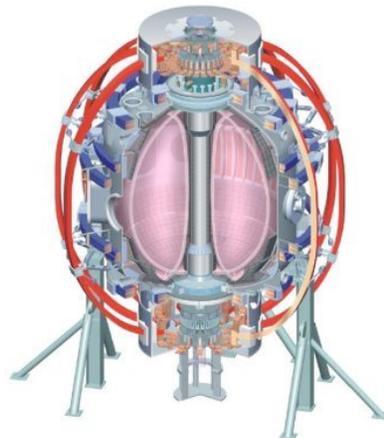


# Nonlinear Gyrokinetic Simulations of Electron Internal Transport Barriers in the National Spherical Torus Experiment

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# Acknowledgements

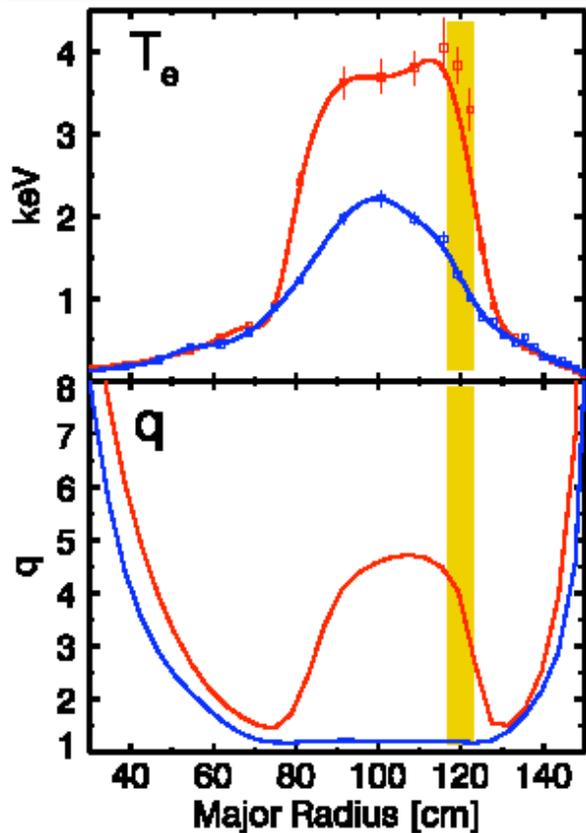
SciDAC Center for the Study of Plasma Microturbulence

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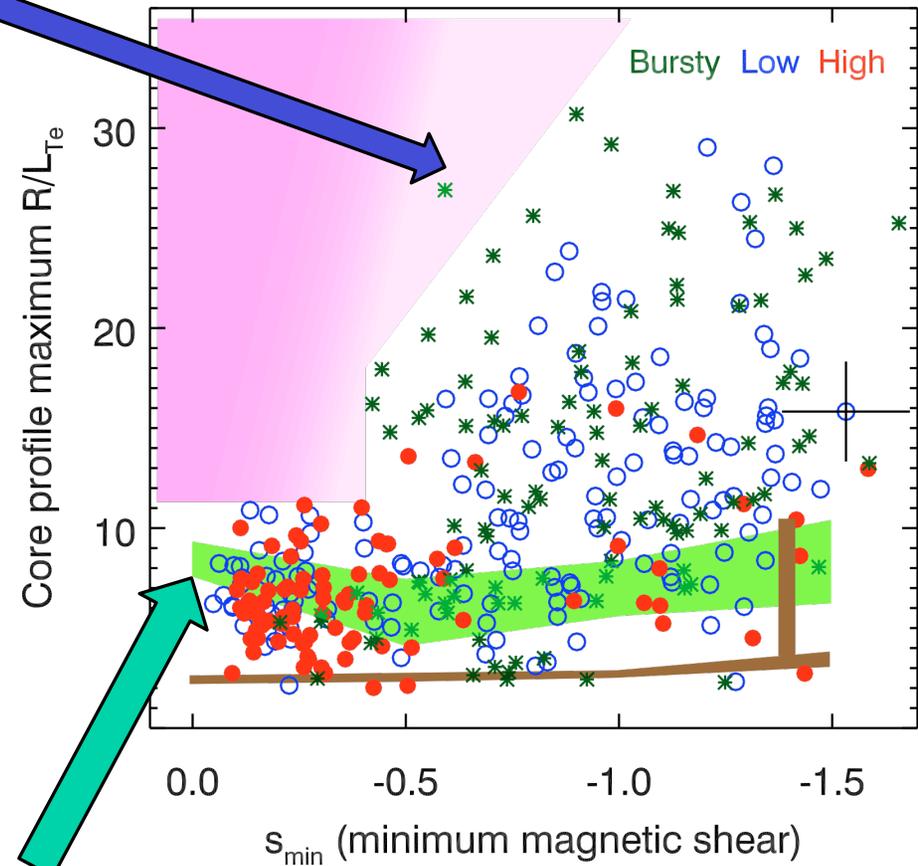
Princeton Plasma Physics Laboratory, Princeton University,  
DOE DE-AC02-09CH11466

# A Puzzle: Some NSTX plasmas violate profile stiffness.

Can heat some plasmas to very steep gradients.



Minimum  $s$  vs. maximum  $T_e$  Gradient



Should be unstable to electron temperature gradient (ETG) turbulence.

Yuh et al PoP (2009)

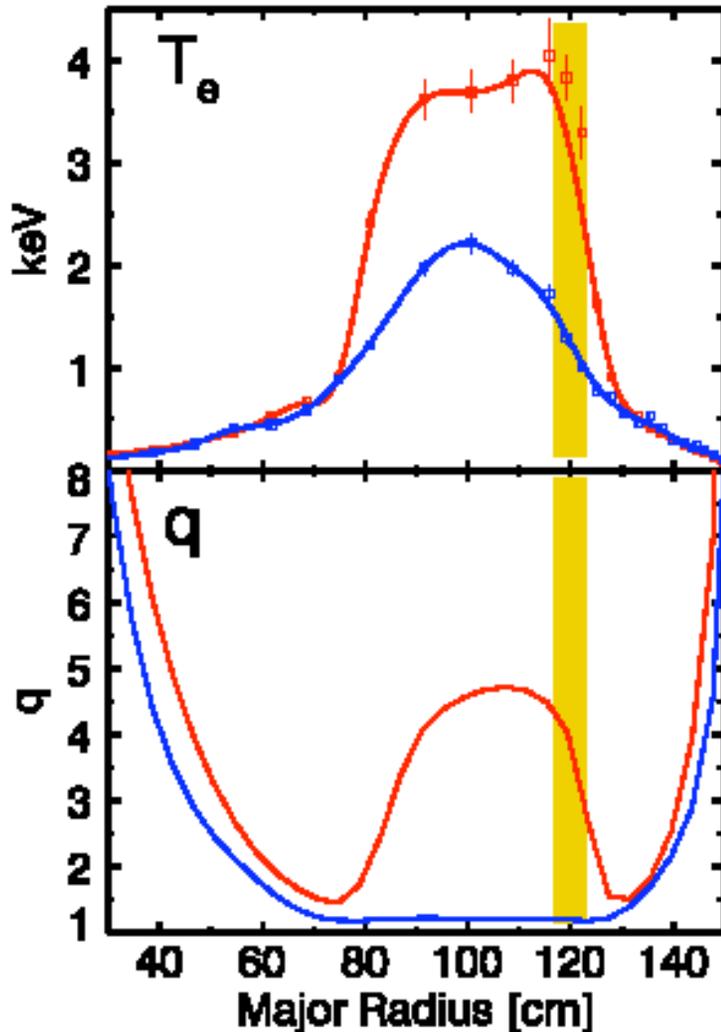
## Goal of work: Understand NSTX behavior

- Can trigger electron Internal Transport Barriers (e-ITB) that push past ETG stiffness threshold
- Coincides with lowering of electron-scale density fluctuations
- Electron transport seems to drop as well
- Shear in the magnetic field geometry seems to be important

**Can numerical simulations help shed light on the experimental observations?**

- What is the connection between electron turbulence and transport during these e-ITB phases?
- What role does magnetic shear play in the suppression of ETG turbulence and/or the formation of e-ITBs?

## Baseline NSTX Reversed Shear Discharge #129354 @ 232 ms



- e-ITB during strong reversed shear
- RF heat drives high electron temperature
- ETG unstable:  $(R/L_{T_e})_{crit} \approx 4.5$

### Physical Parameters

$$\begin{aligned}
 R/L_{n_e} &= 1.74 & \hat{s} &= -2.4 \\
 Z_{eff} &= 3.39 & q &= 2.4 \\
 \mu_e &= 60.0 & \nu_{ei} &= 0.16 (a/c_s)
 \end{aligned}$$

## Simulation Plan: Probe Nonlinear Critical Gradient

- GYRO\*
- Scan electron temperature gradient
- Nonlinear flux tube simulations
- Vary magnetic shear
- Electrostatic
- No background flow shear
- Electron-scale resolution
- ~100,000 CPU hours each at ORNL Cray XT
- ~3 million total CPU hours

*\* J. Candy and E.A. Belli, GYRO Technical Guide, General Atomics Report GA-A26818 (2010).*

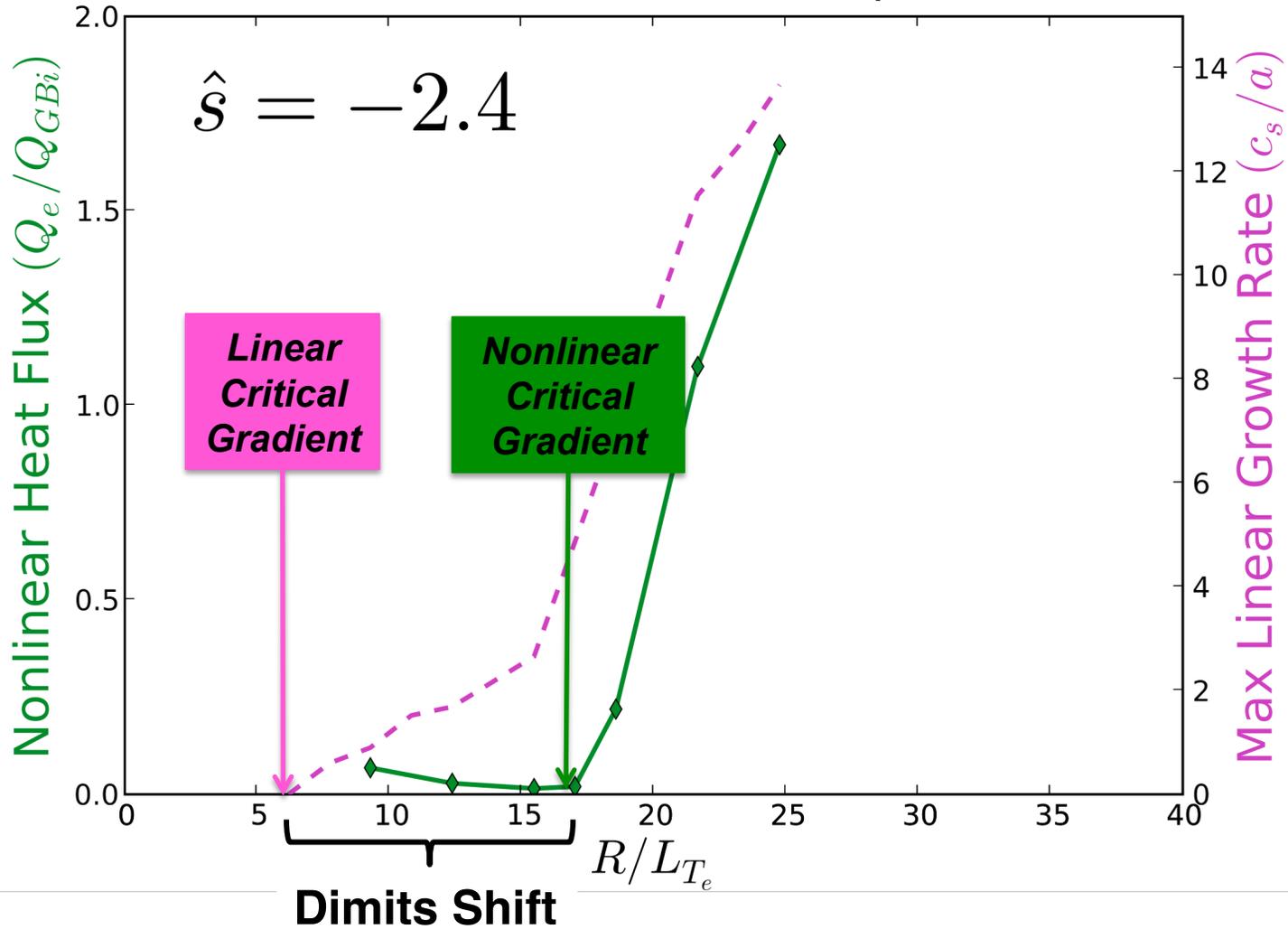
## Numeric Details

- All species gyrokinetic: electrons, deuterium
- 22 points per passing particle orbit
- 12 energy, 24 pitch angle grid points
- 24 toroidal modes
- Electron gyro-radius radial grid resolution

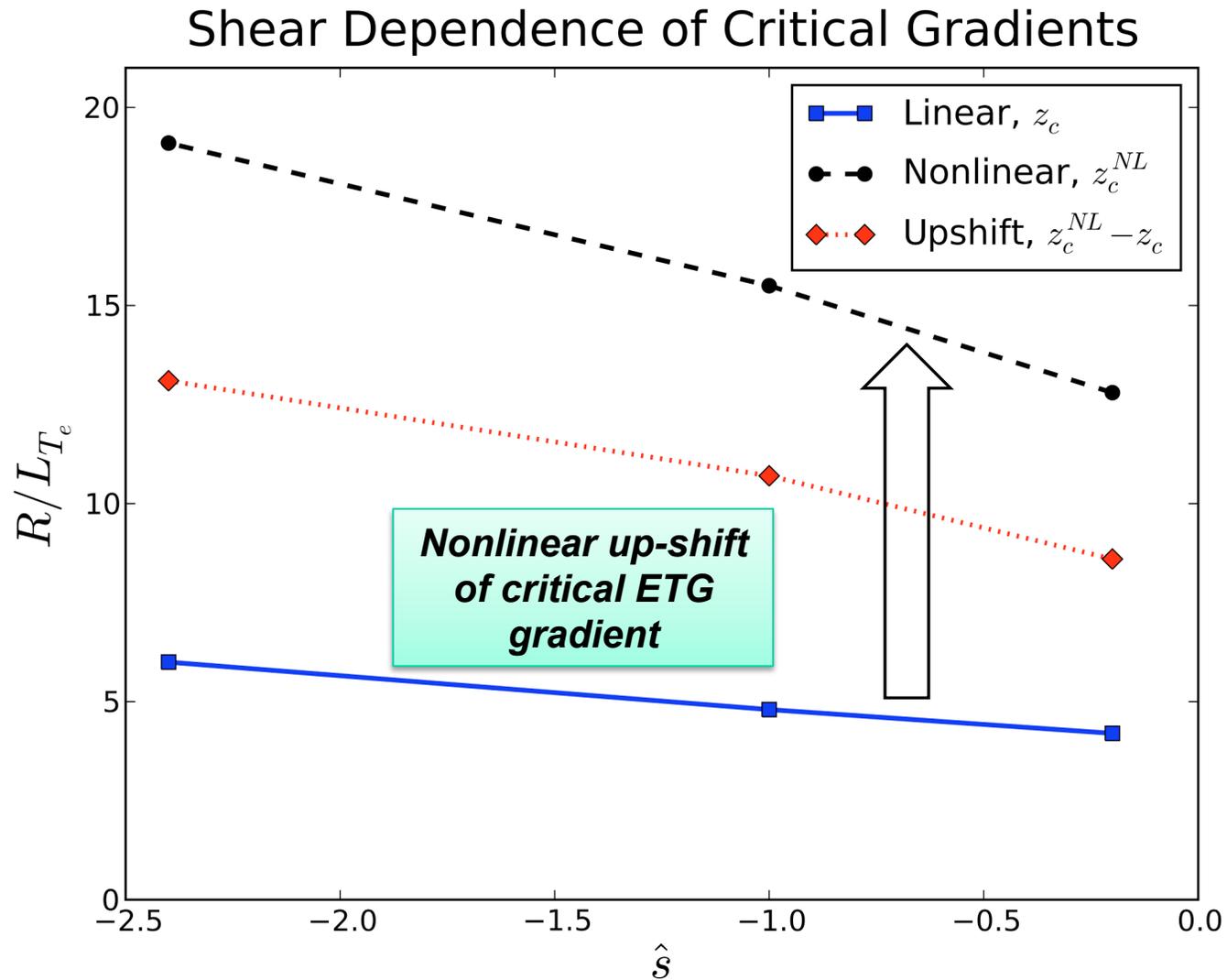
$$\begin{aligned} L_x \times L_y &= 4.26 \times 2.4 \rho_s & k_\theta \rho_s &= [2.618, 60.21] \\ &= 255 \times 144 \rho_e & k_\theta \rho_e &= [0.043, 1.004] \end{aligned}$$

# The Dimits Shift is very large for baseline negative shear.

Electron Heat Flux vs. Electron Temperature Gradient

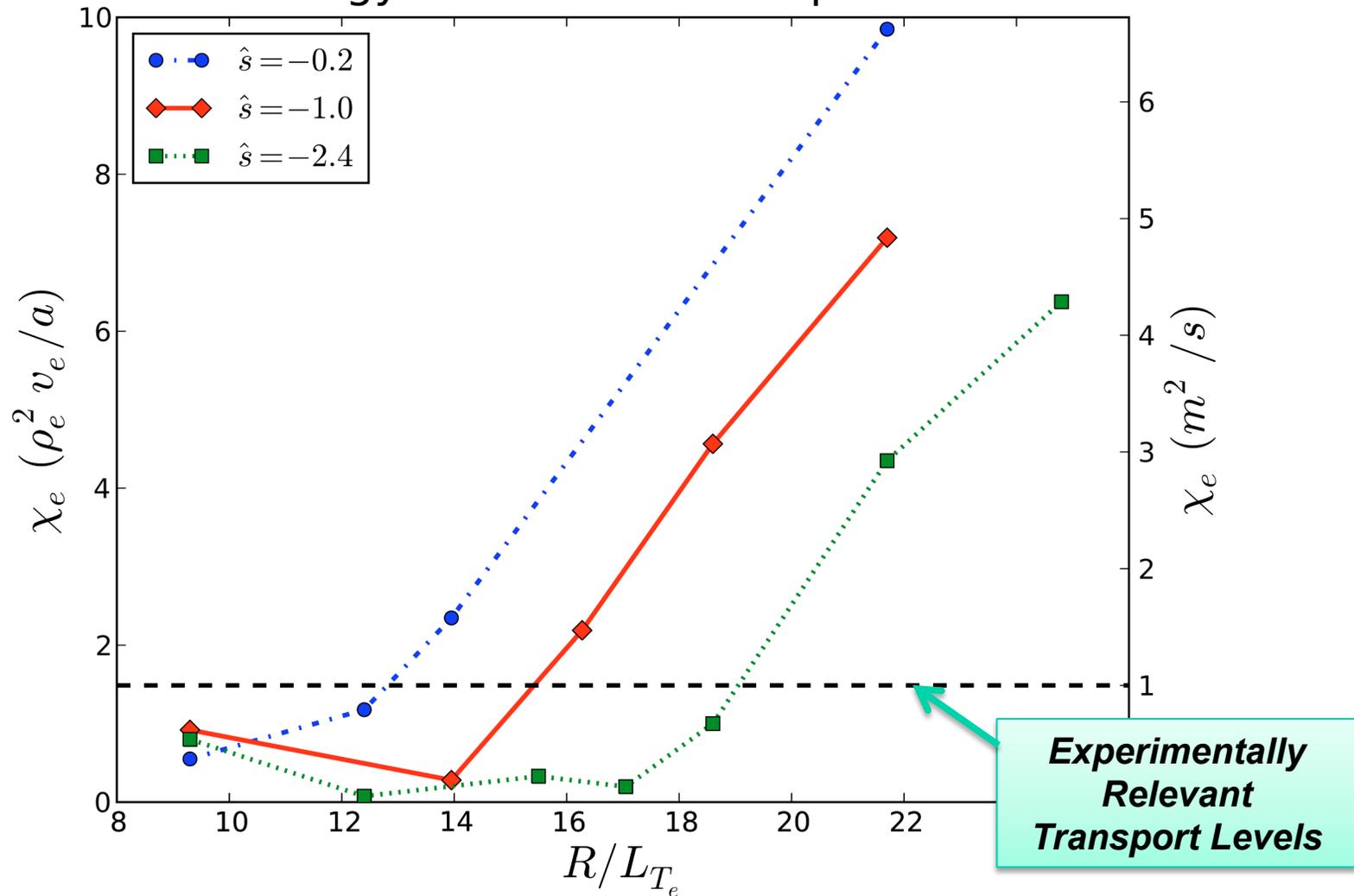


# The up-shift strength depends upon magnetic shear.



# Stiff Profile Threshold Increases With Reversed Shear

## Electron Energy Diffusion vs. Temperature Gradient



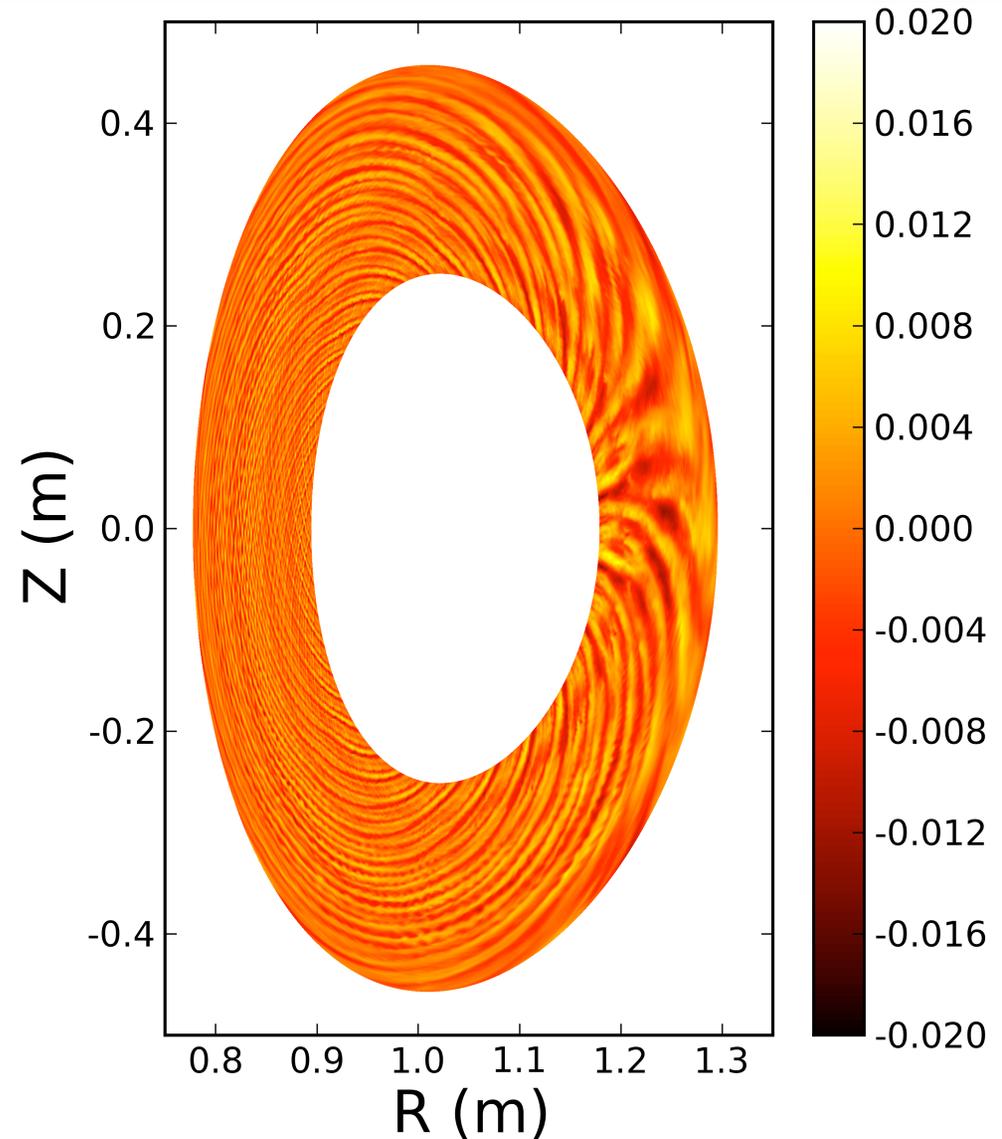
## Below Nonlinear Critical Gradient Threshold: Streamers Sheared Apart, Low Transport

$$R/L_{T_e} \approx 9$$

$$\langle \tilde{n}_e \rangle_{rms} \approx 0.3\%$$

***Eddies Sheared,  
Saturate at Low  
Amplitude***

***Linearly Unstable,  
But Low Levels of  
Transport***



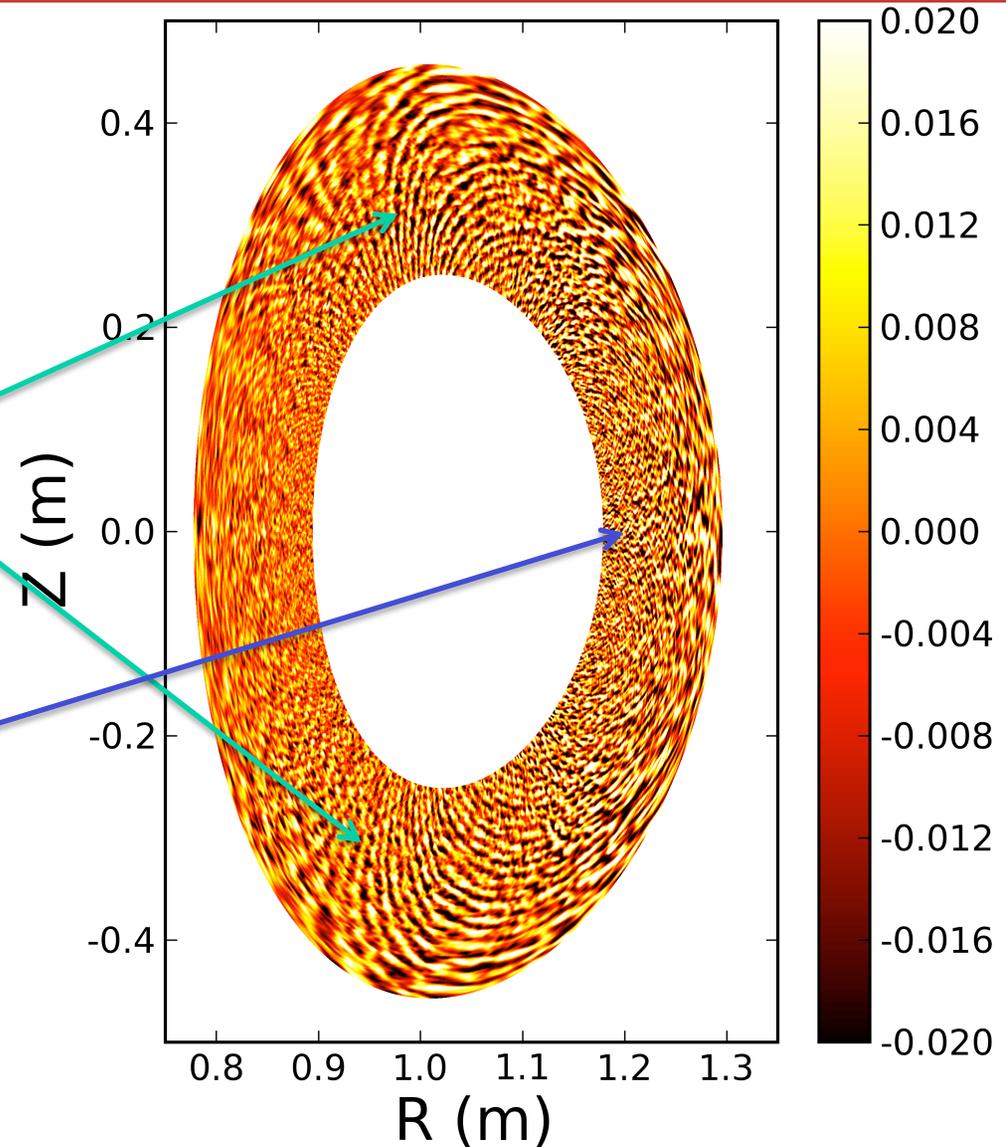
## Above Nonlinear Critical Gradient Threshold: Streamers Not on Midplane, Large Transport

$$R/L_{T_e} \approx 22$$

$$\langle \tilde{n}_e \rangle_{rms} \approx 1.1\%$$

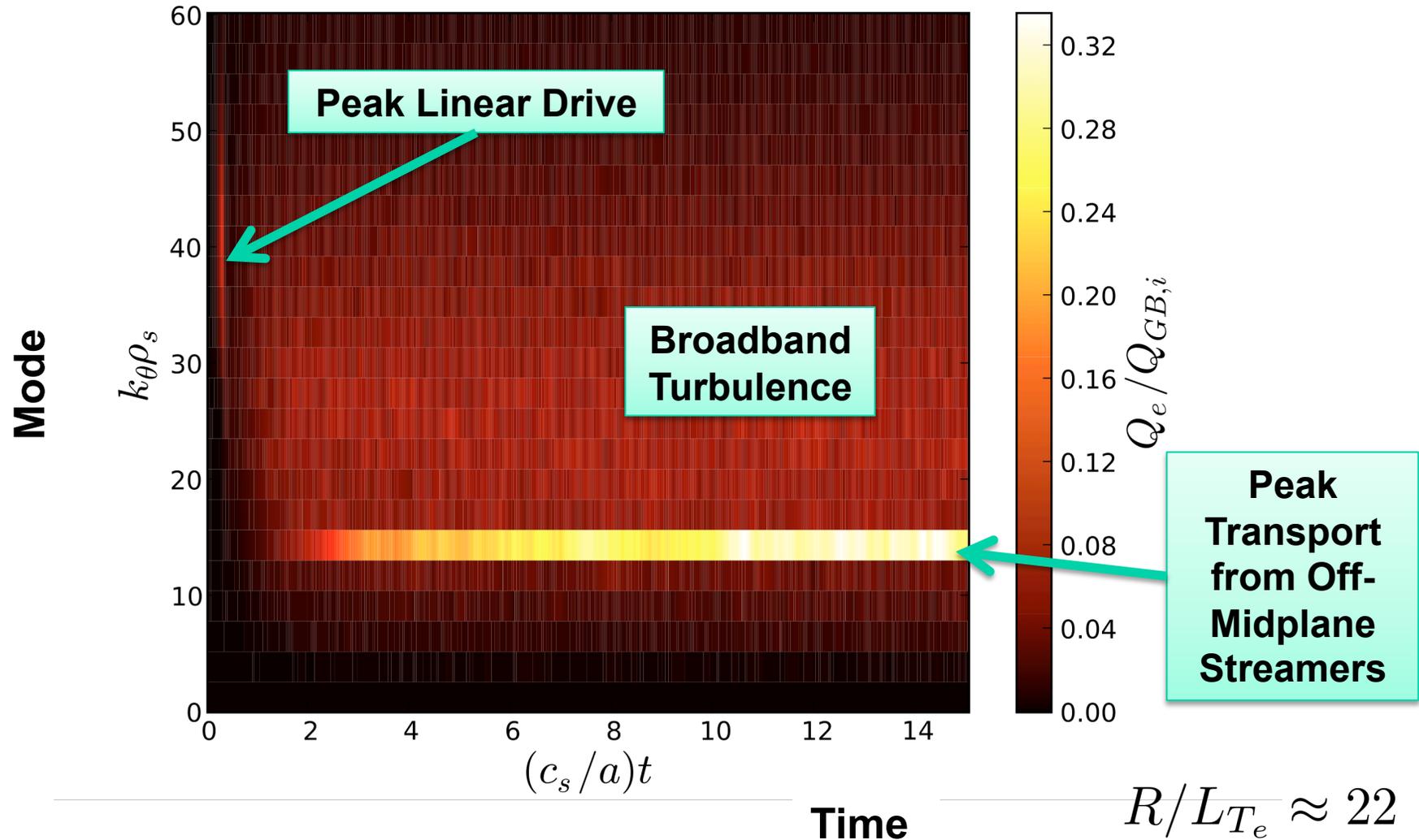
**Radial Streamers  
out of Top and  
Bottom**

**Broadband  
Turbulence**

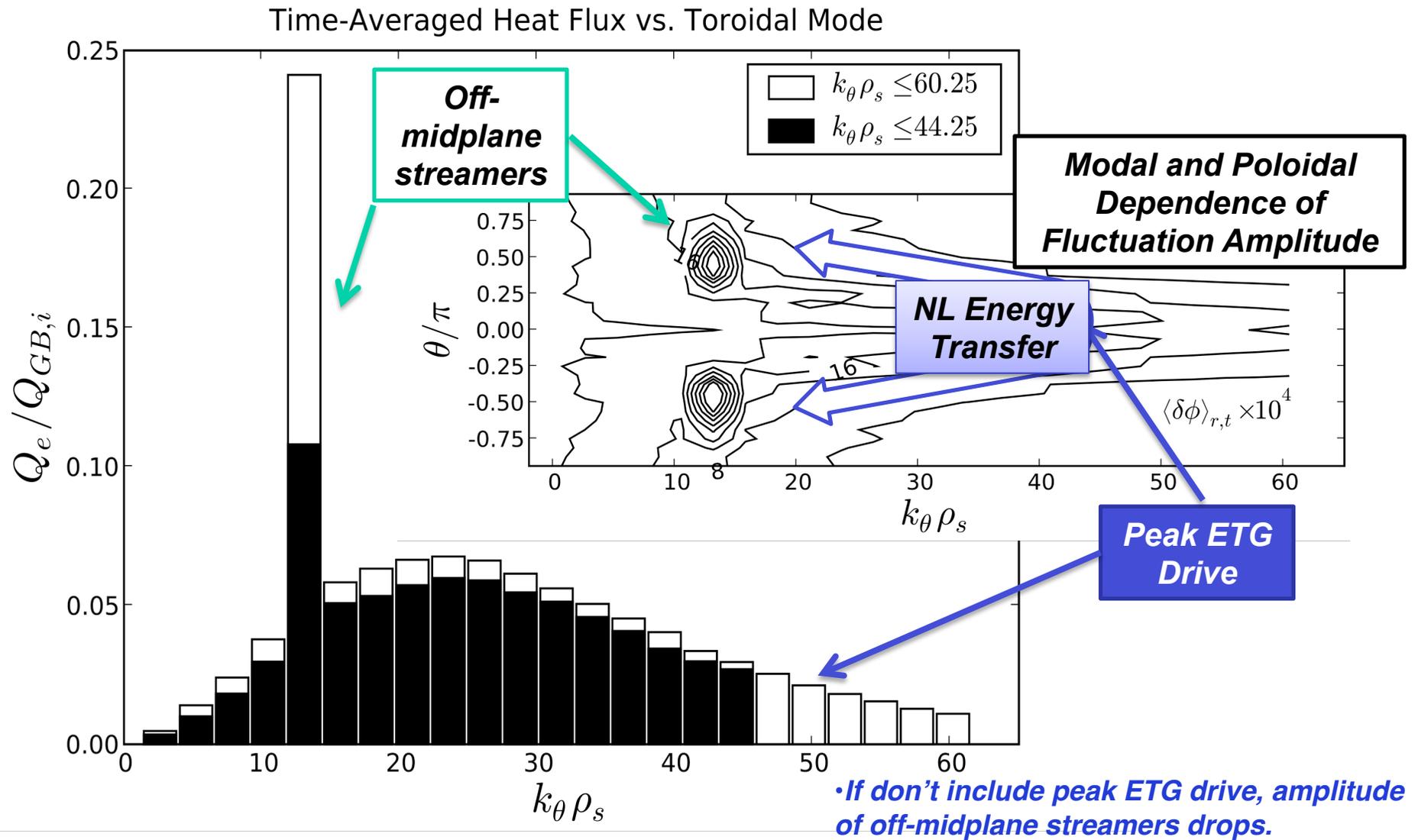


# Above nonlinear critical gradient, broadband turbulence and linearly subdominant peak of transport.

Time Evolution of Heat Flux per Toroidal Mode



# Evidence of Energy Transfer to Off-Midplane Streamers



## Some Testable (?) Speculations

- Performance of e-ITBs is limited by nonlinear critical gradient for transport.
  - Map out critical gradient as function of shear, compare with xp data
  - New validation experiment on NSTX
- Reversed shear discharges can still have significant ETG turbulence off the midplane.
  - Move high-k, look for difference / stronger fluctuations away from midplane
- Transport relies on interplay between very high-k and high-k.
  - Energy transport diagnostics in simulation
  - Map out linear stability properties of both modes, compare w/ nonlin.
- “Bursty” turbulence is characteristic of turbulence near nonlinear critical gradient.
  - Synthetic diagnostics

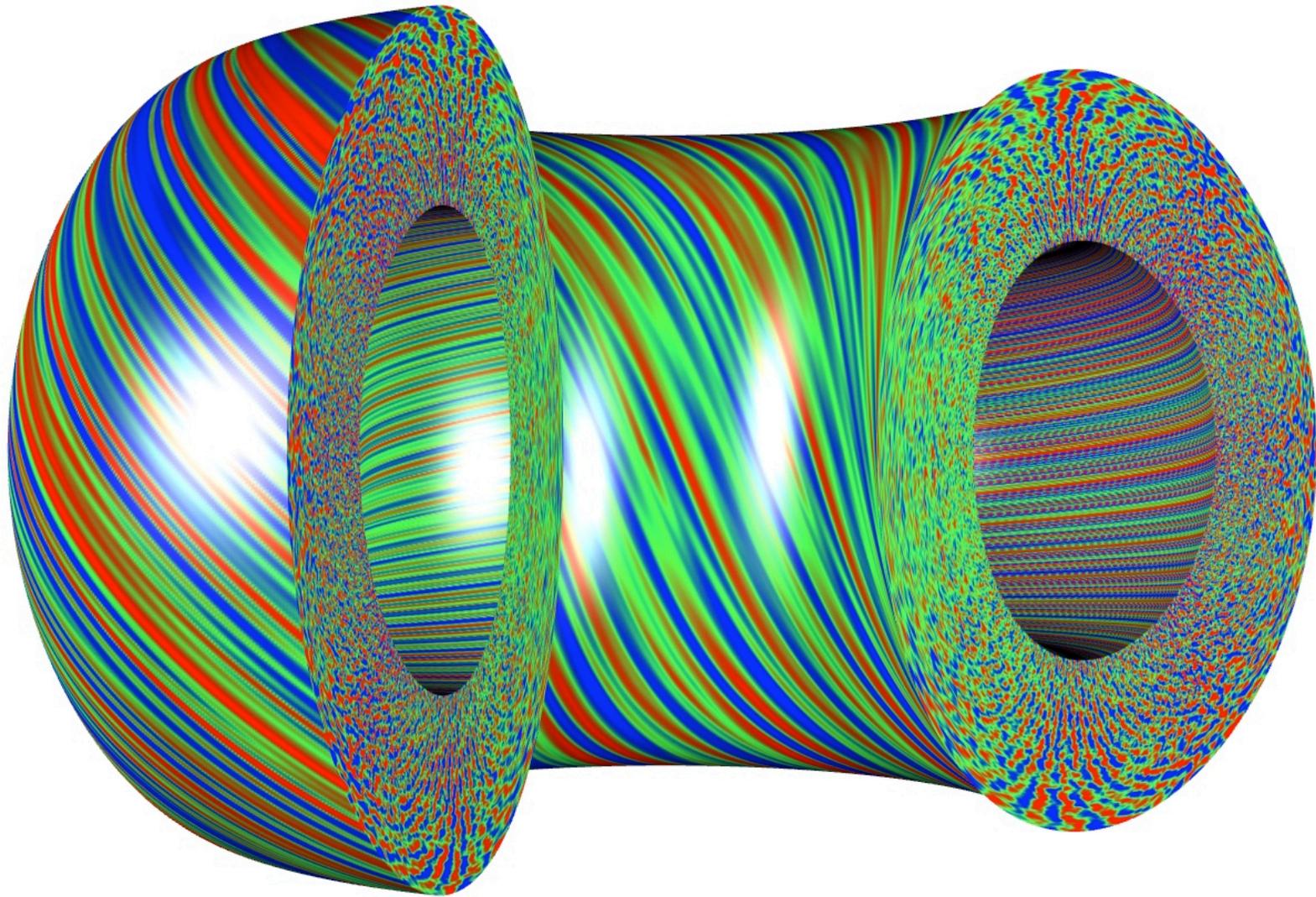
## Future Work

- Thorough analysis of high-transport case
  - Goal: investigate nonlinear gradient threshold, top/bottom streamers
- Apply mag. shear to gyrokinetic secondary instability theory
  - Goal: investigate how strength of ETG damping changes with shear
  - Goal: investigate GK vs. adiabatic ions
- Calculate synthetic high-k spectra based on these GK simulations
  - Goal: comparison with high-k experimental data
  - Goal: investigate “bursty” high-k signals in this regime
- Multi-scale nonlinear simulations
  - Goal: link ion and electron scales, especially if this top/bottom mode is important.
- Numerical convergence studies

## Conclusions

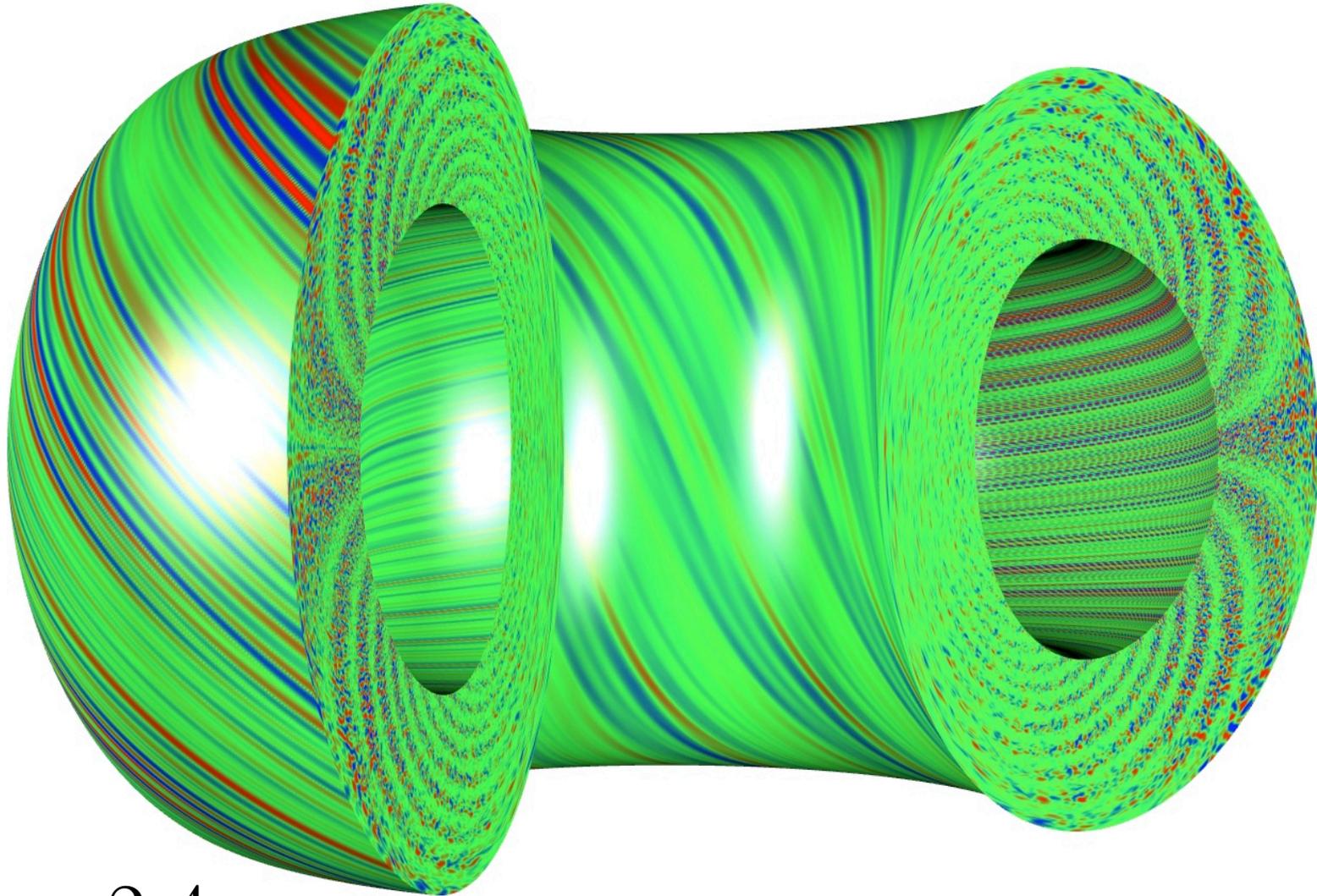
- Reversed shear temperature gradient scans find a second-instability threshold for electron transport.
  - $\sim 3x$  the linear critical gradient
- Nonlinear critical gradient is consistent with observations of maximum attainable gradients in NSTX reversed shear discharges.
- Above threshold, a slow-growing mode saturates with highest amplitude, causes large amount of transport.
  - Nonlinearly driven by peak ETG drive
  - **Streamers out of top and bottom:** midplane streamers sheared

Thank You



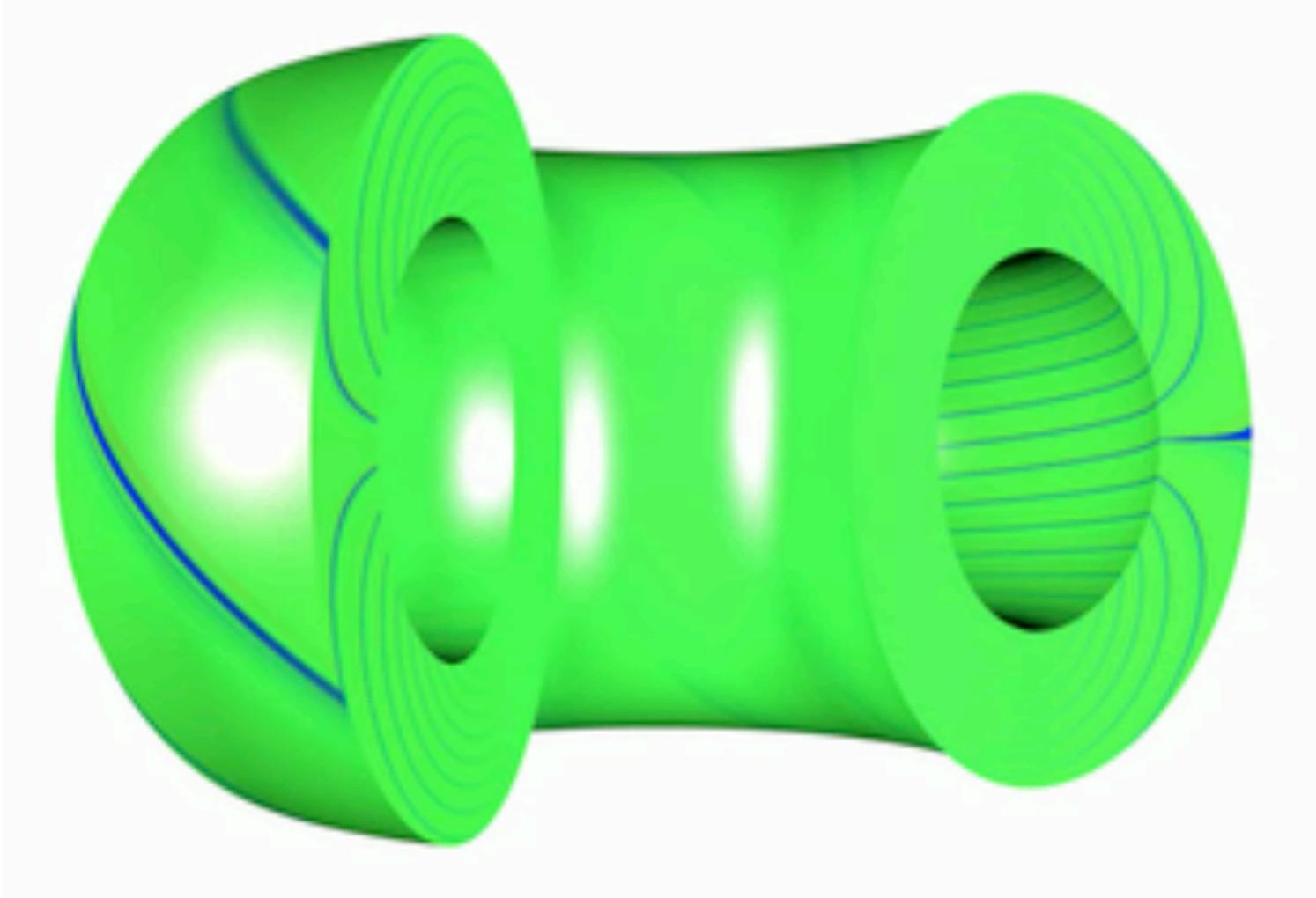
# Extra Slides

## Early Stage of Reversed Shear

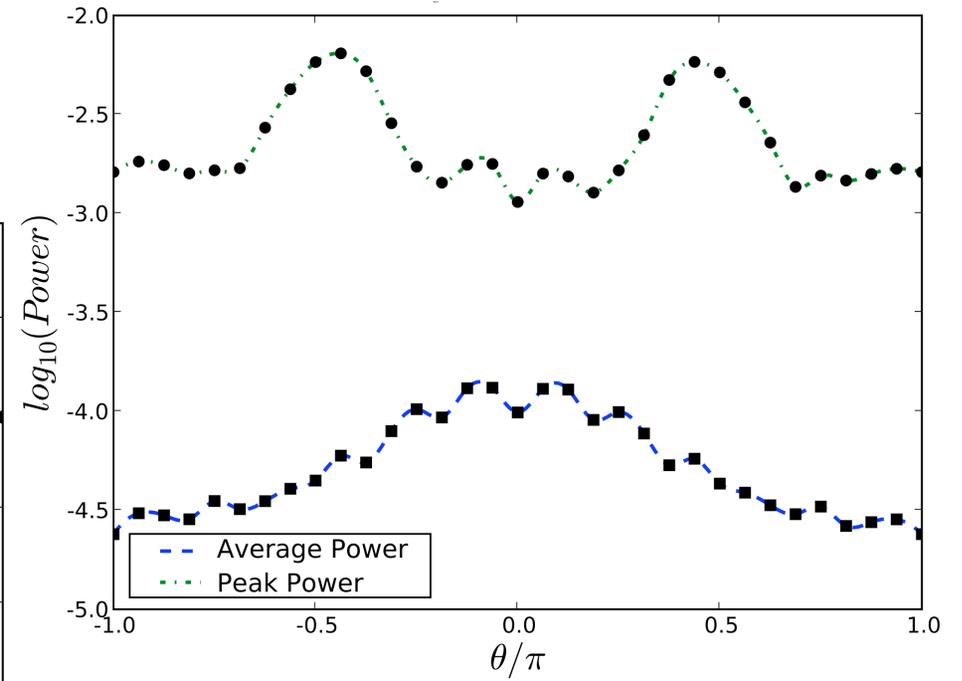
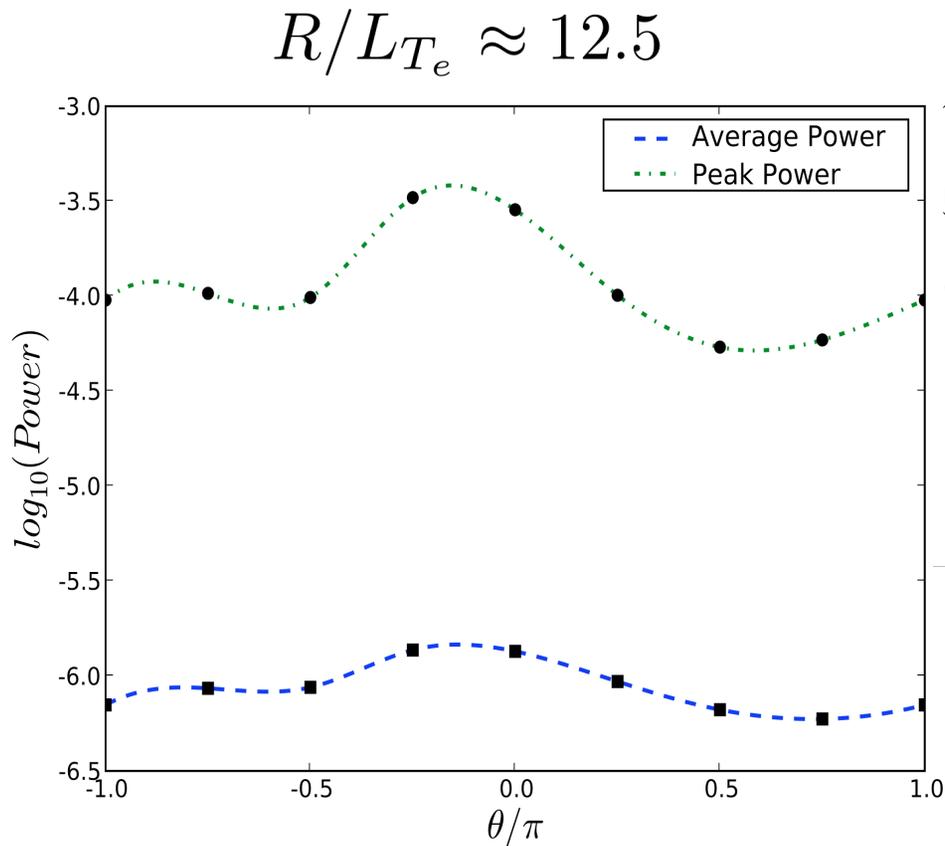


$$\hat{s} = -2.4$$

# Density Fluctuation Evolution



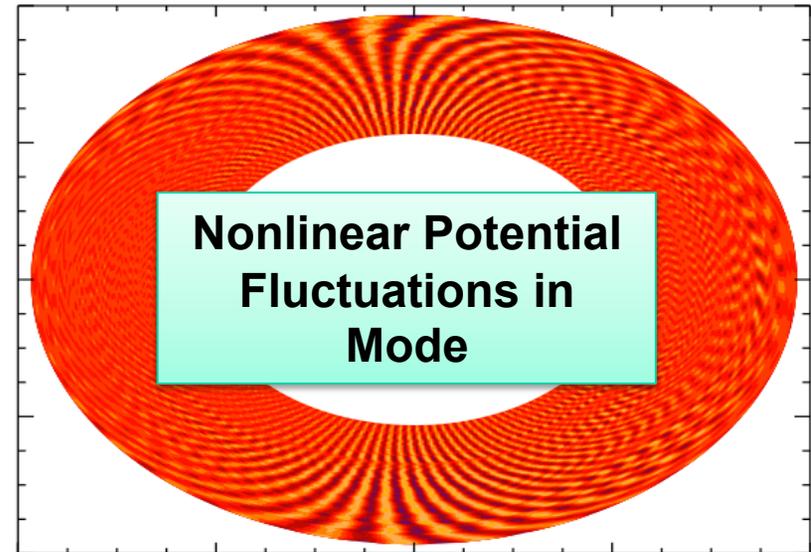
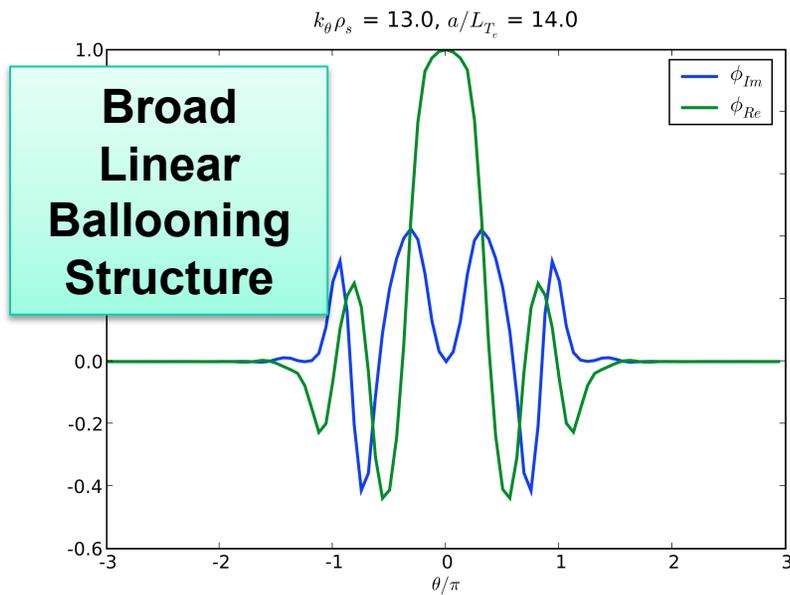
# Poloidal Dependence of Power Spectra Amplitudes



$R/L_{T_e} \approx 22$

$\hat{s} = -2.4$

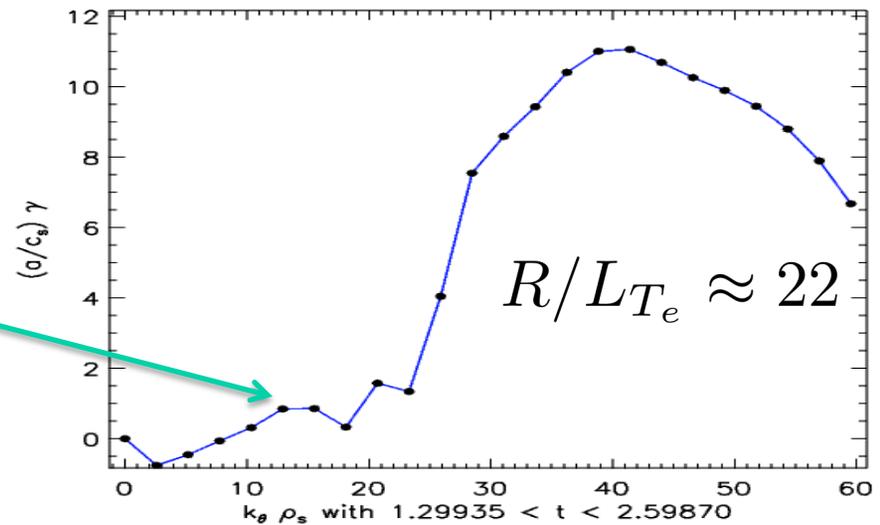
# Mode @ Transport Peak Found With Both Linear Initial Value and Field Eigenmode Solvers



**Sub-dominant Linear Growth Rate, Nonlinearly Saturates at Highest Amplitude**

$$\omega = 25.19 a/c_s$$

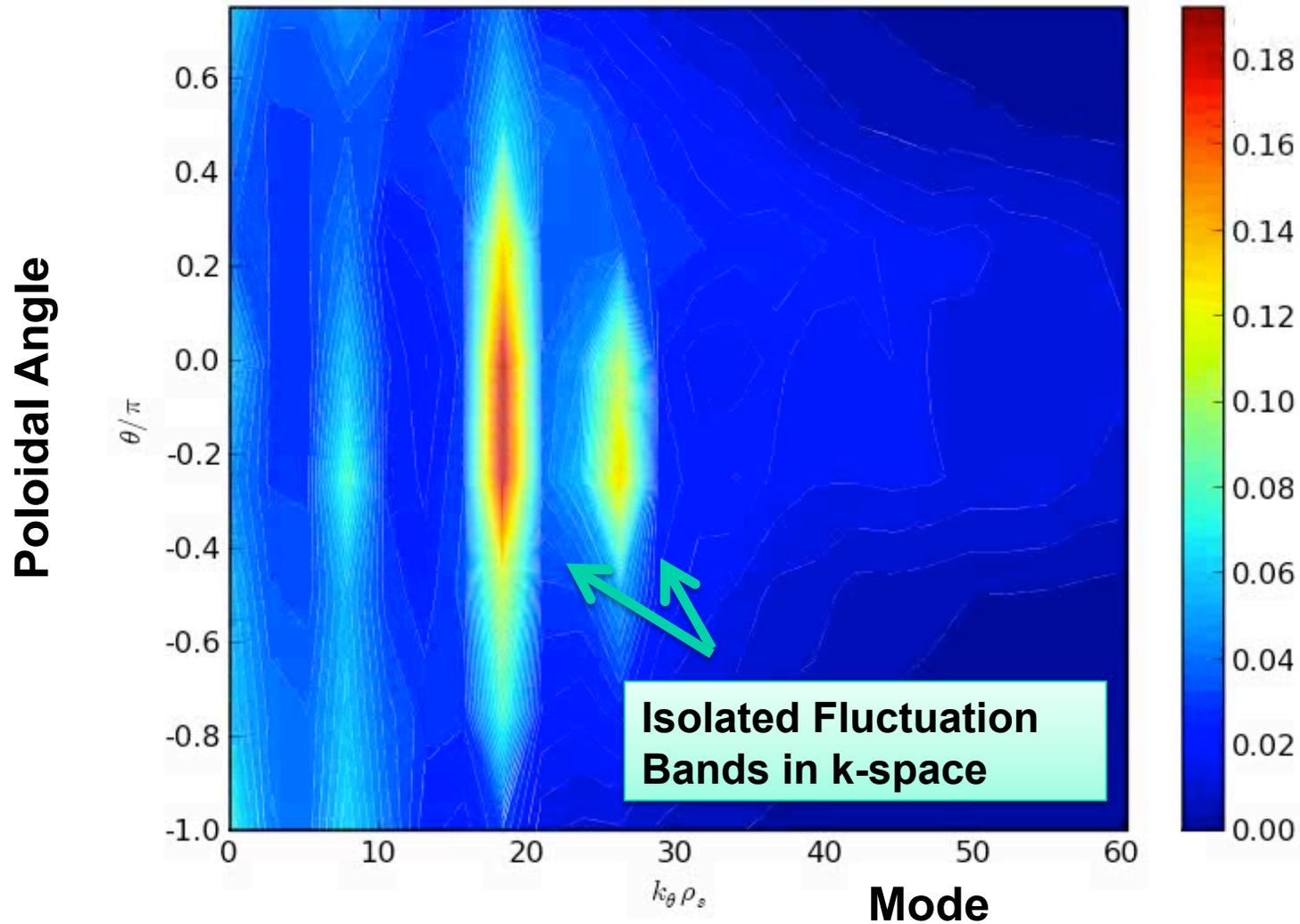
$$\gamma = 0.838 a/c_s$$



# Low-transport modes centered on Midplane

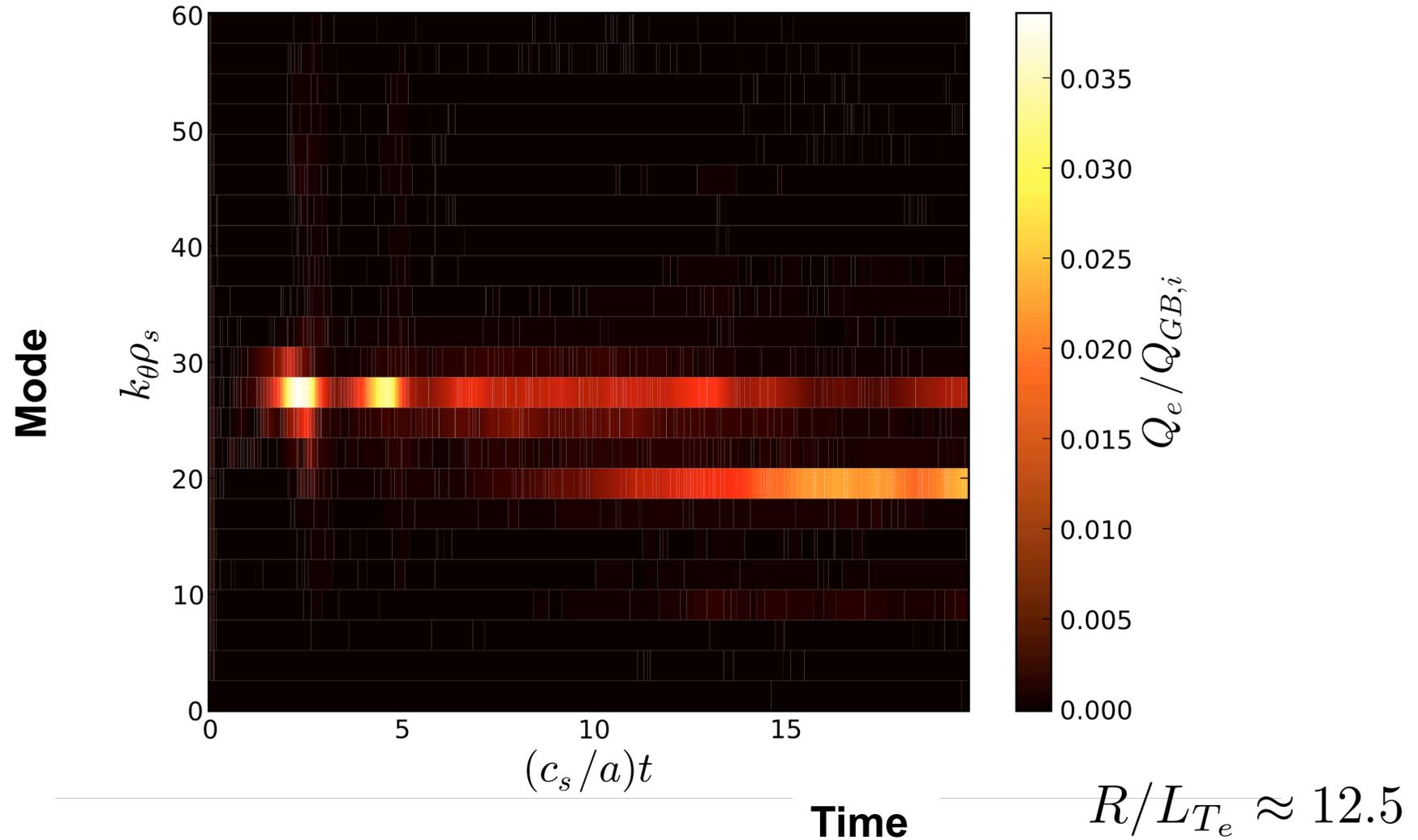
$\phi_{rms}(\theta, k_{\theta} \rho_s)$   $t = 15.015$   
High Res, GK Ions,  $a/LTe = 8$

$R/LTe \approx 12.5$

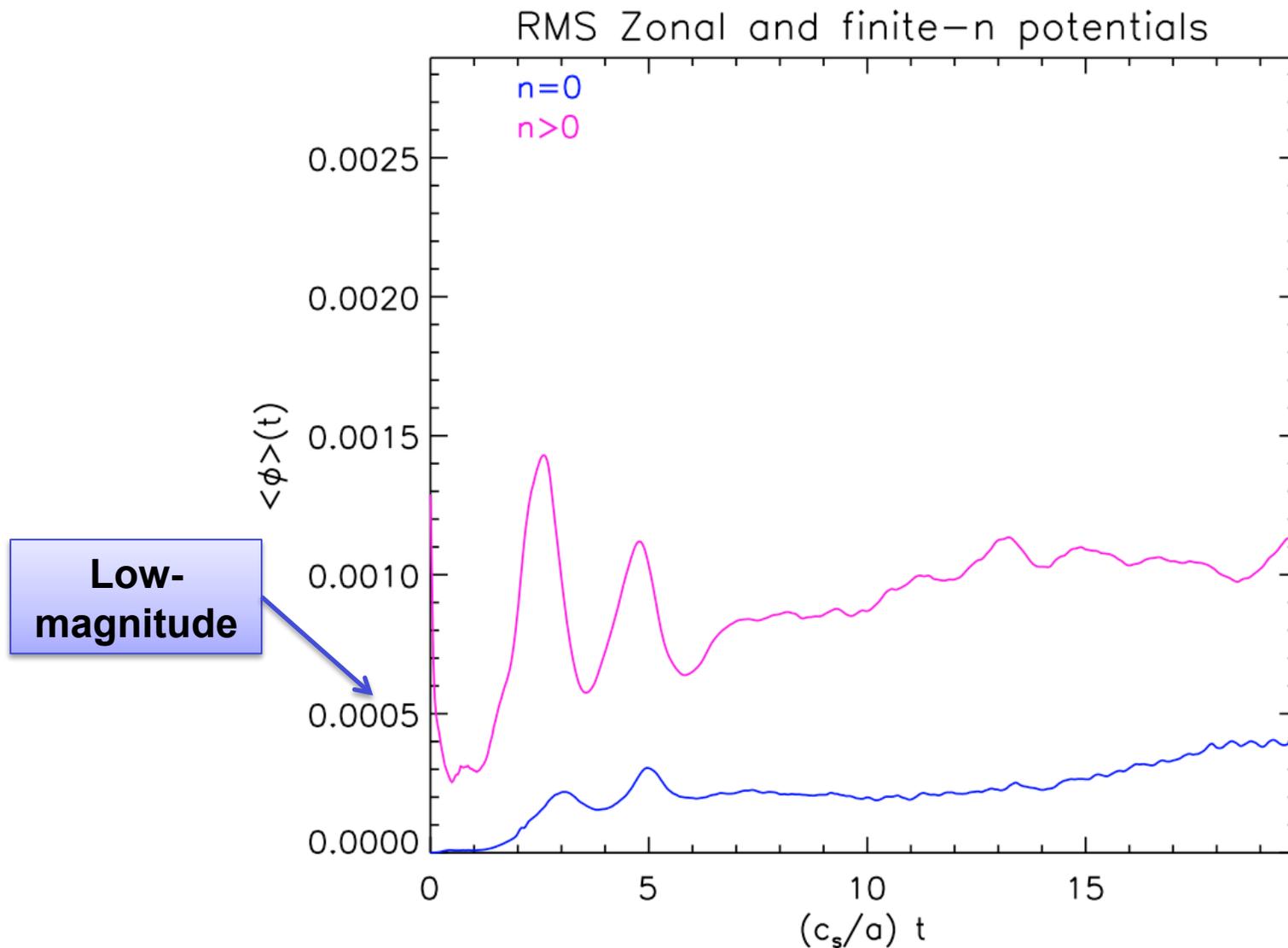


Below nonlinear critical gradient, no broadband turbulence.

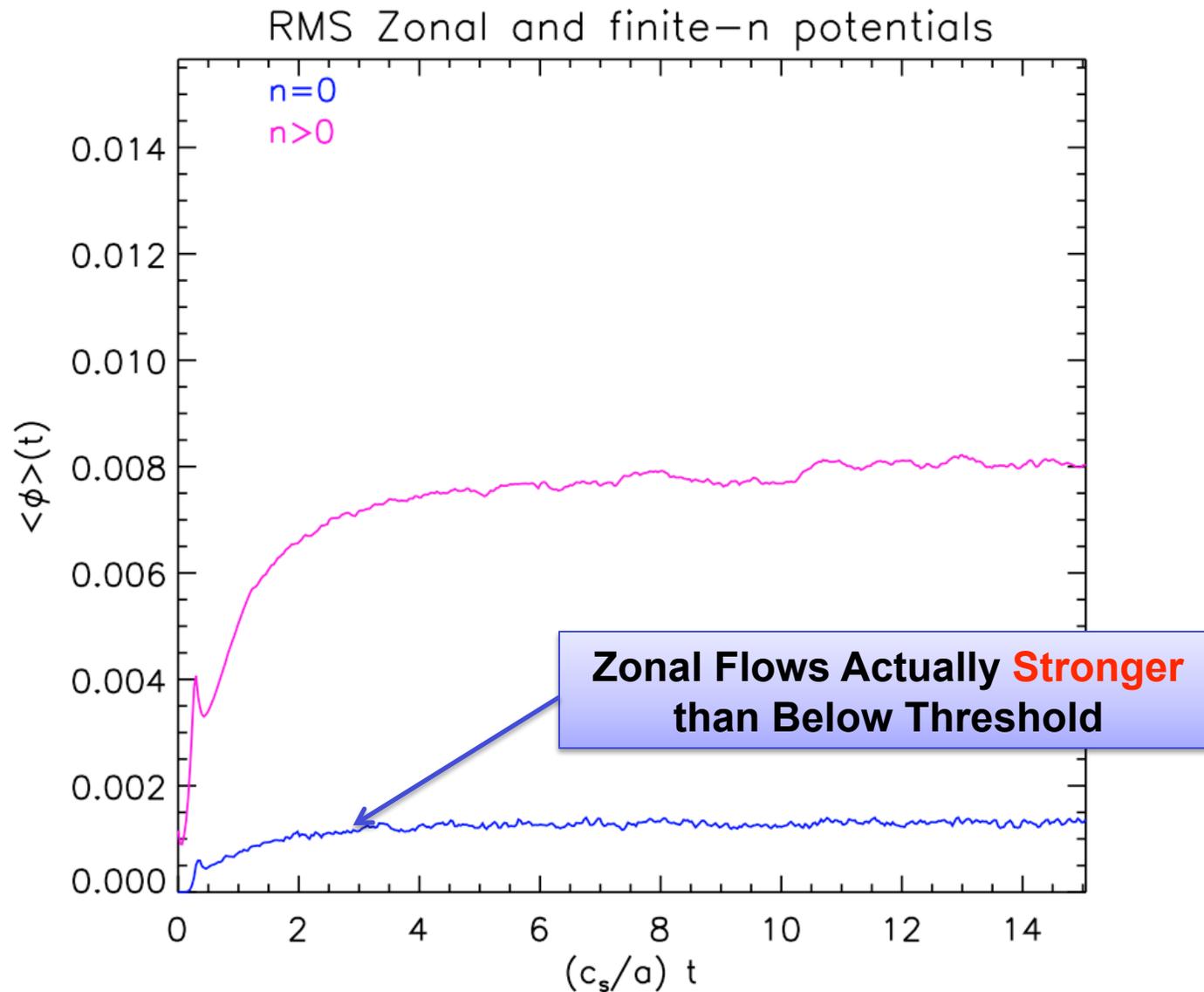
Time Evolution of Heat Flux per Toroidal Mode



# Zonal Flows Appear Correlated with Finite-n Potential Fluctuations Below Critical Gradient



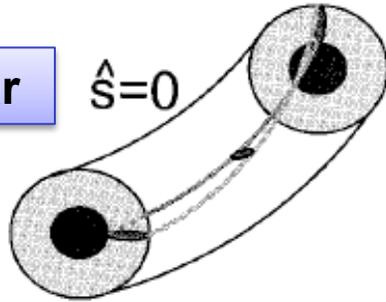
# Above Nonlinear Critical Gradient, Quicker Saturation



# The magnetic field shear can regulate turbulence.

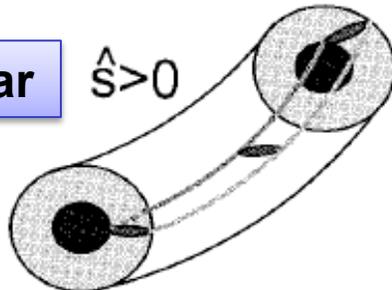
Zero Shear

$$\hat{s} = 0$$



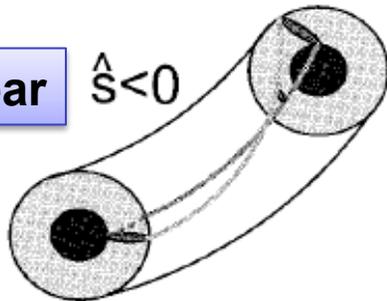
Positive Shear

$$\hat{s} > 0$$



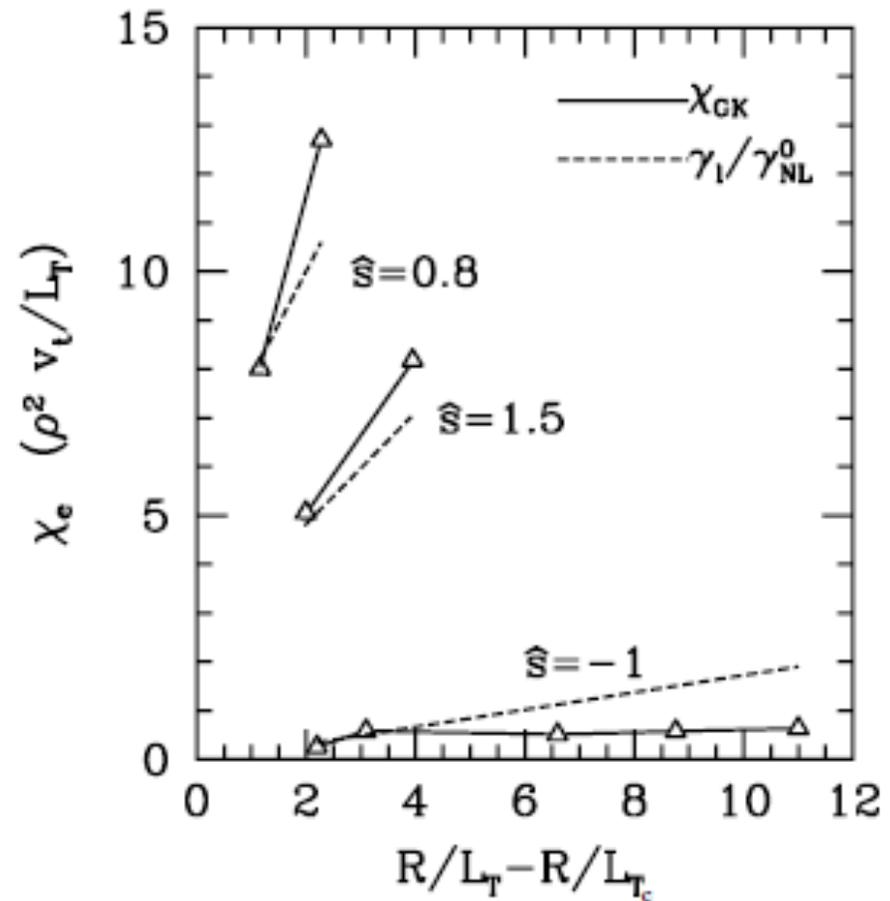
Negative Shear

$$\hat{s} < 0$$



Antonsen et al Phys. Plasmas (1996)

ETG Heat Diffusivity vs. Driving Gradient



Jenko and Dorland PRL (2002)