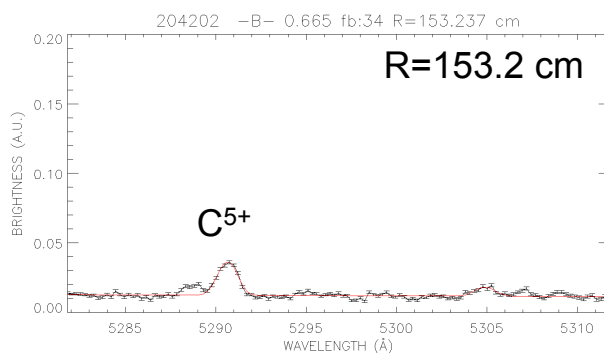
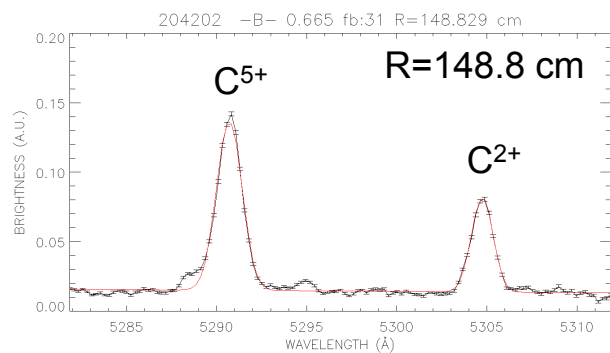
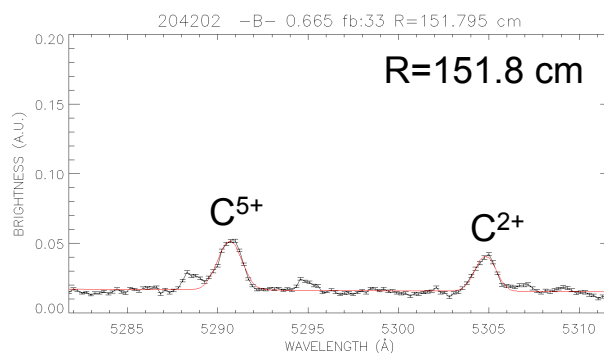
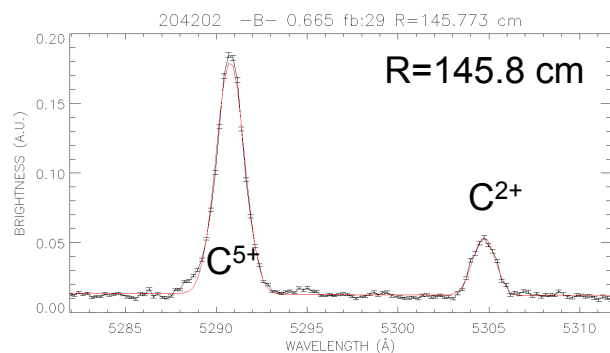
# Better agreement between $n_0$ measurements at higher $T_e$



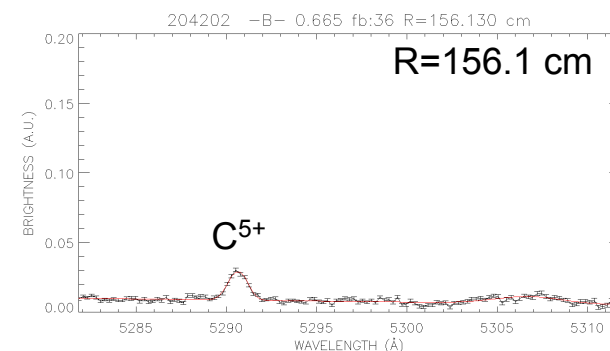
- Ratio of neutral densities plotted for multiple time
- Ratio trends toward 1 as  $T_e$  increases
- At higher  $T_e$ , agreement within a factor of 2
- At lower  $T_e$ , ratio of neutral densities  $\sim 10$
- Plotting data vs. R shows strong deviation outside LCFS



# C<sup>5+</sup> emission observed beyond the LCFS



- C<sup>5+</sup> emission in SOL is inconsistent with local  $T_e$ ,  $N_e$
- C<sup>5+</sup> emission is observed outside of C<sup>2+</sup> emission shell



# Convective transport from “blobs” could explain “extra” $C^{6+}$ beyond LCFS

- $C^{6+}$  lifetime  $\sim 10^{-9}$  sec
- Distance into SOL  $\sim 5$  cm
- Blob velocity  $\sim 10^5$  cm/s
- Edge  $T_e \sim 50$  eV
- Edge  $n_e \sim 10^{13}$  cm $^{-3}$
- Edge  $n_0 \sim 10^{11}$  cm $^{-3}$
- Total recombination rate for Carbon  $Z=6$   
 $Q_{rec}(50 \text{ eV}, 10^{13} \text{ cm}^{-3}) = 2.7 \times 10^{-13} \text{ cm}^2/\text{s}$
- Total charge exchange rate for Carbon  $Z=6$   
 $Q_{cx}(50 \text{ eV}, 10^{13} \text{ cm}^{-3}) = 6.9 \times 10^{-8} \text{ cm}^2/\text{s}$

## Characteristic Times:

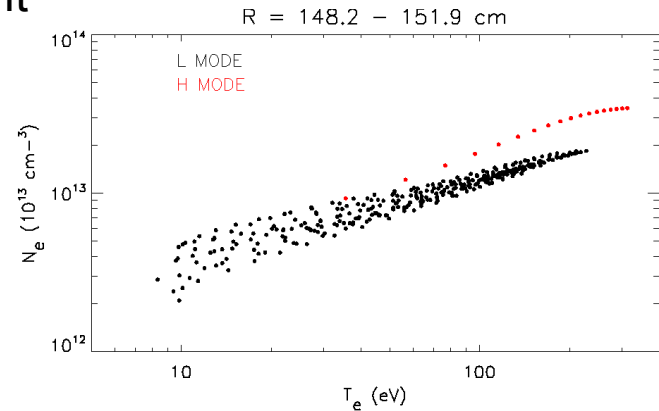
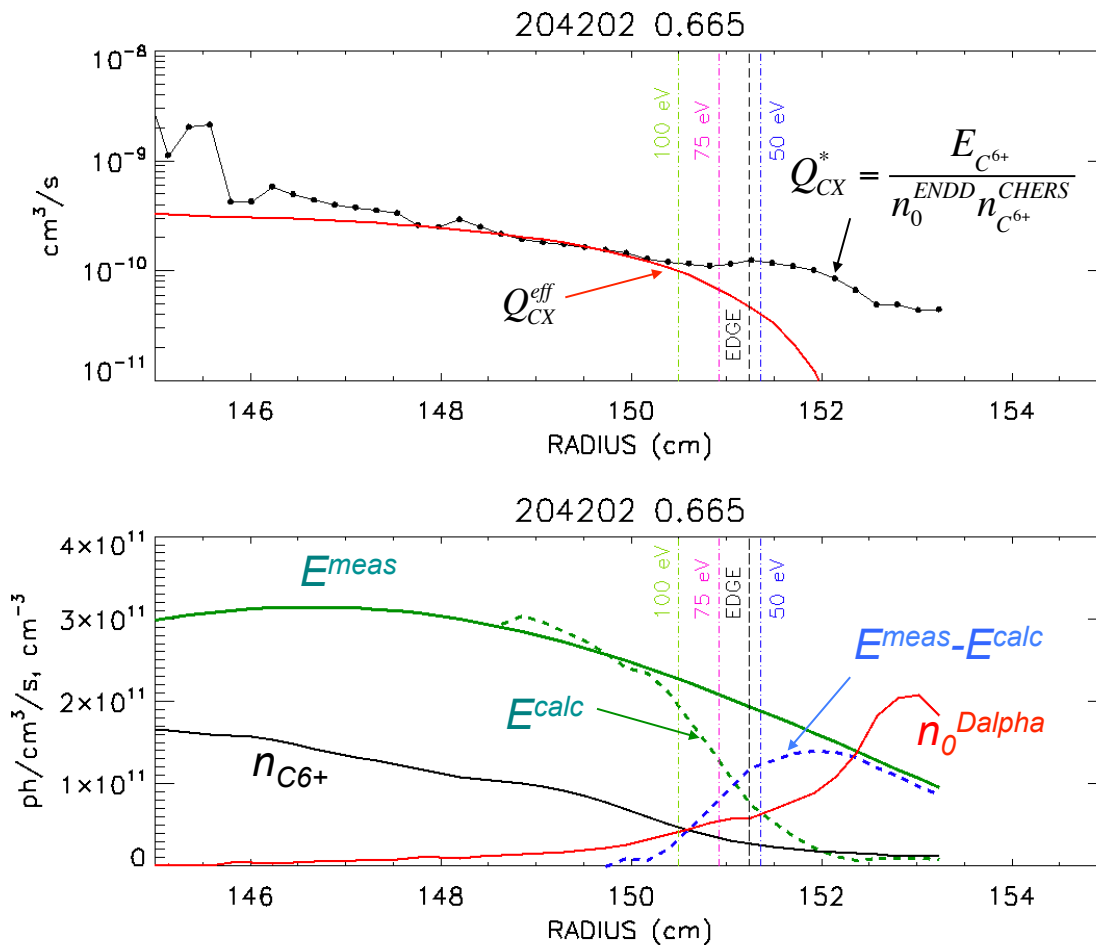
$$\tau_{blob} = \frac{5 \text{ cm}}{10^5 \text{ cm/s}} = 50 \text{ } \mu\text{sec}$$

$$\tau_{CX} = \frac{1}{n_0 Q_{CX}} = 145 \text{ } \mu\text{sec}$$

$$\tau_{REC} = \frac{1}{n_e Q_{REC}} = 365 \text{ msec}$$

# Neutral density from $C^{5+}$ is overestimated outside LCFS due to “extra” $C^{5+}$ emission

- Measured  $C^{5+}$  emissivity exceeds that expected with local  $T_e$ ,  $n_e$  measurements and  $D_\alpha$  neutral density measurement



- The required photoemission rate,  $Q_{CX}^* = Q_{CX}(T_e^*, n_e^*)$  corresponds to different values of electron temperature and density
- Subtracting the expected emission from the measured emission shows an excess signal,  $(E_{meas} - E_{calc})$

# Measured emissivity is a time average of steady emission and intermittent “blob” emission

- Introduce a simple model to describe the measurements
- Steady emission ( $E_0$ ) is consistent with local measured  $T_e$ ,  $n_e$
- Intermittent “blob” ( $E_1$ ) emission would correspond to different values ( $T_e^*$ ,  $n_e^*$ )

$$Q_{CX}(T_e^*, n_e^*) > Q_{CX}^{eff}(T_e, n_e)$$

- The “duty cycle” of the blobs is given as  $f$

$$E_{C^{6+}}^{meas} = E_0 + E_1$$

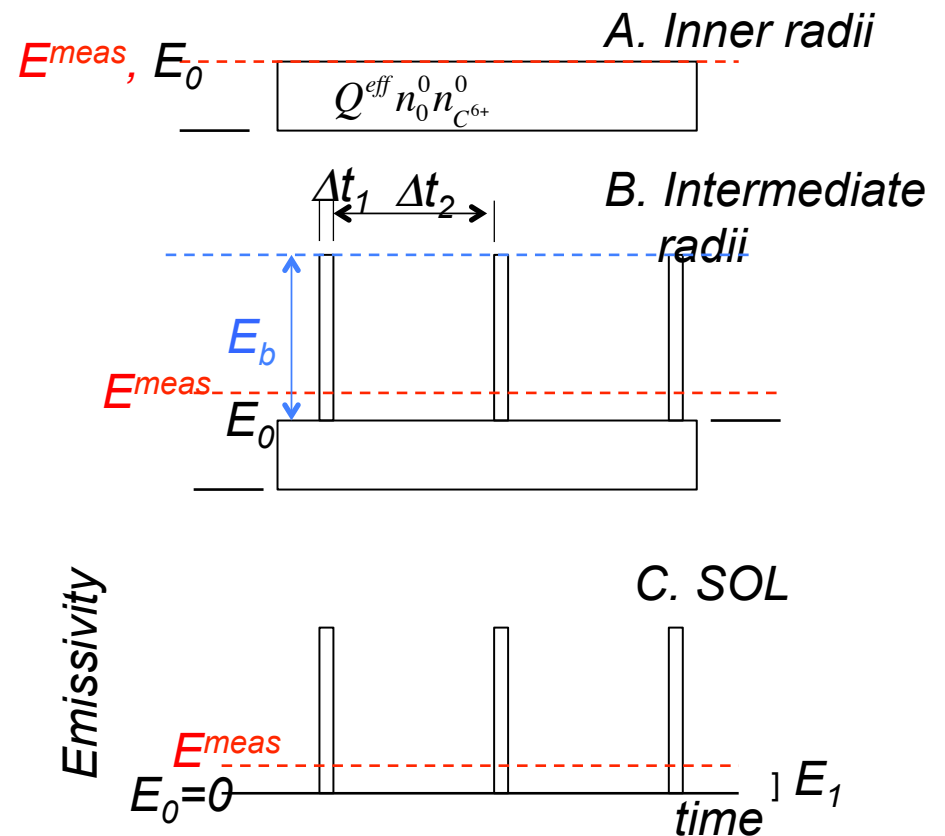
$$E_0 = Q^{eff} n_0^0 n_{C^{6+}}^0 (1 - f)$$

$$E_1 = Q_{CX}(T_e^*, n_e^*) n_0^B n_{C^{6+}}^B f$$

$$f = \Delta t_1 / (\Delta t_1 + \Delta t_2)$$

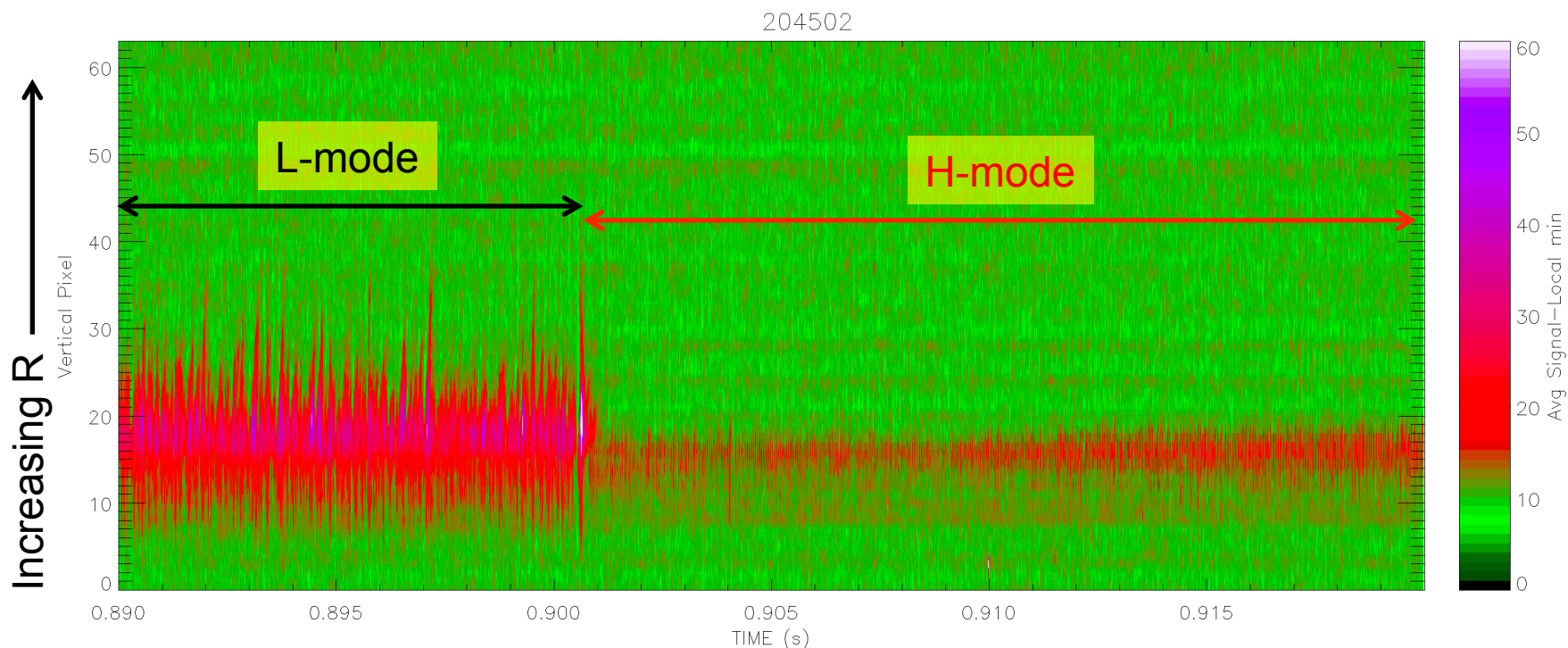
- If the neutral density remains relatively constant, then in the SOL,

$$Q_{CX}^* = \frac{E_{C^{6+}}^{meas}}{n_0^{ENDD} n_{C^{6+}}^{CHERS}}$$



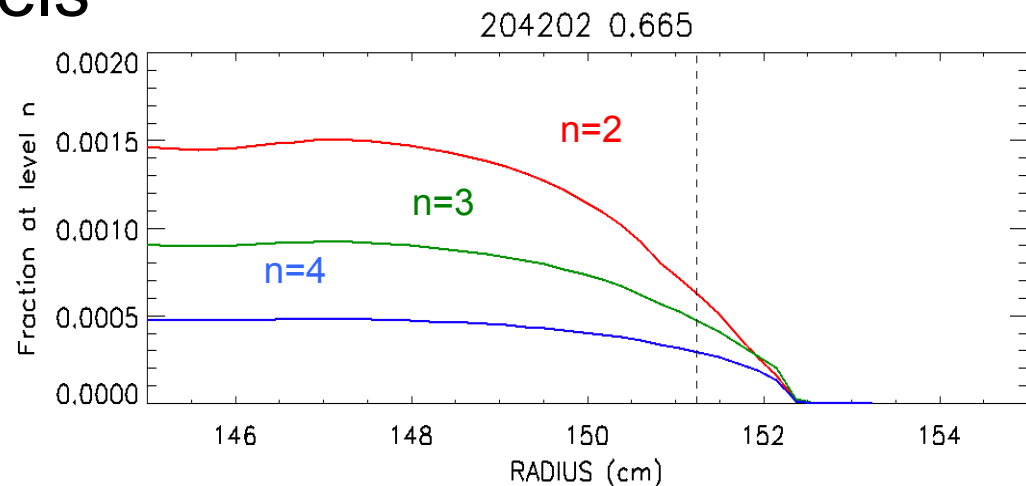
# Intermittent signal from fast Gas Puff Imaging (GPI) system

- Signal from GPI across L-H transition
- Estimated “duty cycle” of blobs  $\sim 8\%$  during L-mode
- ENDD and CHERS signals will be time-averaged over many milliseconds



# Other Comments

- Reflections (ruled on for NSTX-U views) might cause unexplained emission in edge
- $n_0$  from  $D_\alpha$  is an upper limit due to contributions to emission from molecular  $D_2$
- The effective thermal-thermal charge exchange rate for carbon does not take into account contributions from  $n=3$  and  $n=4$  levels



# Summary

- Neutral density measurements made with  $C^{5+}$  emission and  $D_\alpha$  emission
- Neutral density profiles agree within a factor of 2 *inside the LCFS* for L-mode plasmas
- Neutral density profiles *outside the LCFS* deviate up to an order of magnitude
- $C^{5+}$  emission is observed in SOL
- Estimate of necessary photoemission rate outside LCFS suggests higher  $T_e$ ,  $N_e$  values than local measurements
- Convective transport (blobs) of  $C^{6+}$  could explain 'extra'  $C^{5+}$  emission in SOL